# The Application of Elliptic Fourier Analysis in Understanding Biface Shape and Symmetry Through the British Acheulean



Christian Steven Hoggard <sup>1,2</sup> b John McNabb<sup>2</sup> · James Nathan Cole<sup>3</sup>

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# Abstract

Acheulean biface shape and symmetry have fuelled many discussions on past hominin behaviour in regards to the 'meaning' of biface technology. However, few studies have attempted to quantify and investigate their diachronic relationship using a substantial dataset of Acheulean bifaces. Using the British archaeological record as a case study, we first perform elliptic Fourier analysis on biface outlines to quantify and better understand the relationship between biface shape and individual interglacial periods. Using the extracted Fourier coefficients, we then detail the nature of symmetry throughout this period, before investigating both shape and symmetry in parallel. The importance of size (through biface length) as a factor in biface shape and symmetry is also considered. Results highlight high levels of symmetry from Marine Isotope Stage (MIS) 13, followed by increasing asymmetry through the British Acheulean. Other observations include a general shift to 'pointed' forms during MIS 9 and 7 and the importance of size in high biface symmetry levels. This article concludes by discussing the potential importance of secondary deposition and palimpsest sites in skewing the observed relationships throughout the Palaeolithic.

Keywords Biface · Geometric morphometrics · Acheulean · Symmetry

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Christian Steven Hoggard C.Hoggard@cas.au.dk

- <sup>1</sup> Department of Archaeology and Heritage Studies, School of Culture and Society, Aarhus University, 8000 Aarhus, Denmark
- <sup>2</sup> Department of Archaeology, Faculty of Humanities, University of Southampton, Southampton SO17 1BJ, UK
- <sup>3</sup> Department of Geography and Environment, School of Environment and Technology, University of Brighton, Brighton BN2 4GJ, UK

## Introduction

For the last 60 years, many of the established classificatory frameworks for understanding and interpreting past hunter-gatherer societies have been underpinned by analyses of artefact morphology and the categorisation of morphological variation (Bordes 1961; Roe 1969, 1981; Wymer 1968). For studies in early prehistory, this focus on morphological variation is best exemplified through the numerous debates, analyses, interpretations and reinterpretations of biface variability throughout the Acheulean period (c. 1.7 ma to 200 ka) (Machin 2009). Given their broad spatial and temporal coverage, ubiquitous to many (but not all) early prehistoric contexts (Lycett and von Cramon-Taubadel 2008), in addition to the clear imposition of intent so early in the archaeological record, it is unsurprising that there is now a significant corpus dedicated to variability and 'meaning' of Acheulean bifaces (Wynn 1995, 2002; Kohn and Mithen 1999; Machin et al. 2007; Machin 2008, 2009; Mithen 2008; Hodgson 2009; Nowell and Chang 2009; Spikins 2012; Lycett 2015; McNabb et al. 2018). It is for these reasons that the biface is now noted as one of the more studied artefact types within early prehistory (Iovita 2010b), to the extent that Lycett and colleagues (Lycett et al. 2015: 157) liken the multitude of experimental biface studies to that of the use of fruit flies (Drosophila spp.) as a 'model organism' within the biological sciences. Throughout these studies on biface morphology and 'meaning', two aspects have produced perhaps the greatest interest: aspects of bilateral symmetry and planform shape.

Often noted as a hallmark of cognitive evolution (Wynn 2002; Wynn and Coolidge 2016; McNabb and Cole 2015), there have been numerous attempts to quantify, interpret and fundamentally understand bilateral symmetry during the Acheulean. Saragusti et al. (1998) represent one of the earliest attempts to quantify biface symmetry throughout early prehistory. Through an analysis of three archaeological contexts in Israel, Saragusti et al. (1998) concluded that symmetry increased over time. There were a number of statistical issues acknowledged by the authors themselves, specifically associated with the analysed sample size. When this dataset was subsequently extended and analysed by Saragusti et al. (2005: 846), it was observed that "the picture emerging is more complex than a simple monotonic increase in the degree of symmetry over time".

An appreciation and understanding of symmetry were also fundamental to the 'sexy handaxe theory' (Kohn and Mithen 1999), which proposed that Darwinian sexual selection accounted (in part) for biface symmetry and thus enabled material culture proxies to act as biological indicators for individual phenotypic fitness. This prompted an extensive discussion on the role of material culture as an extended phenotype (Hodgson 2009; Machin 2008, 2009; Nowell and Chang 2009), best summarised by Spikins (2012).

Following this, biface symmetry was considered by Wynn (2002), who detailed two cognitive 'thresholds', represented through the evidence of Palaeolithic bifaces. The first threshold, categorised by the deliberate imposition of form in the earliest examples of biface technology, was noted as featuring varying levels of bilateral symmetry (with symmetry not always consistent applied). The second threshold, occurring half a million years ago, was defined as the congruence of bilateral planform and cross-

section symmetry. Wynn's proposed model prompted a mixture of reactions, with some stressing that biface symmetry was an emerging property generated by the extensive flaking of bifaces (Coventry and Clibbens 2002), while others suggested that the recognition of symmetry was an ancient faculty, reflecting the way with which visual stimuli were processed by the brain (Deregowski 2002; Reber 2002). More recently, McNabb et al. (2018:295) note that this discussion led to a view that "... archaeologists should not assume the presence of symmetry in material culture was conscious or culturally learned".

Other researchers have considered the relationship of symmetry to the utilitarian function of the biface. While the use of bifaces in butchery and carcass processing is now extensively attested (Jones 1981; Shick and Toth 1993; Keeley 1980; Mitchell 1996), it was Machin et al. (2007) who first noted in their experimental framework that a large percentage of cutting edge effectiveness could not be solely explained by symmetry (or a number of other linear measurements).

More recently, a number of other arguments and hypotheses have been developed further exploring the 'meaning' of biface symmetry. These include hypotheses of bifaces as advertisements (Machin 2009) and reciprocal altruistic tokens (Spikins 2012). Others have helped to clarify and understand the level of symmetry throughout the Lower and Middle Palaeolithic. For example, Iovita et al. (2017) highlight high levels of symmetry as early as c.700,000 years ago, followed by a *longue durée* involving the variable imposition of symmetry in different assemblages across time (Hosfield et al. 2018; McNabb et al. 2018). For further details on discussions relating to biface symmetry, see Spikins (2012), Hodgson (2015), McNabb and Cole (2015) and McNabb et al. (2018).

Unsurprisingly, aspects of biface shape and form (size *plus* shape) are linked to many of the above discussions on biface symmetry, e.g. shape as indicators for phenotypic fitness (e.g. Kohn and Mithen 1999), with many of the aforementioned themes or directions of research tackled through a shape-centric perspective. For example, just as biface symmetry has been discussed with reference to butchery efficiency and functionality, so too has biface shape. This includes the recent work by Key and Lycett (2017), who analysed the relationship between biface shape, size (size is here defined as mass) and functionality. Using a large dataset of experimentally reproduced bifaces, Key and Lycett (2017) demonstrated that biface shape does not have an immediate impact on cutting effectiveness and that such variation may be related to non-functional issues.

In addition, discussions on the role of biface shape have often focused on aspects of biface reduction strategy and changes associated with resharpening (Emery 2010; Iovita 2009; Iovita and McPherron 2011; Li et al. 2015; McPherron 2000; Serwatka 2015; Shipton and Clarkson 2015; White 1998, 2006), and the use of bifaces in understanding underlying social learning mechanisms (Lycett et al. 2015; Schillinger et al. 2015, 2016, 2017). Given the necessity of powerful exploratory and statistical methodologies for cataloguing and understanding biface shape variance, two- and three-dimensional geometric morphometric (GMM) methodologies have been particularly advantageous in this regard (Archer and Braun 2010; Costa 2010; Iovita 2009, 2010a; Iovita and McPherron 2011; Key and Lycett 2017; Li et al. 2015; Lycett 2007; Lycett et al. 2006; Schillinger et al. 2017; Shipton and Clarkson 2015; Wang et al. 2012).

Central to many previous studies on biface shape and symmetry has been an understanding of whether both shape and symmetry become increasingly standardised towards the end of the Acheulean (Saragusti et al. 1998, 2005; Hodgson 2009, 2015; Beyene et al. 2013; Li et al. 2015; McNabb and Cole 2015; McNabb et al. 2018). Despite these studies, there is a distinct absence of exploratory and statistical frameworks which quantify and investigate the diachronic relationship of biface shape and symmetry (independently *and* concurrently) through the analysis of a large comparative Acheulean dataset. Such studies would be of great benefit to researchers studying broad-scale temporal change in technological behaviour and MIS-specific variability. In addition, such a study would add to the broader literature, challenging and testing the notion of increasing biface shape and symmetry standardisation over time.

Using the British archaeological record as a case study, this paper examines the diachronic relationship in biface shape and symmetry. Specifically, this paper will explore three questions:

- 1. How does biface shape change throughout the British Acheulean and can increasing standardisation in biface shape be observed?
- 2. How does biface symmetry change throughout the British Acheulean and can increasing standardisation in biface symmetry be observed?
- 3. How are the main sources of biface shape variation linked to variations in symmetry, and how does biface size relate to both biface shape and symmetry?

## Methodology

### Dataset and Recording Strategy

To investigate the diachronic relationship of biface shape and symmetry throughout the British Acheulean, and how size is driving any possible correlation, a two-dimensional GMM framework is here presented, encompassing 468 artefacts from ten archaeological sites (Table 1). In their choice, these ten sites represent one of the best-dated and chronostratigraphically secure archaeological sequences in north-western Europe (Hosfield 2011; McNabb 2007). Regarding their raw material, flint is predominant throughout the dataset, with Pontnewydd Cave representing the sole exception, where volcanic raw material was utilised (Aldhouse-Green et al. 2012).

In constructing a dataset, the complete number of bifaces from a museum collection was examined. In instances where collections were significantly larger (i.e. deviating from the mean number of bifaces per collection), a random-number generator (https://www.randomizer.org/) was used to sample 50 bifaces from each site. For comparative purposes, the Late Pleistocene site of Lynford (Boismier et al. 2003, 2012), dating to the Marine Isotope Stage (MIS) 4/3 was included.

Despite the prevalence of three-dimensional GMM methodologies in recent years (Archer et al. 2015, 2017; Herzlinger et al. 2017), a two-dimensional methodology analysing digital photographs of bifaces is here presented. While greater artefact coverage benefits the analytical power of an analysis, when used with caution, the examination of two-dimensional photographs serves a number of advantages, including the potential to record and analyse

Marine Isotope Stage	Context	Sample size	Source	Collection
13 (528–474 kya)	Warren Hill	49	Marshall et al. (2002)	_
	Boxgrove	50	Marshall et al. (2002)	-
11 (427–364 kya)	Bowman's Lodge	28	Marshall et al. (2002)	-
	Elveden	29	Author (JNC)	BM (Sturge Collection)
	Swanscombe	58	Author (JM)	BM (Marston Collection)
9 (334–301 kya)	Broom	50	Marshall et al. (2002)	-
	Furze Platt	69	Author (JM)	BM (Treacher Collection)
7 (242–186 kya)	Cuxton	50	Marshall et al. (2002)	-
	Pontnewydd Cave	37	Author (JNC)	NMW
4/3 (57 kya)	Lynford	48	Author (JNC)	NAU

Table 1 The British Lower and Middle Palaeolithic assemblages used for this study (total: 468)

BM British Museum, United Kingdom, NMW National Museum of Wales, United Kingdom, NAU Northampton Archaeological Unit, United Kingdom

considerably larger datasets, including archival data, illustrations and openaccess repositories.

Digital photographs of each biface were captured by JM and JNC, with the dataset expanded through the Marshall et al. (2002) database, curated by the Archaeological Data Service (ADS) (http://archaeologydataservice.ac.uk/archives/view/bifaces/). To minimise lens distortion (distortion through perspective and optics), a suitable recording strategy was implemented, with profile corrections performed in the CorelDraw Graphics Suite (X7).

In order to analyse biface shape, an outline was first created in the CorelDraw Graphics Suite (using the 'Trace Outline' function), with the original photograph subsequently deleted to reduce pixel noise. The outline was set to a thickness of one pixel and screened for breaks and errors. Incomplete curves were subsequently closed, with all changes also standardised to one pixel in thickness. These outlines were then exported as a Portable Network Graphics (.png file extension) for subsequent recording and analysis.

#### **Elliptic Fourier Analysis**

To investigate biface shape and symmetry, the outlines were examined through elliptic Fourier analysis (EFA), a common method of closed outline shape analysis, extending on from the Fourier series first derived by Jean Baptiste Joseph Fourier (1768–1830). Through EFA, an outline is transformed into an infinite series of repeating trigonometric functions (or harmonics), with four Fourier coefficients per harmonic retained (Ferson et al. 1985; Giardina and Kuhl 1977; Kuhl and Giardina 1982). Through biological studies by Iwata et al. (1998), and later by Iwata et al. (2002) and Yoshioka et al. (2004), the four derived coefficients from the  $n^{\text{th}}$  harmonic can be classified into two categories, pertaining to symmetrical ( $a_n$  and  $d_n$ ) and asymmetrical ( $b_n$  and  $c_n$ ) variations in two-dimensional shape. As a closed outline is constructed by the ratio of these

coefficients, an index of symmetry can be calculated from the ratio of symmetric harmonic coefficients to the sum of the absolute value of all harmonic coefficients (1.0 being calculated as complete bilateral symmetry). Central to the quantification and analysis of biface shape, through the above procedure, is a robust protocol for evaluating rotation. In orienting the bifaces, outlines were rotated for maximum symmetry through the elliptic best-fitting procedure of the first harmonic. The authors do acknowledge that error may be incorporated in planform siding, as non-corresponding edges may be analysed. And as legacy data (i.e. photographs) are here utilised, previous planform siding techniques focusing on scar density or 'doming' (Shipton and Clarkson 2015; Lycett et al. 2015) would prove difficult to determine. However, as studies highlight that the main sources of shape variation largely reflect symmetric changes in shape (Archer et al. 2015, 2017; Shipton and Clarkson 2015; Lycett et al. 2015), and as the first two major sources of variation (i.e. principal component scores) will be examined in detail, this error will be minimal.

In comparison to other closed outline methods including coordinate-point eigenshape (MacLeod 1999), Fourier radius variation and Fourier tangent angles (Zahn and Roskies 1972) and the fitting of polynomial curves (Rogers and Fog 1989), EFA boasts a number of methodological advantages. For this study, EFA permits the quantitative assessment of both biface symmetry and shape through the same analysis, in comparison to the above techniques. EFA also does not require data points to be of the same number or evenly spaced, and thus allows the analysis of complex two-dimensional edges. Furthermore, through the automation of outlines and subsequent digitisation, a replicable methodology with minimal subjectivity and inter-observer error (e.g. Hardaker and Dunn 2005; Underhill 2007) is achieved.

In order to analyse outlines through EFA, the .png files were first synthesised into one thin-plate spline (.tps) file in tpsUtil v.1.69 (Rohlf 2017a), with Cartesian coordinates and positions for each image created using the 'Outline object' tool in tpsDig2 v.2.27 (Rohlf 2017b). Both software programs are open-source and are available online (http://life.bio.sunysb.edu/ee/rohlf/software.html). As these outlines do not require the same number of landmarks throughout the .tps file, and in order to capture as much of the original shape as possible, the raw outline was stored. In total, the 468 bifaces feature  $1808 \pm 829$  Cartesian coordinates. The .tps file was then imported into Momocs v. 1.16 (Bonhomme et al. 2014) for the R Environment (R Development Core Team 2014), with an associated .csv file detailing the biface site, size (through biface length in millimetres) and MIS. In standardising the outlines prior to the EFA, all outlines were normalised to a common centroid (0,0) and rescaled using their centroid size following guidelines by Bonhomme et al. (2017). Normalisation through rotation was unnecessary as this is achieved through elliptic fitting of the first harmonic. In choosing a sufficient number of harmonics necessary to capture sufficient biface shape, the 'calibrate harmonicpower efourier' and 'calibrate deviations efourier' functions in Momocs were used (and supported through the 'calibrate reconstructions efourier' function). Through this procedure, 13 harmonic powers were necessary for 99% harmonic power, here defined as capturing sufficient biface shape. For more information on the fundamentals of EFA and EFA coefficients, see Caple et al. (2017).

### **Analytical and Exploratory Procedure**

To address the first research question, the main sources of shape variation within the ten sites were explored through a principal component analysis (EFA-PCA). The contributions for each principal component were examined through a scree plot, with shape transformations for each major principal component documented. A visual examination of the five interglacials, and their spatial configuration to the theoretical shape changes (i.e. the principal component scores), was conducted through confidence ellipses (66.66%). To explore if bifaces become increasingly standardised through the British Acheulean, variance in the first two principal components were examined through visual examination of the EFA-PCA plot and through box-and-whisker plots (Tukey style).

In exploring if specific biface shapes can be linked to particular periods, and if differentiation in biface shapes can be observed across the five interglacials, a discriminant analysis (with leave-one-out cross-validations), following guidelines by Kovarovic et al. (2011), was conducted. To perform the discriminant analysis, 99% cumulative shape variance totalling the first 21 principal component axes were retained. A discriminant analysis for the individual sites was not performed as three sites (Elveden, Bowman's Lodge and Pontnewydd Cave) do not meet the suggested sample size values (Klecka 1980; Kovarovic et al. 2011; McGarigal et al. 2000).

To support the exploratory exercise, the five interglacials were examined within a statistical multivariate framework. Specifically, a multivariate analysis of variance (MANOVA) of 99% cumulative shape variance was performed within their respective MIS. A null hypothesis (H<sub>0</sub>) of same populations for each variable was assumed, with statistical significance here defined at the 1% significance level (i.e.  $\alpha = 0.01$ ). Bonferroni-corrected *p* values are used throughout this procedure.

In addressing the second research question, the calculated symmetry values were first examined through visual comparison of individual archaeological sites and their respective MIS through box-and-whisker plots. These plots are then supported with calculated coefficient of variation (CV) values for each MIS. Together, these two methods should indicate if increasing standardisation in biface symmetry is observed. To examine if the interglacials have different distributions in symmetry values, a Shapiro-Wilk normality test was first performed for each MIS, with a suitable test for significance then conducted. As four groups feature non-normal distributions, a Kruskal-Wallis test was performed, followed by pairwise Wilcoxon ranked sum tests.

Finally, in addressing the third research question, and the underlying relationship between biface shape, size and symmetry, the first five sources of shape variance were first examined in relation to the calculated symmetry values through Pearson's productmoment correlation and visual examination of the scatterplots. The length measurements were then examined against the calculated symmetry values, and the major principal components, also through Pearson's product-moment correlation and visual examination of the produced scatterplots.

Through this exploratory and analytical framework, diachronic changes in biface shape and symmetry were examined, with the underlying influence of biface size determined.

All graphics and analyses within this text were produced with the help of Momocs v.1.2.9 (Bonhomme et al. 2014), tidyverse v.1.2.1 (Wickham 2009) and cowplot v.0.9.3

(https://github.com/wilkelab/cowplot) for the R environment (R Development Core Team 2014). In encouraging greater data transparency, guidelines from Marwick (2017) were undertaken to ensure that analyses are replicable. We therefore include the .tps file, the necessary metadata (in .csv format) and the R script used for this article. A copy of all the necessary files can also be found on the Open Science Framework (https://osf.io/td92j/).

## Results

When the outlines are examined through EFA-PCA, the first two principal components (theoretical sources of shape variation) account for 78.75% cumulative variance, with the first 21 principal components accounting for 99% cumulative shape variance. In their transformation, the first principal component reflects shape changes from narrow and more-pointed biface shapes to rounded and more-circular biface shapes, with the second principal component extending from narrow-based biface shapes to triangular biface shapes. The third principal component (7.74% cumulative shape variance) represents the first shape change based on asymmetric differences (see the PCContrib function in the R script for more information).

With respect to how these components manifest differences in shape over time, the principal component plot (Fig. 1) demonstrates considerable difference between certain interglacial periods, in their clustering and spatial configuration. Visual inspection of the EFA-PCA highlights considerable overlap in the shape distribution (among the first two principal axes) of examples dating from MIS 9 and MIS 7 (with more positive PC1 and PC2 values), and similarity between the earliest examples of bifaces within the dataset (MIS 13), and examples from Lynford (MIS 4/3). In their totality, on the basis of the first two components, there is increasing shape variance over each period until MIS 4/3.

Through further examination of principal component scores, for the first two axes (Fig. 2a, c), similarities between bifaces in MIS 9 and MIS 7, and examples in MIS 13 and MIS 4/3 are further highlighted. In both examples, MIS 13 bifaces have the least variation in PC1 and PC2 scores, exemplifying a more standardised shape. When examined on an individual site level (Fig. 2b, d), the high degree of shape standardisation at Boxgrove, and to a lesser extent at Warren Hill, can be observed.

Through an assessment of the first 21 principal components (99% cumulative shape variance), a MANOVA was performed to test for statistical significance between the different interglacial periods and their respective shape variance. Through this, statistical significance below the designated 1% significance threshold was observed (*Hotelling-Lawley*: 0.5847, *F*: 3.0733 p < 0.0001). When examined further through Hotelling *t* tests (Table 2), statistical significance to the designated threshold was observed between all possible combinations demonstrating differences in the shape variance of all interglacial periods. Interestingly, when the first 21 principal components are examined through a discrimination analysis (with leave-one-out cross-validation), only 36.11% of all bifaces (169/468) could be correctly classified to their respective MIS. In their totality, the MANOVA and discriminant analysis demonstrate that while each interglacial period features statistically significant group variance, with distinct trends in specific shapes for each period, degrees of overlap indicate that absolute



Fig. 1 An exploration of biface shape and Marine Isotope Stage (MIS) through an elliptic Fourier principal component analysis (EFA-PCA). Confidence ellipses are here set to two-thirds (66.66%)

period-specific shapes cannot be inferred. For more information on both the MANOVA and discriminant analysis (for each MIS and site), refer to the R script.

In examining biface symmetry, calculated as the AD harmonic coefficients divided by their amplitude, a unimodal asymmetric distribution with moderate skewness is observed for all examples, with the majority of bifaces centred on roughly 0.95 (95%) symmetry (Fig. 3a). In better understanding what this score and distribution refers to, see Fig. 4.

When symmetry investigated through their respective interglacial period (Fig. 3b), examples in MIS 13 and MIS 4/3 feature higher median symmetry values than the collective median. Interestingly, throughout the intermediate periods, greater variation in the quartile range and low median symmetry values for each MIS are observed. On an individual site level (Fig. 3c), the temporal trend in increasing asymmetry until MIS 4/3 is again noted, with high levels of symmetry noted at Broom, Boxgrove, Warren Hill and Lynford, and greater variation and thus greater asymmetry in MIS 7 examples. Descriptive statistics of the calculated symmetry values (Table 3) further support a trend in the British Acheulean of increasing asymmetry until the end of the Middle Palaeolithic, with decreased symmetry means, lower minimum symmetry values and higher standard deviations and CVs for MIS 11, MIS 9 and MIS 7.

A non-parametric Kruskal-Wallis rank-sum test demonstrated that statistical significance was observed when biface symmetry values are assessed in relation to MIS (*Chisquared*: 63.104, *df*: 4, p < 0.0001. In further detail, a Wilcoxon rank sum test (Table 4) demonstrates that MIS 13 cannot be differentiated from MIS 4/3 biface symmetry levels but can be differentiated from the intermediate interglacial periods.

Through Pearson's product-moment correlation of the main sources of shape variance and calculated symmetry values, no linear relationship between shape and symmetry for the first two principal components can be observed. For later principal components (Fig. 5), extreme values are associated with greater asymmetry. In their totality, the correlation-based analyses demonstrate that the main sources of biface shape variation throughout the British Acheulean are reflected in symmetric shape changes.

Finally, to understand the underlying factor of size in the shape and symmetry of British Acheulean bifaces, product-moment correlations were performed (Fig. 6). A product-moment correlation of size and symmetry reveals statistical significance to the 0.01 alpha level, specifically that larger bifaces often feature higher symmetry levels (*t*: 3.28, df = 466, *p*: 0.0011, slope: 0.1502). Furthermore, the first two major sources of shape variation (the extension from rounded to pointed shapes and from narrow-based to triangular shapes) were both found to be statistically significant.

## Discussion

This paper performed a two-dimensional GMM framework on a large biface dataset to quantify and investigate biface symmetry and shape through the British Acheulean. Specifically, this paper aimed at examining whether biface shape and symmetry became increasingly standardised through time, with the late Middle Palaeolithic site of Lynford acting as a point of comparison. Questions of specific



**Fig. 2** An exploration of the first two principal component scores through box-and-whisker plots (Tukey style) for both period ( $\mathbf{a}$ ,  $\mathbf{c}$ ) and individual sites ( $\mathbf{b}$ ,  $\mathbf{d}$ ). Site order correlates with Marine Isotope Stage (MIS) and does not reflect a strict chronological order

biface shape linked to particular MIS periods, and the role of size in biface shape and symmetry were also explored.

The analytical framework chosen highlighted considerably high levels of symmetry in MIS 13, reinforcing previous studies examining Acheulean symmetry (McNabb and Cole 2015; Iovita et al. 2017; McNabb et al. 2018; White and Foulds 2018), followed by increasing asymmetry. The recorded variation in symmetry, equivalent to Boxgrove, does not appear (through the above sites) until the late Middle Palaeolithic. A similar pattern is noted for shape variance, with greater standardisation in biface shape documented in MIS 13 and again in MIS 4/3, while decreasing shape standardisation was noted in MIS 11, in MIS 9 and MIS 7. Despite these diachronic changes, the statistical differences between the respective interglacial periods through discriminant analyses demonstrate that *individual shapes* are poor indicators of particular MIS periods. Further investigations highlighted that the main sources of shape variation are associated with changes in symmetry, and that specific shapes are associated with different sizes (Fig. 6).

**Table 2** A MANOVA pairwise table (with Bonferroni-corrected *p* values) of 99% cumulative shape variance (first 21 principal components) tested with respect to Marine Isotope Stage (MIS); significance codes: less than 0.0001 = `\*\*`; less than 0.001 = `\*\*`; greater than 0.01 = ``

	MIS 13	MIS 11	MIS 9	MIS 7	MIS 4/3
MIS 13		***	***	***	***
MIS 11			**	*	***
MIS 9				*	***
MIS 7					***



Fig. 3 An examination of symmetry (AD harmonic coefficients/amplitude) through a histogram (a), and two box-and-whisker plots (Tukey style) examining symmetry against individual Marine Isotope Stage (b), and against individual sites (c)

An analysis of biface shape highlights similarities in the main sources of shape variance to that noted in other studies which have examined biface datasets through a GMM framework (Iovita and McPherron 2011; Serwatka 2015). In this, it is perhaps



Fig. 4 Three shapes depicting the variation in symmetry throughout the dataset (as calculated through the AD harmonic coefficients divided by their amplitude)

beneficial for future studies to develop a grammar, and a language of categorising bifaces, based on the observed changes in GMM analyses, and away from traditional shape-based typologies (e.g. Wymer 1968).

Unexpectedly, our analysis also highlights an observation first noted in the linear morphometric analyses by Roe (1969), and recently developed by Bridgland and White 2015; White and Bridgland 2018), of *biface shape trends* and their pertinence as potential cultural markers. While specific shapes could not be attributed to distinct MIS periods of the Acheulean, the analysis highlighted differences in MIS-specific shape variation, with a preference for more pointed biface shapes from MIS 9 onwards. Exceptions to this trend do exist, the more positive PC scores indicate more rounded examples at Broom for example; however, this study further highlights the appropriateness of long-standing biface classificatory schemes (see White and Bridgland 2018 for more information).

Investigations into the nature of shape and symmetry in each interglacial period may allude to the importance of on-site accumulation and the time-depth of each archaeological site. In instances of higher symmetry and shape standardisation, for example Boxgrove and Lynford, horizons are in situ and are thought to represent strict contemporaneous events, representing a few generations at maximum (Boismier et al. 2012; Roberts and Parfitt 1999). In contrast, many archaeological sites with high asymmetry and shape variance seem to relate more to secondary context sites and palimpsests, representing the accumulation of artefacts over thousands or even tens of thousands of

MIS	Symmetry (AD/	Symmetry (AD/amplitude)					
	Minimum	Maximum	Mean	Std. Dev.	CV		
13 (99)	0.898	0.981	0.951	0.017	1.76		
11 (115)	0.807	0.981	0.939	0.026	2.81		
9 (119)	0.824	0.982	0.935	0.027	2.90		
7 (87)	0.836	0.979	0.925	0.028	3.09		
4/3 (48)	0.899	0.976	0.950	0.017	1.82		

Table 3 Descriptive statistics of symmetry values for each MIS (sample size in subscript)

**Table 4** A non-parametric pairwise Wilcoxon rank sum test (with Bonferroni-corrected p values) for symmetry values and with respect to Marine Isotope Stage (MIS); significance codes: less than 0.0001 = `\*\*`; less than 0.001 = `\*\*`; greater than 0.01 = ``

	MIS 13	MIS 11	MIS 9	MIS 7	MIS 4/3
MIS 13		**	***	***	_
MIS 11			_	*	_
MIS 9				_	*
MIS 7					***

years (McNabb 2007; McNabb and Cole 2015). While site-formation processes can only be proxies for accumulation, and durations cannot be credibly estimated, one must not rule out the influence of deposition in understanding potential biface variability, a point also highlighted by Moncel et al. (2015). Crucially, if reworking from higher/ older deposits can be eliminated, a palimpsest in this context can be of advantage as it samples a range of potential variability across a given time period (for example, the duration over which a river terrace accumulates). Further work is necessary to better understand the role of this potentially important factor and the overall impact on how researchers interpret site assemblages.

This study exemplifies the interpretive potential of large biface datasets through an exploratory and analytical GMM framework and supports previous interpretations (e.g. Saragusti et al. 2005; Cole 2015; McNabb et al. 2018; White and Foulds 2018) using an



Fig. 5 Scatterplots (with smoothed conditional means) for the five principal components assessed against symmetry (AD harmonic coefficients/amplitude)



Fig. 6 Scatterplots (with smoothed conditional means) for size and symmetry (a) and the three major sources of shape variation (b-d)

independent methodology, that symmetry does not seem to be consistently present through the Acheulean. The key to identifying diachronic changes in symmetry is to identify trends in the shift in the medians and interquartile ranges of assemblages constrained by tight temporal frameworks such as in the British Middle Pleistocene. The importance of the interpretative frameworks (White and Bridgland 2018; White and Foulds 2018) currently being applied to the British sequence is that they provide a behavioural explanation for the increase in diversity (handaxe shape and symmetry) seen in the British late Middle Pleistocene.

Through the integration of other early biface sites and a more nuanced understanding of site accumulation and its relationship with hominin occupation and behaviour, the Acheulean can be better quantified and understood. This in turn provides a platform for testing many of the earlier publications discussing the behavioural 'meaning' of these morphological attributes.

## Conclusion

Through an exploratory and analytical GMM analysis of a large biface dataset, it has been possible to examine the nature of diachronic change in biface shape and symmetry through the British Acheulean record. A number of observations were documented, supporting previous views on a high level of shape and symmetry standardisation in MIS 13 and on the inconsistent application of symmetry across the Acheulean time range. This work has also highlighted the variability in symmetry that is present within the British Acheulean record, and alludes to the potential roles of occupation duration, assemblage accumulation and even demography in understanding that variability. However, in understanding the true 'meaning' of biface shape and symmetry, the integration of much larger datasets from mainland Europe, Asia and Africa is now necessary.

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