ORIGINAL ARTICLE

Determining Signifcant Morphological and Hemodynamic Parameters to Assess the Rupture Risk of Cerebral Aneurysms

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Abstract

Hemodynamics and morphology are recognized as major factors in the rupture risk of cerebral aneurysms, and exploration of their relationship is necessary to establish a method that can be employed by clinicians to assess the likelihood of rupture. In this work, morphological analysis and computational fuid dynamics were carried out to examine a database of 58 lateral cerebral aneurysms (26 ruptured and 32 unruptured) distributed among 49 patients. Eight morphological and six hemodynamic parameters were calculated and evaluated for statistical significance. It was observed that size ratio (SR), systolic wall shear stress (SWSS), diastolic wall shear stress (DWSS) and relative residence time (RRT) were statistically signifcant. The SR, DWSS, SWSS, and RRT were employed in multivariate logistic regression, obtaining a combined morphological–hemodynamic model, a pure morphological model, and a pure hemodynamic model to evaluate the odds ratio for rupture risk. The combined model had the highest efficiency, but no distinctive difference existed in the predictive capacity of the three models.

Keywords Morphology · Hemodynamic · Cerebral aneurysm · Rupture risk

Abbreviations

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1 Introduction

It is well known that cerebral aneurysms constitute a risk since their rupture releases blood, causing subarachnoid hemorrhage, morbidity and mortality [[1,](#page-5-0) [2](#page-5-1)]. Nevertheless, aneurysm treatment is often a complex process for clinicians to carry out, and it can have negative outcomes on patients. Therefore, it is desirable to establish a method for the assessment of rupture risk. Morphological analyses have shown that geometric parameters, such as size, aspect ratio (AR) and aneurysm fow angle, have an association with rupture [\[3](#page-5-2)[–6](#page-6-0)]. However, recent computational fuid dynamics (CFD) studies have discussed the role that hemodynamic factors play in the pathogenesis, progression, and rupture of cerebral aneurysms. Wall shear stress (WSS), oscillatory shear index (OSI), and relative residence time (RRT) have been proposed as indicators of aneurysm rupture risk $[7–10]$ $[7–10]$. Therefore, it is necessary to develop a combined hemodynamic–morphological approach to further investigate rupture status.

The aim of this study was to identify signifcant morphological and hemodynamic parameters that discriminate rupture risk. For this purpose, we performed CFD simulations and morphological characterization of 58 patient-specifc lateral cerebral aneurysm models obtained from 49 patients. The aneurysms were located at diferent cerebral regions: the basilar artery, the internal carotid artery, the middle cerebral artery, the pericallosal artery, the posterior communicating artery and the posterior inferior cerebellar artery. All patient-specifc geometries were reconstructed from 3D rotational angiography image data. Eight morphological and six hemodynamic parameters were computed straight from medical images and CFD simulations, respectively. Statistical analysis was carried out to assess the statistical signifcance of each quantity. This work is organized as follows: Sect. [2](#page-1-0) explains the simulation procedure and the tools employed for the analysis, Sect. [3](#page-3-0) presents and discusses the results, and fnally, Sect. [4](#page-5-3) draws conclusions.

2 Materials and Methods

2.1 Computational Method and Boundary Conditions

The patient-specific lateral cerebral aneurysm images were provided by the Instituto de Neurocirugía Asenjo and were obtained with a Philips Integris Allura 3D Rotational Angiograph. A total of 26 ruptured and 32 unruptured aneurysms, distributed among 49 models, were reconstructed for the simulation software Ansys Fluent, following the procedure described by Valencia et al. [[11\]](#page-6-3). Here, we note that the status of all aneurysms was determined during image acquisition and that their evolution was not studied in this work. In addition, from now on, the model corresponding to patient number N is referred to as Case N. The volume mesh was constructed using an unstructured tetrahedral grid with a mesh density of 1500 cells/mm³. The maximum edge size of the cells was set to 0.2 mm. Thus, the system with the maximum number of cells had a volume of 1521 mm^3 and $2,265,413$ elements, whereas the system with the minimum number of cells had a volume of 218 mm^3 and $322,215$ elements. As an example, the mesh of a given system is shown in Fig. [1.](#page-1-1) Higher mesh densities were also studied (2500 and 3500 cells/mm³), but they were not considered in this work since the diferences in the mean and maximum WSS during systole were below 3% when compared to the lowest mesh density. Computational fuid dynamic simulations were performed using the PISO scheme. Velocities and pressure were interpolated with a second order upwind and a second order scheme, respectively. Time was discretized using a second order implicit formulation, and

Fig. 1 Tetrahedral mesh for a given patient-specifc cerebral aneurysm

Fig. 2 Example of fow rate used as the inlet condition

the time step was chosen as $\Delta t = 0.0005$ s. Residuals of the momentum and continuity equations were kept below 10−3. Two cardiac cycles of 0.85 s were simulated, and the results were taken from the second cycle. Blood was assumed to be an incompressible Casson fuid [[12](#page-6-4), [13\]](#page-6-5) with a density of 1065 kg/m^3 . The flow was modeled as laminar. All simulations were run using double precision on a machine with 16 GB RAM and an Intel i7 CPU with four physical cores.

A Womersley velocity profle was set at the inlet, which was obtained as follows. First, 70 blood pulses of diferent patients, measured in their internal carotid artery using Doppler ultrasound, were averaged, obtaining $\bar{V}(t)$. Second, the blood flow of each case was calculated as $Q_i(t) = A_i \overline{V}(t)$, where A_i is the inlet area of case i. Lastly, $Q_i(t)$ was fitted to a Fourier series, obtaining the coefficients $Q_i^n(t)$, which were used to calculate the Womersley velocity profile. An example of flow rate is shown in Fig. [2.](#page-1-2) We remark that the frst step allowed us to have the same average inlet velocity in all cases, avoiding an extra variable associated with diferent infow conditions as explained by Valencia et al. [\[14](#page-6-6)]. No-slip condition was applied to all surfaces, and a pressure pulse oscillating between

80 and 120 mmHg, calculated from a three-element Windkessel circuit, was set to all outlets. This pulse is shown in Fig. [3.](#page-2-0)

2.2 Morphological Parameters

 $NSI = 1 - (18\pi)^{1/3} \frac{V^{2/3}}{S}$

Eight morphological parameters were defned to characterize each aneurysm: AR, size ratio (SR), bottleneck factor (BNF), nonsphericity index (NSI), undulation index (UI), aneurysm angle (α_A), flow angle (α_F) and vessel angle (α_V). The AR was defned as the ratio of the maximum perpendicular height to the neck diameter, the SR was defned as the ratio of the maximum perpendicular height to the parent vessel diameter, and the BNF was defned as the ratio of the width to the neck. The NSI was calculated as follows:

Fig. 3 Pressure waveform employed as the boundary condition for all outlets

Fig. 4 Definition of angles α_{Δ} , α_F and α_V

where V is the volume of the aneurysm and S is its surface. whereas UI was obtained as follows:

$$
UI = 1 - \frac{V}{V_{ch}},
$$

where V_{ch} is the convex hull, which is the smallest volume that fully encloses the aneurysm and that is convex at all points [[15](#page-6-7)]. The α_A was defined as the angle between the neck of the aneurysm and the maximum height of the aneurysm, α_F was defined as the angle between the maximum height of the aneurysm and the parent vessel, and α_V was defned as the angle between the parent vessel and the plane of the aneurysm neck. For more details, these three angles are shown in Fig. [4](#page-2-1).

2.3 Hemodynamic Parameters

Six hemodynamic parameters were calculated for each aneurysm: diastolic WSS (DWSS), systolic WSS (SWSS), timeaveraged WSS (TAWSS), RRT, OSI, and aneurysm formation index (AFI).

SWSS and DWSS were calculated as the WSS, $\tau_{\tau_{000}}$, evaluated at the maximum of the systole, t_s , and the minimum of the diastole, t_d , respectively:

$$
SWSS = \tau_{\omega}(\vec{x}, t_s),
$$

$$
DWSS = \tau_{\omega}(\vec{x}, t_d).
$$

Both SWSS and DWSS were further averaged over the aneurysm area and then normalized by the SWSS and DWSS of the parent vessel, respectively.

The TAWSS was computed as the average of the WSS during a cardiac cycle T:

and then, it was averaged over the aneurysm area and normalized by the TAWSS of the parent vessel.

The OSI compares the mean WSS vector with the mean of the magnitude of the same vector. It was calculated as follows $[16]$:

$$
OSI = \frac{1}{2} \left(1 - \frac{\left| \int_0^T \tau_{\omega}(\vec{x}, t) dt \right|}{\int_0^T |\tau_{\omega}(\vec{x}, t)| dt} \right).
$$

The quantity was also averaged over the aneurysm area.

The RRT is the residence time of particles near the wall, and it was obtained as follows [[17,](#page-6-9) [18\]](#page-6-10):

$$
RRT = \frac{1}{(1 - 2 \times OSI) \times TAWSS}.
$$

The RRT was further averaged over the aneurysm area and normalized by the RRT of the parent vessel.

The AFI compares the local orientation of the instantaneous WSS with the direction of TAWSS, ignoring its magnitude. It was calculated as follows [[19\]](#page-6-11):

$$
AFI = \frac{\tau_{\omega}(\vec{x}, t) \cdot TAWSS}{|\tau_{\omega}(\vec{x}, t)||TAWSS|}
$$

and then, it was averaged over the aneurysm area.

2.4 Statistical Analysis

Table 1 Morphological and hemodynamic parameters for the ruptured and unruptured

groups

The mean and standard deviation of each parameter was calculated for the unruptured and ruptured groups.

The Jarque–Bera test was employed to determine whether a parameter was normally distributed or not. The

non-parametric Mann–Whitney U test was performed to assess the statistical signifcance of abnormally distributed data, whereas the Student's t-test was used for normally distributed data. A P value below 0.005 was considered to be statistically signifcant. In addition, receiver operating characteristics (ROC) analysis was performed to obtain the optimal threshold of each parameter. The efficiency of each ROC curve was measured by calculating its area under the curve (AUC). All parameters found to be statistically signifcant were employed in multivariate logistic regression to identify the most relevant quantities. For comparison purposes, all parameters were scaled to span a range from 0 to 10, which means that a unit increase corresponds to 10% of its observed range. Statistics were carried out using Matlab software (MathWorks).

3 Results and Discussion

3.1 Morphological and Hemodynamic Characterization

The mean and standard deviation of each morphological parameter for the unruptured and ruptured group are presented in Table [1](#page-3-1). It is observed that all these quantities had higher values for the ruptured group. Nevertheless, NSI and α_A had small differences when comparing both groups. In addition, NSI, UI and α_A were not statistically significant, which contrasts other works $[3, 5]$ $[3, 5]$ $[3, 5]$ $[3, 5]$ $[3, 5]$. This result may be due to the bigger database of cases considered in those studies. Moreover, our results revealed that only SR was statistically signifcant. Nevertheless, it is interesting to note that AR, BNF and α_F had P values close to 0.005, which suggests that a bigger database of aneurysms should be analyzed to assess

the statistical signifcance of these three quantities. Table [1](#page-3-1) also shows the statistical analysis of hemodynamic parameters. It was observed that DWSS, SWSS and TAWSS were higher in the unruptured group than in the ruptured, which is in good agreement with previous works [[9,](#page-6-12) [20](#page-6-13), [21](#page-6-14)]. Furthermore, both DWSS and SWSS of the unruptured group had a ratio closer to one when compared to the same magnitudes of the ruptured group. This fnding means that the WSS inside the aneurysm cavity was similar with that of the parent vessel. Nevertheless, this result must be considered cautiously, since there is signifcant variation in these values. Figure [5](#page-4-0) shows the TAWSS felds for some cases of ruptured and unruptured aneurysms. As commented above, it was seen that, overall, the magnitude of WSS was higher for the unruptured group than for the ruptured group. On the other hand, RRT and OSI were higher for the ruptured group than for the unruptured group, which means that particles tend to spend a longer time near the wall and that WSS changes its direction more frequently during a cardiac cycle. Regarding the AFI, a small diference was observed between both groups, making it difficult to infer its incidence in the risk of rupture. Finally, it was observed that DWSS, SWSS and RRT were statistically significant, which is in good agreement with previous results [\[9](#page-6-12), [22](#page-6-15)]. However, other hemodynamic parameters, such as OSI and TAWSS, should also be statistically signifcant, as discussed in other works [[9](#page-6-12), [20](#page-6-13)]. Nevertheless, a higher number of cases is probably needed [\[21](#page-6-14)]. The optimal thresholds of all morphological and hemodynamic parameters were calculated using ROC analysis. The thresholds and AUC are presented in Table [2.](#page-4-1) On one hand, it was observed that NSI, UI and α_A had the lowest AUC values. These quantities also had the highest P values. On the other hand, SR had the highest AUC value (0.745)

and the lowest P value (0.002), which indicates that this parameter is a good indicator for the assessment of rupture risk. This fnding is in good agreement with the results of other studies, which reported that SR is a signifcant predictor, regardless of whether SR is defned on a three-dimensional or two-dimensional basis [\[9](#page-6-12), [22](#page-6-15), [23\]](#page-6-16). The parameter that had the second highest AUC was RRT (-0.726) , which was followed by DWSS and SWSS with similar AUC values (0.725 and 0.722, respectively).

3.2 Multivariate Analysis

SR, DWSS, SWSS and RRT were regressed using the stepwise backward elimination process in order to determine a mathematical model for assessment of the risk of rupture

Fig. 5 TAWSS felds for some distinctive cases. R and U stand for ruptured and unruptured, respectively

Fig. 6 The ROC curves associated with the combined, pure morphological and pure hemodynamic models

of cerebral aneurysms. Following this procedure, SR and DWSS were retained as relevant parameters. Thus, the odds of rupture was expressed as follows:

$$
ODD_{combined} = e^{0.01 + 0.33 \text{SR} - 0.59 \text{DWSS}}.
$$

The AUC of this model was 0.78. In addition, for a unit increase in SR, the odds of rupture increased 1.39 times, whereas for a unit increase in DWSS, the odds decreased 1.80 times. Hence, the odds of rupture is more sensitive to the DWSS parameter. The efficiency of this model was compared to two other odds: one containing only SR, which we call the pure morphological model, and another containing only DWSS, which we call the pure hemodynamic model. For the frst case, the equation was given as follows:

$$
ODDmorph = e-1.55+0.39
$$

The AUC was 0.74 and for a unit increase in SR, the odds increased 1.47 times. For the second case, the model was as follows:

$$
ODDhemo = e1.24-0.63DWSS.
$$

Here, the AUC was 0.72, whereas for a unit increase in WSS, the odds of rupture decreased 1.89 times. When comparing the three models, the one with the highest efficiency was the odds with both parameters. It is interesting to note that the diference between this model and the pure morphological and pure hemodynamic models was 5.13 and 7.69%, respectively. Thus, the three models had similar efficiencies, and their ROC curves were quite similar (see Fig. [6\)](#page-5-5). Nevertheless, for higher accuracy when predicting the risk of rupture of cerebral aneurysms, the morphological–hemodynamic model should be employed.

It is important to note that the parameters that were statistically signifcant here partially difer from those obtained in other studies. For example, Xiang et al. [[9\]](#page-6-12) indicated that

SR, TAWSS, and OSI were relevant parameters, whereas Qin et al. [[24](#page-6-17)] stated that D/W and EL were the most signifcant parameters, where D stood for the ratio between the longest dimension from the aneurysm neck to the dome tip, W was the dome width, and EL was the energy loss. Nevertheless, Qin et al. considered only cerebral aneurysms located in the middle cerebral artery, whereas the database of Xiang et al. consisted of aneurysms located in diferent regions. All in all, the literature available does not provide a sole answer about the most relevant parameters used to assess the risk of rupture of cerebral aneurysms, indicating that more studies are necessary to clarify this subject.

4 Conclusions

Morphological and hemodynamic analyses were performed to determine signifcant parameters used to assess the risk of rupture of cerebral aneurysms. It was found that SR and DWSS were the most signifcant parameters. Using both quantities, a combined morphological–hemodynamic model (AUC 0.78), a pure morphological model (AUC 0.74), and a pure hemodynamic model (AUC 0.72) were proposed to evaluate the likelihood of rupture. The combined model had the highest efficiency, but no significant distinction existed between these models. Since SR is relatively simple to calculate from medical images, the pure morphological model can be employed by clinicians to assess the risk of rupture. However, for better accuracy, and considering that CFD simulations are a relatively fast task to carry out, the combined model should be used to predict the likelihood of rupture.

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