#### **ORIGINAL ARTICLE**



# **Study on the Infuence of Magnetic Circuit Saturation on Suspension Performance of Bearingless Permanent Magnet Synchronous Motor**

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#### **Abstract**

Bearingless permanent magnet synchronous motors can rely on the radial electromagnetic force generated by magnetic feld coupling to achieve active suspension. However, the coupling between magnetic felds may lead to the saturation of the magnetic circuit, which afects the stability of motor suspension force and is one of the key problems to be solved for bearingless motors. In order to investigate the efect of magnetic circuit saturation on the suspension performance, frstly, the equation of the radial suspension force is derived by combining the infuence of the magnetic circuit saturation on the parameters of the motor. The relationship of the magnetic circuit saturation on the stable and fuctuating components of the radial suspension force is obtained, and the fuctuation mechanism of the suspension force under the saturation state is revealed. Secondly, the radial suspension force in diferent saturation states of the magnetic circuit is calculated by fnite element calculation method. Combining the efect of magnetic fux density on the magnetic permeability, the variation of the magnitude and fuctuating of the suspension force with the magnetic feld in diferent magnetic circuit saturation states is given. Finally, the accuracy of the analytical and fnite element calculations is demonstrated experimentally.

**Keywords** Bearingless permanent magnet synchronous motor · Magnetic feld distribution · Magnetic circuit saturation · Suspension force stability

# **1 Introduction**

The bearingless permanent magnet synchronous motor integrates the functions of conventional permanent magnet synchronous motor and magnetic bearing, which not only has the advantages of frictionless magnetic bearing, no lubrication and long life, but also achieves high integration and system simplifcation [\[1](#page-8-0)[–3](#page-8-1)].Therefore, bearingless permanent magnet synchronous motors have potential applications in some special felds, such as high-speed precision electric spindles, fywheel energy storage, blood pumps and centrifugal pumps [\[4](#page-8-2)[–8](#page-8-3)].

For the problem of magnetic circuit saturation, many scholars have conducted a series of studies and verifcations.

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Literature [[9\]](#page-8-4) proposed a load feld prediction model of double-winding permanent magnet synchronous motor based on subdomain model and combined with the equivalent magnetic circuit method to compensate the magnetic saturation of the iron core, which efectively improved the compensation accuracy and made the motor control model more accurate. Based on the basis formula of torque and suspension and combined with gap permeability theory. Literature [\[10](#page-8-5)] analyzed the efect of magnetic saturation on edge fux. The radial force and torque from linear region to saturated region are calculated efectively, which provides theoretical support for the stable operation of bearingless switched reluctance motor under full torque load. Literature [[11\]](#page-8-6) proposed a mathematical model considering magnetic saturation and carried out a regional analysis according to the electromagnetic saturation effect. Based on the influence of diferent parameters on the motor performance, the motor control strategy is improved, which has certain reference value for the optimization design and control performance. In order to characterize the phenomenon of local magnetic saturation in the process of rotor rotation. Literature  $[12]$  $[12]$  $[12]$  introduced a modified coefficient of rotor

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yoke permeability, which greatly shortened the calculation time of finite element analysis and greatly improved the efficiency of machine design. Literature [\[13\]](#page-8-8) proposed an analytical model of torque considering magnetic saturation and completed the nonlinear torque model through B-H loop. According to fnite element calculation, the efectiveness of the proposed modelling method was verifed. Literature [\[14\]](#page-8-9) uses a combination of the response surface model and a multi-objective optimization algorithm to optimize the suspension stability and torque. The optimization process considers not only geometric parameters but also winding distribution. Literature [[15](#page-8-10)] linearizes the mathematical model of BPMSM to achieve optimal control, considering coupling and nonlinearity issues.

Existing analytical methods for bearingless motors mainly focus on the optimization of control algorithms. In this paper, the infuence of magnetic circuit saturation on bearingless motor performance is studied from the aspect of electromagnetic calculation and analysis, on the basis of magnetic circuit coupling analysis, the nonlinear variation law of radial suspension force under diferent magnetic circuit saturation is determined by establishing the radial suspension force nonlinear mathematical model, and the infuence mechanism of magnetic circuit saturation on the stable component and fuctuation component of radial suspension force is revealed.

Firstly, the working mechanism of the bearingless permanent magnet synchronous motor is analyzed, and based on the magnetic circuit method, the efect of magnetic circuit saturation on the motor parameters is revealed. Secondly, based on the traditional suspension force formula, the suspension force analytical model considering the magnetic circuit saturation is derived, the variation of suspension force under diferent saturation conditions of magnetic circuit is determine, and the principle of suspension force fuctuation under saturation condition is revealed. In addition, the radial suspension force under diferent magnetic circuit saturation states is calculated by fnite element method, and the results consistent between the analytical analyses and the fnite element calculations are determined. Finally, the accuracy of the analytical and fnite element calculations is demonstrated by experiments.

## **2 Working Mechanism and Magnetic Circuits of Bearingless Permanent Magnet Synchronous Motor**

The stator of bearingless permanent magnet synchronous motors is embedded with suspension winding and torque winding with diferent pole pairs. The coupling of the magnetic felds of suspension and torque changes the symmetric distribution of magnetic feld, so that the motor can provide



<span id="page-1-0"></span>**Fig. 1** Working principle of bearingless permanent magnet synchronous motor



<span id="page-1-1"></span>**Fig. 2** The magnetic circuit of a permanent magnet synchronous motor

torque and generate the suspension force to support the rotor suspension. Figure [1](#page-1-0) shows the working principle of the bearingless permanent magnet synchronous motor.

The Fig. [1](#page-1-0) gives the distribution of the 4-pole fux linkage Ψ1 generated by the torque magnetic feld and the 2-pole fux linkage Ψ2 generated by the suspension magnetic feld. In the motor, the fux linkage Ψ1 and Ψ2 are enhanced in the same direction and weakened in the opposite direction, which cause the asymmetric distribution of magnetic feld. According to maxwell force generation principle, a radial electromagnetic force along the direction of magnetic feld enhancement will be generated. By controlling the magnitude and phase of the current fowing into the suspension winding, the magnitude and direction of suspension force can be regulated, which achieve the stable suspension of rotor. Due to the asymmetric distribution of magnetic feld, the part of magnetic fux density enhancement is easy satura-tion, which affects the suspension force stability. Figures [2](#page-1-1) and [3](#page-2-0) shows the magnetic circuit of the permanent magnet motor.



<span id="page-2-0"></span>**Fig. 3** Equivalent circuit of permanent magnet synchronous motor

 $R_{\rm e1}$  and  $R_{\rm e2}$  are air gap reluctance;  $F_{\rm sd1}$  and  $F_{\rm sd2}$  are armature magnetic motive force;  $R_{sl1}$  and  $R_{sl2}$  are stator side leakage reluctance;  $R_{\rm st1}$  and  $R_{\rm st2}$  are stator tooth reluctance;  $R_{\rm si}$  is stator yoke reluctance;  $R_{\text{rj}}$  is rotor yoke reluctance;  $R_{\text{pm1}}$  and  $R_{\text{pm2}}$  are permanent magnet reluctance;  $F_{pm1}$  and  $F_{pm2}$  are permanent magnet magnetic motive force;  $R_{r11}$  and  $R_{r12}$  are rotor side leakage reluctances.

$$
\varphi = \frac{2\left(\frac{R_{sI1}}{R_{sI1} + R_{sI1}} F_{sd1} + \frac{R_{rI1}}{R_{pm1} + R_{rI1}} F_{pm1}\right)}{2R_{sI1} + \frac{R_{sj}}{2} + \frac{R_{rI}}{2} + 2R_{e1} + \frac{2R_{pm1}R_{rI1}}{R_{pm1} + R_{rI1}}}
$$
(1)

The magnitude of the reluctance is afected by the saturation degree of the magnetic circuit. The formula ([1](#page-2-1)) shows that under the condition of magnetic circuit unsaturation, the main magnetic fux is proportional to the armature magnetic motive force and permanent magnet magnetic motive force. When the magnetic circuit is saturated, the stator yoke reluctance  $R_{si}$ increases gradually with the saturation degree of the magnetic circuit, and the main magnetic fux changes nonlinearly with the armature magnetic motive force and permanent magnet magnetic motive force.



<span id="page-2-2"></span>**Fig. 4** Magnetic density region distribution

# **3 The Calculation of Suspension Force Considering The Magnetic Circuit Saturation**

<span id="page-2-1"></span>In the air gap, the magnetic feld is approximately perpendicular to the rotor surface, the tangential magnetic feld intensity is approximately 0. The torque magnetic motive force consisted of the magnetic motive force and the permanent magnet magnetic motive force is  $f_1(\theta, t)$ , and the magnetic motive force of the suspension winding is  $f_2(\theta, t)$ . According to the maxwell tensor method, the formula of radial suspension force is as follows.

$$
f_1(\theta, t) = F_{1m} \cos(P_1 \theta - w_1 t + \varphi_1)
$$
  
\n
$$
f_2(\theta, t) = F_{2m} \cos(P_2 \theta - w_2 t + \varphi_2)
$$
  
\n
$$
b_1(\theta, t) = f_1(\theta, t)(\Lambda_0 + \Lambda_1 \cos Z_1 \theta)
$$
  
\n
$$
\approx f_1(\theta, t)\Lambda_0 = F_{1m}\Lambda_0 \cos(P_1 \theta - w_1 t + \varphi_1)
$$
  
\n
$$
b_2(\theta, t) = f_2(\theta, t)(\Lambda_0 + \Lambda_1 \cos Z_1 \theta)
$$
  
\n
$$
\approx f_2(\theta, t)\Lambda_0 = F_{2m}\Lambda_0 \cos(P_2 \theta - w_2 t + \varphi_2)
$$
  
\n(2)

$$
F(\theta, t) = \frac{\mu_{Fe} - \mu_0}{2\mu_{Fe}\mu_0} (B_n^2 + \mu_{Fe}\mu_0 B_t^2) dS \approx \frac{B(\theta, t)^2}{2\mu_0} = \frac{\left[b_1(\theta, t) + b_2(\theta, t)\right]^2}{2\mu_0}
$$
  
= 
$$
\frac{\left[F_{1m}\Lambda_0 \cos(P_1\theta - w_1t + \varphi_1) + F_{2m}\Lambda_0 \cos(P_2\theta - w_2t + \varphi_2)\right]^2}{2\mu_0}
$$
(3)

$$
(\mathbf{3})
$$

where  $\mu_0$  is the vacuum permeability, *S* is the unit surface area of the rotor surface,  $\theta$  is the space position angle,  $P_1$  is the pole pairs number of the torque magnetomotive force,  $P<sub>2</sub>$  is the pole pairs number of the suspension magnetomotive force,  $b_1$  is the torque winding magnetic density,  $b_2$  is the suspension winding magnetic density,  $w_1$  is the angular frequency of torque winding current,  $w_1$  is the angular suspension force, the stator magnetic circuit is divided into three regions (the magnetic fux density enhancement region, the magnetic fux density weakening region and the magnetic fux density symmetry region) in Fig. [4,](#page-2-2) which are distributed along the circumference in the range of  $0 \sim n$ ,  $n \sim \pi, \pi \sim \pi + n$ ,  $\pi + n \sim 2\pi$ . The electromagnetic forces of each region are calculated and summed to obtain the radial suspension force.

$$
F_{1x} = \int_{0}^{n} \frac{\left[b_{1}(\theta, t) + b_{2}(\theta, t)\right]^{2} l r \cos \theta}{2\mu_{0}} d\theta + \int_{\pi}^{n+\pi} \frac{\left[b_{1}(\theta, t) + b_{2}(\theta, t)\right]^{2} l r \cos \theta}{2\mu_{0}} d\theta
$$
  
\n
$$
= \int_{0}^{n} \frac{\left[F_{1m} \Lambda \cos(P_{1}\theta - w_{1}t + \varphi_{1}) + F_{2m} \Lambda \cos(P_{2}\theta - w_{2}t + \varphi_{2})\right]^{2} l r \cos \theta}{2\mu_{0}} d\theta
$$
  
\n
$$
+ \int_{\pi}^{n+\pi} \frac{\left[F_{1m} \Lambda \cos(P_{1}\theta - w_{1}t + \varphi_{1}) + F_{2m} \Lambda \cos(P_{2}\theta - w_{2}t + \varphi_{2})\right]^{2} l r \cos \theta}{2\mu_{0}} d\theta
$$
  
\n(4)

$$
F_{2x} = \int_{n}^{\pi} \frac{\left[b_{1}(\theta, t) + b_{2}(\theta, t)\right]^{2} l r \cos \theta}{2\mu_{0}} d\theta + \int_{n+\pi}^{2\pi} \frac{\left[b_{1}(\theta, t) + b_{2}(\theta, t)\right]^{2} l r \cos \theta}{2\mu_{0}} d\theta
$$
  
\n
$$
= \int_{n}^{\pi} \frac{\left[F_{1m} \Lambda \cos(P_{1}\theta - w_{1}t + \varphi_{1}) + F_{2m} \Lambda \cos(P_{2}\theta - w_{2}t + \varphi_{2})\right]^{2} l r \cos \theta}{2\mu_{0}} d\theta
$$
  
\n
$$
+ \int_{n+\pi}^{2\pi} \frac{\left[F_{1m} \Lambda \cos(P_{1}\theta - w_{1}t + \varphi_{1}) + F_{2m} \Lambda \cos(P_{2}\theta - w_{2}t + \varphi_{2})\right]^{2} l r \cos \theta}{2\mu_{0}} d\theta
$$
  
\n
$$
= 0
$$
 (5)

$$
F = F_{1x} + F_{2x}
$$
  
\n
$$
= \frac{lr(\Lambda_1^2 + \Lambda_2^2)F_{1m}F_{2m}}{2} \Big[ n \cos(\varphi_1 - \varphi_2) + \frac{1}{2} \sin(2n - \varphi_1 + \varphi_2) + \frac{1}{2} \sin(\varphi_1 - \varphi_2) \Big]
$$
  
\n
$$
+ \frac{lr(\Lambda_1^2 - \Lambda_2^2)F_{1m}F_{2m}}{2(P_1 + P_2 \pm 1)} \Big[ \sin \Big[ (P_1 + P_2 \pm 1)n - 2w_1t - (\varphi_1 + \varphi_2) \Big] + \sin(2w_1t + \varphi_1 + \varphi_2) \Big]
$$
  
\n
$$
+ \frac{lr(\Lambda_1^2 - \Lambda_2^2)F_{1m}^2}{42P_2 \pm 1} \sin \Big[ (2P_1 - 1)n - 2w_1t - 2\varphi_1 \Big]
$$
  
\n
$$
+ \frac{lr(\Lambda_1^2 - \Lambda_2^2)F_{2m}^2}{42P_2 \pm 1} \sin \Big[ (2P_2 - 1)n - 2w_2t - 2\varphi_2 \Big]
$$
  
\n(6)

frequency of suspension winding current,  $\varphi$  is the initial phase angle,  $A_0$  is the invariant part of the air gap permeability,  $\Lambda_1$  is the teeth harmonic magnetic permeability.

From the above equations, the magnitude of the radial suspension force is related to the magnetic motive force and magnetic permeability. Infuenced by the properties of ferromagnetic materials, when the magnetic circuit is saturated, the permeability decreases nonlinearly with the increase of magnetic density. The coupling of the 4-pole magnetic feld and the 2-pole magnetic feld increases the possibility of magnetic circuit saturation. In order to accurately calculate the radial

*L* is the motor axial direction, *r* is the rotor outer diameter,  $\Lambda_1$  is the average magnetic permeability of the magnetic density enhancement region,  $\Lambda_2$  is the average magnetic permeability of the magnetic density weakening region,  $\theta$  is the space position angle. From the above analytical formula, it can be seen that the suspension force is consisted of the stable component ① and the fuctuating components ②, ③ and ④ The magnitude of suspension force is related to the magnetic motive force and the magnetic permeability. In the situation of magnetic circuit unsaturation, the magnetic permeability of the enhancement region and the weakening region are

#### <span id="page-4-0"></span>**Table 1** Parameters of the prototype



approximately the same  $(\Lambda_1 \approx \Lambda_2)$ . The magnitude of the stable component of suspension force is proportional to the magnetic motive force, and the magnitude of the fuctuating component of suspension force is approximately 0. When the magnetic circuit of the enhancement region is saturated, the magnetic permeability will change, which is not the same as that in the weakening region ( $\Lambda_1 \approx \Lambda_2$ ). The variation of magnetic permeability will further cause the change of suspension performance.

The increase of the torque magnetic motive force or the suspension magnetic motive force will cause the saturation of the magnetic circuit, and the magnetic permeability of the saturation region will decrease nonlinearly with the increase of the magnetic motive force. In the case of saturation, the magnetic motive force  $F_{1m}$  (or  $F_{2m}$ ) increases, the magnetic permeability  $\Lambda_1^2 + \Lambda_2^2$  decreases. When the increase of the magnetic motive force is greater than the decrease of the magnetic permeability, the stable component of the suspension force will increase nonlinearly with the increase of the magnetic motive force. When the increase of magnetic motive force is smaller than the decrease of magnetic permeability, the stable component of the suspension force will decrease nonlinearly with the increase of magnetic motive force. When the magnetic circuit is saturated, the magnetic permeability  $\Lambda_1^2 - \Lambda_2^2$  will increase with the increase of magnetic motive force. The fuctuation component of the suspension force will increase nonlinearly with the increase of the magnetic motive force, which cause the fuctuation of suspension force. So, the magnetic circuit saturation will afect the stability of the suspension force, and the stability of the suspension force becomes worse with the increase of saturation degree.



<span id="page-4-1"></span>**Fig. 5** The bearingless permanent magnet synchronous motor winding arrangement



<span id="page-4-2"></span>**Fig. 6** The magnetic density distribution with the increase of suspension magnetic



<span id="page-4-3"></span>**Fig. 7** The magnetic density distribution with the increase of torque magnetic feld

# **4 Efect of Magnetic Circuit Saturation on Suspension Force**

# **4.1 Analysis of Magnetic Field Distribution Characteristics under Diferent Saturation Conditions of The Magnetic Circuit**

To further clarify the efect of magnetic circuit saturation on the suspension performance, the mathematical model is established based on the fnite element method. The parameters are shown in Table [1.](#page-4-0) The arrangement of the torque and suspension windings is given in Fig. [5](#page-4-1). A1, B1 and C1 are the suspension windings and A2, B2 and C2 are the torque windings.

The saturation of the magnetic circuit is closely related to the torque magnetic feld and the suspension magnetic. In order to clarify the efect of the magnitude of the torque magnetic feld and the suspension magnetic feld on the magnetic circuit saturation. The magnetic feld distribution under diferent conditions of magnetic circuit saturation is calculated. The variation of the magnetic density distribution with the increase of suspension magnetic feld and the torque magnetic feld are shown in Figs. [6](#page-4-2) and [7](#page-4-3).

The variation of the magnetic density distribution with the increase of suspension magnetic feld is shown in Fig. [6.](#page-4-2) As the suspension winding current increases from 1 to 5A, the magnetic density of the enhancement region increases from 1.7 T to 2.0 T, and the magnetic density of the weakening region decreases from 1.7 T to 0.6 T. The variation of the magnetic density distribution with the increase of torque magnetic feld is shown in Fig. [7](#page-4-3). When the torque magnetic feld increases, the magnetic density increases in both regions.

The above analysis shows that the variation characteristic of magnetic density distribution with the increase of coupled magnetic feld is diferent. As the torque feld increases, the two regions will be saturated. While with the suspension feld increase, only the magnetic density enhancement region will be saturated.

## **4.2 Analysis of Suspension Performance at Diferent Saturation States**

The magnetic circuit saturation will affect the suspension performance of the motor. In order to explore the change of suspension force under diferent saturation states, the magnitude and fuctuation of suspension force is calculated in the case of magnetic circuit saturation caused by torque magnetic feld and suspension magnetic feld separately. Figure [8](#page-5-0) gives the variation of the magnitude and fluctuation of the suspension force with the increase of suspension magnetic feld.

The magnitude of the suspension magnetic field increases gradually with the increase of suspension winding current. It can be seen from Fig. [8](#page-5-0) that when the suspension winding current is less than 3A, the magnitude of the suspension force is proportional to the magnitude of the suspension magnetic feld. The suspension force magnitude increases by 107N when the suspension winding current changes from 1 to 3A. When the suspension winding current is larger than 3A, the magnitude of the suspension force increases nonlinearly with the increase of suspension magnetic feld. The suspension force increases by only 50N when the suspension winding current changes from 6 to 8A.

When the suspension current is less than 3A, the fuctuation of suspension force accounts for 4.38% of the suspension force. The fluctuation of suspension force gradually increases when the suspension winding current is larger than 3A. When the suspension winding current



<span id="page-5-0"></span>**Fig. 8** Variation of the magnitude and fuctuation of the suspension force with the suspension magnetic feld



<span id="page-5-1"></span>**Fig. 9** Variation of the magnitude and fuctuation of the suspension force with the torque magnetic feld

is 11A, the fuctuation of suspension force accounts for 20.17% of the suspension force, which is 5 times that the suspension winding current being 3A.

The Fig. [9](#page-5-1) gives the variation of the magnitude and fuctuation of the suspension force with the increase of torque magnetic feld. When the increase of the torque magnetic feld is less than 15%, the magnitude of the suspension force will increase linearly with the increase of torque magnetic field. The magnitude of suspension force increases by 106N when the torque magnetic feld increases by 15%. When the torque magnetic feld increases more than 15%, the suspension force first increases and then decreases. When the torque magnetic feld is increased by 35%, the magnitude of the suspension is the largest, which is 275 N.

The fuctuation of suspension force accounts for 3.66% of the suspension force when the increase of the torque magnetic feld is less than 15%. After the increase of torque magnetic feld exceeding 15%, the fuctuation of suspension force sharply increases with the increase of torque magnetic feld. The fuctuation of the suspension force accounts for 36.21% of the suspension force when the torque magnetic feld increases by 70%, which is 9 times higher than the torque magnetic feld increasing by 15%.

#### **4.3 The Relationship Analysis of The Magnitude and Phase of Suspension Force**

Because the rotor of bearingless motor may have radial displacement during operation, the direction of suspension force needs to be constantly adjusted to make the motor work stably. The saturation of the magnetic circuit will



<span id="page-6-0"></span>**Fig. 10** The suspension force under diferent suspension magnetic feld phases



<span id="page-6-1"></span>**Fig. 11** The measurement diagram of suspension force

afect magnitude of the suspension force when the suspension magnetic feld phase is adjusted. In order to study the infuence of magnetic circuit saturation on the relationship between the magnetic feld phase and the suspension force magnitude, the magnitude of suspension force under diferent magnetic feld phases is calculated.

As can be seen from Fig. [10](#page-6-0), the magnitude of the suspension force is the same at diferent suspension magnetic feld phases when magnetic circuit is unsaturated, and the variation of the suspension force magnitude is 0.2N at most. However, when magnetic circuit is saturated, the magnitude of the suspension force is diferent at diferent suspension magnetic feld phases, and the variation of the suspension force magnitude is 7N at most. Therefore, in the process of magnetic feld regulation, it is necessary to consider the infuence of magnetic circuit saturation on the suspension force.

#### **5 Experimental Verifcation**

In order to further verify the efective and accuracy of the theoretical analysis and numerical calculation, an experimental prototype is made and tested. As shown in Fig. [11,](#page-6-1) the suspension force testing mechanism is placed at the end covers. The pressure sensors for measuring the radial suspension force are placed between the bearing chamber



(a) The prototype test platform



(b) Suspension force test

<span id="page-7-0"></span>**Fig. 12** Experimental prototype of BPMSM



<span id="page-7-1"></span>**Fig. 13** The results comparison of experimental, fnite element calculation and analytical calculation

and bearing, and eight pressure sensors are placed around the circumference of the bearing chamber to ensure the accuracy of the suspension force testing.

The prototype is placed on the test bench shown in Fig.  $12(a)$  $12(a)$ . The experimental equipment mainly includes transformer, bearingless permanent magnet synchronous motor, power analyzer, voltage signal acquisition circuit, etc. Figure  $12(b)$  $12(b)$  shows the suspension force test. When the prototype is operated, the pressure signal is collected through the sensors at the end caps of the motor and the signal acquisition circuit. The collected signals are displayed by the oscilloscope.

1) Static suspension test: In order to verify the infuence of the magnetic motive force of the suspension winding on the suspension performance, the static test method is used to test the values of each sensor when the current of the suspension winding are diferent, and the magnitude of the suspension force is obtained by the vector synthesis. The experimental results, fnite element calculation results and analytical calculation results are given in Fig. [13,](#page-7-1) respectively.

It can be seen from the Fig. [13](#page-7-1) that the value of the suspension force texted by experiment increases with the increase of the suspension winding current, which is consistent with the results of the fnite element calculation and the analytical calculation, and the maximum error is 3.62N(9%) and 3.5N(10%), respectively.

2) Dynamic suspension test: In order to investigate the infuence of winding frequency on suspension performance, the values of each sensor under diferent winding frequencies are tested. The experimental values of the suspension force are obtained by mathematical analysis, as shown in Table [2](#page-7-2).

As can be seen from Table [2,](#page-7-2) with the increase of frequency, the magnitude of the suspension force remains constant. When the frequency of the motor is changed from 20 to 50 Hz, the prototype test results are around 28N, the results of analytical calculation and fnite element calculation are around 31.4N and 27.3N, respectively. The maximum relative error of the suspension force between the fnite element calculation and the prototype test is 2.2N (7.9%). And the maximum relative error between the analytical calculation results and the prototype test is 3.8N (13.6%).

<span id="page-7-2"></span>**Table 2** Dynamic suspension force measurement results

Frequency $(A)$	Test results $(N)$	FEM results $(N)$	Analytical results $(N)$
20	26.2	28.4	31.1
30	28.4	27.6	31.3
40	28.3	27.7	31.5
50	27.7	28.4	31.7

# **6 Conclusion**

In this paper, a nonlinear mathematical model of the suspension force considering the magnetic circuit saturation is proposed. Based on fnite element method, the magnitude and fuctuation of suspension force are calculated and analyzed. Combined with fnite element analysis, the following conclusions are drawn:

1) The distribution characteristics of magnetic feld in the case of magnetic circuit saturation caused by torque magnetic feld are diferent from that caused by suspension magnetic feld. With the increase of the suspension magnetic feld, the magnetic density of enhancement region increases from 1.7 T to 2.0 T, and the magnetic density of the magnetic density weakening region decrease from 1.7 T to 0.6 T. While, with the increase of the torque magnetic feld, the magnetic density of the two regions both increase by 0.4 T.

2) Afected by the magnetic circuit saturation, the suspension force will nonlinearly increases with the increase of coupled magnetic feld. The magnitude of the suspension force increases by 107N when the suspension winding current changes from 1 to 3A, while the suspension force increases by only 50N when the suspension winding current changes from 6 to 8A. As the torque magnetic feld increase, the magnitude of the suspension force frst increases and then decreases. The suspension force reaches a maximum of 275N when the torque magnet magnetic feld increase by 35%.

3) Compared to the unsaturated case, magnetic circuit saturation will cause sharp increase of suspension force fuctuation. When the suspension winding current increases from 3 to 11A, the fuctuation of suspension force increases from 4 to 20%. When the torque magnetic feld increases from 15 to 50%, the fuctuation of suspension force increases from 3.6% to 20%.

4) Afected by the magnetic circuit saturation, in the process of adjusting the phase of suspension magnetic feld, the magnitude of the suspension force will change. When the magnetic circuit is unsaturated, the magnitude of the suspension force is the same under the diferent phases of suspension magnetic feld, and the variation of suspension force is 0.2N at most. When the magnetic circuit is saturated, the magnitude of the suspension force is diferent, and the variation of suspension force is 7N at most.

#### **Declarations**

**Conflict of interest** No potential confict of interest was reported by the authors.

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