**RESEARCH PAPER**



# **Evaluation of Unsaturated Water Flow Features of Compacted Soil Subjected to Horizontal and Vertical Water Infltration**

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### **Abstract**

The objective of this study is to compare the unsaturated water fow features during horizontal and vertical infltration. To follow the moisture variation (water content  $\theta$  (*z*, *t*)), the time domain reflectometry method is used. The retention curve is obtained by the flter paper method. The suction test results are interpreted by the Van Genuchten (Soil Sci Soc Am J 44(5):892–898, 1980) model. These results allow the determination of the relationships between difusivity and water content ( $D(\theta)$ ) and hydraulic conductivity and water content ( $K(\theta)$ ) by applying the instantaneous profiles method. The results showed that the unsaturated water fow parameters are infuenced by the fow direction and the gravity efect. The difusivity values in the vertical infltration column are higher than those measured in the horizontal infltration column. The experimental points calibrated with the models of Brooks and Corey (J Irrig Drain Div 92(2):61–88, 1966) and Campbell (Soil Sci 117(6):311–314, 1974) have shown that this model fairly well describes the hydraulic conductivity evolution versus water content.

**Keywords** Unsaturated soil · Infltration · Water content · Difusivity · Hydraulic conductivity

# **1 Introduction**

The issue of availability and access to water is undoubtedly one of the major problems that humanity will have to face during this century. Today, it is estimated that one in fve inhabitants of the planet does not have access to sufficient water, and only one in three has good water quality. In this context, it may be useful to recall that "the quantitative and qualitative measurement of the elements of the hydrological and hydrogeological cycles and the measurement of other environmental characteristics that infuence water constitute

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an essential basis for efective water management (Afeltranger and Lasserre [2003](#page-7-0))". Understanding and analyzing the water cycle are the basis of any study or refection on the subject of water management.

Water infltration into soils is a major component of the water cycle. Knowledge of the mechanisms governing infltration fows makes it possible to estimate the unsaturated water flow features in the soil. Among these, hydraulic conductivity represents a fundamental parameter in water transfers, the estimation of which fnds numerous applications in the following felds (Velly [2000\)](#page-8-0): (a) in agriculture for the choice of the type of crop and the methods of drainage and irrigation; (b) in sanitation in order to size a spreading network; (c) in the environment for forecasting the risks of recurrent or accidental contamination of groundwater by surface activities; and (d) in geotechnics within the framework of erodibility and slope stability studies.

Infltration is an essential part of the hydrological cycle. It is defned by the proportion between the surface fow, also called runoff, and the underground flow. The estimation of the importance of the infltration process makes it possible to determine what fraction of the rain will participate in surface runoff and what fraction will participate in the recharge of groundwater.



The hydraulic conductivity values and the water transfer qualifcation parameters can be determined in the laboratory on test specimens taken from the feld or directly in place by means of in situ tests. However, it is often difficult to access this conductivity with the only information that can be conveniently obtained from these tests.

Two soil columns were put through standard infltration tests in the laboratory to fnd out how water moves through unsaturated soil and how gravity afects the water parameters of this soil. During infltration tests, soil water content (moisture) and soil suction were measured to monitor water transfer. Infltration curves were used to describe the water flow and the infiltration rate. The water content profiles were used to observe the soil saturation process and to determine the soil column transit time.

The transient analysis of moisture and efective pressure profles, measured during infltration in an unsaturated soil layer, makes it possible to establish the relationships between the unsaturated water flow parameters (Hamilton et al. [1981](#page-8-1)). These parameters are obtained by applying the generalized Darcy law (Vachaud [1966](#page-8-2); Vauclin [1971](#page-8-3); Wesseling et al. [1966](#page-8-4)). Knowledge of the phenomenological relationships between the unsaturated water fow features in the soil is an essential prerequisite for any quantifcation, by experimental means and by modeling, of water transfers in unsaturated porous media. These relationships make it possible to evaluate the unsaturated water fow parameter values in a saturated state. These relationships cannot be inferred from fundamental soil properties but must be determined by experimental procedures. Often, these relationships are inferred from the water balance during soil wetting or drainage.

Results from all studies seem to be conficting because they consider only the morphology of structure rather than the hydrodynamic functionalities. In summary, the studies show the necessity: (a) to take into account matrix pores and macropores; (b) to consider the feld scale of soil profles rather than the laboratory scale of cores to also assess the heterogeneity induced by compaction; and (c) to directly consider the hydrodynamic functionality of the pores in conducting water and air rather than dwelling on the morphology of soil structure.

Hamilton et al. [\(1981\)](#page-8-1) measured the hydraulic conductivity–suction relationship using a permeameter and a thermocouple psychrometer. They found that the instantaneous profle method works well for clays, which have a degree of saturation varying between 30 and 90%, and for sands, which have a degree of saturation lower than 50%. Tensiometers should be used to measure suction at higher saturation levels. In addition, Daniel [\(1983](#page-8-5)) used the method of instantaneous profles to measure the unsaturated hydraulic conductivity of fne silty sand with the simultaneous use of tensiometers and psychrometers. The method requires several weeks per test,



and the time allocated to the calibration of psychrometers and tensiometers must be added (Hamilton et al. [1981](#page-8-1); Daniel [1983](#page-8-5)). Krisdani et al. [\(2009\)](#page-8-6) adopted the instantaneous profle method for the calculation of residual soil permeability functions in laboratory slope models. These instantaneous profles were calculated using pore pressure measured with tensiometers along the slope models and independently measured soil–water characteristic curves. The instantaneous results of the profle were adjusted by the statistical method to obtain a continuous permeability function. The instantaneous profle method is commonly used for compacted clay soils (Cui et al. [2008\)](#page-8-7). The determination of the water content profle during water infltration is an important part of using this method. In several studies, the water retention test is carried out in parallel with the infltration test, which allows the indirect establishment of the water content profle from the measured suction profle (Ye et al. [2009](#page-8-8); Wang et al. [2013](#page-8-9)). Wei Su et al. ([2018](#page-8-10)) worked on rigid Teguline clay collected from the Albian Bassin Paris region. They discovered that hydraulic conductivity decreases with increasing suction and that the extrapolated value of hydraulic conductivity at zero suction is very similar to the value obtained directly using the constant head method. The successful incorporation of miniature TDR probes and tough flament tape extends the common instantaneous profle method to small laboratory samples and rigid materials (Wei Su et al. [2018\)](#page-8-10). Even though it has been shown that structural changes afect hydraulic properties, the way the raw experimental data are interpreted has a big impact on how the calculated changes in water permeability and suction are made (Dieudonne and Charlier [2017](#page-8-11)).

Da Silva et al. [\(2020](#page-8-12)) used the new version of the Splintex model (Splintex 2.0) to fgure out the unsaturated soil hydraulic conductivity (SHCC) as a function of volumetric water content () and saturated permeability (Ks). The Splintex 2.0 model assumes that soil pores are represented by equivalent capillary tubes and that water fow is a function of pore size distribution. Then, the  $K(\theta)$  data estimates are fitted to the unsaturated soil hydraulic conductivity described by Van Genuchten ([1980](#page-8-13)) and Mualem's equation [\(1976\)](#page-8-14) (VGM). The goodness of fit of  $K(\theta)$  was assessed with a selection of 198 SHCCs measured by the instantaneous profles method. The used data contain measured information on textural composition, bulk and solid densities, total porosity, and  $K(\theta)$  data. Splintex 2.0 provided mean values close to the VGM parameters ftted to the data measured by the instantaneous profle method. For the analyzed texture groups, the SHCC estimates were highly correlated  $(r=0.852)$ .

To calculate difusivity and hydraulic conductivity, soil moisture and suction profles are indispensable. By applying the instantaneous profles method to moisture profles, diferent unsaturated water fow parameters are calculated. The instantaneous profle method is used to determine diffusivity and hydraulic conductivity versus water content or suction (Alimi-Ichola and Gaidi [2006](#page-7-1)). Volumetric water profles are determined using TDR (time domain refectometry) measurements.

# **2 Instantaneous Profles Method**

The instantaneous profles method consists in imposing an infltration at one end of soil column and measuring the moisture spatio-temporal variations  $\theta$  (*z*, *t*) or water potential  $\phi$  (*z*, *t*). We calculate the flow that crosses a section at depth *z*. Then, we use Darcy's generalized law to determine the difusivity and hydraulic conductivity values (Hamilton et al. [1981\)](#page-8-1). The obtained results allow the determination of following relationships: hydraulic conductivity—water content  $(K(\theta))$ ; hydraulic conductivity—suction "pF"  $(K(pF))$ and diffusivity—water content  $(D(\theta))$ , using the instantaneous profle method. It is possible to demonstrate the gravity infuence on the hydraulic conductivity and difusivity.

Darcy's law applied to an unsaturated soil is written:

$$
q = -K(\theta)\frac{\partial \varphi}{\partial z},\tag{1}
$$

with:  $\phi = \psi - z$ , *q*: water flow,  $\psi$ : soil suction

So, 
$$
q = -K(\theta) \left( \frac{\partial \psi}{\partial z} - 1 \right)
$$
 (2)

If we suppose that at section  $z = H(H)$ : height of column) the outing flow is zero, the flow  $q(t)$  which crosses a section at the given position z is determined from the profiles  $\theta(z, t)$ at time t by the equation:

$$
q(t)|_{z} = \frac{1}{\Delta t} \int_{z}^{H} (\theta(z, t + \Delta t) - \theta(z, t)) dz = \frac{\partial I(t)}{\partial t}\bigg|_{z}
$$

 $I(t)$ , represents the water layer flowing through the section *z* between the instant *t* at  $t + \Delta t$ .

The retention curve  $\psi(\theta)$  makes it possible to evaluate the potential gradient ∂*ψ*/∂*z* at time *t* and at section *z*.

The hydraulic conductivity  $K(\theta)$  evolution at an instant t and the section z is calculated from the equation:

$$
K(t)|_{z} = -\frac{q(t)|_{z}}{\left(\frac{\partial \psi(t)}{\partial z} - 1\right)\Big|_{z}}
$$
(3)

At the instant t and the section of given depth z corresponds an average volumetric water content *θ* or an average value of pF. We can therefore associate at any time *t* with Eq. [3](#page-2-0) terms the values of *θ* or of pF. We can write:

<span id="page-2-2"></span>
$$
K(\theta)|_{z,t} = -\frac{q(\theta)|_{z,t}}{\left(\frac{\partial \psi(\theta)}{\partial z} - 1\right)\Big|_{z,t}}
$$
(4)

or

<span id="page-2-3"></span>
$$
K(pF)|_{z,t} = -\frac{q(pF)|_{z,t}}{\left(\frac{\partial \psi(pF)}{\partial z} - 1\right)|_{z,t}}
$$
(5)

The relation  $D(\theta)$  is obtained from Eq. [6](#page-2-1) (Childs and Collis-George [1948\)](#page-7-2):

<span id="page-2-1"></span>
$$
D(\theta)|_{z,t} = K(\theta)|_{z,t} \left. \frac{\partial \psi}{\partial \theta} \right|_{z,t} \tag{6}
$$

By neglecting gravity and adopting the flow to horizontal flow, Eqs. [4](#page-2-2) and [5](#page-2-3) reduce to:

$$
K(\theta)|_{z,t} = -\frac{q(\theta)|_{z,t}}{\left(\frac{\partial \psi(\theta)}{\partial z}\right)|_{z,t}}
$$
(7)

$$
K(pF)|_{z,t} = -\frac{q(pF)|_{z,t}}{\left(\frac{\partial \psi(pF)}{\partial z}\right)\Big|_{z,t}}
$$
(8)

The relation  $D(\theta)$  is obtained from the flow measurements and the volumetric water content gradient:

$$
D(\theta)|_{z,t} = -\frac{q(\theta)|_{z,t}}{\left(\frac{\partial \theta}{\partial z}\right)|_{z,t}}
$$
(9)

The moisture profles integration makes it possible to determine the flowing layer evolution  $I(z,t)$ . We can then draw the water flowing layer curves evolution with time from the moisture profles. The slopes of these curves at diferent times give the fow that crosses the section over time.

#### **2.1 Empirical Models of Hydraulic Conductivity**

<span id="page-2-0"></span>Several empirical models have been proposed to describe the variation of hydraulic conductivity versus volumetric water content or suction. These models are necessary for water transfer modeling in unsaturated porous media. We have wanted from existing models those who better represent the experimental results. We have chosen the Brooks and Corey [\(1966\)](#page-7-3) and Campbell [\(1974\)](#page-7-4) models.



# **2.2 Model of Brooks and Corey ([1966\)](#page-7-3) and Campbell ([1974\)](#page-7-4)**

The experimentally measured permeability coefficient value  $K<sub>s</sub>$  of the studied soil is equal to  $6 \times 10^{-8}$  m/s. The model of Brooks and Corey ([1966](#page-7-3)) and Campbell ([1974\)](#page-7-4) describes the variation of hydraulic conductivity with volumetric water content. The hydraulic conductivity according to this model is written:

$$
K(\theta) = K_S \left(\frac{\theta}{\theta_S}\right)^m \quad \text{when} \quad Y > Y_e \tag{10}
$$

 $\theta_s$  volumetric water content at saturation,  $\psi_e$  inlet air pressure,  $K(\theta)$  hydraulic conductivity at the water content  $\theta$ ,  $K_s$ hydraulic conductivity at  $\theta = \theta_{s}$ , m: empirical constant

We try to find the values of parameters  $\theta_s$ ,  $K_s$  and m which permit to this model to represent well the experimental results.

### **2.3 TDR Method**

Time domain refectometry (TDR) is based on measuring the transit time and the amplitude attenuation of an electromagnetic pulse launched along a transmission line (TL) implanted in the soil. The measurement method was developed by Topp et al. [\(1980\)](#page-8-15), who showed that for many soil materials, there exists an empirical relationship between volumetric water content and soil dielectric constant. The electromagnetic wave attenuation that is propagated along the transmission line is related to the bulk electrical conductivity of the soil (Nadler et al. [1991\)](#page-8-16). Topp et al. [\(1980\)](#page-8-15) proposed to determine the soil volumetric water content *θ*, this relationship:

$$
\theta = -0.053 + 0.29\epsilon - 5.510^{-4} \epsilon^2 + 4.310^{-6} \epsilon^3 \tag{11}
$$

where  $\varepsilon$ , the soil dielectric constant, is measured from the transit time t of an electromagnetic pulse through the soil by:

$$
\varepsilon = (ct/2L)^2 \tag{12}
$$

where  $c$  = velocity of light in free space,  $L$ : length of the used probe rod.

To improve volumetric water content measurement, TDR probes were calibrated with water and diferent soils. So the measurement of the soil water content during this study is obtained from the relationship (Gaidi and Alimi-Ichola [2000](#page-8-17)):

$$
\theta = 0.0548 + 0.0153\varepsilon - 5 \times 10^{-5} \varepsilon^2 + 8 \times 10^{-8} \varepsilon^3 \tag{13}
$$

### **2.4 Infltration Test**

Simultaneous infltration tests on two soil columns are carried out. So, the water fow parameters of unsaturated soil for vertical and horizontal water percolation can be compared.



The infltration tests are performed in a PEHD column with a 600-mm height. The column is composed of rings of 40 mm height and 100 mm diameter. The soil was wetted at a fixed water content and compacted at the desired bulk density in each ring (Alimi-Ichola and Gaidi [2006\)](#page-7-1). Before soil compaction, TDR probes are inserted in eight rings, which compose each test column. The probes consisted of three steel rods of 75 mm in length. After the column setting, TDR probes are located at depths of 2, 10, 18, 26, 34, 42, 50, and 58 mm. The used soil material is clayey sand.

<span id="page-3-1"></span>The experimental setup for this study is illustrated in Fig. [1](#page-3-0). The TDR probes are connected to a multiplexer for sequential measurement. A computer program is used to drive the multiplexer and the two balances. So, infltration fow and TDR measurements are recorded according to the data acquisition program. Cumulative infltration curves are obtained from balance measurements. These balances are placed on heavy supports to absorb any possible vibrations. Balances are reported to have a precision of 1/100 g and are sensitive to vibration. Mariotte's bottles are flled with water and provide the hydraulic load. The efect of the fux mode on the infltration curve and the soil's hydraulic conductivity is measured by fguring out the initial and steady fow rates.

The carried-out test allows a comparison between a vertical and horizontal fows under the same initial conditions.

Van Genuchten ([1980\)](#page-8-13) model is used to describe the experimental water retention curve (14).

$$
\left(\frac{\theta - \theta_r}{\theta_s - \theta_r}\right) = \left[\frac{1}{1 + (\alpha h)^n}\right]^m\tag{14}
$$

where  $\theta_r$ : residual volumetric water content,  $\theta_s$ : saturated volumetric water content  $(h=0)$ ,  $\alpha$ , *n* and *m*: model parameters



<span id="page-3-0"></span>**Fig. 1** The experimental device

<span id="page-4-0"></span>



<span id="page-4-1"></span>**Fig. 2** Retention curve of the soil

The parameters of this model are computed from measured suctions versus volumetric water contents. These parameter values are shown in Table [1](#page-4-0). Bentoumi [\(1995\)](#page-7-5) have shown that the function  $h(\theta)$  derived from Eq. [10](#page-3-1) represents the evolution of the efective head pressure in the soil during infltration. So Eq. [10](#page-3-1) can be used to compute suction profles from volumetric water content profles.

Measured suction points and Eq. ([10](#page-3-1)) are represented in Fig. [2](#page-4-1).

The infltration is performed at constant water head supply  $h_0$  = 25 cm and at an initial water content equal to 10%. The soil in the two columns is compacted to dry bulk density equal to  $1.55$  g/cm<sup>3</sup>.

# **3 Results and Discussion**

## **3.1 Infltration Curve Analysis**

Curves of cumulative infltration versus time are determined from the variation of the Mariotte burette weight. By using the acquisition software, the balances directly provide the infltrated volumes (in text format). The TDR curves obtained from the Tektronix 1502B cable tester unit are recorded on the computer for further analysis.

Infltrated volumes in soil columns are plotted versus time (Fig. [3\)](#page-4-2). This fgure shows that water fow is the same during one day of infltration. After this time, the infltrated volume in the vertical column becomes higher than the infltrated volume in the horizontal column. This



<span id="page-4-2"></span>**Fig. 3** Infltration curve



<span id="page-4-3"></span>**Fig. 4** Infltration curve

difference shows the gravity influence on the infiltration process. After 6 days of infltration, the volume of water infltrated into the vertical column is approximately 153 ml, and that of the horizontal column is only 135 ml. From this time on, the two infltration curves increase in parallel with the same velocity.

The infltration curves of the two columns represented in square root of time  $I = S\sqrt{t}$  (Model of Philip [1969\)](#page-8-18) are represented in Fig. [4.](#page-4-3)

The experimental points regression lines offer a good correlations coefficient. In Philip model,  $S$  (cm/s<sup>1/2</sup>) is the sorptivity and I the cumulative infiltration  $(I = V/A)$ .

Table [2](#page-5-0) contains the sorptivity values (*S*) calculated from the two lines slopes (Fig. [4](#page-4-3)).

The sorptivity value refects the capacity of the soil to retain liquid. The sorptivity value in the vertical column is slightly higher than that obtained in the horizontal column. This result explains the fact that the propagation velocity in a vertical column is higher than that in a horizontal column.

![](_page_4_Picture_20.jpeg)

<span id="page-5-0"></span>![](_page_5_Picture_327.jpeg)

### **3.2 Moisture Profles Analysis**

The soil moisture profle, which represents its volumetric water content distribution at a chosen time t, makes it possible to explain and quantify the process of water infltration in soil. During vertical infltration, moisture propagates through unsaturated soil under gravity forces on the one hand and capillary forces on the other. If the soil capillary forces become too weak, the difusion will be negligible, and the hydraulic load imposed on the soil surface will remain the sole motor of flow (Bentoumi [1995\)](#page-7-5).

Figure [5](#page-5-1)a and b represents the moisture profiles  $\theta = f(z,t)$ in the tow soil columns. By comparing these moisture profles, we notice that:

- The transfer in the two columns begins always with a difusion phenomenon followed by convection.
- At test beginning, the moisture progression in two soil columns is done with same manner.
- An acceleration of flow in vertical column compared to horizontal one.
- The sixth ring in vertical column (probe 6) is reached by liquid after 23 h of infltration. On the other hand, the sixth ring (probe 6 of the horizontal column) is reached by liquid after 1.12 days of fow.
- Water came out from horizontal column bottom after 1.85 days. This duration is only 1.47 days in vertical infltration.
- A global overview of the two moisture profles groups allows concluding that the propagation in vertical column is faster than that in horizontal case. This rapidity in volumetric water content propagation refects the gravity efect on the infltration velocity.

### **3.3 Suction Profles Analysis**

The Van Genuchten model will make it possible to trace the suction profles from volumetric water content profles (Fig. [6\)](#page-6-0). We notice that the soil suction follows the moisture variation. When volumetric water content is high, the suction value (pF) becomes low. Any decrease in volumetric water content is followed by suction increase. Generally, in the two columns, there is not an immense diference in suction profles.

#### **3.4 Difusivity and Hydraulic Conductivity Study**

The difusivity variation curves versus the volumetric water content  $D(\theta)$  obtained by the instantaneous profiles method are shown in Fig. [7.](#page-6-1) The difusivity values of vertical column are higher than those of horizontal column. Therefore, Eq. [\(6](#page-2-1)) overestimates the values of difusivity. This diference further proves gravity infuence on water fow. Despite this diference, the values of the difusivities remain in the same order of magnitude  $(\times 10^{-7})$ .

![](_page_5_Figure_16.jpeg)

<span id="page-5-1"></span>**Fig. 5** Moisture profles

![](_page_5_Picture_18.jpeg)

![](_page_6_Figure_1.jpeg)

<span id="page-6-0"></span>**Fig. 6** Suction profles

![](_page_6_Figure_3.jpeg)

<span id="page-6-1"></span>**Fig. <sup>7</sup>**Difusivity variation curves vs. volumetric water content **Fig. <sup>8</sup>**Model of Brooks and Corey ([1966\)](#page-7-3) and Campbell ([1974\)](#page-7-4): *K*(*θ*)

The soil hydraulic conductivity variation versus volumetric water content is plotted in Fig. [8.](#page-6-2) The hydraulic conductivities in the two columns vary with the same manner. These curves show an increase of hydraulic conductivity according to volumetric water content (horizontal fow and vertical flow cases). For given volumetric water content, the hydraulic conductivity of vertical column is always slightly superior than that of horizontal column. When the water content increases, the difference between the measured hydraulic conductivities increases (in vertical and horizontal flow).

Vertical Flow 6E-08 **Horizontal Flow** Hydraulic Conductivity (m/s) 5E-08 Brooks, Corey and Campbell Model 4E-08 Brooks, Corey and Campbell Model For two columns  $3E-08$  $2E-08$  $1E-08$  $\mathbf 0$  $0,16$  $0,18$  $0,2$  $0,22$  $0,24$  $0,26$  $0,28$  $0,3$ 0,32 Volumetric Water Content (m<sup>3</sup>/m<sup>3</sup>)

<span id="page-6-2"></span>

Since the two soil columns contain the same soil compacted at the same conditions, the two hydraulic conductivity curves must be very close or even superimposed. But in our case, we notice a slight diference between the two curves. This diference probably results from the high velocity of vertical infltration noted in the water profles and the diference in velocity in the infltration curve. In the vertical column, when water saturates a layer causes a slight increase in the hydraulic head in the soil which is not the case in the horizontal column. These variations led

![](_page_6_Picture_9.jpeg)

to a slight dysfunction in the theoretical framework of the instantaneous profle method.

# **3.5 Model**  $K(\theta)$ **—Model of Brooks and Corey [\(1966\)](#page-7-3) and Campbell [\(1974\)](#page-7-4)**

The measured soil permeability coefficient at saturation  $K_s$  is equal to  $6 \times 10^{-8}$  m/s. The model of Brooks and Corey ([1966](#page-7-3)) and Campbell ([1974](#page-7-4)) describes the variation of hydraulic conductivity vs. water content. The hydraulic conductivity of this model is written according to Eq. [10](#page-3-1). We seek the parameters  $\theta_s$ ,  $K_s$  and *m* values which permit at this model to represent well the experimental results.

Figure [8](#page-6-2) shows the experimental points of the horizontal and vertical columns. We also represent the curve given by the model of Brooks and Corey ([1966](#page-7-3)) and Campbell [\(1974\)](#page-7-4) obtained after the model parameters determination. These parameters make it possible to obtain a curve which represents the experimental points. The parameters of this model change depending on the studied case.

Figure [8](#page-6-2) shows the experimental points of the horizontal and vertical columns. We also represent the curve given by the model of Brooks & Corey ([1966\)](#page-7-3) and Campbell [\(1974](#page-7-4)), obtained after the model parameter determination. These parameters make it possible to obtain a curve, which represents the experimental points. The parameters of this model change depending on the studied case.

The saturation water content value in vertical flow is close to that obtained in the horizontal flow case. We also note that the saturation permeability coefficient in the vertical column is slightly higher than that obtained in the horizontal column. The saturation permeability coefficient of the vertical column is 15% higher than the permeability coefficient obtained in the horizontal column. The used model well represents the experimental points of a vertical or horizontal flow. Since the soil in the two columns is the same, we propose to establish a global model representing the measurement points in the two columns (Fig. [8\)](#page-6-2). The global parameters of the model are presented in Table [3.](#page-7-6)

<span id="page-7-6"></span>**Table 3** Parameters of the Brooks and Corey ([1966\)](#page-7-3) and Campbell ([1974\)](#page-7-4) model

	$K_{\rm s}$ (m/s)	$\theta_{\rm s}$ (m <sup>3</sup> /m <sup>3</sup> )	m
Vertical column	$6.4e - 8$	0.3	
Horizontal column	$5.5e - 8$	0.31	5.6
Global curve	$6.0e - 8$	0.31	

### **4 Conclusion**

The study presented in this paper mainly concerns the analysis and interpretation of water infltration tests carried out in the laboratory on unsaturated soil. This study permits some understanding of elements of soil water transfer in vertical and horizontal fow. To follow this transfer in real time and continuously, we used TDR probes. These probes make it possible to measure the soil water content and the electrical conductivity. The developed experimental device allowed for the evolution of moisture profles during infltration. This water content measurement made it possible to assess the infltration rate and soil water fow. The experimental device allowed following the spatiotemporal distributions of water content and soil suction during infltration using TDR probes. During water infltration, there is a progressive propagation of moisture in the soil. The liquid movement by difusion in the unsaturated soil has the same importance as the convection movement under the gravity effect. The convection movement is predominant during horizontal infltration. The unsaturated water fow characteristics are slightly infuenced by the nature of infltration. The difusivity values in the vertical column are higher than those measured in the horizontal column. Also, the hydraulic conductivities are slightly higher in the vertical column. The nature of infltration must therefore be taken into account when dimensioning impermeable barriers. It is especially necessary to be careful when applying the theory of instantaneous profles, it is preferable and sufficient to carry out tests on vertical soil columns to avoid any malfunction of the theoretical framework of the method. This research should be complemented by another study carried out on soil columns percolated by leachate. This research will allow for studying the infuence pollutants on unsaturated water fow features and on soil structure.

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