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Intuitionistic fuzzy fairly operators and additive ratio assessment-based integrated model for selecting the optimal sustainable industrial building options

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In the past few years, the private sectors and industries have focused their attention on sustainable development goals to achieve the better and more sustainable future for all. To accomplish a sustainable community, one requires to better recognize the fundamental indicators and selects the most suitable sustainable policies in diverse regions of the community. Considering the huge impact of construction industry on sustainable development, very less research efforts have been made to obtain worldwide sustainable elucidations for this type of industry. As a large sector of construction industry, industrial buildings consume enormous amounts of energy and financial assets, and play a key character in job creation and life quality improvement in the community. In order to assess the sustainable industrial buildings by means of multiple indicators, the present study introduces a hybrid multi-criteria decision-making methodology which integrates the fairly aggregation operator, the MEthod based on the Removal Effects of Criteria (MERECE), the stepwise weight assessment ratio analysis (SWARA) and the additive ratio assessment (ARAS) methods with intuitionistic fuzzy set (IFS). In this respect, firstly new intuitionistic fuzzy weighted fairly aggregation operators are proposed and then employed to aggregate the decision information in the proposed hybrid method. This operator overcomes the limitations of basic intuitionistic fuzzy aggregation operators. To find the criteria weights, an integrated model is presented based on the MERECE for objective weights and the SWARA for subjective weights of indicators under IFS context. To rank the sustainable industrial buildings, an integrated ARAS method is employed from uncertain perspective. Further, a case study concerning sustainable industrial buildings evaluation is presented to illustrate the superiority and practicality of the developed methodology. The advantages of the developed approach are highlighted in terms of stability and reliability by comparison with some of the existing methods.

“Sustainable development (SD)” aims to minimize the ecological footprints of human activities on the environment while ensuring socio-economic development. The concept of SD has been defined in a different way by diverse organizations and sectors¹. Construction industry is normally one of the leading businesses in both developed and developing nations in respect of employment, involvement to “gross domestic product (GDP)”, environmental footprint and investment^{2,3}. As one of the prime consumers of natural resources, the construction industry has a big part to play in SD. The effective management of the construction industry results in boosted tourism, improved life quality, money circulation, sustainable environment and job creation throughout the country⁴.

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“Industrial buildings (IBs)”, one of the largest segments of construction industry, are factories or other large premises mainly used for storing or manufacturing raw materials, goods or services for economic purposes^{5,6}. Despite of significant role of IBs in SD, few studies have been conducted to establish IBs from sustainable perspective. For instance, Zhao et al.⁷ employed the data envelopment analysis for prioritizing the most sustainable large development projects. In a study, Zeng et al.⁸ put forward hierarchy cluster analysis for investigating industrial sustainability of the manufacturing region. A novel automated tool has been developed for evaluating economic and environmental indicators in the simulation process of sour water stripping plant⁹. To achieve sustainable development goals in Iran, Heravi et al.¹⁰ assessed the IBs with sustainable viewpoints. Heravi et al.¹¹ studied a new decision-making methodology by combining grey doctrine and utility degree with ELECTRE method for assessing “sustainable industrial buildings (SIBs)”.

In earlier times, IB was considered as an isolated container under which production activities took place⁶. Nowadays, the design of IBs is not only limited to four walls and a roof in which certain production activities occurs but it considers the sustainable aspects including contamination caused by the construction process, reduction of greenhouse gas emissions, waste disposal, recycling, workers’ safety, job creation, minimum economic cost etc. With several conflicting qualitative and quantitative sustainability indicators/criteria, the process of SIB selection can be treated as a “multi-criteria decision-making (MCDM)” problem. Due to increasing complexity, imprecise data and vagueness of human mind, it is difficult for the “decision-making experts (DMEs)” to present exact numerical values for the considered attributes. In this regard, Zadeh’s proposal of “fuzzy set theory (FST)” has been accepted as a valuable tool and widely used in implementation to address the ambiguity of human decision.

Further, Atanassov¹² gave the theory of “intuitionistic fuzzy set (IFS)” to get over certain limitations of Zadeh’s FST. It is characterized by the “belongingness degree (BD)” and “non-belongingness degree (ND)”, wherein the values of BD and ND are real numbers between 0 and 1. The main difference between FST and IFS lies in the form of the expression: for FST, only the degree of belongingness is given to each element of the universe, while for IFS, not only the degree of belongingness but also the degree of non-belongingness is given, and their sum is less than or equal to one. In comparison with FST, IFSs could reflect individual’s evaluation results from both positive and negative aspects. There are several situations that can be modelled using IFS but cannot be represented using classical FST. For example, suppose voters may be partitioned into three groups of those who vote for, who vote against and who abstain. If we take $(v_1, 0.7, 0.2)$ as an element of IFS L of voting, we can interpret that “the vote for the applicant is 0.7 in favor to 0.2 against with 0.1 nonparticipations”. Therefore, IFSs are more comprehensive and reasonable than classical fuzzy sets in describing the uncertainty of an object. After the pioneering work of Atanassov¹², several researchers have presented many theories that have been widely used in the fields of clustering, pattern recognition, matching problem, plant leaf recognition, stock prediction etc.^{13–15}.

Research gaps. Based on the prior researches, the following challenges are identified:

- In the literature, some articles^{8,10,16–22} have presented to assess the sustainability in IBs but there is no study which considers the uncertainty of SIBs from intuitionistic fuzzy perspective.
- Several MCDM methods^{23–34} have been developed under intuitionistic fuzzy environment, but the “aggregation operators (AOs)” used in these studies have some counter-intuitive cases.
- The sustainability indicators play an important role in the assessment of IBs. However, the criteria weighting models given by^{10,17,19,22} are suitable only for finding the subjective weights of sustainability indicators. There is no study which determines the combined weights including the objective and subjective weights of sustainability indicators.
- One of the effective MCDM methods, the “additive ratio assessment (ARAS)”³⁵ evaluates and ranks the alternatives according to the utility function value. In this method, the ratio to the optimal value is determined to avoid the difficulties caused by different dimensions of criteria. In the context of IFSs, Mishra et al.^{36–38} proposed the ARAS-based decision support system for assessing the IT personnel selection problem from multiple criteria perspective. However, that study avoids the subjective weights of criteria, which considers the DMEs’ opinions while making a decision. In addition, the AOs used by Mishra et al.³⁶ have some limitations in group decision-making process.

Motivations and key contributions. Existing review studies contributed significantly to “sustainable development indicators (SDIs)” and its relevant subject areas; though, the existence of some important knowledge gaps motivated the present work. Some of these studies are focused upon a specific topic and some address “sustainable industrial building options (SIBOs)” as a topic amongst lots of other subtopics. Therefore, in this study, to classify the most important SDIs, a survey approach has been accomplished using literature review and specialists’ interviews. To assess the SIBOs, a hybrid MCDM technique is proposed by combining the fairly AO³⁹, “Method based on the Removal Effects of Criteria (MEREK)”⁴⁰, “Stepwise Weight Assessment Ratio Analysis (SWARA)”⁴¹ and ARAS methods with IFSs. The developed framework uses IFS theory to consider the uncertainty of information offered by the DMEs in the evaluation process.

Now, the key novelties of this work are presented as follows:

This paper develops an innovative decision-making framework based on fairly aggregation operator, MEREK, SWARA and ARAS methods with intuitionistic fuzzy information.

To aggregate the individual decision information and avoid the drawbacks of basic AOs of IFSs, this study proposes novel intuitionistic fuzzy fairly AOs with their desirable properties.

In the proposed framework, an incorporated criteria weighting model is proposed by combining the MEREC model for objective weights and the SWARA model for subjective weights under intuitionistic fuzzy environment.

This study implements the proposed decision-making framework on a case study of SIBOs assessment problem, in which the criteria weighting tool determines the priorities of the SDIs, while the present ARAS method evaluates and ranks the SIBOs under IFS context.

Organization of this study. The remaining sections are summarized as follows: “Literature review” reviews the literature related to the sustainable industrial buildings. “New intuitionistic fuzzy fairly aggregation operators” firstly discusses the basic definitions and then proposes novel fairly AOs for intuitionistic fuzzy numbers. “New IF-MEREC-SWARA-ARAS methodology” proposes a novel decision-making framework using the MEREC, the SWARA and the ARAS approaches under IFSs setting. “Implementation of proposed method: a case study” presents a case study of SIBOs assessment from intuitionistic fuzzy perspective. In addition, this section performs the sensitivity analysis and comparative study. At last, “Conclusions” presents the concluding remarks and recommendations for future studies.

Literature review

Here, this paper presents the comprehensive review of literature related to this study.

Sustainable development in industrial buildings. Generally environmental aspects of sustainability for IBs are emphasized because of the high materials, energy consumption and waste generation. Despite the fact that the effects of industrial development at regional levels and on economic growth of societies are undeniable. The IB plays one of the significant roles in the SD of any society; therefore, few research efforts have been made in this direction^{42–44}. Few researchers have focused their interest on ecological and economic aspects of sustainability in IBs and ignored the social aspect⁹.

Nowadays, sustainability awareness has become increasingly more significant for the society. In this respect, there are few studies that have analyzed innovation and SD together from a triple bottom line (TBL) perspective for IBs. For example, Zeng et al.⁸ utilized hierarchy cluster analysis for analyzing industrial sustainability. Chen et al.¹⁶ suggested an innovative framework to express the relationship among factory buildings, manufacturing equipment, the process of factory planning and TBL aspects of SD. Infante et al.¹⁸ considered the social, economic and environmental dimensions of sustainability in order to assess the leading corporations in the oil and gas sectors. Tan et al.²⁰ gave an innovative procedure for reuse assessment of IBs under fuzzy environment.

With the use of structural equation modeling, Heravi et al.¹⁰ analyzed and assessed the social, environmental and economic aspects in the selection of IBs. Cuadrado et al.¹⁷ proposed an “analytic hierarchy process (AHP)” method for sustainability assessment of IBs. Further, Heravi et al.¹¹ firstly analyzed and assessed the TBL aspects of SD in IBs. That study introduced a hybrid decision support system for evaluating IBs from sustainability perspectives. Vardopoulos²² proposed an application of fuzzy DEMATEL in the adaptive reuse of urban IBs. Milosevic et al.¹⁹ using the adjusted fuzzy AHP examined the potential for the adaptation of IBs in Nis in Serbia. Tian et al.²¹ structured an MCDM tool for evaluating their used IBs from SD perspective. Till now, no one has developed an integrated MCDM method for assessing SIBOs under IFS environment.

MCDM methods in sustainability. MCDM methods are considered as capable tools to help the scientists and engineers in solving decision-making applications. Over the past few decades, numerous theories and methods have been presented to treat the uncertainty of human intuition. After the pioneering idea of FST⁴⁵, several MCDM methods have been introduced within fuzzy set context⁴⁶. After the pioneering work of Atanassov¹², the theory of IFSs has been used more frequently to reflect the accurate semantics of DMEs.

Since its appearance, the theory of IFS and its applications have attracted more attention from scholars. For instance, Mousavi et al.⁴⁷ introduced a novel intuitionistic fuzzy relative closeness coefficient-based model for the evaluation of construction projects. They derived the DMEs’ significance values using an innovative intuitionistic fuzzy index and criteria’ weights using the concept of closer to ideal solution and farther from negative ideal solution. Cavallaro et al.²³ put forward a hybrid intuitionistic fuzzy MCDM model for assessing concentrated solar power technologies under IFS context. De et al.²⁴ firstly constructed the credit risk evaluation index system and further, suggested a hybrid tool using the AHP with IFS. Mishra and Rani²⁸ discussed a collective framework for choosing a cloud service provider from intuitionistic fuzzy perspective. Liang et al.²⁷ firstly proposed some new intuitionistic fuzzy distance measures and AOs, and further applied to develop an extended “multi-attribute border approximation area comparison (MABAC)” framework for treating correlative MCDM problems. Ghaderi et al.⁴⁸ developed a novel intuitionistic fuzzy information-based decision support system to evaluate and prioritize the decision-making units in accordance with their performances. Zhang et al.³⁴ put forward a novel intuitionistic fuzzy UTASTAR model in treating the low-carbon tourism destination selection. Liu et al.⁴⁹ recommended a latest intuitionistic fuzzy partitioned Bonferroni mean operator to treat the MCDM process. In order to assess the rooftop photovoltaic project sites, Gao et al.²⁶ recommended an MCDM methodology by combining intuitionistic fuzzy score function, prospect theory, analytical network process and linear weighting technique. Ocampo et al.²⁹ suggested the TOPSIS-Sort method with IFSs and demonstrated in arranging the restaurants for apparent experience of clients to COVID-19.

As the criteria weights are very important in making a decision, therefore, several weighting models have been developed in this context. To determine the objective weights of criteria, a novel MEREC model has been developed by Keshavarz-Ghorabae et al.⁴⁰. This method uses the removal effects of criteria in the decision matrix to derive their importance. Ecer and Aycin⁵⁰ introduced a new decision support system using MEREC

weighting-based score aggregation model and used for measuring innovation performance of G7 countries. Hezam et al.⁵¹ put forward an incorporated MCDM framework by combining the MEREC model with intuitionistic fuzzy double normalization-based multiple aggregation approach and applied to evaluate the alternative fuel vehicles problem. The MEREC method has combined with simple weighted sum product model for evaluate and rank the pallet trucks⁵². Recently, Keleş⁵³ measured the performances through MEREC model using geometric mean and harmonic mean as multiplicative functions.

For subjective weights of criteria, Kersulienė et al.⁴¹ initiated the SWARA model in which the experts' opinions are highly preferred. In comparison with AHP⁵⁴, the SWARA approach does not involve a large number of pairwise comparisons and has high consistency. In comparison with best worst method⁵⁵, the SWARA approach does not need to estimate multifaceted linear objective function, has minimum computational difficulty, and is effortless to utilize. In the recent times, the SWARA method has been combined with several MCDM methods under different contexts. Ghenai et al.⁵⁶ incorporated the SWARA with ARAS method to treat the renewable energy systems (RESs) with sustainability perspectives. Further, Alipour et al.⁵⁷ assessed the fuel cell and hydrogen components providers by means of a hybrid Pythagorean fuzzy SWARA-COPRAS approach. A hybrid Pythagorean fuzzy decision support system based on SWARA method has been developed for identifying the key barriers to the adoption of Internet of Things⁵⁸. Yücenur and Şenol⁵⁹ gave a novel decision-making method by combining SWARA and fuzzy "Visekriterijumska optimizacija I kompromisno rešenje (VIKOR)" approaches in waste removal and formation of lean creation procedures.

In the literature, several MCDM methods have been developed to solve the real-life decision-making problems such as construction projects evaluation⁴⁷, assessment of sustainable projects for municipality⁶⁰, sustainable feed stocks selection and renewable products allocation⁶¹, brick production technologies assessment⁶² and so forth. Each method has its own advantage and disadvantage³⁷. The ARAS³⁵, one of the popular MCDM methods, is based on the theory that complex phenomena of the world could be exactly perceived through simple relative comparisons. In terms of SD, Esmail and Geneletti⁶³ made a review of multiple criteria decision approaches in different problems of nature conservation. An integrated intuitionistic fuzzy ARAS method has suggested for assessing the multi-criteria IT personnel problem³⁸. In the context of sustainability, Kandakoglu et al.¹ gave the organized review of the work with multi-criteria in sustainability perspectives from 2010 to 2017. Rostamzadeh et al.⁶⁴ designed an innovative fuzzy information-based ARAS methodology for "sustainable third party reverse logistics providers (S3PRLP)" assessment. Karagöz⁶⁵ incorporated ARAS with "interval type-2 fuzzy sets (IT2FSs)" for the evaluation of recycling facility locations from SD context. Pandey et al.⁶⁶ provide a review on decision methods under uncertainty for clean energy.

Identification and evaluation of SDIs. In the context of SD, indicators should comprise TBL perspective of sustainability. Various building assessment techniques have been presented and employed from sustainable points of view. Because of explicit characteristics and industrial activities, industrial buildings are different from residential and commercial ones. The environmental, economic and social aspects are affecting up these buildings in a diverse manner, particularly when the concern arises to the developing nations from industrial development perspective. In most of the developing countries, sustainability is not being efficiently put in practice. In this study, this paper firstly identifies the sustainability indicators based on existing studies related to IBs^{10,67}. The SDIs and their references are shown in Table 1. The innovation of current research is the hybridization of SDIs and uncertain MCDM method to determine and rank SIBOs and presented in Fig. 1.

New intuitionistic fuzzy fairly aggregation operators

First of all, this section recalls the basic notions of IFSs and further introduces an innovative methodology for solving MCDM problems under IFS context.

Preliminaries. Atanassov¹² put forward the concept of IFSs, which is mathematically defined as

Definition 3.1¹². An IFS L on $\Theta = \{v_1, v_2, \dots, v_n\}$ is given by

$$L = \{\langle v_i, b_L(v_i), n_L(v_i) \rangle : v_i \in \Theta\}, \quad (1)$$

wherein $b_L : \Theta \rightarrow [0, 1]$ and $n_L : \Theta \rightarrow [0, 1]$ presents the "belongingness degree (BD)" and "non-belongingness degree (ND)" of v_i to L in Θ , with the constraint

$$0 \leq b_L(v_i) \leq 1, \quad 0 \leq n_L(v_i) \leq 1 \quad \text{and} \quad 0 \leq b_L(v_i) + n_L(v_i) \leq 1, \quad \forall v_i \in \Theta. \quad (2)$$

The intuitionistic index of an element $v_i \in \Theta$ to L is

$$\pi_L(v_i) = 1 - b_L(v_i) - n_L(v_i) \quad \text{and} \quad 0 \leq \pi_L(v_i) \leq 1, \quad \forall v_i \in \Theta. \quad (3)$$

Xu³³ defined this term $\langle b_L(v_i), n_L(v_i) \rangle$ as an "intuitionistic fuzzy number (IFN)" and denoted by $\wp = \langle b_\wp, n_\wp \rangle$ which satisfies $b_\wp, n_\wp \in [0, 1]$ and $0 \leq b_\wp + n_\wp \leq 1$.

Definition 3.2⁷⁹. For an IFN $\wp_j = \langle b_j, n_j \rangle$, the score and accuracy functions are defined as

$$\mathbb{S}^*(\wp_j) = \frac{1}{2}(b_j - n_j + 1) \quad (4)$$

Dimension	Indicators	References ^a
Environmental (EN)	U_1 : Climate change U_2 : Air pollution U_3 : Violation of animal's territory U_4 : Public health and safety U_5 : Workers and personnel's health and safety U_6 : Recycled/reused materials U_7 : Durable materials U_8 : Recycled water U_9 : Noise pollution U_{10} : Non-hazardous recyclable wastes U_{11} : Hazardous degradable wastes U_{12} : Non-hazardous non-recyclable wastes U_{13} : Renewable raw materials	[2], [5], [8], [9], [12], [15], [16] [3], [8], [11], [12], [16] [17], [18] [2], [3], [8], [9], [10], [11], [12], [14], [15] [2], [3], [5], [8], [9], [10], [11], [12], [14], [15], [16] [5], [8], [18] [2], [4], [7], [9], [15] [6], [18] [2], [3], [9], [10], [11], [15] [2], [3], [4], [7], [8], [9], [10], [11], [13], [15], [16] [2], [3], [4], [7], [8], [9], [10], [11], [13], [15], [16] [2], [3], [4], [7], [8], [9], [10], [11], [13], [15], [16] [3], [5], [6]
Social (SC)	U_{14} : Employment U_{15} : Public comfort U_{16} : Cultural heritage U_{17} : Natural heritage U_{18} : Migration effects U_{19} : Infrastructure improvement U_{20} : Workers and personnel comfort	[3], [11], [14] [1], [2], [3], [5], [9], [10], [11], [13], [15] [3], [10], [11] [3], [7], [18] [1], [18] [11], [18] [2], [4], [7], [9], [12], [15]
Economic (EC)	U_{21} : Effects on national economic indicators U_{22} : Cost of construction U_{23} : Innovation and technological advance U_{24} : Enhancement in capacity of infrastructure U_{25} : Cost of equipment and their installation U_{26} : Cost of operation and maintenance U_{27} : Effects on trade balance (National/Regional)	[17], [18] [2], [9], [15] [4], [7], [11], [12] [2], [9], [12], [15], [16] [2], [9], [15] [2], [9], [15] [1], [18]

Table 1. Evaluation and identification of sustainable development indicators (SDIs). ^a[1] Domac et al., 2005⁶⁸; [2] Von Geibler et al., 2006⁶⁹; [3] San-Jose et al., 2007⁴⁴; [4] Shen et al., 2007⁷⁰; [5] Ugwu and Haupt, 2007⁷¹; [6] USGBC, 2009⁷²; [7] Alwaer et al., 2008⁷³; [8] Aliand Al Nsairat, 2009⁷⁴; [9] Alwaer and Clements-Croome, 2010⁷⁵; [10] San-Jose Lombera and Garrucho Aprea, 2010⁴²; [11] Shen et al., 2011⁷⁶; [12] Bakhoum and Brown, 2012⁷⁷; [13] Chen et al., 2012¹⁶; [14] Cuadrado et al., 2012¹⁷; [15] Larimian et al., 2013⁷⁸; [16] Infante et al., 2013¹⁸; [17] Heravi et al., 2015¹⁰; [18] Heravi et al., 2017¹¹.

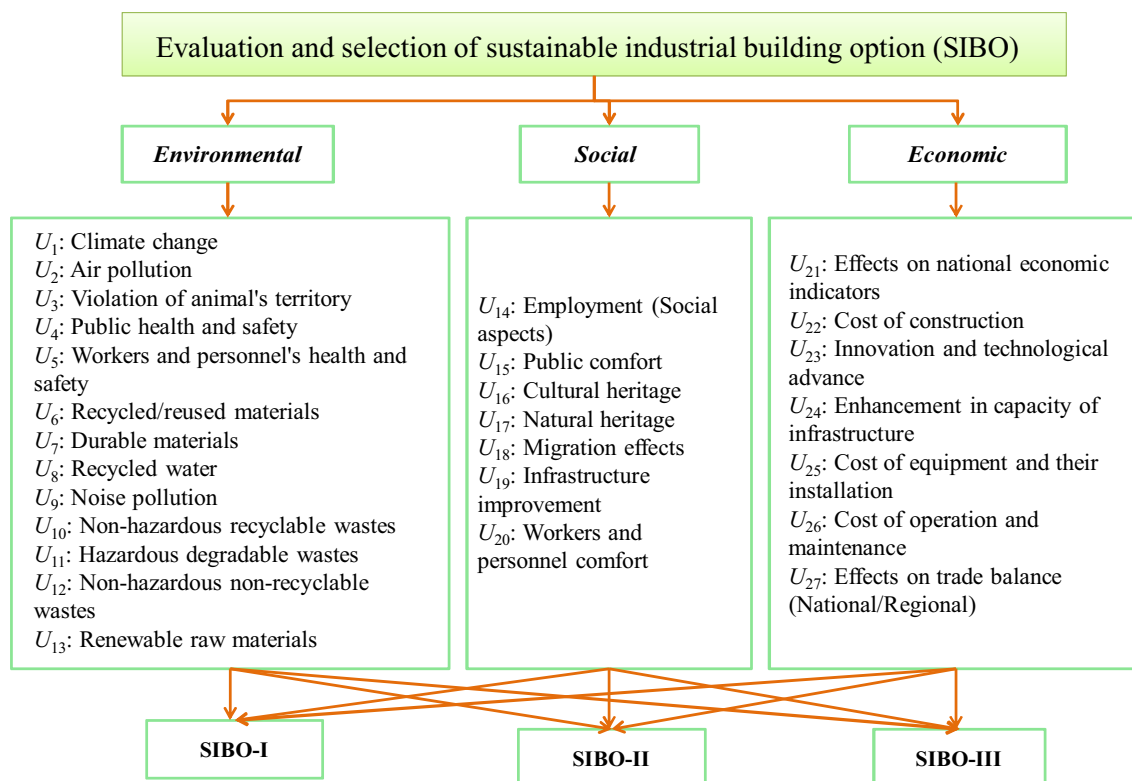


Figure 1. Research framework of selection sustainable industrial building options.

$$H(\wp_j) = \frac{1}{2}(b_j + n_j), \tag{5}$$

Clearly, $\mathbb{S}^*(\wp_j) \in [0, 1]$ and $H(\wp_j) \in [0, 1]$.

Definition 3.3³³. For any two IFNs $\wp_1 = \langle b_{\wp_1}, n_{\wp_1} \rangle$ and $\wp_2 = \langle b_{\wp_2}, n_{\wp_2} \rangle$, and $\alpha > 0$. Then, the basic operations on IFNs are described as.

- (i) $\wp_1^c = \langle n_{\wp_1}, b_{\wp_1} \rangle, \wp_2^c = \langle n_{\wp_2}, b_{\wp_2} \rangle$;
- (ii) $\wp_1 \oplus \wp_2 = \langle b_{\wp_1} + b_{\wp_2} - b_{\wp_1} b_{\wp_2}, n_{\wp_1} n_{\wp_2} \rangle$;
- (iii) $\wp_1 \otimes \wp_2 = \langle b_{\wp_1} b_{\wp_2}, n_{\wp_1} + n_{\wp_2} - n_{\wp_1} n_{\wp_2} \rangle$;
- (iv) $\wp_1 \cap \wp_2 = \langle \min \{b_{\wp_1}, b_{\wp_2}\}, \max \{n_{\wp_1}, n_{\wp_2}\} \rangle$;
- (v) $\wp_1 \cup \wp_2 = \langle \max \{b_{\wp_1}, b_{\wp_2}\}, \min \{n_{\wp_1}, n_{\wp_2}\} \rangle$;
- (vi) $\alpha \wp_1 = \langle (1 - (1 - b_{\wp_1})^\alpha), n_{\wp_1}^\alpha \rangle$;
- (vii) $\wp_1^\alpha = \langle b_{\wp_1}^\alpha, (1 - (1 - n_{\wp_1})^\alpha) \rangle$.

If $b_{\wp_1} = n_{\wp_1}$ and $b_{\wp_2} = n_{\wp_2}$, then by Definition 3.3, we obtain $b_{\wp_1 \oplus \wp_2} \neq n_{\wp_1 \oplus \wp_2}, b_{\wp_1 \otimes \wp_2} \neq n_{\wp_1 \otimes \wp_2}, b_{\alpha \wp_1} \neq n_{\alpha \wp_1}$ and $b_{\wp_1^\alpha} \neq n_{\wp_1^\alpha}$. For example, if $\wp_1 = \langle 0.3, 0.3 \rangle$ and $\wp_2 = \langle 0.4, 0.4 \rangle$, then the basic operations given in Definition 3.3 are as follows:

- (i) $\wp_1^c = \langle 0.3, 0.3 \rangle, \wp_2^c = \langle 0.4, 0.4 \rangle$;
- (ii) $\wp_1 \oplus \wp_2 = \langle 0.58, 0.12 \rangle$, where $b_{\wp_1 \oplus \wp_2} = 0.58$ and $n_{\wp_1 \oplus \wp_2} = 0.12$, therefore, $b_{\wp_1 \oplus \wp_2} \neq n_{\wp_1 \oplus \wp_2}$;
- (iii) $\wp_1 \otimes \wp_2 = \langle 0.12, 0.58 \rangle$, where $b_{\wp_1 \otimes \wp_2} = 0.12$ and $n_{\wp_1 \otimes \wp_2} = 0.58$, therefore, $b_{\wp_1 \otimes \wp_2} \neq n_{\wp_1 \otimes \wp_2}$;
- (iv) $\wp_1 \cap \wp_2 = \langle 0.3, 0.4 \rangle$;
- (v) $\wp_1 \cup \wp_2 = \langle 0.4, 0.3 \rangle$;
- (vi) $\alpha \wp_1 = \langle (1 - (1 - 0.3)^\alpha), 0.3^\alpha \rangle = \langle 0.1633, 0.5477 \rangle$ for $\alpha = 0.5$, where $b_{\alpha \wp_1} = 0.1633$ and $n_{\alpha \wp_1} = 0.5477$, therefore, $b_{\alpha \wp_1} \neq n_{\alpha \wp_1}$;
- (vii) $\wp_1^\alpha = \langle 0.3^\alpha, (1 - (1 - 0.3)^\alpha) \rangle = \langle 0.5477, 0.1633 \rangle$ for $\alpha = 0.5$, where $b_{\wp_1^\alpha} = 0.5477$ and $n_{\wp_1^\alpha} = 0.1633$, therefore, $b_{\wp_1^\alpha} \neq n_{\wp_1^\alpha}$.

Here, none of the operations $\wp_1 \oplus \wp_2, \wp_1 \otimes \wp_2, \alpha \wp_1, \wp_1^\alpha$ found to be fair or neutral in reality. To handle this issue, this paper introduces fairly operations on IFNs in next subsection.

Fairly operations on IFNs. In this part of the study, firstly fairly operations on IFNs are defined and further discussed their properties.

Definition 3.4³⁹. For any two IFNs $\wp_1 = \langle b_{\wp_1}, n_{\wp_1} \rangle$ and $\wp_2 = \langle b_{\wp_2}, n_{\wp_2} \rangle$, and $\alpha > 0$. The fairly operations are defined on IFNs, which as

- (i) $\wp_1 \tilde{\otimes} \wp_2 = \left\langle \left(\left(\frac{b_{\wp_1} b_{\wp_2}}{b_{\wp_1} b_{\wp_2} + n_{\wp_1} n_{\wp_2}} \right) \times (1 - (1 - b_{\wp_1} - n_{\wp_1})(1 - b_{\wp_2} - n_{\wp_2})) \right), \left(\left(\frac{n_{\wp_1} n_{\wp_2}}{b_{\wp_1} b_{\wp_2} + n_{\wp_1} n_{\wp_2}} \right) \times (1 - (1 - b_{\wp_1} - n_{\wp_1})(1 - b_{\wp_2} - n_{\wp_2})) \right) \right\rangle$;
- (ii) $\alpha * \wp_1 = \left\langle \left(\left(\frac{b_{\wp_1}^\alpha}{b_{\wp_1}^\alpha + n_{\wp_1}^\alpha} \right) \times (1 - (1 - b_{\wp_1} - n_{\wp_1})^\alpha) \right), \left(\left(\frac{n_{\wp_1}^\alpha}{b_{\wp_1}^\alpha + n_{\wp_1}^\alpha} \right) \times (1 - (1 - b_{\wp_1} - n_{\wp_1})^\alpha) \right) \right\rangle$.

Proposition 3.1 Let us consider that $\wp_1 = \langle b_{\wp_1}, n_{\wp_1} \rangle$ and $\wp_2 = \langle b_{\wp_2}, n_{\wp_2} \rangle$ be two IFNs and $\alpha > 0$. If $b_{\wp_1} = n_{\wp_1}$ and $b_{\wp_2} = n_{\wp_2}$, then

- (i) $b_{\wp_1 \tilde{\otimes} \wp_2} = n_{\wp_1 \tilde{\otimes} \wp_2}$,
- (ii) $b_{\alpha * \wp_1} = n_{\alpha * \wp_1}$.

Proof

(i) Since $b_{\wp_1} = n_{\wp_1}$ and $b_{\wp_2} = n_{\wp_2}$, then

$$\frac{b_{\wp_1 \tilde{\otimes} \wp_2}}{n_{\wp_1 \tilde{\otimes} \wp_2}} = \frac{\left(\frac{b_{\wp_1} b_{\wp_2}}{b_{\wp_1} b_{\wp_2} + n_{\wp_1} n_{\wp_2}} \right) \times (1 - (1 - b_{\wp_1} - n_{\wp_1})(1 - b_{\wp_2} - n_{\wp_2}))}{\left(\frac{n_{\wp_1} n_{\wp_2}}{b_{\wp_1} b_{\wp_2} + n_{\wp_1} n_{\wp_2}} \right) \times (1 - (1 - b_{\wp_1} - n_{\wp_1})(1 - b_{\wp_2} - n_{\wp_2}))} = \left(\frac{b_{\wp_1} b_{\wp_2}}{n_{\wp_1} n_{\wp_2}} \right) = 1.$$

Thus, $b_{\wp_1 \tilde{\otimes} \wp_2} = n_{\wp_1 \tilde{\otimes} \wp_2}$.

(ii) By following (i), we can show that $b_{\alpha * \wp_1} = n_{\alpha * \wp_1}$ for $b_{\wp_1} = n_{\wp_1}$ and $b_{\wp_2} = n_{\wp_2}$.

For the same example as given in section "Intuitionistic fuzzy weighted fairly AO", we get $\wp_1 \tilde{\otimes} \wp_2 = \langle 0.46, 0.46 \rangle$, where $b_{\wp_1 \tilde{\otimes} \wp_2} = n_{\wp_1 \tilde{\otimes} \wp_2}$. Also, we obtain $\alpha * \wp_1 = \langle 0.1838, 0.1838 \rangle$, where $b_{\alpha * \wp_1} = n_{\alpha * \wp_1}$.

Theorem 3.1 For any two IFNs $\wp_1 = \langle b_{\wp_1}, n_{\wp_1} \rangle$ and $\wp_2 = \langle b_{\wp_2}, n_{\wp_2} \rangle$, and three real numbers $\alpha, \alpha_1, \alpha_2 > 0$, we obtain

- (i) $\wp_1 \tilde{\otimes} \wp_2 = \wp_2 \tilde{\otimes} \wp_1$,
- (ii) $\alpha * (\wp_1 \tilde{\otimes} \wp_2) = (\alpha * \wp_1) \tilde{\otimes} (\alpha * \wp_2)$,
- (iii) $(\alpha_1 + \alpha_2) * \wp_1 = (\alpha_1 * \wp_1) \tilde{\otimes} (\alpha_2 * \wp_1)$.

Proof It is easy to prove by Definition 3.4, thus, the proof is omitted.

Intuitionistic fuzzy weighted fairly AO. In this section, weighted fairly AO is developed for IFNs. Further, their properties are presented in details.

Definition 3.6. Let $\wp_j = \langle b_j, n_j \rangle; j = 1(1)t$ be the set of IFNs. Then the "intuitionistic fuzzy weighted fairly AO (IFWFAO)" is given by

$$IFWFAO(\wp_1, \wp_2, \dots, \wp_t) = (\omega_1 * \wp_1) \tilde{\otimes} (\omega_2 * \wp_2) \tilde{\otimes} (\omega_3 * \wp_3) \tilde{\otimes} \dots \tilde{\otimes} (\omega_t * \wp_t),$$

where ω_j is the weight of $\wp_j (j = 1(1)t)$ satisfying $\omega_j > 0$ and $\sum_{j=1}^t \omega_j = 1$.

Theorem 3.2 The aggregated value by using IFWFAO is also an IFN and given by

$$IFWFAO(\wp_1, \wp_2, \dots, \wp_t) = \left(\left(\frac{\prod_{j=1}^t (b_j)^{\omega_j}}{\prod_{j=1}^t (b_j)^{\omega_j} + \prod_{j=1}^t (n_j)^{\omega_j}} \times \left(1 - \prod_{j=1}^t (1 - b_j - n_j)^{\omega_j} \right) \right), \left(\frac{\prod_{j=1}^t (n_j)^{\omega_j}}{\prod_{j=1}^t (b_j)^{\omega_j} + \prod_{j=1}^t (n_j)^{\omega_j}} \times \left(1 - \prod_{j=1}^t (1 - b_j - n_j)^{\omega_j} \right) \right) \right), \tag{6}$$

where ω_j is the weight of $\wp_j (j = 1(1)t)$ satisfying $\omega_j > 0$ and $\sum_{j=1}^t \omega_j = 1$.

Proof In the following, we will prove Eq. (6) with the use of mathematical induction. It is evident that Eq. (6) is true for $t = 1$. Suppose that Eq. (6) is true for $t = k$, therefore

$$IFWFAO(\wp_1, \wp_2, \dots, \wp_m) = \left\langle \left(\frac{\prod_{j=1}^m (b_j)^{\omega_j}}{\prod_{j=1}^m (b_j)^{\omega_j} + \prod_{j=1}^m (n_j)^{\omega_j}} \times \left(1 - \prod_{j=1}^m (1 - b_j - n_j)^{\omega_j} \right) \right), \left(\frac{\prod_{j=1}^m (n_j)^{\omega_j}}{\prod_{j=1}^m (b_j)^{\omega_j} + \prod_{j=1}^m (n_j)^{\omega_j}} \times \left(1 - \prod_{j=1}^m (1 - b_j - n_j)^{\omega_j} \right) \right) \right\rangle.$$

When $t = m + 1$, we have

$$IFWFAO(\wp_1, \wp_2, \dots, \wp_m, \wp_{m+1}) = (\omega_1 * \wp_1) \tilde{\otimes} (\omega_2 * \wp_2) \tilde{\otimes} (\omega_3 * \wp_3) \tilde{\otimes} \dots \tilde{\otimes} (\omega_m * \wp_m) \tilde{\otimes} (\omega_{m+1} * \wp_{m+1})$$

$$= \left\langle \left(\frac{\prod_{j=1}^m (b_j)^{\omega_j}}{\prod_{j=1}^m (b_j)^{\omega_j} + \prod_{j=1}^m (n_j)^{\omega_j}} \times \left(1 - \prod_{j=1}^m (1 - b_j - n_j)^{\omega_j} \right) \right), \left(\frac{\prod_{j=1}^m (n_j)^{\omega_j}}{\prod_{j=1}^m (b_j)^{\omega_j} + \prod_{j=1}^m (n_j)^{\omega_j}} \times \left(1 - \prod_{j=1}^m (1 - b_j - n_j)^{\omega_j} \right) \right) \right\rangle \tilde{\otimes} \left\langle \left(\frac{(b_{m+1})^{\omega_{m+1}}}{(b_{m+1})^{\omega_{m+1}} + (n_{m+1})^{\omega_{m+1}}} \times \left(1 - (1 - b_{m+1} - n_{m+1})^{\omega_{m+1}} \right) \right), \left(\frac{(n_{m+1})^{\omega_{m+1}}}{(b_{m+1})^{\omega_{m+1}} + (n_{m+1})^{\omega_{m+1}}} \times \left(1 - (1 - b_{m+1} - n_{m+1})^{\omega_{m+1}} \right) \right) \right\rangle$$

Thus, by Definition 3.4, we have

$$IFWFAO(\wp_1, \wp_2, \dots, \wp_m, \wp_{m+1}) = \left\langle \left(\frac{\prod_{j=1}^{m+1} (b_j)^{\omega_j}}{\prod_{j=1}^{m+1} (b_j)^{\omega_j} + \prod_{j=1}^{m+1} (n_j)^{\omega_j}} \times \left(1 - \prod_{j=1}^{m+1} (1 - b_j - n_j)^{\omega_j} \right) \right), \right. \\ \left. \left(\frac{\prod_{j=1}^{m+1} (n_j)^{\omega_j}}{\prod_{j=1}^{m+1} (b_j)^{\omega_j} + \prod_{j=1}^{m+1} (n_j)^{\omega_j}} \times \left(1 - \prod_{j=1}^{m+1} (1 - b_j - n_j)^{\omega_j} \right) \right) \right\rangle.$$

i.e., Eq. (6) holds for $t = m + 1$.

Therefore, Eq. (6) holds for all t . This completes the proof.

Definition 3.6 Consider a collection of IFNs $\wp_j = (b_j, n_j)$ ($j = 1(1)t$). Let $\omega = (\omega_1, \omega_2, \dots, \omega_t)^T$ be the weight vector of \wp_j ($j = 1(1)t$), satisfying that $\omega_j > 0$ and $\sum_{j=1}^t \omega_j = 1$. Then the “intuitionistic fuzzy ordered weighted fairly AO (IFOWFAO)” is defined as

$$IFOWFAO(\wp_1, \wp_2, \dots, \wp_t) = (\omega_1 * \wp_{\sigma(1)}) \tilde{\otimes} (\omega_2 * \wp_{\sigma(2)}) \tilde{\otimes} (\omega_3 * \wp_{\sigma(3)}) \tilde{\otimes} \dots \tilde{\otimes} (\omega_t * \wp_{\sigma(t)}),$$

wherein $(\sigma(1), \sigma(2), \dots, \sigma(t))$ denotes the permutation of $(1, 2, \dots, t)$ with $\wp_{\sigma(j-1)} \geq \wp_{\sigma(j)}$, $\forall j = 2, 3, \dots, t$.

Theorem 3.3 The aggregated value by using IFOWFAO is also an IFN, defined by

$$IFOWFAO(\wp_1, \wp_2, \dots, \wp_t) = \left\langle \left(\frac{\prod_{j=1}^t (b_{\sigma(j)})^{\omega_j}}{\prod_{j=1}^t (b_{\sigma(j)})^{\omega_j} + \prod_{j=1}^t (n_{\sigma(j)})^{\omega_j}} \times \left(1 - \prod_{j=1}^t (1 - b_{\sigma(j)} - n_{\sigma(j)})^{\omega_j} \right) \right), \right. \\ \left. \left(\frac{\prod_{j=1}^t (n_{\sigma(j)})^{\omega_j}}{\prod_{j=1}^t (b_{\sigma(j)})^{\omega_j} + \prod_{j=1}^t (n_{\sigma(j)})^{\omega_j}} \times \left(1 - \prod_{j=1}^t (1 - b_{\sigma(j)} - n_{\sigma(j)})^{\omega_j} \right) \right) \right\rangle. \quad (7)$$

Proof Similar as Theorem 3.2.

Based on Theorems 3.2 and 3.3, we derive the following properties:

Property 3.1 (Idempotency). If all IFNs $\wp_j = (b_j, n_j)$ ($j = 1(1)t$) are equal, i.e., $\wp_j = \wp = (b, n)$, then $IFWFAO(\wp_1, \wp_2, \dots, \wp_t) = \wp$ and $IFOWFAO(\wp_1, \wp_2, \dots, \wp_t) = \wp$.

Property 3.2 (Boundedness). For a collection of IFNs $\wp_j = (b_j, n_j)$ ($j = 1(1)t$), let $\wp^- = \min_j \wp_j$ and $\wp^+ = \max_j \wp_j$. Then, we have $\wp^- \leq IFWFAO(\wp_1, \wp_2, \dots, \wp_t) \leq \wp^+$ and $\wp^- \leq IFOWFAO(\wp_1, \wp_2, \dots, \wp_t) \leq \wp^+$.

Property 3.3 (Monotonicity). Let $\wp_j = (b_{\wp_j}, n_{\wp_j})$ and $\wp_j = (b_{\wp_j}, n_{\wp_j})$ ($j = 1(1)t$) be the group of FFNs and $\wp_j \leq \wp_j$, i.e., $b_{\wp_j} \leq b_{\wp_j}$ and $n_{\wp_j} \geq n_{\wp_j}$, $\forall j = 1(1)t$. Then

$$IFWFAO(\wp_1, \wp_2, \dots, \wp_t) \leq IFWFAO(\wp_1, \wp_2, \dots, \wp_t)$$

and

$$IFOWFAO(\wp_1, \wp_2, \dots, \wp_t) \leq IFOWFAO(\wp_1, \wp_2, \dots, \wp_t).$$

New IF-MEREC-SWARA-ARAS methodology

In this part of the study, a decision support system is established to prioritize the list of alternatives based on multiple criteria on IFs setting. In this respect, an integrated IF-MEREC-SWARA-ARAS technique is given for solving MCDM issues with fully unknown criteria and DMEs' weights. In this process, the IF-MEREC-SWARA model has employed for deriving the combined weights of indicators. In addition, the IFWFA operator is utilized for aggregating the single DME's opinions. On the other hand, the ARAS technique has employed for estimating the prioritization of the alternatives. The outline of the IF-MEREC-SWARA-ARAS methodology is depicted as follows (see Fig. 2):

Step 1: Create the “linguistic decision matrix (LDM)”.

A team of DMEs $T = \{t_1, t_2, \dots, t_\ell\}$ has been made to find the best option(s) among a set of alternatives/options $M = \{M_1, M_2, \dots, M_m\}$ over the criterion set $U = \{U_1, U_2, \dots, U_n\}$. Consider that $Z^{(k)} = (\xi_{ij}^{(k)})_{m \times n}$ be a “linguistic decision-matrix (LDM)” offered by the DMEs, wherein $\xi_{ij}^{(k)}$ refers to the performance of M_i over a criterion U_j in terms of “linguistic values (LVs)” given by k th DME.

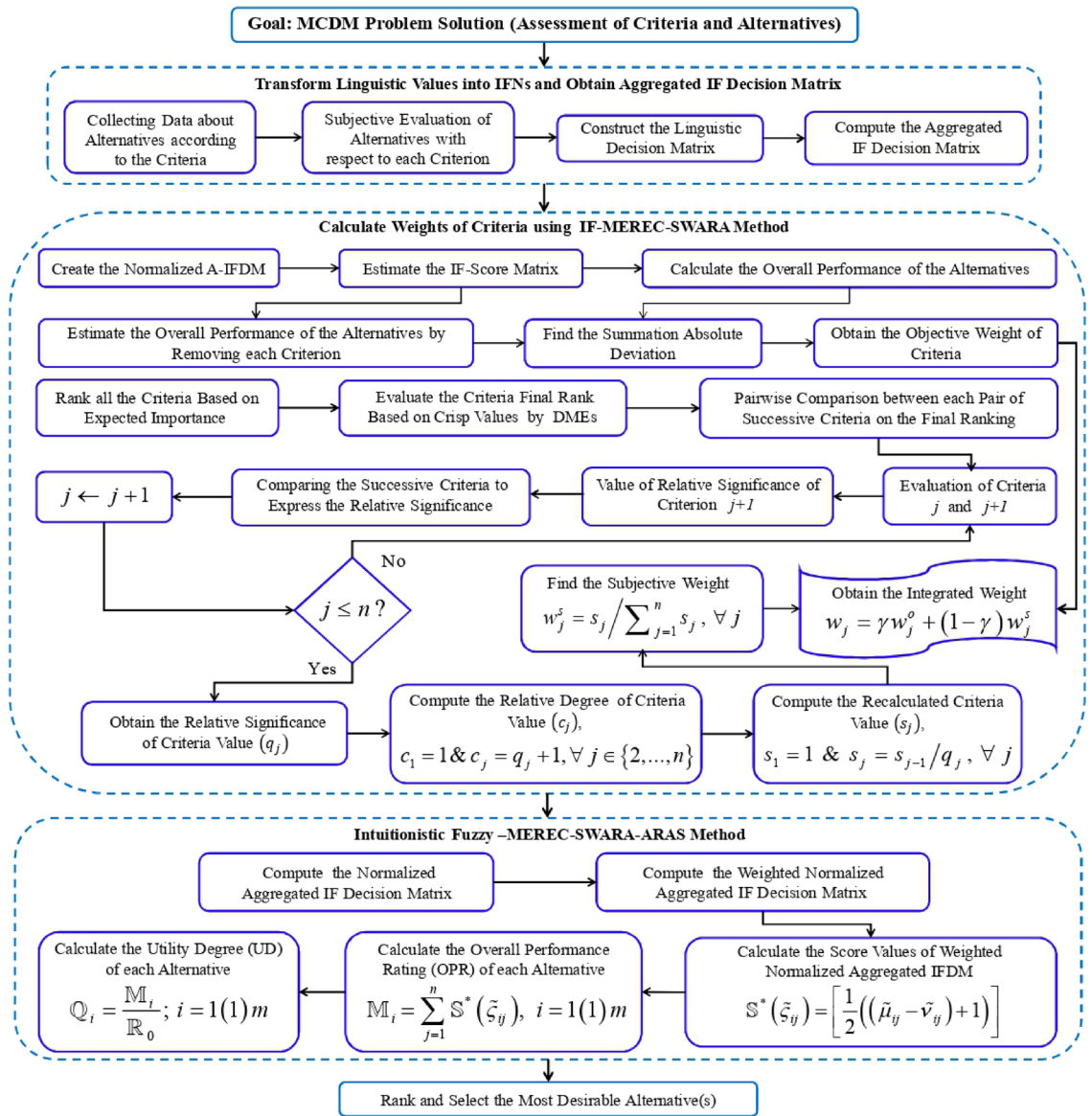


Figure 2. Diagrammatic representation of IF-MEREC-SWARA-ARAS method.

Step 2: Evaluation of DMEs’ weights.

Let $\eta = (\eta_1, \eta_2, \dots, \eta_\ell)^T$ be a set of DMEs’ weights. Let $R_k = (b_k, n_k)$ be an IFN for the evaluation of k th DME. Then, the weighting formula for k^{th} expert is shown in Eq. (8).

$$\eta_k = \frac{\left(b_k + \pi_k \left(\frac{b_k}{b_k + n_k}\right)\right)}{\sum_{k=1}^{\ell} \left(b_k + \pi_k \left(\frac{b_k}{b_k + n_k}\right)\right)}, \quad k = 1(1)\ell. \tag{8}$$

Step 3: Build the “aggregated intuitionistic fuzzy decision-matrix (A-IFDM)”.

To determine the A-IFDM, it is essential to merge each individual LDM into an A-IFDM in accordance with DMEs’ opinions. In this regard, IFWFAO is applied and then obtained the A-IFDM $\mathbb{R} = (\bar{\xi}_{ij})_{m \times n}$, where

$$\bar{\xi}_{ij} = IFWA_{\eta} \left(\xi_{ij}^{(1)}, \xi_{ij}^{(2)}, \dots, \xi_{ij}^{(\ell)} \right) = \left(1 - \prod_{k=1}^{\ell} (1 - b_k)^{\eta_k}, \prod_{k=1}^{\ell} (n_k)^{\eta_k} \right). \tag{9}$$

Step 4: Combined weight-determining model for criteria weights.

In this step, firstly the objective and subjective weights of criteria are derived, and then integrated to find the final criteria weights. This process involves the following cases:

Case I: IF-MEREC for objective weights of criteria⁸⁰.

This model has the following steps:

Step 4a: Compute the “normalized A-IFDM (NA-IFDM)”.

In the process of MCDM, the A-IFDM $\mathbb{R} = (\bar{\xi}_{ij})_{m \times n}$ is transformed into NA-IFDM $\mathbb{N} = (\varsigma_{ij})_{m \times n}$ such that

$$\varsigma_{ij} = \begin{cases} \bar{\xi}_{ij} = (\bar{b}_{ij}, \bar{n}_{ij}), & j \in U_b \\ (\bar{\xi}_{ij})^c = (\bar{n}_{ij}, \bar{b}_{ij}), & j \in U_c \end{cases} \tag{10}$$

where U_b and U_n represent the benefit and cost types of criteria sets, respectively.

Step 4b: Compute the score matrix.

Using Eq. (11), find the score matrix $\Omega = (\eta_{ij})_{m \times n}$ of each IFN ς_{ij} .

$$\eta_{ij} = \frac{1}{2}((\bar{b}_{ij}) - (\bar{n}_{ij}) + 1). \tag{11}$$

Step 4c: Determine the overall performance of the options.

Based on step 4b, we can ensure that the smaller values of η_{ij} provides the better values of the performances. To compute the overall performance of each option, Eq. (12) is utilized.

$$S_i = \ln \left(1 + \left(\frac{1}{n} \sum_j |\ln(\eta_{ij})| \right) \right). \tag{12}$$

Step 4d: Find the performance of the options by removal of criteria separately.

The performance of each option is determined by removing each criterion individually, given by

$$S'_{ij} = \ln \left(1 + \left(\frac{1}{n} \sum_{k, k \neq j} |\ln(\eta_{ik})| \right) \right). \tag{13}$$

Thus, n sets of performances are achieved concerning n criteria.

Step 4e: Sum of absolute deviations.

Let V_j denote the removal effect of j th criterion, which is calculated as

$$V_j = \sum_i |S'_{ij} - S_i|. \tag{14}$$

Step 4f: Derive the objective weights of criteria.

The objective weight of each criterion is determined by Eq. (15).

$$w_j^o = \frac{V_j}{\sum_{j=1}^n V_j}. \tag{15}$$

Case II: IF-SWARA approach for subjective weights of criteria.

The SWARA approach starts by prioritizing the attributes and then pairwise assesses the higher rank attribute to the lower rank attribute. The procedures are as follows:

Step 4g: Compute the score values using Definition 3.2.

Step 4h: Based on DMEs’ preferences, grade the criteria from most significance to the least significance.

Step 4i: The relative significance is derived from the attributes that are placed in the second spot, and succeeding relative significance is found with the attribute j and attribute $j - 1$.

Step 4j: The relative degree c_j is assessed as follows:

$$c_j = \begin{cases} 1, & j = 1 \\ q_j + 1, & j > 1, \end{cases} \tag{16}$$

wherein q_j is the relative significance of average degree.

Step 4k: The initial weight s_j is obtained using

$$s_j = \begin{cases} 1, & j = 1 \\ \frac{s_{j-1}}{q_j}, & j > 1. \end{cases} \tag{17}$$

Step 4l: The subjective weights of criteria is

$$w_j = \frac{s_j}{\sum_{j=1}^n s_j}, \forall j. \tag{18}$$

Case III: Derive the final weights.

Based on the objective and subjective weights of criteria, an incorporated weighting formula is presented by Eq. (19).

$$w_j = \gamma w_j^o + (1 - \gamma) w_j^s, \quad j = 1, 2, \dots, n, \quad (19)$$

wherein $\gamma \in [0, 1]$ is the “precision objective factor of decision strategy”.

Step 5: Define “optimal evaluation degree (OED)” of options using Eq. (20).

$$\mathbb{R}_0 = \begin{cases} \max \xi_{ij}, & j \in U_b, \\ \min \xi_{ij}, & j \in U_c. \end{cases} \quad (20)$$

where U_b and U_c are the benefit and cost-types of attributes, respectively.

Step 6: Obtain the “weighted NA-IFDM (WNA-IFDM)”.

The WNA-IFDM $\mathbb{N}_w = (\tilde{\zeta}_{ij})_{m \times n}$ is computed using Eq. (21).

$$\tilde{\zeta}_{ij} = \bigoplus_{j=1}^n w_j \zeta_{ij} = \left\langle 1 - \prod_{j=1}^n (1 - b_{ij})^{w_j}, \prod_{j=1}^n (n_{ij})^{w_j} \right\rangle, \quad (21)$$

wherein $\zeta_{ij} = \langle \tilde{b}_{ij}, \tilde{n}_{ij} \rangle$ is the weighted IFN.

Step 7: Evaluation of IF-Score values.

By using Eq. (4), the score degrees of WNA-IFDM $\mathbb{N}_w = (\tilde{\zeta}_{ij})_{m \times n}$ are computed as follows:

$$\mathbb{S}^*(\tilde{\zeta}_{ij}) = \left[\frac{1}{2} \left((\tilde{b}_{ij} - \tilde{n}_{ij}) + 1 \right) \right]. \quad (22)$$

Step 8: Determine the “overall performance rating (OPR)” and “degree of utility (UD)”.

The OPR of each alternative is computed by

$$\mathbb{M}_i = \sum_{j=1}^n \mathbb{S}^*(\tilde{\zeta}_{ij}), \quad \forall i. \quad (23)$$

The highest degree of OPR \mathbb{M}_i elucidates the more efficient alternative. The preferences of alternatives can be evaluated using Eq. (23). To find the appropriate options, it is not only necessary to obtain the best ranked candidate but also important to assess the relative influence of considered options, in association to the appropriate candidate. The UD of each option is computed by Eq. (24).

$$\mathbb{Q}_i = \frac{\mathbb{M}_i}{\mathbb{R}_0}; \quad \mathbb{Q}_i \in [0, 1]. \quad (24)$$

Step 9: Estimate the most suitable candidate.

The best alternative can be obtained using

$$\mathbb{M}^* = \left\{ \mathbb{M}_i \mid \max_i \mathbb{Q}_i; \quad i = 1(1)m \right\}, \quad (25)$$

wherein \mathbb{M}^* is most desirable candidate.

Implementation of proposed method: a case study

In the current portion, the developed methodology is utilized on a case study of “sustainable industrial buildings option (SIBO)” selection in India. In this study, we have taken three real petrochemical projects as alternatives. The considered options are taken to be in diverse settings to assess the impact of location-based indicators (e.g. cultural, migration effects and natural heritage), and these sites are among the large cities of India.

Allocating precise data is a difficult task for DMEs in every MCDM problem¹¹. Utilizing IFNs can offer the possibility to tackle ambiguity and uncertainty in DME’s decisions. Thus, the DME does not need to allocate specific values to SDIs. Furthermore, the merits of fairly AO are their observation over the preferences and risk attitudes of DMEs. Hence, in this section, a hybrid model is presented that takes the advantages of IFNs and fairly AO to offer a flexible environment for MCDM. As it is obvious the real world is overwhelmed with uncertainty and vague information, in addition the preferences of DMEs during the MCDM process are not just ordinal sorted, but rather influenced by their risk attitudes. Thus, the ideas of incorporation of IFNs to deal with uncertainty and also AOs to consider risk attitudes and preferences were to make the developed framework more compatible with the real world situations.

To assess the recognized SDIs through literature and perspectives of highly experienced and DMEs in differently located yet significant petrochemical plants of the nation, a questionnaire survey was conducted. Questionnaire permits to reach views and attitudes from a certain respondents as a sample with a quantitative assessment¹¹. The final determination is to allocate the significance levels to the SDIs to be accordingly usable for the MCDM procedure.

In order to validate the suitability on the SDIs’ list and to make sure that the recognized SDIs are practically applicable, a pilot survey was carried out through semi-structured interviews with six experts involved

in petrochemical projects in India. Without any guidance, they presented some definite expertise requests for qualifying of DMEs using a panel, which are applied for determination and qualification of following DMEs, in this study: (a) a professor of founding benchmarks and frameworks with 25 years of experience; (b) Environment, Health and Safety (EHS) expert and operations manager with 20 years of experience; (c) administrator of petrochemical projects assessment with 15 years of experience; (d) financial manager with 20 years of experience. Further, the questionnaire is designed to conduct face to face interview with DME panel, as implemented in first round of survey. In this way, DMEs were able to mention their thoughts, accurate possible errors, and check the compatibility of SDIs with the recent concerns. The outcomes of survey certified that the recognized SDIs are to a high degree compatible with the issues, and no conflicting views received from the DME panel, consequently, execution the second round of survey was not required.

The questionnaire was circulated among 25 professionals, comprising researchers, contractors, and consultant firms with minimum 05 years of experience of petrochemical projects in India. The customary approach to define the participants views related to the significance ratings is the 11-point Likert scale. Though, the views of participants can be imprecise and subjective and the similar words can be observed separately and diverse by the participants due to vagueness. Thus, utilizing crisp numbers are not appropriate to explain the LVs and views addressing significance ratings. In order to treat with the vagueness and uncertainty, IFNs are used to express the linguistic significance ratings and given in Tables 2 and 3. Thus, the relative significance of SDIs is examined and defined using the Likert scale.

For this evaluation process, a set of four DMEs, who are all very skilled in the selected region. Suppose that it is not promising to assess and associate all the projects exactly using the whole recognized SDIs (Table 1). Consequently, the assessment of options were done using a limited number of recognized SDIs, though, the SDIs were the similar for considered options. Here, we choose 27 SDIs (Table 1) based on operation stage of project life cycle. The DME's opinions and the accessible information on SDIs are the key parameters in this evaluation process. Here, we implement the proposed method on SIBOs assessment problem.

LVs	IFNs
Highly considerable (HC)	(0.90, 0.10)
Very considerable (VC)	(0.80, 0.15)
Considerable (C)	(0.70, 0.25)
Average (A)	(0.50, 0.45)
Inconsiderable (I)	(0.40, 0.55)
Very inconsiderable (VI)	(0.20, 0.75)
Extremely inconsiderable (EI)	(0.10, 0.90)

Table 2. Performance rating of DMEs in form of LVs.

LVs	IFNs
Completely satisfactory (CS)	(0.95, 0.05)
Highly satisfactory (HS)	(0.85, 0.10)
Very satisfactory (VS)	(0.80, 0.15)
Satisfactory (S)	(0.70, 0.20)
Slight satisfactory (SS)	(0.60, 0.30)
Fair (F)	(0.50, 0.40)
Slight unsatisfactory (SU)	(0.40, 0.50)
Unsatisfactory (U)	(0.30, 0.60)
Very unsatisfactory (VU)	(0.20, 0.70)
Highly unsatisfactory (HU)	(0.10, 0.80)
Entirely unsatisfactory (EU)	(0.05, 0.95)

Table 3. LVs for performance ranking of options.

DMEs	t_1	t_2	t_3	t_4
LVs	VC(0.80, 0.15)	C(0.70, 0.25)	A(0.50, 0.45)	I(0.40, 0.55)
DMEs Weight	0.333	0.2917	0.2083	0.1667

Table 4. DMEs' weights for SIBO selection.

	M_1	M_2	M_3
U_1	(SU,VU,VU,F)	(FSU,VU,U)	(S,SS,F,F)
U_2	(U,U,F,SS)	(U,VU,VU,SU)	(S,F,SS,F)
U_3	(S,VS,S,S)	(S,VS,VS,S)	(SU,F,S,F)
U_4	(SU,F,S,SS)	(VS,F,S,S)	(SU,SU,SS,F)
U_5	(SU,SS,S,F)	(SU,S,S,VS)	(SS,SU,F,F)
U_6	(VU,SU,U,VU)	(FVU,U,VU)	(VS,S,F,SU)
U_7	(SU,SS,U,F)	(U,VU,U,VU)	(F,SS,F,VS)
U_8	(S,VS,VS,SS)	(F,S,VS,VS)	(SU,F,SS,VU)
U_9	(SU,U,U,F)	(FVS,S,S)	(F,SU,S,F)
U_{10}	(U,VS,S,F)	(SU,SS,S,VS)	(F,SS,SU,F)
U_{11}	(SU,U,U,VU)	(SS,U,U,VU)	(SS,S,F,U)
U_{12}	(S,F,S,SS)	(SU,F,SU,VU)	(S,VS,F,SU)
U_{13}	(SS,F,S,VS)	(F,SS,S,VS)	(SU,SS,SU,F)
U_{14}	(SU,F,S,SS)	(SU,SS,S,VS)	(SU,VS,SS,F)
U_{15}	(VS,SS,F,F)	(SU,VS,S,SS)	(F,SU,VS,F)
U_{16}	(SU,U,VU,U)	(F,U,VU,VU)	(SS,F,VS,F)
U_{17}	(SU,SU,F,F)	(U,VU,SU,VU)	(SS,SU,F,SS)
U_{18}	(SS,VS,S,VS)	(F,VS,S,VS)	(F,VU,U,F)
U_{19}	(SU,F,S,SU)	(SS,VS,S,SU)	(SU,SS,F,SU)
U_{20}	(SS,F,S,F)	(F,SS,F,VS)	(SU,VU,F,VU)
U_{21}	(U,F,VU,SU)	(VU,U,SU,SU)	(SS,S,S,U)
U_{22}	(SU,U,VU,F)	(U,VU,VU,F)	(F,SS,VU,S)
U_{23}	(SS,VS,F,S)	(S,VS,SS,S)	(SS,F,SU,U)
U_{24}	(SU,F,S,SS)	(F,S,F,S)	(S,F,SU,U)
U_{25}	(SU,U,VU,VU)	(F,SU,S,VU)	(SU,SS,U,F)
U_{26}	(U,VU,F,VU)	(F,SS,SU,U)	(F,S,SS,S)
U_{27}	(F,VS,S,F)	(F,SU,F,F)	(U,VU,SU,VU)

Table 5. LDM for SIBO selection.

For this case study, Table 2 presents the “linguistic values (LVs)” and the corresponding IFNs for the SDIs and the IBs evaluation. Table 3 illustrates the LVs by DMEs for the criteria of considered evaluation process. Using Eq. (8) and Table 2, the weight of DMEs are obtained and presented in Table 4. For SIBO assessment, we obtain the LDM $Z^{(k)} = (\xi_{ij}^{(k)})_{m \times n}$ for each DME and are shown in Table 5. Using Eq. (6), Eq. (9) and Table 5, the A-IFDM for SIBOs assessment is computed according to the DMEs’ opinions given in Table 6.

Since the SDIs $U_1, U_2, U_3, U_9, U_{11}, U_{22}, U_{25}$ and U_{26} are cost-type and the rest of all are benefit-type. Hence, using Eq. (10), the NA-IFDM is obtained in Table 7.

In order to derive the objective weights of SDIs, the A-IFDM is normalized by using Eq. (10). Then, the overall performances of the SIBOs are computed by Eq. (11), therefore, we have $S_1 = 0.450, S_2 = 0.504,$ and $S_3 = 0.534.$ With the use of Eqs. (13)–(15), the remaining computational steps of MEREC are determined and given in Table 8.

Table 9 illustrates the LVs by DMEs for the criteria significances. Based on Definition 3.2, the score values of corresponding aggregated IFNs are computed in Table 9.

Using Eqs. (16)–(18) and Table 9, the subjective weight of SDIs is presented in Table 10 and derived as

$$w_j^s = (0.0359, 0.0385, 0.0298, 0.0355, 0.0283, 0.0447, 0.0409, 0.0395, 0.0357, 0.0433, 0.0318, 0.0410, 0.0391, 0.0420, 0.0374, 0.0376, 0.0297, 0.0389, 0.0371, 0.0417, 0.0352, 0.0360, 0.0325, 0.0369, 0.0330, 0.0412, 0.0368).$$

By combining the objective and subjective weights of SDIs, an integrated weight of SDIs ($\tau = 0.5$) are shown as below:

$$w_j = (0.0373, 0.0382, 0.0528, 0.0324, 0.0285, 0.0469, 0.0431, 0.0321, 0.0432, 0.0359, 0.0346, 0.0344, 0.0331, 0.0346, 0.0312, 0.0427, 0.0396, 0.0334, 0.0338, 0.0391, 0.0409, 0.0341, 0.0282, 0.0346, 0.0340, 0.0421, 0.0390).$$

The optimal performance rating (\mathbb{R}_0) of each SIBO is computed using Eq. (20). The obtained OPRs of SIBOs are represented in Table 11.

Based on Eq. (21) and using Table 7, the WNA-IFDM for SIBOs selection is formed and given in Table 12.

	M_1	M_2	M_3
U_1	(0.306, 0.594)	(0.368, 0.532)	(0.602, 0.298)
U_2	(0.389, 0.511)	(0.261, 0.639)	(0.594, 0.306)
U_3	(0.733, 0.185)	(0.755, 0.175)	(0.515, 0.385)
U_4	(0.532, 0.368)	(0.689, 0.231)	(0.459, 0.441)
U_5	(0.544, 0.356)	(0.635, 0.276)	(0.506, 0.394)
U_6	(0.272, 0.628)	(0.310, 0.590)	(0.661, 0.260)
U_7	(0.455, 0.445)	(0.251, 0.649)	(0.589, 0.322)
U_8	(0.741, 0.188)	(0.687, 0.236)	(0.433, 0.467)
U_9	(0.365, 0.535)	(0.677, 0.241)	(0.519, 0.381)
U_{10}	(0.583, 0.335)	(0.602, 0.309)	(0.510, 0.390)
U_{11}	(0.313, 0.587)	(0.378, 0.522)	(0.566, 0.334)
U_{12}	(0.719, 0.199)	(0.391, 0.514)	(0.656, 0.259)
U_{13}	(0.635, 0.275)	(0.632, 0.279)	(0.477, 0.423)
U_{14}	(0.532, 0.368)	(0.602, 0.309)	(0.592, 0.326)
U_{15}	(0.644, 0.277)	(0.632, 0.287)	(0.546, 0.368)
U_{16}	(0.308, 0.592)	(0.319, 0.581)	(0.607, 0.307)
U_{17}	(0.372, 0.528)	(0.269, 0.631)	(0.523, 0.377)
U_{18}	(0.722, 0.205)	(0.696, 0.231)	(0.362, 0.538)
U_{19}	(0.498, 0.402)	(0.661, 0.257)	(0.481, 0.419)
U_{20}	(0.580, 0.320)	(0.589, 0.322)	(0.318, 0.582)
U_{21}	(0.347, 0.553)	(0.298, 0.602)	(0.610, 0.290)
U_{22}	(0.340, 0.560)	(0.275, 0.625)	(0.500, 0.400)
U_{23}	(0.667, 0.252)	(0.715, 0.203)	(0.480, 0.420)
U_{24}	(0.532, 0.368)	(0.509, 0.391)	(0.522, 0.378)
U_{25}	(0.289, 0.611)	(0.464, 0.436)	(0.455, 0.445)
U_{26}	(0.287, 0.613)	(0.476, 0.424)	(0.620, 0.280)
U_{27}	(0.645, 0.273)	(0.471, 0.429)	(0.269, 0.631)

Table 6. The A-IFDM for SIBOs evaluation.

From Table 12 and Eq. (22), the score degrees $\mathbb{S}^*(\tilde{c}_{ij})$ of SIBOs are presented in Table 13. Corresponding to Eq. (23)-Eq. (24), the OPR (\mathbb{M}_i) and UD (\mathbb{Q}_i) of each SIBO is calculated and specified in Table 13. Then, from Eq. (25), the prioritization of the SIBOs is determined as $M_1 > M_2 > M_3$. Hence, the desirable alternative building is M_1 .

Comparative study. Comparison with existing studies is presented to certify the outcomes of introduced ARAS approach. In this respect, we have chosen the previously developed methods which are IF-COPRAS⁸¹ and IF-WASPAS³⁶.

IF-COPRAS model. Steps 1–4: Same as previous method.

Step 5: Sum of the degrees of criteria for benefit and cost-type.

In this step, each option is signified with its addition of maximizing criterion α_i , which is assigned to benefit-type, and minimizing criterion β_i , which is assigned to cost-type using

$$\alpha_i = \bigoplus_{j=1}^l w_j \bar{\xi}_{ij}, \quad i = 1(1)m. \tag{26}$$

$$\beta_i = \bigoplus_{j=l+1}^n w_j \bar{\xi}_{ij}, \quad i = 1(1)m. \tag{27}$$

Here, l is the number of benefit-type and n is the total number of criteria.

Step 6: Calculate the “relative degree (RD)” of each option.

The RD (γ_i) of i th option is obtained using

$$\gamma_i = \mathbb{S}^*(\alpha_i) + \frac{\min_i \mathbb{S}^*(\beta_i) \sum_{i=1}^m \mathbb{S}^*(\beta_i)}{\mathbb{S}^*(\beta_i) \sum_{i=1}^m \frac{\min_i \mathbb{S}^*(\beta_i)}{\mathbb{S}^*(\beta_i)}}. \tag{28}$$

Indicators	M_1	M_2	M_3
U_1	(0.594, 0.306)	(0.532, 0.368)	(0.298, 0.602)
U_2	(0.511, 0.389)	(0.639, 0.261)	(0.306, 0.594)
U_3	(0.185, 0.733)	(0.175, 0.755)	(0.385, 0.515)
U_4	(0.532, 0.368)	(0.689, 0.231)	(0.459, 0.441)
U_5	(0.544, 0.356)	(0.635, 0.276)	(0.506, 0.394)
U_6	(0.272, 0.628)	(0.310, 0.590)	(0.661, 0.260)
U_7	(0.455, 0.445)	(0.251, 0.649)	(0.589, 0.322)
U_8	(0.741, 0.188)	(0.687, 0.236)	(0.433, 0.467)
U_9	(0.535, 0.365)	(0.241, 0.677)	(0.381, 0.519)
U_{10}	(0.583, 0.335)	(0.602, 0.309)	(0.510, 0.390)
U_{11}	(0.587, 0.313)	(0.522, 0.378)	(0.334, 0.566)
U_{12}	(0.719, 0.199)	(0.391, 0.514)	(0.656, 0.259)
U_{13}	(0.635, 0.275)	(0.632, 0.279)	(0.477, 0.423)
U_{14}	(0.532, 0.368)	(0.602, 0.309)	(0.592, 0.326)
U_{15}	(0.644, 0.277)	(0.632, 0.287)	(0.546, 0.368)
U_{16}	(0.308, 0.592)	(0.319, 0.581)	(0.607, 0.307)
U_{17}	(0.372, 0.528)	(0.269, 0.631)	(0.523, 0.377)
U_{18}	(0.722, 0.205)	(0.696, 0.231)	(0.362, 0.538)
U_{19}	(0.498, 0.402)	(0.661, 0.257)	(0.481, 0.419)
U_{20}	(0.580, 0.320)	(0.589, 0.322)	(0.318, 0.582)
U_{21}	(0.347, 0.553)	(0.298, 0.602)	(0.610, 0.290)
U_{22}	(0.560, 0.340)	(0.625, 0.275)	(0.400, 0.500)
U_{23}	(0.667, 0.252)	(0.715, 0.203)	(0.480, 0.420)
U_{24}	(0.532, 0.368)	(0.509, 0.391)	(0.522, 0.378)
U_{25}	(0.611, 0.289)	(0.436, 0.464)	(0.445, 0.455)
U_{26}	(0.613, 0.287)	(0.424, 0.476)	(0.280, 0.620)
U_{27}	(0.645, 0.273)	(0.471, 0.429)	(0.269, 0.631)

Table 7. The NA-IFDM for SIBOs assessment.

Here, $\mathbb{S}^*(\alpha_i)$ and $\mathbb{S}^*(\beta_i)$ denote the score values of α_i and β_i , respectively.

Step 7: Define the “priority order (PO)” of the options.

Corresponding to the RD, the PO of the options is obtained. The maximum RD of option has been ranked as superior significance, and thus, it is the most appropriate option.

$$E^* = \max_i \gamma_i, \forall i. \tag{29}$$

Step 8: Compute the “utility degree (UD)” of each option.

By evaluating the examined options with the optimal one, the UD of each option is calculated based on Eq. (30).

$$\delta_i = \frac{\gamma_i}{\gamma_{\max}} \times 100\%, \quad i = 1(1)m. \tag{30}$$

Now, the results IF-COPRAS⁸¹ are described in Table 14. From Table 6 and Eqs. (26)–(30), α_i, β_i, RD and UD of each SIBO are evaluated. According to UD, M_1 has been found to be the best SIBO since it has the maximum RD (0.546).

IF-WASPAS model. Steps 1–4: Follow the developed model.

Step 5: Estimate the “weighted sum measure (WSM)” and the “weighted product measure (WPM)” using the following expressions:

$$\mathfrak{S}_i^{(1)} = \bigoplus_{j=1}^n w_j \varsigma_{ij}. \tag{31}$$

$$\mathfrak{S}_i^{(2)} = \bigotimes_{j=1}^n w_j \varsigma_{ij}, \quad i = 1, 2, \dots, m. \tag{32}$$

Step 6: Find the measure of “weighted aggregated sum product assessment (WASPAS)” using Eq. (33).

Indicators	(S'_{ij}) values			V_j	w_j^o
	M_1	M_2	M_3		
U_1	0.439	0.492	0.511	0.046	0.0388
U_2	0.436	0.496	0.511	0.045	0.0379
U_3	0.414	0.469	0.516	0.090	0.0757
U_4	0.437	0.497	0.519	0.035	0.0294
U_5	0.437	0.495	0.521	0.034	0.0287
U_6	0.422	0.481	0.526	0.058	0.0491
U_7	0.433	0.477	0.524	0.053	0.0452
U_8	0.444	0.497	0.518	0.029	0.0246
U_9	0.437	0.475	0.515	0.060	0.0507
U_{10}	0.438	0.494	0.521	0.034	0.0285
U_{11}	0.439	0.492	0.513	0.044	0.0374
U_{12}	0.443	0.485	0.526	0.033	0.0279
U_{13}	0.440	0.495	0.520	0.032	0.0270
U_{14}	0.439	0.495	0.522	0.032	0.0272
U_{15}	0.441	0.495	0.522	0.030	0.0250
U_{16}	0.425	0.482	0.525	0.056	0.0478
U_{17}	0.429	0.478	0.522	0.059	0.0496
U_{18}	0.443	0.497	0.514	0.033	0.0279
U_{19}	0.435	0.496	0.520	0.036	0.0305
U_{20}	0.439	0.494	0.512	0.043	0.0365
U_{21}	0.428	0.480	0.525	0.055	0.0465
U_{22}	0.438	0.495	0.516	0.038	0.0322
U_{23}	0.441	0.498	0.520	0.028	0.0240
U_{24}	0.437	0.491	0.522	0.038	0.0323
U_{25}	0.440	0.488	0.519	0.041	0.0351
U_{26}	0.440	0.487	0.510	0.051	0.0431
U_{27}	0.441	0.489	0.509	0.049	0.0412

Table 8. Objective weights for SDIs using IF-MEREC.

$$Q_i = \varepsilon \mathfrak{S}_i^{(1)} + (1 - \varepsilon) \mathfrak{S}_i^{(2)}, \quad i = 1, 2, \dots, m, \quad (33)$$

where $\tilde{h} \in [0, 1][0, 1]$ means strategic coefficient.

Step 7: Prioritize the options with the score value of Q_i .

Using Eqs. (31)–(33), the whole procedures of IF-WASPAS are computed and demonstrated in Table 15.

Therefore, the ranking of SIBOs is $M_1 > M_2 > M_3$ and according to UD, M_1 has been found to be the best SIBO among set of given three alternatives.

To validate the effectiveness of the developed methodology, we also compare it with the IF-TOPSIS⁸² in Table 16. The outcomes of the developed IF-MEREC-SWARA-ARAS framework with extant tools are given in Table 16 and Fig. 3. It can be observed from different parameter viewpoints that the proposed methodology is certainly a novel contribution as it combines all the key aspects of the MCDM procedure for treating the problems within uncertain settings.

The key benefits of the developed IF-MEREC-SWARA-ARAS methodology are discussed as follows:

- The developed IF-MEREC-SWARA-ARAS technique evades the defuzzification and employs the core operations of IFNs through the evaluation and ranking process.
- In IF-TOPSIS⁸², it is necessary to calculate the distances between each assessment of options by means of considered criteria and that of the ideal solution, which is time-consuming and decreases the accuracy of the results. While, the calculation process of the IF-MEREC-SWARA-ARAS method is simpler, and thus the accuracy and reliability of the results are higher.
- The proposed method utilizes the fairly aggregation operators for aggregating the individual decision information, which avoids the drawbacks of existing operators used by Boran et al.⁸², Gitinavard and Shirazi⁸¹, and Mishra et al.³⁶.
- In Boran et al.⁸² and proposed study, the weights of DMEs are obtained using score function based method ensuing in more accurate individual measure for determining the DMEs' weights unlike randomly preferred DMEs' weights in Mishra et al.³⁶.
- To handle the vagueness that appears in MCDM problems, all input variables, i.e., the predictions of options on criteria by several DMEs, DMEs' weights by the experts, and weights of the criteria by DMEs, are con-

Indicators	t_1	t_2	t_3	t_4	Aggregated IFNs	Score values
U_1	F	SU	SS	SU	(0.481, 0.417, 0.102)	0.532
U_2	SS	F	F	SS	(0.553, 0.346, 0.101)	0.603
U_3	VU	U	SU	U	(0.291, 0.608, 0.101)	0.342
U_4	F	F	F	U	(0.471, 0.428, 0.101)	0.522
U_5	VU	VU	VU	SU	(0.237, 0.662, 0.101)	0.288
U_6	VS	SS	S	S	(0.715, 0.205, 0.080)	0.755
U_7	S	F	F	S	(0.613, 0.283, 0.104)	0.665
U_8	SS	VS	VU	U	(0.586, 0.328, 0.086)	0.629
U_9	S	SU	SU	U	(0.472, 0.416, 0.112)	0.528
U_{10}	VS	S	F	F	(0.683, 0.236, 0.082)	0.723
U_{11}	F	U	VU	U	(0.357, 0.541, 0.102)	0.408
U_{12}	VS	SU	F	SS	(0.626, 0.293, 0.081)	0.666
U_{13}	S	SS	SU	U	(0.566, 0.327, 0.107)	0.619
U_{14}	VS	S	U	SU	(0.649, 0.266, 0.085)	0.691
U_{15}	SS	SS	SU	U	(0.522, 0.375, 0.103)	0.574
U_{16}	SS	SU	S	U	(0.524, 0.369, 0.107)	0.578
U_{17}	VU	U	U	SU	(0.287, 0.613, 0.101)	0.337
U_{18}	VS	SU	SU	U	(0.573, 0.345, 0.082)	0.614
U_{19}	S	F	U	VU	(0.511, 0.379, 0.110)	0.566
U_{20}	VS	SU	F	S	(0.643, 0.274, 0.083)	0.684
U_{21}	SS	F	U	VU	(0.462, 0.434, 0.104)	0.514
U_{22}	F	SS	SU	U	(0.485, 0.412, 0.102)	0.537
U_{23}	SU	F	VU	U	(0.380, 0.518, 0.102)	0.431
U_{24}	SS	F	F	U	(0.509, 0.389, 0.102)	0.560
U_{25}	SU	SU	F	VU	(0.394, 0.505, 0.101)	0.445
U_{26}	VU	F	SU	SU	(0.631, 0.288, 0.081)	0.672
U_{27}	SS	SU	U	S	(0.504, 0.388, 0.108)	0.558

Table 9. Score values of SDIs.

sidered as uncertain concerns and expressed in the form of IFNs. The HD is measured as significant way in the entire procedure and the desirable option is determined by means of evaluation values of all three inputs parameters.

To sum up, Table 17 suitably signifies the benefits of the developed model in comparison with Boran et al.⁸², Gitinavard and Shirazi⁸¹ and Mishra et al.³⁶ methods. Therefore, Table 17 shows that the developed model, in comparison with Boran et al.⁸², Gitinavard and Shirazi⁸¹ and Mishra et al.³⁶ tools, has the advantages comprising modeling of uncertainty, the weights of criteria, aggregation operators and DMEs' weights. In this way, the time complexity of the Gitinavard and Shirazi⁸¹ and Mishra et al.³⁶ approaches is lower than the proposed method and Boran et al.⁸² model. Whereas Boran et al.⁸² model has higher time complexity than the developed model and the four methods are suitable with the comparison parameter of support to MCDM. Accordingly, the proposed IF-MEREC-SWARA-ARAS method could be suitable based on its unique features.

Discussion and implications of this work. The proposed ARAS method is extremely dependent on the knowledge of DMEs and the way of their decisions. As an efficient and simple MCDM process, it can efficiently obtain the optimum options on IFSs setting. The results of this study conclude that the suggested framework is unique with its integration of the fairly aggregation operator, IF-MEREC-SWARA and ARAS models on IFSs setting. Its effectiveness and feasibility are illustrated in terms of implementation on a case study of SIBOs selection.

The combination of the MEREC and the SWARA is an effective and relatively latest procedure for the estimation of integrated weights in MCDM problems. It has lower evaluation complexity than some different tools namely AHP, BWM, and other weighting tools. The key advantage of the developed tool is its capability to treat the subjective assessment of DMEs and obtain quantitative significance values to define the RD of each indicator. Various scholars claim that the wide-range implementation of the SWARA tool can be recognized to its mobility and user-friendliness as well as the prospect of uniting with extant models. The ARAS is a comparatively efficient tool for obtaining the solutions in complex problems, specifically those that are related with a variety of assessment problems on under subjective estimations. It relates the UD for obtaining the OPRs of SIBO options (Zavadskas and Turskis, 2010).

Indicators	Score values	Relative significance of SDI values	Relative degree	Recalculated weight	Final weight
U_6	0.755	–	1.000	1.000	0.0447
U_{10}	0.723	0.032	1.032	0.969	0.0433
U_{14}	0.691	0.032	1.032	0.939	0.0420
U_{20}	0.684	0.007	1.007	0.932	0.0417
U_{26}	0.672	0.012	1.012	0.921	0.0412
U_{12}	0.666	0.006	1.006	0.916	0.0410
U_7	0.665	0.001	1.001	0.915	0.0409
U_8	0.629	0.036	1.036	0.883	0.0395
U_{13}	0.619	0.010	1.010	0.874	0.0391
U_{18}	0.614	0.005	1.005	0.870	0.0389
U_2	0.603	0.011	1.011	0.861	0.0385
U_{16}	0.578	0.025	1.025	0.840	0.0376
U_{15}	0.574	0.004	1.004	0.837	0.0374
U_{19}	0.566	0.008	1.008	0.830	0.0371
U_{24}	0.560	0.006	1.006	0.825	0.0369
U_{27}	0.558	0.002	1.002	0.823	0.0368
U_{22}	0.537	0.021	1.021	0.806	0.0360
U_1	0.532	0.005	1.005	0.802	0.0359
U_9	0.528	0.004	1.004	0.799	0.0357
U_4	0.522	0.006	1.006	0.794	0.0355
U_{21}	0.514	0.008	1.008	0.788	0.0352
U_{25}	0.445	0.069	1.069	0.737	0.0330
U_{23}	0.431	0.014	1.014	0.727	0.0325
U_{11}	0.408	0.023	1.023	0.711	0.0318
U_3	0.342	0.066	1.066	0.667	0.0298
U_{17}	0.337	0.005	1.005	0.664	0.0297
U_5	0.288	0.049	1.049	0.633	0.0283

Table 10. Subjective weights for SDIs using the SWARA method.

Criteria	U_1	U_2	U_3	U_4	U_5
\mathbb{R}_0	(0.306, 0.594)	(0.261, 0.639)	(0.515, 0.385)	(0.689, 0.231)	(0.635, 0.276)
U_6	U_7	U_8	U_9	U_{10}	U_{11}
(0.661, 0.260)	(0.589, 0.322)	(0.741, 0.188)	(0.365, 0.535)	(0.602, 0.309)	(0.313, 0.587)
U_{12}	U_{13}	U_{14}	U_{15}	U_{16}	U_{17}
(0.719, 0.199)	(0.635, 0.275)	(0.602, 0.309)	(0.644, 0.277)	(0.607, 0.307)	(0.523, 0.377)
U_{18}	U_{19}	U_{20}	U_{21}	U_{22}	U_{23}
(0.722, 0.205)	(0.661, 0.257)	(0.580, 0.320)	(0.610, 0.290)	(0.275, 0.625)	(0.715, 0.203)
U_{24}	U_{25}	U_{26}	U_{27}		
(0.532, 0.368)	(0.289, 0.611)	(0.287, 0.613)	(0.645, 0.273)		

Table 11. The OPR of sustainable industrial building options.

The outcomes of the study show that environmental (EN) and social aspects are the two most significant dimensions with RDs of 0.4925 and 0.2544, respectively. The economical aspect with relative weights of 0.2531 is the least significant one. The relative weights of different aspects are presented in Fig. 4.

As can be discussed in Fig. 5 and Table 8, based on the DMEs' evaluations, U_3 (Violation of animal's territory, 0.0528), U_6 (Recycled/reused materials, 0.0469) and U_9 (Noise pollution, 0.432) are the most important and U_{23} (Innovation and technological advance, 0.0282), U_5 (Workers and personnel's health and safety, 0.0285) and U_{15} (Public comfort, 0.0312) are the least important SDIs of overall sustainability aspect. In environmental aspects, we find that U_3 (Violation of animal's territory, 0.0528), U_6 (Recycled/reused materials, 0.0469) have more significance than the other SDIs. In the social (SC) aspect, we can say that U_{16} (Cultural heritage, 0.0427) and U_{17} (natural heritage, 0.0396) have more significance than the other SDIs. Also, we can observe the maximum weights of U_{26} (Cost of operation and maintenance, 0.0412) and U_{21} (Effects on national economic indicators, 0.0409) in the economic (EC), which shows the higher important that the other SDIs.

Indicators	\mathbb{R}_0	M_1	M_2	M_3
U_1	(0.033, 0.957)	(0.033, 0.957)	(0.028, 0.963)	(0.013, 0.981)
U_2	(0.038, 0.950)	(0.027, 0.965)	(0.038, 0.950)	(0.014, 0.980)
U_3	(0.025, 0.966)	(0.011, 0.984)	(0.010, 0.985)	(0.025, 0.966)
U_4	(0.037, 0.954)	(0.024, 0.968)	(0.037, 0.954)	(0.020, 0.974)
U_5	(0.028, 0.964)	(0.022, 0.971)	(0.028, 0.964)	(0.020, 0.974)
U_6	(0.049, 0.939)	(0.015, 0.978)	(0.017, 0.976)	(0.049, 0.939)
U_7	(0.038, 0.952)	(0.026, 0.966)	(0.012, 0.982)	(0.038, 0.952)
U_8	(0.042, 0.948)	(0.042, 0.948)	(0.037, 0.955)	(0.018, 0.976)
U_9	(0.033, 0.957)	(0.033, 0.957)	(0.012, 0.983)	(0.021, 0.972)
U_{10}	(0.033, 0.959)	(0.031, 0.961)	(0.033, 0.959)	(0.025, 0.967)
U_{11}	(0.030, 0.961)	(0.030, 0.961)	(0.025, 0.967)	(0.014, 0.980)
U_{12}	(0.043, 0.946)	(0.043, 0.946)	(0.017, 0.977)	(0.036, 0.955)
U_{13}	(0.033, 0.958)	(0.033, 0.958)	(0.032, 0.959)	(0.021, 0.972)
U_{14}	(0.031, 0.960)	(0.026, 0.966)	(0.031, 0.960)	(0.031, 0.962)
U_{15}	(0.032, 0.961)	(0.032, 0.961)	(0.031, 0.962)	(0.024, 0.969)
U_{16}	(0.039, 0.951)	(0.016, 0.978)	(0.016, 0.977)	(0.039, 0.951)
U_{17}	(0.029, 0.962)	(0.018, 0.975)	(0.012, 0.982)	(0.029, 0.962)
U_{18}	(0.042, 0.948)	(0.042, 0.948)	(0.039, 0.952)	(0.015, 0.980)
U_{19}	(0.036, 0.955)	(0.023, 0.970)	(0.036, 0.955)	(0.022, 0.971)
U_{20}	(0.033, 0.956)	(0.033, 0.956)	(0.034, 0.957)	(0.015, 0.979)
U_{21}	(0.038, 0.951)	(0.017, 0.976)	(0.014, 0.979)	(0.038, 0.951)
U_{22}	(0.033, 0.957)	(0.028, 0.964)	(0.033, 0.957)	(0.017, 0.977)
U_{23}	(0.035, 0.956)	(0.031, 0.962)	(0.035, 0.956)	(0.018, 0.976)
U_{24}	(0.026, 0.966)	(0.026, 0.966)	(0.024, 0.968)	(0.025, 0.967)
U_{25}	(0.032, 0.959)	(0.032, 0.959)	(0.019, 0.974)	(0.020, 0.974)
U_{26}	(0.039, 0.949)	(0.039, 0.949)	(0.023, 0.969)	(0.014, 0.980)
U_{27}	(0.040, 0.951)	(0.040, 0.951)	(0.025, 0.968)	(0.012, 0.982)

Table 12. The WNA-IFDM for SIBOs assessment.

Lastly, it should be revealed that if more projects even in small cities were planned as the case study, the outcomes, of course, might be reformed in comparison to projects placed in big cities, for instance, when it is planned to build a project in a small city, a project gains more social worth. The reason is that more social welfares would be brought to the public of a small city than a larger city in terms of job creation and infrastructure development. This indicates the assessment of such a project over others when more attention is waged to the social MCDM.

Sensitivity analysis. In this portion, we discuss the variation of weights of indicators from objective and subjective weights in the “IF-MEREC-SWARA method” for prioritizing SIBOs. In this line, the prioritizations of SIBOs have been obtained using the objective and subjective weights of indicators in lieu of IF-MEREC-SWARA model and are given in Table 18 and Fig. 6. From IF-MEREC, the UD and priority of options are given as follows: The UD of options are as $M_1 = 0.8056$, $M_2 = 0.7228$ and $M_3 = 0.6904$ and prioritization of SIBOs is given as $M_1 > M_2 > M_3$. Applying the IF-SWARA method, the UD and priority of options are discussed as follows: The UD of each option as $M_1 = 0.8374$, $M_2 = 0.7708$ and $M_3 = 0.6702$ and the ranks of SIBOs is given as $M_1 > M_2 > M_3$. From aforesaid investigation, it is concluded that the utilization of diverse values of strategic coefficient will enhance the permanence of the IF-MEREC-SWARA-ARAS method.

Conclusions

The aim of this study is to recommend a new MCDM tool for choosing the most suitable SIBO in uncertain environment. The primary contributions of this study are as follows:

A novel intuitionistic fuzzy weighted fairly AOs and their properties are discussed, which overcome the drawback of existing intuitionistic fuzzy AOs.

This paper further developed a methodology by integrating the fairly AO, the MEREC, the SWARA and the ARAS frameworks with IFs. In the proposed methodology, the fairly AO has been utilized to aggregate the decision information. Moreover, the IF-MEREC-SWARA model has been used to determine the objective and subjective weights of the criteria from intuitionistic fuzzy perspective, while integrated ARAS method has developed to prioritize the alternatives by means of multiple criteria and uncertainty.

A case study for SIBOs assessment has been presented to show the practicability of the present ARAS methodology. Comparative analysis has been discussed to confirm the robustness of the results acquired by proposed

Indicators	R_0	M_1	M_2	M_3
U_1	0.038	0.038	0.032	0.016
U_2	0.044	0.031	0.044	0.017
U_3	0.030	0.013	0.012	0.030
U_4	0.042	0.028	0.042	0.023
U_5	0.032	0.026	0.032	0.023
U_6	0.055	0.018	0.021	0.055
U_7	0.043	0.030	0.015	0.043
U_8	0.047	0.047	0.041	0.021
U_9	0.038	0.038	0.014	0.024
U_{10}	0.037	0.035	0.037	0.029
U_{11}	0.035	0.035	0.029	0.017
U_{12}	0.048	0.048	0.020	0.041
U_{13}	0.037	0.037	0.037	0.025
U_{14}	0.036	0.030	0.036	0.034
U_{15}	0.035	0.035	0.034	0.028
U_{16}	0.044	0.019	0.020	0.044
U_{17}	0.033	0.022	0.015	0.033
U_{18}	0.047	0.047	0.043	0.018
U_{19}	0.040	0.027	0.040	0.025
U_{20}	0.038	0.038	0.039	0.018
U_{21}	0.044	0.021	0.017	0.044
U_{22}	0.038	0.032	0.038	0.020
U_{23}	0.039	0.034	0.039	0.021
U_{24}	0.030	0.030	0.028	0.029
U_{25}	0.037	0.036	0.023	0.023
U_{26}	0.045	0.045	0.027	0.017
U_{27}	0.044	0.044	0.029	0.015
OMR	1.078	0.886	0.805	0.733
Degree of utility	1.000	0.8218	0.7472	0.6800

Table 13. The Score value, OPR and UD for SIBOs assessment.

SIBO	α_i	$S^*(\alpha_i)$	β_i	$S^*(\beta_i)$	γ_i	δ_i
M_1	(0.446, 0.492)	0.477	(0.160, 0.789)	0.186	0.546	100.00%
M_2	(0.415, 0.510)	0.452	(0.203, 0.743)	0.230	0.544	99.75%
M_3	(0.417, 0.519)	0.449	(0.223, 0.717)	0.253	0.522	95.73%

Table 14. The results of IF-COPRAS for SIBO assessment.

Options	$\wp_i^{(1)}$	$\wp_i^{(2)}$	$S(\wp_i^{(1)})$	$S(\wp_i^{(2)})$	$Q_i(\tilde{h})$	Ranks
M_1	(0.540, 0.360, 0.099)	(0.497, 0.404, 0.099)	0.590	0.547	0.5683	1
M_2	(0.505, 0.395, 0.099)	(0.447, 0.455, 0.098)	0.555	0.496	0.5255	2
M_3	(0.463, 0.428, 0.109)	(0.444, 0.456, 0.100)	0.517	0.494	0.5057	3

Table 15. The IF-WASPAS method for prioritizing SIBOs.

Aspects	Boran et al. ⁸² method	Gitinavard and Shirazi ⁸¹ method	Mishra et al. ³⁶ method	Introduced approach
Standards	IF-TOPSIS method	IF-COPRAS method	IF-WASPAS method based on similarity measures	IF-ARAS method based on IF-MEREC-SWARA method
Aggregation process	Arithmetic, geometric	Arithmetic, geometric	Arithmetic, geometric	Fairly aggregation operators
Criteria weights	Computed (IFWAO)	Computed (IFWAO)	Computed (proposed similarity measures)	Computed (IF-MEREC-SWARA method)
MCDM procedure	Group	Group	Group	Group
HD in evaluations	Included	Excluded	Excluded	Included
DME weights	Evaluated (Score function based method)	Evaluated (IFWGO)	Not Applicable	Evaluated (Score value-based procedure)
Normalization type	Linear	Not Applicable	Linear	Linear
Ranking order	$M_1 > M_2 > M_3$	$M_1 > M_2 > M_3$	$M_1 > M_2 > M_3$	$M_1 > M_2 > M_3$
Optimal SIBOs option	M_1	M_1	M_1	M_1

Table 16. Parameters to compare the diverse approaches.

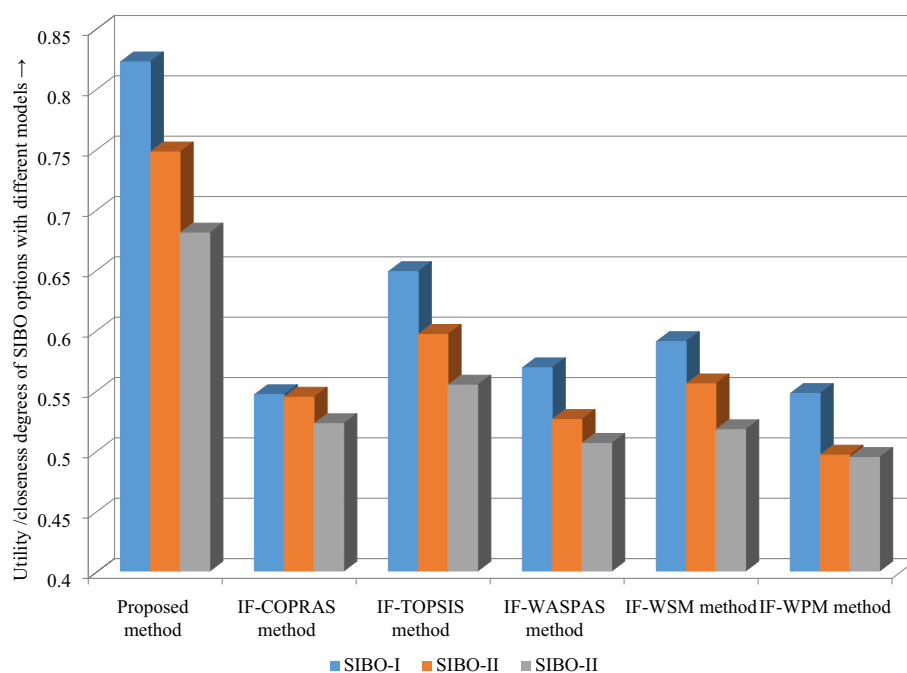


Figure 3. Assessment degree of options for prioritizing SIBO with different methods.

hybrid model. The main benefits of the presented framework are the ease of computation in intuitionistic fuzzy background and utilizing a model for deriving more reasonable weights of SDIs.

However, the proposed study needs to consider the technological and risk aspects of sustainability during the assessment of SIBOs. In addition, there is a need to consider the relation between SDIs, which is missing in the present work. More DMEs should be included in the assessment of SIBOs. In future, the developed methodology can be extended to different uncertain environments such as “q-rung orthopair fuzzy soft rough sets

Comparative parameters	The comparison outcomes
Modeling uncertainty	Due to the consideration of intuitionistic fuzzy information, the four models are suitable to tackle with uncertain settings in SIBO selection problems. Though, the developed model is taken IFs which could suitably intricate the imprecision and subjectivity in MCDM problems describing membership degree, non-membership degree and indeterminacy degree of an element under a set to lessening errors
Weights of SDIs/criteria	The developed model is computed the integrated weights of SDIs combining the objective and subjective weights based on IF-MEREC and IF-SWARA tools. Thus, the developed model could lead to a precise solution. In contrast, in IF-WASPAS, the criteria weight is obtained with similarity measure-based tool, in IF-TOPSIS, the criteria weight is obtained using IFWA operators and in IF-COPRAS, the criteria weight is chosen randomly, which did not consider a procedure for finding the weights of criteria
Aggregation operator	The developed model proposes fairly AOs to combine to avoid data loss. In some cases, when there are many DMEs employed to judge the candidates, first aggregation could lead to data loss. The Boran et al. ⁸² , Gitinavard and Shirazi ⁸¹ and Mishra et al. ³⁶ methods do not consider this concept, therefore, the obtained results from the proposed approach of this study are more reliable
Experts' weights	The developed model and Boran et al. ⁸² model compute the DMEs' weights based on the IF-score value-based tool to decrease errors. Therefore, the developed models could lead to a better solution. The methods given by Gitinavard and Shirazi ⁸¹ and Mishra et al. ³⁶ does not consider this concept
Time complexity	Time complexity is associated to the computational size of model. The methods given by Gitinavard and Shirazi ⁸¹ and Mishra et al. ³⁶ have less time complexity than developed model, because estimating the weights of criteria, DMEs' weights, and considering the AOs in the procedure of the developed IF-MEREC-SWARA-ARAS tool increase the size of essential computations

Table 17. Summarized comparative assessment of the developed model with extant tools.

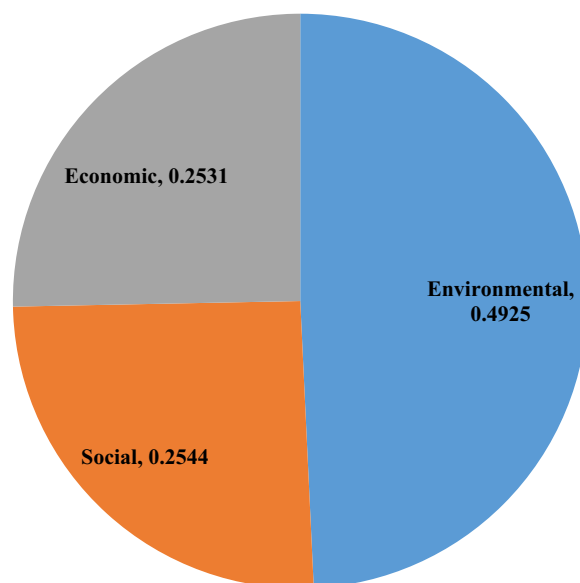


Figure 4. Relative weights of dimension of SDIs for SIBO selection.

(q-ROFSRSs)”, “interval-valued Fermatean fuzzy sets”, “interval-valued hesitant Fermatean fuzzy sets (IVHFFSs)” etc. Moreover, the developed method can also be utilized in treating with diverse MCDM concerns, namely IoT smart city development, low-carbon supplier selection and project selection, and others.

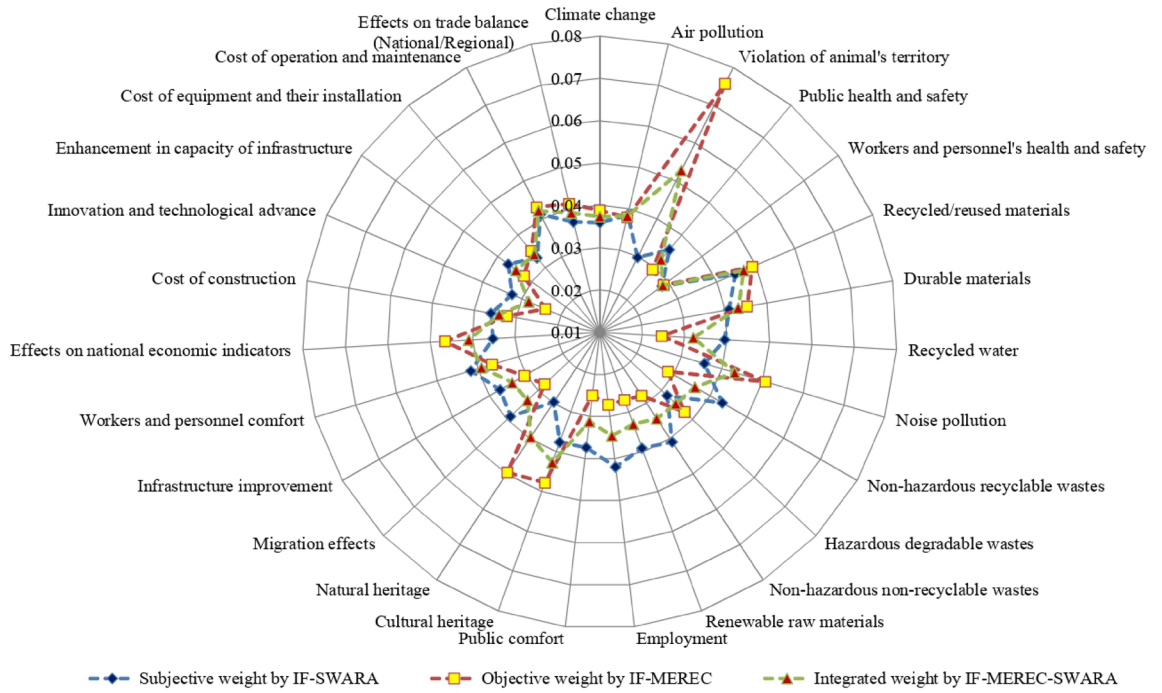


Figure 5. Preference order of SDIs using IF-MEREC-SWARA method.

Weighting model	UDs for SIBOs assessment			Ranks
	M_1	M_2	M_3	
Objective weight by IF-MEREC	0.8056	0.7228	0.6904	$M_1 > M_2 > M_3$
Subjective weight by IF-SWARA	0.8374	0.7708	0.6702	$M_1 > M_2 > M_3$
Integrated method by IF-MEREC-SWARA	0.8218	0.7472	0.6800	$M_1 > M_2 > M_3$

Table 18. The UD for prioritizing SIBOs over different weighting procedures.

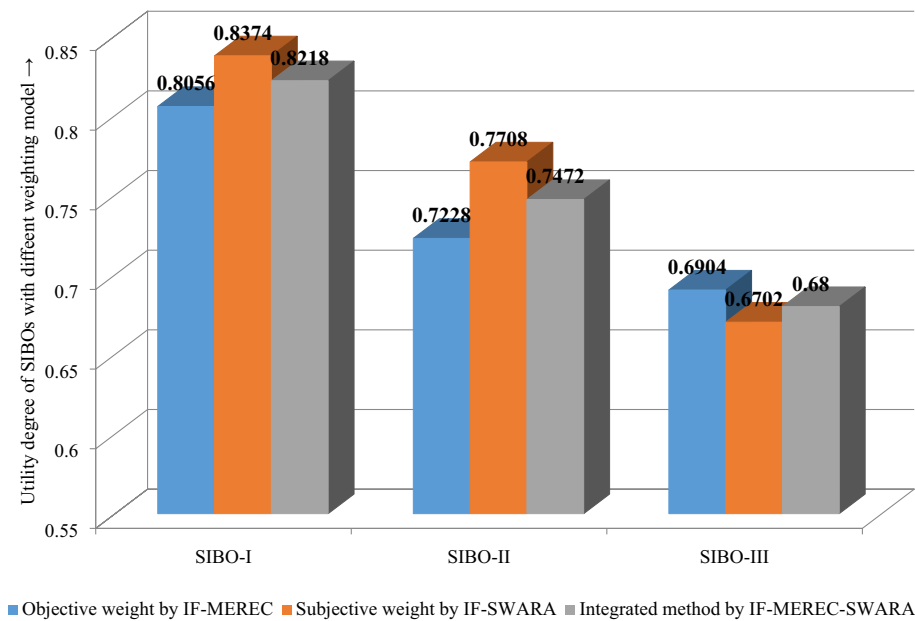


Figure 6. Sensitivity analysis for prioritizing SIBOs with different weighting procedures.

Data availability

All data generated or analyzed during this study are included in this published article.

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A.R.M. : Conceptualization and Writing - Original Draft; P.R. : Formal Analysis and Review & Editing; F.C. : Supervision and Project administration and I.M.H. : Supervision and Validation. All authors reviewed and approved the manuscript.

Competing interests

The authors declare no competing interests.

Additional information

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