

# Mathematical Model of Action Potential in Higher Plants with Account for the Involvement of Vacuole in the Electrical Signal Generation

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Received July 28, 2016; in final form, August 28, 2016

**Abstract**—Electrical signals, including action potential (AP), play an important role in plant adaptation to the changing environmental conditions. Experimental and theoretical investigations of the mechanisms of AP generation are required to understand the relationships between environmental factors and electrical activity of plants. In this work we have elaborated a mathematical model of AP generation, which takes into account the participation of vacuole in the generation of electrical response. The model describes the transporters of the plasma membrane ( $\text{Ca}^{2+}$ ,  $\text{Cl}^-$ , and  $\text{K}^+$  channels,  $\text{H}^+$ - and  $\text{Ca}^{2+}$ -ATPases,  $\text{H}^+/\text{K}^+$  antiporter, and  $2\text{H}^+/\text{Cl}^-$  symporter) and the tonoplast ( $\text{Ca}^{2+}$ ,  $\text{Cl}^-$ , and  $\text{K}^+$  channels;  $\text{H}^+$ - and  $\text{Ca}^{2+}$ -ATPases;  $\text{H}^+/\text{K}^+$ ,  $2\text{H}^+/\text{Cl}^-$ , and  $3\text{H}^+/\text{Ca}^{2+}$  antiporters), with due consideration of their regulation by second messengers ( $\text{Ca}^{2+}$  and  $\text{IP}_3$ ). The apoplasmic, cytoplasmic and vacuolar buffers are also described. The properties of the simulated AP are in good agreement with experimental data. The AP model describes the attenuation of electrical signal with an increase in the vacuole area and volume; this effect is related to a decrease in the  $\text{Ca}^{2+}$  spike magnitude. The electrical signal was weakly influenced by the  $\text{K}^+$  and  $\text{Cl}^-$  content in the vacuole. It was also shown that the contribution of vacuolar  $\text{IP}_3$ -dependent  $\text{Ca}^{2+}$  channels into the generation of calcium spike during AP was insignificant with the given parameters of the model. The results provide theoretical evidence for the significance of the vacuolar area and volume in plant cell excitability.

**Keywords:** action potential,  $\text{Ca}^{2+}$ , higher plants, inositol-3-phosphate, simulation, vacuole

**DOI:** 10.1134/S1990747817010068

## INTRODUCTION

Action potential (AP) is a remote electrical signal generated in response to external stimulation, in particular, light, cold, burn, pressure, touch, injury, etc. AP was revealed for the first time in the nerve and muscle cells of animals [1]. Later, the presence of AP was demonstrated in the higher [2, 3] and lower [4] plants, with the parenchymal cells of conducting bundles of the higher plants apparently having the highest excitability [5]. In contrast to animals, plants are characterized by the more negative values of resting potential and threshold potential for the generation of electrical response [5], the APs are longer (in most cases, 30–50 s and more) [6] and have no overshoot [5]. Plant APs are accompanied by considerable changes in the intra- and extracellular concentrations of  $\text{Ca}^{2+}$ ,  $\text{H}^+$ ,  $\text{K}^+$ , and  $\text{Cl}^-$  [5, 7, 8].

The AP triggers physiological changes including growth slowdown [9, 10], reactive oxygen species (ROS) signal initiation [9, 11], enhanced ATP level in plants [12, 13], decrease in transpiration and guttation [11, 14, 15], reduced photosynthetic activity [16–18], respiration activation [19, 20], etc. The physiological

processes induced by electrical signals contribute to plant resistance to unfavorable factors and adaptation to varying environmental conditions [21–24].

The ion mechanism of AP has to be thoroughly investigated in order to understand the relationships between the effect of external stimulus and the physiological response to this stimulus. The AP mechanism of plants was suggested on the basis of experimental studies [5, 11, 25]. The first stage of the development of electrical response includes the opening of  $\text{Ca}^{2+}$  channels sensitive to various environmental factors [26–28], which leads to an increase in  $\text{Ca}^{2+}$  concentration in the cytoplasm [29]. In its turn, it activates  $\text{Cl}^-$  channels [30–32] and reduces the  $\text{H}^+$ -ATPase activity [25]. The  $\text{Cl}^-$  current depolarizes the membrane, followed by the opening of  $\text{K}^+$  channels and subsequent repolarization. During repolarization,  $\text{H}^+$ -ATPase is activated again and the potential returns to its resting values [25, 33].

It should be noted that the described AP mechanism in the higher plants takes into consideration only the transport systems of the plasma membrane. The

involvement of vacuoles in AP generation was shown in charophytes [34–36], though such studies were not performed in the higher plants. The involvement of vacuoles in AP generation in the higher plants is favored by the following facts. (1) The vacuole occupies a considerable volume of plant cell (50–90%) [37, 38] and its shape is rather variable, which may substantially influence the area-to-volume ratio [39, 40]. One of the consequences of the large volume of the vacuole is the lesser volume of the cytoplasm; as a result, ion concentrations will change much more rapidly, which may lead to the modulation of AP parameters. (2) The vacuole is a depot of  $\text{Ca}^{2+}$  [41], which triggers AP, as well as other ions important for AP generation [8, 25, 35]. (3) The activity of transport systems of the vacuole is regulated by second messengers [42]:  $\text{Ca}^{2+}$  and  $\text{IP}_3$ , the content of which increases during AP [43, 44]. Thus, it may be supposed that the vacuole responds to the changes in composition of the cytoplasm, which cause the activation of its transport systems, i.e., the vacuole can play a key role in signaling and ion homeostasis maintenance.

However, experimental studies of the role of vacuoles in AP generation in the higher plants are difficult to perform because of small cell size. This problem can be solved through the mathematical modeling of AP in the higher plants. There are a number of models describing the involvement of ion transport systems of the plasma membrane in the generation of electrical response in plants [45–51]. In addition, some models describe the involvement of intracellular depots in the regulation of  $\text{Ca}^{2+}$  and electrical activity [43, 44]. Thus, the mathematical models presented in scientific literature cannot be used for theoretical analysis of the role of vacuole in electrogenesis of the higher plants.

This work was aimed at the development of a mathematical model of AP taking into account the ion transport systems of the plasma membrane and the tonoplast and theoretical analysis of the role of vacuole in AP generation in the higher plants.

## MATHEMATICAL DESCRIPTION OF THE MODEL

The model is based on the scheme of transport processes in the plasma membrane and the tonoplast, which is shown in Figure 1. For simplicity, it was assumed that the excited cells had a spherical shape.

The relationship between the changes in the membrane potential and the ion channels is described by the following equation [45, 52]:

$$\frac{dE_m}{dt} = \frac{1}{C} F \sum z_r j_r, \quad (1)$$

where  $E_m$  is the membrane potential,  $C$  is the membrane capacity,  $F$  is the Faraday's constant,  $j_r$  is the ion  $r$  flow,  $z_r$  is the ion  $r$  charge. Potential difference on the plasma membrane was calculated with the value of

electric potential in the apoplast taken as zero. In plants, the systems of both passive and active transport play the key role in the maintenance of membrane resting potential and AP generation [5, 25], which is taken into account in the model.

The passive transport is described by the Goldman–Hodgkin–Katz equation [48, 50]. At the same time, it is known that the activity of ion channels is regulated by the ratio of concentrations of the transported ion on both sides of the membrane [53, 54]. The widely known three-barrier model of ion channel [55, 56] can be used to describe this dependence. We have described the effect of channel saturation. Here, the probabilities that the ion will be linked to the channels at the inner ( $\theta_{in}$ ) and outer ( $\theta_{out}$ ) side are described by the equations

$$\theta_{in} = \frac{c_{in}}{c_{in} + \gamma}, \quad \theta_{out} = \frac{c_{out}}{c_{out} + \gamma}, \quad (2)$$

where  $c_{in}$  and  $c_{out}$  are the ion concentrations on both sides of the membrane (subscripts in and out refer to the cytoplasm and the apoplast (or vacuolar contents), respectively);  $\gamma = \frac{k_2}{k_1}$  is the channel–ion complex dissociation constant, where  $k_1$  is the rate constant for ion binding with the channel site and  $k_2$  is the rate constant for disintegration of the channel–ion complex (for simplicity, it was accepted that these constants are the same on both sides of the channel).

The probabilities that the ion will not be linked to the respective sites of the channel,  $\eta_{in}$  and  $\eta_{out}$ :

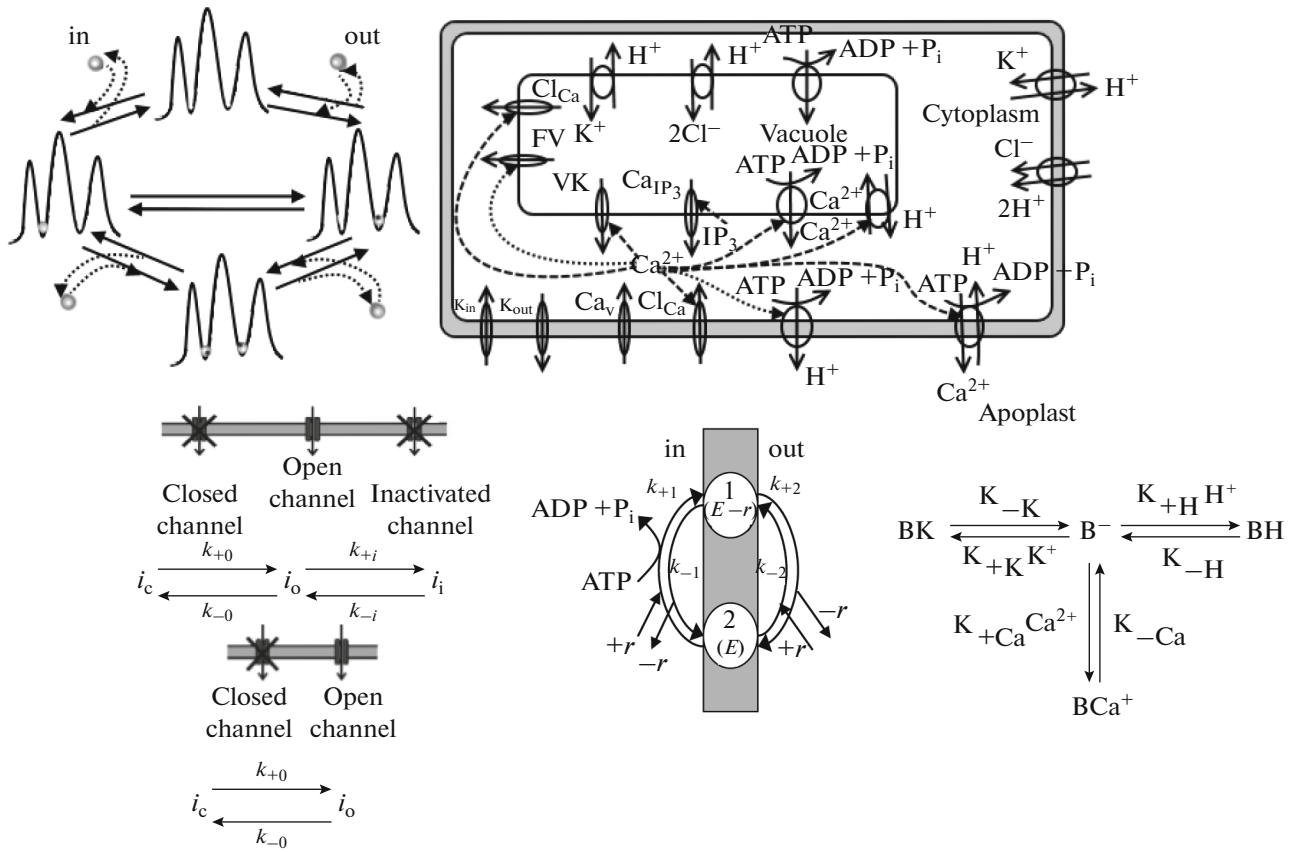
$$\eta_{in} = 1 - \theta_{in} = \frac{\gamma}{\gamma + c_{in}}, \quad \eta_{out} = 1 - \theta_{out} = \frac{\gamma}{\gamma + c_{out}}. \quad (3)$$

It is assumed that the probability of ion passage through the channel is determined by the product of probabilities  $\theta_{in}\eta_{out}$  for the outward flow and  $\theta_{out}\eta_{in}$  for the inward flow. Final Eq. (4) for the passive flow through the channels was used henceforth:

$$J = z u P'_{\max} p_o \frac{(\theta_{in}\eta_{out} - \theta_{out}\eta_{in}) \exp(-zu)}{1 - \exp(-zu)}, \quad (4)$$

where  $p_o$  is the ion channel open-state probability,  $P'_{\max} = P_{\max} c_{\text{chan}}$  is the maximum permeability per unit of area,  $P_{\max}$  is the maximum permeability of the ion channel,  $c_{\text{chan}}$  is the concentration of channels per unit of area,  $z$  is the ion charge,  $u = \frac{E_m F}{RT}$  is normalized dimensionless potential,  $R$  is the gas constant, and  $T$  is the absolute temperature.

The model takes into account the regulation of channels by membrane potential and the presence of ligands. There are charged groups within the channel. They can be differently positioned depending on the potential, thereby determining the channel activity. Different states of channels (closed (c), open (o) and



**Fig. 1.** The model of electrogenesis in higher plants. Scheme at the top right corner presents transport systems and their regulation by  $Ca^{2+}$  and  $IP_3$ . Dashed and dotted lines show activation by second messengers and inactivation, respectively. Scheme at the top left corner is a three-barrier model of a channel; transitions between different states of the channel are shown:  $i_c$ , closed;  $i_o$ , open;  $i_i$ , inactivated. At the bottom right corner, a “two-state” model used to describe ATPases and the buffer system of the apoplast are presented.

inactivated (i) are separated by potential barriers. The barrier crossing rates are determined by interactions between the ions with charged groups in the membrane and their averaged charges ( $c_o$  and  $c_i$ ). The rate constants for channel transitions between different states can be represented by the modified Arrhenius equation [48, 50]:

$$\begin{aligned}
 k_{+o(+i)} &= k_{o(i)} \exp\left(\frac{uc_{o(i)}}{2}\right), \\
 k_{-o(-i)} &= k_{o(i)} \exp\left(u_{o(i)}c_{o(i)} - \frac{uc_{o(i)}}{2}\right),
 \end{aligned}
 \tag{5}$$

where  $k_{+o}$  and  $k_{-o}$  are the rate constants for transition from the closed to open state and back,  $k_{+i}$  and  $k_{-i}$  are the rate constants for transition from the open to inactivated state and back,  $u_o$  and  $u_i$  are the normalized potential barriers for transition of the channels from the close to open state and from the open to inactivated state, respectively,  $k_o$  and  $k_i$  are the rate constants for transition of the channel between the closed and

open states and between the open and inactivated states, with  $u, u_o, u_i$  being equal to zero.

The probabilities of opening for the most of channels are described by a model taking into account only two states of the channel (open ( $p_o$ ) and closed ( $p_c$ ), Eq. (6)); for calcium channel, it is a model with three states (closed, open, inactivated ( $p_i$ ), Eq. (7)) [50]:

$$\frac{dp_o}{dt} = k_{+o}(1 - p_o) - k_{-o}p_o,
 \tag{6}$$

$$\frac{dp_o}{dt} = k_{+o}(1 - p_o - p_i) - k_{-o}p_o - k_{+i}p_o + k_{-i}p_i,
 \tag{7}$$

$$\frac{dp_i}{dt} = k_{+i}p_o - k_{-i}p_i.$$

At the same time, only two approaches are used to describe the probability of ion channel opening. For “slow” channels (i.e., the channels with activation times comparable to or exceeding the time of AP generation, the  $Ca_v$  and  $K_{out}$  channels in the model), differential Eqs. (6) and (7) were solved numerically. For “fast” channels (i.e., the channels with activation

times much less than the time of AP generation, the  $K_{in}$ ,  $Cl_{Ca}$ ,  $FV$ ,  $VK$ , and  $Ca_{IP_3}$  channels in the model), it was considered that the equilibrium state was achieved instantaneously (the stationary solution of Eq. (6)):

$$p_o = \frac{1}{1 + \exp(kc_o(u_o - u))}. \quad (8)$$

As was mentioned previously,  $Ca^{2+}$  and  $IP_3$  regulate the function of most of the passive and active transport systems of the plasma membrane and the tonoplast (Fig. 1). The ligand binding is a probabilistic process depending on ligand concentration ( $[L]$ ), affinity to the channel (reflected in the concentration for half-activation,  $K$ ), and the number of bound ligand molecules (the Hill coefficient,  $n$ ). The probability of channel opening with the activator ligand concentration in the medium  $[L]$ :

$$P_o = \frac{[L]^n}{[L]^n + K^n}. \quad (9)$$

The probability that the channel will remain open at the inactivating ligand concentration in the medium  $[L]$ :

$$P_o = \frac{K^n}{[L]^n + K^n}. \quad (10)$$

In a state of rest, the concentration of calcium in the cytoplasm is low [41]; it penetrates into cells from the environment during depolarization of the plasma membrane. On appearance of an external stimulus, in particular, during depolarization, the enzymes of the cascade of  $IP_3$  synthesis are activated, probably due to local penetration of calcium ions and activation of phospholipase C [57, 58]. When describing the  $IP_3$  dynamics, we relied on the works [44, 58] where it was described depending on the intensity of current through the plasma membrane in *Chara*. Based on the experimental data [59], in our model we also added a component to take into account the synthesis of  $IP_3$  in a state of rest, at the background level (the third summand in Eq. (11)):

$$\frac{d[IP_3]}{dt} = k_4 f(i) i - k_{-4} [IP_3] + J_{\text{synthesis}}, \quad (11)$$

where  $f(i) = 1 - \frac{i_0}{i}$  is the function describing the dependence of  $IP_3$  on the input current,  $i_0$  is the minimum current through the plasma membrane when  $IP_3$  synthesis begins,  $i$  is the input current through the plasma membrane, with  $\frac{i}{i_0} > 1$  for the induction of additional  $IP_3$  synthesis or  $\frac{i}{i_0} < 1$  for  $IP_3$  synthesis at the background level, and  $f(i) = 0$ ,  $k_4$  is the rate constant for  $IP_3$  synthesis,  $k_{-4}$  is the rate constant for  $IP_3$  de-

composition,  $J_{\text{synthesis}}$  is the rate of  $IP_3$  synthesis at the background level, with  $J_{\text{synthesis}} = k_{-4} [IP_3]_{\text{stat}}$ ,  $[IP_3]_{\text{stat}}$  is the background concentration level.

The primary active transport ( $H^+$ -ATPase and  $Ca^{2+}$ -ATPase) is described by using a model for the two states of the pump: with and without the ion. The model not only describes the dependence on ion gradients and the voltage across the membrane but also the effect of saturation. The stationary flows through ATPases [60]:

$$j_p = E_o \frac{k_{+1}k_{+2} - k_{-1}k_{-2}}{k_{+1} + k_{+2} + k_{-1} + k_{-2}}, \quad (12)$$

where  $E_o$  is the total ATPase concentration in the membrane,  $k_{+1}$  is the rate constant for ATPase binding with the ion at the inner side of the membrane,  $k_{-1}$  is the rate constant for disintegration of the ion-ATPase complex without ion transfer across the membrane,  $k_{+2}$  is the rate constant for disintegration of the ion-ATPase complex with ion transfer across the membrane,  $k_{-2}$  is the rate constant for ATPase binding with the ion at the outer side of the membrane. Indices (1) and (2) are used to denote the potential-independent and potential-dependent rate constants, respectively. The rate constants are described as follows [50, 61]:

$$k_{+1} = k_1 [I_1]_{in}, \quad k_{-1} = k_1 \exp\left(\frac{-\Delta G_{ATP}}{RT}\right),$$

$$k_{+2} = k_2 u \frac{1}{1 - \exp(-u)}, \quad (13.1)$$

$$k_{-2} = k_2 [I_1]_{out} u \frac{\exp(-u)}{1 - \exp(-u)},$$

$$k_{+1} = k_1 [I_1]_{in} [I_2]_{out}, \quad k_{-1} = k_1 \exp\left(\frac{-\Delta G_{ATP}}{RT}\right),$$

$$k_{+2} = k_2 u \frac{1}{1 - \exp(-u)}, \quad (13.2)$$

$$k_{-2} = k_2 [I_1]_{out} [I_2]_{in} u \frac{\exp(-u)}{1 - \exp(-u)},$$

where  $k_1$  and  $k_2$  are the rate constants at  $u = 0$ ,  $\Delta G_{ATP}$  is the energy of ATP hydrolysis, ATPases transfer one type of ions,  $[I_1]$ , (13.1) or, when functioning as antiporters, two types of ions,  $[I_1]$  and  $[I_2]$  (13.2).

Secondary active transport is described as a difference between the input and output ion flows. Its activity is determined by membrane potential but it is described by the modified Goldman-Hodgkin-Katz equation [50]. The ion transport via antiport and symport is described by Eq. (14.1) and Eq. (14.2), respectively:

$$j = \frac{Ezu}{1 - \exp(-zu)} \times \left( [A]_{in}^n [B]_{out}^m - [A]_{out}^n [B]_{in}^m \exp(-zu) \right), \quad (14.1)$$

$$j = \frac{Ezu}{1 - \exp(-zu)} \times ([A]_{\text{in}}^n [B]_{\text{in}}^m - [A]_{\text{out}}^n [B]_{\text{out}}^m \exp(-zu)), \quad (14.2)$$

where  $n$  and  $m$  are the numbers of transported ions A and B per working cycle of the transporter,  $E$  is the product of transporter concentration and rate constant at  $u = 0$  and 1 M concentration of the transported ions at both sides of the membrane.

The electrically neutral transport is described by the modified Fick's equation; the ion transport via antiport is described by Eq. (15) [50]:

$$j = E \left( [A]_{\text{in}} [B]_{\text{out}}^m - [A]_{\text{out}}^n [B]_{\text{in}}^m \right). \quad (15)$$

The regulation of active transport systems by ligands is described similar to the ion channels. The operating speed of active transport systems also depends on the ambient temperature. The  $Q_{10}$  coefficient is introduced to describe temperature sensitivity like in the previous work [50].

The competitive binding of apoplastic buffer with the  $\text{Ca}^{2+}$ ,  $\text{K}^+$ , and  $\text{H}^+$  ions is described by the Gradmann's model ([49], see Fig. 1 for the buffer scheme). At the same time, the dynamics of ion association/dissociation is described by the following equations:

$$\frac{d[r]}{dt} = k_{-r} ([r_{\Sigma}] - [r]) - k_{+r} ([B_{\Sigma}] - [Ca_{\Sigma}] - [K_{\Sigma}] - [H_{\Sigma}] + [Ca] + [K] + [H])[r], \quad (16)$$

where  $r$  is one of the ions that can be bound by the buffer ( $\text{Ca}^{2+}$ ,  $\text{K}^+$ , or  $\text{H}^+$ ),  $[r]$  and  $[r_{\Sigma}]$  are its free and total concentrations, respectively,  $k_{-r}$  and  $k_{+r}$  are the rate constants for dissociation and association of the  $r$  ion and buffer complex with the total concentration  $[B_{\Sigma}]$ , respectively,  $[K_{\Sigma}]$  is the total potassium concentration,  $[H_{\Sigma}]$  is the total proton concentration,  $[Ca_{\Sigma}]$  is the total calcium concentration. For calcium, a simplification has been made: one charged group of the apoplast binds one calcium ion.

The curves of pH dependence on the total  $[\text{H}^+]$  concentration in the cytoplasm and in the vacuolar contents have been plotted on the basis of experimental data [62] and are described by the following equation:

$$dpH = \frac{d[\text{H}^+]}{C}, \quad (17)$$

where  $C$  is the buffer capacity,  $dpH$  is the pH change after the entry/release of protons.

Calmodulin, being a calcium buffer, plays a key role in maintaining cytoplasmic free calcium [63]. Calmodulin has two ends, each of them successively binding two calcium ions [64]. The dependence of free calcium concentration ( $[\text{Ca}^{2+}]$ ) on its total concentration (bound + free,  $[Ca_{\Sigma}]$ ) was revealed on the basis of the model proposed in [64]. To simplify the solution, such dependence is described by regression Eq. (18) (the coefficient of determination, 0.999), which is further used to describe the buffer properties of the cytoplasm for calcium:

$$[\text{Ca}^{2+}] = 0.2425[Ca_{\Sigma}]^{0.862}, \quad (18)$$

where coefficient 0.2425 and degree 0.862 were obtained with approximation. In Eq. (18) calcium concentration is expressed in  $\mu\text{mol}$ .

The vacuole has a high calcium concentration [41] and strong buffer properties determined by the high content of compounds capable of binding  $\text{Ca}^{2+}$ , including malates, phosphates, chlorides, carbonates and nitrates, as well as the vacuolar  $\text{Ca}^{2+}$ -binding proteins [65–67]. Therefore, it is assumed that the concentration of calcium ions in the vacuole is constant.

The model was solved numerically by the Euler's method. The parameters and initial conditions for equations of the model were obtained on the basis of the published data (Table 1).

## RESULTS AND DISCUSSION

At the first step of the research, the model was verified by simulating AP generation in response to cooling. The results (Fig. 2, Table 2) show that the simulated signal is in good agreement with experimental responses, in particular, has the basic properties of AP [86–88]: the threshold potential ( $E_{\text{m threshold}}$ ) and temperature threshold ( $T_{\text{threshold}}$ ), above which the AP develops according to the all-or-none principle, depolarization and subsequent repolarization, etc. Thus, the model showed a good correspondence with experimental data and can be used for further analysis.

It is known that the volume and area of the vacuole are highly variable and can change depending on the functional state of a cell [39, 40]. Hereinafter, we investigated the effects of these parameters on the ability of cells to generate electrical response.

The influence of vacuole volume on AP generation by plant cells was studied assuming that the vacuole has a constant area to volume ratio and a spherical shape. The signals simulated by the model are pre-

**Table 1.** Parameters of transport and buffer systems and initial conditions for numerical solution of the mathematical model

Plasmalemma			Tonoplast		
parameter	value	reference	parameter	value	reference
Cl <sub>Ca</sub> channels			FV channels		
$P_{\max}c_{\text{chan}}$	$1 \times 10^{-6} \text{ M cm s}^{-1}$	Accepted	$P_{\max}c_{\text{chan}}$	$1 \times 10^{-7} \text{ M cm s}^{-1}$	[74]
$c_o$	3.1	[68]	$c_o$	0.55	
$u_o$	-4.91	[68]	$u_o$	-2.72	
$\gamma$	0.054 M	[69]	$\gamma$	0.27 M	
$K$	$8 \times 10^{-6} \text{ M}$	[50]	$K$	$6.3 \times 10^{-6} \text{ M}$	
$n$	2	[70]	$n$	0.7	
K <sub>out</sub> channels			VK (TPK1) channels		
$P_{\max}c_{\text{chan}}$	$1.21 \times 10^{-6} \text{ M cm s}^{-1}$	Accepted	$P_{\max}c_{\text{chan}}$	$2 \times 10^{-6} \text{ M cm s}^{-1}$	[75]
$c_o$	1.13	[50]	$p_o$	0.6	
$u_o$	-2.53	[50]	$\gamma$	3.1 M	
$k_o$	$0.5 \text{ s}^{-1}$	[50]	$K$	$7.5 \times 10^{-6} \text{ M}$	
$\gamma$	$3.5 \times 10^{-3} \text{ M}$	Accepted	$n$	1	
K <sub>in</sub> channels			Ca <sub>IP3</sub> channels		
$P_{\max}c_{\text{chan}}$	$1.21 \times 10^{-6} \text{ M cm s}^{-1}$	[53]	$P_{\max}c_{\text{chan}}$	$7 \times 10^{-9} \text{ M cm s}^{-1}$	[76]
$c_o$	2.7	[71]	$\gamma$	0.4 M	
$u_o$	-6.39	[71]	$K$	$2.2 \times 10^{-7} \text{ M}$	
$\gamma$	$3.5 \times 10^{-3} \text{ M}$	[53]	$n$	1	
Ca <sub>v</sub> channels			Cl <sub>Ca</sub> channels		
$P_{\max}c_{\text{chan}}$	$2.5 \times 10^{-10} \text{ M cm s}^{-1}$	[72]	$P_{\max}c_{\text{chan}}$	$1 \times 10^{-6} \text{ M cm s}^{-1}$	[77]
$c_o$	1.15	[50]	$c_o$	2	[78]
$u_o$	-3.51	[50]	$u_o$	-1.68	[78]
$c_i$	1.28	[50]	$\gamma$	0.00144 M	[77]
$u_i$	-7.01	[50]	$K$	$1 \times 10^{-6} \text{ M}$	[72]
$\gamma$	$9.9 \times 10^{-5} \text{ M}$	[54]	$n$	1	[72]
K <sup>+</sup> /H <sup>+</sup> antiport			K <sup>+</sup> /H <sup>+</sup> antiport		
$V_K$	$0.015 \text{ M}^{-1} \text{ s}^{-1}$	[50]	$V_K$	$2.23 \times 10^{-3} \text{ M}^{-1} \text{ s}^{-1}$	Accepted
2H <sup>+</sup> /Cl <sup>-</sup> symport			H <sup>+</sup> /2Cl <sup>-</sup> antiport		
$V_{Cl}$	$3.12 \text{ M}^{-2} \text{ s}^{-1}$	Accepted	$V_{Cl}$	$0.028 \text{ M}^{-3} \text{ s}^{-1}$	[72]
H <sup>+</sup> -ATPase			Ca <sup>2+</sup> /3H <sup>+</sup> antiport		
$E_0$	0.15 M	Accepted	$V_{Ca}$	$9.4 \times 10^{10} \text{ M}^{-4} \text{ s}^{-1}$	[72]
$k_1$	$0.45 \text{ s}^{-1}$	[50]	$K$	$1.5 \times 10^{-5} \text{ M}$	
$k_2$	$2.58 \times 10^{-4} \text{ s}^{-1}$	[50]	$n$	1	
$K$	$4 \times 10^{-7} \text{ M}$	[50, 73]	H <sup>+</sup> -ATPase		
$n$	2	[73]	$E_0$	0.25 M	[72]
Stoichiometry	1H <sup>+</sup> :1 ATP	[72]	$k_1$	$850000 \text{ s}^{-1}$	[79]
			$k_2$	$0.09 \text{ s}^{-1}$	[79]
			Stoichiometry	2 H <sup>+</sup> :1 ATP	[80]

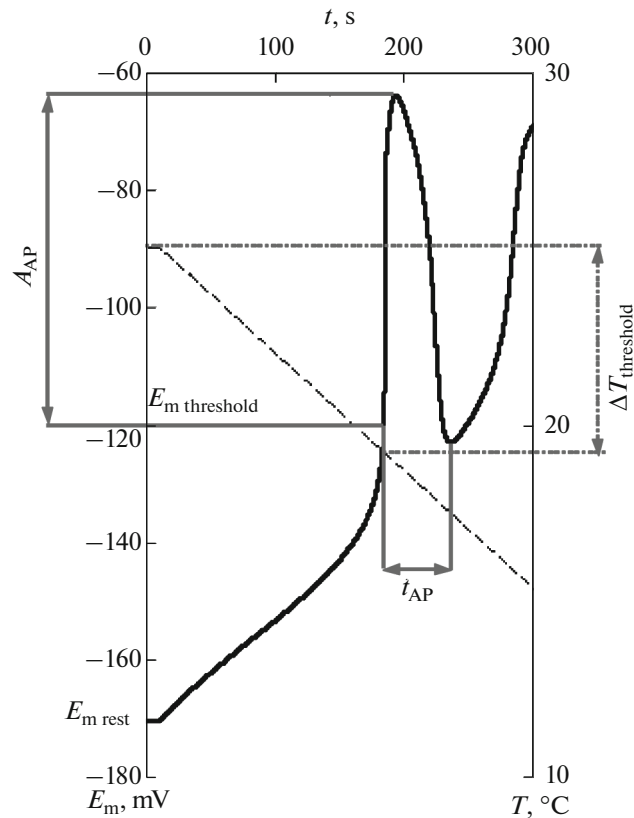
**Table 1.** (Contd.)

Plasmalemma			Tonoplast		
parameter	value	reference	parameter	value	reference
Ca <sup>2+</sup> -ATPase			Ca <sup>2+</sup> -ATPase		
$E_0$	3.23 M	Accepted	$E_0$	0.0083 M	[72]
$k_1$	45 s <sup>-1</sup>	[50]	$k_1$	0.12 s <sup>-1</sup>	[72]
$k_2$	2.58 × 10 <sup>-5</sup> s <sup>-1</sup>	[50]	$k_2$	2.92 × 10 <sup>-7</sup> s <sup>-1</sup>	[72, 81]
$K$	5 × 10 <sup>-7</sup> M	[72]	$K$	7 × 10 <sup>-6</sup> M	[81]
$n$	2	[72]	$n$	1	[38, 82]
Stoichiometry	1Ca <sup>2+</sup> , 1H <sup>+</sup> :1 ATP	[50]	Stoichiometry	1Ca <sup>2+</sup> :1 ATP	[82]
Cell characteristics					
$C$	10 <sup>-6</sup> F sm <sup>-2</sup>	[35]	$Q_{10}$	3	[50]
$E_m$ (plasma membrane)	-170 mV	[5]	$E_m$ (tonoplast)	-40 mV	[5]
$S_{\text{cell}}/V_{\text{cell}}$	10 <sup>4</sup> cm <sup>-1</sup>	[50]	$R_{\text{cell}}$	0.0003 cm	[50]
$V_{\text{ap}}/V_{\text{cell}}$	0.1	[49]	$V_{\text{vac}}/V_{\text{cell}}$	0.5–0.8	[72, 82]
$k_4$	21.5 M <sup>-1</sup> cells <sup>-1</sup>	[44]	$k_{-4}$	0.2 s <sup>-1</sup>	[44]
$i_0$	1 × 10 <sup>-6</sup> A	Accepted	[IP <sub>3</sub> ] <sub>stat</sub>	4.76 × 10 <sup>-8</sup> M	[59]
Initial ion concentrations and buffer properties					
	Apoplast		Cytoplasm		Vacuole
[K <sup>+</sup> ] <sub>0</sub>	3.5 × 10 <sup>-3</sup> M [50]		0.16 M [5, 50]		0.67 M [84]
[Cl <sup>-</sup> ] <sub>0</sub>	2.7 × 10 <sup>-3</sup> M [50]		0.02 [5]		0.07 M [72]
[Ca <sup>2+</sup> ] <sub>0</sub>	3.3 × 10 <sup>-4</sup> M [41]		10 <sup>-7</sup> M [74]		5 × 10 <sup>-3</sup> M [41], accepted as a constant
pH <sub>0</sub>	6.0 [50]		7.2 [83]		5.8 [85]
	[K <sub>Σ</sub> ] <sub>0</sub> = 0.188 M, [H <sub>Σ</sub> ] <sub>0</sub> = 0.0089 M, [Ca <sub>Σ</sub> ] <sub>0</sub> = 0.002 M (accepted) [B] = 0.2 M, K <sub>H</sub> = 10 <sup>-6</sup> M, K <sub>Ca</sub> = 10 <sup>-3</sup> M, K <sub>K</sub> = 10 <sup>-4</sup> M [50]		C <sub>cyt</sub> = 0.02825 M pH <sup>-1</sup> [62] [Ca <sub>Σ</sub> ] <sub>0</sub> = 3.6 × 10 <sup>-7</sup> M (accepted on the basis of Eq. (18) and [Ca <sup>2+</sup> ] <sub>0</sub> = 10 <sup>-7</sup> M)		C <sub>vac</sub> = 0.02874 M pH <sup>-1</sup> [62]

sented in Figure 3. It has been shown that the amplitude of AP and value of the maximum change in ionized calcium ( $\Delta[\text{Ca}^{2+}]$ ) concentration decrease to certain values as the relative volume of the vacuole increases and hereafter change insignificantly (Figs. 4a, 4b). It can be accounted for by the fact that the increase in vacuole volume and area leads to an increase in the number of Ca<sup>2+</sup>-ATPases and Ca<sup>2+</sup>/3H<sup>+</sup> antiporters activated by Ca<sup>2+</sup>, which enhances its transport into the vacuole. As a consequence, more substantial cooling is needed to reach the threshold [Ca<sup>2+</sup>] value that triggers AP. This mechanism is confirmed by the higher tempera-

ture threshold as a result of increase in the vacuole volume (Fig. 4c).

During AP, only a slight electrical response (below 10 mV) including depolarization followed by hyperpolarization is observed on the tonoplast, and the threshold of response generation and slowdown increases along with the increase in vacuole volume (Fig. 3b). According to the data obtained for Chara [34, 35], both depolarization and hyperpolarization can be observed on the tonoplast depending on the cytoplasmic to vacuolar ion content ratio. The responses are characterized by large amplitudes (tens of millivolts) and are apparently determined by the Ca<sup>2+</sup>, Cl<sup>-</sup>, and



**Fig. 2.** Action potential simulated by the model. *Black solid line* shows a change in the potential on the plasma membrane during AP; *black dashed line* shows a temperature change.  $A_{AP}$ , AP amplitude;  $t_{AP}$ , AP duration;  $E_{m\ rest}$ , resting potential;  $E_{m\ threshold}$ , threshold potential, at which AP generation begins;  $\Delta T_{threshold}$ , temperature change necessary for the AP induction. The potential difference across the plasma membrane was calculated at the value of electric potential in the apoplast set to zero.

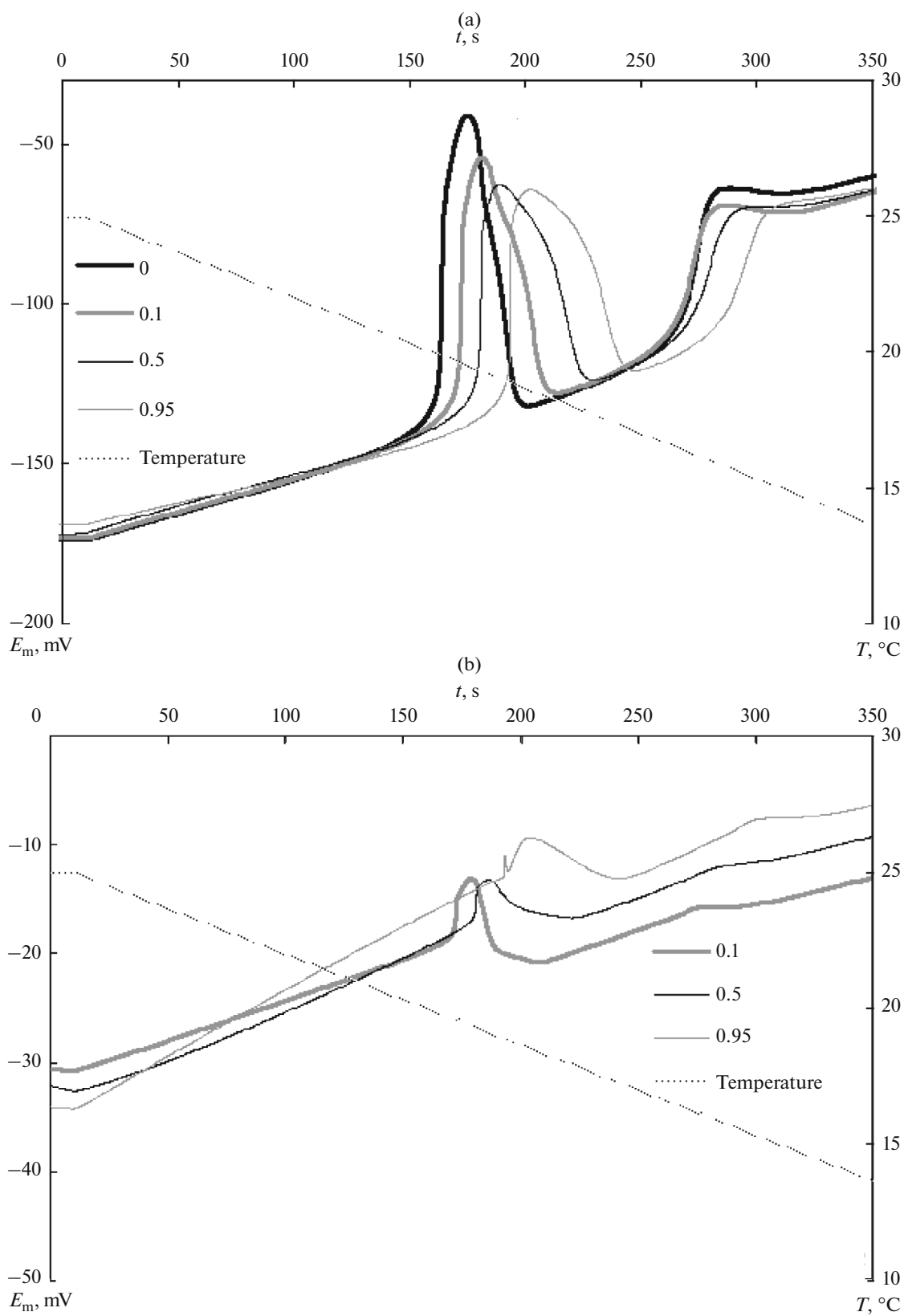
$K^+$  flows [34]. It may be supposed that the mechanism of electrical response on the tonoplast in higher plants is also associated with the  $Ca^{2+}$  flow activating the potassium and chloride channels of the vacuole. At the same time, the low magnitude of response in higher plants is probably accounted for by their specific vacuolar to cytoplasmic ion ratios. The essential role of  $Ca^{2+}$  in the formation of response on the tonoplast is also confirmed by the slowdown of its development at a decrease in the calcium spike.

The vacuole has a variable shape [39, 40] and, hence, the total area of the tonoplast within a cell can change irrespective of the total volume. Hence, we have analyzed the effect of the area of the vacuole on AP generation with its unchanged relative volume taken equal to 0.7 (Fig. 5). In this case, the increase in vacuole area is accompanied by a decrease in the amplitude of electrical response on the plasma membrane and the tonoplast and  $\Delta[Ca^{2+}]$  until disappearance, as well as by an increase in the temperature

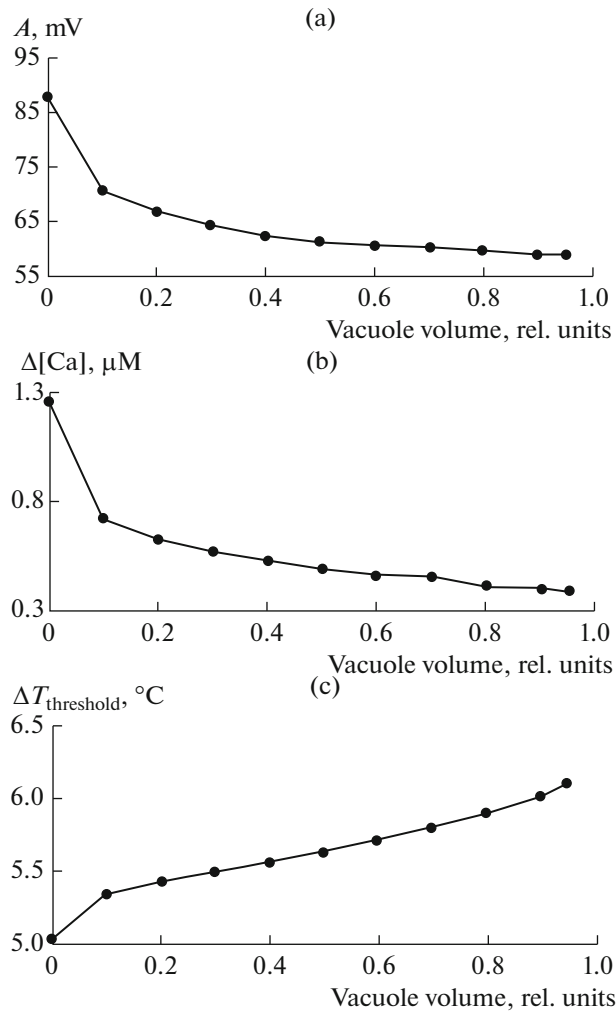
**Table 2.** Comparison of the main characteristics of action potential on the plasmalemma simulated by the model and obtained experimentally

AP characteristic	Signal simulated by the model	Experimental data
$A_{AP}$ , mV	70	40–120 [31, 33, 87, 88]
$t_{AP}$ , s	52	11–285 [25, 31, 33]
$\Delta T_{threshold}$ , °C	5.8	3.8–8.8 [87, 89]
$E_{m\ rest}$ (plasmalemma), mV	–170	–190...–140 [25, 33]
$E_{m\ threshold}$ (plasmalemma), mV	–120	–120 [25]
Maximum rate of repolarization, $mV\ s^{-1}$	3.5	0.5–3.7 [33]





**Fig. 3.** Action potentials simulated by the model with varying relative volumes of the vacuole: (a) signal developing on the plasma membrane; (b) signal developing on the tonoplast. Values of the relative volume are presented in the captions to the lines; zero value corresponds to the AP simulated by the model without vacuole. The potential difference across the plasma membrane was calculated at the value of electric potential in the apoplast set to zero; for calculations of the potential difference on the tonoplast, the potential within the vacuole was set to zero.



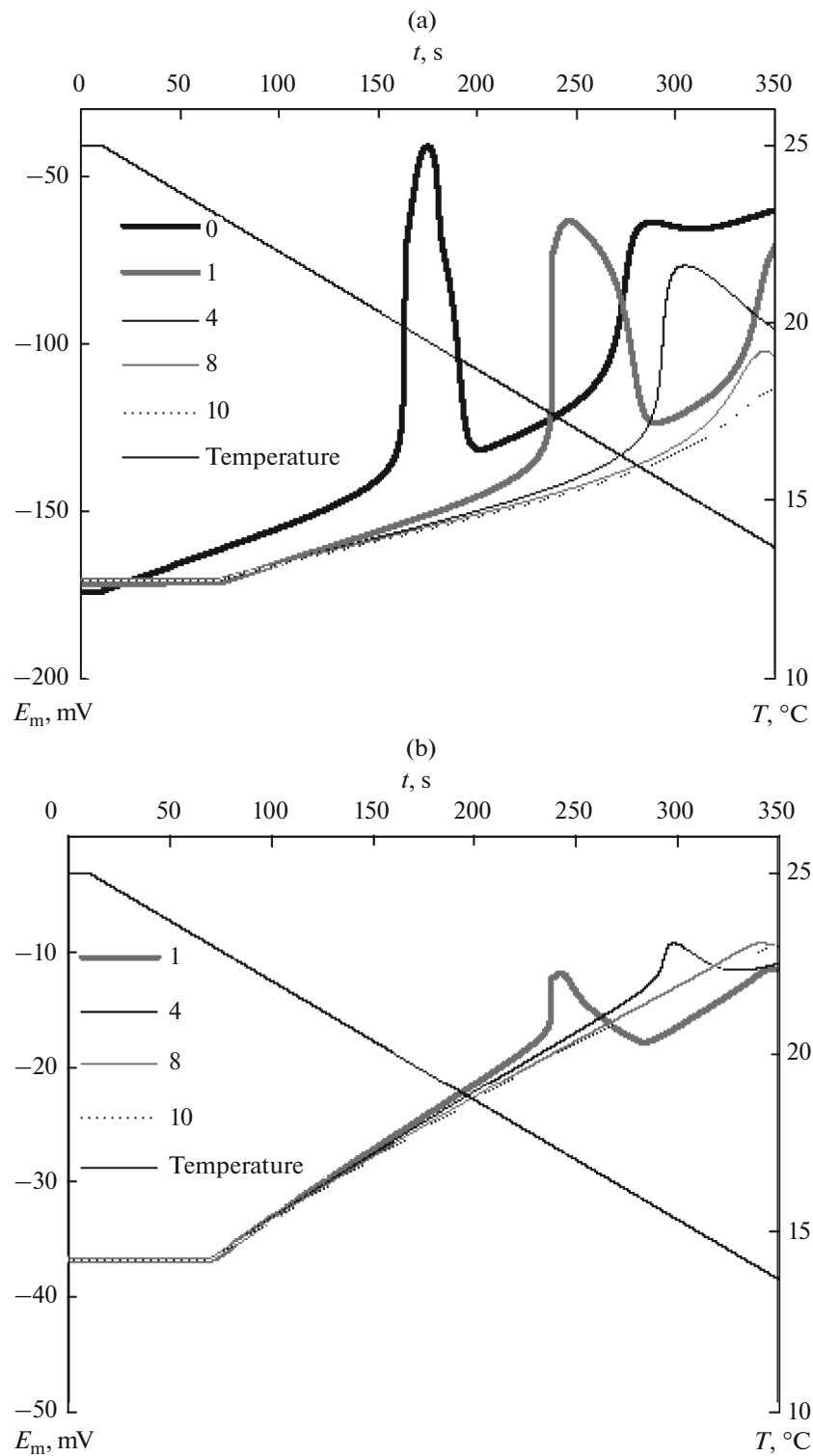
**Fig. 4.** The influence of the vacuole volume on the parameters of action potential and  $\text{Ca}^{2+}$  spike. (a) Dependence of the AP amplitude on the relative volume of vacuole; (b) dependence of the calcium signal amplitude on the relative volume of the vacuole; (c) dependence of the temperature threshold of the AP generation on the vacuole relative volume.

threshold (Fig. 6). Like in case of increasing vacuole volume, the mechanism of signal attenuation with increasing area is probably associated with the increased number of  $\text{Ca}^{2+}$ -ATPases and  $\text{Ca}^{2+}/3\text{H}^{+}$  antiporters in the cell. The similarity of mechanisms is confirmed by the similar curves of the AP amplitude dependence on  $\Delta[\text{Ca}^{2+}]$  with increasing area or volume (Fig. 7).

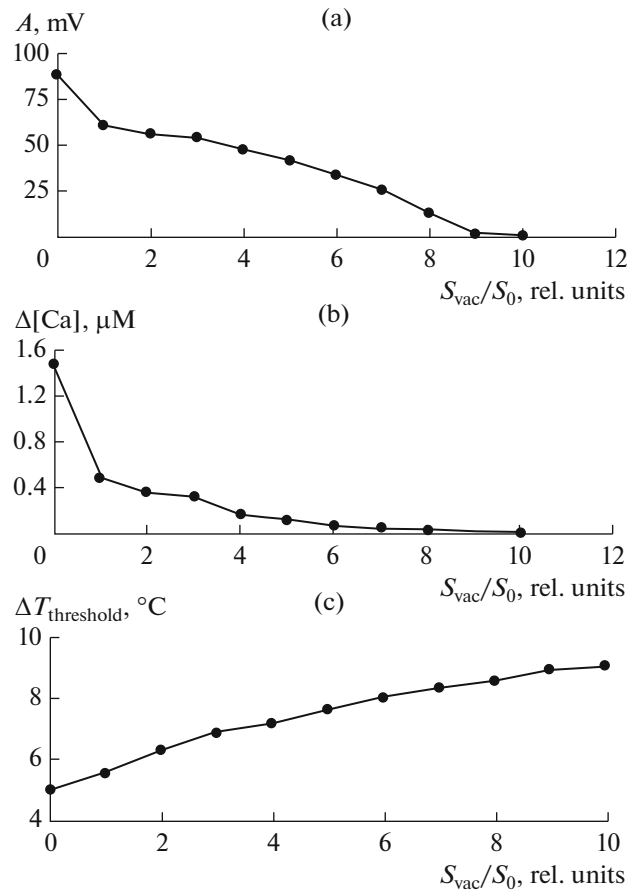
In addition to geometric characteristics, AP can be potentially influenced by the concentrations of vacuolar ions forming the potential. In particular, it is known that potassium and chloride concentrations may vary within a very broad range [72]. Hence, we investigated the effects of different initial concentrations of vacuolar potassium and chloride on the development of electric reactions during cell cooling (Fig. 8). As Figure 8a shows, the decrease in the initial concentration of vacuolar potassium does not lead to substantial changes in AP characteristics but only a slight

decrease in response generation threshold. At the same time, a more negative resting potential is set on the tonoplast (Fig. 8b), probably due to the negative shift in potassium equilibrium potential when the content of potassium in the vacuole decreases. It also increases the thresholds for the development of electrical response on the tonoplast. When the initial chloride concentration in the vacuole is changed, the differences in AP are actually absent (Fig. 8c). The increase in the initial chloride concentration leads to a slight hyperpolarization of the tonoplast (Fig. 8d) and insignificant increase in the thresholds for electrical response development on the tonoplast. Thus, the change in the initial vacuolar content of potassium and chloride has a weak effect on the development of electrical responses during cell cooling.

Since the vacuole can be a source of calcium under the conditions of electrical response development [35, 41], hereinafter we analyzed the role of  $\text{IP}_3$ -sensitive

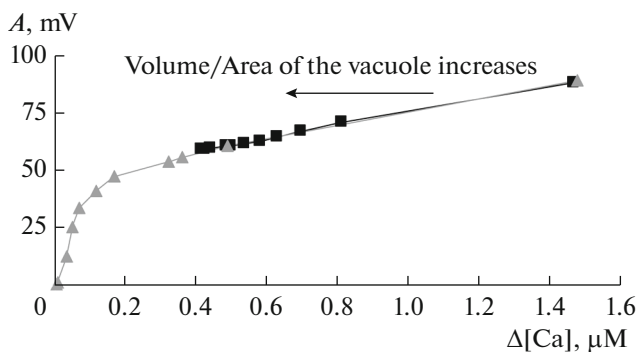


**Fig. 5.** Action potential simulated by the model with varying area and constant volume of the vacuole (0.7): (a) the signal developing on the plasma membrane; (b) the signal developing on the tonoplast. Zero value corresponds to the AP simulated by the model without the vacuole; value 1 corresponds to the AP used for verification of the model; other values demonstrate multiple increases in the area compared to its value for the variant used for verification. The potential difference across the plasma membrane was calculated at the value of electric potential in the apoplast set to zero; the potential difference on the tonoplast was calculated at the value of potential within the vacuole set to zero.



**Fig. 6.** The influence of the vacuole area on the parameters of action potential and  $Ca^{2+}$  spike. (a) Dependence of the AP amplitude on the relative area of the vacuole ( $S_{vac}/S_0$ ); (b) dependence of the calcium signal amplitude on  $S_{vac}/S_0$ ; (c) dependence of the temperature threshold of the AP generation on  $S_{vac}/S_0$ .

vacuolar  $Ca^{2+}$  channels in the formation of  $Ca^{2+}$  spike during AP. The model simulates the increase in the  $Ca^{2+}$  flow through these channels in the depolarization phase and its decrease to a certain minimal stationary value in the repolarization phase (Fig. 9a). The

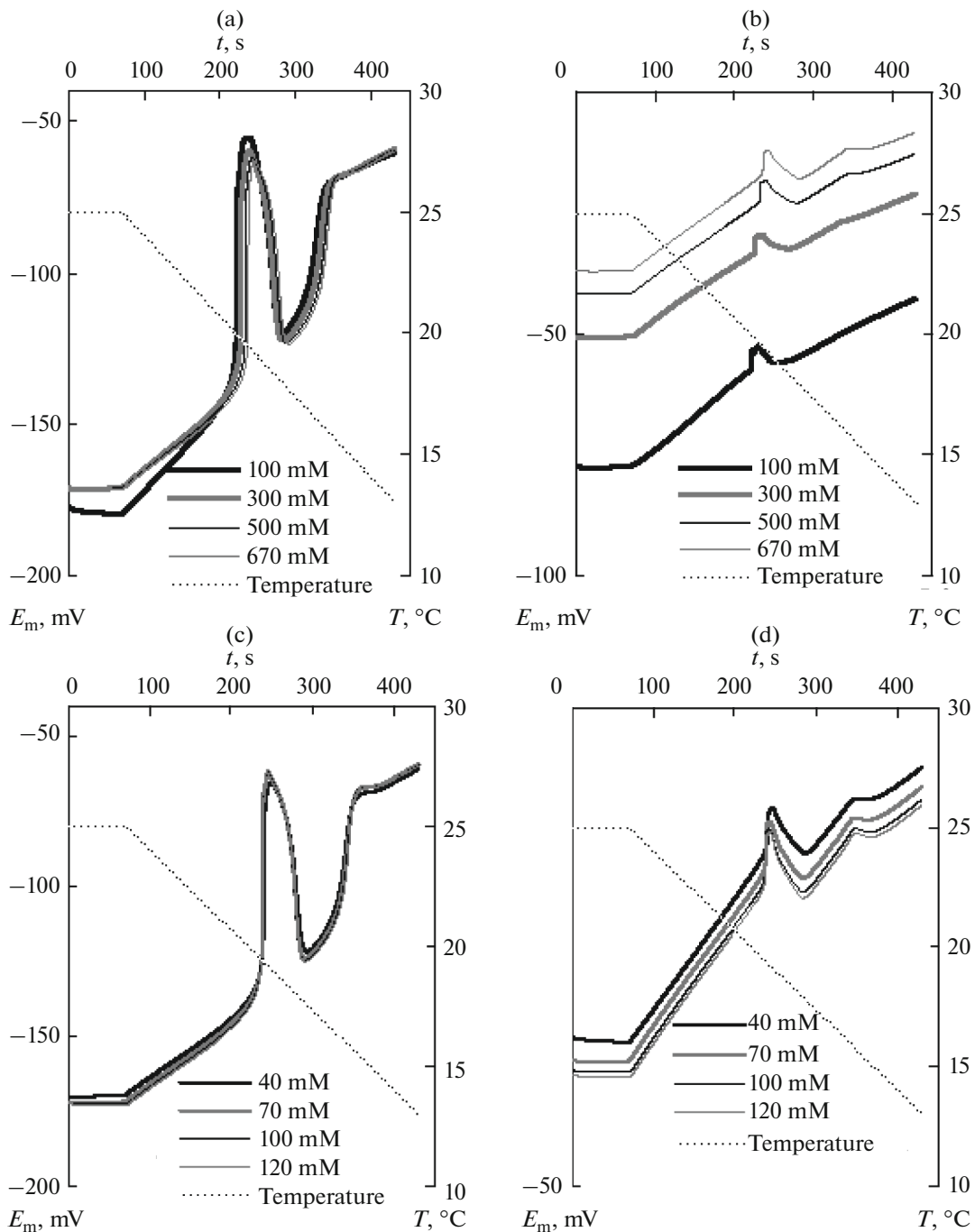


**Fig. 7.** Dependence of the action potential amplitude on calcium peak amplitude with increasing vacuole relative volume (*black*) and with increasing vacuole area at a constant volume (*gray*). Respective values were taken from Figs. 4 and 6.

cells having all transport systems of the plasma membrane and the vacuole were used as a control; the current through  $IP_3$  receptors was only background and did not change after excitation (Fig. 9b). With the inclusion of a component dependent on the value of depolarization current through the plasma membrane, the  $Ca^{2+}$  peak in the cytoplasm increases; however, this increase is small compared to the control: about 30% of the control (Fig. 9c). At the same time, the parameters of AP with  $IP_3$  involved in the regulation of calcium concentration are not substantially different from the parameters without  $IP_3$  (Fig. 9b).

Thus, the vacuole most likely does not make any considerable contribution to the  $Ca^{2+}$  spike formation during AP in the higher plants, at least, when using the permeability values for  $IP_3$  receptors obtained in the experiments with sugar beet [76]. However, it cannot be excluded that they have different permeability to other objects; at a higher permeability of  $IP_3$  receptors, the contribution of the vacuole may be more significant.

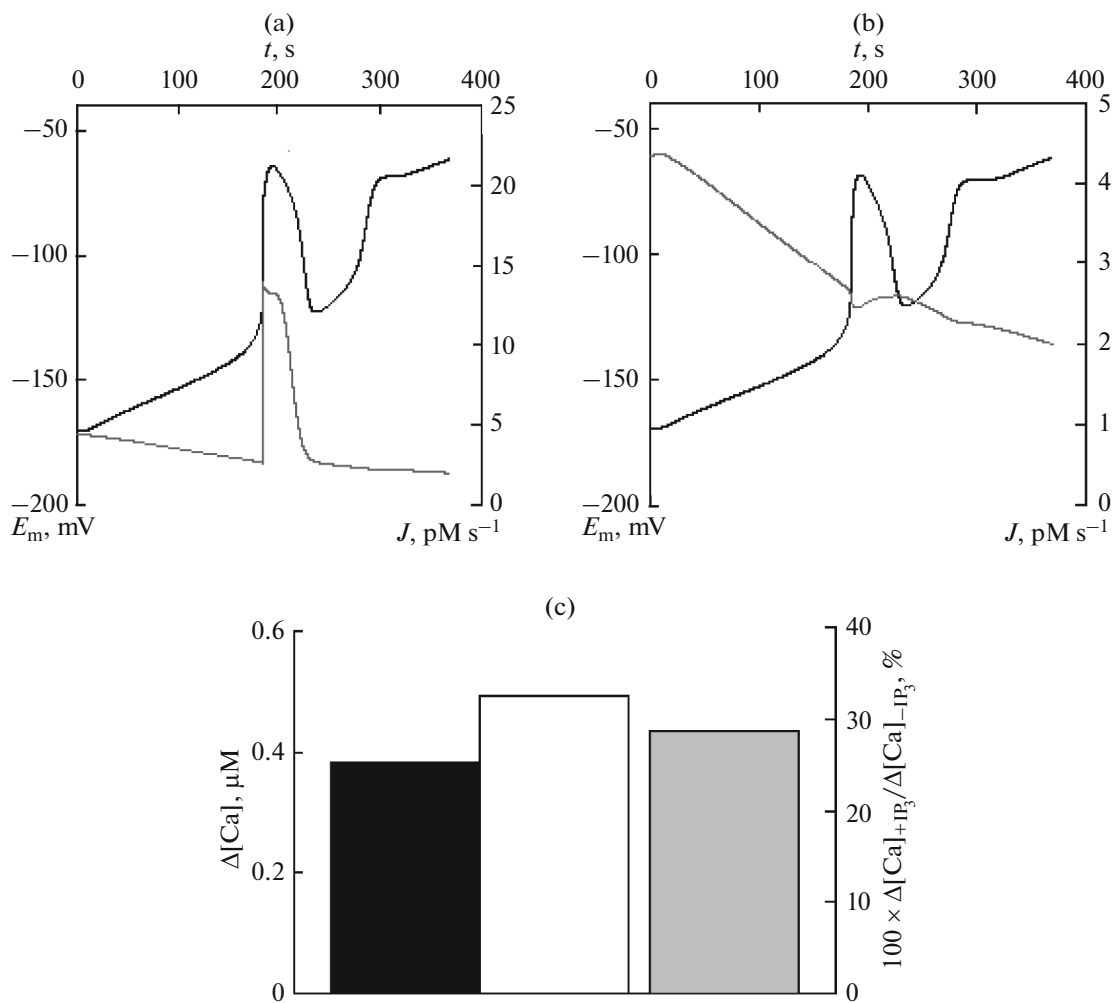
The theoretical analysis of the role of vacuole in the mechanism of AP generation demonstrates its poten-



**Fig. 8.** The influence of the initial concentrations of potassium and chloride ions in the vacuole on the development of electrical responses on the plasma membrane and the tonoplast. The cooling-induced change in potential (a) on the plasma membrane and the tonoplast (b) at different initial potassium concentrations in the vacuole. The cooling-induced change in potential (c) on the plasma membrane and the tonoplast (d) at different initial chloride concentrations in the vacuole. The concentrations are given in the legends. The potential difference across the plasma membrane was calculated at the value of electric potential in the apoplast set to zero; for calculations of the potential difference on the tonoplast, the potential within the vacuole was set to zero.

tial involvement in the regulation of electrical response value with the changing vacuolar area and volume. The concentrations of potassium and chloride ions in the vacuole weakly influence the action potential; the contribution of  $IP_3$ -sensitive  $Ca^{2+}$  channels to the calcium spike formation during AP is minor too. The

result shows that the role of vacuole in AP formation in the higher plants is associated with the consumption of calcium entering the cell by the active transport systems of the tonoplast rather than with  $Ca^{2+}$  release from the vacuole through the channels during AP generation. Thus, one of the functions of the vacuole is probably to



**Fig. 9.** The involvement of IP<sub>3</sub>-sensitive Ca<sup>2+</sup> channels in the generation of AP and Ca<sup>2+</sup> spike. (a) Ca<sup>2+</sup> flow through the IP<sub>3</sub>-dependent Ca<sup>2+</sup> channels and membrane potential changes during AP; (b) Ca<sup>2+</sup> flow through the IP<sub>3</sub>-dependent Ca<sup>2+</sup> channels and the change in membrane potential during AP in the absence of the IP<sub>3</sub> content changes; (c) absolute values of calcium spike during AP with varied (*white column*) and unchanged (*black column*) content of IP<sub>3</sub>, as well as relative contributions of the IP<sub>3</sub>-dependent Ca<sup>2+</sup> channels to the calcium spike generation during AP (*gray column*).

maintain the relatively low concentration of calcium ions in the cytoplasm under excitation. In general, the analysis shows the importance of changes in the parameters of the vacuole for AP modulation in different plant tissues and organs, which may be significant for response in general. The results can explain, in particular, the age-related change in cell excitability [5, 90] probably associated with the changes in vacuole area and shape during plant growth and development.

#### ACKNOWLEDGMENTS

The work was supported by the Russian Science Foundation (project no. 14-26-00098).

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Translated by E.V. Makeeva