

RSM‑Based Empirical Modeling and Thermodynamic Analysis of a Solar Flat Plate Collector with Diverse Nanofuids

Ramachandran Thulasiram¹ · S. Murugapoopathi² · S. Surendarnath³ · Beemkumar Nagappan¹ · **Yuvarajan Devarajan4**

Received: 8 September 2023 / Revised: 15 February 2024 / Accepted: 19 February 2024 / Published online: 27 February 2024 © The Author(s), under exclusive licence to Springer Nature Singapore Pte Ltd. 2024

Abstract

As the energy demand for household applications is increasing, the utilization of solar energy becomes important in fulflling the energy needs of electrical and thermal appliances. Harvesting the energy from solar through solar thermal energy systems will be effectively used in household and industrial heating applications where the consumption of electrical energy is predominant. Solar thermal energy is harvested through simple devices like fat plate collectors but involves many challenges. Solar flat plate collectors' thermal efficiency is improved by increasing the heat transfer rate by replacing the regular fluids with nanofuids due to their superior thermo-physical properties. Investigators are driven to fnd novel energy and exergy analysis by the challenges in efective heat transfer and conservation by improving it by including gold, alumina, and copper oxide nanoparticles. To investigate the energy efficiency characteristics of solar flat plate collectors (FPC), the experiments are carried out by considering the diferent nanofuids (nanofuids with nanomaterials such as gold (Au) and aluminum oxide (AI_2O_3) as well as copper oxide (CuO) as thermal transport media), flow rates of nanofluids (0.016 kg/s, 0.033 kg/s, and 0.05 kg/s), and with mass fraction of nanoparticles $(0\%, 0.1\%, 0.2\%, 0.3\%, \text{and } 0.4\%)$ in nanofluids as variables, such that the energy efficiency, exergy destruction, second law efficiency, entropy generation, and pressure drop performance indicators. The maximum exergy efficiencies are found with *Au* nanofluids 31.55% and 28.78% at 0.4% mass concentration, which has the enhanced second law efficiency compared to water and other nanofluids. At the same time, exergy destruction is found to be minimum (1183.41 W) for *Au* nanoparticle with 0.4% mass fraction and 0.016 kg/min fow rate. The maximum exergy destruction (1509.95 W) was found in the water with 0% concentration at 0.05 kg/min due to the minimum temperature and base fluid heat flow. The energy efficiency and second law efficiencies are well increased with a slight increase in the pressure drop for the 0.4% mass fraction of Au with Al2O3 and CuO nanoparticles. The DoE-based statistical method, the Box-Behnken method, is employed as an experimental design matrix to develop prediction models for exergy responses and pressure drop characteristics. The models are validated through ANOVA results and verified for the R^2 and R^2_{adj} values (>0.95), and the results are obtained from the models. The results of prediction models are found to have a good correlation with experimental results, and the maximum error between the prediction results and the experimental results is less than 5%. As a future scope, the models are suggested for optimizing the process variables to improve energy efficiency, exergy destruction, and pressure drop objectives.

Keywords Flat plate collector · Nanofuids · Energy and exergy · Renewable energy · Sustainable practices

Nomenclature

- Q_w Heat gained by water (kW)
- m_w Mass flow rate of water circulated (kg/s)
 C_{mw} Specific heat of water (kJ/kg K)
- Specific heat of water (kJ/kg K)
- T_f Final temperature (K)
 T_i Initial temperature (K)
- Initial temperature (K)
- Q_b Heat loss from absorber plate (kW)
- m_b Mass of absorber plate (kg)
- C_b Specific heat of absorber plate (kJ/kg K)
- *QL* Energy leak to surroundings (kW)
- µ Viscosity (Pa-Sec)
- U_t Total overall heat transfer coefficient (W/m² K)
-
- $T_{m,st}$ Mean temperature (K)
 T_a Ambient temperature (Ambient temperature (K)
- η Collector efficiency (%)
- m_{nf} Mass flow rate of nanofluid (kg/s)
- $C_{\textit{nf}}$ Specific heat of nanofluid (kJ/kg K)
- I_r Irradiation per unit area (m²)

⁾ Extended author information available on the last page of the article

Introduction

Day to day rise in energy demand in power sectors motivates the researcher to focus on various renewable energy systems. Reduction in fossil fuels and increasing usage make the researchers fnd alternate resources such as solar, wind, and geothermal biomass (Devarajan et al. [2021](#page-12-0)). Among other renewable energy, solar energy is one of the most promising, and an enormous amount of radiant energy is utilized to meet the daily requirements in a country like India. Solar power is utilized in many forms, like collectors and thermal energy storage, and the developments in fat plate collectors help in utilizing solar heat energy for household applications like water heating, cooking, air conditioning, and power production. The FPC with nanofuids with diferent concentrations and sizes of nanoparticles with base fuid attracted the researchers to improve heat transfer enhancements (Munuswamy and Devarajan [2023\)](#page-13-0). Molecular or atomic movements of particles normally increase the energy flow, but introducing nanofluids with base fluids provides augmented heat transfer characteristics for suitable applications. The superior improvement in thermal conductivity, better surface area, good stability, and great movement with nanoparticles with base fuid was observed. The nanoparticle collision with base fuid increased the surface area for heat transfer heat capacity and temperature gradient among the suspended particles. The nanoparticle size, nanomaterial, and conductivity are important factors in selecting suitable nanofuid for enhancing thermal characteristics (Ramasamy et al. [2023](#page-13-1)).

Rathan Kumar et al. ([2022](#page-13-2)) used fat plate collectors to extract energy and utilize it for diferent purposes, like water distillation plants in remote areas, to improve energy

efficiency by around 2.76% . The optimal performance solar collector was mathematically determined by Chamoli [2013.](#page-12-1) The optimum result was applied to the collector to improve the performance such as outlet temperature, fow rate, heat transfer, and exergy efficiency. The second law efficiency improved at 4% for 0.008 kg/s flow rate with an aperture area of 9 m^2 for an outlet temperature of 360 K as optimum design values. Using mathematical modeling, the non-uniform temperature distribution in FPCs was determined by varying inlet temperature, flow rate, and radiance for analyzing exergy rate and loss. The optimum correlation was obtained by Madhu and Balasubramanian [\(2018](#page-13-3)) for experimental data with statistical modeling. The exergy improvement was obtained as 5.95% with exergy loss of 72.96% variation for non-uniform variation in sun and absorber area for 50 °C entry temperature, 0.05 kg/s mass flow with radiance energy of 800 $W/m²$. Naveenkumar et al. ([2022](#page-13-4)) designed the double side solar still using aluminum and glass wool to improve the exergy rate, heat transfer, and evaporation rate with base fuid water and 0.1% (volume basis) *Cuo*, *ZnO*, and aluminum oxide nanofluids. The energy efficiency of 21.3% , 19.4% , and 17% and exergy efficiency of 50.1%, 36.8%, and 23.8% were improved for the above three nanofuids. The solar FPC with marquise was designed with water and alumina nanofuid (0.1% volume fraction) with varying fow rates from 1 to 5 Lit/min. The exergy and energy efficiencies were determined under varied inlet and outlet temperatures, flow rates, radiation intensity, and atmospheric conditions. The maximum energy and exergy efficiencies of nanofuid mixed with water observed were 28.2% and 34.4% higher than pure water circulation by Arora et al. ([2019](#page-12-2)). Eltaweel and Abdel-Rehim ([2019\)](#page-12-3) designed a lower absorbing capability of solar collectors and better transformation of the energy of the based fuid to improve thermosiphon circulation and carbon nanotubes (10–40 nm diameter) with concentrations of 0.01%, 0.05%, and 0.1% (wt.) with distilled water. The maximum efficiency was attained for nanotubes with 0.1% concentration for 1.5 Lit/min. Circulations were 34.1% with a collector size reduction of 34%, and further forced circulation increased efficiency by 6.2% . The exergy efficiency with nanofluid was improved by 38.21% with distilled water. Verma et al. ([2016\)](#page-13-5) experimentally investigated the solar collector with *MgO* nanofluid with water at various concentrations (0.25, 0.5, 0.75, 1.0, 1.25, and 1.5%) with 0.5, 1.0, 1.5, 2.0, and 2.5 Lit/min, respectively. The thermal and second law efficiency obtained for 0.75% concentration, 1.5 Lit/min fow rate as 9.34% higher, 32.93% improvements with irreversibility of 0.0611W/K. The FPC with *CuO* nanofuid with water was designed and optimized to improve the collector efficiency by varying the tilting angle, nanoparticle size, and heat loss. Sint et al. (2017) (2017) observed that enhancing

the volume concentration by up to 2% led to a corresponding improvement in collectors' efficiency of up to 5% , in comparison to water. Choudhary et al. [\(2020](#page-12-4)) enhanced the thermal properties and stability under varying *MgO* concentrations $(0.04-0.2\%)$ with flow rate $(0.5-2.5 \text{ Lit/min})$. The highest collector efficiency improved at 69.1% , and the energy factor increased by 16.7% with 0.2% concentration at 1.5 Lit/min with the U-V spectroscopy stabilization process. Solar FPC thermo-physical properties were analyzed using carbon nanotubes by Said et al. [\(2016](#page-13-7)) to improve the particle size, temperature, and loading using sodium dodecyl sulfate as a surfactant. The frst and second law efficiency was improved to 95.12% and 26.15% , as water was 42.1% and 8.8%, respectively. The effective utilization of solar energy with nanofuids, thermal coatings, and booster refectors has improved the frst and second law efficiencies using thermal collectors by Murugan et al. ([2022](#page-13-8)). The intensity of radiant energy maximized outlet temperature and thermal performance with fow rate. The chrome and carbon coatings with absorber plates improved thermal efficiency. Notably, the nanoparticle inclusion with base fuid improved the collector's thermal conductivity and efficiency at specified operating conditions. As a future scope, the authors suggested that the impact of the heat conduction route of *Au* and *Cu* and other nanomaterials on the improvements in thermal performance and heat transmission rate of solar thermal collectors must be analyzed.

From the literature survey, it has been identifed that most of the researchers conducted experimental investigations using various nanomaterials like aluminum oxide $(Al₂O₃)$, copper oxide (CuO), cerium oxide (CeO₂), and carbon nanotubes with diferent percentages of mass fraction combinations on the base fuids. The performance was reduced over time, the performance of the fuids was reduced, and the impact of nanomaterials destruction was found to be more in detroiting the base fuid heat transfer characteristics. In such cases, Au is found to be one of the good options as nanoparticles to improve the performance of the base fuid. Also, many researchers discussed three performance parameters: energy efficiency, exergy destruction, second law efficiency and pressure drop in the FPC.

The novelty of the work lies in the systematic exploration and optimization of solar fat plate collectors using a combination of nanomaterials, detailed testing, statistical analysis, and the development of accurate prediction models for practical applications. This research extensively analyzes energy efficiency, exergy destruction, second law efficiency, entropy generation, and pressure drop characteristics of solar FPCut with *Cu*, alumina, and gold nanoparticles-based nanofluids. The nano particle concentrations are varied from 0.1 to 0.5% and with diferent fow rates of nanofuids (0.016–0.05 kg.s). A hypothesis is developed for objectives as empirical models for the response's energy efficiency, energy destruction, second law efficiency, and pressure drop are developed using the response surface method. The models developed are verifed for adequacy and compared with the experimental responses. The detailed discussion on the impact of the variables on the performance parameters was also discussed with future scope.

Fabrication and Testing of Solar Flat Plate Collector with Nanofuids

The solar collector is designed with an occupied area of 2000 mm \times 1000 mm \times 100 mm with an absorption area of 1.9m2 , as shown in Fig. [1.](#page-2-0) The absorber plate is a corrugated sheet made of copper of 0.4-mm thickness. The header pipes are made of copper with 25-mm diameter. The riser tubes are made of copper of 12.5-mm diameter and welded under the corrugated design of the absorber plate. The side and collector bottom are covered with glass wool insulation to avoid heat loss. A glass cover of 4-mm thickness made of toughened glass is placed on the top of the collector.

The specifcations of the solar collector are provided in Table [1.](#page-3-0) To test the performance of the collector with nanofuids, the Al_2O_3 − H_2O , CuO − H_2O , and Au − H_2O nanofluids were prepared with 0.1%, 0.2%, 0.3%, and 0.4% by volume concentration of nanoparticles. In the two-step process, Triton X-100 (surfactant) of 0.02% was mixed with deionized (distilled) water to avoid nanoparticle agglomeration. Followed by blending of Al_2O_3 , *CuO*, and *Au* nanoparticles in the size range of 20–40 nm with water using the ultrasonicator to get homogeneous suspension. The properties of nanofuids prepared and were calculated using the following relations (Eqs. [1](#page-2-1)[–4\)](#page-3-1) (Ramasamy et al. [2023\)](#page-13-1) and are tabulated (Table [2\)](#page-4-0).

$$
\rho_{nf} = \rho_{nf}(\phi) + \rho_{nf}(1 - \phi) \tag{1}
$$

$$
\mu_{nf} = \frac{\mu_{bf}}{(1 - \phi)^{2.5}}
$$
 (2)

Fig. 1 Solar flat plate collector with nanofluids experimental setup

$$
\frac{k_{nf}}{k_{bf}} = \frac{k_{np} + 2k_{bf} + 2(k_{np} - k_{bf})}{k_{np} + 2k_{bf} + (k_{np} - k_{bf})\phi}
$$
\n(3)

$$
C_{p,nf} = C_{p,np}(\phi) + C_{p,bf}(1 - \phi)
$$
\n(4)

The variation of viscosity, specifc heat, density, and thermal conductivity of Al_2O_3 , CuO, and Au nanofluids with diferent nanoparticle concentrations are shown in Table [2](#page-4-0).

Energy and Exergy Analysis of Solar Flat Plate Collector

The maximum work extracted from the system under diferent operating conditions is energy. The energy analysis describes the efectiveness of each device under preferred operating conditions. The energy analysis determines the amount of energy production during its operation. However, at the same time, energy analysis does not describe the quantity of useful energy available or transformed. For optimum utilization of **Table 2** Properties of

concentration

energy, in order to reduce entropy generation, exergy analysis is required. The exergy analysis locates the energy degradation of the device quantitatively. The efficiency improvements are associated with various operating conditions named energy and exergy analysis. The exergy efficiency gained major attention from researchers due to its losses associated with diferent devices. The energy destructed in many forms is called irreversibility caused by friction, pressure drop, mixing, fow rate, radiation, and convective losses in the plate and fuid. The exergy analysis measures the useful energy recoverable from the system and quantifes energy destroyed or entropy generated. The demand for energy, fossil fuel depletion, cost, and thermal system design makes more attention towards energy and exergy analysis to improve optimal energy usage with minimum cost and environmental balance.

Energy Analysis of Solar FPC

Energy and exergy analysis of solar FPC were carried out to discuss the frst and second law analysis of thermodynamics in this study. The first law discusses only efficiency of solar collectors but the losses in various devices like absorber plate, storage tank, solar radiation, and leakage of energy from the solar collectors were dealt with exergy analysis using the following relations (Eqs. [5](#page-4-1)[–12](#page-4-2)).

$$
Q_w = m_w C_{pw} (T_f - T_i)
$$
\n⁽⁵⁾

$$
Q_b = m_b C_b (T_f - T_i) \tag{6}
$$

$$
Q_L = U_t (T_{m,st} - T_a) \tag{7}
$$

$$
T_{m,st} = (T_i + T_f)/2
$$
\n⁽⁸⁾

$$
A = \pi r^2
$$

\n
$$
U_l = U_t + U_b + U_s
$$
\n(9)
\n
$$
U_t = \left[\frac{N}{\sqrt{(T - T_s)^{0.33}}} + \frac{1}{h} \right]^{-1} + \left[\frac{\sigma (T_p^2 + T_a^2)(T_p + T_a)}{\sqrt{(2N + 1)}} \right]
$$

$$
U_t = \left[\frac{1}{C \left(\frac{T_p - T_a}{N + f} \right)^{0.33}} + \frac{1}{h_w} \right] + \left[\frac{1}{(1/\epsilon_p) \left(\frac{2N + f - 1}{\epsilon_g} \right) - N} \right]
$$
(10)

$$
U_b = \frac{k_i}{t_i} \tag{11}
$$

$$
U_s = \frac{A_{cs}k_i}{A_p t_i} \tag{12}
$$

The thermal efficiency of the flat plate solar collector (η) is the ratio of energy storage in the storage tank to the total solar radiation on the collector, which can be expressed as

$$
\eta = m_{nf} C_{nf} (T_f - T_i) / (I_T A_p)
$$
\n(13)

Collector efficiency factor (F') is given by the relation

$$
F\prime = \frac{1/U_l}{W\left\{\frac{1}{U_l[D+(W-D)F]} - \frac{1}{\pi Dh}\right\}}\tag{14}
$$

Exergy Analysis of Solar FPC

Exergy is the maximum output that can be achieved relative to the environment temperature. The general equation of the exergy balance is (Eq. [15\)](#page-5-0)

$$
\dot{E}_{in} + \dot{E}_s + \dot{E}_{out} + \dot{E}_l + \dot{E}_d = 0
$$
\n(15)

The inlet exergy rate measures the fluid flow and the absorbed solar radiation rate. The inlet exergy rate with fuid flow can be calculated by Sarhaddi et al. ([2010](#page-13-9)) using the following relation (Eq. [16](#page-5-1)).

$$
\dot{E}_{in,f} = \dot{m}C_p \{ T_{in} - T_a - T_a \ln(T_{in}/T_a) \} + (\dot{m} \Delta P_{in}/\rho) \tag{16}
$$

where ΔP_{in} is the pressure difference of the fluid with the surroundings at entrance and *r* is the fluid density.

The absorbed solar radiation exergy rate is calculated as:

$$
\dot{E}_{in,Q} = \eta I_T A_p (1 - (T_a - T_s) \tag{17}
$$

T is apparent sun temperature and equals to 75% of blackbody temperature.

Total inlet exergy rate of the solar collector can be calculated as:

$$
\dot{E}_{in} = \dot{E}_{inf} + \dot{E}_{in,Q} \tag{18}
$$

At steady state conditions, where the fuid is fowing, the stored exergy rate is zero.

$$
\dot{E}_s = 0 \tag{19}
$$

When only the exergy rate of outlet fluid flow is considered, the outlet exergy rate can be defned as Devarajan et al., [\(2021\)](#page-12-5)

$$
\dot{E}_{out,f} = -\dot{m}C_p \{ T_{out} - T_a - T_a \ln(T_{out}/T_a) \} + (\dot{m}\Delta P_{out}/\rho)
$$
\n(20)

The heat leakage from the absorber plate to the environment can be defned as the leakage exergy rate and calculated.

$$
\dot{E}_l = -UA_p(T_p - T_a) \left[1 - \left(\frac{T_a}{T_p}\right) \right]
$$
\n(21)

where the overall heat loss coefficient U is optimized at $4.6797 \text{ w/m}^2 \text{K}$ (Sarhaddi et al. [2010](#page-13-9)).

The destroyed exergy rate caused by the temperature difference between the absorber plate surface and the sun can be expressed.

$$
\dot{E}_{d,\Delta T_s} = -\eta I_T A_p T_a \left[\frac{1}{T_p} - \frac{1}{T_s} \right]
$$
\n(22)

The destroyed exergy rate by pressure drop is expressed by (Suzuki [1988](#page-13-10)):

$$
\dot{E}_{d,\Delta P} = -\frac{\dot{m}\Delta P}{\rho} \{T_a \ln(T_{out}/T_a)/(T_{out} - T_{in})\}
$$
\n(23)

The destroyed exergy rate caused by the temperature difference between the absorber plate surface and the agent fluid can be calculated from (Suzuki [1988\)](#page-13-10):

$$
\dot{E}_{d,\Delta T_f} = -\dot{m}C_p T_a \left[\ln \left(\frac{T_{out}}{T_{in}} \right) - \frac{T_{out} - T_{in}}{T_p} \right]
$$
(24)

So, the total destroyed exergy rate can be calculated from:

$$
\dot{E}_d = \dot{E}_{d,\Delta T_s} + \dot{E}_{d,\Delta P} + \dot{E}_{d,\Delta T_f}
$$
\n(25)

The exergy destruction rate can also be expressed from:

$$
\dot{E}_d = T_a \dot{S}_{gen} \tag{26}
$$

where *S gen* is the overall rate of entropy generation and can be calculated from (Bejan [1996](#page-12-6))

$$
\dot{S}_{gen} = \dot{m}C_p \ln(T_{out}/T_{in}) - \dot{Q}_s / T_s + \dot{Q}_o / T_a \tag{27}
$$

where Q_S is solar energy absorbed (W) by the collector surface as expressed.

$$
\dot{Q}_s = I_T(\tau \alpha) A_p \tag{28}
$$

And Q_O is the heat loss to the environment (W),

$$
\dot{Q}_o = \dot{Q}_s - \dot{m}C_p(T_{out} - T_{in})
$$
\n(29)

Ultimately, combining all the expression above, the exergy efficiency equation of the solar collector can be analyzed (Sarhaddi et al. [2010](#page-13-9)):

$$
\eta_{ex} = \frac{\dot{m} \left[C_p \left[T_{out} - T_{in} - T_a \ln(T_{out}/T_{in}) \right] - \left(\frac{\Delta P}{\rho} \right) \right]}{\left[I_T A_p (1 - \left(\frac{T_a}{T_s} \right) \right]}
$$
(30)

Empirical Modeling of Energy, Exergy, and Pressure Drop in FPC

To avoid the computational cost of complex engineering problems with high-fdelity simulations and recursive experimental investigations, using empirical models is the surrogate in keeping the engineering designs explorable given the design space. Statistical techniques are highly preferred in developing empirical models for problems where a smaller number of experiments are possible and where the responses are to be generated with no direct dependency on the variables. A set of combinational parameters from the range of variables is plugged into the empirical model to quickly estimate the responses without conducting the complete analysis. Box-Behnken Design (BBD) is a kind of statistical technique used in the response surface methodology (RSM) and is specially designed to ft second order mathematical model. The BBD is an independent and quadratic design that contains fractional factorial design, and the treatment of the model is a combination of midpoints and edges of problem space (Demirpolat et al. [2021\)](#page-12-7). The BBD designs are almost rotatable orthogonal designs made of three, four, and fve-level factors that fx the mid-point between the lowest and highest values of the range provided. Including center points in the BBD helps estimate the coefficients for the second-order model by making rotatable designs. Due to this use of face-centered and rotatability of design heredity, the BBD requires a meager number of experimental runs to achieve the empirical model. To generate the BBD and develop the response functions for the problem defned in this article, a standard statistical package, Minitab 17, is used. The Minitab handles a wide set of available data for tasks like data consolidation, analysis, and reporting. Also, from past research, the DoE is more accurate, consistent, and simpler than traditional manual estimation techniques. The set of three-level experimental orthogonal blocks is created using the BBD, for which a second-order full quadratic can be ftted for the response surface model. To investigate the exergy analysis on the solar fat plate collector and to create a hypothesis, the energy efficiency (first law efficiency), exergy destruction, second law efficiency (η_{II}) , and pressure drop (ΔP) were considered as responses. The design matrix is generated using BBD for the variables of nanofuids, the mass fraction of the nanoparticles, and the mass fow rate of the nanofuids as per the range shown in Table [3.](#page-6-0) The design matrix contains 20 experiments generated (Table [4](#page-7-0)) within the range of variables considered. The experiments are conducted on the solar fat plate collector to determine the energy efficiency, exergy destruction, second law efficiency, and pressure drop for the 20 experiments defned by the BBD. The results of the experiments of BBD are analyzed for the model development and verifed for the model adequacy. The signifcance of the RSM quadratic models developed and tested through ANOVA for the *Fisher* test and *P*-test. The results of ANOVA for the quadratic models energy efficiency, exergy destruction, second law efficiency, and the pressure drop are shown in Table [4](#page-7-0).

The development of empirical correlations using the Minitab 17 (DoE) software was carried out through the following steps.

Step 1: Selection and fnalization of the design variables and their ranges (Table [3\)](#page-6-0)

Step 2: Selection of the appropriate DoE model from the Minitab 17 software, according to the level of the ranges

Table 3 The range of variables for the exergy analysis

Parameter	Range	
	Min	Max
Nanoparticle fraction, NF	0	2
Mass fraction, MF $(\%)$	$_{0}$	0.4
Flow rate, FR (kg/s)	0.016	0.05

available. Considering all three variables and their possible range levels, a three-factor, three-level, face-centered, nearly rotatable Box-Behnken design was chosen.

Step 3: Using the chosen design, the experiment uncoded experimental design matrix was generated, containing 20 diferent sets of experiments.

Step 4: The respective set of experiments is conducted to determine responses that require empirical correlations. Step 5: Simulate the results of the responses and conduct the ANOVA test, *P*-test, and *F*-test to verify the R^2 and R_{adj}^2 values to confirm the fitness of the experimental results for the respective responses.

Step 6: Develop the empirical correlations from the respective coefficients table and verify the responses obtained from the correlations for a set of variables within the range defned.

The empirical prediction equation is generated based on infuencing variables with a 95% confdence level, and the adequacy of the model is tested through ANOVA of each response (Table [4\)](#page-7-0). The *p* value represents the degree of confidence level of coefficients, and the correlations are assessed for the closeness to a 95% probability level. In the ANOVA, *p* values for frst-order and second-order parameters of response should be less than 0.05 and are deemed to be relevant. If the *p* value is beyond 0.05, it is considered insignifcant on both frst and second-order parameters and hence omitted from the approximation function. In this model generated, the parameters for all the responses are found to be signifcant as the *p* values are found to be less than 0.005.

The ANOVA table fndings also provided the testing regression parameters R^2 and R_{adj}^2 used to test the model suitability and validate the model for prediction efficiency. The R^2 is obtained from the regression variables that minimize the variation in the prediction model. If the value is closer to unique, the model completely complies with the data experimented with and is identifed as more precise. The R^2 and R^2 _{adj} values of the energy efficiency, exergy destruction, second law efficiency, and pressure drop in the prediction regression models are closer to one. They can forecast the characteristics of the responses for the set of design variables in their defned range. Based on the coefficients obtained from the models, the prediction models (Eqs. [27](#page-5-2)[–30](#page-5-3)) are developed for the response parameters and used to predict the approximate responses. The experimental results shown in Table [5](#page-8-0) and the second-order regression equation representing the energy efficiency, exergy destruction, second law efficiency (η_{II}), and pressure drop (ΔP) are expressed as a function of the parameters of the collector (Eqs. [31–](#page-8-1)[34,](#page-8-2)). Using the quadratic polynomial model, the relationship between responses and the responses is obtained in actual units. The responses from the prediction model

Table 4 RSM design matrix and the comparison of experimental and predicted results

Table 5 Model adequacy for fitting of second-order model

results show that the responses obtained from the regression model agree with experimental responses (Table [4\)](#page-7-0), and the error between the results falls within 5%.

Energy efficiency =
$$
0.31689 - 0.01186I * NF + 1.2409 * MF
$$

$$
+ \, 2.307 * FR + 0.01824 NF * NF - 2.1027
$$

$$
* MF * MF + 58.25 * FR * FR + 0.08829NF
$$

$$
* MF - 0.5211 * NF * FR - 4.744 * MF * FR
$$
 (31)

Exergy destruction = $1369.10 - 9.60 * NF - 670.1 * MF$

$$
+ 6980 * FR - 18.21 * NF * NF + 560.4
$$

\n
$$
* MF * MF - 96056 * FR * FR - 105.07
$$

\n
$$
* NF * MF + 1243.9 NF * FR + 6763
$$

\n
$$
* MF * FR
$$
 (32)

Second Law efficiency $\eta_{II} = 0.27510 + 0.00680 \text{ NF} + 1.3138$

$$
* MF - 11.297 * FR + 0.03336 * NF * NF
$$

- 1.1093 * MF * MF + 157.09 * FR * FR
+ 0.19592 * NF * MF - 1.9712 * NF * FR
- 13.924 * MF * FR
(33)

Pressure drop $\Delta P = 1168 - 7713$ NF + 345 $*$ MF + 173531

$$
* FR + 3794 * NF * NF + 1967 * MF * MF
$$

$$
- 2338560 * FR * FR + 27846 * NF * MF
$$

$$
+4117 * NF * FR + 201477 * MF * FR
$$
 (34)

Results and Discussions

Efect of Mass Fraction on Thermal Conductivity

The first and second law efficiencies mainly depend on the conductivity of nanofuids. Figure [2](#page-8-3) shows the variation in mass fraction of diferent nanofuids with thermal conductivity. The conductivity of nanofuids increases with an increase in mass fractions. The suspended nanoparticles tend to increase the conductivity of the base fuid with an increase in mass fractions. The thermal conductivity of

Fig. 2 Variation in thermal conductivity with mass fraction

Fig. 3 Variation in energy efficiency with mass fraction

nanofluids variation of *Au* is higher than CuO and Al_2O_3 due to diameter, porosity, nanomaterial, and mass fraction (Said et al [2016\)](#page-13-7). The temperature variation with solar radiation improves the thermal conductivity of various nanofuids due to molecular dispersion and density variation (Murugan et al. [2022](#page-13-8)).

The mass fraction of different nanofluids with energy efficiency is given in Fig. 3 . The energy efficiency is one factor in identifying the losses in energy in diferent forms. The energy efficiency improved with temperature and mass fraction of nanofuid concentration. However, the improved mass concentration increased fuid viscosity prominently to intensify the frictional losses. The variation in solar energy radiation varies with the volume fraction of various nanoparticles that could improve the efficiency of collectors. By experiment, the maximum energy efficiency for FPC is found to be 6.34% and 8.41% higher for 0.3% Au mass fraction based Al_2O_3 and CuO nanofluids. Further improvements in mass fraction increased the viscosity of various nanofluids, which decreased the energy efficiency. At the same time, the energy efficiencies obtained from the empirical correlations for 0.3% Au mass fraction are found to be 6.29% and 8.481% for the Al_2O_3 and CuO nanofuids. This shows the closeness of the results of the prediction model.

Efect of Mass Fraction on Pressure Drop

The pressure variation with a combination of nanofuid concentration for various mass fractions is given in Fig. [4.](#page-9-0) The increase in mass concentration increases the viscosity of the nanofuids, which gives resistance to the fuid movements. The fow resistance increases the pumping power, but at the same time, it improves the heat transfer rates of diferent nanofuids. The *Au* nanoparticle pressure drop was higher than other nanofuids with diferent mass concentrations. There was an improvement in heat transfer with pressure drop due to increased nanoparticle concentration, density, and decrease in velocity (Bayareh [2022\)](#page-12-8).

Fig. 4 Variation in pressure drop with mass fraction

Fig. 5 Variation in outlet temperature with mass fraction

Efect of Mass Fraction on Outlet Temperature

Figure [5](#page-9-1) shows the outlet temperature of different nanofluids with mass concentrations of Au, CuO , and Al_2O_3 . The outlet temperature is the one key parameter that directly affects solar collectors' energy efficiency under varying operating conditions. The variation in nanoparticle concentration with water improves the outlet temperature of the fuids in solar collectors. The Au nanoparticle maximum outlet temperature was 3.92% and 5.74% higher than 0.4% mass concentration *CuO* and Al_2O_3 .

Effect of the Mass Fraction on Exergy Efficiency

The second law efficiency of various nanofluid concentrations with diferent nanoparticles is shown in Fig. [6.](#page-9-2) The exergy efficiency mainly depends on the mass

Fig. 6 Variation in exergy efficiency with mass fraction

concentration, size, and nanoparticle material. The *Au* nanoparticle performance was higher than other nanofuids, and an increase in mass concentration improved the collector efficiency due to the maximum heat flow rate. The maximum exergy efficiency of *Au* was 31.55% and 28.78% higher than Al_2O_3 and *CuO* at 0.4% mass concentration. The enhanced second-law efficiency of Au nanoparticles in solar collectors may improve the collectors' performance compared to water and other nanofluids (Kumar et al. [2020](#page-13-11)).

Efect of the Mass Fraction on Entropy Generation

The entropy generation is the reverse of the exergy efficiency of solar collectors, and the cause of irreversibility is due to the friction and pressure losses associated with the entropy generation of various nanoparticles. The nanoparticle mass fraction of Au, CuO , and Al_2O_3 with entropy generation is presented in Fig. [7](#page-10-0). The Au nanoparticle mass concentration varies from 0 to 0.4%, decreasing the entropy generation by 9.15% due to improved heat transfer and outlet temperature variation. For CuO and Al_2O_3 nanoparticle, the entropy generation decreases by 6.45% and 5.39% for the same operating conditions. The increased thermal conductivity and improved heat fow greatly decreased the entropy generation in solar collectors. At lower mass concentrations, the entropy generation increased due to the time the base fuid and absorber plate took to conduct heat (Bejan [1996](#page-12-6)).

Efect of the Mass Fraction on Exergy Destruction

The exergy destruction of various nanofuids with mass concentrations is shown in Fig. [8.](#page-10-1) The exergy destruction decreases with an increase in mass concentration due to the particle's nanoparticle size, nanomaterial, and heat capacity.

Fig. 7 Variation in entropy generation with mass fraction

Fig. 8 Variation in exergy destruction with mass fraction

The minimum destruction found for 0.4% mass fraction of *Au*, *CuO*, and *Al*₂*O*₃ was 1323.86 W, 1418.2 W, and 1319.38 W, respectively, due to improved outlet temperature and enhanced heat fux in the absorber plate due to nanoparticle concentration. The maximum exergy destruction was found for water at 0% concentration as 1509.95 W due to more heat required for heating water without nanoparticle concentration. Exergy destruction decreases with increased mass fraction of various nanoparticles due to density variation, collector intensity, and fuid friction caused concentration and viscosity of various nanofuids (Dharmalingam et al. [2017](#page-12-9)).

Efect of System Variables on Responses

The effect of the variables on the responses particular regions of interest on responses is analyzed through response surfaces. Figure [9](#page-10-2) shows the variation in the surface plot of pressure drop, mass flow rate, and mass fraction for the averaged mass concentration of various

Fig. 9 Surface plot of pressure drop against the fow rate and mass fraction %

Fig. 11 Surface plot of second law efficiency (η_{II}) against the flow rate and mass fraction %

nanoparticles. Pressure drop increases with mass concentration and particle size increase and optimum at 0.03 kg/ min flow rate. Figure 10 shows the surface plot of energy efficiency with flow rate and mass fraction for the averaged

Fig. 12 Surface plot of energy destruction against the fow rate and mass fraction %

mass concentration of diferent nanoparticles. The collectors' efficiency improved with nanoparticle concentration and flow rate (Seralathan et al. 2023). The optimum efficiency was obtained for Au nanofuid with 0.2% concentration and 0.05 kg/s. The outlet temperature and heat flow improved with nanoparticle mass concentration and fow rate. The second law of efficiency depends on solar collectors' flow rate, particle concentration, and outlet temperature (Singh and Yadav [2022](#page-13-13)). Figure [11](#page-11-1) shows the second law efficiency with flow rate and mass fraction of Au, CuO, and Al_2O_3 nanofluids. The maximum exergy efficiency was 63.63% for Au nanofluid with 0.016 kg/s at 0.4% mass fraction. The *Au* nanoparticle shows superior behavior to other nanoparticles due to its thermal conductivity and specifc heat capacity (Khosravi et al. [2022\)](#page-12-10). Figure [12](#page-11-2) shows the surface plot of exergy destruction with fow rate and mass fraction of diferent nanoparticles. Exergy destruction decreases with increasing nanoparticle concentration and mass fow rate of nanofuid (Mahdavi et al. [2022\)](#page-13-14). The minimum exergy destruction observed was 1183.41 W for *Au* nanoparticle with 0.4% mass fraction and at 0.016 kg/

min fow rate. The maximum exergy destruction of 1509.95 W was found for water at 0% concentration at a flow rate of 0.05 kg/min due to lower temperature and base fuid heat flow than the nanoparticle (Dharmalingam et al. [2017](#page-12-9)).

Conclusion

The study conducted a comprehensive analysis of energy and exergy on fat plate collectors using water-based Au, CuO, and Al_2O_3 nanofluids with varying mass fractions and flow rates. The empirical correlations developed for energy efficiency, exergy destruction, second law efficiency, and pressure drop using a response surface methodology (RSM) approach were found to predict the responses for the defned variables with an error of less than 5%. The study identifed that the addition of nanoparticles, particularly 0.4% mass fraction of Au with Al_2O_3 and CuO, showed improved second law efficiencies of 31.55% and 28.78%, respectively. It was observed that the pressure drop increased with the addition of nanoparticles, with a higher pressure drop in nanofuids with Au nanoparticles. The energy efficiency of the collector improved significantly with a maximum of 0.2% nanoparticle concentration, particularly with Au nanoparticles at 0.2% mass fraction, showing the maximum energy of 72.96% compared to other combinations. Furthermore, the study inferred that the use of nanoparticles in fat plate collectors improved heat transfer and energy efficiency with minimum entropy generation by increasing fow rates. The Au-based nanofuids with 0.2% mass fraction and at a mass fow rate showed comparatively better heat transfer rate and entropy generation.

The fndings of this study are signifcant as they provide valuable insights into the impact of nanofuids on the performance of fat plate collectors. The results demonstrate the potential for significant improvements in energy efficiency and heat transfer rates by utilizing nanofuids, particularly with specific mass fractions and flow rates. These findings are consistent with previous research that has highlighted the improved thermal efficiency of flat plate solar collectors when conventional heat transfer fuids are replaced with nanofuids. The study's emphasis on the reduction of entropy generation and the enhancement of energy efficiency aligns with the broader goal of optimizing the parameter for maximizing energy efficiency and second law efficiency while minimizing exergy destruction and pressure drop in solar collector systems. This research contributes to the understanding of the thermal performance enhancement of fat plate solar collectors using nanofuids, particularly in terms of energy efficiency, exergy destruction, and second law efficiency. The fndings underscore the potential for signifcant improvements in heat transfer and energy efficiency by leveraging nanofluids, thereby offering valuable insights for the optimization of solar collector systems in the future.

Author Contribution Murugapoopathi S and Ramachandran T conceived the idea of the work.

Beemkumar Nagappan and Yuvarajan Devarajan designed the experiments.

Surendarnath S supervised the study.

Data Availability The datasets used and/or analyzed during the current study are available from the corresponding author upon reasonable request.

Code Availability Not applicable.

Declarations

Ethics Approval and Consent to Participate Not applicable.

Consent for Publication Not applicable.

Competing Interests The authors declare no competing interests.

References

- Arora S, Fekadu G, Subudhi S (2019) Energy and exergy analysis of marquise shaped channel fat plate solar collector using Al2O3– water nanofluid and water. J Solar Energ Engg 141(4). [https://doi.](https://doi.org/10.1115/1.4042454) [org/10.1115/1.4042454](https://doi.org/10.1115/1.4042454)
- Bayareh M (2022) Exergy analysis of solar chimney power plants: a review. Sustain Energy Technol Assess 53:102568. [https://doi.org/](https://doi.org/10.1016/j.seta.2022.102568) [10.1016/j.seta.2022.102568](https://doi.org/10.1016/j.seta.2022.102568)
- Bejan A (1996) Entropy generation minimization: the new thermodynamics of fnite-size devices and fnite-time processes. J Appl Phys 79(3):1191–1218. <https://doi.org/10.1063/1.362674>
- Chamoli S (2013) Exergy analysis of a fat plate solar collector. J Energ South Africa 24(3):8–13. [https://doi.org/10.17159/2413-3051/](https://doi.org/10.17159/2413-3051/2013/v24i3a3137) [2013/v24i3a3137](https://doi.org/10.17159/2413-3051/2013/v24i3a3137)
- Choudhary S, Sachdeva A, Kumar P (2020) Investigation of the stability of MgO nanofuid and its efect on the thermal performance of fat plate solar collector. Renew Energy 147:1801–1814. [https://](https://doi.org/10.1016/j.renene.2019.09.126) doi.org/10.1016/j.renene.2019.09.126
- Demirpolat AB, Aydoğmuş E, Arslanoğlu H (2021) Drying behavior for Ocimum basilicum Lamiaceae with the new system: exergy analysis and RSM modeling. Bio Conver Biorefne 12(2):515– 526.<https://doi.org/10.1007/s13399-021-02010-x>
- Devarajan Y, Nagappan B, Choubey G, Vellaiyan S, Mehar K (2021) Renewable pathway and twin fueling approach on ignition analysis of a dual-fuelled compression ignition engine. Energ & Fuels 35:9930–9936.<https://doi.org/10.1021/acs.energyfuels.0c04237>
- Devarajan Y, Nalla BT, Babu MD, Subbiah G, Mishra R, Vellaiyan S (2021) Analysis on improving the conversion rate and waste reduction on bioconversion of Citrullus lanatus seed oil and its characterization. Sustain Chem Pharm 1;22:100497
- Dharmalingam R, Kandasamy R, Sivagnana Prabhu KK (2017) Lorentz forces and nanoparticle shape on water based Cu, Al 2 O 3 and SWCNTs. J Mol Liq 231:663–672. [https://doi.org/10.1016/j.](https://doi.org/10.1016/j.molliq.2016.11.048) [molliq.2016.11.048](https://doi.org/10.1016/j.molliq.2016.11.048)
- Eltaweel M, Abdel-Rehim AA (2019) Energy and exergy analysis of a thermosiphon and forced-circulation fat-plate solar collector using MWCNT/water nanofuid. Case Stud Therm 14:100416. <https://doi.org/10.1016/j.csite.2019.100416>
- Khosravi K, Mohammed HI, Mahdi JM, Silakhori M, Talebizadeh Sardari P (2022) Developing a predictive model and multi-objective optimization of a photovoltaic/thermal system based on energy and

exergy analysis using response surface methodology. SSRN Electro J.<https://doi.org/10.2139/ssrn.4171638>

- Kumar A, Sharma M, Thakur P, Thakur VK, Rahatekar SS, Kumar R (2020) A review on exergy analysis of solar parabolic collectors. Sol Energy 197:411–432. [https://doi.org/10.1016/j.solener.2020.](https://doi.org/10.1016/j.solener.2020.01.025) [01.025](https://doi.org/10.1016/j.solener.2020.01.025)
- Madhu S, Balasubramanian M (2018) Efect of swirling abrasives induced by a novel threaded nozzle in machining of CFRP composites. Int J Adv Manuf Technol 95:4175–4189. [https://doi.org/](https://doi.org/10.1007/s00170-017-1488-2) [10.1007/s00170-017-1488-2](https://doi.org/10.1007/s00170-017-1488-2)
- Mahdavi N, Mojaver P, Khalilarya S (2022) Multi-objective optimization of power, CO2 emission and exergy efficiency of a novel solar-assisted CCHP system using RSM and TOPSIS coupled method. Renew Energy 185:506–524. [https://doi.org/10.1016/j.](https://doi.org/10.1016/j.renene.2021.12.078) [renene.2021.12.078](https://doi.org/10.1016/j.renene.2021.12.078)
- Munuswamy DB, Devarajan Y (2023) Critical examination of the role of silica nanoparticle dispersions in heat transfer fuid for solar applications. Silicon 15:571–581. [https://doi.org/10.1007/](https://doi.org/10.1007/s12633-022-02015-9) [s12633-022-02015-9](https://doi.org/10.1007/s12633-022-02015-9)
- Murugan M, Saravanan A, Elumalai PV, Kumar P, Ahamed Saleel C, Samuel OD, Setiyo M, Enweremadu CC, Afzal A (2022) An overview on energy and exergy analysis of solar thermal collectors with passive performance enhancers. Alex Eng 61(10):8123– 8147.<https://doi.org/10.1016/j.aej.2022.01.052>
- Naveenkumar R, Shanmugam S, Veerappan A (2022) Performance and exergy analysis of solar-operated vacuum fan and external condenser integrated double-slope solar still using various nanofuids. Envi Sci Pollut Res 30(5):12883–12902. [https://doi.org/10.1007/](https://doi.org/10.1007/s11356-022-22919-8) [s11356-022-22919-8](https://doi.org/10.1007/s11356-022-22919-8)
- Ramasamy D, R R, T R, S M, S S (2023) Optimisation of fow and fuid properties of nanofuids to enhance the performance of solar fat plate collector using MCDM technique. Proc Inst Mech Eng C 095440892211507.<https://doi.org/10.1177/09544089221150738>
- Rathan Kumar L, Madhu S, Mothilal T, et al (2022) Efect of walnut powder reinforcement on the mechanical properties of biodegradable natural fax/hemp fbre-based composites. Materials Today: Proceedings 69:1387–1393. [https://doi.org/10.1016/j.matpr.2022.](https://doi.org/10.1016/j.matpr.2022.09.203) [09.203](https://doi.org/10.1016/j.matpr.2022.09.203)
- Said Z, Saidur R, Sabiha MA, Hepbasli A, Rahim NA (2016) Energy and exergy efficiency of a flat plate solar collector using pH

treated Al2O3 nanofuid. J Clean Prod 112:3915–3926. [https://](https://doi.org/10.1016/j.jclepro.2015.07.115) doi.org/10.1016/j.jclepro.2015.07.115

- Sarhaddi F, Farahat S, Ajam H, Behzadmehr A (2010) Exergetic performance assessment of a solar photovoltaic thermal (PV/T) air collector. Energy Build 42(11):2184–2199. [https://doi.org/10.](https://doi.org/10.1016/j.enbuild.2010.07.011) [1016/j.enbuild.2010.07.011](https://doi.org/10.1016/j.enbuild.2010.07.011)
- Seralathan S, Chenna Reddy G, Sathish S, Muthuram A, Dhanraj JA, Lakshmaiya N, Velmurugan K, Sirisamphanwong C, Ngoenmeesri R, Sirisamphanwong C (2023) Performance and exergy analysis of an inclined solar still with baffle arrangements. Heliyon 9(4):e14807.<https://doi.org/10.1016/j.heliyon.2023.e14807>
- Singh V, Yadav VS (2022) Optimizing the performance of solar panel cooling apparatus by application of response surface methodology. Proc Inst Mech Eng C 236(22):11094–11120. [https://doi.org/](https://doi.org/10.1177/09544062221101828) [10.1177/09544062221101828](https://doi.org/10.1177/09544062221101828)
- Sint NKC, Choudhury IA, Masjuki HH, Aoyama H (2017) Theoretical analysis to determine the efficiency of a CuO-water nanofluid based-fat plate solar collector for domestic solar water heating system in Myanmar. Sol Energ 155:608–619. [https://doi.org/10.](https://doi.org/10.1016/j.solener.2017.06.055) [1016/j.solener.2017.06.055](https://doi.org/10.1016/j.solener.2017.06.055)
- Suzuki A (1988) General theory of exergy-balance analysis and application to solar collectors. Energy 13(2):153–160. [https://doi.org/](https://doi.org/10.1016/0360-5442(88)90040-0) [10.1016/0360-5442\(88\)90040-0](https://doi.org/10.1016/0360-5442(88)90040-0)
- Verma SK, Tiwari AK, Chauhan DS (2016) Performance augmentation in fat plate solar collector using MgO/water nanofuid. Energy Convers Manag 124:607–617. [https://doi.org/10.1016/j.encon](https://doi.org/10.1016/j.enconman.2016.07.007) [man.2016.07.007](https://doi.org/10.1016/j.enconman.2016.07.007)

Publisher's Note Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.

Springer Nature or its licensor (e.g. a society or other partner) holds exclusive rights to this article under a publishing agreement with the author(s) or other rightsholder(s); author self-archiving of the accepted manuscript version of this article is solely governed by the terms of such publishing agreement and applicable law.

Authors and Afliations

Ramachandran Thulasiram¹ · S. Murugapoopathi² · S. Surendarnath³ · Beemkumar Nagappan¹ · **Yuvarajan Devarajan4**

- \boxtimes Yuvarajan Devarajan yuvarajand.sse@saveetha.com
- ¹ Department of Mechanical Engineering, Faculty of Engineering and Technology, Jain (Deemed-to-Be University), Bangalore, India
- ² Department of Mechanical Engineering, PSNA College of Engineering and Technology, Dindigul, India
- ³ Department of Mechanical Engineering, DVR & Dr HS MIC College of Technology (A), Vijayawada, India
- Department of Mechanical Engineering, Saveetha School of Engineering, SIMATS, Saveetha University, Chennai, Tamil Nadu, India