# **ELECTRONIC PROPERTIES OF SEMICONDUCTORS**

# **Localization of the Interband Transitions in the Bulk of the Brillouin Zone of III–V Compound Crystals**

**V. V. Sobolev\* and D. A. Perevoshchikov**

*Udmurt State University, Izhevsk, 426034 Russia \*e-mail: sobolev@uni.udm.ru* Submitted September 17, 2015; accepted for publication October 14, 2015

**Abstract**—The localization of the transitions in the bulk of the Brillouin zone that form the main structures in the spectra of the imaginary part of the permittivity in the range up to  $\sim$  7 eV for III–V semiconductors (AlSb, GaSb, InSb, and InAs) is determined using electron density functional theory. It is established that intense transitions occur not only in the vicinity of the high-symmetry axes of the Brillouin zone, but also in some specific large volumes of the irreducible part of the Brillouin zone.

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### 1. INTRODUCTION

III–V Semiconductors are widely used for the fabrication of various optoelectronic devices [1]. Therefore, its electronic structure has been investigated in many experimental and theoretical studies  $[2-29]$ . The theoretical curves of the imaginary part of the permittivity  $\varepsilon_2(E)$  [8–21] in the range to ~7 eV include three maxima  $(E_1, E_2, \text{ and } E_1)$  and a wide step  $E_0$ <sup>'</sup> between  $E_1$  and  $E_2$ . In rare cases [9, 11, 13, 14, 18, 20], a poorly pronounced structure is observed between *E*<sup>2</sup> and  $E_1$ , which has no commonly accepted notation and hereinafter is denoted as *Ex*.  $E_1^{'}$ 

The characteristic feature of these studies is that the  $\varepsilon_2(E)$  spectral maxima are caused by transitions at high-symmetry points Γ, *L*, *X*, and *K* of the Brillouin zone (BZ) and along three axes  $\Lambda$  ( $\Gamma - L$ ),  $\Delta$  ( $\Gamma - X$ ), and  $\Sigma(\Gamma - K)$ ; the irreducible part of the BZ is shown in Fig. 1. Hereinafter, the coordinates of all points in reciprocal space are given in the units  $2\pi/a_0$ , where  $a_0$ is the crystal-lattice parameter, and the system of coordinates is chosen such that the coordinates of the BZ high-symmetry points acquire the values  $(0, 0, 0)$ for Γ, (0.5, 0.5, 0.5) for *L*, (1, 0, 0) for *X*, (0.75, 0.75, 0) for *K*, (1, 0.25, 0.25) for *U*, and (1, 0.5, 0) for *W*.

The maximum  $E_1$  with the longest wavelength is formed by transitions from the two upper valence bands (UVBs)  $V_1$  and  $V_2$  to the lower conduction band (LCB)  $C_1$  at the  $\Lambda$  axis. It is located in the portion from the point  $(0.15, 0.15, 0.15)$  to L, depending on the crystal and calculation technique [8–13, 18] or only in the immediate vicinity of point *L* [17, 19, 21]. The maximum  $E_2$  is formed mainly by transitions between the UVB and LCB [8–14]. The most intense transitions occur in the vicinity of the  $\Sigma$  axis from the point (0.45, 0.45, 0) to the point  $K[8, 10-12]$ , as well as along the Δ axis [8, 9, 11, 17, 19, 21], especially near the point *X*  $[8, 9, 17, 21]$ . The existence of the third maximum  $E_1$ <sup>'</sup> is attributed to transitions from the bands  $V_1$  and  $V_2$  to  $C_2$  located at the point  $L$  [9, 10, 13, 21] and its vicinity to the point (0.375, 0.375, 0.375) [11, 12] and on the  $\Delta$  axis [11]. The existence of the small structure  $E_x$  is related to transitions from the UVB to the second LCB  $(C_2)$  that occur in the bulk of the BZ near the points from ~(0.5, 0.0, 0.0) to ~(0.7, 0.0, 0.0) on the  $\Delta$  axis [9, 11, 13, 14]. The step  $E_0^{\prime}$  is formed with the involvement



**Fig. 1.** Irreducible part of the Brillouin zone and schematic arrangement of the  $\Gamma_1 L_1 U_1 X_1$  and  $\Gamma_2 L_2 U_2 X_2$  planes and the points  $B_1$ ,  $B_2$ , and  $B_3$ .

of transitions from two UVBs: in the LCB in the portion of the  $\Delta$  axis from (0.5, 0.0, 0.0) to (0.7, 0.0, 0.0) [9, 11, 12, 18] and the second LCB in the vicinity of the BZ center [8, 9, 11, 13, 17, 18].

In addition, in [9, 10, 13, 18], quantitative schemes of the more complex localization of the transitions and their positioning in a wide range of **k** points were suggested. The largest differences in the schemes of localization of the transition structures occur in the case of the main maximum  $E_2$ . In particular, the decisive role in the formation of  $E_2$  is played by the  $X-U$  axis and its vicinity [9], the  $\Delta$ , *W–K*, and *L–W* axes [18], the vicinity of the point *K* and the  $L-U$  axis of triangular shapes at the Γ*LK* and Γ*LUX* faces of the irreducible part of the BZ [10], and the vicinity of the point (0.75, 0.25, 0.25) at  $\Gamma LUX$  [13]. The bands  $E_x$  and  $E_1$  in [18] are formed by transitions from  $V_1$  and  $V_2$  to  $C_2$  along the  $\Delta$ ,  $X-W$ , and  $L-W$  axes.  $E_1^{'}$ 

Thus, in all these calculations, the localization of the transition bands of four III–V crystals was investigated using only the general schemes of isoenergetic surfaces with very approximate indication of the region of their positioning in the BZ. It is commonly accepted that the role of a BZ region in the formation of  $\varepsilon_2(E)$  spectral structures is a nontrivial problem; the data of different calculations are noticeably different and contradictory.

The optical spectra of the III–V crystals in a wide energy range were experimentally investigated in many studies [2–6, 24–27]. The permittivity spectra were obtained using ellipsometry techniques mainly in the range of 1.5–6.5 eV at temperatures of  $T = 10$  K for GaSb [25], 22 K for InAs [27], 100 K for InSb [26], and 300 K for AlSb [24]. In all these spectra, one can clearly see the long-wavelength maximum  $E_1$  at (2.4  $\pm$ 0.45) eV, the main maximum  $E_2$  at (4.27  $\pm$  0.27) eV, and the poorly pronounced maximum  $E_1$  at higher energies. In addition, on both sides of the main maximum, there are structures  $E'_0$  and  $E_x$  with a lower intensity.  $E_1^{'}$ 

In [3, 5–7], III–V crystals were investigated in the region of the long-wavelength absorption edge at liquid-helium temperatures. This allowed their UVB and LCB in the vicinity of the point  $\Gamma$  to be investigated and the band gaps to be determined with high accuracy: GaSb, InSb, and InAs are direct-gap semiconductors with direct band gaps  $E_{gd}^e(\Gamma) = 0.811, 0.23$ , and 0.418 eV, respectively (the index *e* indicates experimental values). The AlSb UVB maximum is located at the center of the BZ, the LCB minimum, at the point *X*, and the corresponding value of the indirect

band gap is 
$$
E_{gi}^e(\Gamma - X) = 1.677
$$
 eV.

The aim of this study is to obtain new information on the localization of the transition bands for the four most popular III–V crystals in specific BZ volumes.

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#### 2. CALCULATION TECHNIQUE

The bands and spectra of the imaginary part of the permittivity of the four III–V compounds were calculated on the basis of electron-density functional theory using the Wien2k software package [30] without taking spin–orbit coupling into account. The spinorbit interaction mainly splits the long-wavelength maximum  $E_1$  into a doublet without changing its relatively simple localization and only slightly affects the other  $\varepsilon_2(E)$  structures. Therefore, disregarding this effect noticeably simplifies the calculation without a decrease in the information supplied on the localization and energy of the other  $\varepsilon_2(E)$  maxima. In this software package, the FP–LAPW technique is used and the generalized gradient approximation GGA–PBE is applied as an exchange–correlation potential [31]. The experimental lattice parameters of the crystals are  $a_0 = 6.1355$  Å for AlSb, 6.096 Å for GaSb, 6.479 Å for InSb, and 6.058 Å for InAs [28]. The main drawback of ab initio calculations with the use of the local-field and generalized gradient approximations is a noticeable reduction in the band-gap energy  $E_{gd}(\Gamma)$  [5, 20– 23, 29]. This effect is especially pronounced in narrow-gap crystals with experimental values of  $E<sub>g</sub>(\Gamma)$  = 0.23 (InSb) and 0.418 eV (InAs): when the experimental crystal-lattice parameter  $a_0$  is used, the theoretical band gap *Egd* vanishes. Therefore, without loss of generality of the calculated transition-band localization spectra, we obtained the positive energies *Egd*(Γ) for InSb and InAs in the calculation of their bands with use of the parameters  $a_0 = 6.364$  and 5.900 Å decreased by 1.8–2.6% of their experimental values for InSb and InAs, respectively. Integration over the entire volume of the irreducible part of the BZ was performed by the tetrahedral technique [32] on the basis of 4612 *K* points. In calculating the spectra of the imaginary part of the permittivity, we used the formula [5]

$$
\varepsilon_2 = \frac{4\pi^2 e^2}{m^2 (\hbar \omega)^2 \Omega_0} \sum_{V,C} \int \frac{|P_{CV}|^2 f(E_C)[1 - f(E_V)]}{|\nabla_{\mathbf{k}}(E_C(\mathbf{k}) - E_V(\mathbf{k}))|} dS, \tag{1}
$$

where *e* and *m* are the elementary charge and electron mass, respectively;  $\Omega_0$  is the unit-cell volume;  $E_V$  and  $E_c$  are the valence- and conduction-band energies, respectively;  $P_{CV}$  is the matrix element of the probability of the transition from the valence band *V* to the conduction band  $C$ ;  $f(E)$  is the Fermi–Dirac distribution function; and *S* is the surface of constant energy  $E_c(\mathbf{k}) - E_V(\mathbf{k}) = \hbar \omega$ . It can be seen that the  $\varepsilon_2(E)$  spectrum has features at  $\nabla_k E_C = \nabla_k E_V$ , i.e., in the case of covariance of the valence and conduction bands. This underlies the highly simplified, yet frequently applied theoretical analysis of the  $\varepsilon_2$  curves; the  $\varepsilon_2(E)$  spectral maxima are assigned to the transitions with energies at which the corresponding pairs of bands are covariant in the largest region of **k** space. In addition, a noticeable role in the permittivity calculations can be played



**Fig. 2.** Functions  $\varepsilon_2(E)$  of the (*1*) AlSb, (*2*) GaSb, (*3*) InSb, and (*4*) InAs crystals.

by the matrix element of the transition probability  $P_{CV}$ in the light-wave electromagnetic field [33] determined from the formula

$$
P_{CV} = -A_0 \frac{ie\hbar}{mc\Omega_0} \int_{\Omega_0} \Psi_{V,\mathbf{k}}^*(r) \nabla \Psi_{C,\mathbf{k}}(r) dr, \qquad (2)
$$

where  $\psi_{V, k}$  and  $\psi_{C, k}$  are the initial and final electronic states,  $A_0$  is the amplitude of the electromagnetic-wave vector potential, and *c* is the speed of light in vacuum. Taking into account  $P_{CV}$  can significantly change the interband transition intensity.

Based on the obtained data on the band structure and matrix elements of the transition probabilities, the localization of transitions in the BZ was determined using the software package developed at the Optical Spectroscopy Department of Udmurt State University. For the widest maxima  $E_1$  and  $E_2$ , transition localization was studied not only for the maximum energy, but over the energy range where the majority of the investigated band is located.

#### 3. RESULTS OF CALCULATIONS AND DISCUSSION

First, we calculated the energy bands of the AlSb, GaSb, InSb, and InAs crystals over the entire BZ volume. It was established that GaSb, InSb, and InAs are direct-band semiconductors with the band gap  $E_{gd}^t$  at the point  $\Gamma: E_{gd}^t(\Gamma) = 0.33$  eV (GaSb), 0.11 eV (InSb), and 0.15 eV (InAs) (index *t* indicates that the values

were obtained theoretically). The UVB maximum for AlSb is located at the point Γ; the LCB minimum is located at the point  $X$ ; and the band-gap energies acquire values of  $E_{gd}^t(\Gamma) = 1.61$  eV,  $E_{gi}^t(\Gamma - L) =$ 1.37 eV, and  $E_{gi}^t(\Gamma - X) = 1.25$  eV. We introduce the corrections  $\Delta_{e-t} = E_{gd}^e(\Gamma) - E_{gd}^t(\Gamma)$  for GaSb, InSb, and InAs and  $\Delta_{e-t} = E_{gi}^e(\Gamma - X) - E_{gi}^t(\Gamma - X)$  for AlSb, which are related to the traditional reduction of the theoretical data on  $E_{g}^{t}$  relative to the experimental data on  $E_g^e$ . Thus, our calculated data are reduced by 0.12– 0.48 eV: Δ*e*–*<sup>t</sup>* = 0.43 eV (AlSb), 0.48 eV (GaSb), 0.12 eV (InSb), and 0.27 eV (InAs).  $E_{gi}^e(\Gamma - X) - E_{gi}^t$ 

The AlSb bands have no significant differences from the bands of the other investigated compounds, except for the indirect-gap character. Therefore, below we denote the bands of all four crystals similarly. The upper valence bands  $V_1$  and  $V_2$  are degenerate along the two principle axes,  $\Lambda$  and  $\Delta$ , and in their closest proximity. At the other BZ high-symmetry points, the level  $V_2$  is located lower than  $V_1$  by an energy ranging from 0.5 to 1.5 eV. Assuming the traditional scheme of UVB maximum positioning at the point  $\Gamma$  to be an energy reference point, we obtain that the two UVBs in all the crystals are located in the range from 0 to  $(-3.5 \pm 0.3)$  eV and the third UVBs lie in the range from 0 to  $(-6.2 \pm 0.8)$  eV. The lower conduction bands have a complex structure and overlap in many directions. The width of the two lower conduction bands  $C_1$ and  $C_2$  are  $\sim$  (4.3  $\pm$  0.3) eV.

Then, based on the obtained bands with regard to the correction  $\Delta_{e-t}$ , for each crystal the spectra of the imaginary part of the permittivity  $\varepsilon_2(E)$  were calculated. They contain five main structures:  $E_1$ ,  $E_0$ ,  $E_2$ ,  $E_x$ , and  $E'_1$  (Fig. 2). The energies of these structures are listed in Table 1 in comparison with similar values from other theoretical and experimental publications. The difference between our data and the experimental results is predominantly no larger than 0.1 eV and reaches  $0.36$  eV for  $E_2$  (InSb) and  $E_1^{'}$  (InAs). It is worth noting that, due to the features of symmetry of the bands  $V_1$  and  $V_2$ , the intensities of the transitions with their involvement are radically different. The vicinity of the long-wavelength maximum  $E_1$  from the energy of the long-wavelength absorption edge to the step  $E_{0}^{'}$ forms the transitions from only two degenerate UVBs to the LCBs ( $V_{1,2} \rightarrow C_1$ ). In the high-energy region (step  $E'_0$ ), transitions to the second LCB ( $V_{1,2} \rightarrow C_2$ ) begin. The most intense maximum  $E_2$  is formed mainly by the transitions  $V_1 \rightarrow C_1$  (see the second column in Table 2). Starting from  $E_x$ , their contribution, along with  $V_2 \rightarrow C_1$ , significantly decreases. Therefore,

in the region of structures  $E_x$  and  $E'_0$  the decisive role

Compound	Source	$E_1$	$E_0^"$	$E_2$	$E_{\rm x}$	$E_1'$
AlSb	our data	2.81	3.73	4.05	4.95	5.09
	exptl. $[24]$	2.838	3.76	4.00		5.22
	theor. $[15]$	2.8		3.8		4.7
	theor. $[17]$	2.67	3.44	3.86		5.06
GaSb	our data	2.28	3.38	4.23	5.06	5.47
	exptl. $[25]$	2.16	3.4	4.13	5.11	5.4
	theor. $[15]$	1.9		3.6		4.8
	theor. $[17]$	1.95	3.04	4.00		—
InSb	our data	1.93	3.22	3.83	4.42	4.98
	exptl. $[26]$	1.968	3.14	4.186		5.22
	theor. $[16]$	2.17		4.10		5.20
	theor. $[17]$	1.86	2.88	4.13		5.09
InAs	our data	2.63	4.17	4.54	5.07	5.91
	exptl. [27]	2.608		4.54	5.282	6.261
	theor. $[17]$	2.55	4.21	4.61		
	theor. $[20]$	3.33		4.55	5.10	5.90

**Table 1.** Energies of the main structures in the  $\varepsilon_2$  spectra of the AlSb, GaSb, InSb, and InAs crystals

All the values are given in eV, exptl., and theor. indicate experimental and theoretical results, respectively.

**Table 2.** Contributions (%) of the transitions  $V_1 \to C_1$  of the  $\varepsilon_2(E)$  spectrum to the intensity of the main  $E_2$  maximum in different regions of the Brillouin zone of the AlSb, GaSb, InSb, and InAs crystals

Compound	Region						
	the entire Brillouin-zone volume	<b>TLUX</b>	$\Gamma_1L_1U_1X_1$	region II	region III		
AlSb	88.5	30	12	13	33.5		
GaSb	92	39	12		34		
InSb	86	29	16		37.5		
InAs	84	31	15		31		

is played by the transitions  $V_1 \rightarrow C_2$ . The effect of the other pairs of bands is weaker. Therefore, until  $\sim$ 7 eV, it is sufficient to consider localization in reciprocal space for only transitions from the two UVBs to the two LCBs. It should be taken into account that in describing our data on localization in any BZ region, we will also take into account its vicinity with radius  $\delta$ , unless the other is specified ( $\delta \approx 0.0434 \times 2\pi/\text{\AA}$ ).

## *3.1. The E1 Maximum*

According to the calculations, transitions to the regions of the long-wavelength maximum occur only from the two UVBs to the LCB. The intensity of the transition  $V_1 \rightarrow C_1$  is higher than the intensity of the transition  $V_2 \rightarrow C_1$  by a factor of 2–2.5. Both bands are concentrated mainly in the following  $\Lambda$  axis segments: from *L*(0.5, 0.5, 0.5) to the point (0.15, 0.15, 0.15) and from *L* to the point (0.44, 0.44, 0.44) for AlSb; from *L* to the point  $(0.24, 0.24, 0.24)$  and from the point (0.22, 0.22, 0.22) to the point (0.15, 0.15, 0.15) for

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GaSb; from the point  $(0.41, 0.41, 0.41)$  to the point (0.22, 0.22, 0.22) and from *L* to the point (0.26, 0.26, 0.26) for InSb; from the point (0.43, 0.43, 0.43) to the point (0.26, 0.26, 0.26) and from *L* to the point (0.30, 0.30, 0.30) for InAs and for the bands  $V_1 \rightarrow C_1$  and  $V_2 \rightarrow C_1$ , respectively. A part of their intensity corresponds to the very small  $\delta$  (AlSb) and 2 $\delta$  vicinity (GaSb, InSb, and InAs) of the Λ axis on the Γ*LK* plane and a small area at the intersection of the Γ*KWX* and Γ*LW* planes near the points (0.14, 0.06, 0.0), (0.17, 0.09, 0.0), (0.20, 0.10, 0.0), and (0.23, 0.12, 0.0) for AlSb, GaSb, InSb, and InAs, respectively.

In contrast to the simplified results reported in  $[8-13, 17-19, 21]$ , our data show that, for all four crystals, the localization of both bands of the transitions  $V_1 \rightarrow C_1$  and  $V_2 \rightarrow C_1$  along the  $\Gamma - L$  direction is complex and inhomogeneous: they occur not only in the closest vicinity of the point *L*, but also in specific regions on the  $\Lambda$  axis (in contrast to [8–13, 18]) and the Γ*LK* plane (as in [10] for GaSb); the transitions from  $V_1$  to  $V_2$  along  $\Lambda$  have radically different intensi-



**Fig. 3.** Localization of the interband transitions for the main  $E_2$  maximum of the AlSb, GaSb, InSb, and InAs crystals on (a) the  $\Gamma LUX$  and (b)  $\Gamma_1L_1U_1X_1$  planes (region I).

ties, despite the degeneracy of this pair in energy; in the vicinity of the intersection of the Γ*KWX* and Γ*LW* planes, their intensities significantly increase.

# *3.2. The*  $E_0$ <sup>'</sup> *Step*

In the case of the  $E_0$  step, our data are more detailed than the results of other calculations. The most important role in all of the investigated compounds is played by the transitions  $V_{1, 2} \rightarrow C_2$  in the vicinity of  $\sim$ (3–4) $\delta$  near the BZ center (on average, the transitions in AlSb are a bit closer to the point Γ than in InSb) and the transitions  $V_{1,2} \rightarrow C_1$  along the  ${E}^{'}_0$ 

segments on the Γ*KWX* plane near the Δ axis. In GaSb, InSb, and InAs, the key role is played by the maxima in the spectra of partial contributions of the transitions from the two UVBs to the second LCB and in AlSb the transitions from the second UVB to the LCB are most important.

#### 3.3. The E<sub>2</sub> Maximum

The maximum of the most intense band is located at ~4.05 eV (AlSb), 4.23 eV (GaSb), 3.83 eV (InSb), and 4.54 eV (InAs) (Table 1 and Fig. 2). It is related by  $\sim$ (88  $\pm$  4)% to the transitions from the UVBs to the LCB in the large region of the bulk of the BZ (Table 2). The entire set of **k** points can be divided into the following regions: (i) the vicinity of the Γ*LUX* plane (region I in Fig. 3), (ii) the vicinity of the Γ*LK* plane (region II in Fig. 4), and (iii) the vicinity of the  $\Gamma_2 L_2 U_2 X_2$  plane (region III in Fig. 1). Since the band  $E_2$  is relatively wide, regions I, II, and III are separated into an additional three parts responsible for (i) the long-wavelength (white) and (ii) short-wavelength (dark-grey) parts of the structure  $E_2$  and (iii) the immediate vicinity of the maximum (light-grey). We limit the long-wavelength side of the main maximum by energies to 3.90 eV (AlSb), 4.16 eV (GaSb), 3.64 eV (InSb), and 4.27 eV (InAs) and the short-wavelength side, to 4.21 eV (AlSb), 4.30 eV (GaSb), 3.96 eV (InSb), and 4.76 eV (InAs).

The transitions concentrated in region I are responsible for  $\sim$  (42–51)% of the contribution to the band *E*2 and are limited in the BZ by the Γ*LUX* and  $\Gamma_1 L_1 U_1 X_1$  planes. The points  $\Gamma_1, L_1, U_1$ , and  $X_1$  have the coordinates ( $\delta$ ,  $\delta$ , 0.0), (0.5 +  $\delta$ /3, 0.5 +  $\delta$ /3, 0.5 -2δ/3), (1.0,  $0.25 + 0.5$ δ,  $0.25 - 0.5$ δ), and (1.0, δ, 0.0), respectively. Thus, region I for all the crystals occupies a significant part on the  $\Gamma LUX$  ( $\Gamma_1L_1U_1X_1$ ) face and is limited by the segments  $\Gamma$ –*X*( $\Gamma$ <sub>1</sub>–*X*<sub>1</sub>), *X*–*U*(*X*<sub>1</sub>–*U*<sub>1</sub>), and  $L$ –*U* ( $L_1$ – $U_1$ ) on one side and by a V-shaped curve with ends located on the  $\Gamma$ –*X* ( $\Gamma$ <sub>1</sub>–*X*<sub>1</sub>) and *L*–*U*  $(L_1-U_1)$  axes on the other side. The formation of the long-wavelength side of the band  $E_2$  occurs mainly near this V-shaped curve. The region located closer to the point  $U(U_1)$  and the  $U-X(U_1-X_1)$  axis is responsible for the short-wavelength side. Although the distance between the outer and inner faces of region I is very small ( $\sim \delta/\sqrt{2}$ ), the configuration and intensity radically change upon transition from the first to the second face (Table 2): the region itself somewhat increases, but the intensity decreases by a factor of 2–3. It follows explicitly from these data that the points *X*  $[8, 9, 17, 21], (0.75, 0.25, 0.25), [13],$  and the axes  $\Delta$ [11, 19] and *X*–*U* [9] amount only to a small part of the wide spectrum of **k** points responsible for the intense transitions at Γ*LUX* and Γ<sub>1</sub>*L*<sub>1</sub>*U*<sub>1</sub>*X*<sub>1</sub>.

The description of region II is similar to that of region I, if we replace the Γ*LUX* plane with the Γ*LK*



**Fig. 4.** Localization of the interband transitions for the main  $E_2$  maximum of the AlSb, GaSb, InSb, and InAs crystals on (a) the  $\Gamma L K$  and (b)  $\Gamma_1 L_1 K_1$  planes (region II).

one and the  $\Gamma_1 L_1 U_1 X_1$  plane with the  $\Gamma_1 L_1 K_1$  one (Fig. 4). The point  $K_1$  has the coordinates (0.75 + 0.5δ, 0.75–0.5δ, 0). On the Γ*LK* face, the Σ axis, especially near the vertex  $K$ , is the most important for our investigations: in particular, in InSb its role is insignificant  $(\sim 3\%)$ ; in GaSb and InAs, its contribution is ~7%; and in AlSb, it is ~13%. Thus, the  $\Sigma$ -axis value is not as important in the formation of the band  $E_2$  as was described in [8, 11, 12, 18, 19, 21].

Region III is located in the  $\delta$  vicinity of the  $\Gamma_2 L_2 U_2 X_2$  plane; its position in the irreducible part of the BZ is schematically shown in Fig. 1 along the  $B_1B_2$ and  $B_1B_3$  segments. For all four crystals, the point  $B_1$ has the coordinates (0.85, 0.11, 0.0); the point  $B_2$  has

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the coordinates (0.45, 0.225, 0.00) for AlSb and (0.5, 0.25, 0.0) for the remaining crystals; and the point  $B_3$ has the coordinates  $(0.7, 0.5, 0.3)$  for InSb and  $(0.67, 0.5, 0.3)$ 0.5, 0.33) for the other crystals. The highest intensity of the transitions in region III is concentrated near the intersection of the Γ*KWX* and Γ*LW* planes, i.e., in the vicinity of the point  $B_2$ .

Thus, the band  $E_2$  of the AlSb, GaSb, InSb, and InAs crystals is formed not in a narrow range of points, but in a wide region of **k** points located not only on the Γ*LUX* and Γ*LK* faces, as was mentioned in [10] for GaSb, but in the bulk of the BZ. The importance of the  $\Delta$  and  $\Sigma$  axes depends heavily on the investigated compound.

# *3.4. The Ex Structure*

The occurrence of the  $E<sub>x</sub>$  structure following the  $E<sub>2</sub>$ structure in energy in the spectra of the theoretical  $\varepsilon_2(E)$  curves is related to the occurrence of a weak maximum in transitions from the UVB to the second LCB at  $\sim$ 5.0 eV (AlSb, GaSb, InAs) and  $\sim$ 4.4 eV (InSb) (Table 1 and Fig. 2). They attain the highest intensity along the  $\Delta$  axis from the point (0.43, 0.0, 0.0) to the point (0.78, 0.0, 0.0). In [9, 11, 13, 17] for GaSb, InSb, and InAs, these transitions occur from the point  $(0.50, 0.0, 0.0)$  to the point  $(0.7, 0.0, 0.0)$ . The transitions of most interest occur in the bulk of the irreducible part of the BZ, which are not described in other publications. These transitions are less intense, than those located along the  $\Delta$  axis and are concentrated along an arched curve. One end of this curve is located on the  $\Lambda$  axis at the points (0.33, 0.33, 0.33) for AlSb, (0.30, 0.30, 0.30) for GaSb, (0.26, 0.26, 0.26) for InSb, and (0.19, 0.19, 0.19) for InAs and the other end is located in the vicinity of the point (0.50, 0.28, 0.0) for GaSb, InSb, and InAs and the point (0.50, 0.25, 0.0) for AlSb.

# 3.5. The  $E_1$ <sup>'</sup> Maximum

The  $E'_1$  maximum is formed by the same pair of bands as  $E_x$ . This pair of bands is located in a wide spectrum of **k** points from the vicinity of the vertex *L*, but, in contrast to [9, 10, 13, 21] for GaSb, InSb, and InAs, there are no transitions at the point *L* itself. A part of the transitions is concentrated at the high-symmetry axes of the BZ; at the  $\Lambda$  axis in the vicinity of the points (0.45, 0.45, 0.45) for AlSb and GaSb (0.43, 0.43, 0.43) for InSb, and (0.37, 0.37, 0.37) for InAs; on the  $L$ –*U* axis in the vicinity of the points (0.58, 0.46, 0.46) for AlSb, (0.56, 0.47, 0.47) for GaSb, (0.59, 0.455, 0.455) for InSb, and (0.61, 0.455, 0.445) for InAs; on the  $L-K$  axis in the vicinity of the points located at the same distance from *L* as the points on the *L*–*U* axis; and on the *L*–*W* axis in the vicinity of the point  $(0.60, 0.50, 0.40)$  for all four crystals. In other studies, the transitions on the  $\Lambda$  axis for AlSb, InSb, and InAs are located in the vicinity of the point (0.375, 0.375, 0.375) [11, 12]. Localization of the transitions on the *L*–*W* axis was described only in [18] for GaSb, but without specifying a region. Transitions on the  $\Delta$  axis, as in [11, 18] for GaSb, InSb, and InAs, were also revealed by us, but their intensity is very low.

#### 4. CONCLUSIONS

The imaginary part of the permittivities of AlSb, GaSb, InSb, and InAs was calculated using the FP–LAPW technique in the generalized gradient approximation (GGA–PBE) in the range to  $\sim$ 7 eV. The novelty of this study is that, for III–V crystals, the most intense transitions can be concentrated not only in the vicinity of the high-symmetry axes of the Brillouin zone, but also in its bulk. This concerns, to the greatest extent, band  $E_2$ , which is formed with the involvement of a significant part of the Brillouin zone in the vicinity of the Γ*LUX* and Γ*LK* planes and in the vicinity of the point (0.45, 0.225, 0.0) for AlSb or (0.5, 0.25, 0.0) for GaSb, InSb, and InAs. Detailed schemes of localization of different parts of the transition bands in the bulk of the Brillouin zone are presented.

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