**ORIGINAL ARTICLE**



# **Second‑Order Nonlinear Disturbance Observer Based Adaptive Disturbance Rejection Control for PMSM in Electric Vehicles**

**Chengshun Yang<sup>1</sup> · Tao Hua1 · Yuchen Dai2 · Xiaoning Huang1 · Dongdong Zhang1**

Received: 1 April 2022 / Revised: 6 August 2022 / Accepted: 12 August 2022 / Published online: 1 September 2022 © The Author(s) under exclusive licence to The Korean Institute of Electrical Engineers 2022

### **Abstract**

In this paper, a high-performance nonlinear control technique is presented to address the robust anti-disturbance speed tracking problem for permanent magnet synchronous motors (PMSM) in electric vehicles. In the frst step, the dynamic model of PMSM is established, and the controller is designed based on backstepping control. Additionally, consider eliminating the diferential noise of the virtual controller and approving the virtual control rate and its derivative through the command flter in order to avoid complicated high-order derivatives. Then, based on the PMSM model, an improved model reference adaptive system (MRAS) is proposed to account for unknown parameter perturbation. Besides, in order to improve the antiinterference capability of the system during operation, a second-order nonlinear disturbance observer model is developed, and the robustness of the system is improved by combining the model with linear sliding mode control. Finally, the stability of the system is established using Lyapunov stability criteria, and the hardware-in-the-loop platform is established to demonstrate that the controller in this paper has excellent anti-interference abilities and robustness.

**Keywords** Electric vehicle · Permanent magnet synchronous motor · Second-order disturbance observer · Model reference adaptive system · Backstepping

# **1 Introduction**

With the continuous development of energy technology, electric vehicles have become an important part of the green road in the feld of transportation with the advantages of energy-saving and emission reduction [[1](#page-10-0)]. In EV drive systems, permanent magnet synchronous motors are widely used because of their high efficiency, high torque to

 $\boxtimes$  Yuchen Dai whutdyc@126.com

> Chengshun Yang yangchengshun@126.com

Tao Hua huaxiaott@126.com

Xiaoning Huang 1009133507@qq.com

Dongdong Zhang zddpig@163.com

<sup>1</sup> School of Electric Power Engineering, Nanjing Institute of Technology, Nanjing 211167, China

School of Automation, Wuhan University of Technology, Wuhan 430070, China

inertia ratio, high power density, and wide range of operating speeds [[2\]](#page-10-1)- [\[3](#page-10-2)]. However, the driving system of PMSM is highly nonlinear, strongly coupled, and multivariable [\[4](#page-10-3)]. At the same time, the variation of electric vehicle parameters and external load interference make the precise speed regulation of permanent magnet synchronous motor complicated.

For electric vehicles, with the random change of road conditions and the long-term operation of the motor, the motor parameters such as stator resistance, inductance, and permanent magnet fux will change [\[5](#page-10-4)]. Due to the modelbased backstepping control strategy, its control performance and effect greatly depend on the accuracy of the model [\[6](#page-10-5)]. In order to prevent the reduction of motor control performance caused by parameter perturbation, when the motor parameters change, the identifed parameters are fed back to the controller and corrected to ensure the control accuracy of the controller. Considering the error of off-line parameter identifcation of permanent magnet synchronous motor, it is hoped to realize online parameter identifcation and feedback accurate motor parameters to the control system for motor speed regulation control. Traditional online parameter identifcation methods include: the least square method, extended Kalman flter method, model parameter adaptive method,

and some other intelligent identifcation (neural network, genetic optimization algorithm). Based on the traditional least square method, the nonlinear least square method is introduced in [[8\]](#page-11-0), reducing the parameter identifcation error and improving the convergence speed. However, only two parameters of resistance and quadrature axis inductance can be identifed. Other scholars use the Kalman flter algorithm [\[9\]](#page-11-1) and neural network intelligent algorithm [\[10\]](#page-11-2) for identifcation. However, most algorithms can only identify two parameters, and the amount of calculation is signifcant, especially the results generated by the intelligent algorithm are uncertain. In order to realize the simultaneous identifcation of multiple parameters of the motor, people use the model reference adaptive system to identify the stator resistance, inductance, and permanent magnet fux linkage of the permanent magnet synchronous motor. In [\[11\]](#page-11-3)- [\[12](#page-11-4)], when the model refers to the identifcation parameters of the adaptive system, the adaptive convergence rate of each parameter to be identifed is derived with the help of Popov hyperstability theory, which ensures the convergence of the identifcation algorithm. However, the accuracy of parameter identifcation depends on the adjustment of PI parameters in the adaptive convergence rate. In the identifcation parameters of the model reference adaptive system, its performance mainly depends on the design of the adaptive rate. Because it is challenging to select the corresponding Lyapunov function when designing the adaptive rate through Lyapunov, for this reason, there are few reports about the model reference adaptive system identifcation parameters based on Lyapunov selection of the adaptive rate at home and abroad.

In recent years, people have studied to solve the disturbance problem caused by torque change by introducing disturbance observer (DO) into the control system [\[13](#page-11-5)]- [\[14](#page-11-6)]. In addition, due to the unmodeled dynamics and time-varying parameters, PMSM cannot establish an accurate mathematical model. These factors are also considered to interfere with the PMSM driving system. Through the combination of DO and sliding mode control method  $[15]$  $[15]$ , the problem of mismatched interference is solved. However, the disadvantage of sliding mode disturbance observer is that the interference estimation noise is severe, the flter will lead to estimation delay, and the initial estimation peak of the disturbance observer is not taken into account. In reference  $[16]$ , a finite time disturbance observer is constructed for the PMSM system. The error of the disturbance observer can converge in fnite time and reduce the infuence of the chattering problem. However, the permanent magnet synchronous motor system may be damaged due to the initial estimated peak value entering the system. In [\[17](#page-11-9)], a nonlinear disturbance observer is designed, which has the advantages of simple design and high estimation accuracy. Generally speaking, the accuracy of the observer is improved by increasing the gain coefficient of the disturbance observer, but the estimation peak will be seriously increased due to the increase of the gain. When a larger estimated peak is compensated in the initial time of the system, the hardware will be damaged. Obviously, there are still some challenges in the current methods to suppress the interference of the driving system.

Motivated by these observations, in order to improve the speed, accurate tracking control, and anti-interference ability of the permanent magnet synchronous motor of an electric vehicle, a second-order nonlinear disturbance observer-based adaptive disturbance rejection controller is proposed in this paper. The main contributions of this paper are summarized as follows:

- 1 Considering the time-varying parameters of permanent magnet synchronous motor, a step-by-step online identifcation method for an improved model reference adaptive system is designed. The adaptive law is set by Lyapunov stability theory to ensure the system's stability during identifcation.
- 2 The unmodeled disturbance of the PMSM motor system is estimated, and a time-varying second-order nonlinear disturbance observer is designed to compensate the PMSM controller of the electric vehicle, and the initial estimation peak of the disturbance observer is eliminated.
- 3 Through the backstepping control algorithm combined with the command flter, the direct derivation of the virtual control quantity in the traditional backstepping controller is avoided, and the output signal of the command flter is the derivative of the virtual controller after all.

The rest of this paper is organized as follows. Section [2,](#page-2-0) the dynamic model of PMSM is established, and some common lemmas are given. In Sect. [3,](#page-2-1) a model reference adaptive system parameter identifcation controller based on a second-order disturbance observer (MRAS-SODO) is designed and the stability of the system is proved. Section [4](#page-7-0) verifes the effectiveness of the designed synchronous controller through the hardware in the loop simulation platform of permanent magnet synchronous motor. Sect. [5](#page-10-6) summarizes the conclusions.



<span id="page-2-2"></span>**Fig. 1** The PMSM drive system in EVs

## <span id="page-2-0"></span>**2 Dynamic Model of PMSM**

As shown in Fig. [1](#page-2-2), the motor drive system of the electric vehicle is mainly composed of the following parts. The direct current (DC) power supply is provided by the electric vehicle battery, the DC bus capacitor can flter out the high-frequency voltage fuctuation, and the inverter is used as the actuator for electric energy conversion [[19](#page-11-10)]- [[20\]](#page-11-11). The dynamic model of PMSM in the *dq*-frame can be described as

$$
\frac{di_d}{dt} = -\frac{R_s}{L_s}i_d + p\omega_m i_q + \frac{1}{L_s}u_d
$$
\n
$$
\frac{di_q}{dt} = -\frac{R_s}{L_s}i_q - p\omega_m i_d - p\omega_m \frac{\varphi_f}{L_s} + \frac{1}{L_s}u_q
$$
\n
$$
\frac{d\omega_m}{dt} = \frac{1}{J}(T_e - B\omega_m - T_L - T_d)
$$
\n
$$
T_e = \frac{3}{2}p\varphi_f i_q
$$
\n(1)

where  $i_d$ ,  $i_g$ ,  $u_d$  and  $u_g$  denote the stator currents and voltages in the  $dq$ -frame;  $R_s$  is the stator resistance;  $L_s$  is the stator inductances in the *dq*-frame; *p* is the number of pole pairs;  $\varphi_f$  represents the permanent magnet flux; *J* is the moment of inertia; *B* is the viscous friction of the rotor;  $T_e$  denotes the electromagnetic torque;  $T_L$  is the load torque and disturbance torque, respectively, and  $T<sub>d</sub>$  represents friction torque and some unknown torque.

Define  $\phi_d = -\Delta \frac{3p\varphi_f}{2J} i_q + \Delta \frac{B}{J} \omega_m + \Delta \frac{1}{J} T_L$  denotes the unknown lumped disturbance.The mechanical motion equation of dynamic model [\(1](#page-2-3)) can be rewritten as

$$
\frac{d\omega_m}{dt} = \frac{3p\varphi_f}{2J}i_q - \frac{B}{J}\omega_m - \frac{1}{J}T_L - \phi_d
$$
\n(2)

#### **2.1 Related Lemmas**

To design the proposed control method and stability analysis, the following Lemmas are introduced.

**Lemma 1** *The polynomial represented by the Hurwitz matrix is stable*, *and all roots of the polynomial have negative real parts. The coefficient matrix of linear ordinary differential equation is Hurwitz matrix*, *which is the asymptotic stability of the modifed system*.

**Lemma 2** [\[21](#page-11-12)] : *Young*'*s inequality*: *for any nonnegative real number x*,*y*, *the following inequality holds*

$$
xy \le \frac{x^p}{p} + \frac{y^q}{q} \tag{3}
$$

*where p* > 1 *and*  $\frac{1}{p} + \frac{1}{q} = 1$ *. The equality sign holds when and only when*  $x^p = y^q$ .

# <span id="page-2-1"></span>**3 Design of the Controller for PMSM of EVs**

<span id="page-2-3"></span>In this part, we propose an online parameter identifcation controller based on a second-order nonlinear disturbance observer for PMSM of electric vehicles to improve tracking accuracy and anti-interference efficiency. In this design process, ∗*̂* is defned as the estimated value of variable ∗, and  $\tilde{*}$  is the estimated error, which satisfies  $\tilde{*}$  =  $\tilde{*}$  −  $*$ .

## **3.1 Identifcation Parameter Online**

Model reference adaptive system (MRAS) designs the model containing the parameters to be identifed as the identifcation model and takes the existing system as the reference model. Under the same input-output conditions, the errors of the reference model and the identifcation model are taken as the input of the parameter adaptive convergence rate. The parameters of the identifcation model are adjusted according to the designed adaptive rate to make the error between it and the reference model converge to zero to complete the online parameter identifcation.

<span id="page-2-4"></span>First, fix the rotor flux linkage  $\varphi_f$ , identify the  $R_s$  and *Ls* parameters.

Design reference model as

$$
\begin{pmatrix}\n\dot{i}_d \\
\dot{i}_q\n\end{pmatrix} = \begin{pmatrix}\n-m & p\omega_m \\
-p\omega_m & -m\n\end{pmatrix} \begin{pmatrix}\n\dot{i}_d \\
\dot{i}_q\n\end{pmatrix} + \begin{pmatrix}\nn & 0 \\
0 & n\n\end{pmatrix} \begin{pmatrix}\nU_d \\
U_q\n\end{pmatrix} + \begin{pmatrix}\n0 \\
-p\omega_m\varphi_f n\n\end{pmatrix}
$$
\n(4)

Design identifcation model as

$$
\begin{pmatrix}\n\dot{i}_a^c \\
\dot{i}_q^c \\
\dot{i}_q^c\n\end{pmatrix} = \begin{pmatrix}\n-\hat{m} & p\omega_m \\
-p\omega_m & -\hat{m}\n\end{pmatrix} \begin{pmatrix}\n\dot{i}_d^c \\
\dot{i}_q^c \\
\dot{i}_q^c\n\end{pmatrix} + \begin{pmatrix}\n\hat{n} & 0 \\
0 & \hat{n}\n\end{pmatrix} \begin{pmatrix}\nU_d \\
U_q\n\end{pmatrix} + \begin{pmatrix}\n0 \\
-p\omega_m\varphi_f\hat{n}\n\end{pmatrix}
$$
\n(5)

where  $i_d^c$  and  $i_q^c$  are the reference values of stator current  $i_d$ and  $i_q$  respectively.

Based on the reference model and identifcation model, the error between them is

$$
\begin{pmatrix}\n\dot{i}_d - \dot{i}_d^c \\
\dot{i}_d - \dot{i}_q^c\n\end{pmatrix} = \begin{pmatrix}\n-m & p\omega_m \\
-p\omega_m & -m\n\end{pmatrix} \begin{pmatrix}\n\dot{i}_d - \dot{i}_d^c \\
\dot{i}_q - \dot{i}_q^c\n\end{pmatrix} + \begin{pmatrix}\n\dot{i}_d^c & -U_d \\
\dot{i}_q^c & -(U_q - p\omega_m\varphi_f)\n\end{pmatrix} \begin{pmatrix}\n\hat{m} - m \\
\hat{n} - n\n\end{pmatrix}
$$
\n(6)

$$
\begin{aligned}\n\text{D e f i n e} \qquad & e_1 = \begin{pmatrix} i_d - i_d^c \\ i_q - i_q^c \end{pmatrix}, \qquad A = \begin{pmatrix} -m & p\omega_m \\ -p\omega_m & -m \end{pmatrix}, \\
B = \begin{pmatrix} i_d^c & -U_d \\ i_q^c & -(U_q - p\omega_m \varphi_f) \end{pmatrix}, C = \begin{pmatrix} \hat{m} - m \\ \hat{n} - n \end{pmatrix} \\
\text{Transform model (6) to the following form}\n\end{aligned}
$$

$$
\dot{e}_1 = Ae_1 + BC \tag{7}
$$

The Lyapunov function is defned as

$$
V(e_1) = \frac{1}{2} (e_1^T Q e_1 + C^T K C)
$$
 (8)

where *Q* and *K* is a real symmetric positive defnite matrix, And  $Q = K = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$ .

Combining [\(7\)](#page-3-1), the derivative of  $V(e_1)$  is

$$
\dot{V}(e_1) = \frac{1}{2} \left( \dot{e}_1^T Q e_1 + e_1^T Q \dot{e}_1 + \dot{C}^T K C + C^T K \dot{C} \right)
$$
(9)

where  $\begin{cases} e_1^T Q e_1 = C^T B^T Q e_1 + e_1^T A^T Q e_1 \\ e_1^T Q e_1 - e_1^T Q A e_1 + e_1^T Q B C \end{cases}$  $e_1^T Q e_1 = e_1^T Q A e_1 + e_1^T Q B C$ , The dynamic model  $(9)$  $(9)$  can be rewritten

$$
\dot{V}(e_1) = \frac{1}{2} \left[ e_1^T (A^T Q + QA) e_1 + C^T B^T Q e_1 + e_1^T Q B C \right. \\
 \left. + \dot{C}^T K C + C^T K \dot{C} \right]
$$
\n(10)

Because of

$$
A^T Q + QA
$$
  
=  $\begin{pmatrix} -m & -p\omega_m \\ p\omega_m & -m \end{pmatrix} \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} + \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} -m & p\omega_m \\ -p\omega_m & -m \end{pmatrix}$   
=  $\begin{pmatrix} -2m & 0 \\ 0 & -2m \end{pmatrix}$  (11)

where  $-2m = -2 \times \frac{R_s}{L_s} < 0$ , therefore  $e_1^T (A^T Q + QA) e_1$  is a negative defnite function.

For the rest of formula  $(10)$  $(10)$ , simplify it to get

$$
CTBTQe1 + e1TQBC + CTKC + CTKC
$$
  
= 2( $\hat{m}$  -  $m$ )  $\left[ i_d^c (i_d - i_d^c) + i_q^c (i_q - i_q^c) + (\hat{m} - \hat{m}) \right]$   
+ 2( $\hat{n}$  -  $n$ )  $\left[ -U_d (i_d - i_d^c) - (U_q - p\omega_m \varphi_f) (i_q - i_q^c) + (\hat{n} - \hat{n}) \right]$  (12)  
+ (  $\hat{n}$  -  $\hat{n}$  )

<span id="page-3-0"></span>When  $(C^T B^T Q e_1 + e_1^T Q B C + C^T K C + C^T K C) = 0$ , then  $\dot{V}(e_1) < 0$  can be satisfied.

Define 
$$
\begin{cases} i_a^c (i_d - i_d^c) + i_q^c (i_q - i_q^c) + (\dot{m} - \dot{m}) = 0 \\ -U_d (i_d - i_d^c) - (U_q - p\omega_m \varphi_f) (i_q - i_q^c) + (\dot{n} - \dot{n}) = 0 \end{cases}
$$

⎩ The adaptive rate of m and n can be calculated as

<span id="page-3-1"></span>
$$
\begin{cases}\n\hat{m} = \int_0^t - \left[ i_d^c \left( i_d - i_d^c \right) + i_q^c \left( i_q - i_q^c \right) \right] dt + m_0 \\
\hat{n} = \int_0^t \left[ U_d \left( i_d - i_d^c \right) + \left( U_q - p \omega_m \varphi_f \right) \left( i_q - i_q^c \right) \right] dt + n_0\n\end{cases}
$$
\n(13)

After obtaining the stator resistance  $R_s$  and inductance numbers  $L_s$ , identify the rotor flux linkage  $\varphi_f$  as follows

Design reference model

$$
\frac{di_q}{dt} = -\frac{R_s}{L_s}i_q - p\omega_m i_d - \frac{1}{L_s}p\omega_m\varphi_f + \frac{1}{L_s}U_q
$$
\n(14)

<span id="page-3-2"></span>Design identifcation model

$$
\frac{di_q^c}{dt} = -\frac{R_s}{L_s}i_q^c - p\omega_m i_d - \frac{1}{L_s}p\omega_m \hat{\varphi}_f + \frac{1}{L_s}U_q
$$
\n(15)

Similarly, according to Lyapunov stability, the adaptive rate of rotor flux linkage  $\varphi_f$  can be calculated as

<span id="page-3-3"></span>
$$
\hat{\varphi}_f = \int_0^t - \left[ p\omega_m \left( i_q - i_q^c \right) \right] dt + \varphi_{f0} \tag{16}
$$

## **3.2 Disturbance Observer Design and Stability Proof**

**Assumption 1** Assuming that the unknown lumped disturbance  $\phi_d$  is of Eq. [\(2\)](#page-2-4) continuous and bounded, and satisfy- $\log \frac{1}{2}$  $\phi_d^{(i)}$   $\leq \mu_1, i = 0, 1, 2.$ 

Here  $\phi_d$  indicates that the perturbation and the gradient of the parameters (such as viscous friction *B*, the moment of inertia *J*, permanent maget flux  $\varphi_f$ , etc.) are not only continuous but also have an upper bound.

In order to estimate the mismatch disturbance in the permanent magnet synchronous motor system and eliminate the peak value of the initial time estimation, a time-varying second-order nonlinear disturbance observer is used for compensation, which can be designed as follows

$$
\begin{cases}\n\hat{\phi}_d = \rho_1 + \lambda_1 x_1 \\
\dot{\rho}_1 = -\lambda_1 (x_2 + \hat{\phi}_d) + \hat{\phi}_d \\
\hat{\phi}_d = \rho_2 + \lambda_2 x_1 \\
\dot{\rho}_2 = -\lambda_2 (x_2 + \hat{\phi}_d)\n\end{cases}
$$
\n(17)

$$
\begin{cases}\n\lambda_1 = \mu_1 (1 - e^{-\mu_2 t}) \\
\dot{\lambda}_1 = \mu_1 \mu_2 e^{-\mu_2 t} \\
\lambda_2 = \mu_3 (1 - e^{-\mu_4 t}) \\
\dot{\lambda}_2 = \mu_3 \mu_4 e^{-\mu_4 t}\n\end{cases}
$$
\n(18)

where  $x_1 = \omega_{mref} - \omega_m$ ,  $x_2 = \dot{x}_1 + \phi_d$ ,  $\mu_1, \mu_2, \mu_3, \mu_4$  is the positive constant,  $\rho_1$ ,  $\rho_2$  is the auxiliary variable of the second-order observer,  $\lambda_1$ ,  $\lambda_2$  is the gain coefficient of the observer.

**Theorem 1** *According to the time*-*varying second*-*order nonlinear disturbance observers* ([17\)](#page-4-0) , *the disturbances and their derivatives of the system* [\(2](#page-2-4)) *are uniformly ultimately bounded*.

*Proof* The error of disturbance observation  $\phi_d$ ,  $\dot{\phi}_d$  can be defined as  $\tilde{\phi}_d$ ,  $\tilde{\dot{\phi}_d}$ 

$$
\tilde{\phi}_d = \dot{\phi}_d - \hat{\phi}_d \tag{19}
$$

$$
\dot{\tilde{\phi}}_d = \dot{\phi}_d - \left( -\lambda_1 \left( x_2 + \hat{\phi}_d \right) + \hat{\phi}_d + \lambda_1 \dot{x}_1 \right) \tag{20}
$$

Then take the  $x_2 = \dot{x}_1 + \phi_d$  in [\(20\)](#page-4-1)

$$
\begin{aligned}\n\dot{\phi}_d &= \dot{\phi}_d - \left( -\lambda_1 x_2 - \lambda_1 \hat{\phi}_d + \hat{\phi}_d + \lambda_1 x_2 + \lambda_1 \phi_d \right) \\
&= \hat{\phi}_d - \lambda_1 \tilde{\phi}_d\n\end{aligned} \tag{21}
$$

Similarly, the following expression can be obtained.

Defne error as

$$
e_d = \left[\tilde{\phi_d} \ \tilde{\phi_d}\right]^T \tag{23}
$$

$$
\dot{e}_d = A_d e_d + B_d \dot{\phi}_d \tag{24}
$$

where  $A_d =$  $\begin{bmatrix} -\lambda_1 & 1 \end{bmatrix}$  $-\lambda_2$  0 ]  $B_d =$  $\lceil 0$ 1 ] .

As a result, through design  $\lambda_1 = 2k_0$ ,  $\lambda_2 = k_0^2$ , Then can get  $\lambda(A_d) = \lambda_{\text{max}}(A_d) = \lambda_{\text{max}}(A_d) = -k_0$ , Thus, it is constructed as Hurwitz matrix. In addition, the infuence of the estimated peak is weakened by design  $\mu_2 > \frac{1}{k_0}$ ,  $\mu_4 > \frac{1}{k_0}$ .

Design the Lyapunov function for  $\dot{e}_d = A_d \dot{e}_d + B_d \ddot{\theta}_d$  as

$$
V(e_d) = e_d^T P e_d \tag{25}
$$

<span id="page-4-0"></span>where P and Q are real symmetric positive definite matrices,  $A_d^T P + P A_d = -Q$ . Take the derivative of  $V(e_d)$  and get

$$
\dot{V}(e_d) \n= e_d^T P e_d + e_d^T P e_d \n= (B_d \ddot{\phi}_d)^T P e_d + e_d^T A_d^T P e_d + e_d^T P A_d e_d + e_d^T P B_d \ddot{\phi}_d
$$
\n(26)  
\n
$$
= e_d^T (A_d^T P + P A_d) e_d + (B_d \ddot{\phi}_d)^T P e_d + e_d^T P B_d \ddot{\phi}_d
$$
\n
$$
= -e_d^T Q e_d + (B_d \ddot{\phi}_d)^T P e_d + e_d^T P B_d \ddot{\phi}_d
$$

Because P is a real symmetric matrix, so

$$
\dot{V}(e_d) = -e_d^T Q e_d + 2e_d^T P B_d \ddot{\phi}_d \n\leq -e_d^T Q e_d + 2 ||e_d||_2 \lambda_{\text{max}}(P) ||B_d||_2 ||\ddot{\phi}_d||_2 \n\leq -e_d^T Q e_d + 2 ||e_d||_2 \lambda_{\text{max}}(P) \mu_1 \n\leq -(1 - \kappa) e_d^T Q e_d - \kappa e_d^T Q e_d \n+ 2 ||e_d||_2 \lambda_{\text{max}}(P) \mu_1
$$
\n(27)

where  $0 < \kappa < 1$ If let  $-κ e^T_d Qe_d + 2||e_d||_2 λ_{max}(P)μ_1 ≤ 0$ , then can get the  $||e_d||_2 \leq \frac{\kappa e_d^T Q e_d}{2||e_d||_2 \lambda_{\max}}$  $\frac{\log_{d} \mathcal{Q} e_{a}}{2\left\|e_{d}\right\|_{2} \lambda_{\max}(P)\mu_{1}}.$ Then  $\dot{V}(e_d) \le -(1 - \kappa)e_d^T Q e_{d1} \le 0$  holds, The proof is  $\Box$   $\Box$ 

<span id="page-4-1"></span>*Remark 1* In our design of second-order nonlinear disturbance observer, if only the gain term exists as in a normal sliding mode observer, ensuring convergence or improving the accuracy of the observer by expanding the gain coefficient may seriously increase the problems of estimated peaks and chattering. To summarize, the estimated errors of the observers of a second-order nonlinear disturbance observer can be asymptotically stable.

#### **3.3 Design of Controller and Stability Proof**

*Step 1*: Construct the transformed error and Command Filter.

In order to realize the accurate speed tracking performance constraint of PMSM, based on dynamic model ([1\)](#page-2-3),the system tracking error is defned as

$$
z_1 = \omega_m - \omega_{mref}, z_2 = i_q - i_q^c, z_3 = i_d - i_d^c \tag{28}
$$

where,  $\omega_{\text{mref}}$  is the target reference speed,  $i_q^c$  is the reference value of q-axis current and  $i_q^d = 0$ ,  $i_q^c$  is the reference value of d-axis current.

In order to solve the diferential expansion problem in the traditional backstepping control design, and considering the input saturation in practice, the instruction flter is introduced, so that the derivative of the virtual controller can be obtained from the integral link [[18](#page-11-13)]. The Command Filter is difned as

$$
\begin{bmatrix}\n\dot{q}_1 \\
\dot{q}_2\n\end{bmatrix} = \begin{bmatrix}\n0 & 1 \\
-2\zeta_i \sigma_{ni} S_R \left(\frac{\sigma_{ni}}{2\zeta_i}\right) - 2\zeta_i \sigma_{ni}\n\end{bmatrix} \begin{bmatrix}\nq_1 \\
q_2\n\end{bmatrix} + \begin{bmatrix}\n0 \\
-2\zeta_i \sigma_{ni} S_R \left(\frac{\sigma_{ni}}{2\zeta_i}\right)\n\end{bmatrix} S_M(u)
$$
\n(29)

where,  $S_M(.)$  and  $S_R(.)$  are the amplitude limiting and rate limiting respectively;  $\zeta$ <sub>i</sub> and  $\sigma$ <sub>ni</sub> are the damping and bandwidth of the Command Filter respectively.

Considering the estimation error of Command Filter, the filter error compensation signal  $\varepsilon$  is designed as

$$
\dot{\varepsilon} = -k_1 \varepsilon + \frac{3p\varphi_f}{2J} \left( i_q^c - i_q^d \right) \tag{30}
$$

where,  $i_q^c$  is the output of the virtual control law after passing through the command flter.

*Step 2*: Construct the virtual control law.

Redefne speed tracking error as

$$
\bar{z}_1 = z_1 - \varepsilon_1 \tag{31}
$$

According to function [\(2](#page-2-4)) and ([30](#page-5-0)), the derivative of  $\bar{z}_1$  is calculated as

$$
\dot{\overline{z}}_1 = \frac{3P\varphi_f}{2J} i_q - \frac{1}{J} B_m \omega_m - \frac{1}{J} T_L - \phi_d
$$
  
\n
$$
- \omega mref + K_1 \xi - \frac{3P\varphi_f}{2J} \left( i_q^c - i_q^d \right)
$$
  
\n
$$
= -K_1 \overline{z}_1 + \frac{3P\varphi_f}{2J} z_z + \tilde{\phi}_d - \hat{\rho} sign(\overline{z}_1)
$$
\n(32)

where  $\rho$  is the observation error boundary of disturbance  $\phi_d$ , and satisfy  $\|\tilde{\phi}_d\| \leq \rho$ ,  $\hat{\rho}$  is an estimate of  $\rho$ .  $L_1$  and  $w_1$  are nositive constant positive constant.

In order to stabilize the error  $\bar{z}_1$ , define the Lyapunov function of  $V_2 = \frac{1}{2}\bar{z}_1^2$  and the derivative of  $V_2$  is obtained

$$
\dot{V}_2 = -K_1 \bar{z}_1^2 + \frac{3P\varphi_f}{2J} \bar{z}_1 z_z + \bar{z}_1 \big( \tilde{\varphi}_d - \hat{\rho} sign(\bar{z}_1) \big)
$$
(33)

*Step 3*: Construct the real control law.

In order to improve the robustness of the system, the linear sliding mode surface is introduced into the inner loop control, and the sliding mode surfaces of d-axis and q-axis are defned as

<span id="page-5-2"></span>
$$
S_q = \sigma z_2
$$
  
\n
$$
S_d = \sigma z_3
$$
\n(34)

At the same time, the sliding mode reaching laws are chosen as

<span id="page-5-1"></span>
$$
\dot{S}_q = -h_2 \text{sig}(S_q) - \rho_2 S_q
$$
  
\n
$$
\dot{S}_d = -h_3 \text{sig}(S_d) - \rho_3 S_d
$$
\n(35)

where,  $h_2$ ,  $h_3$ ,  $\rho_2$ ,  $\rho_3 > 0$  is the designed controller parameter.

 $Sign(x)$  is also commonly referred to as a sign function and is defned as follows

$$
sign(x) = \begin{cases} 1, & x > 0 \\ 0, & x = 0 \\ -1, & x < 0 \end{cases}
$$
 (36)

<span id="page-5-0"></span>It can be seen that sign  $(x)$  is a discontinuous function, so the existence of symbolic function will further aggravate the chattering phenomenon. In this paper, sigmoid function is considered, that is, sig (.) in Eq. [\(35](#page-5-1)), Instead of the traditional symbolic function, the sliding mode chattering phenomenon is weakened.

$$
sig(x) = \frac{2}{1 + exp(-Qx)} - 1
$$
 (37)

where  $Q > 0$ , it can be seen from the expression that the sigmoid function is smooth and continuous.

According to the mathematical model of IPMSM, the derivative of Eq. [\(34](#page-5-2)) can be obtained as

$$
\dot{S}_q = \sigma \dot{z}_2 = \sigma \left( \dot{i}_q - \dot{i}_q^c \right)
$$
\n
$$
= \sigma \left( -m\dot{i}_q - p\omega_m \dot{i}_d - np\omega_m \varphi_f + nU_q - \dot{i}_q^c \right)
$$
\n
$$
= \sigma \left( -(\hat{m} - \tilde{m})\dot{i}_q - p\omega_m \dot{i}_d - (\hat{n} - \tilde{n})p\omega_m \varphi_f + (\hat{n} - \tilde{n})U_q - \dot{i}_q^c \right)
$$
\n
$$
\dot{S}_d = \sigma \dot{z}_3 = \sigma \left( \dot{i}_d - \dot{i}_d^c \right)
$$
\n
$$
= \sigma \left( -m\dot{i}_d + p\omega_m \dot{i}_q + nU_d - \dot{i}_d^c \right)
$$
\n
$$
= \sigma \left( -(\hat{m} - \tilde{m})\dot{i}_d + p\omega_m \dot{i}_q + (\hat{n} - \tilde{n})U_d - \dot{i}_d^c \right)
$$
\n(38)

Defne the Lyapunov function as

$$
V_3 = V_2 + \frac{1}{2}S_q^2 + \frac{1}{2}S_d^2 + \frac{1}{2}\sigma^2 \tilde{m}^2 + \frac{1}{2}\sigma^2 \tilde{n}^2
$$
 (39)

The derivative of  $V_3$  can be calculated as

$$
\dot{V}_{3} = \bar{z}_{1}\dot{\bar{z}_{1}} + S_{q}\dot{S}_{q} + S_{d}\dot{S}_{d} + \delta^{2}\tilde{m}\dot{\hat{m}} + \delta^{2}\tilde{n}\dot{\hat{n}}
$$
\n
$$
= -k_{1}\bar{z}_{1}^{2} + \frac{3p\varphi_{f}}{2J}\bar{z}_{1}z_{2} + \bar{z}_{1}(\tilde{\phi}_{d} - \hat{\rho}sign(\bar{z}_{1}))
$$
\n
$$
+ \sigma S_{q}(-\hat{m}i_{q} - p\omega_{m}i_{d} - \hat{n}p\omega_{m}\varphi_{f} + \hat{n}U_{q} - \dot{i}_{q}^{c})
$$
\n
$$
+ \sigma S_{d}(-\hat{m}i_{d} + p\omega_{m}i_{q} + \hat{n}U_{d} - \dot{i}_{d}^{c} + h_{3}sig(S_{d})) \qquad (40)
$$
\n
$$
+ \sigma \rho_{2}S_{q}^{2} + \sigma h_{2}S_{q}sig(S_{q}) + \sigma \rho_{3}S_{d}^{2} + \sigma h_{3}S_{d}sig(S_{d})
$$
\n
$$
- h_{2}S_{q}sig(S_{q}) - h_{3}S_{d}sig(S_{d}) - \rho_{2}S_{q}^{2} - \rho_{3}S_{d}^{2}
$$
\n
$$
+ \tilde{m}(\delta^{2}\dot{\hat{m}} + \sigma S_{q}i_{q} + \sigma S_{d}i_{d})
$$
\n
$$
+ \tilde{n}(\delta^{2}\dot{\hat{n}} + \sigma S_{q}(p\omega_{m}\varphi_{f} - U_{q}) - \sigma S_{d}U_{d})
$$

According to Eq. ([40\)](#page-6-0) and Lyapunov stability theorem, the d-axis and q-axis controllers are designed as

$$
u_q = \frac{1}{\hat{n}} \left( \hat{m}i_q + p\omega_m i_d + p\omega_n \varphi_f \hat{n} + i_q^c - h_2 \text{sig}(S_q) - \rho_2 S_q \right)
$$
\n
$$
\tag{41}
$$

$$
u_d = \frac{1}{\hat{n}} (\hat{m}i_d - p\omega_m i_q + i_d^c - h_3 \text{sig}(S_d) - \rho_3 S_d)
$$
 (42)

According to the adaptive rate designed by MRAS

$$
\begin{cases}\n\dot{\hat{m}} = -\left(\dot{t}_d^c z_3 + \dot{t}_q^c z_2\right) \\
\dot{\hat{n}} = U_d z_3 + \left(U_q - p \omega_m \varphi_f\right) z_2\n\end{cases} \tag{43}
$$

Equations  $(41)$  $(41)$  and  $(42)$  are brought into the Eq.  $(40)$  $(40)$ 

$$
\dot{V}_3 = -k_1 \bar{z}_1^2 + \frac{3p\varphi_f}{2J} \bar{z}_1 z_2 - h_2 S_q \text{sig}(S_q) - h_3 S_d \text{sig}(S_d) \n- \rho_2 S_q^2 - \rho_3 S_d^2 + \bar{z}_1 (\tilde{\phi}_d - \hat{\rho} \text{sign}(\bar{z}_1)) \n+ \tilde{m} (\delta^2 z_2^2 + \delta^2 z_3^2)
$$
\n(44)

In order to consider the stability of time-varying secondorder non-linear disturbance observer, reselect Lyapunov candidate function as



**Fig. 2** HIL platform setup

<span id="page-6-8"></span>
$$
V_4 = V_3 + \frac{1}{2} (\tilde{d}^2 + \tilde{\rho}^2 / L_1)
$$
  
=  $\frac{1}{2} \bar{z}_1^2 + \frac{1}{2} S_d^2 + \frac{1}{2} S_q^2 + \frac{1}{2} \sigma^2 \tilde{m}^2 + \frac{1}{2} \sigma^2 \tilde{n}^2$   
+  $\frac{1}{2} (\tilde{\phi}_d^2 + \tilde{\rho}^2 / L_1)$  (45)

<span id="page-6-0"></span>Subsequently, the derivative of  $V_4$  can be calculated as

<span id="page-6-7"></span>
$$
\dot{V}_4 = \dot{V}_3 + \tilde{\phi}_d \dot{\phi}_d + \tilde{\rho} \dot{\rho} / L_1 \tag{46}
$$

Furthermore, in order to eliminate the coupling term  $\frac{3p\varphi_f}{2J} \bar{z}_1 z_2$ in Eq. ([44](#page-6-3)), define  $0 < \gamma < 1$ , then we can obtain

<span id="page-6-4"></span>
$$
-k_1\bar{z}_1^2 + \bar{z}_1 z_2 \frac{3p\varphi_f}{2J} \leq -k_1\gamma |\bar{z}_1|^2 - k_1(1-\gamma)\bar{z}_1^2 + \frac{3p\varphi_f}{2J} |\bar{z}_1||z_2| \tag{47}
$$

<span id="page-6-2"></span><span id="page-6-1"></span>Assuming the condition  $|\bar{z}_1| \ge \frac{3p\varphi_f|z_2|}{2k_1\gamma J}$  can be satisfied, then inequality Eq. ([47\)](#page-6-4) can be represented as

<span id="page-6-5"></span>
$$
-k_1 \bar{z}_1^2 + \frac{3p\varphi_f \bar{z}_1 z_2}{2J} \le -k_1 (1 - \gamma) \bar{z}_1^2 \tag{48}
$$

Evidently, this condition can be achieved by adjusting the parameter  $k_1$ .

Note that the term  $-\overline{z}_1(\hat{\phi}_d + \hat{\rho} sign(\overline{z}_1))$  in ([44](#page-6-3)) has the following unequal relationship

<span id="page-6-3"></span>
$$
\bar{z}_1(\hat{\phi}_d - \hat{\rho}sign(\bar{z}_1)) \le |\bar{z}_1||\hat{\phi}_d| - \bar{z}_1 \rho sign(\bar{z}_1) \n- \bar{z}_1 \tilde{\rho} sign(\bar{z}_1) \le -\bar{z}_1 \tilde{\rho} sign(\bar{z}_1) \le -\tilde{\rho}\hat{\rho}/L_1 - w_1 \tilde{\rho}\hat{\rho}/L_1
$$
\n(49)

According to Lemma 2 , the following inequality can be obtained for  $-w_1 \tilde{\rho} \hat{\rho} / L_1$ 

<span id="page-6-6"></span>
$$
-w_1 \tilde{\rho} \hat{\rho} / L_1 \le -w_1 \tilde{\rho}^2 / 2L_1 + w_1 \rho^2 / 2L_1 \tag{50}
$$

According to  $(48)$  $(48)$ ,  $(50)$ , Then, Eq.  $(46)$  $(46)$  can be rewritten as

$$
\dot{V}_4 \le -k_1(1-\gamma)\bar{z}_1^2 - \rho_2 S_q^2 - \rho_3 S_d^2 - w_1 \bar{\rho}^2 / 2L_1 \n+ w_1 \rho^2 / 2L_1 + \tilde{m} (\delta^2 z_2^2 + \delta^2 z_3^2) \n\le -\kappa V_4 + v
$$
\n(51)

 $\text{where} \quad \kappa = \min\left\{2K_1(1-\ell), 2\rho_3, 2\rho_2, w_1\right\}v = w_1\rho^2/2L_1,$  $+\tilde{m}(\delta^2 z_2^2 + \delta^2 z_3^2)$ , for  $\forall t \ge t_0$ , the ([51](#page-7-1)) can be obtained.

Further, for  $\forall t \geq t_0$ 

$$
V_4(t) \le \left(V_4(t_0) - \frac{\xi}{\kappa}\right) e^{-\kappa(t - t_0)} + \frac{\xi}{\kappa} \le V_4(t_0) + \frac{\xi}{\kappa} \tag{52}
$$

The proof is completed.

*Remark 2* The filtering error of command filter is bounded in fnite time. Thus, compensated tracking error is bounded, indicating that all the signals in the control system can be regarded as semi-globally uniformly ultimately bounded.



<span id="page-7-2"></span>**Fig. 3** Topology of the HIL platform

#### <span id="page-7-0"></span>**4 Results and Analysis**

<span id="page-7-1"></span>Built an electric vehicle PMSM hardware in the loop platform based on FPGA, and the efectiveness of the proposed parameter identifcation control method is clarifed by the HIL test [\[23\]](#page-11-14)- [[24\]](#page-11-15), which can be seen in Fig. [2.](#page-6-8) The realtime implementation platform adopts FPGA+dSPACE architecture. In this system, dSPACE is the controller, and FPGA is used to simulate the PMSM and inverter. The real-time control system is constructed using the DS1202 baseboard and DS1302 I/O board, which are included in the dSPACE. The FPGA board consists of Cyclone IV E: EP4CE115F23I7 device, a 48Mhz clock, and twelve 12-bit digital to analog converter (DAC) channels, which can realize powerful parallel real-time computing function [[25\]](#page-11-16)- [\[26\]](#page-11-17).

Using the Verilog language in the Quartus II software, the FPGA program is downloaded into the FPGA chip. In the FPGA program, the equivalent circuit of PMSM and the operation principle of DC power supply and inverter are described. A voltage signal is superimposed on a random noise to create a virtual DC voltage source, and a PWM signal is used to control the voltage at the input of the PMSM equivalent circuit. In the PMSM HIL platform, the deadtime, turn-on, and turn-off times of IGBT are also emulated in order to make it more realistic  $[27]$ , which can be seen in Fig. [3.](#page-7-2)

Unlike simulation, the PMSM HIL platform is able to operate in real-time, which means that when designing the control method, the real-time computing power of the controller must be considered. Due to the transmission of signals through metal wires in the PMSM HIL platform, the signals may contain some noise and delays, which is consistent with the experimental platform. The PMSM HIL platform operates as follows: (1) The stator current and angular velocity of the PMSM calculated by the FPGA board are transmitted to



<span id="page-7-3"></span>**Fig. 4** Composite control strategy

#### <span id="page-8-0"></span>**Table 1** Parameters of the PMSM

Name	Symbol	Value
Armature resistance	$R_{\rm s}$	$0.05\Omega$
Stator inductance of d-axis	$L_{\rm s}$	2mH
Stator inductance of $q$ -axis	$L_{\scriptscriptstyle\rm v}$	2mH
Permanent magnet flux	$\varphi_f$	1/3Wb
Number of poles	p	$\mathfrak{D}$
Equivalent inertia		$0.033$ kg · m <sup>2</sup>
Viscous friction coefficient	R	0.0003Nms
DC catenary voltage	$V_{dc}$	1000V

<span id="page-8-1"></span>**Table 2** Parameters of the control method





<span id="page-8-2"></span>**Fig. 5** Speed tracking control response of PI control

the dSPACE via wires in real-time; (2) dSPACE calculates real-time the control signal; (3) To generate pulse signals, the control signal of the PMSM is modulated with space vector pulse width modulation (SVPWM) and sent to the FPGA board.

The above results prompted the development of a PMSM hardware-in-the-loop simulation platform, where the FPGA is responsible for describing the PMSM dynamic model, and dSPACE is used as the PMSM controller for electric vehicles to calculate the control signals for each permanent magnet synchronous motor in real-time. The parameters of PMSM and the proposed control method are set forth in Tables [1](#page-8-0) and [2](#page-8-1) .

An appropriate sampling time is chosen as  $100\mu s$ , the dead-time is set to  $3\mu s$ , the turn-on time of IGBT is set to  $0.35\mu s$ , and the turn-off time of IGBT is set to  $0.1\mu s$ . In FPGA boards, the turn-on voltage drop of the diode and the insulated gate bipolar transistor (IGBT) is simulated





<span id="page-8-3"></span>**Fig. 6** Speed tracking control response of Backstepping control



<span id="page-8-4"></span>**Fig. 7** Speed tracking control response of MRAS-SODO control



<span id="page-8-5"></span>**Fig. 8** Response curves of  $i_q$  under different control methods

and set to 0.7V and 1.8V, respectively. In order to provide a fair and comprehensive comparison, the proposed control method in Fig. [4](#page-7-3) is compared to the two other methods, one is the Backstepping nonlinear control method (BSC), and the other is traditional PI control. The two cases are then used to analyze the speed tracking performance as well as the anti-disturbance performance of EVs at variable speeds under three control strategies.

As a measure of the efectiveness of the method and to simulate the fuctuation of the speed of electric vehicles on urban roads more realistically, the reference speed is used as the speed change signal. Furthermore, owing to the complexity of road conditions, the load torque is suddenly increased and decreased at  $t = 4s$  and  $t = 8s$ , respectively. The speed tracking control responses of three controllers are shown in Figs. [5,](#page-8-2) [6](#page-8-3) and [7](#page-8-4). During the startup phase



<span id="page-9-0"></span>**Fig. 9** Response curves of  $i_d$  under different control methods

<span id="page-9-1"></span>**Table 3** Vehicle start-up phase performance

Algorithms	Overshoot(rpm)	Arrival time $(s)$	Peak current(A)
PI	2	0.03	7.5
<b>BSC</b>		0.015	6.5
$MRAS - SODO$	$\mathcal{D}$	0.01	

<span id="page-9-2"></span>**Table 4** Performance at the phase of a sudden load torque





<span id="page-9-3"></span>**Fig. 10** Command flter input and output signal

of the electric vehicle, the PI control and BSC have a lag in speed tracking; however, the control strategy proposed in this paper does not have a lag and has an immediate response to speed tracking. It is noteworthy that when a load disturbance occurs, the PI control and backstep control have tracking speed errors, but the control strategy using the second-order disturbance observer has a smaller tracking speed error and no initial estimated peak value.



<span id="page-9-4"></span>**Fig. 11** Stator resistance  $R_s$  identification waveform



<span id="page-9-5"></span>**Fig. 12** Stator inductance  $L<sub>s</sub>$  identification waveform



<span id="page-9-6"></span>**Fig. 13** permanent magnet flux  $\varphi_f$  identification waveform

Additionally, the MRAS-SODO speed tracking accuracy is relatively accurate.

To compare the current control performance between different control methods, Figs. [8](#page-8-5) and [9](#page-9-0) shows the *dq*-frame currents of the outer front in-wheel PMSM under diferent control methods. The proposed control method reduces the chattering of the *dq*-frame currents signifcantly compared to the other two methods. Table [3](#page-9-1) is the quantitative comparison of motor speed overshoot, response time, and peak current under diferent control methods during the starting phase of the vehicle. From the data in Table [3](#page-9-1), it can be seen that MRAS-SODO has a faster tracking performance than PI and BSC. In addition, the chattering of motor speed,  $i_d$  and  $i_q$  under MRAS-SODO control is smaller than that of PI and



<span id="page-10-7"></span>**Fig. 14** Speed tracking control response of diferent controls

BSC. In addition, MRAS-SODO effectively suppresses the transient current at the initial moment.

When the load torque changes suddenly, it can be seen from the data comparing the performance in Table [4](#page-9-2) that MRAS-SODO can restore the PMSM system to a steady state faster compared to PI and BSC. In addition, the  $i_d$  and  $i_q$  in MRAS-SODO have the smallest transient overshoot when the load changes abruptly compared to PI and BSC.

Figure [10](#page-9-3) shows the curve of the input signal and output signal of the command flter. Selecting appropriate parameters  $\zeta$ <sub>i</sub> and  $\sigma$ <sub>ni</sub> can make the output signal accurately track the change of the input signal. When the speed changes step by step, the overshoot is reduced after passing through the command flter, so as to solve the problem of diferential expansion.

In order to verify the tracking performance of the online identifcation algorithm for parameter changes, the motor parameters are changed under constant speed and torque. After the parameter identifcation is stable, after the simulation time of 3s, stator resistance  $R_s$  and flux linkage  $\varphi_f$ should be increased, and stator inductance  $L<sub>s</sub>$  should be decreased, respectively. As shown in Figs. [11,](#page-9-4) [12](#page-9-5) and [13,](#page-9-6) after a short dynamic adjustment, the motor parameters can converge to the modifed parameter values, among them, the speed waveforms of the three controllers when the parameters change are shown in Fig. [14](#page-10-7). The identifcation error of stator resistance  $R<sub>s</sub>$  is 2.5 %, the identification error of stator inductance  $L<sub>s</sub>$  is 4.8 %, and the identification error of stator inductance  $L<sub>s</sub>$  is 2 %. This paper shows that the parameter identifcation used in this paper is highly accurate.

# <span id="page-10-6"></span>**5 Conclusion**

In this paper, we study the accuracy of speed tracking control of PMSM in electric vehicles through the use of MRAS and second-order disturbance observers and solve the problems related to parameter perturbation and antiinterference ability. First, a dynamic model for the PMSM drive system is established in the *dq*-frame, and we consider the unmodeled dynamics, time-varying parameters, and torque variations. Additionally, a step-by-step MRAS can also be implemented, and the speed of parameter adaptation is determined by Lyapunov stability theory, which can match the design parameters of the motor controller after the motor parameters have changed. Following this, a new second-order disturbance observer is designed in order to account for the mismatch disturbance caused by diferent road conditions and eliminate the initial peak value of the disturbance observer. On the basis of this data, the *d*-inner frame ring and *q*-frame controller are used to design a linear sliding surface, thus improving the robustness of the PMSM drive system. Further, the derivative of the virtual signal is approximated by an instruction flter, which solves the problem of complexity explosion. Finally, the stability of the controller is determined, as well as the performance of the proposed control strategy based on the simulation and realtime simulation results: electric vehicle variable speed and constant speed drive. In future work, the control scheme proposed in this paper will be validated using real-life PMSM experimental platforms.

**Funding** Funding was provided by China Scholarship Council (202106950045), Scientic research fund project of Nanjing Institute of Technology (JCYJ201817), Open Research Fund of Jiangsu Collaborative Innovation Center for Smart Distribution Network (XTCX201902)

# **References**

- <span id="page-10-0"></span>1. Wu Y, Ng A, Yu Z, Huang J, Meng K, Dong Z (2021) A review of evolutionary policy incentives for sustainable development of electric vehicles in China: strategic implications. Energy Policy 148B:111983
- <span id="page-10-1"></span>2. Park J, Jung S, Ha J (2018) Variable Time Step Control for Six-Step Operation in Surface-Mounted Permanent Magnet Machine Drives. Trans Power Electr 33(2):1501–1513
- <span id="page-10-2"></span>3. Dai Y, Ni S, Xu D, Zhang L, Yan X (2021) Disturbance-observer based prescribed-performance fuzzy sliding mode control for PMSM in electric vehicles. Eng Appl Artif Intell 104:103461
- <span id="page-10-3"></span>4. Yu J, Chen B, Yu H (2018) Neural networks-based command fltering control of nonlinear systems with uncertain disturbance. Information SciencesInformatics and Computer Science. Inf Sci 426:50–60
- <span id="page-10-4"></span>5. Yang J, Chen W-H, Li S, Guo L, Yan Y (2017) Disturbance/ uncertainty estimation and attenuation techniques in PMSM drives-a survey. IEEE Trans Industr Electron 64(4):3273–3285
- <span id="page-10-5"></span>6. Dai Y, Ni S,i Xu D, Zhang L, Yan X (Sept. 2021) Disturbanceobserver based prescribed-performance fuzzy sliding mode control for PMSM in electric vehicles. Eng Appl Artif Intell vol. 104
- 7. Eid BM, Rahim NA, Selvaraj J, El Khateb AH (2016) Control methods and objectives for electronically coupled distributed energy resources in microgrids: a review. IEEE Syst J 10(2):446–458
- <span id="page-11-0"></span>8. Jin H, Liu Z, Zhang H, Liu Y, Zhao J (2018) A dynamic parameter identifcation method for fexible joints based on adaptive control. IEEE/ASME Trans Mechatron 23(6):2896–2908
- <span id="page-11-1"></span>9. Shi Y, Sun K, Huang L, Li Y (2012) Online identifcation of permanent magnet fux based on extended Kalman flter for IPMSM drive with position sensorless control. IEEE Trans Industr Electron 59(11):4169–4178
- <span id="page-11-2"></span>10. Yousri D, Allam D, Eteiba MB (2019) Chaotic whale optimizer variants for parameters estimation of the chaotic behavior in permanent magnet synchronous motor. Appl Soft Comput 74:479–503
- <span id="page-11-3"></span>11. Dong D, Xu W, Xiao X, Liu Y (2021) Online magnetizing inductance identifcation strategy of linear induction motor based on second-order sliding-mode observer and MRAS. In: 2021 13th International symposium on linear drives for industry applications (LDIA)
- <span id="page-11-4"></span>12. Zhao L, Huang J, Liu H, Li B, Kong W (2014) Second-order sliding-mode observer with online parameter identifcation for sensorless induction motor drives. IEEE Trans Industr Electron 61(10):5280–5289
- <span id="page-11-5"></span>13. Liu X, Yu H, Yu J, Zhao L (2018) Combined speed and current terminal sliding mode control with nonlinear disturbance observer for PMSM drive. IEEE Access 6:29594–29601
- <span id="page-11-6"></span>14. Wang YW, Zhang WA, Yu L (2020) A linear active disturbance rejection control approach to position synchronization control for networked interconnected motion system. IEEE Trans Control Netw Syst 7(4):1746–1756
- <span id="page-11-7"></span>15. Apte A, Joshi VA, Mehta H, Walambe R (2020) Disturbanceobserver-based sensorless control of PMSM using integral state feedback controller. IEEE Trans Power Electron 35(6):6082–6090
- <span id="page-11-8"></span>16. Bayat F, Mobayen S, Javadi S (2016) Finite-time tracking control of nth-order chained-form non-holonomic systems in the presence of disturbances. ISA Trans 63:78–83
- <span id="page-11-9"></span>17. Wei X, Wu Z, Karimi H (2016) Disturbance observer-based disturbance attenuation control for a class of stochastic systems. Automatica 63:21–25
- <span id="page-11-13"></span>18. Xu D, Dai Y, Yang C, Yan X (2019) Adaptive fuzzy sliding mode command-fltered backstepping control for islanded PV microgrid with energy storage system. J Franklin Inst 356(4):1880–1898
- <span id="page-11-10"></span>19. Qu L, Qiao W, Qu L (2021) An extended-state-observer-based sliding-mode speed control for permanent-magnet synchronous motors. IEEE J Emerg Select Topics Power Electr 9(2):1605–1613
- <span id="page-11-11"></span>20. Cui K, Wang C, Gou L, An Z (2020) Analysis and design of current regulators for PMSM drives based on DRGA. IEEE Trans Transp Electr 6(2):659–667
- <span id="page-11-12"></span>21. Yang C, Ni S, Dai Y, Huang X, Zhang D (2020) Anti-disturbance fnite-time adaptive sliding mode backstepping control for pv inverter in master-slave-organized islanded microgrid. Energies, vol. 13
- 22. Wang X, Guo J, Tang SJ, Qi S (2019) Fixed-time disturbance observer based fxed-time back-stepping control for an air-breathing hypersonic vehicle. ISA Trans 88:233–245
- <span id="page-11-14"></span>23. Roshandel Tavana N, Dinavahi V (2015) A general framework for FPGA-based real-time emulation of electrical machines for HIL applications. IEEE Trans Industr Electron 62(4):2041–2053
- <span id="page-11-15"></span>24. Mojlish S, Erdogan N, Levine D, Davoudi A (2017) Review of hardware platforms for real-time simulation of electric machines. IEEE Trans Transp Electr 3(1):130–146
- <span id="page-11-16"></span>25. Edrington CS, Steurer M, Langston J, El-Mezyani T, Schoder K (2015) Role of power hardware in the Loop in modeling and simulation for experimentation in power and energy systems. Proc IEEE 103(12):2401–2409
- <span id="page-11-17"></span>26. Zhang L, Liu J, Qi W, Chen Q, Long R, Quan S (2019) A parallel modular computing approach to real-time simulation

of multiple fuel cells hybrid power system. Int J Energy Res 43(10):5266–5283

<span id="page-11-18"></span>27. Zhao L, Liu Z, Chen H (2011) Design of a nonlinear observer for vehicle velocity estimation and experiments. IEEE Trans Control Syst Technol 19(3):664–672

**Publisher's Note** Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.

Springer Nature or its licensor holds exclusive rights to this article under a publishing agreement with the author(s) or other rightsholder(s); author self-archiving of the accepted manuscript version of this article is solely governed by the terms of such publishing agreement and applicable law.

**Chengshun Yang** received the Ph.D. degree in College of Automation, Nanjing University of Aeronautics and Astronautics, Nanjing, China, in 2013. He is currently an associate professor of the school of electrical engineering, Nanjing Institute of Technology. He is mainly engaged in teaching and research in the feld of power transmission and distribution engineering and new technologies. His research interests include unmanned aerial vehicle inspection technology of transmission lines, state perception, grid-connected operation of distributed power generation, and advanced control methods.

**Tao Hua** is currently pursuing the MA.Eng degree in electrical engineering with the School of Electrical Engineering, Nanjing Institute of Technology, Nanjing, China. His research interests include nonlinear robust control, vehicle motor control, and micro-grids.

**Yuchen Dai** is currently pursuing the Ph.D. degree in traffic information engineering and control with the School of Automation, Wuhan University of Technology, Wuhan, China. He is also currently a Visiting Ph.D. student with the College of Design and Engineering, National University of Singapore, Singapore. He was an Electrical Engineer with State Grid Jinhua power supply company, Jinhua, China, from 2014 to 2016. His research interests include nonlinear robust control, multi-agent systems, vehicle motor control, renewable energy, and micro-grids.

**Xiaoning Huang** received the MA.Eng degree in power system and automation from the School of Electrical Engineering, Southeast University, China. He is currently a professor of the school of electric power of Nanjing Institute of Technology. He has long been committed to the scientifc research and teaching of power transmission and distribution engineering. His research direction is power system operation and control, power transmission and distribution equipment and power grid safety.

**Dongdong Zhang** was born in Xiangshui, Jiangsu Province, China in 1990. He received the B.Sc. and Ph.D. degree from Chongqing University, Chongqing, China in 2012 and 2017. He is the faculty of Nanjing Institute of Technology now. His research interests mainly include high voltage engineering, electric insulation and electric apparatus fault detection. He is the author or coauthor of over 20 technical papers.