

## Dependence of the Friction Speed on the Wind Speed in the Surface Air Layer

V. A. Gladkikh<sup>a</sup>, V. P. Mamyshev<sup>a</sup>, I. V. Nevzorova<sup>a</sup>, and S. L. Odintsov<sup>a, \*</sup>

<sup>a</sup>V.E. Zuev Institute of Atmospheric Optics, Siberian Branch, Russian Academy of Sciences, Tomsk, 634055 Russia

\*e-mail: odintsov@iao.ru

Received March 1, 2021; revised March 1, 2021; accepted March 18, 2021

**Abstract**—The empirical relationships between the friction speed (dynamic speed) and the crosswind speed are considered for different conditions (time of the day, season, stratification type, observation site, and measurement altitude). Initial experimental data used to derive these relationships were acquired by ultrasonic weather stations operating in the surface air layer at different observation sites.

**Keywords:** surface air layer, wind speed, friction speed, turbulence

**DOI:** 10.1134/S1024856021050080

### INTRODUCTION

The friction speed  $u_*$  enters into computational schemes used for forecasting the state of the atmosphere (see, e.g., [1–6] and references therein). To find  $u_*$ , it is necessary to know the mixed moments of turbulent components of the wind vector. However, the information about turbulence is usually lacking at the initial stage of a forecast. To acquire it, some “external” parameters should be used, for example, probable horizontal wind speed  $V_h$ . In this work, we consider empirical relationships  $u_*(V_h)$  for different conditions (time of the day, season, and stratification type). The experimental data for the analysis of these relationships were received from ultrasonic weather stations (UWS) [7] operating in the surface air layer at two observation sites: (1) IAO, at the edge of Tomsk (Akademgorodok), on the urbanized territory, 5 m above the roof of the laboratory building of the Institute of Atmospheric Optics, Siberian Branch, Russian Academy of Sciences (IAO SB RAS), 17 m above the underlying surface; (2) BEC—Basic Experimental Complex of IAO SB RAS, natural landscape, large forest opening, measuring altitudes are 5 and 10 m; measuring frequency is 10 times per second (10 Hz). We analyze the experimental data acquired in 2019. The measurements were interrupted for technical reasons. The estimates below were calculated over 10-min intervals.

The friction speed is often calculated by the equation (see, e.g., [8–14])

$$u_* = \sqrt[4]{(u'w')^2 + (v'w')^2}, \quad (1)$$

though its classic definition has the form [15–17]:

$$u_* = \sqrt{-u'w'}. \quad (2)$$

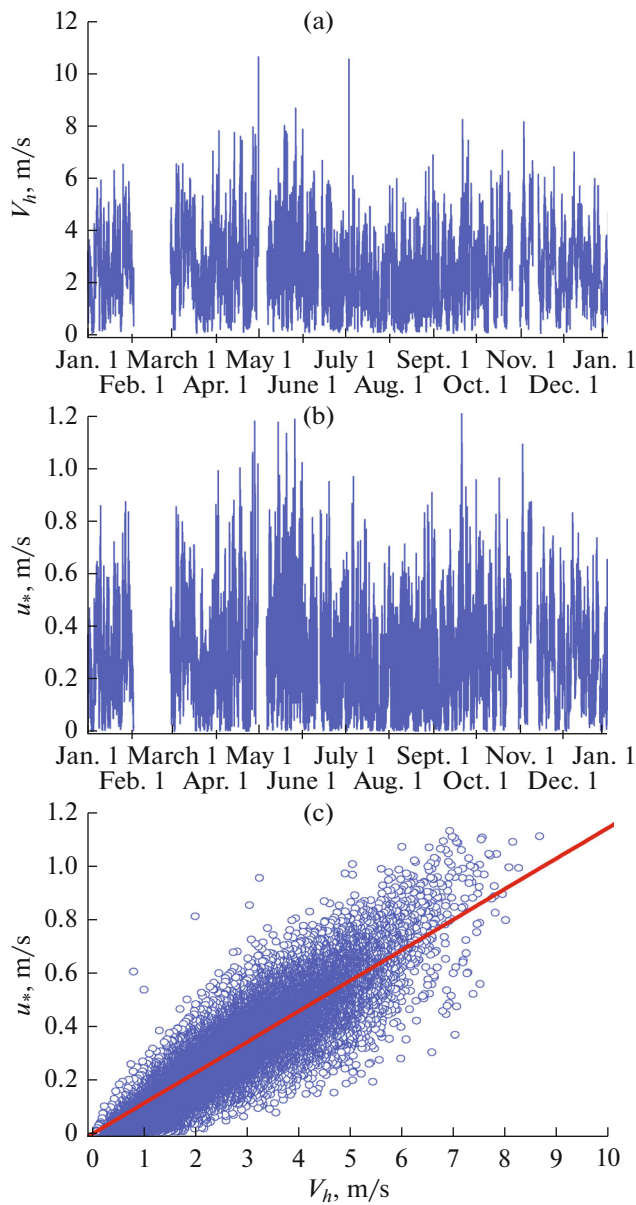
In Eqs. (1) and (2),  $u'$ ,  $v'$ , and  $w'$  are the pulsation components of the longitudinal, cross, and vertical speeds, respectively. The bar above means averaging over a time period. The procedure used for distinguishing the pulsation components of the wind vector is described in [18].

Below, we calculate  $u_*$  by Eq. (1). Let us make one more remark about the “classical” specification of the friction speed: its value should be determined in the immediate vicinity of the underlying surface and correspond to the roughness height (parameter)  $z_0$ , which is approximately equal to 5–15 cm at BEC and 0.5–1 m at IAO (according to the gradation [19] accounting for the season). For  $u_*$  estimates at altitudes  $z > z_0$ , the term “local values” is often used [5]. Later on, we analyze just the local values of  $u_*$ . A detailed study of the measuring altitude dependence of  $u_*$  is an individual problem and is beyond the scope of this work.

The main purpose of the study is to consider a possibility of a rough estimate of the friction speed in the surface air layer based on the known (or predicted) data on the horizontal wind speed at an observation site. This can be useful, for example, in the cases where researchers have information only about the average wind speed at this site. An additional task was to generally consider the effect of such external parameters as the season, time of the day, wind direction, and vertical turbulent heat fluxes on the friction speed.

### RESULTS

Figure 1 provides for general ideas about  $u_*$  and  $V_h$  ranges during the first period of measurements (2019).

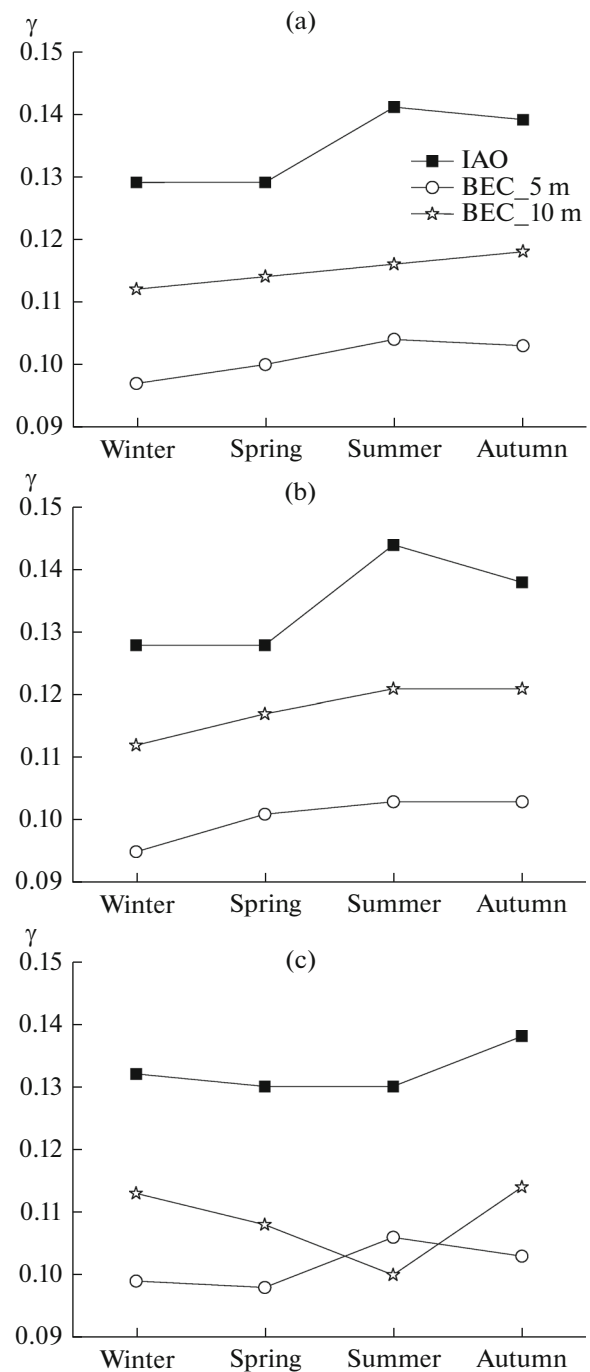


**Fig. 1.** (a) Wind speed and (b) friction speed measured at BEC\_10 m point throughout 2019; (c) dependence of the friction speed on the wind speed throughout the measuring period and its linear approximation (straight line).

It has been plotted for the BEC site at an altitude of 10 m (BEC\_10 m) and shows the relationship between  $u_*$  and  $V_h$  throughout the period and its linear approximation with the determination factor (approximation quality) [20]  $k_d \approx 0.94$ . The determination factor can vary from 0 (bad quality) to 1 (excellent quality).

The main aim of this work is the study of parameters (slopes) of the relationship approximating lines

$$u_*(V_h) \approx \gamma V_h, \quad (3)$$



**Fig. 2.** The approximation parameter versus season from (a) daily (00:00–24:00), (b) daytime (10:00–17:00), and (c) nighttime (22:00–05:00) measurements in 2019.

i.e., the analysis of dependences of the dimensionless factors  $\gamma$  on different conditions. The friction speed is assumed zero at any altitude if  $V_h = 0$ .

An example of approximation of the dependence  $u_*(V_h)$  by Eq. (3) for BEC\_10 m (over 2019) is shown in Fig. 1b (straight line), where  $\gamma = \gamma_{B10} \approx 0.115$ . For BEC\_5 m,  $\gamma = \gamma_{B05} \approx 0.100$ , and for IAO,  $\gamma = \gamma_A \approx 0.133$

**Table 1.** Values of the factors  $\gamma$  and  $k_d$  and the sample length  $T$  (in hours) used for the estimation

| Site     | Time        | Parameter | Winter | Spring | Summer | Autumn |
|----------|-------------|-----------|--------|--------|--------|--------|
| BEC_5 m  | 00:00–24:00 | $\gamma$  | 0.097  | 0.100  | 0.104  | 0.103  |
|          |             | $k_d$     | 0.95   | 0.94   | 0.90   | 0.94   |
|          |             | $T$       | 2616   | 2042   | 2072   | 595    |
|          | 10:00–17:00 | $\gamma$  | 0.0958 | 0.101  | 0.103  | 0.103  |
|          |             | $k_d$     | 0.95   | 0.94   | 0.91   | 0.95   |
|          |             | $T$       | 758    | 595    | 607    | 374    |
|          | 22:00–05:00 | $\gamma$  | 0.099  | 0.098  | 0.106  | 0.103  |
|          |             | $k_d$     | 0.96   | 0.93   | 0.88   | 0.93   |
|          |             | $T$       | 770    | 594    | 603    | 391    |
| BEC_10 m | 00:00–24:00 | $\gamma$  | 0.112  | 0.114  | 0.116  | 0.118  |
|          |             | $k_d$     | 0.95   | 0.95   | 0.91   | 0.94   |
|          |             | $T$       | 2071   | 1909   | 2035   | 1190   |
|          | 10:00–17:00 | $\gamma$  | 0.112  | 0.117  | 0.121  | 0.121  |
|          |             | $k_d$     | 0.96   | 0.96   | 0.92   | 0.95   |
|          |             | $T$       | 603    | 554    | 594    | 339    |
|          | 22:00–05:00 | $\gamma$  | 0.113  | 0.108  | 0.100  | 0.114  |
|          |             | $k_d$     | 0.96   | 0.93   | 0.86   | 0.93   |
|          |             | $T$       | 611    | 561    | 596    | 359    |
| IAO      | 00:00–24:00 | $\gamma$  | 0.129  | 0.129  | 0.141  | 0.139  |
|          |             | $k_d$     | 0.93   | 0.91   | 0.93   | 0.93   |
|          |             | $T$       | 2674   | 1953   | 2129   | 1342   |
|          | 10:00–17:00 | $\gamma$  | 0.128  | 0.128  | 0.144  | 0.138  |
|          |             | $k_d$     | 0.93   | 0.91   | 0.93   | 0.93   |
|          |             | $T$       | 783    | 573    | 620    | 383    |
|          | 22:00–05:00 | $\gamma$  | 0.132  | 0.13   | 0.13   | 0.138  |
|          |             | $k_d$     | 0.93   | 0.92   | 0.93   | 0.93   |
|          |             | $T$       | 780    | 570    | 626    | 400    |

(not shown). A similar analysis, but with addition of a free term in the right part of Eq. (3), was carried out in, e.g., [13, 14]. In particular, estimates for the parameters  $\gamma$  in the range  $\sim 0.05\text{--}0.1$  for altitudes of 5 and 10 m are presented in [13] (measurements were carried out within the CASES-99 experiment in October 1999).

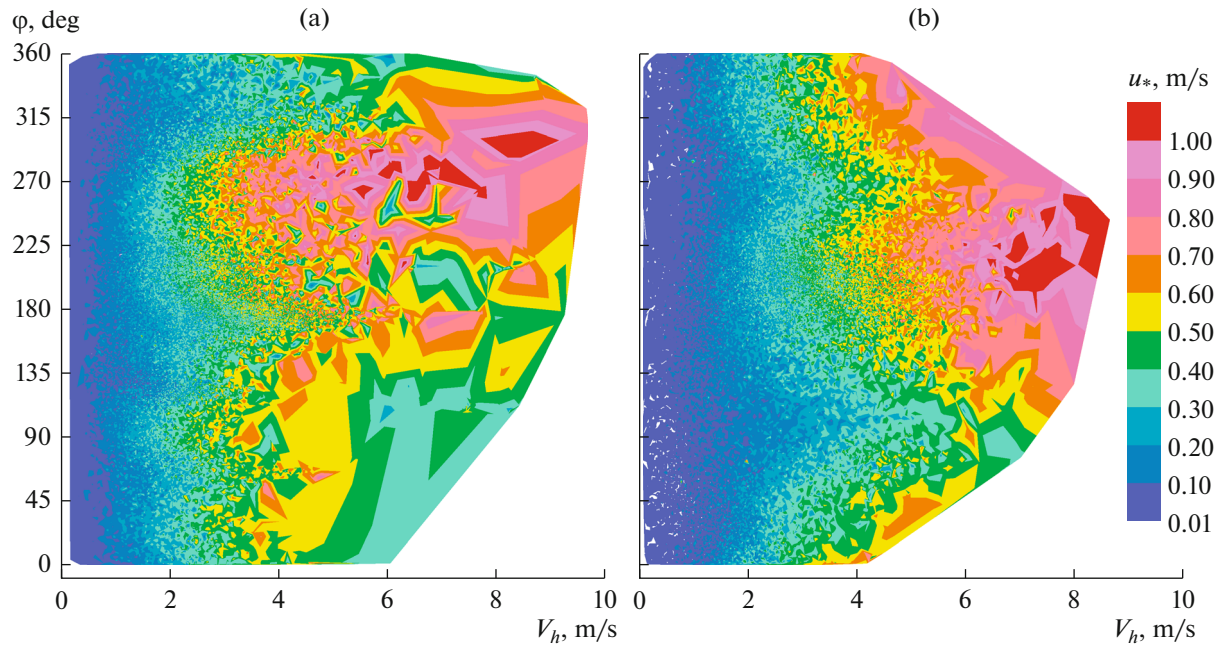
Let us now consider the results for some special cases. First, we consider the estimates of  $\gamma$  in different seasons of 2019: winter (January, February, November, and December), spring (March–May), summer (June–August), and autumn (September–October) (Table 1). The values of  $\gamma$  obtained after such a division are collected in the table. Days are additionally divided into daylight and night hours, which are assumed to be from 10:00 to 17:00 and from 22:00 to 05:00 local time, respectively, for all seasons.

According to the results in Table 1, the quality of the linear approximation of  $u_*(V_h)$  can be generally considered satisfactory, except for measurements in

summer nighttime at the BEC site ( $k_d < 0.9$ ). The statistical reliability of the estimates (the total length of the samples  $T$ , over which the statistics was calculated) can also be considered satisfactory.

For illustrative purposes, the coefficients  $\gamma_A$ ,  $\gamma_{B05}$ , and  $\gamma_{B10}$  are plotted in Fig. 2 versus season and time of day by the data from Table 1. According to Fig. 2, the friction speed most actively increases with the wind speed at the IAO site ( $(\gamma_A > \gamma_{B05}, \gamma_{B10})$  in all seasons and at any time of the day. At the BEC\_10 m point, the friction speed increases faster with the wind speed than at BEC\_5 m, with the exception of the night hours in the summer. Note also that the rate of increase in  $u_*$  with an increase in  $V_h$  is higher in summer and autumn than in winter and spring. This primarily refers to daytime and estimates of  $\gamma$  over 24 h.

The above results are only general estimates of the characteristics of linear approximation (3) of the function  $u_*(V_h)$  and their dependences on the measure-



**Fig. 3.** Correlation between the friction speed and the wind speed and direction at (a) IAO and (b) BEC\_10 m sites ( $\varphi$  is the wind azimuth).

ment site, season, and time of day. For a more detailed study of the wind dependence of the friction speed in the surface air layer, it is necessary to consider not only the wind speed  $V_h$ , but also other wind characteristics, for example, its direction  $\varphi$ . An adequate parameterization of the function  $u_*(V_h)$  is naturally much more difficult to derive in this case, although this can significantly improve the estimate (forecast) of the  $u_*$  value based on the known (predicted) wind speed and direction. We previously used a similar approach when parameterizing the relationship between the turbulence kinetic energy and wind speed [21] and showed its efficiency.

In this work, we did not aim to derive possible parameterizations of the function  $u_*(V_h, \varphi)$ , but only to estimate its general regularities throughout 2019 for observation sites IAO and BEC (measurements at an altitude of 10 m) (Fig. 3).

Certain regularities in the relationship  $u_* \leftrightarrow \varphi$  are obvious at both observation sites which, in principle, can be parameterized. However, the analysis of these dependences has not been carried out during this stage.

The influence of the stratification type in the surface air layer on the relationship  $u_*(V_h)$  can be estimated from Fig. 2, since it shows the values of  $\gamma$  for nighttime (predominantly stable stratification) and daytime (predominantly unstable or indifferent stratification) conditions. Some difference in the rate of increase of  $u_*$  with the wind speed  $V_h$  is obvious in the cases selected.

A more detailed pattern of the relationship  $u_*(V_h, Q_z)$  ( $Q_z$  is the vertical turbulent heat flux,  $W/m^2$ ) at the BEC\_10 m point is shown in Fig. 4. The stratification is stable at negative values of  $Q_z$  and unstable (or close to indifferent) at positive  $Q_z$ . This example does not show a particular effect of  $Q_z$  on  $u_*$ . The features of the pattern near its “boundaries” under weak wind may be connected with insufficient statistical availability of the estimates in these conditions. Therefore, we can conclude that there is no explicit need in accounting for  $Q_z$  in the simplest parameterization of the relationship  $u_*(V_h)$ .

## CONCLUSIONS

Let us formulate the main conclusions from the work.

The main purpose of the analysis was to verify a possibility of rough estimation of the local friction speed (dynamic speed) in the surface air layer based on the measured (or predicted) horizontal wind speed. A linear relationship between these parameters was used for the estimation. As a result, the gradients of the increment of the friction speed were calculated and analyzed for different seasons and different times of the day in an area with a natural landscape at altitudes of 5 and 10 m, as well as in an urbanized area at an altitude of 17 m from the underlying surface. The quality of linear approximation of the dependence under study can be considered satisfactory in almost all cases considered. The resulting estimates of rates of increase

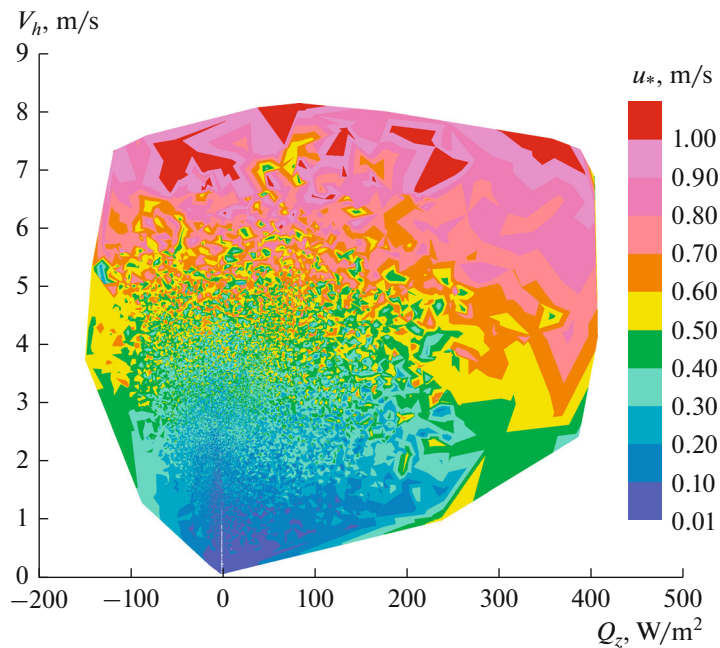


Fig. 4. Correlation between the friction speed and the wind speed and vertical turbulent heat flux at BEC\_10 m point.

coincide in order of magnitude with the results of other authors.

The influence of the wind direction and surface vertical turbulent heat fluxes and the necessity of taking them into account when estimating the friction speed versus the wind speed are briefly considered. It is found that it is desirable to take into account the wind direction, while the effect of turbulent heat flux in the surface air layer can be ignored in this approach.

The results of our work naturally correspond only to specific observation points. However, we hope that the general approach to rough estimation of the friction speed from the average wind speed is applicable to other observation sites.

#### FUNDING

The work was supported by the Russian Ministry of Science and Higher Education (V.E. Zuev Institute of Atmospheric Optics, Siberian Branch, Russian Academy of Sciences). Experimental material was received with the use of equipment of the Common Use Center Atmosfera of the IAO SB RAS.

#### CONFLICT OF INTEREST

The authors declare that they have no conflicts of interest.

#### REFERENCES

1. Y. Dai, S. Basu, B. Maronga, and S. R. de Roode, "Addressing the grid-size sensitivity issue in large-eddy

simulations of stable boundary layers," *Bound.-Lay. Meteorol.* **178** (1), 63–89 (2021).

2. F. Barbano, E. Brattich, and S. Di Sabatino, "Characteristic scales for turbulent exchange process in a real urban canopy," *Bound.-Lay. Meteorol.* **178** (1), 119–142 (2021).

3. G. Tian, B. Conan, and I. Calmet, "Turbulence-kinetic-energy budget in urban-like boundary layer using large-eddy simulation," *Bound.-Lay. Meteorol.* **178** (2) 201–223 (2021).

4. L. I. Kurbatskaya and A. F. Kurbatskii, "Calculation of the turbulent friction velocity in a mathematical model of an urban heat island in a stably stratified environment," *Atmos. Ocean. Opt.* **29** (5), 561–564 (2016).

5. A. F. Kurbatskii, *Introduction in the Simulation of Momentum and Scalar Turbulent Transfer* (GEO, Novosibirsk, 2007) [in Russian].

6. E. A. Panasenko and A. V. Starchenko, "Determination of urban district atmospheric air pollution in accordance with observational data," *Atmos. Ocean. Opt.* **22** (2), 186–191 (2009).

7. V. A. Gladkikh and A. E. Makienko, "Digital ultrasonic weather station," *Pribory*, No. 7, 21–25 (2009).

8. F. Castellvi, K. Suvocarev, M. L. Reba, and B. R. K. Runkle, "Friction-velocity estimates using the trace of a scalar and the mean wind speed," *Bound.-Lay. Meteorol.* **176** (1), 105–123 (2020).

9. S. Mukherjee, P. Lohani, K. Kumar, S. Chowdhuri, T. Prabhakaran, and A. K. Karipot, "Assessment of new alternative scaling properties of the convective boundary layer: application to velocity and temperature spectra," *Bound.-Lay. Meteorol.* **176** (2), 271–289 (2020).

10. B. Maronga, C. Knigge, and S. Raasch, “An improved surface boundary condition for large-eddy simulations based on Monin–Obukhov similarity theory: Evaluation and consequences for grid convergence in neutral and stable conditions,” *Bound.-Lay. Meteorol.* **174** (2), 297–325 (2020).
11. L. G. N. Martins, G. A. Degrazia, O. C. Acevedo, F. S. Puhales, P. E. S. De Oliveira, C. A. Teichrieb, and S. M. Da Silva, “Quasi-experimental determination of turbulent dispersion parameters for different stability conditions from a tall micrometeorological tower,” *J. Appl. Meteorol. Climatol.* **57** (8), 1729–1745 (2018).
12. L. K. Berg, K. R. Newsom, and D. D. Turner, “Year-long vertical velocity statistics derived from Doppler lidar data for the continental convective boundary layer,” *J. Appl. Meteorol. Climatol.* **56** (9), 2441–2454 (2017).
13. J. Sun, D. H. Lenschow, M. A. LeMone, and L. Mahrt, “The role of large-coherent-eddy transport in the atmospheric surface layer based on CASES-99 observations,” *Bound.-Lay. Meteorol.* **160** (1), 83–111 (2016).
14. J. Sun, E. S. Takle, and O. C. Acevedo, “Understanding physical processes represented by the Monin–Obukhov bulk formula for momentum transfer,” *Bound.-Lay. Meteorol.* **177** (1), 69–95 (2020).
15. A. S. Monin and A. M. Yaglom, *Statistical Hydromechanics*. Vol. 1. *Turbulence Theory* (Gidrometeoizdat, St. Petersburg, 1992) [in Russian].
16. *Atmospheric Turbulence and Pollutant Propagation Simulation*, Ed. by F.T.M. N’istadt, H. Van Dop (Gidrometeoizdat, Leningrad, 1985) [in Russian].
17. A. H. Hrgian, *Atmospheric Physics* (Gidrometeoizdat, Leningrad, 1978), vol. 2 [in Russian].
18. V. A. Gladkikh, I. V. Nevzorova, and S. L. Odintsov, “Statistics of outer turbulence scales in the surface air layer,” *Atmos. Ocean. Opt.* **32** (4), 450–458 (2019).
19. L. T. Matveev, *Atmospheric Physics* (Gidrometeoizdat, St. Petersburg, 2000) [in Russian].
20. V. A. Kolemaev, O. V. Staroverov, and V. B. Turundaevskij, *Probability Theory and Mathematical Statistics* (Vysshaya shkola, Moscow, 1991) [in Russian].
21. A. A. Mamysheva and S. L. Odintsov, “Analysis of the dependence of the normalized turbulent kinetic energy on the wind direction and type of stratification in the near-ground atmospheric layer over urbanized territory,” *Atmos. Ocean. Opt.* **25** (5), 377–386 (2012).

*Translated by O. Ponomareva*