System of Traction AC Power Supply with Catenary Supports Not Connected with a Railway Track

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Abstract—A system of traction ac power supply is suggested. It is revealed that grounding the supports of group grounding cables is the most promising way of providing reliable operation of existing types of distance protective systems. The probabilistic characteristics of the voltages at the catenary supports are determined taking into account the random character of parameters determining the voltage levels at the supports upon short circuits in the traction network. The mathematical expectation of the number of dangerous situations over a 100-km piece of line is calculated when using a railway track to ground supports and when using the proposed system of grounding catenary supports. It is revealed that the number of dangerous situations when grounding of the catenary supports is not done does not exceed the corresponding value over electrified piece of lines where a railway track is used to ground the supports. It was established that, when the value of resistance of the group-grounding-cable—support system is less than 7.5 Ω , the operation of traction power supply during thunderstorms is no worse than with a traction network when a railway track is used to support grounding.

Keywords: traction power supply system, catenary support, grounding conductor, short circuit
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appreciable increase in the reliability of auto-
 $\frac{d\mathbf{r}}{dt} = \dot{E}_A - \dot{I}_{IA} Z_{CA}$, $\dot{U$ **DOI:** 10.3103/S1068371219060063

An appreciable increase in the reliability of automatic locking devices, including railway track circuits and signaling, centralization, and blocking devices, during a thunderstorm is possible due to a decrease in the number of lightning strokes of a railway track. This can be achieved by abstaining from grounding ac catenary supports. However, the operation of current and distance protective systems of traction power supply systems is made more complicated in this case.

Grounding catenary supports of a group grounding cable is a quite promising means of providing the reliable operation of existing types of distance protective systems, for what the cable with the length no more than 600 m by grounding wires is connected in two places with artificial grounding conductors. The spreading resistance of each grounding conductor does not exceed 15 $Ω$.

The design diagram to define the complex values of impedances of zones that are protected by distance mipedances of zones that are protected by distance
protective systems in the piece of lines with supports disconnected from the railway track is shown in Fig. 1. ں .
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In accordance with the mesh-current method, we have

$$
\dot{I}_{A} = \frac{\dot{U}_{1}Z_{t,nII} - U_{II}Z_{III}}{Z_{t,n}Z_{t,nII} - Z_{III}^{2}}, \ \dot{I}_{B} = \frac{\dot{U}_{II}Z_{t,nI} - U_{I}Z_{III}}{Z_{t,nI}Z_{t,nII} - Z_{III}^{2}},
$$

grounding conductor, short circuit
\nAt
$$
U_I = \dot{E}_A - \dot{I}_{IA} Z_{CA}
$$
, $\dot{U}_{II}^{\text{TM}} = \dot{E}_B - \dot{I}_{IB} Z_{CB}$,
\n
$$
Z_{\text{t,nI}} = Z_{\text{e,II}} - \frac{Z_{12}^2}{Z_2} I_1 + \frac{Z_{12} (Z_{12} - Z_2)}{Z_2 \gamma} (1 - e^{-\gamma I_1}) + \frac{1}{2} Z_B + R_B + Z_{\text{e,III}},
$$
\n
$$
Z_{\text{t,nII}} = Z_{\text{e,III}} - \frac{Z_{12}^2}{Z_2} I_2 + \frac{Z_{12} (Z_{12} - Z_2)}{Z_2 \gamma} (1 - e^{-\gamma I_2}) + \frac{1}{2} Z_B + R_B + Z_{\text{e,III}},
$$
\n
$$
Z_{\text{t,nIII}} = \frac{Z_{12} (Z_{12} - Z_2)}{Z_2 \gamma} (1 - e^{-\gamma I_1}) (1 - e^{-\gamma I_2}) + \frac{Z_{12}}{Z \gamma} (1 - e^{-\gamma (I_1 + I_2)}) + \frac{1}{2} Z_B e^{-\gamma (I_1 + I_2)} + R_B + Z_{\text{e,III}}.
$$

The equivalent electrical parameters of the contact network, for example, in the node power-supply circuit, are

$$
Z_{e, \text{if}} = 0.5(Z_1 + Z_a)l_1 + Z_{t, \text{sA}},
$$

\n
$$
Z_{e, \text{if}} = 0.5(Z_1 + Z_a)l_2 + Z_{t, \text{sB}},
$$

\n
$$
Z_{e, \text{ifII}} = (Z_1 + Z_a) \frac{l_{t, \text{s}} + l_1}{2l_{t, \text{s}}}
$$

Fig. 1. (1) Estimated circuit of the traction network at part of a line with catenary supports disconnected from railway track: traction substations A and B, (*2*) contact network of even and odd railway tracks, (*3*) switches of section switch box, (*4*) switches of traction substations, (*5*) insulators of catenary supports, (*6*) catenary supports, (*7*) group grounding cable, (*8*) spreading resistance of artificial grounding conductor, and (*9*) railway track; *sc*1 and *sc*2 are the locations of short circuits of the contact network to the GGC; Z_{cia} and Z_{cib} are the complex impedances of external power supply system and traction substations A and B reduced to a **Fig. 1.** (*I*) Estimated circuit of the traction network at part of a line with catenary supports disconnected from railway track: traction substations A and B, (*2*) contact network of even and odd railway tracks, (*3*) consideration and neighboring zones; and I_A and I_B are the currents in the supply lines of traction substations A and B. ork of every support
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where Z_1 is the impedance of 1 km of the contact network–ground circuit, Z_a is the mutual inductive reactance of 1 km between the contact network–ground circuit of the first railway track and the contact network–ground circuit of the second railway track, Z_{12} is the mutual inductive reactance of 1 km between the contact network–ground circuit and the rails–ground circuit, Z_2 is the complex impedance of 1 km of the railway tracks—ground circuit; γ and Z_{w} are the propagation coefficient and the wave impedance of the railway track, R_{φ} is the spreading resistance of two in-parallel groundings, and $l_{1,2}$ is the distance from traction substations A and B to the point of insulation failure. way tracks—ground circuit; γ and Z_w are the proption coefficient and the wave impedance of the rail-
 I track, R_g is the spreading resistance of two in-parallel undings, and $I_{1,2}$ is the distance from traction

distribution in the contact networks of the first and of the second railway tracks is determined, for example, -when a node connects a circuit by the formulas (the short circuit is at point $K2$, Fig. 1) A
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e connects a circuit by the fo
\nis at point K2, Fig. 1)
\n
$$
\dot{I}_a = \dot{I}_A \dot{E} - \dot{I}_B (0.5 - E),
$$

\n $\dot{I}_b = \dot{I}_A (1 - E) + \dot{I}_B (0.5 - E),$
\n $\dot{I}_c = \dot{I}_A \dot{E} - \dot{I}_B (0.5 + E),$
\n $\dot{I}_d = \dot{I}_D = 0.5 \dot{I}_B,$

at $E = 0.5 l_1/l_{\text{ts}}$, where l_{ts} is the distance from traction substation A to the section switch box.

The design formulas for equivalent electrical parameters and when other connecting circuits of contact network are presented in [2].

It was established in [3] that, when voltage supply to the support is disconnected from the railway track, distance protective systems are reliably triggered, sending a signal to disconnect the faulted piece of line.

The data obtained above on the possibility of using the existing distance protective systems at the piece of lines with the supports disconnected from the railway track were confirmed with experiments carried out by the personnel of the Railroad Electrotechnical Laboratory of the North Caucasus Railway. It was noted that the spreading resistance of the support foundation has a nonlinear behavior and when supplying the voltage of 25 kV the spreading resistance of the support foundation decreases on average by 20% as compared with the data obtained by measurements with a highresistance ohmmeter. This is explained by increasing the designed length of the support foundation due to sparking in the ground.

CALCULATION OF VOLTAGES ON A SUPPORT DISCONNECTED FROM A RAILWAY TRACK UPON INSULATION FAILURE OF A CONTACT NETWORK

Catenary supports need to be disconnected from railway tracks is necessary to carry out, assuming that electrical safety conditions are met when working near the supports, which are largely determined by the possibility of reinforcing a concrete support and the structure of the metal support relative to the remote ground.

Table 1. Voltages on the support when grounding to the railway track is nor used (the numerator corresponds to impedance of the external power supply system $Z_s = j3.5$ Ω, and the denominator corresponds to impedance of the external power supply system $Z_S = j5.0$ Ω)

Charact eristic	Voltage, kV, at the support when grounding to the railway track is not used at the distance from the traction substance to the short circuit, km						
			4			10	
$M \ell q U_0$	1.55/1.3	2.90/2.8	1.57/1.5	2.40/2.3	1.5/1.4	1.9/1.8	1.2/1.2
$\sigma \ell q U_0$	0.3/0.2	0.45/0.4	0.3/0.29	0.40/0.38	0.25/0.24	0.32/0.3	0.2/0.2

The support potential relative to the remote ground in conditions of insulation failure is y_1 = $\frac{dy_1}{dx}$

= $\dot{q}_0 = \dot{I}$

$$
\dot{\phi}_{o} = \dot{I} R_{\text{sup}},\tag{1}
$$

where \dot{I} is the complex value of short-circuit current flowing through supports, the spreading resistance of foundation of which is R_{sup} .

When several supports are connected with a group grounding cable (GGC), which is connected with two artificial grounding conductors, by R_{sup} should be understood equivalent resistance $R_{e,i}$, which is defined by the relation

$$
\frac{1}{R_{\rm e,i}} = \sum_{i=1}^{n} \frac{1}{R_{\rm sup}} + \frac{1}{R_{\rm gl}} + \frac{1}{R_{\rm g2}},
$$

where *n* is the number of supports connected with the GGC into one piece of line; there are $n \approx 8-9$ supports; and $R_{\rm gl}$ and $R_{\rm gl}$ are the spreading resistances of artificial grounding conductors, which is 15 Ω.

The computation scheme of spreading resistance of the catenary support foundation is presented in detail in [2].

The results of analytical calculations suggest that it is advisable to connect a support reinforcement to a GGC. This will permit in some cases to do without building artificial grounding conductors that are connected to a GGC.

The voltages on the railway track and the GGC depend on a number of random parameters: the railsto-earth transition resistance, the spreading resistance of the support foundation, the distance from the traction substation to the short circuit, and the resistance of supply power system [1].

Based on the calculations by formula (1) and their statistical analysis, the characteristics of a log-normal law of voltage distribution at the supports connected with a GGC were determined: the mathematical expectation was $m\ell qU_0$, and the standard deviation was $\sigma \ell qU_0$. The characteristics are presented in Table 1.

In addition, it was established that the potential relative to ground of the supports connected with the group grounding cable when it grounding in two places to artificial grounding conductors, at insulation failure of the contact network is practically independent of the rails-ground transition resistance and at confidence probability $β = 0.95$ has confidence interval $U_0\beta$ = 0.95 = 10.5–18 kV.

PROBABILISTIC AND STATISTICAL ESTIMATION OF ELECTRICAL SAFETY CONDITIONS OF PERSONNEL PLACING NEARBY THE DISCONNECTED FROM RAILWAY TRACK CATENARY SUPPORTS

It was proposed in [2, 4] to determine the conditions of electrical safety to use the mathematical expectation of the number of dangerous situations caused by insulation failure at catenary supports:

$$
M(P) = P1N_{n.p},
$$

where *P*1 is the probability of one person experiencing an electrical shock and $N_{n,p}$ is the number of people near the catenary supports.

Then, one can write

$$
P1 \cdot s.c = 1 - (1 - P1)N_{s.c},
$$

where $N_{\rm s.c}$ is the number of short circuits in the traction network on the piece of line (L_d) for 1 year.

The probability of a person suffering an electric shock $(P1 \cdot s.c)$ when coming into contact with the support is equal to the product of the probabilities of a number of independent events: appearance of the short circuit mode in the contact network for the time of touching the person to the support; exceeding the voltages generating when short circuit by permissible values (P_u) ; coincidence of the times of electric current pulse effect and the most vulnerable phase of the cardiac cycle (P_t) . Thus, we have [4]

$$
M(P) = \frac{\eta A N_{s.c}}{T_0} P_u P_l,
$$

where *A* is the total time the person is near the catenary support, η is a coefficient taking into account the time during which the person on the ground is in direct contact with the support, and $T_0 = 8760$ is the number of hours in a year.

The obtained expression makes it possible to take into account the dependence of the probability of a person experiencing an electric shock on the distance from one section of supports connected with the group grounding cable to the short circuit.

The probability of a dangerous situation appearing for a person working near the support when there is a short circuit on the railway track at any point on a 100-km railroad is

$$
P_{ur} = \frac{1}{N_P^2} \frac{1}{L} \int_0^L d1 \frac{1}{N_{\sup}} \sum_{j=1}^{N_{\sup}} P\{\overline{U}_0(1_j, x_j) > \overline{U}(t)\},\tag{2}
$$

at $N_{\rm st} = 100/L$, where $N_{\rm st}$ is the average number of the stages between traction substations; *L* is the distance between adjacent traction substations, km; and $N_{\rm sun}$ is the average number of supports on the piece of line with length *L*.

Let us consider the case of a short circuit arising as a result of insulation failure on a catenary support. As the short circuit can arise with equal probability at any support and the person also can be placed with equal probability at any support, then from the formula of total probability we will obtain:

$$
P_{i0} = \frac{1}{N_{\text{st}}^2 N_{\text{sup}}^2} \sum_{j=1}^{N_{j\text{st}}} \sum_{j=1}^{N_{j\text{st}}} [P\{\overline{U}_0(l_i, x_j) > \overline{U}(t)\} \\ + P\{\overline{U}_{\text{sup}}(l_i, x_j) > \overline{U}(t)\} \\ + 2P\{\overline{U}_{\text{gr}}(l_i, x_j) > \overline{U}(t)\}],
$$

where $U_0(l_i; x_j)$, $U_{\text{sup}}(l_i; x_j)$, and $U_{\text{gr}}(l_i; x_j)$ are the voltages that are generated at the support and at the artifi c ial grounding conductor at distance x_j from the traction substation when the short circuit is at distance *li* from the traction substation.

The obtained expression differs from the analogous expression presented in [4] in the amount of the third term in square brackets.

Let us denote as $U_0(l; x)$ the voltage at the supports of a section located at distance *X* from traction substation, which is generated as a result of a short circuit to the railway track in the point at distance ℓ from the substation.

The probability of exceeding the permissible value of actuating voltage is

$$
P\{U_0(l, x) > U_g(t)\},\
$$

where $U_{o}(t)$ is the permissible voltage at the support depending on the time of activation of protection [2].

Let us determine this probability assuming that $U_{\alpha}(t)$ is a random variable distributed by log-normal law. It follows from the monotony of the logarithm that

$$
P\{U_0(l,x) > U_g(t)\} = F(lgU_0(l,x)).\tag{3}
$$

All short circuits in the catenary can separated by two groups: short circuits of the catenary directly at the supports combined in a line part, and short circuits of a catenary to the railway track outside the part.

Let us denote as P_0 the probability that the short circuit occurred due to insulation failure of the contact network located at the supports combined into sections. The value of P_{ins} is then found by the formula of total probability [5]:

$$
P_{\rm ins} = P_0 P_{\rm ins0} + (1 + P_0) P_{\rm i.r},
$$

where P_{i0} and $P_{i,r}$ are the probabilities of a person experiencing an electric shock upon insulation failure on the support of the section and the appearance of a short circuit on the railway track.

We will assume that the locations of the part of the line of supports connected with the GGC and of the short circuit have equal probabilities of being anywhere between the traction substations. Then *x* and ℓ are independent random variables distributed by a uniform law on the segment $[0; L]$, where *L* is the distance between traction substations. Therefore, the probability of a person experiencing an electrical shock upon a short circuit at the railway track at any point of the railway track piece of a line with length L_c is

$$
P_{\rm i.r} = \frac{1}{N_{\rm s.c}} \sum_{i=1}^{N_{\rm s.p}} \frac{1}{N_{\rm s.p}} \frac{dI}{L} P\{U_0(l, x) > U_g\},\tag{4}
$$

where $N_{\rm s.c} = L_{\rm c}/L$ is the average number of substation zones on calculated piece of line L_c (for example, when $L_c = 100 \text{ km}$, $N_{\text{is}} = L/\Delta$ is the average number of sections at the piece of line with length L) and Δ is the distance between pieces of line, i.e., the length of one piece of line equal to 600 m.

We will write formula (4) taking into account formula (3) in the form

$$
P_{\text{i.r}} = \frac{\Delta}{L_{\text{c}}L} \sum_{i=1}^{L/\Delta} \frac{1}{N_{\text{s.p}}} \int_{0}^{L} F[\log U_{0}(l, x)] dl.
$$

Let us consider the short circuit arising from insulation failure of the contact network directly in the section.

Since the short circuit can arise with the same probability in any section, then, by the formula of total probability, finally the expression for finding the probability of exceeding the permissible values of real voltages will be of the form

$$
P_{i} = P_{0} \frac{\Delta^{2}}{L_{c}L} \sum_{i=1}^{N_{is}} \sum_{j=1}^{N_{is}} F[\log U_{0}(l_{i}, x_{j})]
$$

+
$$
\frac{(1 - P_{0})\Delta}{L_{c}L} \sum_{i=1}^{N_{is}} \int_{0}^{L} F[\log U_{0}(l_{j}, x_{i})]dl,
$$
 (5)

where $l_i = i\Delta; x_j = j\Delta$ are the distances from the *i*th and *j*th sections up to the traction substation and $U_0(l_i; x_j)$ is the voltage generated at the *j*th section upon insulation failure of the contact network of the *i*th section.

The formulas corresponding to the various grounding methods of catenary supports can be derived from

the general expression for probability P_i of the actuating voltages exceeding permissible values.

Let $M(P1)$ and $M(P2)$ be the mathematical expectations of the number of dangerous situations for personnel when using the railway track for grounding supports and using as a grounding conductor only reinforcements of supports connected into sections with a length of 600 m.

Assuming reliable operation of the protective systems of traction systems at parts of lines with catenary supports disconnected from a railway track, we have

where N_{con} is the number of insulation failures of contact network for a year in the sections of the supports located at the calculated part of the line.

Let us note that permissible voltages $U_a(t)$ are random variables distributed by a logarithmic-normal law.

According to the described methodology, the mathematical expectations of the number of dangerous situations at a part of a line with a length of 100 km when railway track supports are used for grounding M(P1) and with the proposed grounding system of the catenary supports M(P2) were calculated (Table 2).

It follows from Table 2 that the number of dangerous situations when grounding catenary supports are not used does not exceed the analogous values at electrified parts of lines at which a railway track is used to support grounding.

Therefore, when disconnection of emergency state the system of traction electric supply with disconnected from the railway track supports, based on the requirements of electrical safety, is more safety than the system, in which the railway track is used for grounding.

ESTIMATION OF THE LEVELS OF LIGHTNING OVERVOLTAGES IN A CONTACT NETWORK AT PARTS OF A LINE WITH SUPPORTS DISCONNECTED FROM A RAILWAY TRACK

As noted above, not using a railway track as a natural grounder is the most promising way to increase the operating reliability of electrified parts of rail lines.

When lightning current flows from a railway track, an overvoltage arises on low-voltage power lines of sig-

naling, centralization, blocking, and communication devices, which significantly exceeds the permissible values for insulation of electrical installations.

Possible causes of damage to the insulation of a contact network are low reliability of lightning arresters, including surge arresters, as well as specific features of the lightning protection of traction networks, in which the propagation velocities of electromagnetic waves in the contact network and railway track differ significantly.

The circuit of lightning current distribution in the contact network at the piece of lines with supports disconnected from a railway track is shown in Fig. 2.

Let us approximate the instantaneous value of lightning current flowing in the contact network right at the place of discharge [2]:

$$
i = I_{ml} e^{-at} \sin \omega t. \tag{7}
$$

The parameters in expression (7) were defined in [2].

With a wave approaching a surge wave coming to the catenary support, the voltage at insulation changes by the law

$$
u_{\sup} = iZ_{\text{c.w.i}} = I_{m1}Z_{\text{c.w.i}}e^{-a\left(t-\frac{I_1}{v}\right)}\sin\left[\omega\left(t-\frac{I_1}{v}\right)\right],
$$

Fig. 2. Estimated circuit of distribution of lightning current in the contact network at parts of lines with supports disconnected from railway tracks: (*1*) contact network, (*2*) insulator of support, (3) parameters R_0 and L_0 of catenary support, (*4*) lightning protection device, and (*5*) grounding conductor of lightning protection device.

Fig. 3. Peterson circuit for calculation of refracted (reflected) waves of voltage and current at the disconnected from railway track supports.

and the voltage at lightning arresters changes by the law

$$
U_{\text{lt}} = I_{m1} Z_{\text{c.w.}i} e^{-a\left(t - \frac{I_1}{v}\right)} \sin \omega \left(t - \frac{I_1}{v}\right),
$$

^l ^a ^t

where ν is the propagation velocity of a electromagnetic wave in the contact network; Z_{cw} is the wave impedance of the contact network, which can be taken equal to 200 Ω [6]; Z_w is the wave impedance of the lightning current channel, which is equal to 300 Ω [7]; and ℓ_1 and ℓ_2 are the distances from the lightning discharge into contact network to the support and lightning protection device.

The presented relations make it possible to calculate the voltage in the contact network until the point of time of insulation breakdown of the catenary support.

When the pulse voltage at the support reaches 50% of the permissible value (U_{per}) , insulation breakdown occurs. The time at which an insulation breakdown occurs is calculated from the relation

$$
U_{\text{per}} = I_{m1} Z_{\text{c.w.}i} e^{-a\left(t - \frac{I_1}{V}\right)} \sin \omega \left(t_{\text{br}} - \frac{I_1}{V}\right).
$$

With an inappreciable error, one can write

$$
t_{\text{br}} = \frac{e_{\text{l}}}{v} - \frac{1}{\alpha} \ln \frac{U_{\text{per}}}{I_{m1} Z_{\text{c.w.i}}}.
$$

Upon breakdown of the insulation of the contact network at point of time $t = t_{\text{br}}$, reflected and refracted waves are generated. To evaluate the operation of the lightning protection apparatus, the refracted waves in the contact network at the parts of a line with supports disconnected from the railway track are important.

We will calculate the refracted waves in the contact network and in the support using the Peterson circuit (Fig. 3).

The expression for incident voltage in operator form in accordance with the Peterson circuit (Fig. 3) has the form

$$
U_{\text{inc}}(P) = \frac{I_{m1}Z_{\text{c.w.i}}\omega}{\left(\rho + \alpha\right)^2 + \omega^2}e^{-t_{\text{inc}}\rho}.\tag{8}
$$

The refracted wave of voltage in the contact network is then defined from the relation: at $t_{\text{br}} \leq t$,

$$
u_{\text{ref}}(t) = I_{m1}\omega \frac{Z_{\text{c.w.i}}R_0}{Z_{\text{c.w.i}} + R_0} x \left\{ \frac{-\beta}{(\alpha - \beta)^2 + \omega^2} e^{-\beta(t - t_{\text{br}})} + \frac{1}{\omega} \sqrt{\frac{\alpha^2 + \beta^2}{(\alpha - \beta)^2 + \omega^2}} e^{-\alpha(t - t_{\text{br}})} \sin[\omega(t - t_{\text{br}} - \lambda)] \right\},\,
$$

where

$$
\beta = \frac{2R_0 + Z_{c.w.i}}{2Z_c}, \ \lambda = \arctan\left(-\frac{\omega}{\alpha}\right) - \arctan\frac{\omega}{\beta - \alpha}.
$$

The obtained expression makes it possible to determine the voltage propagating along the contact network from the point of time immediately after breakdown of the support insulation until the point of time at which the lightning protection device is activated.

Consequently, the voltage at the lightning protection device changes according to the expressions

$$
\frac{l_2}{v} \le t \le \frac{l_2}{v} + t_{\text{br}}
$$

at

$$
U_{\Gamma} = I_{m1} Z_{\text{c.w.}i} e^{-a\left(t - \frac{l_2}{v}\right)} \sin \omega \left(t - \frac{l_2}{v}\right),
$$

but, when $\frac{l_2}{v} + t_{\text{br}} < t$, the sum of $\frac{l_2}{v} + t_{\text{br}}$ is substituted for $t_{\rm br}$.

The duration of this voltage is determined by the time the possible response of the lightning arrester. It is determined by approximate methods assuming that the instantaneous voltage at the arrester/overvoltage limiter taking into account its volt–second characteristic is known.

To simplify the calculations, we will assume that support inductance $L_{\text{sup}} = 0$. The voltage of the refracted wave is then

$$
U_{\rm ref} = I_{m1} Z_{\rm c.w.i} e^{-a\left(t - \frac{I_1}{v}\right)} \sin \omega \left(t_{\rm br} - \frac{I_1}{v}\right) \frac{2R_0}{2R_0 + Z_{\rm c.w.i}}.
$$

When insulation breakdown occurs, reflected and refracted waves are generated at the catenary support. The input impedance of the support foundation is significantly less than the wave impedance of the contact network. The maximum voltage value of the refracted wave is

$$
U_{\text{max ref}} = I_{m1} Z_{\text{c.w.i}} \frac{2R_{\text{e}}}{R_{\text{e}} + Z_{\text{c.w.i}}},
$$

or the expression will take the approximate form

$$
U_{\text{max ref}} = 2I_{m1}R_{\text{e}}.
$$

Thus, at $I_m = 10$ kA, the resistance of the foundation part of supports is $R_{\text{sup}} = 10 \Omega$ and $Z_{\text{ref.w}} = 200 \Omega$. The maximum value of the voltage of the refractive wave in the contact network is $U_{\text{max,ref}} = 0.25 \times 10 \times 2 \times 10 =$ 50 kV.

Diagrams of the probability of the amplitudes of lightning currents according to the data of different authors are presented in [7]. In particular instances, the maximum value of lightning currents reaches about 100 kA. In this case, the maximum value of the voltage of a refracted wave will significantly exceed the permissible voltage of the insulators of the contact network [6]. To keep them from breaking down, it is needed to mount the overvoltage limiter on the support; however, it is economically unfeasible to do this on all supports. Using a lightning protection conductor to avoid lightning current coming into the contact network is not possible for both technical and economic considerations.

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