**ORIGINAL PAPER**





# **A Development and Assessment of Variable-Incidence Angle Vortex Generator at Low Reynolds Number of ~ 5×104**

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Received: 4 July 2018 / Revised: 6 October 2018 / Accepted: 18 October 2018 / Published online: 13 November 2018 © The Korean Society for Aeronautical & Space Sciences and Springer Nature Singapore Pte Ltd. 2018

#### **Abstract**

The aerodynamic benefit for conventional vortex generator (VG) is often counterbalanced by the appearance of parasite drag. An immovable installation similar to a fixture also limited its application. To overcome those issues, this paper proposes a variable-incidence-angle vortex generator (VIVG). Counter-rotated miniature gears with a single rack-pinion system adjust the incidence angle of the VIVG, thereby precisely control mixing flux at boundary layer interface with minimizing the parasite drag. The variable incidence angle of the VIVG was then examined to evaluate the applicability of the VIVG at low Reynolds number. The VIVG was mounted on a NACA 0015 airfoil, and a low-turbulence blowing type wind tunnel was employed. We found that the VIVG effectively eliminated laminar separation bubbles, and suppressed separation at Reynolds number of  $5.4 \times 10^4$ ; excessive lift production at low Reynolds number became similar to a theoretical value of potential flow  $(C_L = 2\pi\alpha)$ . It was also found that the VIVG can reduce the drag in the pre-stall region at the low Re with small incidence angles, providing a noticeable increment of the lift-to-drag ratio. The large incidence angle of VIVG was also useful both to extend the stall point and to produce higher lift force with reasonable efficiency. These clearly indicate that the VIVG is applicable for performance improvement of aerodynamic devices operated in low Reynolds number flow fields.

**Keywords** Flow control · Vane-type vortex generator · Variable-incidence-angle vortex generator · Low Reynolds number flow · Laminar flow separation

## **1 Introduction**

Various aerodynamic devices in low Reynolds number flow fields, such as small-scale wind turbines [\[1\]](#page-5-0), always suffer a certain drawback due to a scale effect [\[2–](#page-5-1)[4\]](#page-5-2). This drawback commonly stems from a laminar-dominant flow field with a lack of inertia, which is insufficient to overcome the adverse pressure gradient over the maximum thickness of the aerodynamic devices. In an airfoil, for instance, stall appears at much lower angles of attack, and lift is substantially reduced in the pre-stall region  $[5]$ . Intricate events in the boundary layer, such as laminar separation, transition in free shear layer, reattachment, laminar separation bubbles (LSB), and leading-edge bubbles (LEB) are other features accelerating the reduction of the aerodynamic performance  $[6, 7]$  $[6, 7]$  $[6, 7]$ .

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Among these, LSB is known as the primary source degrading the overall aerodynamic performance; LSB commonly results in undesired fluctuation and discontinuity in the aerodynamic lift, accompanied with substantial drag [\[4\]](#page-5-2). Highly sensitive characteristics of the LSB depending on both the angle of attack and the Reynolds number also create an oscillating force with back-and-forth movement of the LSB in the pre-stall region, eventually destabilizing the negative pressure distribution on the suction side of aerodynamic devices with dynamic transition and separation points  $[8-10]$  $[8-10]$ .

Several active flow control devices such as excitation actuators  $[11-13]$  $[11-13]$ , suction and blowing actuators  $[14-16]$  $[14-16]$ , and synthetic jet actuators [\[17,](#page-6-5) [18\]](#page-6-6) have been investigated to suppress the flow separation and thereby improve the aerodynamic performances. Micro driving instruments such as piezoceramic actuators [\[19\]](#page-6-7) were inserted in active flow control devices to produce massive flux, which induces strong mixing at the boundary layer interfaces, thereby supplying additional energy to the boundary layer in a straightforward way. Therefore, these give us reliable improvement of aerodynamic performance with arbitrary control of the volume

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of fluid, mixing strength, and excitation level for each circumstance. However, delicate mechanical parts requiring additional energy resources to operate, which degrade the overall efficiency, remain the biggest weakness for the application of such devices.

Use of vortex generators (VGs) could be an alternate way to control boundary layer separation. These devices are usually only constructed in simple shapes such as zig-zag trips, wedges, wishbones, and wheelers  $[20-23]$  $[20-23]$ , and have been widely used to control the flow separation in various aerodynamic devices such as thick airfoil sections near the hubs of large wind turbines [\[22\]](#page-6-10). These devices also guarantee adequate flow control capability to prevent the flow separation [\[24,](#page-6-11) [25\]](#page-6-12). The use of VGs, however, requires an in-depth consideration of device shape and dimensions, because it permanently accompanies with a parasite drag, which degrades overall aerodynamic performance. Griffin [\[26\]](#page-6-13), for example, tested the several VG configurations on a two-dimensional section of a wind turbine blade and showed that the VGs could increase an annual energy production up to 10%, but always gives rise to a substantial dynamic load. The recent study on the effect of VGs [\[27\]](#page-6-14) further showed that the VGs could offset the performance degradation due to a surface contamination, but did not bring out better aerodynamic performance than the clean case.

The previous results showing an insufficient performance of the VGs may stem from non-optimized adoption in the initial design stage. The shapes and dimensions are more significant in low Reynolds number flow fields, in which intricate flow structures become dominant [\[3\]](#page-5-7). In particular, the incidence angle between two vanes of VGs, which is the preliminary parameter determining the strength of the counter-rotating vortex pair, should be investigated in advance to achieve higher efficiency without losing the overall aerodynamic performance of aerodynamic devices in low Reynolds number flow fields.

In this paper, we propose a variable-incidence-angle vortex generator (VIVG). This consists of counter-rotated miniature gears with a single rack-pinion system, which can be installed under aerodynamic devices, adjust the arbitrary incidence angle of vanes with minimizing the parasite drag for each circumstance. We then evaluated the effect of the incidence angle of VIVG on the aerodynamic characteristics of a NACA 0015 airfoil at Reynolds number of  $5.4 \times 10^4$ . For a wide range of incidence angles and angles of attack, a low turbulence blowing type wind tunnel and a balance system were employed to measure the lift and drag of the airfoil with the VIVG. It was found that the VIVG is effective at suppressing the laminar separation and eliminating the LSB. It was also found that the VIVG can provide better efficiency in most pre-stall regions with a small incidence angle. Large incidence angle was also useful, both to extend the stall point and to produce maximum lift with reasonable efficiency. These all imply that the VIVG can provide better aerodynamic performance at low Reynolds number.

#### **2 Experimental Setup and Procedure**

Lin [\[24\]](#page-6-11) and Ashill et al. [\[25\]](#page-6-12) collected literature dealing with the flow control performance of various shapes of VGs and other flow control devices; they reported that a vane-type VG had the most excellent flow control performance. This vanetype VG is composed of a pair of bisymmetrical fins, like mirror images of each other, with a certain incidence angle to induce a counter-rotating vortex pair.

Figure [1](#page-2-0) shows the shape and dimensions of the VIVG installed on a NACA 0015 airfoil. The airfoil had a chord length *c* of 150 mm and a span of 294 mm. This airfoil was fabricated by a 3d printer with poly lactic acid filament. In order to smooth out the surface of the airfoil, polyester putty and sand paper with grit levels from P100 to P2000 were used.

The VIVG in this paper was composed of fifteen pairs of vanes and was installed at 0.2*c* from the leading edge. Each vane of the VIVG had a triangular shape with height *h* and length  $l = 2$  *h*, where  $h = 0.02c$ . The distance between fins, *s*, and the spatial interval of the pair of vanes, *z*, are 2.5 *h* and 6.0 *h*, respectively. These vanes were mounted on the shaft of each counter-rotating miniature gear. Here, two bearings supporting each shaft prevented the misalignment of the fins. Each pair of vanes had one additional pinion gear, which meshed with a rack gear; using the single linear input on the rack gear, the incidence angles of the entire set of vanes were automatically adjusted.

Figure [2](#page-2-1) shows the test setup in this study. A blowing type wind-tunnel at KAIST, which had a test section of 1000 mm  $(L) \times 300$  mm (W)  $\times 300$  mm (H) was employed. The maximum speed of the freestream is 30 m/s, with a turbulence intensity less than 0.8%.

To accurately adjust the angle of attack, the airfoil was mounted on a stepper motor, which had a resolution of 0.005° (A200K-M599-G7.2, Autonics Co.). Two single-axis bending beam type loadcells were installed between the airfoil and the stepper motor to measure the lift and drag. Each loadcell (OBU-1, Bongshin) had a measurement range of  $\pm$  1 kgf and resolution of 0.02% at maximum load, and were connected to signal amplifiers (DN AM310, Dacell) and to a DAQ system (PXIe-6361, NI) for data acquisition. To avoid unpredictable effects from misalignment and/or backlashes in the apparatus, as shown in Fig. [2,](#page-2-1) a calibration matrix for the loadcells was determined under mounted condition; these showed identical values to those given by the manufacturer.

The freestream speed was fixed at 5.0 m/s, corresponding to a Reynolds number of  $5.4 \times 10^4$ . The aerodynamic forces were measured in a range of angle of attack of − 10 to 20° at



<span id="page-2-1"></span><span id="page-2-0"></span>**Fig. 1** Schematic of the VIVG installed on NACA 0015 airfoil

**Fig. 2** Experimental setup



intervals of 0.5° (a total of 61 angles of attack); the incidence angles of the VIVG started from 0 to 38.2° at intervals of 7.65° (a total of 6 incidence angles); these were controlled by a high-precision servo motor (XH-430-W210R, Robotis®) mounted in the airfoil. The data in each case was collected for 30 s with a sampling frequency of 1 kHz. An in-house code written in LabVIEW™ was used to control the stepper motor and measurement process; this automatically shifted the angle of attack to the next sequence with fixed spatial and temporal intervals (0.5° and 30 s) for each designated incidence angle. 5000 data samples were extracted from the data for white noise reduction, and were calibrated to extract the aerodynamic forces. Each force was decomposed to lift and drag with respect to angles of attack, and normalized to the aerodynamic coefficients using Eqs. [\(1\)](#page-2-2) and [\(2\)](#page-2-3),

<span id="page-2-2"></span>
$$
C_{\rm L} = \frac{2L}{\rho U_{\infty}^2 S} = \frac{2(F_{\rm X} \sin \alpha + F_{\rm Y} \cos \alpha)}{\rho U_{\infty}^2 S},\tag{1}
$$

<span id="page-2-3"></span>
$$
C_{\rm D} = \frac{2D}{\rho U_{\infty}^2 S} = \frac{2(F_X \cos \alpha - F_Y \sin \alpha)}{\rho U_{\infty}^2 S}.
$$
 (2)

<span id="page-3-0"></span>

Type-A measurement uncertainty was evaluated [\[28\]](#page-6-15). The resolution of the stepper motor of  $\pm 0.005^{\circ}$  resulted in a value of  $\pm 0.0167\%$  of angle of attack. A change in temperature from 6.55 to 7.75  $\degree$ C also gave us the density of  $1.260 \pm 0.005$  kg/m<sup>3</sup> (0.397%). The freestream velocity had a range of  $5.0 \pm 0.05$  m/s ( $\pm 1.00\%$ ). Including the resolution of the loadcells given by the manufacturer  $(\pm 0.002 \text{ N}; 0.375\%)$ , overall uncertainty level of each coefficient became  $\pm 2.18\%$  of the maximum lift.

Figure [3a](#page-3-0) and b show ensemble averages of the lift coefficient  $C_{L}$  for the selected angles of attack  $\alpha$  and their standard deviations SD for the airfoil without the VIVG (clean airfoil). Here,  $\Delta C_L$  denotes the ensemble-averaged  $C_L$  subtracted from the mean values in each  $\alpha$ , as shown in Eq. [\(3\)](#page-3-1),

$$
\Delta C_{\rm L} = C_{\rm L} - \frac{\sum_{i=1}^{N} C_{\rm L, i}}{N}.
$$
\n(3)

At  $\alpha < 6^{\circ}$ , the  $\Delta C_{\rm L}$  did not need a large number of samples to converge. The  $\Delta C_L$  at  $\alpha > 6^\circ$  required relatively more samples due to both the separation and the turbulent wake, but 5000 samples still seemed to be sufficient to converge. This implies that white noise during measurements was properly isolated from the results, and SD can inform us of the perturbation and/or the turbulent characteristics, as shown in Fig. [3b](#page-3-0). We found that the overall aerodynamic characteristics could be briefly classified into three regions with respect to the level of SD; (i) fully laminar flow with small  $\alpha$  $(0 < \alpha < 2.0)$ , (ii) intermediate region that contains relatively large-scale LSB and/or LEB  $(2.0 < \alpha < 7.5)$ , and iii) fully separated flow with strong fluctuation ( $\alpha$  > 7.5). These results are clearly in line with the previous study that demonstrated five distinctive flow structures for similar Reynolds number flow fields  $[6]$ .

To validate both our results and the measurement system, we further compared the  $C_{\rm L}$  to that of the previous study [\[6\]](#page-5-4).

Figure [4a](#page-4-0) shows two  $C<sub>L</sub>$  curves obtained by two different wind-tunnel facilities. Here, the VIVG were disassembled from the surface for a fair comparison (clean case). In the pre-stall region  $(0 < \alpha < 7.5^{\circ})$ , the two curves show excellent agreement. Both curves exhibit two features in common; excessive lift production beyond that predicted by the potential flow theory  $(C_L = 2\pi\alpha)$  at  $0 < \alpha < 3.5^{\circ}$ , and a degraded growth rate at  $3.5 < \alpha < 7.5^{\circ}$ . These are typical flow characteristics at low Reynolds number [\[6,](#page-5-4) [9,](#page-5-8) [10\]](#page-6-0); the existence of LSB and a barely separated boundary layer over the LSB produced the excessive lift at lower  $\alpha$ , and early-starting separation before the stall angle degraded the growth rate in the *C*<sup>L</sup> (refer to Figs. [4b](#page-4-0)ii, iii for the flow structures in detail). In the post-stall region ( $\alpha$  > 7.5°), however, the two curves showed comparable disagreement. The *C*<sup>L</sup> in this study had a relatively gentle arc at the stall, and maintained a *C*<sup>L</sup> level after the stall higher than that of the previous study [\[6\]](#page-5-4). Huang and Lee [\[6\]](#page-5-4) reported that a strong turbulent intensity in the freestream resulted in the higher  $C_{L}$  values after the stall, and *C*<sup>L</sup> dramatically increased when the turbulent intensity reached 0.4%. Therefore, it can be concluded that the higher turbulent intensity of  $\sim 0.8\%$  in this study was the main source maintaining the strong aerodynamic lift in the post-stall region. Such intricate aerodynamic characteristics was also an appropriate test bed to evaluate the VIVG developed in this study.

## <span id="page-3-1"></span>**3 Results and Discussion**

Figure [5](#page-4-1) displays the  $C_{L}-\alpha$  curves for the selected incidence angles  $β$ . It was found that regardless of the level of  $β$ , the lift increment in the clean airfoil was nearly eliminated by the VIVG. All curves with VIVG, therefore, obeyed the theoretical level of *C*<sup>L</sup> (dashed line), at least in the range of  $0 < \alpha < 3.5^{\circ}$ . The other increment due to LEB at  $3.5 < \alpha < 7.5^{\circ}$ also vanished (refer to Fig. [4b](#page-4-0)iii). Overall tendencies of *C*<sup>L</sup>



<span id="page-4-0"></span>**Fig. 4** Comparison of *C*<sup>L</sup> with the previous study [\[6\]](#page-5-4); Fig. [4b](#page-4-0) was reproduced by the authors



<span id="page-4-1"></span>**Fig. 5**  $C_{\text{L}}$  depending on  $\beta$ 

with VIVG, therefore, showed monotonic increments in the pre-stall region. Note that the LSB was deeply dependent on the turbulent intensity [\[6\]](#page-5-4). This implies that using the VIVG can give us robust lift production for various levels of atmospheric turbulence. The linear growth of  $C_{\text{L}}$  in the prestall region also implies easier prediction via an aerodynamic model.

Figure [5](#page-4-1) also shows that using sharp  $\beta$  postponed the stall, thereby producing higher lift at higher  $\alpha$ . In the case of  $\beta$  = 38.3°, for example,  $C_L$  had a 14.3% higher value ( $C_L$ )  $\sim$  0.75 at  $\alpha$  = 10°) than that of the VIVG with  $\beta$  = 0° ( $C_L \sim$  0.66  $\alpha = 8.5^{\circ}$ );  $C_L$  had an 8.3% higher value than that of the clean airfoil case ( $C_L \sim 0.70 \alpha = 9^\circ$ ). This clearly indicates that the VIVG was also useful to suppress turbulent separation in low Reynolds number flow fields (refer to Fig. [4b](#page-4-0)v for the flow structure in detail).

<span id="page-4-2"></span>**Fig. 6**  $C_D$  depending on  $\beta$ 

The same influences of the VIVG were found in the drag coefficients  $C_D$ . Figure [6](#page-4-2) shows  $C_D$  with respect to  $\beta$ . One noteworthy feature was the drag reductions at  $0 < \alpha < 8.0^{\circ}$ , with small  $\beta$  values of 7.7 and 15.3° (Fig. [4i](#page-4-0)). The VIVG in this range of  $\alpha$  attenuated  $C_D$  to ~ 11.3%. This informs us that the presence of LSB at low Reynolds number could induce considerable drag, which is much stronger than that of the parasite drag of each vane of the VIVG. This also clearly indicates that eliminating LSB with adequate  $\beta$ , which can be achieved by the VIVG, can significantly reduce aerodynamic drag in the pre-stall region.

The VIVG also extended the pre-stall region, similar to the case of  $C_L$ . As shown in Fig. [6i](#page-4-2)i, from  $\alpha = 8.5^{\circ}$ , the stall point was extended to  $\alpha = 10^{\circ}$  with  $\beta = 38.3^{\circ}$ . This shows that the VIVG with an appropriate  $\beta$  can enhance the range of operation of aerodynamic devices at low Reynolds number.

Figure [7](#page-5-9) shows the lift-to-drag ratio L/D. We found that the VIVG is able to maintain the overall efficiency with small  $\beta$  at  $0 < \alpha < 2.5^{\circ}$ , it even eliminated LSB and reduced the lift



<span id="page-5-9"></span>**Fig. 7** Lift-to-drag ratios depending on β

augmentation (refer to Fig. [4b](#page-4-0)ii for the LSB). This informs us that LSB is always accompanied by heavy drag even it can augment the lift, and using the VIVG with adequate  $\beta$  to eliminate LSB can be a good option to preserve the efficiency. It was also found that small  $\beta$  values of 7.7 and 15.3° elevated L/D in most ranges of  $\alpha$ , from 2.5° to the stall angle. At  $\alpha = 6^{\circ}$ , for example, L/D with  $\beta = 15.3$  reached 11.96, which is a 12.2% higher efficiency than that of the clean case (*L*/*D*  $=$  10.66). This clearly indicates that adopting the VIVG is highly recommended for aerodynamic devices operating at low Reynolds number. In particular, the VIVG would be very suitable for energy harvesting systems such as wind turbines [\[1,](#page-5-0) [22\]](#page-6-10).

Using the VIVG with high  $\beta$  also guaranteed better efficiency near the stall angle. The L/D of 9.75 with  $\beta = 38.3^\circ$  at the stall angle was almost twice the value of the clean airfoil case. Although this *L*/*D* was only 79.5% of the maximum value of L/D (at  $\beta = 15.3^\circ$  and  $\alpha = 7.5^\circ$ ), it is still useful when heavy aerodynamic lift is necessary.

Excessive mixing flux of the vortex pair generated by the active flow control devices frequently reduces the overall aerodynamic performance due to the growth of parasite drag [\[26,](#page-6-13) [27,](#page-6-14) [29,](#page-6-16) [30\]](#page-6-17). The *L*/*D* in this study indicates that the variable incidence angles are sufficient to obtain better aerodynamic performance without losing efficiency for the various circumstance. In addition, the VIVG developed in this study would be great tools to control low Reynolds number flow fields.

## **4 Conclusion**

In this paper, we propose the VIVG, which provide adjustable incidence angle of vanes thereby minimizing the parasite drag, which permanently appears in the conventional VGs. We then examined incidence angles of the VIVG and its flow control performance in low Reynolds number flow fields of  $5.4 \times 10^4$ . The NACA 0015 airfoil was employed, and the clean airfoil was also examined for comparison. The results from the clean airfoil clearly show intricate aerodynamic characteristics such as excessive  $C_{\text{L}}$  and lower growth rate in the pre-stall region due to laminar separation and ensuing LSB/LEB. These results were in an excellent agreement with the previous study, which showed intricate boundarylayer-events depending on the angle of attack. We found that using the VIVG with adequate incidence angles is highly recommended for performance improvement of aerodynamic devices, which operate in low Reynolds number flow fields. The VIVG was capable of stabilizing  $C_{\text{L}}$  in the pre-stall region, so that it became similar to a theoretical value of potential flow. The VIVG also effectively eliminated LSB and suppressed separation. The VIVG with small  $\beta$  significantly reduced the drag in most pre-stall regions; this resulted in a substantial improvement of L/D. The VIVG with large  $\beta$  was also useful to extend the stall point, thereby achieving both maximum lift and moderate efficiency.

**Acknowledgements** This work was supported by the New and Renewable Energy Core Technology Program of the Korea Institute of Energy Technology Evaluation and Planning (KETEP), granted financial resources by the Ministry of Trade, Industry and Energy, Republic of Korea. (No. 20153030023880).

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