

## Phase Equilibria in the $\text{Tl}_5\text{Te}_3$ – $\text{Tl}_9\text{BiTe}_6$ – $\text{Tl}_9\text{TbTe}_6$ System

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**Abstract**—Phase equilibria in the  $\text{Tl}_5\text{Te}_3$ – $\text{Tl}_9\text{BiTe}_6$ – $\text{Tl}_9\text{TbTe}_6$  system have been studied using differential thermal analysis, X-ray diffraction, and microhardness measurements. We have mapped out a number of vertical sections, the 760-K isothermal section of its phase diagram, and projections of its liquidus and solidus surfaces. The composition dependences of lattice parameters and microhardness have been obtained. The system has been shown to contain a continuous series of solid solutions, which crystallize in a tetragonal structure ( $\text{Tl}_5\text{Te}_3$  type, sp. gr.  $I4/mcm$ ).

**Keywords:** thallium tellurides, terbium tellurides, thallium bismuth tellurides, phase equilibria, liquidus surface, solid solutions, crystal lattice

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### INTRODUCTION

Chalcogenides of heavy  $p$ -block elements have attracted researchers' attention as functional materials possessing interesting optical, photoelectric, thermoelectric, and other properties [1–3]. Some of them are topological insulators and are thought to be potentially attractive for use in spintronics and quantum computers [4, 5]. Rare-earth tellurides are widely used in the fabrication of electronic devices, such as microbatteries and highly efficient multilayer solar cells [6]. According to *ab initio* calculation results [7],  $\text{LaBiTe}_3$  is a topological insulator and possesses thermoelectric properties [8].

The thallium telluride  $\text{Tl}_5\text{Te}_3$  has thermoelectric properties and is the most suitable parent compound for engineering novel composition materials. This compound crystallizes in tetragonal symmetry (sp. gr.  $I4/mcm$ ,  $a = 8.930 \text{ \AA}$ ,  $c = 12.598 \text{ \AA}$ ,  $Z = 4$ ) [9] and, owing to some specific features of its crystal structure, has a number of ternary analogs with the general formulas  $\text{Tl}_4\text{A}^{\text{IV}}\text{Te}_3$  ( $\text{A}^{\text{IV}} = \text{Sn}, \text{Pb}$ ) and  $\text{Tl}_9\text{B}^{\text{V}}\text{Te}_6$  ( $\text{B}^{\text{V}} = \text{Sb}, \text{Bi}$ ) [10–12].

These compounds possess thermoelectric properties [13–16], and  $\text{Tl}_9\text{BiTe}_6$  offers a record high thermoelectric performance ( $ZT = 1.2$  at 500 K) [15]. Moreover, according to Arpino et al. [17]  $\text{Tl}_5\text{Te}_3$  and  $[\text{Tl}_4](\text{Tl}_{1-x}\text{Sn}_x)\text{Te}_3$  have surface topological states.

The existence of  $\text{Tl}_9\text{LnTe}_6$ -type compounds—new structural analogs of  $\text{Tl}_5\text{Te}_3$ —was first demonstrated by Imamaliyeva et al. [18] and Babanly et al. [19]. They identified the melting behavior of these compounds and determined their melting points and lattice parameters. Data on their physical properties demonstrate that these compounds possess thermoelectric and magnetic properties [20–22].

To obtain complex phases of variable composition with the  $\text{Tl}_5\text{Te}_3$  structure, Babanly et al. [23] and Imamaliyeva et al. [24, 25] studied phase equilibria in systems of  $\text{Tl}_5\text{Te}_3$  and its analogs and identified continuous series of substitutional solid solutions.

As a continuation of our previous studies of such systems, this work focuses on the phase equilibria in the  $\text{Tl}_5\text{Te}_3$ – $\text{Tl}_9\text{BiTe}_6$ – $\text{Tl}_9\text{TbTe}_6$  system.

The constituent tellurides of this system have been the subject of extensive studies. The  $\text{Tl}_9\text{BiTe}_6$  compound melts congruently at 830 K and has a broad homogeneity range [11]. Doert and Böttcher [26] investigated the crystal structure of this compound and refined its lattice parameters:  $a = 8.855 \text{ \AA}$  and  $c = 13.048 \text{ \AA}$  ( $Z = 2$ ). The  $\text{Tl}_9\text{TbTe}_6$  compound decomposes peritectically at 780 K and crystallizes in tetragonal symmetry with lattice parameters  $a = 8.871 \text{ \AA}$  and  $c = 12.973 \text{ \AA}$  ( $Z = 4$ ) [27]. The constituent binary systems  $\text{Tl}_5\text{Te}_3$ – $\text{Tl}_9\text{BiTe}_6$  [11] and  $\text{Tl}_5\text{Te}_3$ – $\text{Tl}_9\text{TbTe}_6$  [28] of

Some properties of the constituent tellurides and solid solutions of the  $\text{Tl}_9\text{TbTe}_6$ – $\text{Tl}_9\text{BiTe}_6$  system

Phase	Thermal events during heating, K	Tetragonal lattice parameters, Å		$H_\mu$ , MPa
		<i>a</i>	<i>c</i>	
$\text{Tl}_9\text{TbTe}_6$	780, 1110	8.871(2)	12.973(5)	1000
$\text{Tl}_9\text{Bi}_{0.2}\text{Tb}_{0.8}\text{Te}_6$	783–803, 1046	8.868(3)	12.985(6)	1090
$\text{Tl}_9\text{Bi}_{0.4}\text{Tb}_{0.6}\text{Te}_6$	790–815	8.864(2)	13.001(5)	1070
$\text{Tl}_9\text{Bi}_{0.6}\text{Tb}_{0.4}\text{Te}_6$	800–822	8.861(2)	13.015(6)	1060
$\text{Tl}_9\text{Bi}_{0.8}\text{Tb}_{0.2}\text{Te}_6$	805–825	8.858(4)	13.031(7)	1030
$\text{Tl}_9\text{BiTe}_6$	830	8.855(3)	13.048(5)	980

The error of determination was 3–4 K in the temperatures of thermal events and 20 MPa in microhardness.

the ternary system under investigation contain continuous series of solid solutions with the  $\text{Tl}_5\text{Te}_3$  structure.

### EXPERIMENTAL

The congruently melting compounds  $\text{Tl}_5\text{Te}_3$  (723 K) and  $\text{Tl}_9\text{BiTe}_6$  (830 K) were synthesized by melting elemental thallium, tellurium, and bismuth at temperatures slightly (30–50 K) above their melting points in silica ampules pumped down to  $\sim 10^{-2}$  Pa, followed by slow cooling (furnace-cooling). Given that  $\text{Tl}_9\text{TbTe}_6$  melts incongruently [27, 28], the as-prepared, inhomogeneous cast alloy was ground into powder, thoroughly mixed, and pressed into a disk, which was then annealed at 750 K for 1000 h. All of the synthesized

compounds were identified by differential thermal analysis (DTA) and X-ray diffraction.

Alloys of the  $\text{Tl}_5\text{Te}_3$ – $\text{Tl}_9\text{BiTe}_6$ – $\text{Tl}_9\text{TbTe}_6$  system were prepared by melting the presynthesized constituent tellurides under vacuum. Given that even prolonged (1000 h) homogenizing annealing of the as-cast alloys failed to ensure equilibration of the samples, by analogy with previous studies the as-cast alloys were ground into powder, thoroughly mixed, and pressed into disks, which were then fired at 700 K for  $\sim 800$  h.

DTA heating curves were obtained in the range from room temperature to  $\sim 1400$  K at a heating rate of 10 K/min using a Netzsch 404 F1 Pegasus differential scanning calorimeter system. The crystal structure of the constituent tellurides and intermediate alloys was

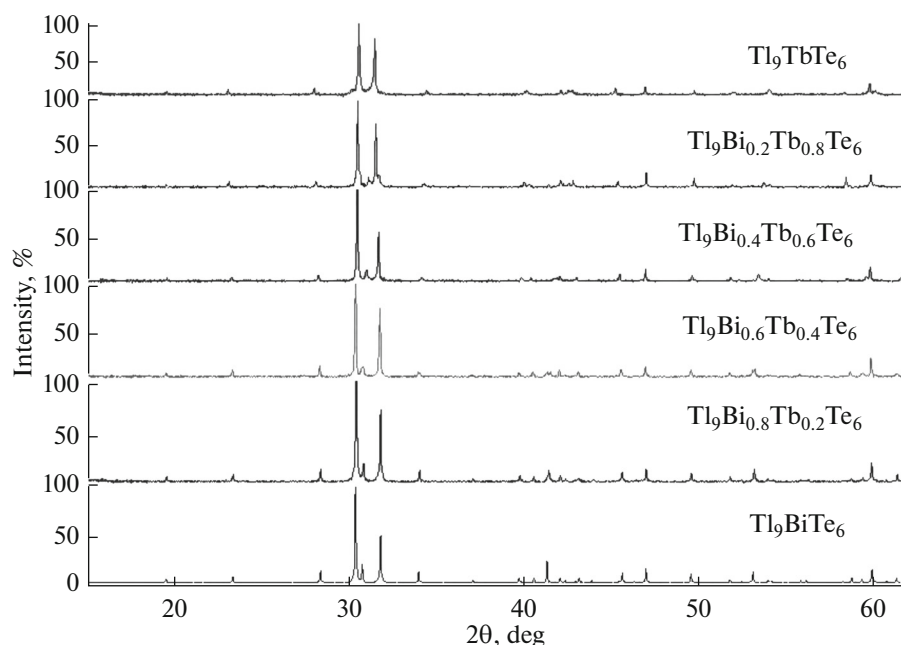
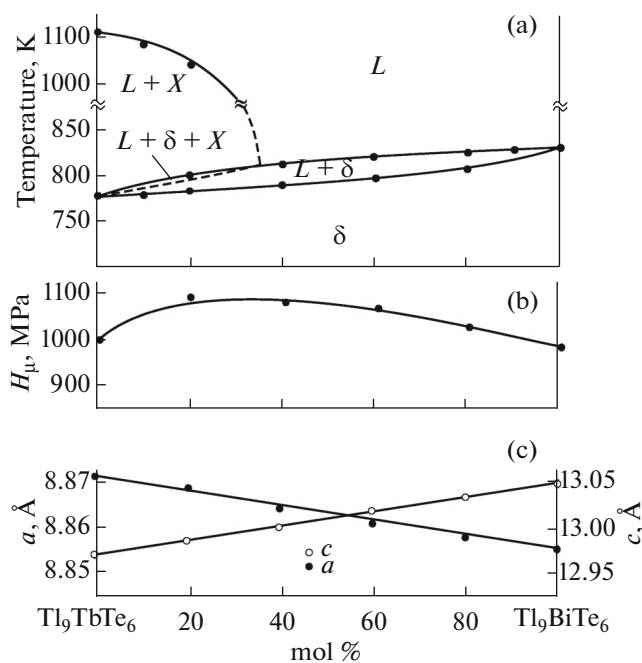


Fig. 1. X-ray powder diffraction patterns of alloys in the  $\text{Tl}_9\text{TbTe}_6$ – $\text{Tl}_9\text{BiTe}_6$  system.



**Fig. 2.** Phase diagram (a) and composition dependences of microhardness (b) and lattice parameters (c) for alloys of the  $\text{Tl}_9\text{TbTe}_6$ – $\text{Tl}_9\text{BiTe}_6$  system.

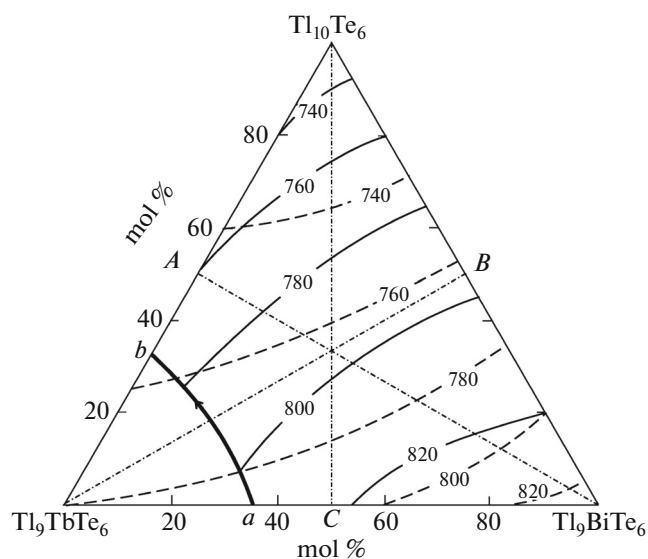
studied by X-ray diffraction at room temperature on a Bruker D8 powder diffractometer ( $\text{CuK}\alpha$  radiation) in the angular range  $2\theta = 10^\circ$ – $70^\circ$ . Microhardness measurements were performed on a PMT-3 microhardness tester and an indenter load of 0.2 N.

## RESULTS AND DISCUSSION

A joint analysis of experimental data obtained in this study by the above techniques and of previous results [11, 28] on the  $\text{Tl}_5\text{Te}_3$ – $\text{Tl}_9\text{BiTe}_6$  and  $\text{Tl}_5\text{Te}_3$ – $\text{Tl}_9\text{TbTe}_6$  systems allowed us to identify phase equilibria in the  $\text{Tl}_5\text{Te}_3$ – $\text{Tl}_9\text{BiTe}_6$ – $\text{Tl}_9\text{TbTe}_6$  system (table, Figs. 1–5).

X-ray diffraction results indicate the formation of a continuous series of solid solutions in the constituent binary system  $\text{Tl}_9\text{TbTe}_6$ – $\text{Tl}_9\text{BiTe}_6$ . As seen in Fig. 1, the X-ray diffraction patterns of the constituent tellurides and intermediate alloys in this system are similar to that of  $\text{Tl}_5\text{Te}_3$ , with a slight shift of their reflections. The composition dependences of the lattice parameters (calculated with the Topas V3.0 program) for the solid solutions (table) follow Vegard's law to within the present experimental uncertainty (Fig. 2c).

The  $T$ – $x$  phase diagram of the  $\text{Tl}_9\text{TbTe}_6$ – $\text{Tl}_9\text{BiTe}_6$  system (Fig. 2a) demonstrates the formation of a continuous series of solid solutions with the  $\text{Tl}_5\text{Te}_3$  structure ( $\delta$ -phase). However, the system is not pseudobi-



**Fig. 3.** Projections of the liquidus (solid lines) and solidus (dashed lines) surfaces in the  $\text{Tl}_5\text{Te}_3$ – $\text{Tl}_9\text{BiTe}_6$ – $\text{Tl}_9\text{TbTe}_6$  system. The dot-dashed lines represent the cuts studied.

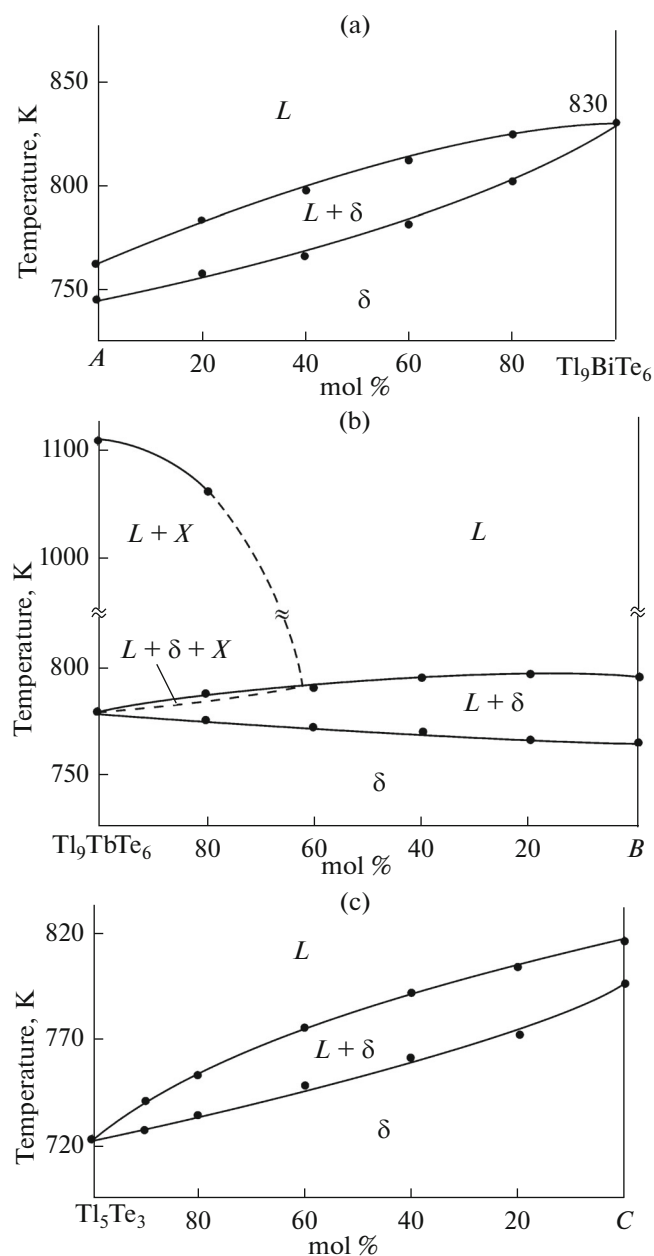
nary because of the incongruent melting of  $\text{Tl}_9\text{TbTe}_6$ . In a wide composition range ( $>35$  mol %  $\text{Tl}_9\text{BiTe}_6$ ), we observe the primary crystallization of another refractory phase,  $X$  (presumably  $\text{TlTbTe}_2$ ), which leads to the formation of the  $L + X$  and  $L + X + \delta$  phase regions in the phase diagram. Because of its narrow temperature range, the  $L + X + \delta$  phase region was not detected in our experiments and is marked by a dashed line.

The composition dependence of microhardness in Fig. 2b is consistent with the phase diagram: it has a flat maximum, which is characteristic of systems with a continuous series of substitutional solid solutions [29].

The projection of the  $T$ – $x$ – $y$  phase diagram onto the Gibbs composition triangle (Fig. 3) indicates that the liquidus surface comprises two phase fields, corresponding to the primary crystallization of the  $X$ -phase and  $\delta$ -solid solution. These surfaces are separated by curve  $ab$ , which represents the  $L + X \leftrightarrow \delta$  peritectic equilibrium. The solidus is formed by a single surface (dashed isotherms), corresponding to the onset of the melting of the  $\delta$ -phase.

Figure 4 shows the  $\text{Tl}_9\text{BiTe}_6$ – $A$ ,  $\text{Tl}_9\text{TbTe}_6$ – $B$ , and  $\text{Tl}_5\text{Te}_3$ – $C$  vertical sections through the phase diagram of the  $\text{Tl}_5\text{Te}_3$ – $\text{Tl}_9\text{BiTe}_6$ – $\text{Tl}_9\text{TbTe}_6$  system (where  $A$ ,  $B$ , and  $C$  represent the 1 : 1 alloys in the constituent binary systems).

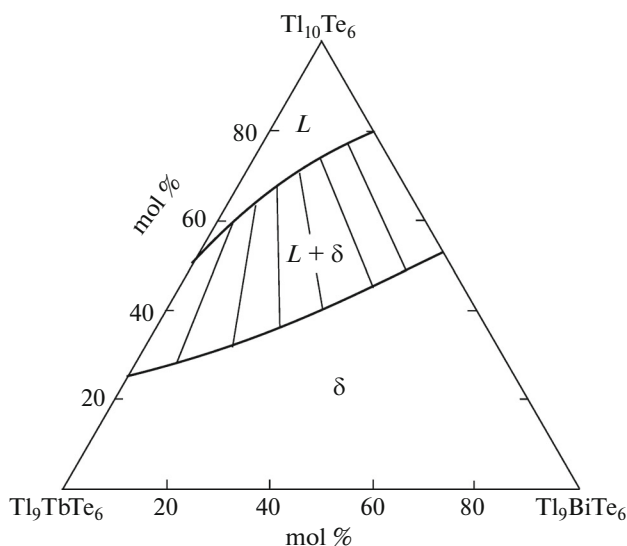
It is seen in Figs. 4a and 4c that only the  $\delta$ -phase crystallizes from the melt over the entire composition range on the  $\text{Tl}_9\text{BiTe}_6$ – $A$  and  $\text{Tl}_5\text{Te}_3$ – $C$  joins.



**Fig. 4.** (a)  $Tl_9BiTe_6$ - $A$ , (b)  $Tl_9TbTe_6$ - $B$ , and (c)  $Tl_5Te_3$ - $C$  vertical sections through the phase diagram of the  $Tl_5Te_3$ - $Tl_9BiTe_6$ - $Tl_9TbTe_6$  system.

On the  $Tl_9TbTe_6$ - $B$  join (Fig. 4b), the  $\delta$ -phase crystallizes from the melt in the composition range 0–60 mol %  $Tl_9TbTe_6$ . At higher  $Tl_9TbTe_6$  contents, the first to crystallize is the  $X$ -phase. This is followed by the univariant peritectic reaction  $L + X \leftrightarrow \delta$ . As a result, the  $X$ -phase disappears and the excess melt crystallizes to give the  $\delta$ -phase.

It is worth noting that, in the  $Tl_5Te_3$ - $Tl_9BiTe_6$ - $Tl_9TbTe_6$  system, the directions of the tie lines in the  $L + \delta$  two-phase regions do not coincide with the  $T$ - $x$



**Fig. 5.** 760-K isothermal section through the phase diagram of the  $Tl_5Te_3$ - $Tl_9BiTe_6$ - $Tl_9TbTe_6$  system.

planes of inner sections and vary with temperature. The directions of the tie lines at 760 K are clearly demonstrated by the corresponding isothermal section of the phase diagram (Fig. 5).

## CONCLUSIONS

We have studied phase equilibria in the  $Tl_5Te_3$ - $Tl_9BiTe_6$ - $Tl_9TbTe_6$  system. The system has been shown to contain a continuous series of solid solutions with a tetragonal structure ( $Tl_5Te_3$  type, sp. gr.  $I4/mcm$ ). The  $T$ - $x$ - $y$  phase diagram mapped out in this study and its isothermal sections can be useful in choosing melt compositions for the growth of single crystals of  $\delta$ -solid solutions with tailored composition by directional solidification.

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