

# High-temperature short-range order in $\text{Mn}_3\text{RhSi}$

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Conventional phase transitions are well understood in terms of the order parameter, based on the Landau–Ginzburg–Wilson theory. However, unconventional magnetic orders have been observed in clean systems such as MnSi. The unconventional magnetic orders of conduction electrons in the metallic phase has been observed for high-temperature superconductors and heavy fermion compounds. However, these unconventional magnetic orders have been limited to relatively low temperatures as quantum phase transitions. Here high-temperature magnetic short-range order is observed as one of the unconventional magnetic orders at temperatures up to 720 K in a noncentrosymmetric intermetallic antiferromagnet  $\text{Mn}_3\text{RhSi}$  with a well-ordered lattice. The magnetic Mn ions form a hyperkagome network of corner-sharing triangles, where the spins are geometrically frustrated. The spin network is equivalent to that of a spin liquid and non-Fermi-liquid material,  $\beta\text{-Mn}$ . Our observation indicates that a metallic phase with magnetic short-range order exists at high temperatures.

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Unconventional magnetic order of conduction electrons<sup>1</sup> has been observed in a paramagnetic metallic state of MnSi under pressure by neutron diffraction<sup>2</sup> and  $\mu$ SR measurements<sup>3</sup>. The similar unconventional magnetic order has been observed near the magnetic transition temperatures of inhomogeneous chiral-spin states in MnSi and FeGe<sup>4–6</sup>. As another case of unconventional magnetic order, solitonic spin liquid (SL) has been reported in an incommensurate magnetic phase of Fe<sub>1+y</sub>Te in a very narrow temperature range above the Néel temperature, as observed by a local magnetic probe, Mössbauer spectroscopy<sup>7</sup>. An inhomogeneous magnetic ordered state has also been observed in a triangular lattice magnet,  $\alpha$ -NaMnO<sub>3</sub>, with nanometer-scale phase separation far below room temperature<sup>8,9</sup>. The origin of this order is attributed to local symmetry breaking by defects in the crystal structure. In addition, magnetic fragmentation has been reported for the spin ice compound Nd<sub>2</sub>Zr<sub>2</sub>O<sub>7</sub> below 1 K<sup>10</sup>, where the tetrahedral network is known to break local symmetry for magnetic orderings, such as in an all-in-all-out structure. Manganese monoxide MnO<sup>11</sup> with distorted face-centered cubic lattice of Mn is known as high-temperature magnetic short-range order (SRO) magnet. The magnetic diffuse scattering of SRO is observed up to  $530 \pm 20$  K<sup>12</sup> at the same  $Q$ -position as that of the long-range magnetic Bragg peak<sup>13</sup>. The temperature is much higher than the Néel temperature of about 120 K<sup>13</sup>.

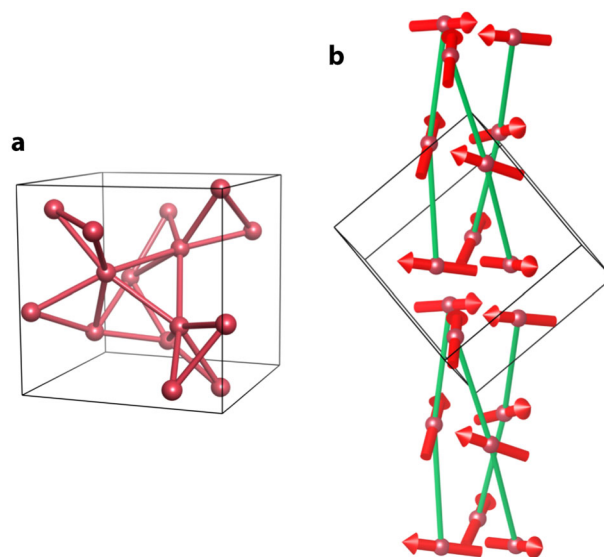
These cases of unconventional magnetic order have been observed near critical points accompanied by symmetry breaking. The conditions may be close to multicritical points, as discussed by Belitz et al.<sup>1</sup> These cases violate the Lifshitz condition in the Landau theory of second-order magnetic transitions as noncentrosymmetric magnetic ordering with the Dzyaloshinskii–Moriya (DM) interaction<sup>14–16</sup> or incommensurate magnetic order<sup>7</sup>. Under the violation of the Lifshitz condition, we may expect an unconventional magnetic order due to an inhomogeneous order parameter. Thus far, however, the observed temperature ranges have been limited, where the ordered states are usually observed as a quantum phase transition at low temperatures.

Here, we report high-temperature magnetic SRO above the long-range magnetic transition temperature ( $T_N = 190$  K) in a noncentrosymmetric intermetallic antiferromagnet, Mn<sub>3</sub>RhSi, which is a novel compound with a  $\beta$ -Mn structure.

## Results and discussion

According to structural refinements of the X-ray and neutron diffraction patterns at  $T = 293$  K (Supplementary Note 1, Supplementary Figs. 1 and 2), the Mn atoms selectively occupy the 12-fold site (12b), similar to the Wyckoff 12d position of the  $\beta$ -Mn structure (Fig. 1a), whereas the Rh and Si atoms preferentially occupy two different 4-fold sites (4a) derived by splitting the Wyckoff 8c position of  $\beta$ -Mn, as previously observed for this compound family<sup>17–19</sup>. The 12-fold site is the magnetic moment site of  $\beta$ -Mn and forms a three-dimensional hyperkagome network as an ordered phase (Fig. 1a), whereas the Rh and Si atoms occupy non-magnetic sites in the  $\beta$ -Mn structure. In the case of  $\beta$ -Mn, the former 12-fold site is coordinated by near-neighbor (NN) Mn atoms with a distance of 2.66 Å, whereas the latter 8-fold site is surrounded by NN Mn atoms with a distance of 2.36 Å. The long and short bond lengths are consistent with the localized and itinerant natures of Mn 3d electrons at these sites, respectively<sup>20</sup>.

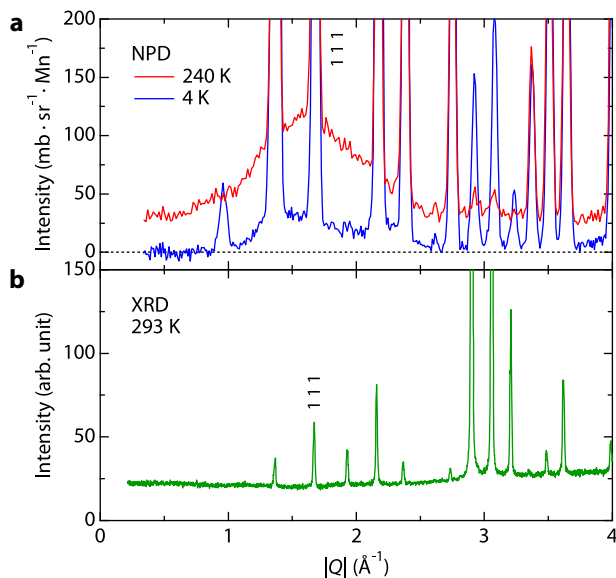
Below  $T_N$ , the magnetic Bragg peaks, such as 100 and 110, develop (Supplementary Note 1, Supplementary Fig. 2). Those  $Q$ -positions are different from that of SRO in contrast to the case of MnO<sup>13</sup>. The refined long-range magnetic structure is shown in Fig. 1b, where each triangular unit consists of a 120° spin



**Fig. 1 Magnetic structure.** **a** Hyperkagome network of Mn magnetic sites in the cubic unit cell of Mn<sub>3</sub>RhSi. The 12b site of  $P2_13$  is preferentially occupied by Mn magnetic moments. **b** Helical spin rod of triangular units along [111]. Vertical bonds correspond to the  $J_5$  ferromagnetic interaction described in ref. 21.

configuration accompanied by a small ferromagnetic component normal to the triangular plane. The triangle units form a helical spin rod along the [111] direction, which results in a geometrically frustrated hyperkagome structure. The Mn magnetic moment at  $T = 4$  K is estimated as  $2.61 \pm 0.03 \mu_B$ . In addition to the magnetic Bragg peaks, strong diffuse scattering is observed near  $Q = 1.7 \text{ \AA}^{-1}$ , as shown in Fig. 2a. This scattering is not observed in the X-ray diffraction pattern in Fig. 2b or the electron diffraction patterns (Supplementary Note 2, Supplementary Fig. 3), confirming its magnetic origin. The  $Q$  position is precisely identical to the previously observed magnetic diffuse scattering position for SL in  $\beta$ -Mn<sub>0.8</sub>Co<sub>0.2</sub><sup>21</sup> or spin glass (SG) in  $\beta$ -Mn<sub>1-x</sub>In<sub>x</sub><sup>20</sup>. The original  $\beta$ -Mn is a well-known SL material with a three-dimensional hyperkagome network of triangular Mn spin units<sup>21</sup>. Non-Fermi-liquid (NFL) behavior is also indicated in  $\beta$ -Mn based on the exponent of the temperature dependence of the resistivity and the scaling of the dynamical spin susceptibility<sup>22</sup>. The magnetic diffuse scattering remains at  $T = 4$  K, suggesting the coexistence of two types of magnetic orderings with different coherence lengths at different  $Q$  positions. The magnetic diffuse scattering intensity increases as the temperature increases up to  $T_N$ . The integrated intensity is estimated as  $\sim 0.8 \mu_B$  at 4 K and increases to  $\sim 1.3 \mu_B$  at 300 K, based on the reverse Monte Carlo simulation reported in ref. 23 (Supplementary Note 3). However, the magnetic diffuse scattering remains at temperatures above  $T_N$ , persisting to  $\sim 700$  K, as shown in Fig. 3a. According to an isotropic short-range spin correlation model analysis (Supplementary Note 4), the SRO spin correlation primarily consists of an antiferromagnetic (AFM) correlation between the first NN spins and a ferromagnetic correlation between the fifth NN spins, as reported in ref. 21.

The observed diffuse scattering of Mn<sub>3</sub>RhSi can be attributed to a SRO. To estimate the volume fraction of the SRO in Mn<sub>3</sub>RhSi,  $\mu$ SR measurements were performed.  $\mu$ SR is a unique tool that can reveal the SRO volume fraction. This tool has been successfully applied for studies of phase separations in materials near the quantum phase transition<sup>3</sup>. In addition, the spin-lattice relaxation rate of  $\mu$ SR assists in our assessment of the magnetism<sup>20</sup>.



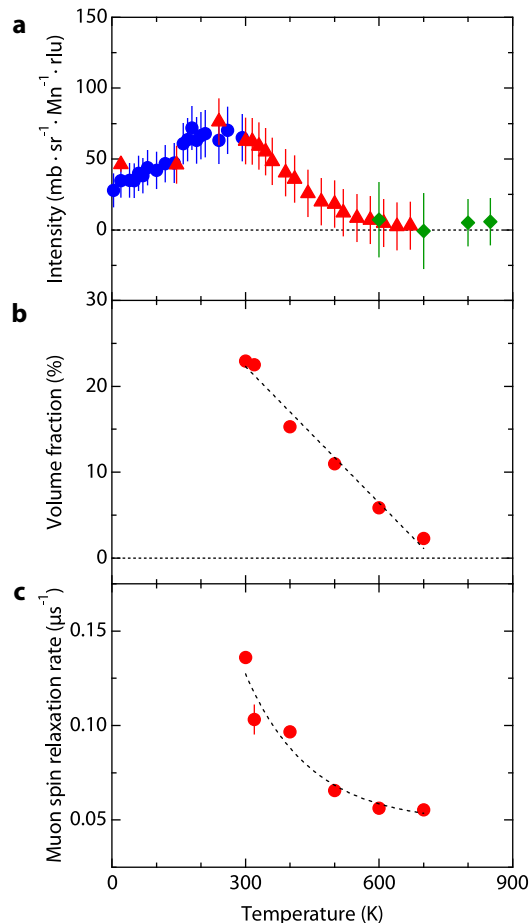
**Fig. 2** Enlarged neutron and X-ray diffraction patterns. **a**, **b** Diffuse scattering under nuclear Bragg peaks of neutron diffraction patterns at  $T = 240$  and  $4$  K on an absolute scale (**a**) and the X-ray diffraction pattern at  $T = 293$  K (**b**).

In  $\text{Mn}_3\text{RhSi}$ , the SRO was observed as a decrease in the normalized initial asymmetry in the paramagnetic phase. The temperature dependence of the magnetic volume fraction over the whole volume is shown in Fig. 3b, following the estimation methods described in the methods (muon spin relaxation measurements). The volume begins to increase as the temperature decreases below  $720 \pm 21$  K. In contrast, the muon spin relaxation rate,  $\lambda$ , of the remaining paramagnetic component exhibits Curie–Weiss behavior, as shown in Fig. 3c, where the Weiss temperature roughly corresponds to  $T_N$ .

In the paramagnetic region, magnetic diffuse scattering appears gradually, with the  $\mu\text{SR}$  measurement showing a linear increase in SRO volume fraction with decreasing temperature. These different temperature dependences suggest that the magnetic moment in the SRO state gradually develops with decreasing temperature.

Based on the  $\mu\text{SR}$  measurement (Supplementary Note 5), the SRO volume fraction was 22.9% at  $T = 300$  K. According to neutron diffraction measurements at  $T = 4$  K, the ordered magnetic moment was  $2.61 \mu_B$ , whereas the magnetic moment of the diffuse scattering was approximately  $0.8 \mu_B$ . The total magnetic moment reaches  $2.73 \mu_B$  at  $4$  K. As the temperature increases to  $300$  K, only the magnetic moment of diffuse scattering remains at  $1.3 \mu_B$ . Based on the 22.9% SRO volume fraction at  $300$  K, the total magnetic moment is expected to decrease from  $2.73 \mu_B$  at  $4$  K to  $1.31 \mu_B$  at  $300$  K. This value of  $1.31 \mu_B$  is almost the same as the observed value of  $1.3 \mu_B$  by neutron diffuse scattering at  $300$  K. This coincidence suggests that the magnetic moment is transferred from the SRO to the long-range order at the other  $Q$  position on cooling below the Néel temperature.

One may suspect that the magnetic diffuse scattering may be induced by disorders such as local defects or elemental substitutions at individual sites in the crystal structure. In addition, not only the magnetic structure but also the crystal structure may be phase-separated, as observed in the triangular lattice magnet  $\alpha\text{-NaMnO}_3$ <sup>8,9</sup>. The crystal structure of  $\text{Mn}_3\text{RhSi}$  was studied by both neutron and X-ray diffraction measurements, and neither defects nor elemental disorders were identified in the range of  $3\sigma$  (Supplementary Note 1, Supplementary Table 1). However, nuclear diffuse scattering may be included in Fig. 2a, as observed

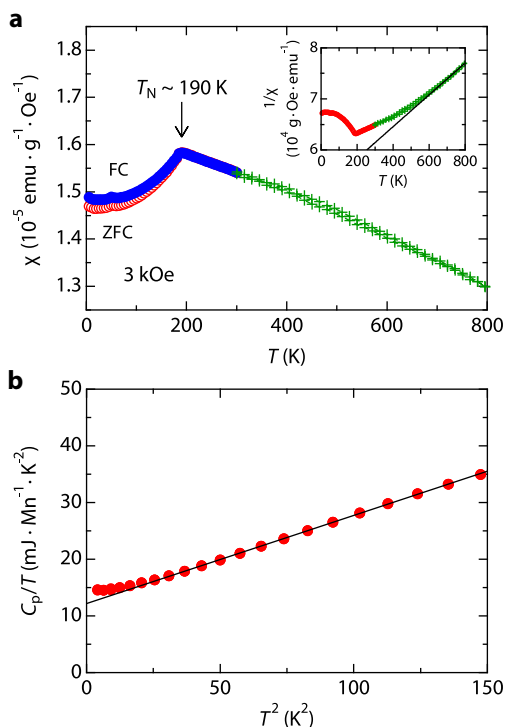


**Fig. 3** Temperature dependence of magnetic diffuse scattering intensity, short-range order volume fraction, and muon spin relaxation rate.

**a** Temperature dependence of the integrated magnetic diffuse scattering intensity near  $Q = 1.7 \text{ \AA}^{-1}$ . The circles correspond to low-temperature cryostat measurements, the triangles correspond to cryofurnace measurements, and the diamonds correspond to furnace measurements. **b** Volume fraction of the magnetic short-range ordering component estimated from the normalized initial asymmetry. **c** Muon spin relaxation rate of the paramagnetic component,  $\lambda$  ( $\mu\text{s}^{-1}$ ). The data point for  $320$  K was obtained using ARGUS, whereas the other points were obtained using HiFi.

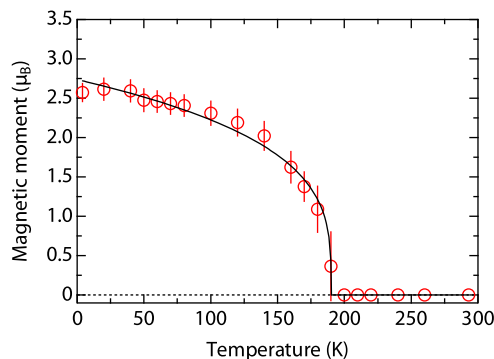
at  $Q = 0.8 \text{ \AA}^{-1}$  for  $\beta\text{-Mn}_{1-x}\text{In}_x$ <sup>20</sup>. In the case of  $\text{Mn}_3\text{RhSi}$ , nuclear diffuse scattering at  $Q = 0.8 \text{ \AA}^{-1}$  is not observed in the X-ray diffraction pattern, as shown in Fig. 2b. Our electron diffraction measurement shows diffuse scattering peaks at  $\{1/2 \ 1/4 \ 2\}$  as the lowest reciprocal point, which corresponds to  $Q = 2.01 \text{ \AA}^{-1}$  (Supplementary Note 2, Supplementary Fig. 3). This diffuse scattering is not observed in the X-ray diffraction pattern of Fig. 2b, possibly due to its weak intensity. The diffuse scattering intensity significantly decreased from  $T = 100$  K to  $300$  K, suggesting that the lattice strain may disappear above  $300$  K. Based on these results, we conclude that the SRO does not originate from disorder.

The SRO in this new compound,  $\text{Mn}_3\text{RhSi}$ , is confirmed by a complementary use of neutron diffraction, X-ray diffraction, electron diffraction, and  $\mu\text{SR}$  measurements in this work. The SRO effect is manifested in the physical properties of  $\text{Mn}_3\text{RhSi}$  as follows. The temperature dependence of the magnetic susceptibility of  $\text{Mn}_3\text{RhSi}$  exhibits non-Curie–Weiss behavior over a wide temperature range from the long-range magnetic transition temperature ( $T_N = 190$  K) to  $\sim 700$  K (Fig. 4a). The detailed study of the magnetic susceptibility is shown in Supplementary Note 6.



**Fig. 4** Magnetic susceptibility and specific heat capacity. **a** Temperature dependence of zero-field-cooled and field-cooled magnetic susceptibilities  $\chi (= M/H)$  under a magnetic field of 3 kOe for a polycrystalline sample of  $\text{Mn}_3\text{RhSi}$ . The crosses denote measurements in a high-temperature SQUID furnace. The inset shows the inverse magnetic susceptibility. The black solid line is a Curie–Weiss fit in the temperature range from 700 to 800 K. **b** Low-temperature specific heat capacity of  $\text{Mn}_3\text{RhSi}$ . The electronic specific heat  $\gamma$  is estimated as  $12.18 \pm 0.03 \text{ mJ Mn}^{-1} \text{ K}^{-2}$ , and the Debye temperature  $\theta_D$  is  $275.2 \pm 0.2 \text{ K}$ .

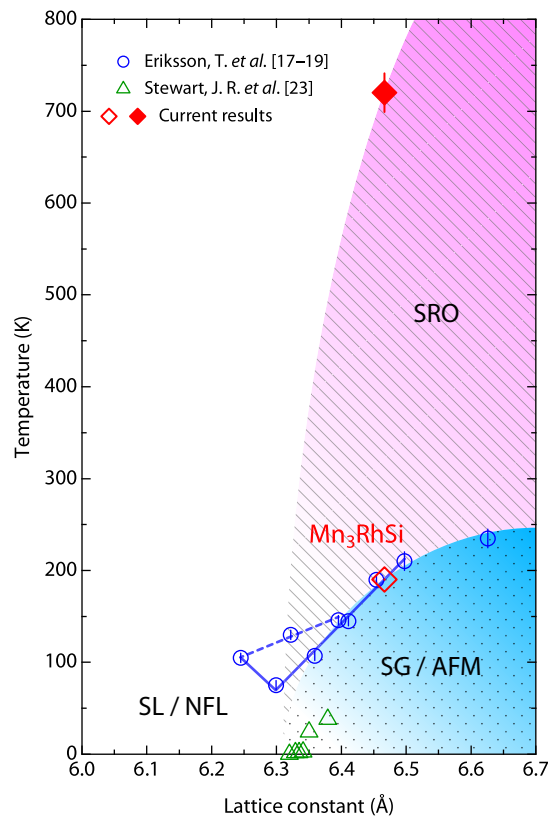
As a possible origin of this non-Curie–Weiss behavior, one may consider a possible coupling of localized spins and conduction electrons as the Kondo effect in this compound. However, the low-temperature specific heat capacity does not show any significant enhancement of the electron mass, as illustrated in Fig. 4b. The estimated Sommerfeld constant  $\gamma$  is  $12.18 \pm 0.03 \text{ mJ Mn}^{-1} \text{ K}^{-2}$ , while  $\beta$ -Mn is known as a heavy  $3d$  electron material with a Sommerfeld constant of  $70 \text{ mJ Mn}^{-1} \text{ K}^{-2}$ <sup>24</sup>.  $\beta$ -Mn shows a broad peak at  $\sim 140 \text{ K}$  in the temperature dependence of the magnetic susceptibility, which may correspond to the Kondo temperature. Based on the specific heat results, we conclude that the Kondo effect is not the origin of this non-Curie–Weiss behavior. Some low-dimensional magnets also show a hump structure in the magnetic susceptibility, such as Bonner–Fisher-type magnets<sup>25</sup>. However, the present compound is a three-dimensional cubic magnet. The critical exponent of the temperature dependence of the Mn magnetic moment is close to  $1/3$ , conforming to the classical model of a three-dimensional magnet. The solid line in Fig. 5 is a least-squares fit to the ordered magnetic moment based on the classical power-law function expressed as  $\mu(T) = \mu_0 (1 - T/T_N)^\beta$ . The fitting gives a long-range magnetic transition temperature of  $190.1 \pm 0.2 \text{ K}$  and a critical exponent  $\beta$  of  $0.28 \pm 0.03$ . The obtained transition temperature is consistent with that of the magnetic susceptibility measurement. The critical exponent suggests a second-order-type phase transition, with three-dimensional spin interactions corresponding to the Ising, XY, or Heisenberg model in  $\text{Mn}_3\text{RhSi}$ <sup>26</sup>. This result excludes the possibility of Bonner–Fisher-type magnetic susceptibility in the paramagnetic region. Based on these results, the



**Fig. 5** Temperature dependence of the Mn magnetic moment of  $\text{Mn}_3\text{RhSi}$ . Error bars were obtained from Rietveld analysis of the neutron diffraction data. The solid line is a power-law fitting curve, as described in the text.

origin of the present non-Curie–Weiss temperature dependence can be attributed to the SRO effect.

Similar ternary cubic compounds, such as  $\text{Mn}_3\text{TX}$  ( $T = \text{Co, Ir}$ ;  $X = \text{Si, Ge}$ )<sup>17–19</sup>, have primarily been characterized with respect to their crystallographic and long-range ordered magnetic structure. The published data are inconclusive regarding possible SRO in these series, but non-Curie–Weiss behavior and broad magnetic diffuse scattering signals in neutron powder diffraction patterns above the ordering temperature may warrant further research on these compounds. Results for the series of compounds with the  $\beta$ -Mn structure suggest that  $\text{Mn}_3\text{RhSi}$  is located near a quantum critical point between a SL state and a long-range AFM ordered state, as shown in Fig. 6, where the long-range magnetic transition temperature decreases as the lattice constant decreases toward the quantum critical point. As the lattice constant decreases, the electronic bandwidth  $W$  increases. Therefore, the decrease in  $T_N$  with decreasing  $U/W$  is consistent with the theoretical expectation for an AFM metal. However, some variations in  $T_N$  are shown for the different systems in Fig. 6, suggesting that other parameters, such as the DM interaction, are required to describe this phase diagram. In this sense, there may be a quantum multicritical point<sup>1</sup> that depends on the bandwidth, the DM interaction, and other parameters such as the Fermi surface topology. Our remarkable finding is the widely spread unconventional magnetic SRO up to 720 K, as illustrated in Fig. 6. Although this SRO state has not been confirmed in other compounds, magnetic diffuse scattering has been observed in  $\beta$ -Mn<sup>24</sup>,  $\beta$ - $\text{Mn}_{0.8}\text{Co}_{0.2}$ <sup>21</sup>,  $\beta$ - $\text{Mn}_{1-x}\text{In}_x$ <sup>20</sup>, and  $\beta$ - $\text{Mn}_{1-x}\text{Al}_x$ <sup>23</sup>. Notably, diffuse scattering occurs in  $\beta$ -Mn<sup>24</sup>, but the intensity decreases with decreasing temperature, and almost disappears at low temperatures. For  $\beta$ - $\text{Mn}_{0.8}\text{Co}_{0.2}$ , however, the diffuse scattering intensity decreases with increasing temperature, and almost disappears at  $T = 200 \text{ K}$ <sup>21</sup>. Therefore, the SRO transition temperature may be approximately 200 K for  $\beta$ - $\text{Mn}_{0.8}\text{Co}_{0.2}$ . These results suggest that the SRO transition temperature rapidly decreases toward the quantum critical point, as illustrated in Fig. 6. Near the critical point, the family of  $\beta$ -Mn compounds exhibits NFL behavior<sup>22</sup>, as observed in  $\text{MnSi}$ <sup>4</sup>. Therefore, the phase diagram of Fig. 6 may include B20 family compounds. The SRO of  $\text{MnSi}$  at ambient pressure occurs at 1 K above the helical magnetic order temperature of  $29 \text{ K}$ <sup>4</sup>. For  $\text{FeGe}$ , the precursor region corresponds to  $\sim 2 \text{ K}$  above the long-range magnetic order temperature of  $278.2 \text{ K}$ <sup>5</sup>, and the NFL behavior seems to disappear in the SG/AFM phase. Thus far, the SRO has a limited temperature range, possibly because of the weak DM interaction of  $3d$  elements. The pseudogap state of cuprates may also be categorized as an unconventional magnetic ordered state of conduction electrons<sup>27</sup>. This issue is a central concept in condensed matter physics,



**Fig. 6 Phase diagram of  $\beta$ -Mn structure compounds.** Temperature results for the family of compounds with the  $\beta$ -Mn structure<sup>17–19,23</sup> as a function of the cubic lattice parameter, in addition to  $\text{Mn}_3\text{RhSi}$  (open and closed diamonds). The open circles with error bars present results for  $\text{Mn}_3\text{CoSi}$ ,  $\text{Mn}_3\text{IrSi}$ ,  $\text{Mn}_3\text{CoGe}$ ,  $\text{Mn}_3\text{IrGe}$ , and their binary compounds<sup>17–19</sup>. The open triangles present results for  $\beta\text{-Mn}_{1-x}\text{Al}_x$ <sup>23</sup>. The result for the SL compound  $\beta$ -Mn occurs at 6.32 Å on the quantum critical point, where NFL behavior is observed<sup>22</sup>. SG behavior is observed in aluminum-doped  $\beta$ -Mn<sup>23</sup>, whereas the compound family of  $\text{Mn}_3\text{RhSi}$  exhibits a long-range AFM transition.

accompanying Fermi surface reconstruction. The magnetic ordering of cuprates is suppressed by their low-dimensionality in addition to carrier doping, whereas the large superexchange coupling  $J$  leads to the development of unconventional magnetic order as the pseudogap state. In contrast, the magnetic ordering of  $\text{Mn}_3\text{RhSi}$  with a large Mn magnetic moment is suppressed by geometrical frustration, where SRO appears at high temperatures. Here, the present finding of SRO in  $\text{Mn}_3\text{RhSi}$  provides a novel platform for studying the unique properties of unconventional magnetic order over a wide temperature range.

## Methods

**Sample preparation and quality.** Polycrystalline samples were prepared from stoichiometric amounts of high-purity powders of the constituent elements (99.9% pure Mn, 99.9% pure Rh, and 99.99% pure Si). The compounds were synthesized by a conventional arc melting method in an argon atmosphere. The polycrystals were sealed in an evacuated quartz tube, annealed at 900 °C for 3 days and 800 °C for 1 week, and subsequently quenched in water. The phase purity was examined by X-ray powder diffraction using a desktop diffractometer with Cu K $\alpha$  radiation. No traces of impurity phases were found within the experimental accuracy. The chemical composition of the samples was verified by scanning electron microscopy and energy-dispersive X-ray spectroscopy (SEM/EDS) analysis. The SEM/EDS elemental mapping indicated a homogeneous distribution of atoms and an atomic ratio of Mn:Rh:Si = 58:21:22, which is consistent with the stoichiometric composition within an error of ~1%. Magnetization measurements were performed using a Superconducting Quantum Interference Device magnetometer at the CROSS-Tokai User Laboratory II. Specific heat measurements were performed with an AC capacitance bridge in a two-probe configuration.

**Neutron diffraction experiments.** Neutron powder diffraction data were collected on the Wide-Angle Neutron Diffractometer (WAND, HB-2C) installed at the High Flux Isotope Reactor (HFIR) at Oak Ridge National Laboratory (ORNL), employing Ge (113) reflection to produce a monochromatic neutron beam with a wavelength of 1.4827 Å. A 5.0-g powder sample was loaded into a vanadium can (7.5-mm inner diameter). Crystal and magnetic structure refinements were performed by the Rietveld method with the program FullProf<sup>28</sup> and visualized with the software VESTA<sup>29</sup>. The magnetic form factor of the Mn atom was used in the analysis. Representational analysis was conducted using the program SARA<sup>30</sup> to identify a reasonable model for the symmetry-allowed magnetic structure.

The absolute magnetic diffuse scattering intensity was estimated using the method described in Supplementary Note 4, and the results were analyzed following the method described in Supplementary Note 5.

**Muon spin relaxation measurements.** The  $\mu\text{SR}$  experiments were performed using the HiFi and ARGUS spectrometers at the ISIS facility, Rutherford Appleton Laboratory. A polycrystalline ingot was cut and mounted in a light furnace for high-temperature measurements. The decay-positron asymmetry function was measured as a function of time, under zero field or under a longitudinal field of 10 mT, as shown in Supplementary Note 5.

The volume fraction shown in Fig. 3b was estimated from the normalized asymmetry as follows. The initial asymmetry is an instrumental parameter that can be obtained from a non-magnetic material, such as a silver foil. The asymmetry decreases in a magnetically ordered material over a short time, depending on the magnetic moment size. The decreasing time can be very short, on the order of 0.2  $\mu\text{s}$ . In this case, the asymmetry can be observed as a sudden reduction near the zero time point using a pulsed muon spectrometer. The magnitude of the reduction in the spectrum is the ratio of the magnetically ordered volume because the muons randomly exhibit local magnetic ordering. The zero position of the zero magnetic moment was determined from the maximum initial asymmetry of the original time spectra at 700 K, which had a value of 20.8%. Therefore, in the normalized asymmetry graph, a value of 1 corresponds to the initial asymmetry of the time spectra at 700 K, and 0 indicates the minimum asymmetry of the time spectra at 300 K for up to 15  $\mu\text{s}$ , considering the lower limit of the error bar. The minimum asymmetry was 14.1% in this case. The same approach was applied to normalize the time spectrum acquired at 320 K from a different spectrometer, which confirmed the repeatability of the data and analysis. It should be noted that the magnetic volume consists of the quasistatic magnetic moments in  $\mu\text{SR}$  time window below 0.1 meV.

## Data availability

All relevant data are available from the authors on request.

## Code availability

The program FullProf is distributed free of charge (<https://www.ill.eu/sites/fullprof/>). The software VESTA64 is distributed free of charge for academic users under the VESTA License (<https://jp-minerals.org/vesta/jp/download.htm>).

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## Author contributions

The polycrystalline Mn<sub>3</sub>RhSi sample was synthesized by H.Y. The neutron diffraction patterns were analyzed by H.Y., whereas the  $\mu$ SR spectra were analyzed by D.P.S. with the help of I.W. Neutron diffraction patterns were collected by H.Y., M.H., M.F., S.C., and J.F., and  $\mu$ SR spectra were acquired by D.P.S., J.L., A.B., L.C., and I.W. The magnetic susceptibility was measured by M.I. and H.Y. The specific heat capacity was measured by Y.Y. The chemical composition of Mn<sub>3</sub>RhSi was analyzed by K.K. using EDS. Electron diffraction measurements based on transmission electron microscopy were performed by A.K. and S.M. This paper was written by S.S. and H.Y., with input from the remaining authors. This research project was organized by S.S. All authors have approved this paper.

## Competing interests

The authors declare no competing interests.

## Additional information

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