

# Metal oxides for thermoelectric power generation and beyond

Yining Feng<sup>1</sup> · Xiaodong Jiang<sup>1</sup> · Ehsan Ghafari<sup>1</sup> · Bahadir Kucukgok<sup>1,2</sup> ·  
Chaoyi Zhang<sup>1</sup> · Ian Ferguson<sup>3</sup> · Na Lu<sup>1,2,4</sup>

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**Abstract** Metal oxides are widely used in many applications such as thermoelectric, solar cells, sensors, transistors, and optoelectronic devices due to their outstanding mechanical, chemical, electrical, and optical properties. For instance, their high Seebeck coefficient, high thermal stability, and earth abundancy make them suitable for thermoelectric power generation, particularly at a high-temperature regime. In this article, we review the recent advances of developing high electrical properties of metal oxides and their applications in thermoelectric, solar cells, sensors, and other optoelectronic devices. The materials examined include both narrow-band-gap (e.g.,  $\text{Na}_x\text{CoO}_2$ ,  $\text{Ca}_3\text{Co}_4\text{O}_9$ ,  $\text{BiCuSeO}$ ,  $\text{CaMnO}_3$ ,  $\text{SrTiO}_3$ ) and wide-band-gap materials (e.g., ZnO-based,  $\text{SnO}_2$ -based,  $\text{In}_2\text{O}_3$ -based). Unlike previous review articles, the focus of this study is on identifying an effective doping mechanism of different metal oxides to reach a high power factor. Effective dopants and doping strategies to achieve high carrier concentration and high electrical conductivities are highlighted in this review to enable the advanced applications of metal oxides in thermoelectric power generation and beyond.

**Keywords** Oxides · Thermoelectric · Power factor · Solar cells · Optoelectronic power generation

## 1 Introduction

Thermoelectric (TE) materials have the ability to directly convert heat into electricity for power generation via the Seebeck effect [1, 2]. It can play a crucial role in renewable energy production since 60% of energy produced worldwide is waste as the form of heat. Additionally, as a solid-state device, TE technology has many attractive features such as high reliability, environmental friendliness, and no moving parts [3].

Despite recent advances in TE research, the potential impact of TE technology for power generations is hindered by the heavy usage of toxic, rare, and expensive (e.g., Te and Se) elements and their low power output. For instance, there are only three major TE material systems commercially available for from low- to high-temperature regimes including  $\text{Bi}_2\text{Te}_3$  (300–500 K) [4],  $\text{PbTe}$  (500–600 K) [5], and  $\text{SiGe}$  (600–800 K) [6]. Their applications, particularly Te-based materials, are largely restricted by the toxicity, limited element resources, and material degradation at high temperatures [7, 8].

Metal oxides, on the other hand, are promising candidates to circumvent these challenges due to their earth abundancy, low cost, non-toxicity, and high thermal stability [9–11]. More importantly, their electronic properties can be tuned from insulator behavior to metallic behavior by manipulating their crystal structures, chemical compositions, and doping concentrations [12, 13]. These unique material properties open an exciting opportunity to obtain high power output in metal oxides. In fact, for TE power generation applications, a material with high power factor is even more important than having a high efficiency, since most waste heat sources are free (e.g., waste heat from car exhaust, gas engine) and unlimited (e.g.,

✉ Na Lu  
luna@purdue.edu

<sup>1</sup> Lyles School of Civil Engineering, Sustainable Materials and Renewable Technology (SMART) Laboratory, Purdue University, West Lafayette, IN, USA

<sup>2</sup> Birk Nanotechnology Center, Purdue University, West Lafayette, IN, USA

<sup>3</sup> College of Engineering and Computing, Missouri University of Science and Technology, Rolla, MO, USA

<sup>4</sup> School of Materials Engineering, Purdue University, West Lafayette, IN, USA

solar radiations) [14]. To this end, the focus of this review article is on examining the metal oxide potentials for TE power generation with an emphasis on materials with high power factor. Effective doping strategies in achieving high power factor are highlighted for various metal oxides, particularly,  $\text{Na}_x\text{CoO}_2$  [15],  $\text{Ca}_3\text{Co}_4\text{O}_9$  [16],  $\text{BiCuSeO}$  [17],  $\text{CaMnO}_3$  [18],  $\text{SrTiO}_3$  [19], ZnO-based [20],  $\text{SnO}_2$ -based [21], and  $\text{In}_2\text{O}_3$ -based [22] alloys. More broadly, recent advancement of metal oxides for potential commercial applications in thermal- and electrical-related fields is summarized, which includes TE power generators, solar cells, and sensors.

## 2 Fundamental physics of thermoelectric metal oxides

The quality of materials for TE application is described by a dimensionless parameter  $ZT$  [7], which is defined as the following:

$$ZT = \frac{S^2\sigma}{\kappa} T \tag{1}$$

where  $S$  is the Seebeck coefficient,  $\sigma$  is the electrical conductivity, and  $\kappa$  is the thermal conductivity. In physics,  $\kappa$  consists of the electronic part ( $\kappa_e$ , due to carrier transport) and lattice part ( $\kappa_l$ , due to phonon transport). The term  $S^2\sigma$  is called the power factor (PF). A high PF indicates that a TE power generator can achieve a high power output.

Seebeck coefficient ( $S$ , in V/K) is an intrinsic material property, which measures the thermoelectric voltage induced in response to a temperature difference across the material.  $S$  represents the energy difference between the averaged charge carrier energy versus the Fermi energy. It can be expressed as the following:

$$S = \left( \frac{k_B}{-q} \right) \left( \frac{E_c - E_F}{k_B T} + \frac{\Delta_n}{k_B T} \right) \tag{2}$$

where  $E_F$  is the Fermi level, in which the dependence on the temperature ( $T$ ) and the Boltzmann constant ( $k_B$ ) is made explicit. For semiconductors, the Seebeck value can be negative (electron conduction) or positive value (hole conduction); therefore, the absolute value is more important. For doped semiconductors, the relationship between the Seebeck coefficient and carrier concentration can be expressed as the following:

$$S = \frac{8\pi^2 k_B^2}{3eh^2} m^* T \left( \frac{\pi}{3n} \right)^{2/3} \tag{3}$$

where  $k_B$  is the Boltzmann constant,  $e$  is the carrier charge,  $h$  is Planck's constant,  $m^*$  is the effective mass of the charger carrier, and  $n$  is the carrier concentration. As can be seen, lower

carrier concentration is desirable for materials to reach high Seebeck coefficient.

Electrical conductivity ( $\sigma$ ) describes the ease of conducting charge carrier transport of a material, which is defined as:

$$\sigma = ne\mu \tag{4}$$

where  $n$  is the carrier concentration,  $e$  is the carrier charge, and  $\mu$  is the mobility. To reach high electrical conductivity, a high carrier concentration is desirable; however, it often degenerates the Seebeck coefficient of materials as governed by Eq. (3). Therefore, an optimized carrier concentration of TE materials is often found at  $10^{19}$ – $10^{21}/\text{cm}^3$  [23]. The electrical conductivity of ideal TE materials is usually on the order of  $10^3$  (S/cm); however, the electrical conductivity of metal oxides is often lower, on the order of  $10$ – $10^2$  (S/cm). Thus, the investigation of effective doping mechanism on improving electrical conductivity without degenerating the Seebeck coefficient is crucial to enable their applications in TE power generation and related fields.

Thermal conductivity ( $\kappa$ ), on the other hand, is the parameter that describes how efficiently a material can conduct heat. In the case of semiconductors, the total thermal conductivity ( $\kappa_T$ ) consists of contributions from both electron and phonon transports, defined as the following:

$$\kappa_T = \kappa_e + \kappa_l \tag{5}$$

where  $\kappa_e$  and  $\kappa_l$  are, respectively, the electron and lattice thermal conductivities.  $\kappa_l$  is known as the most important mechanism for heat conduction in semiconductors at temperatures close to room temperature, which normally accounts for 90% contributions in wide-band-gap materials.

For good TE materials, the typical value of thermal conductivity is  $\kappa_T < 2$  W/mK [24]. Low thermal conductivity can be seen intuitively as an important parameter to maintain a certain temperature gradient across the junctions, which is essential for reaching high  $ZT$  in a material system [25]. Otherwise, the temperature gradient would quickly turn into equilibrium and cancel the materials TE effect. Therefore, recent efforts in TE materials research have been heavily focused on reducing thermal conductivity to achieve high  $ZT$  using various strategies, such as nano-structuring, phonon rattling, and band structuring as reported in previous studies [26–28]. To this end, most previous review articles focus on examining various mechanisms to achieve low thermal conductivity of materials. Very few literatures have discussed mechanisms to reach high power output of TE materials [29], and none of them focused on metal oxides.

Unlike previous literatures, we have systematically examined effective strategies to achieve high power output for potential applications in TE power generation. Much attention is paid to examining the effective dopants of various metal oxides to achieve high electrical conductivity without degrading

the Seebeck value or vice versa. As such, this review article will pave the road to the development of cost-effective, earth-abundant, and high-performance metal oxides for TE power generation and other thermal-electrical-related applications.

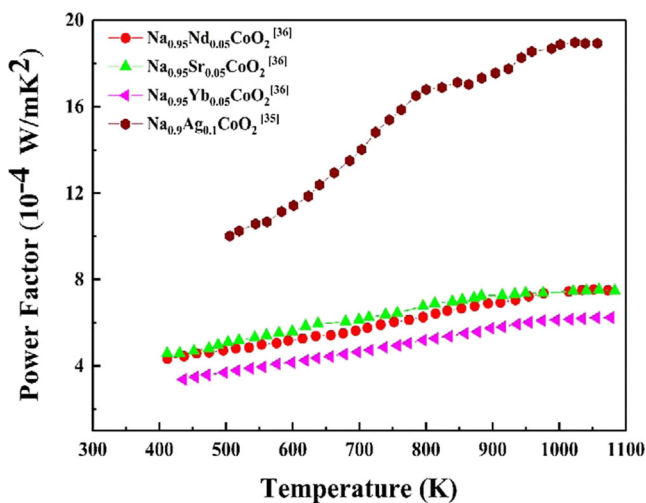
### 3 TE properties of metal oxides

#### 3.1 Narrow band gap

##### 3.1.1 $\text{Na}_x\text{CoO}_2$

$\text{Na}_x\text{CoO}_2$  is composed of the alternating stacks of sodium-ion ( $\text{Na}^+$ ) plane and  $\text{CoO}_2$  plane along with the  $c$ -axis, with a hexagonal layered crystal structure. Phonon and electron transports follow different paths in this structure. The electrons/holes are transported by passing through the  $\text{CdI}_2$ -type  $\text{CoO}_2$  layer for  $p$ -type electronic conduction, while the disordered charge-balancing  $\text{Na}^+$  layer is providing the path for phonons. The materials with this kind of layered structure are so-called “phonon glass electronic crystals,” which often show high electrical conductivity with low thermal conductivity [30], an ideal material property for thermoelectric applications. Therefore, the  $p$ -type alkali cobalt oxide-based compounds have been recognized as the most promising oxide TE materials [16, 31, 32]. Additionally, the polycrystalline  $\text{Na}_{0.85}\text{CoO}_2$  was reported to exhibit PF as high as  $14 \times 10^{-4} \text{ W/mK}^2$  at 300 K [15, 33]. The quite high PF values of either single or polycrystalline  $\text{Na}_x\text{CoO}_2$  indicate its great potential for TE power generation.

The TE properties of polycrystalline  $\text{Na}_x\text{CoO}_2$  have been widely investigated with different dopants and doping level of  $\text{Na}_x\text{CoO}_2$ . The effects of different metal dopants on the PF values of  $\text{Na}_x\text{CoO}_2$  are shown in Fig. 1. It was found that



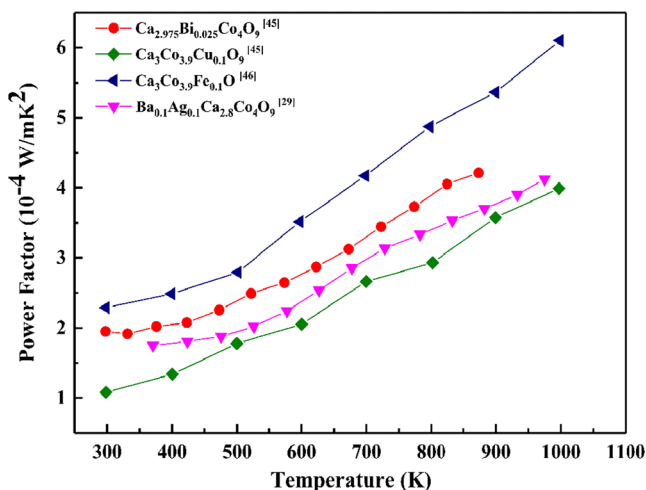
**Fig. 1** Power factor values of  $\text{Na}_x\text{CoO}_2$  with different dopants as a function of temperature

silver (Ag) doping is the most effective because it can improve the electrical conductivity and the Seebeck coefficient of  $\text{Na}_x\text{CoO}_2$  simultaneously, resulting in an enhanced PF value. Ag, as a metal-phase dopant, can obviously increase the electrical conductivity, but the mechanism of Ag doping enhancing the Seebeck value is still unclear. It could be caused by the uniform Ag doping in the samples or the electron-electron correlation [34]. With 10% Ag doping,  $\text{Na}_x\text{CoO}_2$  achieved the PF as high as  $18.92 \times 10^{-4} \text{ W/mK}^2$  at  $\sim 1100 \text{ K}$  with the carrier density of  $\sim 10^{21}/\text{cm}^3$  [35]. Compared with un-doped  $\text{NaCoO}_2$ , other dopants (Y, Nd, Sr, Sm) have little effects on improving PF values [36], and some dopants (Ni, Yb) even have negative effects [36, 37]. Because of the interdependent relations between the Seebeck coefficient and electrical conductivity, these dopants often improve one while they degrade the other. In contrast, doping transition metal elements turn out to be more effective in improving the PF of  $\text{Na}_x\text{CoO}_2$  composites.

##### 3.1.2 $\text{Ca}_3\text{Co}_4\text{O}_9$

$\text{Ca}_3\text{Co}_4\text{O}_9$  is another promising  $p$ -type TE material due to its high Seebeck coefficient and electrical conductivity [38–40]. The crystal structure of  $\text{Ca}_3\text{Co}_4\text{O}_9$  is similar to  $\text{Na}_x\text{CoO}_2$ , which is stacked by the  $\text{CdI}_2$ -type  $\text{CoO}_2$  layer and  $\text{Ca}_2\text{CoO}_3$  layer (rock salt-type structure) alternatively along the  $c$ -axis. For  $\text{Ca}_3\text{Co}_4\text{O}_9$ , the  $\text{CoO}_2$  planes of  $\text{Ca}_3\text{Co}_4\text{O}_9$  are mainly responsible for electrical conduction while the interlayers ( $\text{Ca}_2\text{CoO}_3$ ) between the  $\text{CoO}_2$  planes transfer the heat by phonons. The un-doped polycrystalline  $\text{Ca}_3\text{Co}_4\text{O}_9$  shows the Seebeck coefficient, electrical conductivity, and PF of  $150 \mu\text{V/K}$ ,  $80 \text{ S/cm}$ , and  $1.5 \times 10^{-4} \text{ W/mK}^2$ , respectively, at room temperature [41]. It was reported that doping noble metals, such as Ag, at the Ca cationic atom site can simultaneously increase the Seebeck coefficient and electrical transport properties, thus resulting in an enhanced PF [42]. This is mainly due to the substitution of  $\text{Ag}^+$  for  $\text{Ca}^{2+}$  in  $\text{Ca}_3-x\text{Ag}_x\text{Co}_4\text{O}_9$  ( $0 < x < 0.3$ ) which results in more improvement for the Fermi-level  $E_F$  than that for the valence band energy  $E_V$  of the crystal system [43]. For thermoelectric materials, the Seebeck coefficient is proportional to  $E_F - E_V$ . Therefore, it can be concluded that Ag doping in  $\text{Ca}_3\text{Co}_4\text{O}_9$  enhances the Seebeck coefficient. Although the PF value of  $\text{Na}_x\text{CoO}_2$  is much larger than that of  $\text{Ca}_3\text{Co}_4\text{O}_9$  at 300 K,  $\text{Ca}_3\text{Co}_4\text{O}_9$  is being more widely used in TE applications because of its high stability on compositional changes [44].

The doping effects of different transition metal (TM) elements on the PF of  $\text{Ca}_3\text{Co}_4\text{O}_9$  are shown in Fig. 2. With the temperature increasing from 300 to 1000 K, the PF of the polycrystalline  $\text{Ca}_3\text{Co}_4\text{O}_9$  with different dopants increased [29, 45–47]. It can be found that the substitution of transition elements (Fe, Bi, Mn, Ba, Ga) for Ca or Co has a positive effect on the PF improvement of  $\text{Ca}_3\text{Co}_4\text{O}_9$ . Fe is the most



**Fig. 2** Power factor values of  $\text{Ca}_3\text{Co}_4\text{O}_9$  doped with the transition metal elements as a function of temperature

effective dopant which has drastically increased the PF of  $\text{Ca}_3\text{Co}_4\text{O}_9$  from  $2.3 \times 10^{-4}$  to  $6.10 \times 10^{-4}$   $\text{W/mK}^2$  at  $\sim 1000$  K. Fe ions replace the Co ions in the  $\text{CoO}_2$  layers, and this substitution changes the electronic structure and increases the electronic correlations. Thus, doping Fe causes an enhancement in both the Seebeck coefficient and electrical conductivity [46]. On the other hand, doping Cu and Ag decreases the PF value because Cu/Ag ions mainly occupy the sites of Co ions in the  $\text{Ca}_2\text{CoO}_3$  layers, which results in an increase of electrical conductivity but a decrease of the Seebeck coefficient.

### 3.1.3 BiCuSeO

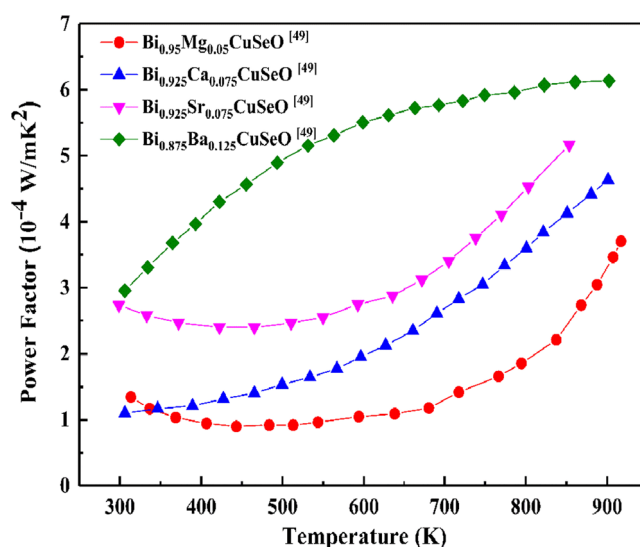
BiCuSeO oxyselenide was first reported as a promising TE material in 2010 [48]. BiCuBeO belongs to the layered ZrCuSiAs-type structure with the tetragonal space group  $P4/nmm$  [49]. The crystal structure is alternately stacked by  $(\text{Bi}_2\text{O}_2)^{2+}$  layers and  $(\text{Cu}_2\text{Se}_2)^{2-}$  layers along with the  $c$ -axis. The  $(\text{Bi}_2\text{O}_2)^{2+}$  layers are mainly responsible for the carrier (holes) transport while the  $(\text{Cu}_2\text{Se}_2)^{2-}$  layers are for reserving charges. The un-doped polycrystalline BiCuSeO shows the Seebeck coefficient and electrical conductivity of  $350 \mu\text{V/K}$  and  $1.12 \text{ S/cm}$  at 300 K, respectively, leading to a low PF of  $0.14 \times 10^{-4} \text{ W/mK}^2$  [49]. This is mainly due to the low electrical conductivity caused by the intrinsic low carrier concentration of  $1 \times 10^{18}/\text{cm}^3$ . This value is much lower than the optimized doping concentration of TE materials ( $10^{19}$ – $10^{21}/\text{cm}^3$ ) [50–53]. To enhance the TE properties of BiCuSeO, the alkaline-earth metals (Mg, Ca, Ba, and Sr) with  $2^+$  valence have been reported to be good  $p$ -type dopants replacing the  $\text{Bi}^{3+}$  in BiCuSeO [49, 54–56]. Doping these elements can improve the electrical conductivity by increasing the carrier concentration, which leads to an enhancement of PF.

Figure 3 summarizes the different metal dopants on the PF values of  $\text{Bi}_{1-x}\text{M}_x\text{CuSeO}$  ( $\text{M} = \text{Mg}, \text{Ca}, \text{Sr}$  and  $\text{Ba}$ ). As shown, the PF of BiCuSeO was greatly improved by doping  $\text{M}^{2+}$  compared to its undoped crystal structure. The electrical transport properties of BiCuSeO change from semiconducting behavior to metallic behavior once  $\text{M}^{2+}$  is doped, resulting in a significant increase in electrical conductivity without degrading the Seebeck coefficient. Among all the dopants,  $\text{Ba}^{2+}$  doping resulted in the highest electrical conductivity in the  $\text{Bi}_{0.875}\text{Ba}_{0.125}\text{CuSeO}$  sample, which reached  $535 \text{ S/cm}$  at 300 K [55]. Thus, the largest PF ( $\sim 6.14 \times 10^{-4} \text{ W/mK}$  [2]) was achieved at 900 K. With the  $\text{Ba}^{2+}$  modulation doping, the PF of BiCuSeO has achieved PF as high as  $10 \times 10^{-4} \text{ W/mK}^2$  at  $\sim 900$  K [17], which is the highest PF value of doped BiCuSeO ever reported.

Alkali metals, such as Na, have also shown promises in improving the PF of BiCuSeO [57], but the limitation of solubility in BiCuSeO impeded their potential as good  $p$ -type dopants. Recently, Pb/Ca co-doping has been reported as an efficient way to enhance the TE properties of BiCuSeO [17, 58]. Under Pb/Ca co-doping, the PF of BiCuSeO has reached  $\sim 10 \times 10^{-4} \text{ W/mK}^2$  at room temperature [58].

### 3.1.4 CaMnO3

Perovskite oxide  $\text{CaMnO}_3$  has been considered as a good  $n$ -type TE material due to its high Seebeck coefficient in the range of  $-300 \mu\text{V/K}$ – $400 \mu\text{V/K}$  [59–62] and chemical stability at temperatures up to 1200 K [63]. Although  $\text{CaMnO}_3$  has relatively high Seebeck coefficient, its electrical conductivity is very low ( $0.1$  to  $1 \text{ S/cm}$  in the temperature range 300–1000 K), which often results in low PF values [64]. Previous studies indicated that with a minor electron



**Fig. 3** Power factor values of  $\text{Bi}_{1-x}\text{M}_x\text{CuSeO}$  ( $\text{M} = \text{K}, \text{Mg}, \text{Ca}, \text{Sr}$ , and  $\text{Ba}$ ) as a function of temperature



doping at the A ( $\text{Ca}^{2+}$ ) and B sites ( $\text{Mn}^{4+}$ ), its electrical conductivity can be significantly increased. As such, the high PF of  $\text{CaMnO}_3$  TE materials has been achieved by replacing the A site and B site with rare-earth ions,  $\text{Y}^{3+}$ ,  $\text{Bi}^{3+}$ , and  $\text{Nb}^{5+}$  and  $\text{Ta}^{5+}$ ,  $\text{Mo}^{6+}$ , and  $\text{W}^{5+}$ , respectively [65].

Ohtaki et al. reported that the electron transport properties of  $\text{CaMnO}_3$  have been improved by replacing the A site and B site with different lanthanides [18, 60, 66] and heterovalent cations such as W, Ta, Ru, Mo, and Nb [67–71], respectively. Several studies have been carried out to investigate the TE properties of  $\text{CaMnO}_3$ , particularly focusing on strategies to increase the electrical conductivity without significantly decreasing the Seebeck coefficient. Figure 4 exhibits the PF of single and co-doped  $\text{CaMnO}_3$  with respect to temperature. Clearly, Bi-substituted  $\text{CaMnO}_3$  shows the largest PF of all the samples. Doping larger cations such as  $\text{Bi}^{3+}$  on the Ca site results in high electrical conductivity caused by the higher mobility of the carriers [60]. The highest PFs of  $4.67 \times 10^{-4} \text{ W/mK}^2$  at 423 K and  $3.74 \times 10^{-4} \text{ W/mK}^2$  at 965 K were achieved for  $\text{Ca}_{1-x}\text{Bi}_x\text{MnO}_3$  with a Bi composition at  $x = 0.03$  (Fig. 4) [72]. However, the co-doped  $\text{Ca}_{0.96}\text{Bi}_{0.04}\text{Mn}_{0.96}\text{Nb}_{0.04}\text{O}_3$  sample shows a lower PF because of the decrease of the electrical conductivity. Compared to Bi-substituted  $\text{CaMnO}_3$ , the increased amount of  $\text{Nb}^{5+}$  into the  $\text{MnO}_6$  octahedra leads to a more serious lattice distortion [73]. As a result, the electrical conductivity is decreased due to a reduction in carrier mobility, which leads to the lower PF of the co-doped  $\text{Ca}_{0.96}\text{Bi}_{0.04}\text{Mn}_{0.96}\text{Nb}_{0.04}\text{O}_3$  sample.

Lan et al. [74] studied the TE properties of polycrystalline  $\text{Ca}_{1-x}\text{Gd}_x\text{MnO}_3$  ( $x = 0.02, 0.04, \text{ and } 0.06$ ) synthesized via a chemical co-precipitation method. The maximum electrical

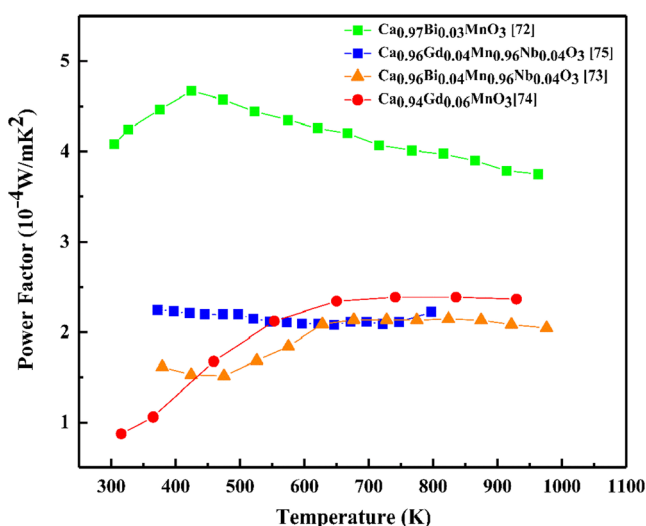
conductivity of  $113.4 \text{ S/cm}$  was discovered for Gd-doped  $\text{CaMnO}_3$  sample at  $x = 0.06$ , which resulted in the highest PF of  $2.3 \times 10^{-4} \text{ W/mK}^2$  at 950 K, shown in Fig. 4. Nag et al. [75] examined the transport properties of the co-substituted  $\text{Ca}_{1-x}\text{Gd}_x\text{Mn}_{1-x}\text{Nb}_x\text{O}_3$  ( $0 \leq x \leq 0.1$ ) perovskite synthesized by solid-state reaction. The increase of electrical conductivity can be attributed to the formation of  $\text{Mn}^{3+}$ , which results in the increase of carrier concentration. However, the Seebeck coefficient is lower in co-doped  $\text{CaMnO}_3$  samples due to the high carrier concentration, which results in a relatively low PF of  $2.0 \times 10^{-4} \text{ W/mK}^2$  at 800 K.

### 3.1.5 $\text{SrTiO}_3$

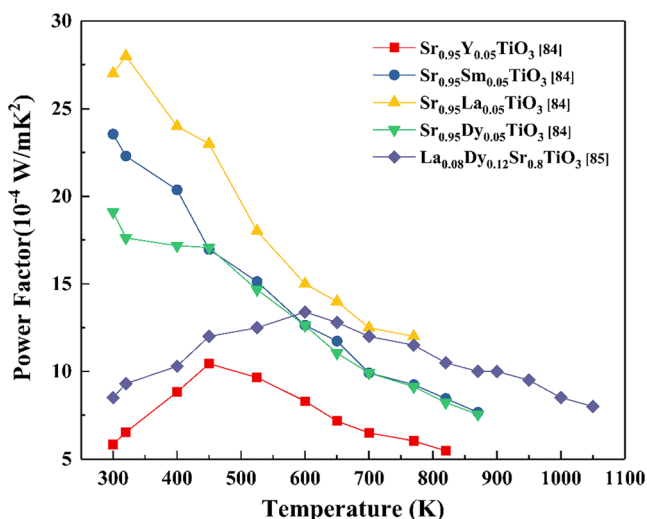
Strontium titanate ( $\text{SrTiO}_3$ )-based perovskite oxide materials have shown *n*-type electrical conduction behavior, and they have an ideal cubic crystal structure (space group  $pm3m$ , lattice parameter  $a = 0.3905 \text{ nm}$  at 300 K, and melting point 2353 K) [63, 76]. Recently,  $\text{SrTiO}_3$  has been recognized as a promising candidate for low-temperature TE applications, since it has good electrical conductivity and large Seebeck coefficient ( $\sim 100 \mu\text{V/K}$ ) at high doping concentration ( $n \sim 10^{21} \text{ cm}^{-3}$ ) [30]. This is mainly due to its high electron mobility ( $10$  to  $100 \text{ cm}^2/\text{V/s}$ ) [30] and large effective mass ( $m^* \sim 2\text{--}16 m_0$ ) [77–79], which arises from its *d*-band nature and conduction band degeneracy [80, 81]. Furthermore, the electrical conductivity of the  $\text{SrTiO}_3$  can be changed from insulating to metallic behaviors through different doping mechanisms such as introducing oxygen vacancies or substitutional doping of the  $\text{Sr}^{2+}$  or  $\text{Ti}^{4+}$  sites with higher-valence elements (e.g.,  $\text{La}^{3+}$  for  $\text{Sr}^{2+}$  sites or  $\text{Nb}^{5+}$  for  $\text{Ti}^{4+}$  sites) [79, 82, 83].

Okuda et al. [81] first reported the highest PF  $28\text{--}36 \times 10^{-4} \text{ W/mK}^2$  at 300 K for heavily La-doped  $\text{SrTiO}_3$  single crystals with doping concentration of  $0.2\text{--}2 \times 10^{21}/\text{cm}^3$ , which is comparable to that of  $\text{Bi}_2\text{Te}_3$ , the state-of-the-art low-temperature TE material. The unexpectedly high PF is due to the large Seebeck coefficient ( $\sim 350 \mu\text{V/K}$ ) caused by the high degeneracy of the conduction band as well as the large energy-dependent scattering rate. Also, heavily Nb-doped  $\text{SrTiO}_3$  single crystals at carrier concentration of  $3.3 \times 10^{21}/\text{cm}^3$  achieved high PF ( $\sim 20 \times 10^{-4} \text{ W/mK}^2$ ) at 300 K. The high Seebeck coefficient ( $\sim 240 \mu\text{V/K}$ ) at room temperature was caused by the large effective mass ( $m^* \sim 7.3\text{--}7.7 m_0$ ) [80].

Figure 5 shows that  $\text{Sr}_{0.95}\text{La}_{0.05}\text{TiO}_3$  reaches the highest PF of  $28 \times 10^{-4} \text{ W/mK}^2$  at 320 K due to the large Seebeck coefficient as discussed before. Since Sm, Dy, and Y are rare-earth elements, they have smaller ionic radius compared to  $\text{Sr}^{2+}$ , which results in a decreased lattice parameter [84]. Compared to La-doped  $\text{SrTiO}_3$ , the La- and Dy-co-doped  $\text{La}_{0.08}\text{Dy}_{0.12}\text{Sr}_{0.8}\text{TiO}_3$  sample has lower PF due to the decreased electrical conductivity. The electrical conductivity



**Fig. 4** Power factor values of doped  $\text{CaMnO}_3$  with various dopants as a function of temperature



**Fig. 5** Power factor values of doped SrTiO<sub>3</sub> with various dopants as a function of temperature

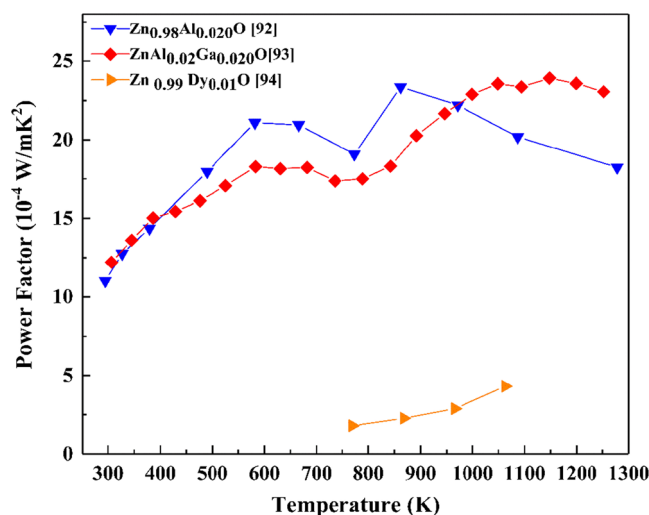
decreases can be attributed to the reduced carrier mobility caused by the formation of the second phase (Dy<sub>2</sub>Ti<sub>2</sub>O<sub>7</sub>) during the doping mechanism [85]. However, Y-doped SrTiO<sub>3</sub> has the lowest PF mainly due to the low Seebeck coefficient.

## 3.2 Wide band gap

### 3.2.1 ZnO-based

Zinc oxide (ZnO) has a direct wide band gap of 3.37 eV and large exciton-binding energy of 60 meV [86, 87]. It is a non-toxic, low-cost, and earth-abundant material which is stable at a high temperature. These properties make it a promising candidate for *n*-type TE materials for energy harvesting in high-temperature applications [88–90]. At room temperature, Lu et al. has reported that the PF of bulk ZnO materials was achieved at about  $0.75 \times 10^{-4}$  W/mK<sup>2</sup> at carrier concentration ( $n \sim 10^{-17}$ /cm<sup>3</sup>), due to the high crystal quality resulting in a large Seebeck coefficient ( $\sim 478$   $\mu$ V/K) [91].

Figure 6 presents the temperature-dependent PF of ZnO-based TE materials. A general trend of PF increasing with the increase of temperature can be observed, and Al has been used as the most common dopant to enhance the TE properties of ZnO. Despite the high Seebeck for the Al-doped nano-bulk and bulk ZnO samples, the electrical conductivity of these samples is extremely low leading to a small PF value. Compared to their nano-structured counterparts, the bulk Zn<sub>0.96</sub>Al<sub>0.02</sub>Ga<sub>0.02</sub>O and Zn<sub>0.98</sub>Al<sub>0.02</sub>O alloys showed a higher PF in the temperature range from 300 to  $\sim 1300$  K [92, 93], which can be attributed to a better crystal quality in the bulk materials leading to higher electrical conductivity. Because the doped Al<sup>3+</sup> and Ga<sup>3+</sup> usually substitute for Zn<sup>2+</sup> in ZnO and act as *n*-type donors, these dopants significantly enhance the electrical property of ZnO. Furthermore, the largest PF value



**Fig. 6** Power factor values of doped ZnO with various dopants as a function of temperature

( $23.9 \times 10^{-4}$  W/mK<sup>2</sup>) was obtained in bulk Zn<sub>0.96</sub>Al<sub>0.02</sub>Ga<sub>0.02</sub>O at  $\sim 1147$  K reported by Ohtaki et al. [93], which remains the highest PF of all high-temperature *n*-type oxides that was ever reported.

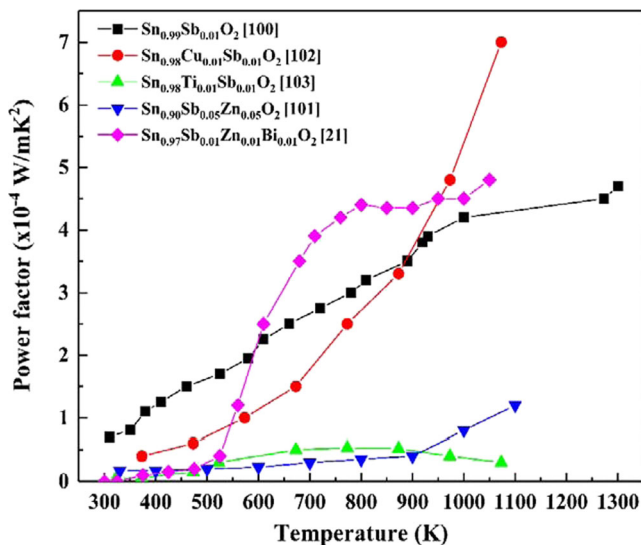
The addition of a small amount of Dy<sub>2</sub>O<sub>3</sub> has been also found to be effective for improving the thermoelectric properties of ZnO [94]. The highest power factor of  $4.46 \times 10^{-4}$  W/mK<sup>2</sup> at 1100 K was obtained for Zn<sub>0.995</sub>Dy<sub>0.005</sub>O. The PF is approximately 56 times larger than that of undoped ZnO ( $0.08 \times 10^{-4}$  W/mK<sup>2</sup> at 1100 K) [94]. It was reported that the addition of Dy<sub>2</sub>O<sub>3</sub> leads to an increase in the electrical conductivity, which can be attributed to the substitution of Dy<sup>3+</sup> for Zn<sup>2+</sup>. As a result, this increased carrier concentration of the system can compensate for the electrical charge balance [94].

### 3.2.2 SnO<sub>2</sub>-based

Tin oxide (SnO<sub>2</sub>) is a wide-band-gap (3.6 eV) semiconductor that crystallizes in a rutile-type structure [95]. Due to its electrical and optical properties, SnO<sub>2</sub> and impurity-doped SnO<sub>2</sub> are mainly used as an electrode for dye-sensitized solar cell [95] and electrochromic devices [96], a catalyst in chemical reactions [97], a varistor [98], and a gas sensor [99].

Rubenis et al. [100] reported that the TE properties of Sn<sub>1-x</sub>Sb<sub>x</sub>O<sub>2</sub> ( $x = 0, 0.01, 0.03, 0.05$ ) were synthesized by spark plasma sintering and subsequently air annealing at 1173 K. The addition of Sb<sub>2</sub>O<sub>5</sub> increased the carrier concentration of SnO<sub>2</sub>. Thus, the Seebeck coefficient decreased but the electrical conductivity increased up to a maximum of 5.5 times at the Sb-doping level of  $x = 0.03$ . The Sn<sub>0.99</sub>Sb<sub>0.01</sub>O<sub>2</sub> sample has the highest PF value of  $4.5 \times 10^{-4}$  W/mK<sup>2</sup> at 1073 K.

Figure 7 shows that Sn<sub>0.94</sub>Sb<sub>0.03</sub>Zn<sub>0.03</sub>O<sub>2</sub> reaches the maximum PF of  $2.13 \times 10^{-4}$  W/mK<sup>2</sup> at 1060 K, which is 126% higher



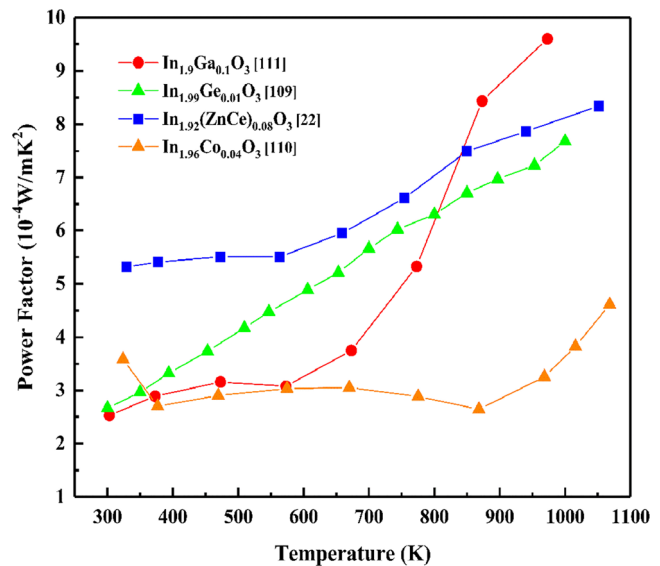
**Fig. 7** Power factor values of doped  $\text{SnO}_2$  with various dopants as a function of temperature

than that of the undoped sample. The electrical conductivity increases are due to the carrier concentration that was caused by an increase in Sb doping and the density of Zn doping [101]. Moreover, the Bi-doped  $\text{Sn}_{0.97}\text{Sb}_{0.01}\text{Zn}_{0.01}\text{Bi}_{0.01}\text{O}_2$  sample has reached the maximum PF of  $4.8 \times 10^{-4} \text{ W/mK}^2$  at 1060 K. Yanagiya et al. [21] reported that Bi increased the electrical conductivity by increasing the number of free electrons in  $\text{SnO}_2$ , where Bi behaves as a donor. Also, the addition of CuO to the Sb-doped  $\text{SnO}_2$  increased the PF at a high temperature ( $T > 1000 \text{ K}$ ). The substitution of Cu for Sn decreased carrier concentration because Cu is divalent but Sn is quadrivalent. As a result, the Seebeck coefficient increased. Also, the addition of the CuO has significantly improved the relative density of  $\text{SnO}_2$  ceramics [102]. As such, the electrical conductivity increased with the increased carrier mobility. The Cu- and Sb-co-doped  $\text{Sn}_{0.98}\text{Cu}_{0.01}\text{Sb}_{0.01}\text{O}_2$  reached the highest PF value of  $7 \times 10^{-4} \text{ W/mK}^2$  at 1073 K. However, Ti- and Sb-co-doped  $\text{Sn}_{1-x-y}\text{Ti}_x\text{Sb}_y\text{O}_2$  samples had lower PF values due to the electrical conductivity decreases with adding more  $\text{TiO}_2$  because  $\text{TiO}_2$  dissolved in  $\text{SnO}_2$  that caused the reduction of the mobility, resulting in the decrease of the electrical conductivity [103].

### 3.2.3 $\text{In}_2\text{O}_3$ -based

Indium oxide ( $\text{In}_2\text{O}_3$ ) is a semiconductor with a band gap of 3.6 eV, [104] which has recently gained interest as a promising candidate for high-temperature TE applications due to its high stability at air. It has been shown that the electrical properties of  $\text{In}_2\text{O}_3$  can be drastically changed by doping with Sn, Mo [105, 106], Zr, Ti [107, 108], and W [109].

Figure 8 shows that  $\text{In}_{1.92}(\text{ZnCe})_{0.08}\text{O}_3$ -nanostructured ceramic exhibits the highest PF of  $8.36 \times 10^{-4} \text{ W/mK}^2$  at



**Fig. 8** Power factor values of doped  $\text{In}_2\text{O}_3$  with various dopants as a function of temperature

1050 K<sup>22</sup>. This is due to the influence of nanostructuring and point defects on TE properties of the  $\text{In}_2\text{O}_3$  system. Point defect hinders the atomic-scale scattering and improves the carrier concentration thereby increasing PF. Utilizing the spark plasma-sintering process, co-doped polycrystalline  $\text{In}_2\text{O}_3$  ceramics were fabricated by Liu et al. [110]. They have achieved high electrical conductivity and Seebeck coefficient, which resulted in PF of  $4.53 \times 10^{-4} \text{ W/mK}^2$  at 1070 K for  $\text{In}_{1.96}\text{Co}_{0.04}\text{O}_3$ . Later, Liu et al. [111] prepared single-element Ga-doped  $\text{In}_2\text{O}_3$  ceramics by spark plasma sintering to explore their TE properties at high temperatures. The slight change in the Seebeck coefficient and a significant enhancement of the electrical conductivity ( $\sim 400 \text{ S/cm}$ ) at 973 K were caused by an increase of carrier concentration through doping Ga, which achieved the highest PF of  $9.6 \times 10^{-4} \text{ W/mK}^2$  in  $\text{In}_{1.90}\text{Ga}_{0.10}\text{O}_3$  at 973 K.

Table 1 summarizes the TE properties of various metal oxides with different dopants at a high-temperature regime, approximately 800 K. It has shown that metal oxides have good TE performance at high-temperature range. For *n*-type materials, the highest PF value was found as of  $22 \times 10^{-4} \text{ W/mK}^2$  for  $\text{Zn}_{0.98}\text{Al}_{0.02}\text{O}$ , which is close to that of SiGe, the state-of-the-art high-temperature TE material. For *p*-type materials, the highest PF value was reported as  $16 \times 10^{-4} \text{ W/mK}^2$  for  $\text{Na}_{0.95}\text{Ag}_{0.05}\text{CoO}_2$ , which is lower than that of *n*-type materials. Despite *p*-type materials having high Seebeck coefficient caused by the large effective mass of the hole, their electrical conductivity is much lower due to the difficulty of doping. Thus, the investigation of effective doping mechanisms is very important, particularly for *p*-type TE materials, to explore more applications such as solar cells, transistors, sensors, and photodetectors.

**Table 1** Thermoelectric properties of metal oxides measured at 800 K by different dopants, *S* is for Seebeck Coefficient,  $\sigma$  is for electrical conductivity, and PF is for power factor

Material	Dopants	$ S $ ( $\mu\text{V/K}$ )	$\sigma$ (S/cm)	$k$ (W/mK)	PF ( $\times 10^{-4}$ W/mK <sup>2</sup> )	Ref.
Narrow band gap, <i>p</i> -type						
Na <sub>x</sub> CoO <sub>2</sub>	Y	149.5	271.9	1.72	6.08	[36]
	Nd	150.0	280.8	1.43	6.32	[36]
	Sr	156.2	276	1.37	6.73	[36]
	Sm	145.4	271.8	1.38	5.75	[36]
	K	140.0	313	1.35	6.13	[36]
	Yb	139.0	268	1.47	5.18	[36]
Ca <sub>4</sub> Co <sub>4</sub> O <sub>2</sub>	Ag	205.2	392.1	1.34	16.51	[35]
	Bi	166.7	145.76	–	4.05	[45]
	Fe	234.7	88.41	1.92	4.87	[46]
BiCuSeO	Ga	173.6	114.17	1.52	3.44	[47]
	Mg	352.2	30	0.33	3.72	[49]
	Sr	202.4	110.30	0.30	4.52	[49]
	Ba	170.0	207	0.25	5.98	[49]
Narrow band gap, <i>n</i> -type						
CaMnO <sub>3</sub>	Gd	147	113	1.41	2.44	[74]
	Bi	206	95.87	1.62	4.07	[72]
	Bi, Nb	166	77.6	1.82	2.14	[73]
	Gd, Nb	150	100	1.2	2.25	[75]
SrTiO <sub>3</sub>	La	210	250	5.5	11.03	[84]
	Sm	223	126	–	6.27	[84]
	Gd	206	130	–	5.52	[84]
	Dy	200	140	–	5.60	[84]
	La, Dy	159	420	3.46	10.62	[85]
Wide band gap, <i>n</i> -type						
ZnO	Al	163	839	12	22.29	[92]
	Al, Ga	173	611	6.2	18.29	[93]
	Dy	55	80	–	0.24	[94]
SnO <sub>2</sub>	Sb	150	190	11.5	4.28	[100]
	Cu, Sb	70	100	7	0.49	[102]
	Ti, Sb	65	100	2.1	0.42	[103]
	Sb, Zn	150	15	–	0.34	[101]
	Sb, Zn, Bi	125	290	–	4.53	[21]
In <sub>2</sub> O <sub>3</sub>	Ga	150	375	0.25	8.44	[111]
	Co	203	65	–	2.68	[110]
	Zn, Ge	126	428	3.2	6.79	[22]

*S* Seebeck coefficient,  $\sigma$  electrical conductivity, *PF* power factor

In summary, transitional metal elements are effective dopants for metal oxides to reach high power factor. For Na<sub>x</sub>CoO<sub>2</sub>, Ag has proven to be a good dopant as it increases both electrical conductivity and Seebeck coefficient simultaneously, which results in the highest PF value for *p*-type metal oxides. For *n*-type oxides, both CaMnO<sub>3</sub> and SrTiO<sub>3</sub> have shown good TE performance, particularly with Bi and La doping, respectively. For wide-band-gap materials, Ga-doped In<sub>2</sub>O<sub>3</sub> has shown promising TE properties for high-TE-power-generation applications.

## 4 Commercial application of metal oxides for TE power generation and beyond

### 4.1 TE device for power generation

As a heat engine, the efficiency of thermoelectric device is governed by the Carnot efficiency and the materials' figure of merit *ZT* as the following:

$$\eta = \frac{T_H - T_C}{T_H} \left( \frac{\sqrt{1 + ZT} - 1}{\sqrt{1 + ZT} + T_C/T_H} \right) \tag{6}$$



where  $T_H$ ,  $T_C$ , and  $T_M$  are the hot-side, cold-side, and average temperatures, respectively. As a cost-effective alternative to conventional TE materials, oxides have superior thermal stability to be used for devices operated at a high-temperature regime to achieve higher Carnot efficiency (theoretical maximum)  $\eta_C = (T_H - T_C)/T_H$ , thus achieving much higher energy efficiency for power generation.

The simplest design of TEG consists of a  $p$ -leg and  $n$ -leg connected by conducting strips in series and covered by ceramic plate with heat conduction in perpendicular. Matsubara et al. [112] reported that a fin-type-oxide thermoelectric device was fabricated by using  $\text{Ca}_{2.75}\text{Gd}_{0.25}\text{Co}_4\text{O}_9$  as  $p$ -leg and  $\text{Ca}_{0.92}\text{La}_{0.08}\text{MnO}_3$  as  $n$ -leg. The high power density of the TE device was achieved at  $21 \text{ mW/cm}^2$  at  $\Delta T = 390 \text{ K}$ . This high performance was observed in oxide-based thermoelectric generators, because the power factor of both  $p$ - and  $n$ -type materials increased with temperature, with no bipolar effect observed. Another oxide-based TE device was fabricated from Man's group using  $\text{CaMgO}_2(\text{CMO-25-42S})$  as TE module [113]. A large power density of  $92 \text{ mW/cm}^2$  was reported at  $\Delta T = 440 \text{ K}$  compared to the previous study. It is interesting to note that the power outputs, in both cases, are sufficient to power small electronics, sensors, and other optoelectronic devices. Intriguingly, metal oxide-based TE generators have shown great promises for high-temperature power generation through waste heat harvesting.

## 4.2 Solar cells

In solar cell application, metal oxides such as  $\text{SnO}_2$  [95],  $\text{ZnO}$  [114], and  $\text{SrTiO}_3$  [115] are often used as photoelectrodes in dye solar cells (DSCs) [116, 117]. DSCs are made by a layer of dye-anchored mesoporous metal oxides, known as photoelectrodes, and covered with conducting glass plates on both sides [118]. Like TEG devices, efficiency is also important for solar cells. The efficiency of DSC is defined as [119]

$$\eta = \frac{J_{SC} V_{OC} FF}{P_{IN}} \quad (7)$$

where  $J_{SC}$  is current per unit active area,  $V_{OC}$  is open-circuit voltage,  $FF$  is fill factor, and  $P_{IN}$  is power input.

Durrant et al. have fabricated a DSC with  $\text{ZrO}_2$ -doped  $\text{TiO}_2$ -blocking layer, which resulted in a 35% efficiency improvement and reached  $V_{OC} = 50 \text{ mV}$  [120]. This significant efficiency improvement was attributed to the increased electron density of The  $\text{ZrO}_2$ -doped  $\text{TiO}_2$  thin films. As such, a significant recombination loss was prevented at short-circuit condition. However, the overall efficiency of photoelectric conversion at the device level has only reached 8.1%. Comparing with the 24.7% efficiency from a silicon-based solar cell, the DSC with metal oxide photoelectrode still needs much improvement [119]. For instance, much effort is needed

in synthesizing high-crystallinity metal oxides to increase charge collection efficiency in DSC without adversely affecting dye loading and, consequently, the short circuit current density.

## 4.3 Gas sensor application

Another related application for metal oxides is gas sensors. Gas sensors are used to detect toxic gas-like carbon monoxide (CO) and nitrous oxide ( $\text{N}_2\text{O}$ ). Metal oxides are usually both thermally and chemically stable and, hence, very suitable for gas-sensing application. For example,  $\text{SnO}_2$  and  $\text{TiO}_2$  can be used for CO sensors, and  $\text{ZnO}$  can be used in  $\text{N}_2\text{O}$  sensors. According to Barbi [121],  $\text{SnO}_2$ -based CO sensor has the best performance at a temperature of 523 K and response ( $R_0/R$ ) of 2.2 at 20 ppm. This significant improvement was attributed to the ultra-fine crystal size (400 Å) of  $\text{SnO}_2$ , which increased the free-carrier density of nanocrystals and localized the higher concentration of adatoms.

## 5 Summary

In this paper, we discuss recent advances in oxide-based thermoelectric materials and devices for power generation through waste heat harvesting. Metal oxides offer very promising solutions to the development of non-toxic and cost-effective thermoelectric devices for power generations. For low-temperature operation (300 K), the highest PF was found as  $28.3 \times 10^{-4} \text{ W/mK}^2$  in  $n$ -type  $\text{Sr}_{0.95}\text{La}_{0.05}\text{TiO}_3$ , which is in competition to that of BiTe, the state-of-the-art TE material at low-temperature regime. For high temperature (1147 K), the highest PF ( $23.9 \times 10^{-4} \text{ W/mK}^2$ ) was obtained in  $\text{Zn}_{0.96}\text{Al}_{0.02}\text{Ga}_{0.02}\text{O}$ , which makes  $\text{ZnO}$  as the best reported  $n$ -type TE material.

Despite the recent advancement, metal oxides for TE power generation are still in their early stage of development, and many scientific and technological challenges need to be addressed. For instance, it is very difficult to reach high electrical conductivity of metal oxides without degrading their Seebeck value simultaneously. Achieving high doping concentration and  $p$ -type behavior in wide-band-gap metal oxides remains a significant challenge. Regardless, the scientific and technological importance of developing metal oxide TE materials is evident, and the outlook is very promising. Clearly, discovering effective doping mechanisms to achieve high power output is essential to the development of thermoelectric power generation, solar cells, gas sensors, and photodetectors.

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**Yining Feng** is pursuing her PhD degree of Civil Engineering at Purdue University. She is also a guest graduate student at Argonne National Lab. Her current research interests range from nanostructured oxides for high temperature thermoelectric applications to flexible thermoelectric devices for medium to low temperature applications. Yining has published one book chapter, four journal papers and one conference proceeding. Yining has attended the 2017 National Science

Foundation (NSF) Innovation Corps (I-Corps) as an entrepreneur lead on high temperature thermoelectric technology development.



**Ian Ferguson** currently based at Missouri University of Science and Technology (Missouri S&T), most recently, as the founding Vice Provost and Dean of the College of Engineering Computing. His research has focused on building interdisciplinary teams to use compound semiconductor materials and devices for applications in the areas of sensors, illumination, energy harvesting, and spintronics. He has active research collaborations in the US, Europe, and Asia, which

has resulted in over 490 refereed journals and conference papers. He has been actively involved in the entrepreneurial process of establishing new companies has co-founded a business incubator, PiES, that was named



one of the “5 Incubators That Are Shaping the Future of Green Business”. He is a Fellow of the Royal Society of Arts, Manufactures and Commerce (FRSA) and Fellow of IEEE, IOP and SPIE.



**Na (Luna) Lu** is an associate professor of the Lyles School of Civil Engineering, School of Materials Engineering (by Courtesy) and Birck Nanotechnology Center at Purdue University. She is leading a multi-disciplinary research group that develops nanostructured materials and devices for energy harvesting, sensing and non-destructive testing. Lu has authored over 60 referred publications; one book, four book chapters, one patent and three provisional patents. She has given numerous keynote and invited talks at top research conferences, including

Material Research Society (MRS), The Mineral, Metals and Materials (TMS), and SPIE Photonic West, etc. Lu has won several scientific awards, including the 2014 National Science Foundation (NSF) CAREER Award. She has also founded a spin-off company with the technologies invented at her research lab.