# **NANOMATERIALS, CERAMICS**

# Non-Isothermal Crystallization Kinetics of Fe<sub>2</sub>O<sub>3</sub>–CaO–SiO<sub>2</sub> **Glass Containing Nucleation Agent**  $P_2O_5/TiO_2^{-1}$

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**Abstract**—Fe<sub>2</sub>O<sub>3</sub>–CaO–SiO<sub>2</sub> glass ceramics containing nucleation agent P<sub>2</sub>O<sub>5</sub>/TiO<sub>2</sub> were prepared by sol-gel method. The samples were characterized by X-ray diffraction (XRD) and differential scanning calorimetry (DSC). The activation energy and kinetic parameters for crystallization of the samples were calculated by the Johnson-Mehi-Avrami (JMA) model and Augis-Bennett method according to the results of DSC. The results showed that the crystallization mechanism of  $Fe<sub>2</sub>O<sub>3</sub>$ –CaO–SiO<sub>2</sub> glass, whose non-isothermal kinetic parameter *n* = 2.3, was consistent with surface crystallization of the JMA model. The kinetics model function of Fe<sub>2</sub>O<sub>3</sub>–CaO–SiO<sub>2</sub> glass,  $f(\alpha) = 2.3(1-\alpha)[-ln(1-\alpha)]^{0.57}$ , was also obtained. The addition of nucleation agent  $P_2O_5/TiO_2$  could reduce the activation energy, which made the crystal growth modes change from onedimensional to three-dimensional.

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#### INTRODUCTION

Magnetic mediated hyperthermia (**MMH**) was a new cancer therapy developed in recent years.  $Fe<sub>2</sub>O<sub>3</sub> - CaO-SiO<sub>2</sub>$  glass ceramics, due to their strong magnetism and good biological activity, were widely concerned by researchers. So MMH using  $Fe<sub>2</sub>O<sub>3</sub> - CaO-SiO<sub>2</sub>$  ferromagnetic glass ceramics prepared by melting method had made great progress in animal experiments  $[1-3]$ . The Fe<sub>2</sub>O<sub>3</sub>–CaO–SiO<sub>2</sub> glass ceramics as bioactive material had also been prepared by sol-gel method [4]. Glass ceramics prepared by sol-gel method were of higher purity, more specific surface area and inherent porous nature at low reaction temperature [5, 6], thus sol-gel method was widely applied to the preparation of new glass ceramics.

Glass ceramics were prepared by controlled crystallization, so the crystallization kinetics and mechanism of nucleation and growth were the key factors to optimize the processing parameters for desired product [7]. While activation energy and crystallization mechanisms were the most important kinetic parameters for the crystallization of glasses, which can be obtained by differential thermal analysis (DTA) and differential scanning calorimetry (DSC) results [8– 11]. A variety of non-isothermal theoretical models were proposed to explain the crystallization kinetics of glasses, and several models were frequently used to identify the non-isothermal crystallization mechanism in the previous works [12–15]. The results indicated that effects of different nucleation agent on the crystallization kinetics parameters were different, appropriate nucleation agent could reduce the activation energy, increase the crystallization growth index and promote the occurence of bulk crystallization. Stookey believed that efficient internal nucleation of glass enabled the development of homogeneous and fine-grained microstructure [16]. The effect of nucleating agents  $TiO<sub>2</sub>$  and  $P<sub>2</sub>O<sub>5</sub>$  on the controlled crystallization process of glass had been discussed [17–19]. However, the effect of  $TiO<sub>2</sub>$  and  $P<sub>2</sub>O<sub>5</sub>$  on the crystallization of  $Fe<sub>2</sub>O<sub>3</sub> - CaO-SiO<sub>2</sub>$  glass ceramics had not been investigated.

The crystallization mechanisms of  $Fe<sub>2</sub>O<sub>3</sub> - CaO-SiO<sub>2</sub>$ glass ceramics prepared by sol-gel method were discussed in present work. A series of DSC under nonisothermal conditions were carried out at various heating rates so as to determine the crystallization kinetic parameters and the kinetics model function. Then the crystallization kinetic parameters of the samples containing nucleation agent  $TiO<sub>2</sub>$  and  $P<sub>2</sub>O<sub>5</sub>$  were also calculated on the base of the above results to analyze the effect of nucleation agent on the crystallization of  $Fe<sub>2</sub>O<sub>3</sub> - CaO-SiO<sub>2</sub>$  glass ceramics, which could provide some theoretical support to the preparation of  $Fe<sub>2</sub>O<sub>3</sub> - CaO-SiO<sub>2</sub>$  glass ceramic containing nucle-

 $<sup>1</sup>$  The article is published in the original.  $\qquad \qquad$  ation agent.</sup>

#### EXPERIMENTAL

Glass sample *B*1 with composition 19.2CaO– 7.24SiO<sub>2</sub>–2.1Fe<sub>2</sub>O<sub>3</sub> while samples *B*2 and *B*3 have the basic composition with 1 wt% of the nucleator  $TiO<sub>2</sub>/P<sub>2</sub>O<sub>5</sub>$  in excess of 100% were prepared. The solution of tetraethyl orthosilicate (TEOS) and ethanol were prepared. Distilled water was added in the solution, the molar ratio of TEOS and water was 1 : 15. Then hydrochloric acid was added in the solution and stirred with a magnetic stirrer for 10 min before the calcium nitrate and iron nitrate were added in the solution. The resulting solution was then transferred into water bath box and maintained at 45○C for 150 min. Then the temperature was raised up to 65 °C until colloidal tilt lost liquidity. The samples were aged for 7 days at room temperature. The gels obtained were baked in the drying oven at  $120^{\circ}$ C for 12 h, and were heated at 550°C for 1 h in a heat treatment furnac, then slowly cooled to room temperature, the mass glasses were obtained. The glass samples were ground into powder and measured by DSC. The nucleation and crystal growth temperature ranges can be fixed according to the DSC curve. At last the samples were heat-treated for 1h in atmosphere.

X-ray diffraction (XRD) analysis was performed with a XD-6 X-ray diffractometer at room temperature, with CuK<sub> $\alpha$ </sub> radiation, 36 kV voltage and 20 mA current. X-ray data were collected in the  $5 < 20 < 80$ range. Prior to the XRD test, the samples were ground into powder and filtered through 300-mesh gauze. The XRD patterns were then compared with those in the Joint Committee on Powder Diffraction Standards (JCPDS).

The samples were characterized by DSC using SDT-Q600 differential thermal scanning analyzer. The sample weight was about 10.00 mg, and alumina was used as reference. The temperature range of collected data was  $500~1100$ °C in the air.

#### THEORETICAL ANALYSIS

The isothermal crystallization process in glasses were usually described by the JMA equation [20, 21],

$$
\alpha = 1 - \exp[-(kt)^n],\tag{1}
$$

where  $\alpha$  is the crystallized fraction which is crystallized at time *t*, *n* is the Avrami exponent which depends on the mechanism of the growth and dimensionality of crystal, *k* is a rate constant that follows an Arrhenius equation

$$
k = k_0 \exp(-E/RT), \tag{2}
$$

where  $k_0$  is the pre-exponential factor,  $E$  is the activation energy. Taking the first derivative of  $\alpha$  with respect to *t*, the rate equation can be obtained

$$
\frac{d\alpha}{dt} = (1 - \alpha)n k^n t^{n-1},\tag{3}
$$

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and eliminating *t* by  $\alpha$  from Eq. (1)

$$
\frac{d\alpha}{dt} = (1 - \alpha)nk[-\ln(1 - \alpha)]^{(n-1)/n}.\tag{4}
$$

Which can be expressed as the product of *k*(*T*) and *f*(α)

$$
\frac{d\alpha}{dt} = k(T)f(\alpha). \tag{5}
$$

Where

$$
f(\alpha) = n(1 - \alpha) [-\ln(1 - \alpha)]^{(n-1)/n}.
$$
 (6)

Where *k*(*T*) is temperature dependent rate constant,  $f(\alpha)$  is the kinetics model function related to the mechanism.

The DTA was carried with a constant heating rate, the temperature changed linearly with time

$$
T = T_0 + \beta t,\tag{7}
$$

where  $T_0$  is the temperature at which the crystallization begins and *T* is the temperature at time *t*, β is the heating rate. For non-isothermal process, according to Eq.  $(2)$  and Eq.  $(7)$ , Eq.  $(1)$  can be written as

$$
\alpha = 1 - \exp\left[-\left(k_0 \exp\left(-\frac{E}{R}\right)\right)^n \left(\frac{T - T_0}{\beta}\right)^n\right],\qquad(8)
$$

Eq. (5) can be written as

$$
\frac{d\alpha}{dt} = \frac{k_0}{\beta} \exp\left(-\frac{E}{RT}\right) f(\alpha). \tag{9}
$$

In this work the composite integral method [22, 23] was based on the Coats–Redfern equation [24], which was rewritten as follows

$$
\ln\left(\beta \frac{g(\alpha)}{T^2}\right) = \ln\left(\frac{k_0 R}{E}\right) - \frac{E}{RT},\tag{10}
$$

where  $g(\alpha)$  is the integral expression of the kinetics model function

$$
g(\alpha) = \int_{0}^{\alpha} \frac{d\alpha}{f(\alpha)}.
$$
 (11)

So the curve  $\ln(\beta g(\alpha)/T^2)$  vs.  $1/T$  for a given analytical form of  $g(\alpha)$  should be a straight line at different heating rates. Then the kinetic model  $f(\alpha)$  that gives the best correlation coefficient was chosen, for which the data fall in a single master straight line. The activation energy *E* and non-isothermal kinetic parameter *n* can be calculated from Augis-Bennett approximation method [25, 26]

$$
\ln\left(\frac{\beta}{T_p - T_0}\right) = \ln k_0 - \frac{E}{RT_p},\tag{12}
$$

$$
n = \frac{2.5}{\Delta T} \frac{RT_p^2}{E}.
$$
 (13)

6  $-5$  $-4$  $-3$ 2  $-1$ 0 1 2 3

10

 $-15$ 

 $-12$ 

-9 6

*DSC*, μ V

3

0 3

Where  $T_p$  is the temperature of the maximum DSC peak,  $\Delta T$  is the full width at half maximum of the DTA

**Fig. 1.** XRD patterns of the glass samples heated at 850°C.

#### RESULTS AND DISCUSSION

In order to determine the crystalline phase formed by thermal treatment, XRD analysis was carried on the samples. Similar XRD patterns were obtained indicating the crystallization of two major crystalline phases, wollastonite and hematite, according to the JCPDS cards (Fig. 1). While some hydroxylapatite and schorlomite were also present in sample *B*2 and *B*3, respectively.

The DSC curves of the investigated glasses at various heating rates were shown in Fig. 2. Kinetic analysis was performed by the initial temperature  $T_0$  and the highest peak  $T_p$  of the DSC curve. The non-isothermal kinetic parameter *n* were shown in Table 1, which were calculated according to Eq. (13). The average values *n* of samples *B*1, *B*2, *B*3 were 2.21, 3.72, 3.60, respectively. The conversion degree in the range 0.1– 0.7 was chosed to analyse the non-isothermal data because that the errors were relatively high at the beginning and the end of the DTA curves.

The activation energy of crystallization  $E$  and  $k_0$  of sample *B*1 were calculated from Augis-Bennett approximation method. The curves  $ln[β/(T_p - T_0)]$  vs.  $1/T_p$ were drawn (Fig. 3). The activation energy *E* was calculated from the slope while  $k_0$  was obtained from the intercept,  $E = 487.3 \text{ kJ} \text{ mol}^{-1}$ ,  $k_0 = 3.294 \times 10^{22} \text{ min}^{-1}$ . The value of *n* was optimized combined with Eq. (8), with *n* = 2.0, 2.1, 2.2, 2.3, 2.4. The results showed that  $n = 2.3$  close to the actual results according to the comparison of  $\alpha = \alpha(T)$  (Fig. 4). It comes out that a



600 700 800 900 1000 1100 1200

918.2

913.5 909.2

868.0

841.5 853.6

825.4

5˚C/min  $10^{\circ}$ C/min 20˚C/min

40˚C/min

*B*2

35˚C/min 30˚C/min

20˚C/min

40˚C/min

*B*1

**Fig. 2.** DSC curves of the glass samples.

 $T, \degree C$ 

915.5

600 700 800 900 1000 1100 1200

896.5

*B*3

satisfactory agreement among the experimental and reconstructed  $\alpha = \alpha(T)$  curves exist. However, the error of  $\beta = 40^{\circ}$ C min<sup>-1</sup> was slightly high. The reason

**Table 1.** The non-isothermal kinetic parameters *n* of the samples

B1		B2		B <sub>3</sub>	
$\beta$ , °C min <sup>-1</sup>	$\boldsymbol{n}$	$\beta$ , °C min <sup>-1</sup>	n	$\beta$ , °C min <sup>-1</sup>	n
	2.19	20	3.53	20	3.38
10	2.08	30	3.10	30	4.03
20	2.34	35	3.98	35	3.76
40	2.22	40	4.24	40	3.25



peak.

 $0 \frac{1}{10} \frac{1}{20} \frac{1}{30} \frac{1}{40} \frac{1}{50} \frac{1}{60} \frac{1}{70} \frac{1}{80} \frac{1}{90}$  $\begin{array}{c} S \ S \end{array}$   $\begin{array}{c} S \ S \end{array}$ W h  $M$  W<sub>MM</sub>  $H \parallel \cdot \cdot \cdot \parallel$   $\cdots$   $H$   $H$   $H$ HH H H h H H H H H H H H w∭III ™ W W  $\frac{h}{v}$  w W W  $W_{\text{H}}$  W  $W_{\text{M}}$  M<sup>W</sup> W Intensity (counts) 90<br>2θ W-wollastonite H-hematite M-magnetite h-hydroxylapatite S-schorlomite *B*1 *B*<sup>2</sup> *B*3 W H MILLE I M W S



**Fig. 3.** The plots of  $\ln[\beta/(T_p - T_0)]$  vs.  $1/T_p$ .

was that the peak was obvious with high heating rate, but the temperature with a certain lag which caused the baseline drift obviously. The kinetics model function was preliminary obtained according to Eq. (6),  $f(\alpha) = 2.3(1 - \alpha) [-\ln(1 - \alpha)]^{0.57}, g(\alpha) = [-\ln(1 - \alpha)]^{0.44}.$ 

The curves  $\ln(\beta g(\alpha)/T^2)$  vs.  $1/T$  was obtained cor-<br>ponding to the composite integral method Eq. (10) responding to the composite integral method Eq. (10) (Fig. 5a). All points are placed around a single line for all heating rates, which indicate that the kinetics model function was suitable for  $Fe<sub>2</sub>O<sub>3</sub> - CaO-SiO<sub>2</sub>$ glass. The activation energy  $E = 536.8$  kJ mol<sup>-1</sup> of *B*1 was obtained from the line  $5(a)$  ( $r = 0.995$ ). The linear correlation coefficient *r* was 0.998 (Fig. 5b) while the heating rate was carried below  $20^{\circ}$ C min<sup>-1</sup>, and the activation energy  $E = 490.7$  kJ mol<sup>-1</sup> was in good agreement with  $E = 487.3$  kJ mol<sup>-1</sup> obtained from Augis-Bennett approximation method.



**Fig. 4.** The experimental and reconstructed  $\alpha = \alpha(T)$  curves for kinetic model  $n = 2.3$ ,  $E = 487.3$  kJ mol<sup>-1</sup>,  $k_0 = 3.294 \times 10^{22}$  min<sup>-1</sup>.  $3.294 \times 10^{22}$  min<sup>-1</sup>.

The kinetics model function obtained from Augis-Bennett method was suitable for  $Fe<sub>2</sub>O<sub>3</sub> - CaO-SiO<sub>2</sub>$ glass according to the above results. So the activation energys and kinetic parameters of sample *B*2 and *B*3, which were listed in Table 2, were also calclated so as to investigate the effect of nucleation agent. The results showed that the glasses containing nucleation agent had lower activation energy compared to *B*<sup>1</sup> without nucleation agent, the activation energy of glass containing nucleation agent  $P_2O_5$  was the lowest. The Avrami exponent  $n_{B1} = 2.21$  indicates one-dimensional crystallization with a constant bulk nucleation rate, while  $n_{B2} = 3.72$  and  $n_{B3} = 3.6$  indicates volume nucleation and three-dimensional growth mechanism [27]. A  $P_2O_5$  and TiO<sub>2</sub> usually had different effect to the activation energy,  $TiO<sub>2</sub>$  could reduce activation energy in all the systems while  $P_2O_5$  could reduce acti-



**Fig. 5.** The plots of  $\ln(\beta g(\alpha)/T^2)$  vs.  $1/T$ . (a)  $5^{\circ}$ C min<sup>-1</sup>  $\leq \beta \leq 40^{\circ}$ C min<sup>-1</sup>; (b)  $5^{\circ}$ C min<sup>-1</sup>  $\leq \beta \leq 20^{\circ}$ C min<sup>-1</sup>.

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**Table 2.** Activation energy and kinetic parameters of the samples

Sample	75 I	В2	
E, kJ mol <sup>-1</sup>	487.3	244.)	271.0
	2.21	3.72	3.60

vation energy only in some systems [28]. However, both  $P_2O_5$  and TiO<sub>2</sub> could reduce activation energy to similar level in  $Fe<sub>2</sub>O<sub>3</sub> - CaO-SiO<sub>2</sub>$  glass. Both of them  $n \approx 4$ , which indicate that they had the similar crystallization mechanism.

## **CONCLUSIONS**

The JMA and Augis-Bennett method as well as the composite integral method were used for the analysis of the non-isothermal kinetic of  $Fe<sub>2</sub>O<sub>3</sub> - CaO-SiO<sub>2</sub>$ glass and  $Fe<sub>2</sub>O<sub>3</sub> - CaO-SiO<sub>2</sub>$  glass containing nucleation agent  $P_2O_5$  and TiO<sub>2</sub>. The results showed that the kinetics model of *B*1 was consistent with JMA model, whose  $n = 2.3$  with one-dimensional crystallization, while the kinetics model function of  $Fe<sub>2</sub>O<sub>3</sub> - CaO SiO<sub>2</sub>$  glass was preliminary obtained. It comes out that a satisfying agreement of these calculated curves with those experimentally obtained. The addition of nucleation agent  $P_2O_5$  and TiO<sub>2</sub> could reduce the activation energy of  $Fe<sub>2</sub>O<sub>3</sub> - CaO-SiO<sub>2</sub>$  glass, which caused the crystal growth modes change from one-dimensional to three-dimensional.

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