**POLYMER BLENDS**

# **Phase Equilibria in a Polystyrene–Poly(butyl acrylate) System**

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**Abstract**—Phase equilibria in polystyrene–poly(*n*-butyl acrylate) systems containing polystyrene of various molecular masses were studied for the first time via optical interferometry at temperatures between 280 and 500 K. The phase diagrams of the systems were obtained, the pair interaction parameters were determined, and the dependences of the parameters on the molecular mass of polystyrene and temperature were found. The possibility of thermodynamic analysis of phase diagrams in terms of the classical Flory–Huggins–Scott theory and the possibility to predict generalized phase diagrams of polystyrene–poly(*n*-butyl acrylate) sys tems on the basis of the experimental values of the pair interaction parameters were shown.

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In recent years, in the field of polymer chemistry, the controlled synthesis of copolymers of a given architecture of the macromolecular chain has been actively investigated. In particular, copolymers of homogeneous compositions and various structures with a narrow molecular-mass distribution—includ ing multiblock, gradient, and random copolymers have been studied  $[1-3]$ . However, in addition to the features of the method used to prepare copolymers [4–6], the data on the intermolecular interaction of the initial homopolymers of the copolymers are of great importance to estimate the properties of the copolymers and the characteristics of their supramo lecular organization [7, 8]. In [9–12], an independent study of the solubilities, thermodynamics of mixing, and phase structures of mixtures of homopolymers was reported to be necessary to obtain the above-men tioned data.

Poly(*n*-butyl acrylate) (PBA) and polystyrene (PS) are one of the pairs of polymers used in the design of pressure-sensitive adhesives [13] and adhesives for var ious purposes [14] as well as in the synthesis of copol ymers with various microstructures of chains [3, 5, 15, 16]. Until recently, these polymers were thought to be completely incompatible [17]. However, this conclu sion was drawn based on the determination of the sol ubilities of melts and solutions of polymers character ized by  $M \ge 10^5$ . For example, the limit of compatibility of PS with  $M = 5.2 \times 10^5$  and PBA with  $M = 1.19 \times$ 105 was found in [18, 19] via the melt-titration tech nique at a temperature of 423 K to be  $\sim 0.001$  wt %. In continuation of these studies, the goal of the present study was to extend the range of measurements and examine in detail the phase equilibrium in the PBA– PS system within a wide range of temperatures and molecular masses of the components.

#### EXPERIMENTAL

PBA and PS with narrow molecular-mass distribu tions (Sigma-Aldrich) were used. Their characteristics are summarized in Table 1.

The solubilities of polymers were examined via the laser interference microscopy method [20, 21]. PS films  $120-150$  µm thick prepared via the pressing technique were used in all measurements.

A convenient measurement technique [22] was used. PS film samples 5 mm  $\times$  10 mm in area were placed between two 5-mm-thick pieces of optically transparent glass with a semitransparent layer of metal (nichrome) characterized by a high coefficient of reflection applied on their inner surfaces via thermal vacuum deposition. A small wedge angle of approxi mately 5° was formed by metal fixators of various thicknesses (for example, 100 and 120 µm for a 120-µm-thick PS film). The samples were brought into optical contact with the inner surfaces of the pieces of glass at a temperature 20–30 K higher than the glass-transition temperature of PS, with the largest

**Table 1.** Characteristics of the studied polymers

Polymer	$M_{\rm n} \times 10^{-3}$	$M_{\rm n}/M_{\rm w}$	$T_{\rm g}^*$ , K	$T^*_{\text{degr}}, K$
<b>PBA</b>	35.0	1.17	223	570
$PS-1$	1.2	1.03	343	550
$PS-2$	2.3	1.07	348	550
$PS-3$	3.6	1.01	353	550
$PS-4$	4.1	1.00	353	550
$PS-5$	30.0	1.02	373	566

\*Obtained from DSC and TGA data.



**Fig. 1.** Temperature dependences of the refractive indexes of (*1*) PS-5, (*2*) PS-3, (*3*) PS-2, (*4*) PS-1, and (*5*) PBA.

side of the sample being placed perpendicularly to the edge of wedge. In this case, the direction of the diffu sion flux coincided with that of the interference bands. The formed cell was placed into a diffusion cell at a temperature controlled with a precision of  $\pm 1$  K. A capillary was then filled with the melt of PBA, and the moment of the contact of PS phase with PBA phase was considered to be the beginning of the diffu sion process.

A helium–neon laser with a wavelength of 632 nm was used as a light source. The interference patterns were recorded with the use of a digital video camera, and the images were transferred to a personal com puter. Measurements were taken in the regime of step wise increases and decreases in temperature from 280 to 500 K. The interference patterns were processed via a convenient technique [21, 22].

The temperature dependences of the refractive indexes of PS and PBA were obtained in the prelimi nary experiments (Fig. 1). At temperatures above  $T_{\rm g}$ , for example, at 380 K for PS-1, the difference between the refractive indexes of PS and PBA was shown to be 0.13 and corresponded to the appearance of approxi mately 42 interference bands in the interdiffusion zone. This result indicates that the increment of the refractive index per band is 0.003 and that the preci sion of measurement of the concentration change between two bands is 2.4 vol %.

## RESULTS AND DISCUSSION

### *Interdiffusion Zones*

Figure 2 shows typical interference patterns of the regions of conjugation of phases, that is, interdiffusion zones between PBA and PS. At temperatures from 363 to 433 K, the interdiffusion zone of samples of PS with  $M_n \geq 3.6 \times 10^3$  is the superposition of three regions: namely, the regions of pure PS and PBA, **I** and **II**, respectively; the phase boundary, **V**; the region of dis solution of PBA in PS, **IV**; and the region of dissolu tion of PS in PBA, **III**.

Under the used isothermal conditions, the concen trations corresponding to the compositions of coexist ing phases,  $\varphi'$  and  $\varphi''$ , that is, the limit solubilities of PBA in PS and PS in PBA at a given temperature, are established on both sides of the phase boundary and remain constant during the whole observation period. The compositions of the coexisting phases at the phase boundary were determined according to the technique used in [23] for the treatment of concentration pro files. This structure of the transition zone character ized by a concentration gradient is general and observed in all studied PS–PBA systems. The specific ities of the various systems consist in the various exten sions of interdiffusion zones and the various numerical values of the compositions of the coexisting phases.

In regions **III** and **IV** of the mixing of components, in contrast to phase boundary **V**, the continuous changes in both the sizes of regions and the profiles of

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**Fig. 2.** Interference patterns (left) and corresponding schematic profiles of the concentration distribution (right) characterizing the interdiffusion zones of PBA and (a) PS-4 at 443 K or (b) PS-1 at 403 K.

the concentration distribution of components within the regions with time are observed. All points of the concentration profiles change their positions along the *X* diffusion coordinate strictly according to the  $X - t^{1/2}$ law of diffusion (Fig. 3); that is, the diffusion mecha nism of mixing of polymers is observed.

An increase in temperature leads to the conver gence of compositions of coexisting phases toward each other at the phase boundary, thereby resulting in degradation of the boundary at the mixing tempera ture. Under these conditions, the interdiffusion zone consists of interference bands smoothly varying after the transition from one pure component to the other (Fig. 2b, region **III**). That is, a single-phase gradient structure is formed.

The subsequent step cooling leads to the appear ance of the phase boundary within the interdiffusion zone, and the regions of amorphous separation spon taneously form near the boundary. These regions are located in a certain area of the concentration profile at a given temperature. During long-term observation at *T* = const, the following stages occur: the formation of local matrix-inclusion dispersed structures in the mentioned zones, complete separation of these struc tures via the Ostwald maturation mechanism, and the final formation of the above-described structure of the interdiffusion zone after heating.

Note that the complete mutual dissolution of the components of systems containing PS with  $M_n \ge 3 \times 10^3$ is not observed up to the decomposition temperatures of the components (Table 1). In this case, the zone of dis solution of PS in PBA that increases with temperature is observed only (Fig. 2a, region **III**). The limit of solubility of PBA in the PS matrix (Fig. 2a, region **IV**) does not exceed ~5 vol %, even at high temperatures.

#### *Phase Diagrams*

Binodal curves of the diagrams of amorphous sep aration of PS–PBA systems were plotted at various



**Fig. 3.** Kinetics of motion of the diffusion front of (*1*, *3*) PS in PBA and (*2*, *4*) PBA in PS measured at (*1*, *2*) 413 K and  $(3, 4)$  423 K.



**Fig. 4.** Phase diagrams of PBA–PS systems containing (*1*) PS-1, (*2*) PS-2, (*3*) PS-3, (*4*) PS-4, and (*5*) PS-5. Experimental data were obtained during (black circles) heating and (white circles) cooling, and (dashed lines) the binodal domes of curves *3* and *4* were calculated with the use of the program PhaDiag.

temperatures on the basis of the compositions of coex isting phases (Fig. 4). Analysis of these dependences makes it possible to make the following conclusions. First, the data on the compositions of coexisting phases obtained after step heating agree well with those obtained after step cooling, a result that suggests the reproducibility and equilibrium of the boundary curves. Second, in all cases, the solubilities of poly mers increase with an increase in temperature. This circumstance indicates the presence of the upper crit ical solution temperature (UCST) in the studied sys tems. The UCST was experimentally determined only in the case of PS with  $M_n < 3 \times 10^3$  (Fig. 4). Third, the positions of the binodal domes depend on the molec ular mass of PS. Systems containing oligomeric PSs— PS-1 and PS-2—show complete solubility at temperatures above 403 and 443 K, respectively. For other systems, the binodal domes are located in the region of high temperatures close to the region of thermal deg radation of polymers (Fig. 4, Table 1).

The thermodynamic analysis of the experimental data was performed under the following assumptions. The following relationships exist between the chemi cal potentials of components for all compositions of coexisting phases of binodal curves:

$$
\Delta \mu'_1 = \Delta \mu''_1 \quad \text{and} \quad \Delta \mu'_2 = \Delta \mu''_2,
$$

where  $\Delta \mu_i$  is the change in the chemical potential of the *i*th component in the first  $(\Delta \mu_i)$  and second  $(\Delta \mu_i)$ phases.

Expressions for the chemical potentials of compo nents are derived from the Flory–Huggins–Scott the ory of polymer solutions [24] with allowance for the



**Fig. 5.** Temperature dependences of the pair interaction parameters for PBA and (*1*) PS-2, (*2*) PS-4, and (*3*) PS-5 with arrows indicating the UCST positions.

concentration dependence of the pair interaction parameter,  $\chi(\varphi_i)$ ):

$$
\ln \varphi_1' + \left(1 - \frac{r_1}{r_2}\right) \varphi_2' + r_1 \chi_{12} (\varphi_2')^2
$$
\n
$$
= \ln \varphi_1'' + \left(1 - \frac{r_1}{r_2}\right) \varphi_2' + r_1 \chi_{12} (\varphi_2'')^2
$$
\n
$$
\ln \varphi_2' + \left(1 - \frac{r_2}{r_1}\right) \varphi_1' + r_2 \chi_{21} (\varphi_1')^2
$$
\n
$$
= \ln \varphi_2'' + \left(1 - \frac{r_2}{r_1}\right) \varphi_1'' + r_2 \chi_{21} (\varphi_1'')^2
$$
\n(2)

where  $r_i$  is the degree of polymerization of a component,  $\varphi_i$  is the volume fraction of the *i*th component in the first phase,  $\varphi_i$  is the volume fraction of the *i*th component in the second phase,  $\chi_{12} = \chi + \frac{\partial \chi}{\partial \varphi_1}$ ,  $\chi_{21} = \chi + \frac{\partial \chi}{\partial \varphi_2}$ , and  $\chi$  is the pair interaction parameter.

**Table 2.** Thermodynamic characteristics of systems at the critical point

<b>PS</b>	$M_{\rm n} \times 10^{-3}$	$\chi_{\text{crit}}$ (calculated)	$T_{\text{crit}}$ , K
	1.2	0.063	403/397*
2	2.3	0.037	443/446*
3	3.6	0.027	$510*$
	4.1	0.024	$523*$
	30.0	0.007	559*

\* Values calculated via the described technique.



**Fig. 6.** Dependences of the pair interaction parameter of PBA and PS on the molecular mass of PS at (*1*) 380, (*2*) 400, (*3*) 420, and (*4*) 450 K with triangles indicating points calculated via the proposed technique for a PS with  $M_n =$  $1.5 \times 10^{4}$ .

The solutions to Eqs. (1) and (2) with respect to  $\chi_{12}$ and  $\chi_{21}$  lead to the following equations:

$$
\chi_{12} = \frac{\ln \varphi_1 - \ln \varphi_1'}{r_1((\varphi_2')^2 - (\varphi_2'')^2)} - \left(\frac{1}{r_1} - \frac{1}{r_2}\right) \frac{1}{\varphi_2' + \varphi_2'},\tag{3}
$$

$$
\chi_{21} = \frac{\ln \varphi_2 - \ln \varphi_2}{r_2(\left(\varphi_1'\right)^2 - \left(\varphi_1''\right)^2)} - \left(\frac{1}{r_2} - \frac{1}{r_1}\right) \frac{1}{\varphi_1' + \varphi_1''}. \tag{4}
$$

The parameters of the critical point are determined by the following equation [23]:

$$
\chi_{\rm cr} = \frac{1}{2} \left( \frac{1}{\sqrt{r_1}} + \frac{1}{\sqrt{r_2}} \right)^2.
$$
 (5)

The numerical  $\chi_{12}$  and  $\chi_{21}$  values of the PS–PBA system were calculated through Eqs. (3) and (4) on the basis of the composition of the coexisting phases. Note that the obtained  $\chi_{12}$  and  $\chi_{21}$  values actually coincide. This result indicates the absence of the concentration dependence of the pair interaction parameters of the components in the system.

The temperature dependences of  $\chi$  are shown in Fig. 5. The values of the pair interaction parameter change within the relatively narrow range 0.01–0.07. All of the studied systems show linear dependences of  $\chi$  on  $T^{-1}$ , with the extrapolation of the latter to the critical conditions (Eq. (5)) making it possible to esti mate the UCST values. These values are close to those measured experimentally (Table 2). The slopes of the temperature dependences are positive, a circumstance that is typical of systems characterized by the presence of the UCST.



Fig. 7. Calculated generalized phase diagram of the PBA–PS-2 system with indicated (*1*) binodal and (*2*) spinodal positions of the  $T_g$  values of (3) PS and (4) PBA, and (5) the line of destruction of components.

The dependences of the pair interaction parame ters on the molecular mass of PS at various tempera tures are summarized in Fig. 6. Parameter  $χ$  decreases with an increase in the molecular mass of PS, asymp totically approaching the limit  $\chi_{\infty}$  values of approximately 0.03 at 450 K and 0.04 at 400 K.

On the basis of the temperature dependences of  $χ$ , binodal and spinodal curves were calculated and gen eralized phase diagrams were obtained. The results suggest that the examined systems follow the classical Flory–Huggins–Scott theory. Figure 7 shows that the generalized diagram of the oligomeric PS-2–PBA sys tem includes the critical point and the binodal and spinodal curves dividing the temperature and concen tration field into the region of true solutions, **I**; the region of metastable states, **II**; and the region of labile solutions, **III**. In addition, the diagram contains data on the values of the glass-transition temperatures of PS and PBA; region **IV** of the vitrification of the com ponents of the system; and boundary dashed line *5*,

separating region **V** of the thermal degradation of polymers and their compositions.

In conclusion, it was shown that the phase behavior of PBA–PS systems may be predicted in a wide range of molecular masses of the components on the basis of the dependences of the pair interaction parameters on temperature and molecular mass. Therefore, the boundary curves of the diagrams of the phase and physical states of the previously studied PS–PBA sys tem [18] containing polymers of high molecular masses (PS of  $M = 5.2 \times 10^5$  and PBA of  $M = 1.19 \times$ 10<sup>5</sup>) were calculated. Note that the dependence of  $χ$ on  $T^{-1}$  (Fig. 5) was used in all calculations after its extrapolation to the values at the critical point. The obtained diagrams (solid and dashed lines) and the lit erature data (point *2*) [18, 19] are shown in Fig. 8. The calculated binodal and spinodal curves are located in the region of infinitely dilute solutions. This result agrees well with the experimental data previously obtained in [18, 19].



**Fig. 8.** (*1*) Calculated spinodal and (*2*) experimental data [18] for the PS–PBA system containing PS with  $M = 5.2 \times$  $10<sup>5</sup>$  and PBA with  $M = 1.19 \times 10<sup>5</sup>$ . Regions **II** and **III** correspond to those in Fig. 7.

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