PHYSICOCHEMICAL ANALYSIS OF INORGANIC SYSTEMS

Solid–Liquid Phase Equilibria of the Quaternary System − Na^+ , Mg²⁺//Cl⁻, B₄O²⁻–H₂O at 298.15 K

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 ${\rm Abstract-Solubility}$ data for the quaternary system ${\rm Na}^+$, ${\rm Mg}^{2+}//C l^-$, ${\rm B_4O}_7^{2-}$ ${\rm H_2O}$ is very important for the separation of magnesium and boron from the salt lake brines in Qaidam Basin. The solubility of the quater-

nary system Na⁺, Mg²⁺//Cl⁻, B₄O₇²⁻-H₂O at *T* = 298.15 K and *p* = 0.1 MPa was investigated experimentally with the method of isothermal dissolution equilibrium, and meanwhile physicochemical properties including density, refractive index and pH value were determined. In the phase diagrams of the quaternary system at 298.15 K, there are two invariant points, five univariant isothermal dissolution curves, and four crystallization regions corresponding to NaCl, Na_2BaO_7 10H₂O, $MgCl_2$ 6H₂O and $Mg_2B_6O_{11}$ 15H₂O, respectively. The density, refractive index and pH value of the quaternary system at 298.15 K present a regular variation with the increasing of Mg^{2+} concentration.

Keywords: stable phase equilibrium, phase diagram, borate, inderite **DOI:** 10.1134/S0036023622040064

INTRODUCTION

Boron compounds have an important application in glass, ceramics, chemical industry, light industry, nuclear industry and so on because of its own merits: light weight, high strength, heat resistance and other good properties [1]. All aspects of national production and life are inseparable from lithium metal and its compounds, ranging from traditional fields such as glass, metallurgy and ceramics to other front-end fields including aerospace and new energy [2–4]. As the available amounts of solid ores are decreasing, the development of liquid borate mineral resources has become an inevitable tendency in future. Liquid mineral resources are mainly distributed in salt lake brine, seawater, geothermal water, and oil-field water. There are abundant salt lake brine resources in the Qaidam Basin, China with high contents of lithium, magnesium, and boron, which is of great exploitation potential and strategic importance [5, 6].

Due to the change of the coordination number of borate ion B–O, the structure of borate ion in solution is complex and the existing forms are various, such as metaborate (BO_2^-) , diborate $(B_2O_4^{2-})$, triborate $(B_3O_5^-)$, and polytetraborate $(B_4O_7^{2-}, B_6O_{10}^{2-})$ [7]. The existing form of boron depends on its concentration

and external conditions, such as coexisting ion species, concentration, pH value, and temperature [8]. The study of the multi-temperature phase diagram is great significance to the development of salt lake brine resources. Therefore, the multi-temperature phase diagram of subsystem containing borate has been studied and reported, such as the ternary system $(Na^+,$ $Mg^{2+}//B_4O_7^{2-} - H_2O$ [9], $(Li^+, Mg^{2+}//B_4O_7^{2-} - H_2O)$, Na^+ , $\text{Mg}^{2+} / / \text{B}_4\text{O}_7^{2-} - \text{H}_2\text{O}$) [10], $(\text{Mg}^{2+} / / \text{Cl}^-$, $\text{B}_4\text{O}_7^{2-} H_2O$, Mg^{2+} //Cl⁻, $B_6O_{11}^{2-}$ -H₂O) [11, 12] and (K⁺//Cl⁻, $B_4O_7^{2-}$ -H₂O, K⁺//SO₄², B₄O₇²⁻-H₂O) [13], the quaternary system $(K^+//Cl^-, SO_4^{2-}, B_4O_7^{2-} - H_2O)$ [14], $(Li^+, Na^+, Mg^{2+}//B_4O_7^{2-}-H_2O)$ [15–17], $(Mg^{2+}//Cl^-,$ SO_4^{2-} , $B_4O_7^{2-}$ -H₂O) [18] and (Na⁺, K⁺, Mg²⁺// $B_4O_7^{2-} - H_2O$) [19], the quinary system (Na⁺, K⁺, Mg^{2+} //SO $_4^{2-}$, B₄O $_7^{2-}$ -H₂O) [20], and the complex system (Li⁺, K⁺, Rb⁺, Mg²⁺//SO₄²⁻, B₄O₇²⁻–H₂O) [21]. In order to better separate and purify the sodium, magnesium and borate containing resource from salt-lake brine, the isothermal solubilities and the corresponding solution physicochemical properties including density, refractive index and pH value for the quaternary system Na⁺, Mg²⁺//Cl⁻, B₄O₇²-H₂O at *T* = 298.15 K and $p = 0.1$ MPa were presented in this paper.

EXPERIMENTAL

Apparatus and reagents. A magnetic stirring thermostatic water bath (HXC-500-8A, Beijing Fortunejoy Sci. Technol. Co., Ltd.) was used to control the temperature with a precision of 0.01 K. For determining the densities (ρ) , a digital densimeter (DMA 4500, Anton Paar Co., Ltd.) that can automatically control the sample cell temperature within 0.01 K was applied with a precision of ± 0.15 mg cm⁻³. In order to measure the refractive index (n_D) , an Abbe refractometer (Abbemat 550, Anton Paar Co., Ltd.) with a precision of ± 0.0001 was used. The pH value was determined by a high precision PHSJ-5 pH meter (Shanghai Precision Scientific Instruments Co. Ltd., China) with an accuracy of ± 0.01 . Solid phase was identified by the X-ray powder diffractometer (MSAL XD-3, Beijing Purk Instrument Co., Ltd.).

The chemicals of analytical grade were obtained from the Sinopharm Chemical Reagent Co., Ltd: NaCl (0.995 in mass fraction), MgCl₂·6H₂O (0.992 in mass fraction), $Na₂B₄O₇$ 10H₂O (0.992 in mass fraction), and were recrystallized with doubly deionized water (DDW) before use. The hungtsaoite $(MgB_4O_7.9H_2O,$ 0.99 in mass fraction) were synthesized in our lab [22]. Doubly deionized water (DDW) with conductivity less than 1×10^{-4} S m⁻¹ was used to prepare the series of the artificial synthesized brines and chemical analysis.

Method. The equilibrium experiment in this work was conducted by the method of isothermal dissolution equilibrium [23, 24]. In briefly, the series of artificial synthesized complexes are sealed in hard polyethylene bottles and placed in the magnetic stirring thermostatic bath (HXC-500-8A). The temperature of the bath was checked with a separate thermometer, and the standard deviation of the temperature for 1 day was less than 0.1 K. In order to accelerate the establishment of equilibrium states, the magnetic stirring thermostatic bath was set 150 rpm stirring speed. At regular intervals, the magnetic stirring was paused for 4 h to probe for chemical analysis, and when the composition of the sample became constant, it indicated that the equilibrium had been achieved. It took about 10 days to reach equilibrium for this system. And then, the corresponding solution physicochemical properties including ρ , pH, and n_D were determined, samples of the liquid phase were taken for chemical analysis. In addition, the solid phase minerals were identified with the X-ray powder diffraction.

The concentration of Cl^- in liquid phase was analyzed by titration with $AgNO₃$ standard solution in the presence of potassium chromate indicator. The concentration of boron in liquid phase was analyzed by the gravimetric methods of mannitol with sodium hydroxide standard solution in the presence of double indicator of methyl red and phenolphthalein. The Mg^{2+} ion concentration was determined with modified EDTA complexometric titration method in the presence of Eriochrome Black-T as an indicator, and the uncertainty of the analytical results is less than ± 0.003 in mass fraction. The $Na⁺$ ion concentration was evaluated according to ion balance.

RESULTS AND DISCUSSION

Phase Diagram of the Quaternary System

$$
Na^{+}, Mg^{2+}//Cl^{-}, B_4O_7^{2-} - H_2O
$$

The experimental data on the solubilites of the quaternary system Na^+ , $Mg^{2+}//Cl^-$, $B_4O_7^{2-}$ -H₂O at 298.15 K were determined and are presented in Table 1. The composition of the liquid phase in the quaternary system was expressed in mass fraction (w_b) and Jänecke index $[J_b/(mol/100 mol)]$, with $J(2Na⁺)$ + $J(Mg^{2+}) = 100$. The calculating formula for J_b is

$$
J_{\rm b} = \frac{n_{\rm b}}{n(2\text{Na}^+) + n(\text{Mg}^{2+})} \times 100.
$$

The calculating formula for water concentration is

$$
J(\mathrm{H}_{2}\mathrm{O}) = \frac{w_{(\mathrm{H}_{2}\mathrm{O})}}{18.0153[n(2\mathrm{Na}^{+}) + n(\mathrm{Mg}^{2+})]} \times 100.
$$

The *J* refers to the calculated Jänecke indices of different substances, which reflects the percentage of various ions or water relative to the total equivalent valence moles of cations (anions) based on the principle of equivalent mole valence in the reciprocal quaternary system.

On the basis of the experimental data in Table 1, the phase diagrams of the quaternary system at 298.15 K were plotted, as shown in Figs. 1 and 2. In Fig. 1, the dry-salt phase diagram consists of four crystallization zones corresponding to sodium chloride (NaCl), bischofite (MgCl₂·6H₂O), borax (Na₂B₄O₇·10H₂O) and inderite $(Mg_2B_6O_{11} \cdot 15H_2O)$. Hungchaoite $(MgB₄O₇·9H₂O)$, an incongruently dissolved solid, represents a metastable phase, which easily convert to $Mg_2B_6O_{11}$ 15H₂O in this system. As can be seen in Fig. 1, because of the transformation of equilibrium solid phase from hungchaoite ($MgB_4O_7.9H_2O$) to inderite $(Mg_2B_6O_{11}$ ^{-15H₂O) with low solubility, the crystalliza-} tion field of $Mg_2B_6O_{11}$ 15H₂O is the largest, while the $MgCl₂·6H₂O$ is the smallest. The size of the mineral crystallization zone is in the order $Mg_2B_6O_{11}$ 15H₂O > $NaCl > Na₂B₄O₇$: 10H₂O > MgCl₂·6H₂O. With increasing of the temperature, the solubilities of different salts have changed in the system, which may be shown on the changes of the crystallization fields. To explaining the causes of the formation of the salt and

Ind $-Mg_2B_6O_{11}$ ·15H₂O, Borax—Na₂B4 $_2O$, Ha—Na2 $_2$ O, Ha $_3$ —Na $_2$ B₄Cl₃·6H₂·6H₂O. –, Not detected.

Fig. 1. Dry-salt phase diagram of the quaternary system $(Na^+, Mg^{2+} // CI^-, B_4O_7^{2-} - H_2O)$ at 298.15 K; (•) liquid phase, (–) isotherm curve.

the order of crystallization zone in the salt-water system would help choose the best stage for extracting one component or another from the brines in developing technological processes.

There are five univariant curves corresponding to E_1F_1 (Na₂B₄O₇·10H₂O + NaCl), E_2F_1 $(Mg_2B_6O_{11} \cdot 15H_2O + Na_2B_4O_7 \cdot 10H_2O)$, $F_1F_2(NaCl +$ $Mg_2B_6O_{11}$ 15H₂O), E_3F_2 (MgCl₂·6H₂O + NaCl) and F_2E_4 (Mg₂B₆O₁₁·15H₂O + MgCl₂·6H₂O), indicating the cosaturation of two salts, respectively.

Three invariant points F_1 and F_2 cosaturated with three minerals are marked as follows:

Point F_1 is saturated with salts NaCl + $Na_2B_4O_7$ 10H₂O + $Mg_2B_6O_{11}$ 15H₂O. The mass fraction composition of the corresponding liquid phase is $w(Na^+) = 10.34\%, w(Mg^{2+}) = 0.05\%, w(Cl^-) =$ 15.80% , $w(B_4O_7^{2-}) = 0.64\%$, and $w(H_2O) = 73.17\%$.

Point F_2 is saturated with salts NaCl + $MgCl₂·6H₂O + Mg₂B₆O₁₁·15H₂O$. The mass fraction composition of the corresponding liquid phase is $w(Na^+) = 0.27\%$, $w(Mg^{2+}) = 7.79\%$, $w(Cl^-) = 22.78\%$, $w(B_4O_7^{2-}) = 0.79\%$, and $w(H_2O) = 68.37\%$.

In Fig. 2, the ordinate is the Jänecke index of water, and the abscissa is the Jänecke index of magnesium. It can be further found that Jänecke index values of $J(H₂O)$ are changed regularly with the change of $J(Mg²⁺)$, and have singularity changes at the invariant points. As can be seen in Fig. 2, the values of $J(H_2O)$ in the univariant solubility isothermal curve of E_2F_1 are decreased sharply with increasing of $J(Mg^{2+})$ at

Fig. 2. Water-phase diagram of the quaternary system $(Na^+, Mg^{2+} // Cl^-, B_4O_7^{2-} - H_2O)$ at 298.15 K.

298.15 K. On the univariant solubility isothermal curves of F_1F_2 , F_2E_3 and F_2E_4 , the values of $J(H_2O)$ are gradually decreased with the increase of $J(Mg^{2+})$.

Figure 3 shows the identification results of the solid phase minerals using an X-ray diffractometer. Figure 3a shows the XRD pattern of mineral $Mg_2B_6O_{11}$ 15H₂O. Figure 3b shows the XRD pattern of point F_1 , which was well matched to the standard diffraction pattern of NaCl, $Na_2B_4O_7$ 10H₂O and $Mg_2B_6O_{11}$ 15H₂O with powder diffraction file (pdf) nos. 02-0818, 12-0258, and 11-0583, respectively.

Solution Physicochemical Properties of the Quaternary System

The solution physicochemical properties including density, refractive index and pH value of the quaternary system Na⁺, Mg²⁺//Cl⁻, B₄O²⁻ $-H_2$ O at 298.15 K were determined and are presented in Table 1, and the diagram of solution density, refractive index and pH value with the concentration of $J(Mg^{2+})$ were plotted in Fig. 4.

In Figs. 4a, 4b, solution density and refractive index have the same tendency. The density values of the equilibrium liquid phase increased gradually with the increasing concentration of $J(Mg^{2+})$ in the solubility isotherm curves of E_2F_1 , F_1F_2 , and F_2E_3 because of the addition of the other salt, and decreased with the increasing concentration of $J(Mg^{2+})$ in the solubility isotherm curves of E_1F_1 and F_2E_4 .

Figure 4c shows the pH value versus composition of $J(Mg^{2+})$ in the solution. The pH values of the equilibrium liquid phase increased gradually with the increasing concentration of $J(Mg^{2+})$ in the solubility isotherm curves of E_1F_1 , F_2E_4 , and F_2E_3 , and

Fig. 3. X-ray diffraction pattern of solid phases: (a) $Mg_2B_6O_{11}$: 15H₂O, (b) $(Na_2B_4O_7$: 10H₂O + $Mg_2B_6O_{11}$: 15H₂O + NaCl).

decreased with the increasing concentration of $J(Mg^{2+})$ in the solubility isotherm curve of E_2F_1 and F_1F_2 . On the curves of E_2F_1 and F_1F_2 , the pH values of the equilibrium liquid phase decreased gradually because of the increase of total Mg^{2+} molality in the solution with dissolving of $MgCl₂$.

CONCLUSIONS

Solid-liquid phase equilibria of the quaternary sys-

tem Na⁺, Mg²⁺//Cl⁻, B₄O₇²⁻-H₂O at 298.15 K were investigated using the isothermal dissolution method. Solubilities and physicochemical properties including density, refractive index and pH value were measured experimentally. Phase diagram of the quaternary system consist of two invariant point and four crystallization regions corresponding to NaCl, $MgCl₂·6H₂O$, $Na₂B₄O₇$ 10H₂O and $Mg₂B₆O₁₁$ 15H₂O, respectively. The size of crystallization areas of salt is in the order $Mg_2B_6O_{11}$ 15H₂O > NaCl > Na₂B₄O₇ 10H₂O > $MgCl₂·6H₂O$. Hungchaoite $(MgB₄O₇·9H₂O)$, an incongruently dissolved solid, represents a metastable phase, which easily convert to $Mg_2B_6O_{11}$ 15H₂O. The solution density and refractive index in the quaternary system changed regularly with increasing of $J(Mg^{2+})$ concentration in the solution. This phase diagram can be used to guide the separating process of magnesium and boron salts from the salt lake brine.

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CONFLICT OF INTEREST

The authors declare that they have no conflicts of interest.

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