Identification of Vehicle Model Parameters under External Disturbances

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Abstract—The paper proposes an approach to identification of model parameters of a vehicle subjected to external disturbances. Parameter estimates are generated using iteration procedure, which consists in estimation of the vehicle state vector including the disturbances and in estimation of vehicle model parameters using the least squares method. Identified parameters are insensitive to various external disturbances. The proposed approach was tested in full-scale tests. Modeling results are presented.

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INTRODUCTION

If a vehicle control law is synthesized using a noninvariant approach with account for vehicle dynamics, the vehicle mathematical model is required to estimate its state vector. Usually, the mathematical model in state space can be constructed based on the natural forces and moments affecting the vehicle accurate to several parameters, which are refined or determined by solving the identification problem during the fullscale tests. Identification methods should satisfy certain requirements, namely:

—sufficient accuracy;

----independence of initial conditions;

—immunity to external disturbances;

-consideration for the measurement errors of onboard devices.

Currently, the most widespread methods used for identification of vehicle model parameters are based on [1-3]

—prediction errors;

-subspaces;

-multialternative filtering.

In publications [4, 5], which became classical in identification of surface ship model parameters, hydrodynamic model coefficients are determined by the error prediction method using gradient procedure. The measurement prediction is realized by extrapolating the value of state vector using the Kalman filter multiplied by the observation matrix. In dynamic model of Kalman filter no external disturbances are considered, which makes the identified parameters very sensitive to disturbances.

Algorithm for identification of hydrodynamic coefficients of autonomous underwater vehicle (AUV) model using Gauss-Newton gradient procedure is addressed in [6]. Navigation and dynamic motion

parameters are estimated by the Kalman filter using invariant model of the vehicle motion and orientation, which allows parameter determination by IMU data with sonar receiver aiding.

An approach described in [7] uses error prediction method with model parameter identification by the least squares method (LSM). Measurements were performed using AUV special cable-supported model under various motions reproduced by the test facility, which also measured the model motion characteristics. The forces acting on the model were measured by dynamometers.

The method considered in [8] determines the parameters of ship linear dynamic model described in state space. Specific features of LSM application are discussed, however, external actions such as wind, heave, and stream are not taken into consideration.

Subspace identification approach has been recently studied in many publications (see for example [9]). In [9], identification is performed in two steps: (1) Hankel matrix is constructed using input and output signals; the model order is determined by this matrix; singular value decomposition of Hankel matrix is performed; and augmented observation matrix, and vehicle dynamic and observation matrices are constructed; (2) control matrices are constructed using LSM. With this approach, the model initially has an approximating character. Construction of approximating dynamic models is illustrated in [10, 11]. Example of using multialternative filtering is provided in [12].

It should be noted that the described methods suffer from significant dependency of parameter estimates on external disturbances. Advantages and disadvantages of these methods are analyzed in detail in [13], and the list of drawbacks of methods is given in Table 1.

Method	Drawback
Prediction errors	Values of identified parameters depend on external disturbances. Nonlin- ear filtering problem should be solved with account for sensitivity equa- tion if extended Kalman filter is used.
Subspaces	Values of identified parameters depend on external disturbances. It is dif- ficult to associate the state vector components with physical meanings.
Multialternative filtering	The set of models should be constructed with account for external distur- bances; data recording interval to select the most reliable hypothesis is rather long; a large set of models is required to provide sufficient accu- racy; nearly identical models have the same identification procedure

External disturbances critically complicate identification of model parameters. Then as described in above-mentioned publications, the identified model parameters strongly depend on the disturbance level, which degrades the parameter estimates if the contribution of disturbances is not considered in identification. The paper considers the techniques used to reduce the effect of external disturbances on parameter determination accuracy if identification problem is solved using prediction error method. Modeling results are presented which demonstrate the efficiency of the proposed methods. This approach was used to identify the model parameters for a hydrographic ship.

Main Aspects of Identification Problem

Effective application of identification methods is mostly determined by correct understanding of associated limitations, so here we provide the statement of identification problem.

Let the vehicle dynamic model be described by an equation

$$X_{K+1} = A(\alpha)X_K + B(\beta)u_K + W + W_K, \qquad (1)$$

where X_K is model state vector at time K, u_K is the control vector (input signal); A is the dynamic matrix linearly depending on parameter vector α , B is the control matrix linearly depending on parameter vector β , W and W_K are the vectors characterizing low-frequency (constant and slowly varying) and high-frequency components of disturbances.

Measurement vector (output signal) is given by

$$Y_K = HX_K + V_K, \tag{2}$$

where V_K is the vector of measurement errors.

To account for disturbances we include them in the state vector and describe by the following models: constant disturbances W_i , by $\dot{W}_i = 0$, and slowly varying disturbance components, by first order Markov process.

Based on the model (1) and additionally introduced state vector components the output can be predicted. Predicted output \tilde{Y}_{K+1} for the next step is described by the relations:

$$\tilde{X}_{K+1} = A\hat{X}_{K} + Bu_{K}, \quad \tilde{Y}_{K+1} = H\tilde{X}_{K+1},$$
 (3)

where \tilde{X}_{K+1} is the predicted state vector; \hat{X}_{K} is the sate vector estimate for the current step determined by the equation:

$$\hat{X}_{K} = \tilde{X}_{K} + K_{K} \left(Y_{K-1} - H \hat{X}_{K-1} \right).$$
(4)

In (3), vector \hat{X}_{K} is the augmented vector including constant and slowly varying disturbances; matrices of extended system are denoted by A and B and are given by

$$\mathbf{A} = \begin{bmatrix} A(\alpha) & 0 \\ 0 & A_W \end{bmatrix}, \ \mathbf{B} = \begin{bmatrix} B(\beta) \\ 0 \end{bmatrix},$$

where A_W is the matrix of dynamic models of disturbances W, 0 denotes the corresponding zero matrixes.

Kalman gain K and covariance matrix P are given by

$$K_{K} = AP_{K}H^{T}(HP_{K}H^{T} + R)^{-1}; P_{K+1} = AP_{K}A^{T} + GG^{T} - AP_{K}H^{T}(HP_{K}H^{T} + R)^{-1}HP_{K}A^{T}.$$
(5)

Here P_0 is the initial covariance matrix of state vector components, R is V covariance matrix, G is the matrix of intensities of generating noises included in disturbance model.

Let us make two comments on generation of filter (4), (5).

First, the Kalman filter should be calculated with account for matrix *A*, whose components should be determined. Further suppose that components of A are known but to a low accuracy and thus the filter should be robust to uncertainty of model parameters. This filter can be constructed by studying the sensitivity to dynamic matrix components. Constructing robust filters is addressed for example in [14]. If the model parameters are unknown, it is difficult to construct a filter.

Second, matrices A and H should be such that observability condition (all components of state vector can be estimated using the measurements) is met.

Table

The Problem of Identification of Vehicle Model Parameters

We have a set of data

$$Z^{N} = \{Y_{1}, u_{1}, Y_{2}, u_{2}, \dots Y_{N}, u_{N}\}.$$
 (6)

The structure of dynamic and control matrices is set accurate to unknown parameters. Information in Z^N should be used to determine the parameters of model (1), i.e., identify unknown parameters of matrices $A(\alpha)$ and $B(\beta)$.

In this context, the criterion of model parameter determination will be the prediction error [2, 3]. Thus a good model is a model which predicts well, i.e., generates small prediction errors for the available observation data. Prediction error for one step is determined by the equation

$$\varepsilon_K = Y_K - H\hat{X}_K. \tag{7}$$

Model parameters are determined by error minimization criterion

$$J(\alpha,\beta,Z^{N}) = \frac{1}{N} \sum_{K=1}^{N} \varepsilon_{K}^{2}.$$
(8)

Then the estimate of model parameters is given by

$$(\hat{\alpha}, \hat{\beta}) = \operatorname*{arg\,min}_{\alpha, \beta} J(\alpha, \beta, Z^N).$$
 (9)

After introduction of criterion the identification problem is reduced to searching for its extremum. Computational methods used to determine the parameters are described in sufficient detail in [2, 3].

Approach to Model Parameter Identification

Here, we consider the case where the parameters of dynamic and control matrices are unknown. Therefore, data required to construct the filter and to estimate the state vector are lacking.

Make the following assumptions: (1) observation matrix is such that all components of state vector of dynamic model (1) are observed, some part of which are observed jointly with the disturbances; disturbances are not observed directly; (2) conditions of state vector observability are met, i.e., disturbances included in the state vector can also be estimated.

With these assumptions, observation matrix H can be represented as

$$H = \begin{bmatrix} E & H_1 \end{bmatrix},\tag{10}$$

where E is the unity matrix of the relevant dimensions, matrix H_1 has at least one nonzero component.

To estimate the model parameters in the first approximation, we use only available data: data set Z^N according to (6) and the structure of extended dynamic and control matrices.

As a state vector estimate, we use the measurement at the previous step $\hat{X}_{K-1} \approx Y_{K-1}$ according to the first formula in (3) and the corresponding control u_{K-1} , assuming that disturbances are zero. Summing the prediction errors (7), we come to criterion (8). Minimizing this criterion by unknown model parameters, we obtain the equation to determine the first approximations of these parameters. Minimization is performed using LSM method.

We generate the matrix

$$Y^N = \begin{bmatrix} Y_1 & Y_2 & \dots & Y_N \end{bmatrix}$$
(11)

and matrix

$$Z_0^N = \begin{vmatrix} Y_0^0 & Y_1^0 & \dots & Y_{N-1}^0 \\ u_0 & u_1 & \dots & u_{N-1} \end{vmatrix}.$$
 (12)

Then matrix equation to determine the first approximations of model parameters using the observations of input-output pairs will be given by

$$\begin{bmatrix} A & B \end{bmatrix} Z_0^N = Y^N. \tag{13}$$

Equation (13) has the only solution with respect to the block matrix [A B]

$$\begin{bmatrix} A & B \end{bmatrix} = Y^N \left(Z_0^N \right)^T \left[Z_0^N \left(Z_0^N \right)^T \right]^{-1}, \qquad (14)$$

if there are no linearly depending columns among the matrix columns $Z_0^N (Z_0^N)^T$ (otherwise, Eq. (13) has infinitely many solutions, among which we choose the solution with the minimal norm).

The first approximations of parameters are used to construct the Kalman filter according to (4) and (5). The estimates of state vector components including the disturbances obtained using this Kalman filter and data set (11) and (12) are used to determine the approximations of model parameters as follows. Generate the updated measurements

$$Y_i^1 = Y_i - H_1 W_i^1, (15)$$

by subtracting the estimates of disturbances obtained at each filtering step from the available measurements. Generate matrix Z_1^N (12) with the updated measurements Y_i^1 . Using (14) and replacing Z_0^N by Z_1^N , we obtain the next approximation of the model parameters. We repeat the calculation procedure in the same manner as for the first approximation with updating of measurements Y_i^2 to determine the next approximation, etc.

The described iteration procedure refines the disturbances and the parameter estimates at each step.

Example. Here we provide an example of using the proposed identification approach for the model of lateral motion of hydrographic ship:

$$\dot{V}_{y} = a_{11}VV_{y} + a_{12}V\omega + b_{1}V^{2}\delta + F, \quad \dot{\omega} = a_{21}VV_{y} + a_{22}V\omega + b_{2}V^{2}\delta + lF, \quad \dot{F} = -\mu_{F}F + \sigma_{F}\sqrt{2\mu_{F}}w_{1}; \quad (16) \dot{V}_{Ty} = -\mu_{V}V_{Ty} + \sigma_{V}\sqrt{2\mu_{V}}w_{2},$$

where V_y is the ship lateral speed through the water; ω is the yawing angular velocity; F is the normalized slowly varying lateral component of the wind force (force divided by the sum of the ship weight and the additional mass); V_{Ty} is the unaccounted slowly vary-

ing current component being the systematic error of measurement; μ_F and μ_V are the values inverse to correlation interval; σ_F and σ_{V_T} are RMS disturbances; w_i is the independent generating white noise of unit intensity; *V* is the ship speed through the water (measured by water speed log and assumed known to sufficient accuracy); δ is the control action (rudder displacement); a_{ij} and b_i are the model parameters; *l* is the known normalized arm of lateral component of wind force (the arm multiplied by the sum of the ship weight and the additional mass and divided by the sum of ship inertia moment and the added mass moment of inertia of water with respect to the vertical axis; the formulas to calculate them are given in all reference books on ship control theory).

Generate the discrete model using the continuous model (16):

$$V_{yK+1} = a_{11}V_{yK} + a_{12}\omega_K + b_1\delta_K + F_K, \quad \omega_{K+1} = a_{21}V_{yK} + a_{22}\omega_K + b_2\delta_K + lF_K, \quad F_{K+1} = \mu_F F_K + g_F w_{1K}, \quad (17) V_{TyK+1} = \mu_V V_{TyK} + g_V w_{2K},$$

with the parameters a_{ij} and b_i to be identified denoted as in earlier formulas.

Measurement equations are given by

$$y_{VK} = V_{\text{GPS}K} \sin(\text{COG}_{\text{GPS}K} - K_K) + \upsilon_{VK};$$

$$y_{\omega K} = \omega_K + \upsilon_{\omega K},$$
(18)

where V_{GPS} is the speed over ground, COG_{GPS} is the course over ground measured by GNSS receivers; v_{ω} , v_{V} are white noise processes.

For identification purposes, the vehicle performs a zigzag maneuver set by the following rudder control. At the initial moment, the ship heading K_0 is fixedd. Yawing angle ψ is calculated by the formula $\psi = K - K_0$, where *K* is the current heading. At initial moment the rudder is displaced to the starboard through the angle $\delta = \delta_0$ with maximum speed. The rudder is kept in this position until yawing angle ψ reaches the preset value ψ_0 . Then the rudder is displaced to the port through the angle $\delta = -\delta_0$ and is kept in this position until the yawing angle reaches $(-\psi_0)$, etc. Denote this maneuver by (ψ_0/δ_0) .

Due to methodical reasons, Eq. (17) does not account for the dependency of discrete model parameters a_{ij} and b_i on the speed of motion (this dependency is known, and parameters of discrete model can always be recalculated for continuous model with account for the speed through the water measured by the water speed log or speed through the water can be estimated by the proposed method using the equations of the ship longitudinal motion). As confirmed by the practice, during zigzag maneuver speed through the water is nearly constant after the second rudder displacement. First measurement (18) is related to the state vector components as follows

$$y_{VK} = V_{\text{GPS}K} \sin(\text{COG}_{\text{GPS}K} - K_K) + \upsilon_{V_TK}$$

= $V_{0K} \sin \alpha_{DK} + V_T \sin(K_T - K_0 - \psi_K) + \upsilon_{V_TK}$, (19)

where V_0 is the speed through the water, α_D is the drift angle; V_T is the current speed, K_T is the current heading.

The first summand in (19) is V_y , and the second summand after expanding the sinus of angle difference with account for first order smallnesses for angle ψ can be presented as $V_T \sin(K_T - K_0) + V_T \cos(K_T - K_0)\psi_K$. Then $V_T \sin(K_T - K_0) = V_{Ty}$, and the second summand can be neglected if heading K_0 is crossing the main current stream.

The measurement matrix becomes $H = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 \end{bmatrix}$.

State vector components are observable in accordance with observability criterion.

Error in measurement prediction y_{VK+1} using the first model equation (17) according to the proposed approach is generated using the previous measurements

$$\varepsilon_{K+1} = y_{VK+1} - \hat{y}_{VK+1} = y_{VK+1} - (a_{11}y_{VK} + a_{12}\omega_K + b_1\delta_K).$$

Using all the measurements from the first to the N-th measurement, summing the prediction errors and minimizing criterion (8), determine the first approximation of model parameters for the first equation. Similarly, we determine the model parameters in the system second equation (17). After estimating the system state vector (17) using the first approximation of model parameters, we obtain the estimates of state vector components given in Fig. 1.

The plots demonstrate that the yawing angular velocity is estimated rather accurately (true values and estimates agree); for the component V_y the estimate is between the measurement and true value curves; disturbing force is practically not estimated (true value of normalized force is $5 \times 10^{-3} \text{ m/s}^2$); the current component is estimated as a half value (true value is 0.3 m/s).

Generate the prediction error using the parameters of the first approximation for the second approximation with account for the estimated wind force and current

$$\varepsilon_{K+1} = y_{VK+1} - \hat{y}_{VK+1} = y_{VK+1} \\ - \left\{ \left[\tilde{a}_{11} \left(y_{VK} - \hat{V}_{TK} \right) + \tilde{a}_{12} \omega_K + \tilde{b}_1 \delta_K + \hat{F}_K \right] - \hat{V}_{TK+1} \right\}.$$

For the next iterations, the procedure is repeated.

Estimate the parameter second approximation using the set of prediction errors. Use the similar procedure for the second equation of the system (17). After several iterations we obtain the refined model parameters (Fig. 2) and parameter estimates (Fig. 3). Horizontal straight lines in Fig. 2 correspond to the true values.



Fig. 1. Estimate of system (16) state vector based on the first approximation of model parameters.

Figure 3 shows that the disturbances are estimated sufficiently accurately, the estimates of lateral velocity component practically coincide with the true values.

The 25th iteration provided the following accuracies of model parameter estimation: for a_{11} —10%, for a_{12} —10%, for a_{21} —25%, for a_{22} —20%, for a_{1} —20%, for a_{2} —5% of the true values.

Modeling results demonstrate that iterative process of refining the model parameters converges, then parameter estimation error is 10-15% of the true value.

This procedure was checked in the tests of control channel of navigation-control system onboard a hydrographic ship. The identified model parameters were used to synthesize a control law, whose quality is confirmed by highly stable stabilization during tack-ing [15].

CONCLUSIONS

Analysis of traditional methods used to identify the vehicle model parameters in state space has shown that their disadvantages are associated with parameter high susceptibility to the acting disturbances.

We propose an approach to identify model parameters of sea vehicles exposed to slowly varying disturbances (with neglected high-frequency components) with initially unknown model parameters, which makes the identified parameters immune to external disturbances.

The proposed approach was implemented in navigation control system software to stabilize the hydrographic ship. The results of sea trials reveal fairly good ship stabilization using the control law synthesized



Fig. 2. Modeling the refinement of model parameters in 25 iterations.

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Fig. 3. Estimate of state vector based on the 25th approximation of model parameters.

with the help of identified model parameters in conditions of wind and wave disturbances.

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