**NANOSCALE AND NANOSTRUCTURED MATERIALS AND COATINGS**

# **The Effect of the Affinity of Components of Polymer/Carbon Nanotube Nanocomposites on Their Properties**

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**Abstract**—We introduce the concept of structural affinity of the components of polymer/carbon nanotube nanocomposites quantitatively estimated in the framework of fractal analysis. The affinity of the components significantly affects the characteristics that are essential for nanocomposites, that is, the level of interfacial adhesion and the degree of aggregation of the nanofiller. This means that the degree of affinity completely determines the elastic modulus of the nanocomposite at a fixed concentration of the nanofiller. In turn, this indicator is determined by the structure of carbon nanotubes in the polymer matrix. The creation of highmodulus nanocomposites requires achieving full (or close to it) affinity of the components of these nanomaterials.

**Keywords:** nanocomposite, carbon nanotubes, affinity, structure, aggregation, interfacial adhesion, fractal dimension

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# INTRODUCTION

Affinity is a thermodynamic characteristic that quantitatively describes the degree of interaction between substances [1]. This term refers to the affinity of one substance for another during a reaction. The terms "chemical affinity," "electron affinity," "proton affinity," etc. are commonly used. In the case of nanocomposites, affinity is usually understood as the thermodynamic affinity between a nanofiller and a polymer matrix [2, 3]. Regarding polymer nanocomposites, in addition to chemical aspects, there is also structural affinity defined as the closeness of the structural characteristics of the nanocomposite components, which can be characterized by the difference in the fractal dimensions of the surface of the nanofiller and the polymer matrix.

The goal of this work is a quantitative description of this structural affinity and its effect on the final properties of nanocomposites.

# EXPERIMENTAL

Industry-produced (PP) Kaplen grade 01030 was used as the matrix polymer. Polypropylene of this grade has a melt flow index of 2.3–3.6 g/10 min, a weight-average molecular weight of  $\sim$  (2–3)  $\times$  10<sup>5</sup>, and a polydispersity index of 4.5.

We used Taunit carbon nanotubes (CNTs) with an outer diameter of 20–70 nm, an inner diameter of 5– 10 nm, and a length of 2 μm or more as a nanofiller. In the studied PP/CNT nanocomposites, the CNT concentration varied within 0.25–3.0 wt %.

PP/CNT nanocomposites were obtained by mixing the components in a melt in a Thermo Haake Reomex RTW 25/42 twin-screw extruder (Germany). Mixing was performed at a temperature of 463–503 K and a screw rotation speed of 50 rpm for 5 min. Test samples were obtained by injection molding using a Test Sample Molding Apparate RR/TS (Ray-Ran, United Kingdom) at a temperature of 503 K and a pressure of 43 MPa.

Mechanical tests for uniaxial tension were performed using samples in the form of a double-sided blade with dimensions according to GOST (State Standard) 11262-80. The tests were carried out with a universal Gotech Testing Machine CT-TCS 2000 (Germany) at a temperature of 293 K and a strain rate of  $\sim$  2  $\times$  10<sup>-3</sup> s<sup>-1</sup>.

### RESULTS AND DISCUSSION

Affinity, as applied to the description of interfacial effects in polymer nanocomposites, can be interpreted as difference  $\Delta d_f$  between fractal dimensions of the polymer matrix structure  $d_{\rm f}$  and nanofiller surface  $d_{\rm surf}$ :

$$
\Delta d_{\rm f} = d_{\rm f} - d_{\rm surf}.\tag{1}
$$

Dimensions  $d_f$  and  $d_{\text{surf}}$  can be determined as follows. Carbon nanotubes in the polymer matrix of the



**Fig. 1.** Dependence of parameter  $b_{\alpha}$  characterizing the level of interfacial adhesion on difference in dimensions Δ*d*<sup>f</sup> for PP/CNT nanocomposites.

nanocomposite form ring-shaped formations of radius  $R_{\text{CNT}}$  [4], the value of  $d_{\text{surf}}$  of which is [5]

$$
d_{\text{surf}} = 2 + 1.75(R_{\text{CNT}} - 0.14),\tag{2}
$$

where radius  $R_{\text{CNT}}$ , specified in micrometers, for the nanocomposites under consideration is taken according to the data of [6].

The dimension of the nanocomposite structure  $d_f$ , which is assumed to be the dimension of the polymer matrix structure, is determined by the equation [6]

$$
d_{\rm f} = (d-1)(1+\nu), \tag{3}
$$

where *d* is the dimension of the Euclidean space in which the fractal is considered (in our case,  $d = 3$ ) and ν is the Poisson's ratio determined from the results of mechanical tests using the relation [7]

$$
\frac{\sigma_{\rm Y}}{E_{\rm n}} = \frac{1 - 2v}{6(1 + v)},
$$
\n(4)

where  $\sigma_Y$  and  $E_n$  are the yield stress and elastic modulus of the nanocomposite, respectively.

It should be expected that degree of affinity (structural affinity) of the nanocomposite components  $\Delta d_f$ primarily affects the level of the polymer matrix– nanofiller interfacial adhesion, which can be characterized by dimensionless parameter  $b_{\alpha}$  [8]. The value of  $b_\alpha$  can be determined using the following percolation relation [8]:

$$
\frac{E_{\rm n}}{E_{\rm m}} = 1 + 11 \left( c b_{\alpha} \varphi_n \right)^{1.7},\tag{5}
$$

where  $E_n$  and  $E_m$  are the elastic moduli of the nanocomposite and matrix polymer, respectively (the ratio  $E_n/E_m$  is usually called the "degree of reinforcement" of the nanocomposite),  $c$  is a coefficient ( $c \sim 2.8$  for carbon nanotubes [8]), and  $\varphi_n$  is the volume concentration of the nanofiller, which can be estimated according to the well-known equation [8]

$$
\varphi_n = \frac{W_n}{\rho_n} \tag{6}
$$

Here,  $W_n$  is the weight concentration of the nanofiller and  $\rho_n$  is its density determined for carbon nanotubes as [8]

$$
\rho_{\rm n} = 188 (D_{\rm CNT})^{1/3}, \text{ kg/m}^3, \tag{7}
$$

where  $D_{\text{CNT}}$  is the outer diameter of a carbon nanotube given in nanometers.

Figure 1 shows the dependence of the level of interfacial adhesion characterized by parameter  $b_{\alpha}$  on the affinity of the nanocomposite components characterized by the difference in the dimensions  $\Delta d_f$  for PP/CNT nanocomposites. As expected, there is a strong decrease in  $b_{\alpha}$  as  $\Delta d_f$  increases, which is described by a linear relationship, analytically expressed by the following equation:

$$
b_{\alpha} = 11.8 - 17.5 \Delta d_{\rm f}.
$$
 (8)

It follows from Eq. (8) that the maximum value  $b<sub>\alpha</sub>$  = 11.8 for the nanocomposites under consideration takes place in the case of complete affinity of the nanocomposite components, i.e., at  $\Delta d_f = 0$ . At  $\Delta d_f = 0.68$ ,  $b_\alpha =$ 0; that is, interfacial adhesion is completely absent.

Next, let us consider the effect of the affinity of the components of PP/CNT nanocomposites on the degree of nanofiller aggregation; this process is the most significant of those adversely affecting the properties of these nanomaterials. The degree of such aggregation can be estimated by parameter χ determined by the equation [9]

$$
\chi = \frac{\varphi_n}{\varphi_n + \varphi_{if}},\tag{9}
$$

where  $\varphi_{if}$  is the relative proportion of interfacial regions.

The sum of ( $\varphi_n + \varphi_{if}$ ) can be determined using the following percolation relation [8]:

$$
\frac{E_{\rm n}}{E_{\rm m}} = 1 + 11(\varphi_{\rm n} + \varphi_{\rm if})^{1.7} \,. \tag{10}
$$

Figure 2 shows dependence  $\chi[(\Delta d_f)^3]$  for the nanocomposites under consideration; we selected such a form of this dependence to linearize it. The data in Fig. 2 are analytically described by the following equation:

$$
\chi = 0.02 + 1.07 \left(\Delta d_{\rm f}\right)^3,\tag{11}
$$

which indicates two specific features of the relationship between parameters  $\chi$  and  $\Delta d_{\rm f}$ . First, the degree of



**Fig. 2.** Dependence of the degree of nanofiller aggregation, characterized by parameter χ on difference in dimensions Δ*d*<sup>f</sup> for PP/CNT nanocomposites.

nanofiller aggregation cannot be zero, and the minimum value of  $\chi$  for PP/CNT nanocomposites is 0.02. Second, there is a strong (cubic) dependence of the degree of aggregation of carbon nanotubes on the affinity of the nanocomposite components. This dependence is explained by comparing the graphs in Figs. 1 and 2. An increase in the degree of affinity, characterized by the difference  $\Delta d_f$ , weakens the level of interfacial bonds, characterized by the parameter  $b_{\alpha}$ , which prevents the "sticking" (combining) of individual nanoparticles into their aggregates. Consequently, a decrease in  $b_\alpha$  due to an increase in  $\Delta d_f$ intensifies the aggregation process.

An increase in  $\Delta d_f$  with an increase in the concentration of carbon nanotubes in PP/CNT nanocomposites is due to structural factors. An increase in  $\varphi_n$ determines a decrease in radius  $R_{\text{CNT}}$  of ring-shaped formations in CNTs and decreases surface dimension  $d_{\text{surf}}$  of these formations according to Eq. (2) at a practically constant dimension of the structure of PP/CNT nanocomposites  $d_f = 2.74$  [6]. This conclusion is confirmed by the dependence  $\Delta d_f(R_{\text{CNT}})$  for PP/CNT nanocomposites (Fig. 3). As expected, there is a decrease in  $\Delta d_f$  as  $R_{\text{CNT}}$  increases, which can be analytically expressed by the following empirical equation:

$$
\Delta d_{\rm f} = 0.89 - 1.28 R_{\rm CNT},\tag{12}
$$

where  $R_{\text{CNT}}$  is again given in micrometers.

The value of  $R_{\text{CNT}}$  cannot be zero or less than  $D_{\text{CNT}}$ , and its theoretical minimum value can be estimated from a combination of Eqs. (8) and (12). At the maximum value of  $\Delta d_{\rm f}$  = 0.68, the minimum value of  $R_{\rm CNT}$ is 0.164 μm, which is close to the similar value of this



Fig. 3. Dependence of difference in dimensions  $\Delta d_f$  on radius  $R_{\text{CNT}}$  of ring-shaped formations of carbon nanotubes for PP/CNT nanocomposites.

radius of 0.208 μm, obtained within the percolation theory [6]. In turn, the value  $\Delta d_f = 0$  is realized at  $R_{\text{CNT}} = 0.72 \,\mu\text{m}$ . This confirms the structural origin of the affinity of the polymer nanocomposite components.

In [9], the following percolation relation was proposed to determine degree of reinforcement *E*n/*E*m of polymer nanocomposites:

$$
\frac{E_{\rm n}}{E_{\rm m}} = 1 + 11 \left( \frac{\varphi_{\rm n}}{\chi} \right)^{1.7}.
$$
 (13)

The combination of Eqs. (11) and (13) yield the following relationship for estimating degree of reinforcement  $E_n/E_m$  of nanocomposites:

$$
\frac{E_{\rm n}}{E_{\rm m}} = 1 + 11 \left( \frac{\varphi_{\rm n}}{0.02 + 1.07 \left( \Delta d_{\rm f} \right)^3} \right)^{1.7} . \tag{14}
$$

Equation (14) is significant in two aspects. First, it demonstrates that one of the essential indicators of polymer nanocomposites, namely, the degree of reinforcement, is determined only by the affinity of the nanocomposite components at a fixed concentration of nanofiller. Second, this ratio indicates a way to increase the elastic modulus of nanocomposites with high-modulus nanofillers (carbon nanotubes, graphene) by decreasing  $\Delta d_f$ . The potential of these nanofillers is underused; the current level of their utilization is approximately 8% [4]. The maximum achievable elastic modulus of a nanocomposite can be estimated using a simple mixture rule [10]:

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**Fig. 4.** The comparison of degree of reinforcement  $E_n/E_m$ , (*1*) calculated by Eq. (14) and (*2*) experimental, on volume concentration of the nanofiller  $\varphi_n$  for PP/CNT nanocomposites.

$$
E_n^{\max} = E_{\text{CNT}} \varphi_n + E_m (1 - \varphi_n), \tag{15}
$$

where  $E_{\text{CNT}}$  is the nominal modulus of elasticity of carbon nanotubes, which is  $\sim$  1000 GPa [4].

The estimates by Eq. (15) at  $\varphi_n = 0.05$  yield  $E_n^{\max}$  or, for the case of the nanocomposites under consideration with the value  $E_m \approx 1 \text{ GPa}$ ,  $E_n/E_m \approx 51$ . The estimate of  $E_n/E_m$  by Eq. (14) at  $\varphi_n = 0.05$  and  $\Delta d_f = 0$ gives the same  $E_n/E_m$  value. This means that, for the full implementation of high values of the elastic modulus of CNTs and graphene, it is necessary to achieve the full affinity of the nanocomposite components or the condition  $\Delta d_{\rm f} = 0$ .

Figure 4 compares the dependences of degrees of reinforcement  $E_n/E_m$  on volume concentration of the nanofiller  $\varphi_n$  for PP/CNT nanocomposites calculated by Eq. (14) and experimentally obtained. We observed a good agreement between theory and experiment: their average discrepancy is 3%, which does not exceed the experimental error in determining this parameter, confirming the correctness of the model proposed in this work.

In conclusion, the following circumstance should be noted. In the Euclidean approximation, quantities  $d_f$  and  $d_{\text{surf}}$  are constant;  $d_f = 3$  and  $d_{\text{surf}} = 2$ ; that is,  $\Delta d_f = 1$ . According to Eq. (9), this means negative values of  $\varphi_{if}$  and, according to Eq. (12), negative values of  $R_{\text{CNT}}$ , which has no physical meaning. Therefore, the analysis of the structure and properties of polymer nanocomposites requires the use of fractal analysis methods.

# **CONCLUSIONS**

Therefore, in this work, we introduced the postulate of physical or structural affinity of the nanocomposite components as the difference between the fractal dimensions of the polymer matrix structure and the nanofiller surface. An increase in this difference (decrease in affinity) significantly decreases the level of interfacial adhesion and dramatically (as the cubic dependence) enhances the process of nanofiller aggregation. Affinity is controlled by a structural factor, namely, the formation of ring-shaped formations of carbon nanotubes, i.e., their bend. The level of affinity expressed by the above difference in dimensions completely controls the degree of reinforcement or modulus of elasticity of the nanocomposite at a fixed concentration of the nanofiller. The creation of highmodulus polymer/carbon nanotube nanocomposites requires achieving full (or close to it) affinity of the components of these nanomaterials.

#### CONFLICT OF INTEREST

The authors declare that they have no conflicts of interest.

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