

# **To buy or to do it yourself? Pollution policy and environmental goods in developing countries**

**Roberta Sestini1 · Donatella Pugliese2**

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# **Abstract**

We analyse the effects of emissions taxes set by a developing country within a twocountry model, with two asymmetric downstream frms and a foreign upstream ecoindustry, and under the assumption that the more efficient firm may either obtain the environmental technology from the foreign innovator, or engage in abatement effort or fnally do not abate at all. A tougher climate policy may become the key driver for inducing the more efficient firm to engage in production of the abatement technology, leading also to a fall in total emissions. The impact on aggregate welfare is not clear-cut and heavily depends on frms' heterogeneity: only if the cost asymmetry is low enough the transition to the mixed equilibrium with one licensee and the other firm exerting abatement effort would make the society better off.

**Keywords** Trade and environment · Eco-industry · Environmental regulation · Emissions technologies

**JEL Classifcation** H23 · F18 · Q55 · Q56

 $\boxtimes$  Roberta Sestini sestini@diag.uniroma1.it Donatella Pugliese

donatella.pugliese@gmail.com

<sup>2</sup> Doctoral School of Economics, Sapienza University of Rome, Viale dell'Università 36, 00185 Rome, Italy

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<sup>1</sup> Department of Computer, Control and Management Engineering, Sapienza University of Rome, Via Ariosto 25, 00185 Rome, Italy

# **1 Introduction**

Rising pollution in the developing world is undoubtedly a major concern nowadays: China became the largest greenhouse gas emitter in 2005 and still remains in this position, followed by the United States and the European Union, while Brazil and India rank ffth and eighth biggest polluters, respectively (Outlook on the Global Agenda 2015, World Economic Forum).

Yet, the "bottom up" approach, implemented through goals defned at the national level, that emerged during the negotiations leading to the Paris 2015 Climate Conference (COP 21), implies that climate policy will remain sub-global and uneven in the near future. In Paris agreement it was explicitly recognized that developed countries should have a leading role in reducing their domestic emissions, and that some degree of fexibility and technological and fnancial support should be guaranteed to developing countries. Helping these countries to cope with the impact of increasing greenhouse emissions and climate change is thus a key issue which also intersects with multiple international initiatives aimed at liberalizing trade for the so-called environmental goods  $(EGs).<sup>1</sup>$  $(EGs).<sup>1</sup>$  $(EGs).<sup>1</sup>$ 

In particular, the EU and other members of the World Trade Organization (WTO) aim at boosting international trade in these products and services that directly contribute to environmental protection by liberalising trade in EGs through negotiating an Environmental Goods Agreement (EGA).<sup>[2](#page-1-1)</sup> Reducing barriers to trade in environmental goods and services has been on the global agenda since the launch of the WTO Doha Round: the rationale is that a successful outcome would create a double win, for trade and for the environment. This is because "the lower prices for abatement goods resulting from liberalizing trade in the sector will enhance environmental protection worldwide and beneft developing as well as developed countries" (Sinclair-Desgagnè [2008](#page-29-0)). However, the gain from trade liberalization in EGs

<span id="page-1-0"></span><sup>&</sup>lt;sup>1</sup> The OECD/Eurostat Informal Working Group on the Environment Industry developed at the end of the 1990's a widely-shared defnition and classifcation for the environmental goods industry. According to this, "the environment industry consists of activities which produce goods and services to measure, prevent, limit, minimize or correct environmental damage to water, air, and soil, as well as problems related to waste, noise and eco-systems" (Organization for Economic Cooperation and Development/Eurostat [1999](#page-29-1)). It is well-documented that pollution abatement accounts for most of the industry income. In the same decade the European Commission recognized the role of this industrial sector, emphasising how "the development of a strong environmental goods and services industry can make a major contribution to enabling enterprises to better integrate cleaner technologies and environmental practices in production and more generally improve environmental performance" (Communication from the Commission on Environment and Employment, Building a Sustainable Europe, COM(97)592 fnal).

<span id="page-1-1"></span><sup>&</sup>lt;sup>2</sup> Since July 2014, a group of WTO members launched plurilateral negotiations for the establishment of the EGA, with the aim of eliminating tarifs on selected environmental goods. Since then, the number of participants has grown, with currently 46 WTO members. From 2014 to 2016, intensive negotiations and discussions were carried out, resulting in a "landing zone" of 304 products. Yet, progress on reaching an agreement since then has stalled and participation of developing countries in these plurilateral initiatives was limited. At the regional level, a noteworthy initiative is the APEC Agreement on Environmental Goods, which aims to voluntarily reduce applied tarifs on 54 product categories of environmental goods, representing so far the most concrete trade liberalization commitment among a large group of countries (UNEP [2018\)](#page-29-2).

accruing to developing countries is far from established. For instance De Melo and Solleder [\(2018](#page-29-3)) argue that current negotiations involve mainly high-income countries, with the exception of China and Costa Rica, and show that, in order to have real benefts, an increase in regulatory convergence and in the number of participants to the agreement would be required. In a similar vein, Zugravu-Soilita ([2017\)](#page-30-0) empirically assesses the total efects of trade fows in environmental goods, fnding that "negative, indirect technique efects do not compensate the positive, direct scale-composition efects in the EGs' net importing countries, with the total efect on pollution being harmful".

During the last two decades, due to the increasing importance of the EG sector, a growing body of theoretical literature on the relationship between environmental policy and the market for abatement goods and services has appeared. The main upshot of these studies is to analyse the consequences of imperfect competition<sup>[3](#page-2-0)</sup> in this market for second-best emission taxes. The issue was frst tackled by David and Sinclair-Desgagnè ([2005\)](#page-29-4), proving that the optimal pollution tax must depart from the Pigouvian rule and be set above the marginal social cost of damage, in order to compensate for the lower level of abatement induced by higher prices of EGs. Several extensions were developed (see Canton et al. [2008;](#page-29-5) David and Sinclair-Desgagnè [2010](#page-29-6); Perino 2010; David et al. [2011](#page-29-7); Canton et al. [2012,](#page-29-8) among the others) mainly under the assumption of a closed economy.

Framing the issue in an open economy setting, Feess and Muehlheusser [\(2002](#page-29-9)) frst integrate the eco-industry into the theory of strategic environmental policy and challenge the conventional wisdom on ecological dumping showing that tighter environmental regulation may benefit the country where the eco-industry is located.<sup>[4](#page-2-1)</sup> More closely related to our paper, Nimubona [\(2012](#page-29-10)) considers the effects of trade liberalization—leading to an exogenous reduction of EG-import tarifs—on a developing country that imports *all* its consumption of EGs from a monopolistic ecoindustry located in a developed country. The key question addressed in this study is how lower barriers to trade in EG affect the quality of the environment in developing countries. The answer is not unequivocal, as, notwithstanding the fall in EG prices, the regulator may strategically respond by setting laxer pollution taxes with a worsening in pollution.

Other related papers are Canton [\(2007](#page-29-11)) and Dijkstra and Mathew [\(2016](#page-29-12)). In the former study, in a set-up where abatement goods are supplied in two countries (say North and South) characterized by diferent abilities to produce them and under perfect competition among polluting frms, the role of trade liberalization in reducing pollution is questioned. The latter work considers one domestic downstream polluting frm and two upstream frms (one domestic and one foreign) and examines the impact of liberalization on the domestic upstream frm's R&D incentive, reaching

<span id="page-2-0"></span><sup>&</sup>lt;sup>3</sup> Data and stylized facts indicate clearly that abatement goods and services are delivered by a monopoly or by a Cournot oligopoly or fnally by a monopolistic competitive market structure.

<span id="page-2-1"></span><sup>4</sup> Feess and Muehlheusser [\(2002](#page-29-9)) consider an international duopoly with one frm in each country selling on a third market, and introduce an eco-frm in the home country (say the North) supplying both downstream frms at an exogenous price.

ambiguous results. Most attention, however, was devoted to revisiting the Pigouvian tax rule taking into account *both* the market power of the eco-industry and international rent-shifting intents. Notably, both Canton ([2007\)](#page-29-11) and Nimubona [\(2012](#page-29-10)) conclude that, in the presence of an international eco-industry, EG-importing countries are led to set lower emission taxes—with respect to a closed-economy scenario—so to shift some rent from foreign EG suppliers.

The aim of our paper is to contribute to the above recalled debate. In particular, our aim is to answer to a *complementary* question with respect to Nimubona ([2012\)](#page-29-10), namely we wonder whether it is benefcial for a developing country, both for the environment and for the whole society, to *fully* rely on EGs produced abroad. To this end, we build a two-country model (a developed and a developing country) with two (heterogenous) polluting frms producing and selling in the developing country and competing *à la Cournot*. Given an environmental tax set in the developing country, the two frms may import all their consumption of the EG from a monopolistic innovator (frm *M*) located in the developed country. The licensed eco-technology enables firms to reduce pollution and thus expenditure on emissions tax. The less efficient firm, if not licensed, will continue to emit pollution. The more efficient firm, further to buying the EG from the foreign innovator, has the capability to engage in abatement efort. The foreign innovator sells its pollution abatement goods through a fxed-fee licensing contract and operates with zero production costs.

Climate policy enacted in the developing country is assumed to be exogenous; as recognized in the policy debate, the tax rate on GHG emissions is moderate. The problem is structured as a three-stage game: at the frst stage the foreign innovator announces the number of available licenses. Then the two polluting frms decide whether or not to purchase the license, or—for frm 1—to engage in abatement effort. Finally, at the third stage, firm 1 and firm 2 simultaneously choose their output and abatement levels.

Our paper borrows in large part from Kim and Lee [\(2016](#page-29-13)), as to modelling choices. Their set-up, however, does not tackle the possibility for frms to produce in-house their abatement goods and services, is mostly framed in terms of a closed economy, and is aimed at comparing two diferent types of licensing contracts, fxed-fee *versus* auction licensing.

Besides, we adopt many of the hypotheses in Nimubona [\(2012](#page-29-10)) about the presence of an eco-industry owned and located in the North and selling EGs in both countries markets, being these markets segmented. Also, we share with this study the attention devoted to the consequences on environmental quality in the South of easing the access to EGs produced abroad. However Nimubona ([2012\)](#page-29-10) does not allow for local firms engaging in abatement effort, and assumes that the consumption good is supplied in a perfectly competitive market. The novelty of our approach is clearly acknowledged by some of the most infuential scholars in this strand of literature.<sup>[5](#page-3-0)</sup>

<span id="page-3-0"></span><sup>&</sup>lt;sup>5</sup> Notably, David and Sinclair-Desgagnè [\(2010](#page-29-6)) close their paper by claiming that "Studying the consequences of other relevant and more complex industry structures, however, (with asymmetric environment frms or polluters also able to make their own abatement goods, notably) will require additional research".

We argue that our set-up captures some relevant features of EG supply and of their consumption in developing countries. First, there is evidence of an increasing concentration in the environmental industry, pursued also by means of mergers and acquisitions.<sup>[6](#page-4-0)</sup> Second, due also to multiple initiatives to reduce tariffs, the demand for EGs is rapidly expanding in developing countries, whilst the domestic sector is still immature.<sup> $\prime$ </sup> Finally, as explicitly recognized in Zhang  $(2011)$  $(2011)$ , developing countries, in the face of trade liberalization, are taking diferent courses: some of them for instance South Africa—are reducing tarifs to import abatement technologies at lower cost, whilst others—e.g. India, China and Ukraine—are imposing high tarifs or local content requirements to develop local productive capacities. This justifes our attention to "mixed" confgurations, where some frms become licensees while others start to develop abatement technologies by their own.

We fnd that, provided the cost asymmetry is not very pronounced and under moderate climate policy, the "mixed" configuration with one firm (the more efficient one) engaging in environmental innovation and the rival frm obtaining the license (henceforth *E*, *L*) represents an equilibrium for the developing country for a wide set of parameters values. As to the impact of climate policy enacted in the developing country on environmental quality, it is shown that a marginal increase in the tax rate may trigger a regime switching—from the *L*, *N* to the *E*, *L* equilibrium—accompanied by a fall in total emissions. Thus a tougher climate policy may become the key driver for inducing the more efficient firm to engage in production of the abatement technology, being also efective in terms of emissions reduction. Finally, the efects on aggregate welfare depend heavily on frms' heterogeneity: only if the cost asymmetry between polluting frms in the developing country is low enough the transition to the *E*, *L* equilibrium would succeed in making the society better of.

Thus our study does not support global and uniform trade liberalisation for EGs. Rather it recognizes that making cleaner technologies developed abroad more easily available might be benefcial for developing countries insofar as this spurs the adoption of tighter emissions policies and the transition to an equilibrium where the more efficient firms engage in environmental innovation.

The paper unfolds as follows. Section [2](#page-5-0) presents the model and analyses the opti-mal licensing strategy. Section [3](#page-16-0) explores the effectiveness of emissions taxation under the different equilibrium configurations. Section [4](#page-20-0) deals with some welfare implications. In Sect. [5](#page-23-0) we discuss an extension of the model. Finally, Sect. [6](#page-25-0) draws some conclusions.

<span id="page-4-0"></span><sup>6</sup> The top largest environmental frms are located in the US, Germany, France and Japan and UK. None of the top frms is located in a developing country (Nimubona [2012;](#page-29-10) Canton [2008](#page-29-15)).

<span id="page-4-1"></span><sup>7</sup> Global trade in selected environmental goods increased from USD 0.9 trillion in 2006 to its peak of USD 1.6 trillion in 2014, with developing countries accounting for a small, but increasing, portion of the global imports of EGs (UNEP [2018\)](#page-29-2). According to a report by the International Trade Center, market size is already substantial in developed countries, while growth rates are particularly high for developing countries in Asia, the Middle East and Africa (see [http://www.intracen.org/publication/Trade-in-envir](http://www.intracen.org/publication/Trade-in-environmental-goods-and-services-Opportunities-and-challenges/) [onmental-goods-and-services-Opportunities-and-challenges/\)](http://www.intracen.org/publication/Trade-in-environmental-goods-and-services-Opportunities-and-challenges/).

# <span id="page-5-0"></span>**2 The model**

Let us consider a partial equilibrium model with two downstream frms, frm 1 and frm 2, and two countries. Country *I* and *II* represent respectively a developed country—or a group of nations—located in the North, and a developing country—or geographical area—located in the South. We assume that the two frms manufacture and sell the same homogeneous good in country *II*. Following Nimubona ([2012\)](#page-29-10), Dijkstra and Mathew ([2016\)](#page-29-12) and Greaker and Rosendahl [\(2008](#page-29-16)), we posit that the downstream output markets are separated in the two countries, so that frm 1 and frm 2 compete locally *à la Cournot* and there is no international trade for this good. When producing, both frms also generate pollution and face an exogenous environmental tax *t*, with  $0 < t < t_1$ , meaning that environmental policy is less stringent than in country *I*.

The inverse demand function is linear and writes as  $P = A - Q$ , where  $Q = (q_1 + q_2)$  denotes total output and  $q_i$  is firm *i*'s output level. The duopoly is asymmetric and the two firms face a constant marginal (and unit) production cost  $c_i$ ,  $i = 1, 2$ . For the sake of simplicity we normalize the unit production cost of firm 1 at zero; thus the production cost of firm 2 is such that  $A/2 > c_2 \ge c_1 = 0.8$  $A/2 > c_2 \ge c_1 = 0.8$ 

In our set-up, we consider that the eco-industry, i.e. the upstream sector supplying polluting frms in abatement goods and services, is not viable for technological and/or fnancial reasons in the South of the world, being owned and located in the developed country (country *I*).[9](#page-5-2)

As common in the literature on EG supply (see e.g. Nimubona [2012;](#page-29-10) David and Sinclair-Desgagnè [2010](#page-29-6); Perino 2010), we assume that the eco-industry is a monopoly selling an environmental good in both markets. However these markets can be seen as segmented, due to diferences in local environmental regulations and standards. It is well-documented that abatement goods and services are nowadays supplied by a few frms operating in an imperfectly competitive market, characterized by signifcant barriers to entry in the form of high fxed costs, IPR patent protection and economies of scope (David and Sinclair-Desgagnè [2010;](#page-29-6) Perino 2010). Moreover, as argued in Nimubona ([2012\)](#page-29-10), "EG-exporting countries might be engaged in a number of policies aimed at promoting their exports, including actions that enhance the market power of their eco-industrial frms through contracting and subcontracting". Since eforts for trade liberalization have at least partially succeeded in easing

<span id="page-5-1"></span><sup>&</sup>lt;sup>8</sup> This condition guarantees interior solutions for output and abatement effort at the equilibrium.

<span id="page-5-2"></span><sup>&</sup>lt;sup>9</sup> The environmental goods and services sector is sometimes called eco-industry or environmental industry. According to the definition proposed by OECD and by the Statistical Office of the European Commission (Eurostat), "The environment industry consists of activities which produce goods and services to measure, prevent, limit, minimize or correct environmental damage to water, air, and soil, as well as problems related to waste, noise and eco-systems. These include cleaner technologies, products and services which reduce environmental risk and minimize pollution and resource use" (Organization for Economic Cooperation and Development/Eurostat [1999\)](#page-29-1). It is widely recognized that pollution abatement accounts for most of the industry income. For an in-depth analysis of the sector and its evolution over time see Sinclair-Desgagnè ([2008\)](#page-29-0) and Eurostat [\(2016](#page-29-17)).

the access to EGs produced abroad for polluting frms in country *II*, we consider no tarifs nor transport costs. Henceforth we will refer to the monopolistic provider of the eco-technology as the external innovator (or frm *M*), namely the foreign frm able to produce abatement goods and to license its technology to one or two polluting frms by means of a fxed-fee licensing contract. Also, as in Kim and Lee ([2016\)](#page-29-13), we set the production cost of the external innovator to zero.<sup>10</sup>

The licensed eco-technology enables frms to reduce pollution and consequently expenditure on emissions tax. We introduce in this basic set-up the possibility for the more efficient firm  $(firm 1)$  to engage in abatement effort. In other words, the more capable frm, instead of buying the licensed technology from the external innovator, may carry out environmental innovation and produce the eco-technology by itself, whilst the choice of the other frm is, as in Kim and Lee [\(2016](#page-29-13)), between buying or not the licensed technology provided by the foreign innovator. We assume that, if frm 1 provides by itself for the environmental good, its abatement function is additively separable. Thus, following Ulph ([1996\)](#page-29-18) and Petrakis and Xepapadeas [\(2003](#page-29-19)), we adopt the specifcation for frm 1's cost function, when it exerts abatement effort:  $c(q_1, a_1) = c_1 q_1 + \left(\frac{a_1^2}{2}\right)$  where  $\left(\frac{a_1^2}{2}\right)$  are the environmental innovation costs. This is additively separable in production costs and environmental innovation costs and characterized by constant returns to scale in production and decreasing returns in abatement effort.

To summarize, the set of abatement options for firm 1 is given by  $S_1 = \{E, L, N\}$ , where *E* stands for engaging in abatement effort, *L* for obtaining a license, and *N* for doing nothing, neither exerting effort nor buying the license. Instead, for firm 2, it is given by  $S_2 = \{L, N\}.$ 

The emission function is defined as  $e_i = e(q_i, a_i) = \frac{(q_i - a_i)^2}{2}$ , where  $i = 1, 2$  and  $a_i$ is the amount of abatement goods purchased by polluters from the innovator or produced by the firm to reduce the emissions level, with  $0 \le a_i \le q_i$ .<sup>[11](#page-6-1)</sup> As customary in this literature, it holds that  $e_{q_i}(q_i, a_i) > 0$ , meaning that more production implies more pollution,  $e_{a_i}(q_i, a_i) < 0$ , so that more abatement lowers total emissions,  $e_{q_i q_i}(q_i, a_i) > 0$ , i.e. the more the firm produces, the more the last unit pollutes, and  $e_{a_i a_i}^{\text{max}}(q_i, a_i) > 0$ , i.e. there are decreasing returns in abatement. Lastly, we have that  $e_{q_i a_i}(q_i, a_i) < 0$ , i.e. the higher the abatement the lower the pollution generated by the last unit of output. The environmental damage function is assumed to be quadratic in aggregate emissions and given by:  $D(E) = dE = \sum_{i=1}^{n} \frac{d}{2}$  $\frac{d}{2}(q_i - a_i)^2$ , where *d* is marginal environmental damage which is constant in total emissions level.

<span id="page-6-0"></span> $10$  On this point Kim and Lee ([2016\)](#page-29-13) prove that fixed-fee licensing is preferred to royalty licensing when the innovator's production cost is either zero or sufficiently small. This finding can be seen as a justification of our assumption.

<span id="page-6-1"></span><sup>&</sup>lt;sup>11</sup> This formulation follows Canton et al.  $(2012)$  $(2012)$  and Kim and Lee  $(2016)$  $(2016)$ . Notice that many studies con-sidering EG provision (see, e.g., David and Sinclair-Desgagnè [2005,](#page-29-4) [2010;](#page-29-6) Canton [2007](#page-29-11); David et al. [2011](#page-29-7)) employ an additively separable emission function, implicitly assuming that frms carry out just end-of-pipe pollution abatement. Introducing a more general emission function—as in Greaker and Rosendahl [\(2008](#page-29-16))—allows to include in the analysis additional segments of the eco-industry.

The game runs as follows: in the frst stage, for a given emission tax, an ecoinnovator located in country *I* announces the availability of a number *k* of licenses for a fxed-fee, *f*(*k*). In the second stage, two polluting frms located in country *II* simultaneously decide whether or not to purchase a license, or (for frm 1) to engage in abatement efort. In the third stage, they determine their abatement levels and choose their outputs competing *a' la Cournot*. As usual, the sub-game perfect Nash equilibrium is derived through backward induction.

#### <span id="page-7-1"></span>**2.1 The scenarios with no endogenous efort**

*L*, *N case: frm 1 is licensed, frm 2 is not licensed.* We briefy recap in what follows the results obtained (see Kim and Lee [2016\)](#page-29-13) in a scenario where there is just one firm able to produce the environmental technology in country *I*. This frm (frm *M*) announces a number  $k = 1$  of licenses and charges the same fixed fee,  $f(k) = f(1)$ . Notice that, being the upstream and downstream markets in country *I* and in country *II* segmented, we proceed to solve the model only for the developing country.

The objective functions of a licensed frm and non-licensed frm are, respectively:

$$
\pi_i^L(k) = P(Q)q_i^L - c_i q_i^L - t(e_i^L)^2 - f(k)
$$
\n(1)

$$
\pi_j^N(k) = P(Q)q_j^N - c_j q_j^N - t(e_j^N)^2 \tag{2}
$$

where  $q_i^L$  and  $q_j^N$  are the output of the licensed firm and the output of the nonlicensed firm, with  $Q = q_i^L + q_j^N$ ,  $e_i^L = \frac{(q_i^L - q_i^L)^2}{2}$  and  $e_j^N = \frac{(q_j^N)^2}{2}$  for  $i, j = 1, 2, i \neq j$ .

When the efficient firm is the licensee, by solving the first-order conditions, we obtain that:

$$
\hat{q}_1^L = \hat{a}_1^L = \frac{A(1+t) + c_2}{3 + 2t},\tag{3}
$$

<span id="page-7-0"></span>
$$
\hat{q}_2^N = \frac{A - 2c_2}{3 + 2t} \tag{4}
$$

Notice that  $\frac{\partial \hat{a}^L_i}{\partial t} > 0$ . As expected, the abatement level of the licensed firm is positively correlated with the level of taxation.

The equilibrium profit of the efficient firm buying the license is then:

$$
\hat{\pi}_1^L(1) = \frac{[A(1+t) + c_2]^2}{(3+2t)^2} - f(1)
$$
\n(5)

while the equilibrium profit of the inefficient firm that does not buy the license and pollutes is:

$$
\hat{\pi}_2^N(1) = \frac{(A - c_2)^2 (2 + t)}{2(3 + 2t)^2}
$$
\n(6)

*N*, *L case:* firm *1* is not licensed, firm 2 is licensed. When an inefficient firm obtains a license, solving the proft maximization problem, it comes out that:

$$
\hat{q}_1^N = \frac{A + c_2}{3 + 2t}
$$

$$
\hat{q}_2^L = \hat{a}_2 = \frac{A(1 + t) - c_2(2 + t)}{3 + 2t}
$$

The equilibrium profits of the efficient firm are:

$$
\hat{\pi}_1^N(1) = \left(\frac{t+2}{2}\right) \left(\frac{A+c_2}{2t+3}\right)^2\tag{7}
$$

while, for the less efficient firm, equilibrium profits read as:

$$
\hat{\pi}_2^L(1) = \left[ \frac{A(1+t) - c_2(2+t)}{2t+3} \right]^2 - f(1)
$$
\n(8)

It is now possible to calculate the value of the license with  $k = 1$  and no endogenous abatement effort. In order to be incentive-compatible, the fixed fee  $f(1)$  for the eco-technology has to be equal to the maximum proft diference of each licensee between the circumstances of acceptance and rejection of the licensing ofer, given that the other firm is not accepting the license at Nash equilibrium. Therefore  $f_i(1)$  is such that  $\hat{\pi}^L_i(1) - \hat{\pi}^N_i(0) = 0$ , and likewise for  $f_j(1)$ .

For each frm the maximum willingness to pay is given by:

<span id="page-8-1"></span>
$$
f_1(1) = \frac{t[A(1+t) + c_2]}{2(3+2t)^2(1+t)^2(3+t)^2}g(A, t, c_2)
$$
\n(9)

<span id="page-8-0"></span>
$$
f_2(1) = \frac{tA(1+t) - c_2(2+t)}{2(3+2t)^2(1+t)^2(3+t)^2}h(A, t, c_2)
$$
\n(10)

where  $g(A, t, c_2) = [2At^4 + 2(7A + c_2)t^3 + 12(3A + c_2)t^2 + 3(13A + 8c_2)t + 15(A + c_2)]$  and  $h(A, t, c_2) = [2(A - c_2)t^4 + 2(7A - 8c_2)t^3 + 12(3A + 4c_2)t^2 + 3(13A + 21c_2)t + 15(A + 2c_2)].$ 

Since  $f_1(1) > f_2(1) > 0$  the innovator will set the fixed fee at  $f_1(1) = \max[f_1(1), f_2(1)]$  and sell the license to the efficient firm.

The equilibrium profts of the external innovator (frm *M*), due to the assumption of zero production costs, are equal to the fxed fee for the sold license, namely:

$$
\pi_{\text{NO}}^M(1) = f_1(1) = \frac{t[A(1+t) + c_2]^2}{2(3+2t)^2(1+t)^2(3+t)^2} [2t^3 + 12t^2 + 24t + 15]
$$
(11)

where "NO" stands for "no endogenous effort". It is easily shown that  $\frac{\partial \pi_{\text{NO}}^{M}(1)}{\partial c} > 0$ and  $\frac{\partial \pi_{\text{NO}}^M(1)}{\partial t} > 0$ . This means that, when the cost gap (i.e. *c*<sub>2</sub>) increases, the value of the license (and therefore the external innovator profit) increases as well. As expected, an increase in the tax rate also boosts frm *M*'s equilibrium profts.

*L*, *L case: frm 1 is licensed, frm 2 is licensed.* If the number of licenses that the external innovator may offer is two, i.e.  $k = 2$ , we obtain that  $\hat{q}_1^L = \frac{A + c_2}{3}$  and  $\hat{q}_2^L = \frac{A - 2c_2}{3}.$ 

The profits, at the equilibrium, are then:

<span id="page-9-1"></span>
$$
\hat{\pi}_1^L(2) = \left(\frac{A + c_2}{3}\right)^2 - f(2)
$$
\n(12)

and

<span id="page-9-2"></span>
$$
\hat{\pi}_2^L(2) = \left(\frac{A - 2c_2}{3}\right)^2 - f(2). \tag{13}
$$

In this scenario, since the external innovator wants to allocate both licenses, the value of the license has to be equal to the lower value between the willingness to pay of the two firms. The maximum willingness to pay for the more efficient firm can be obtained from  $\hat{\pi}_{1}^{L}(2) - \hat{\pi}_{1}^{N}(1) = 0$ ; it turns out to be:  $f_{1}(2) = \frac{t(A+c_{2})^{2}(8t+15)}{18(3+2t)^{2}}$ .

The maximum willingness to pay for the less efficient firm can be derived from  $\hat{\pi}_2^L(2) - \hat{\pi}_2^N(1) = 0$  and reads as follows:  $f_2(2) = \frac{t(A - 2c_2)^2(8t + 15)}{18(3+2t)^2}$ . Since  $f_1(2) > f_2(2)$ , the external innovator will set the optimal fixed fee at  $f_2(2) = \min[f_1(2), f_2(2)]$ . Therefore  $\hat{\pi}_{1}^{L}(2) = (\frac{A+c_{2}}{3})^{2} - f_{2}(2)$  and  $\hat{\pi}_{2}^{L}(2) = (\frac{A-2c_{2}}{3})^{2} - f_{2}(2)$ .

The equilibrium profit for the external innovator when  $k = 2$  is thus:

<span id="page-9-3"></span>
$$
\pi_{\text{NO}}^M(2) = 2f_2(2) = \frac{t(15 + 8t)(A - 2c_2)^2}{9(3 + 2t)^2} \tag{14}
$$

#### <span id="page-9-4"></span>**2.2 Introducing endogenous abatement efort**

Again, at the frst stage of the game, the foreign innovator announces the number of available licenses k, with  $k \in \{1, 2\}$ . In this scenario we introduce the possibility of environmental innovation. Instead of buying the license from an external innovator or to pollute, firm 1 may exert abatement effort by developing environmentallyclean production technologies able to reduce emissions. We remind that, in our setup, it is a prerogative of the more efficient firm to produce by itself the abatement technology. $^{12}$ 

<span id="page-9-0"></span><sup>&</sup>lt;sup>12</sup> There is a bunch of empirical studies showing that firm investment in abatement technology is posi-tively related to firm productivity (Forslid et al. [2011](#page-29-20), [2018\)](#page-29-21), or exhibits an inverted-U-shape with respect to frm productivity.

*E*, *L case: frm 1 exerts abatement efort, frm 2 is licensed.* In this case, with  $k = 1$ , the objective function for the firm that does not buy the license and exerts abatement effort is as follows:

$$
\pi_1^E(1) = P(Q)q_1^E - \left[c_1q_1^E + \frac{(a_1^E)^2}{2}\right] - te_1^E \tag{15}
$$

where the superscript "E" stands for "endogenous abatement effort". The less efficient frm can instead buy the license since we assume that it does not have the capabilities to develop the abatement technology. The proft of a licensed frm is then:

$$
\pi_2^L(1) = P(Q)q_2^L - c_2 q_2^L - t e_2^L - f(1)
$$
\n(16)

where  $c_1 = 0$ ,  $e_i = e(q_i, a_i) = \frac{(q_i - a_i)^2}{2}$ , and  $i, j = 1, 2, i \neq j$ .

From firms' profit maximization problem, we obtain that:  $\tilde{q}_2^L = \frac{\tilde{q}_2}{5t+3}$ <br>=  $\frac{(2t+1)A-(3t+2)c_2}{5t+3}$ ,  $\tilde{q}_1^E = \frac{(A+c_2)(1+t)}{5t+3}$  and  $\tilde{q}_1^E = \frac{t(A+c_2)}{5t+3}$ .

Notice that, as expected, the endogenous effort of the more efficient firm is positively correlated with the tax rate. Due to the specifc features of the licensed ecotechnology—which allows at the equilibrium for an abatement equal to output, the effort of firm 1  $(\tilde{a}_1^E)$  is not always higher than the environmental good level  $(\tilde{a}_2^E)$ bought by the less efficient firm; when the efficiency gap is high, the endogenous effort of the efficient firm is surely greater than the abatement of the less efficient one.[13](#page-10-0)

The resulting equilibrium profts read as follows:

<span id="page-10-1"></span>
$$
\tilde{\pi}_1^E(1) = \frac{(3t^2 + 5t + 2)(A + c_2)^2}{2(5t + 3)^2} \tag{17}
$$

$$
\tilde{\pi}_2^L(1) = \frac{[A(2t+1) - (3t+2)c_2]^2}{(5t+3)^2} - f(1)
$$
\n(18)

*E*, *N* case: firm 1 exerts abatement effort, firm 2 is not licensed. With  $k = 0$ , the objective functions are:

$$
\pi_1^E = P(Q)q_1^E - \frac{(a_1^E)^2}{2} - t\frac{(q_1^E - a_1^E)^2}{2}
$$

$$
\pi_2^N = P(Q)q_2^N - c_2q_2^N - t\frac{(q_2^N)^2}{2}.
$$

By solving the profit maximization problem we get:  $\tilde{q}_1^E = \frac{(1+t)(A(1+t)+c_2)}{3t^2+7t+3}$ ,  $\tilde{q}_2^N = \frac{A(2t+1) - c_2(2+3t)}{3t^2 + 7t + 3}$  and  $\tilde{a}_1^E = \frac{t(A(1+t) + c_2)}{3t^2 + 7t + 3}$ . Therefore equilibrium profts are given by:

<span id="page-10-0"></span><sup>13</sup> If  $A > 4c_2$ , then  $\tilde{a}_1^E < \tilde{a}_2^L$ ,  $\forall t$ . If  $2c_2 < A < 4c_2$ ,  $\tilde{a}_1^E > \tilde{a}_2^L$  for  $t > \frac{A-c_2}{4c_2-A} \ge \frac{1}{2}$ .

<span id="page-11-0"></span>
$$
\tilde{\pi}_1^E(0) = \frac{\left[A(1+t) + c_2\right]^2 \left(3t^2 + 5t + 2\right)}{2 \left(3t^2 + 7t + 3\right)^2}
$$
\n(19)

<span id="page-11-1"></span>
$$
\tilde{\pi}_2^N(0) = \frac{(t+2)[A(2t+1) - c_2(2+3t)]^2}{2(3t^2 + 7t + 3)^2}
$$
\n(20)

Under the assumption that frm 1 may enact environmental innovation and with  $k = 1$ , the value of the license has to be such that firm 1 is indifferent between buying the license—with payoff  $\hat{\pi}_{1}^{L}(1)$  as in Eq. [\(5](#page-7-0))—and enacting environmental innovation, gaining  $\tilde{\pi}_{1}^{E}(0)$ , as in Eq. [\(19](#page-11-0)). This means that  $f_{1}(1)$  is such that  $\hat{\pi}_1^L(1) - \tilde{\pi}_1^E(0) = 0.$ 

The value of the license for the efficient firm is then:

<span id="page-11-2"></span>
$$
f_1(1) = \frac{t(3t+5)(2t^2+6t+3)\Delta^2}{2(3t^2+7t+3)^2(3+2t)^2}
$$
(21)

where  $\Delta = [A(1 + t) + c_2].$ 

For the less efficient firm the cost of the license  $f_2(1)$  has to be such that  $\tilde{\pi}_{2}^{L}(1) - \tilde{\pi}_{2}^{N}(0) = 0.$ 

The value of  $f_2(1)$  is then:

$$
f_2(1) = \frac{t\Phi^2[15 + 54t + 59t^2 + 18t^3]}{2(3t^2 + 7t + 3)^2(5t + 3)^2}
$$
(22)

with  $\Phi = [A(1 + 2t) - c_2(2 + 3t)].$ 

Let us defne now

$$
c_f = \frac{135A + 756A t + 1617A t^2 + 1640A t^3 + 786A t^4 + 144A t^5}{216 t^5 + 1140 t^4 + 2236 t^3 + 2013 t^2 + 846 t + 135} + \frac{\sigma A (10 t^2 + 9 + 21 t)}{216 t^5 + 1140 t^4 + 2236 t^3 + 2013 t^2 + 846 t + 135}
$$
  
where  $\sigma = \sqrt{(3 t + 5) (2 t^2 + 6 t + 3) (18 t^3 + 59 t^2 + 54 t + 15)}$  (23)

Carrying out the comparison between the values of the license when  $k = 1$  and firm 1 may engage in environmental innovation, we can state that:

**Proposition 1** *With*  $k = 1$ *, and for a given t, when*  $0 < c_2 < c_f$  *the optimal fixed fee is*  $f_2(1)$  *and the less efficient firm obtains the license. When*  $c_2 > c_f$  *the optimal fixed fee is*  $f_1(1)$  *and the more efficient firm obtains the license.* 

*Proof* See Appendix A. □

It can be proved (see Appendix A) that the inequality  $f_2(1) > \frac{c}{2} f_1(1)$  always holds for every value of *t* when  $c_2$  < (>)  $c_f$ .



<span id="page-12-0"></span>**Fig. 1** Optimal licensing strategy if  $k = 1 (A = 30)$ 

This proposition shows that, when the cost asymmetry is pronounced, the external innovator opts for an exclusive licensing contract with the more efficient firm, and *vice versa*, when it is low, frm 2 is the licensee. This is due to the fact that a high  $c_2$  depresses output and thus consumption of the environmental good by the less efficient firm, thereby making licensing to this firm less attractive. Conversely, a pronounced cost asymmetry boosts both production and willingness to pay for the license by firm 1. Besides, it is interesting to point out that  $c_f$  is positively related with *t* meaning that a stringent environmental policy (i.e. a quite high tax rate) will stimulate the efficient firm to perform environmental innovation.

As Fig. [1](#page-12-0) highlights, in the area below  $c_f$ , the foreign innovator (firm  $M$ ) sets the license price at the maximum possible price  $f_2(1)$ , and the less efficient firm obtains the license. Hence, when  $k = 1$  and  $c_2 < c_f$  the equilibrium configuration *E*, *L* may occur, where the less efficient firm buys the license  $(L)$  while the efficient one is engaged in environmental innovation (*E*).

When  $k = 1$  and  $c_2 > c_f$  the equilibrium configuration is given by *L*, *N*, where no effort arises, the more efficient firm buys the license and the other does abate at all. This is not the preferred outcome if the government goal in the developing country is to induce innovation by local frms.

The equilibrium proft of the external innovator (frm *M*) is either

<span id="page-12-1"></span>
$$
\pi_{\text{end}}^M(1) = f(1) \cdot 1 = f_2(1) \tag{24}
$$

or

<span id="page-12-2"></span>
$$
\pi_{\text{end}}^M(1) = f(1) \cdot 1 = f_1(1) \tag{25}
$$

where "end" stands for "endogenous effort".

#### **2.3 Value of the license with endogenous effort and**  $k = 2$

The hypothesis of endogenous effort plays an important role when we analyse the license value with  $k = 2$ , because, differently from the set-up in Kim and Lee  $(2016)$  $(2016)$ , the efficient firm faces a choice between buying the license from the external provider or performing environmental innovation and producing the environmental good by itself.<sup>14</sup> As usual, each firm's maximum willingness to pay for the license has to respect the incentive compatibility constraint, which is modifed accordingly.

Thus, for the efficient firm, the value of  $f_1(2)$  has to be such that  $\hat{\pi}_1^L(2) - \tilde{\pi}_1^E(1) = 0$ where  $\hat{\pi}_{1}^{L}(2)$  is as in Eq. [\(12](#page-9-1)) and  $\tilde{\pi}_{1}^{E}(1)$  is as in Eq. [\(17](#page-10-1)). Therefore:

$$
f_1(2) = \frac{t(A + c_2)^2 (23t + 15)}{(450t^2 + 540t + 162)}
$$

Likewise, for the less efficient firm,  $f_2(2)$  has to be such that  $\hat{\pi}_2^L(2) - \tilde{\pi}_2^N(0) = 0$ where  $\hat{\pi}_2^L(2)$  is as in Eq. [\(13](#page-9-2)) and  $\tilde{\pi}_2^N(0)$  is as in Eq. ([20\)](#page-11-1).

Thus:

$$
f_2(2) = \frac{\Phi(1+t)[A(1+t) + c_2] + \Phi^2}{(3t^2 + 7t + 3)^2} + \frac{\Phi^2t}{2(3t^2 + 7t + 3)^2} + \frac{(A - 2c_2)^2}{9} - \frac{\Phi(A - c_2)}{3t^2 + 7t + 3}
$$
(26)

with  $\Phi = [A(1 + 2t) - c_2(2 + 3t)].$ 

**Proposition 2** *With*  $k = 2$  *the optimal fixed fee is*  $f_2(2)$  *and both firms obtain the license*.

#### *Proof* See Appendix B.

As shown in Appendix B, it can be proved that  $f_1(2) > f_2(2)$  for feasible values of the tax rate *t*. In order to sell both licenses, the external innovator will set the license price equal to  $min{f_1(2), f_2(2)} = f_2(2)$ . The external innovator profit is thus  $\pi^{M}(2) = 2 \min\{f_{2}(2), f_{1}(2)\} = 2f_{2}(2)$  since it sells two licenses at fee  $f_{2}(2)$  having no production costs.

Carrying out some comparative statics, it turns out that  $\frac{\partial \pi^M(2)}{\partial t} > 0$ . This means that a tougher environmental policy spurs the external innovator profts because the licensees will increase their willingness to pay to reduce their tax burden. Also,  $\frac{\partial \pi^M(2)}{\partial c_2} > 0$ ,

implying that the higher is the efficiency gap, the better off is the external innovator.

Moreover, it is possible to show that:

<span id="page-13-1"></span>
$$
\qquad \qquad \Box
$$

<span id="page-13-0"></span><sup>&</sup>lt;sup>14</sup> Notice that the *N*, *L* configuration is dominated by the *L*, *N* one, as shown in Sect. [2.1.](#page-7-1) Therefore, also the *E*, *L* equilibrium is strictly preferred to the *N*, *L* one. Accordingly, we neglect this scenario in what follows.

<span id="page-14-4"></span>**Proposition 3** *The profit of the foreign innovator when the efficient firm may exert abatement efort is lower than in the case when he is the only innovator*.

*Proof* See Appendix C. □

Comparing both  $\pi_{end}^M(1) = f_2(1)$  and  $\pi_{end}^M(1) = f_1(1)$  with  $\pi_{NO}^M(1)$  from Eq. ([11\)](#page-8-0), we get that the external innovator can extract more value when the efficient firm does not have the capability to develop environmental innovation. The same conclusion holds if one compares  $\pi^M(2) = 2f_2(2)$  with  $\pi^M_{\text{NO}}(2)$  from Eq. ([14\)](#page-9-3). This means that, in the absence of other options, the maximum willingness to pay for the license by local firms is greater, thus boosting firm *M*'s profits.

#### <span id="page-14-1"></span>**2.4 Optimal licensing strategy**

At the frst stage of the game the external innovator announces the number of licenses he will provide. In order to make this decision the foreign producer of the eco-technology compares the equilibrium profits for  $k = 1$  and  $k = 2$ , depending also on the cost asymmetry between the two polluting frms. It comes out that:

<span id="page-14-2"></span>**Proposition 4** *If*  $0 \le c_2 < c_h$ , *then*  $\pi^M(2) > \pi^M(1)$  *and firm M will provide two licenses. If*  $c_2 > c_h$ , *then*  $\pi^M(2) < \pi^M(1)$  *and he will provide only one license to the inefficient firm.* 

*Proof* See Appendix D. □

Moreover,

<span id="page-14-3"></span>**Proposition 5** *If*  $0 \leq c_2 < c_g$ , the external innovator prefers to sell two licenses *w.r.t licensing to the efficient firm, whereas, when*  $c_2 > c_g$  *he prefers to sell one license to the more efficient firm.* 

*Proof* See Appendix D. ◯

As shown in Appendix D, for a reasonable range of values of the tax rate *t*, we are allowed to consider a threshold ranking such that  $0 < c_h < c_g < c_f$ , as depicted in Fig.  $2<sup>15</sup>$  Hence, for a given *t*, and combining the results in the two Propositions here above, the equilibrium licensing strategies are as follows:

• if  $c_2$  is above the threshold  $c_f$  the external innovator does not have the incentive to provide two licenses since he can extract more proft by selling only one license to the efficient firm. He will therefore optimally set the number of licenses equal

<span id="page-14-0"></span><sup>&</sup>lt;sup>15</sup> Assuming that the tax rate on emissions is moderate is coherent with stylized facts about developing countries, as recognized in the policy debate. Moreover, the theoretical literature suggests that, in the presence of abatement technology trade, the tax rate that maximizes domestic welfare in country *II* should be lower than marginal damage.



<span id="page-15-0"></span>**Fig. 2** Optimal licensing strategies  $(A = 30)$ 

to one  $(k = 1)$ . The equilibrium configuration is thus *L*, *N* where firm 1 buys the license and frm 2 does not abate at all;

- when  $c_h < c_2 < c_f$ , the external innovator sets the number of licenses equal to one  $(k = 1)$  and the efficient firm will engage in abatement effort. Instead, the less efficient firm will buy the license at the price specified in Eq.  $(21)$  $(21)$ . The equilibrium confguration arising in this case is *E*, *L*;
- finally, when  $c_2$  is below the threshold  $c_h$ , the external innovator will sell two licenses and the equilibrium confguration *L*, *L* occurs, where both frms are licensees.

The equilibrium regions are summarized in Fig. [2,](#page-15-0) according to the degree of cost asymmetry between the two firms  $(c_2)$  and to the stringency of environmental policy set in the developing country.

Notice that in our set-up, provided the cost asymmetry is not very high, there is always room for an equilibrium where a firm exerts effort and produces by itself the environmental good, namely the *E*, *L* case. In other words, if a frm may engage in environmental innovation, the equilibrium with  $k = 2$  is less likely to occur, as compared to a set-up where frms' options are restricted to being a licensee or do not abate at all. This is because a "mixed" equilibrium arises for  $c_h < c_2 < c_f$ , in contrast with the results in Kim and Lee [\(2016](#page-29-13)), where, below a certain threshold value for  $c_2$ , the innovator's optimal strategy is to provide two licenses  $(k = 2)$ . Notice also that the likelihood of the *E*, *L* equilibrium is enhanced under moderate climate policy, a condition very common in developing economies.

#### <span id="page-16-0"></span>**3 Licensing strategies and total emissions**

In this section we carry out a comparison of total emission levels under the diferent scenarios. Our aim in so doing is to assess the environmental efectiveness of mitigation measures, assuming that pollution is not transboundary.<sup>[16](#page-16-1)</sup> We remind that the emission function we employ is defined as:  $e_i = e(q_i, a_i) = \frac{(q_i - a_i)^2}{2}$  where  $i = 1, 2$ . Thus total emissions level is given by  $E = e_1 + e_2$ .

*L*, *N* case,  $k = 1$ . When firm 1 is the licensee and firm 2 is not (*L*, *N* case), we obtain that total emissions are as follows:

$$
E_{\text{L,N}}(k=1) = \frac{(A - 2c_2)^2}{2(2t + 3)^2}
$$
 (27)

Notice that this scenario represents the equilibrium outcome (see Sect. [2.4\)](#page-14-1) when  $c_2 > c_f$ .

 $E$ , *N* case,  $k = 0$ . In this scenario, i.e. when firm 1 exerts abatement effort and frm 2 does not buy the license, total emissions are given by:

$$
E_{\text{E,N}}(k=0) = \frac{(5A^2 - 12A c_2 + 9c_2^2) t^2 + (6A^2 - 12A c_2 + 12c_2^2) t}{18 t^4 + 84 t^3 + 134 t^2 + 84t + 18}
$$
  
+ 
$$
\frac{2A^2 - 2A c_2 + 5c_2^2}{18 t^4 + 84 t^3 + 134 t^2 + 84t + 18}
$$
 (28)

 $E, L \, case, k = 1$ . In this scenario firm 1 performs environmental innovation and firm 2 is the licensee. Thus total emissions read as:

$$
E_{\rm E,L}(k=1) = \frac{(A + c_2)^2}{2(5t + 3)^2}
$$
 (29)

We remind that this case represents an equilibrium whenever  $c_h < c_2 < c_f$ .

*L*, *L case*,  $k = 2$ . When  $k = 2$  both firms buy the license. Therefore  $e_1^L = 0$ ,  $e_2^L = 0$ , and total emissions are null. This is an equilibrium outcome when  $c_2 < c_h$ .

*E*, *E* case,  $k = 0$ . For the sake of comparison, we also solved the model under the hypothesis that, *ceteris paribus*, both firms engage in abatement effort. Therefore the emissions by frm 1 and by frm 2 are given, respectively, by:

$$
e_1^E = \frac{\left[A + c_2 + t\left(2A + c_2\right)\right]^2}{2\left(8t^2 + 10t + 3\right)^2}
$$

$$
e_2^E = \frac{\left[A - 2c_2 + t\left(2A - 3c_2\right)\right]^2}{2\left(8t^2 + 10t + 3\right)^2}
$$

<span id="page-16-1"></span><sup>&</sup>lt;sup>16</sup> As claimed in Nimubona [\(2012](#page-29-10)), considering transboundary pollution with asymmetric countries would make the analysis cumbersome. We foresee that, under this hypothesis, regulators in both countries should coordinate their efforts to deal with inefficiencies due to the presence of the the eco-industry. The issue of pollution leakage is tackled in Canton [\(2008](#page-29-15)), assuming that polluting firms are price-takers, countries are symmetric, and taxes are imposed also on the eco-industry.

and total emissions are then:

$$
E_{\text{E,E}}(k=0) = \frac{\left(8A^2 - 8A c_2 + 10 c_2^2\right) t^2 + \left(8A^2 - 8A c_2 + 14 c_2^2\right) t}{128 t^4 + 320 t^3 + 296 t^2 + 120 t + 18} + \frac{2A^2 - 2A c_2 + 5 c_2^2}{128 t^4 + 320 t^3 + 296 t^2 + 120 t + 18}
$$
\n(30)

*N*, *N case*,  $k = 0$ . Finally a scenario which could be of some interest, representing a sort of benchmark, is when both frms do not buy the license nor carry out environmental innovation. At the equilibrium, their emissions are:

$$
e_1^N = \frac{(A + c_2 + A t)^2}{2 (t^2 + 4t + 3)^2}
$$

$$
e_2^N = \frac{[A - 2c_2 + t (A - c_2)]^2}{2 (t^2 + 4t + 3)^2}
$$

Thus total emissions read as:

$$
E_{N,N}(k=0) = \frac{\left(2A^2 - 2A c_2 + c_2\right)^2 t^2 + \left(4A^2 - 4A c_2 + 4c_2^2\right) t + 2A^2 - 2A c_2 + 5c_2^2}{2(t+3)^2(t+1)^2}
$$
\n(31)

Considering the three diferent scenarios occurring at the equilibrium, it is immediate to fnd out that the *L*, *L* confguration dominates over all other cases in terms of minimizing total emissions.<sup>17</sup> Moreover, it is possible to show that:

**Proposition 6** *If*  $t > (3c_2)/(A - 4c_2) > 0$ , then total emissions under the E, L sce*nario are lower than under the L*, *N case*.

*Proof* Straightforward. First consider that  $E_{LN} - E_{EL}$  is an increasing and concave function of *t*. This is solved for  $t_1 = ((3c_2)/(A - 4c_2))$  and for  $t_2 = (-3(2A - c_2)/(7A - 8c_2))$ , with  $t_2 < 0$  and  $t_1 > 0$  for  $A > 4c_2 > 0$ .  $\Box$ 

Interestingly, the function  $E_{\text{LN}} - E_{\text{EL}}$  increases in *A*, for  $A > 4c_2 > 0$ , meaning that the superior performance of the  $E$ ,  $L$  configuration, in terms of leading to lower emissions, is magnifed as market size in country *II* increases.

While Figs. [3](#page-18-0) and [4](#page-18-1) illustrate the relationship between total emissions and the tax rate in all possible scenarios (and for "sufficiently low" and "quite high" values of  $c_2$ , respectively), Figs. [5](#page-19-0) and [6](#page-19-1) focus on equilibrium scenarios (again, for "sufficiently low" and "quite high" values of  $c_2$ ).

<span id="page-17-0"></span><sup>&</sup>lt;sup>17</sup> In this equilibrium configuration emissions are zero, which is mainly driven by the emission function we employ. With a diferent specifcation, the utterly superior performance of the licensed technology would be mitigated.



<span id="page-18-0"></span>**Fig. 3** Low  $c_2$ : total emissions comparison  $(A = 30, c_2 = 2)$ 



<span id="page-18-1"></span>**Fig.** 4 High  $c_2$ : total emissions comparison ( $A = 30$ ,  $c_2 = 3.5$ )

For low levels of the tax rate, irrespective of the cost asymmetry, the total emission level is minimized, but for the  $L$ ,  $L$  configuration, when the efficient firm is the licensee and the inefficient firm does not abate at all  $(L, N)$  scenario). However, for intermediate values of *t*, the mixed equilibrium *E*, *L* yields the lowest level of emissions, performing better than the case where both frms carry out environmental innovation. Notice that only when the tax rate is high enough, the scenario where



<span id="page-19-0"></span>**Fig. 5** Low  $c_2$ : focus on emissions comparison ( $A = 30$ ,  $c_2 = 2$ )



<span id="page-19-1"></span>**Fig.** 6 High  $c_2$ : focus on emissions comparison ( $A = 30$ ,  $c_2 = 3.5$ )

both firms exert abatement effort would lead to an overall level of emissions comparable with the *L*, *N* case (but still higher with respect to the *E*, *L* scenario). Nevertheless, when *t* reaches that level, the equilibrium outcome would be represented by the *L*, *L* confguration.

From the assessment of total emissions, it turns out that increasing the tax rate may bring about a regime switching—from the *L*, *N* to the *E*, *L* equilibrium confguration—associated with a reduction in overall emissions. The threshold value of *t* leading to a regime switching is higher the greater is the cost heterogeneity among firms: when  $c_2$  becomes particularly high the economy might be "trapped" in the *L*, *N* equilibrium confguration with a suboptimal emissions level. In other words, a tougher climate policy may become the key driver for inducing the more efficient frm to engage in production of the abatement technology, being also efective in terms of emissions reduction.

This result somehow mimics well-established fndings from the empirical literature about the relevant role played by regulation and environmental policy for the difusion of climate change-mitigation technologies. Notably, since 1990 environmental policies have accelerated the pace of innovation and technology transfer by creating a market for environmentally-sound technologies (Dechezleprêtre et al. [2011](#page-29-22)). At the same time, and interestingly for our work, the availability of new technologies (and thus the increasing integration of the international technology space) seems to have affected the regulation decision of non-innovative countries, accelerating the adoption of more stringent measures in developing countries. Evidence of this virtuous circle is documented by Lovely and Popp [\(2011](#page-29-23)).

Through the lenses of our model, easing the access to EGs produced abroad for developing countries would be benefcial insofar as it spurs the adoption of tighter emissions policies, thus bringing about a regime switching, from the *L*, *N* to the *E*, *L* equilibrium confguration.

## <span id="page-20-0"></span>**4 Some considerations on welfare**

In this section we propose a comparison of the welfare properties of the diferent possible scenarios, with the aim of providing some policy implications.<sup>18</sup> Again, we examine all the scenarios, even the cases that are not equilibrium confgurations, in order to obtain an exhaustive picture. However, we will pay a particular attention to the equilibrium confgurations, depending on the degree of local frms' heterogeneity.

*L*, *N case*,  $k = 1$ . When  $k = 1$ , and the efficient firm is the licensee while the other frm does not buy the license, the total welfare function is given by:

<span id="page-20-2"></span>
$$
W_{L,N}(1) = \int_0^Q P(u)du - c_2 q_2^N - de_2^N - f_1(1)
$$
 (32)

 $E, L \, case, k = 1$ . In this case the foreign innovator provides the license only to the less efficient firm while the other performs environmental innovation. Thus total welfare reads as:

<span id="page-20-3"></span>
$$
W_{\text{E,L}}(1) = \int_0^Q P(u)du - c_2 q_2^L - \frac{a_1^2}{2} - de_1^E - f_2(1)
$$
 (33)

<span id="page-20-1"></span><sup>&</sup>lt;sup>18</sup> The full analytical expressions for equilibrium welfare functions are not reported here below for lack of space. They are available from the authors upon request.



<span id="page-21-0"></span>**Fig. 7** Low  $c_2$ : total welfare comparison  $(A = 30, c_2 = 2, d = 4)$ 

*L*, *L case*,  $k = 2$ . When  $k = 2$  and an external innovator provides the license to both frms, total welfare is as follows:

<span id="page-21-1"></span>
$$
W_{L,L}(2) = \int_0^Q P(u)du - c_2 q_2^L - 2f_2(2)
$$
 (34)

For the sake of comparison we consider also:

*E*, *E* case,  $k = 0$ . This is the case with  $k = 0$ , where both firms exert abatement effort. Total welfare is given by:

$$
W_{\rm EE}(0) = \int_0^Q P(u) du - c_2 q_2^E - \frac{a_1^2}{2} - \frac{a_2^2}{2} - de_1^E - de_2^E \tag{35}
$$

*N*, *N case*,  $k = 0$ . Finally, when  $k = 0$ , and both firms do nothing, neither buy the license or exert effort, the welfare function is:

$$
W_{N,N}(1) = \int_0^Q P(u)du - c_2 q_2^N - de_1^N - de_2^N \tag{36}
$$

The highly non-linear nature of the aggregate welfare measures, evaluated at equilibrium quantities and abatement levels, prevents us from obtaining general results. Therefore, the analysis of the welfare properties of the diferent confgurations is carried out by means of numerical methods. We argue that this methodology does not unduly restrict the signifcance of our analysis.



<span id="page-22-0"></span>**Fig. 8** High *c*<sub>2</sub>: total welfare comparison (*A* = 30, *c*<sub>2</sub> = 3.5, *d* = 4)

For a quite low level of  $c_2$  (see Fig. [7](#page-21-0)), and for a moderate level of taxation, the equilibrium confgurations are given by *L*, *N* and *E*, *L*, depending on the tax rate. In this scenario, switching from the equilibrium where frm 1 is the licensee and the other firm does not abate at all  $(L, N)$  to the mixed equilibrium where the efficient firm exerts effort and the less efficient one gets the license  $(E, L)$  brings about also an increase in aggregate welfare. However, as the fgure highlights, under tougher climate policy (i.e. higher *t*), inducing both frms to engage in the production of environmental goods (i.e. the *E*, *E* scenario) would make the society better off.

On the other hand, when the cost asymmetry is more pronounced, namely for a higher value of  $c_2$  (see Fig. [8\)](#page-22-0), it turns out that switching from the *L*, *N* equilibrium to the configuration with endogenous effort  $(E, L)$  would imply a decrease in aggregate welfare. More precisely, there exists a range of *t* values such that having any confguration with at least one licensee or a duopoly with both frms producing their environmental technology would deliver more welfare with respect to the *E*, *L* confguration. This fnding might be due to the particular emissions technology function, which allows frms to abate all their emissions when they are licensees, coupled with the positive correlation in the *E*, *L* case between abatement costs born by firm 1 and the cost asymmetry parameter, while the less efficient firm pays a license fee increasing in  $c_2$ .

It is noteworthy to mention that in both cases, either with low or with high cost asymmetry, the configuration with  $k = 2$  ( $L$ ,  $L$ ) delivers the highest level of aggregate welfare. Nevertheless, if the heterogeneity is quite pronounced, switching to the *L*, *L* equilibrium would require a tight emissions taxation regime, a condition uncommon (and suboptimal) in developing countries.



<span id="page-23-1"></span>**Fig. 9** Very high  $c_2$ : total welfare comparison ( $A = 30$ ,  $c_2 = 5$ ,  $d = 4$ )

Moreover, as  $c_2$  increases, the economy might be "trapped" in the *L*, *N* equilibrium confguration. In this last case, as shown in Fig. [9,](#page-23-1) the level of aggregate welfare is always suboptimal, regardless of the tax rate value.

#### <span id="page-23-0"></span>**5 Intellectual property rights regimes: discussion of results**

Introducing endogenous abatement effort can be interpreted as allowing the efficient frm in the developing country to imitate a patented technology developed abroad (i.e. in country *I*), due to a regime of weak patent protection or to patenting of the eco-technology only in the developed country.<sup>19</sup> To explore this, one can consider a game where at the frst stage the regime of IPR protection is chosen in country *II*, being the strategy set for the government in the developing country given by  $S = \{W, ST\}$ , namely *Weak* or *Strong*. Thus, under the *Weak* regime, the more efficient frm is able to engage in abatement efort through costly imitation of the technology owned by the foreign innovator. On the other hand, if the *Strong* regime is in place, i.e. when patent protection is strong (or the technology is patented in both countries), both polluting frms cannot develop the technology by their own and—as in Sect. [2.1](#page-7-1)—can either buy the license or do not abate at all.

As a matter of fact, Kim and Lee [\(2016](#page-29-13)) solve for the subgame perfect Nash equilibrium when the *Strong* regime is in place , while in our model (in Sect. [2.2](#page-9-4) et seq.) we derive equilibrium strategies for the subgame under the *Weak* IPR regime. In particular, for the former subgame, it is found that the external innovator licenses to both firms (only to the efficient firm) if  $c_2 \leq c_f(c_2 > c_f)$  or for *t* small enough

<span id="page-23-2"></span>We are indebted to an anonymous referee for suggesting this point.

(greater than  $t_f$ ) (see Kim and Lee [2016,](#page-29-13) Proposition 1).<sup>20</sup> For the latter subgame (*Weak*) we remind that the equilibria are represented by *N*, *L*, or *E*, *L* or fnally *L*, *L*, according to the values of the parameter  $c<sub>2</sub>$  and to the tax rate (see Propositions [4](#page-14-2)) and [5](#page-14-3) here above and Fig. [2](#page-15-0)).

Notice that, as shown in Proposition  $3$ , all the strategies in the subgame with endogenous abatement effort are dominated by the strategies in subgame with strong IPR protection, i.e. when frm *M* is the only innovator. Thus, if the foreign innovator *could* infuence the choice of the IPR regime, he would strictly prefer, as expected, strong patent protection in both countries, in order to discourage imitation.

Regarding the effects on total emissions, we found that, for a low degree of cost asymmetry (say  $c_2 = 2$ ), having strong IPR protection would lead to a "regime" switch"—from *L*, *L* to *L*, *N* equilibrium—accompanied by a worsening in environmental quality for  $t > 1.6$ , as compared with the regime allowing for imitation.<sup>[21](#page-24-1)</sup> Yet, for a higher degree of cost asymmetry (e.g. with  $c_2 = 3.5$ ), the equilibrium would be given by *N*,  $L$ ,  $\forall t$ , with an increase in total emissions for  $t > 0.5$ , with respect to the alternative regime. $^{22}$  $^{22}$  $^{22}$ 

We then performed numerical simulations, following the approach in Sect. [4,](#page-20-0) with the aim of comparing the welfare properties of the two subgames at hand, in the case with imitation by the efficient firm, and in the scenario with strong patent protection. Notably, we considered, for the subgame with *Strong* IPR protection, the following equilibrium welfare functions:

$$
W_{L,N}^S(1) = \int_0^Q P(u)du - c_2 q_2^N - de_2^N - f_1(1)
$$
 (37)

where  $f_1(1)$  is as in Eq. ([9\)](#page-8-1), and

$$
W_{L,L}^{S}(2) = \int_{0}^{Q} P(u)du - c_2 q_2^L - 2f_2(2)
$$
 (38)

with  $f_2(2) = \frac{t(A-2c_2)^2(8t+15)}{18(3+2t)^2}$  (see Sect. [2.1\)](#page-7-1). As to the subgame with *Weak* patent protection, we took into account  $W_{LN}(1)$  from Eq. ([32\)](#page-20-2),  $W_{EL}(1)$  as in Eq. [\(33](#page-20-3)) and  $W_{\text{LL}}(2)$  as in Eq. [\(34](#page-21-1)).

For any degree of cost asymmetry, we found that, reasonably, letting strong patent protection is never the preferred choice for the government in country  $II^{23}$ . The rationale for this result could be due to the higher willingness to pay for the abatement technology in the subgame with strong IPR protection, which boosts frm *M*'s profts accruing to the developed country and consequently depresses welfare in country *II*.

<span id="page-24-0"></span><sup>&</sup>lt;sup>20</sup> We found that the threshold  $c_f$  is a decreasing convex function of *t*, such that for  $c_2$  and/or *t* small, the equilibrium configuration is given by  $L$ ,  $L$ , and *vice versa* for  $c_2$  and/or  $t$  high enough, the equilibrium strategies are *L*, *N*.

<span id="page-24-1"></span> $21$  See Fig. [5,](#page-19-0) Sect. [3.](#page-16-0)

<span id="page-24-2"></span> $22$  See Figs. [5](#page-19-0) and [6](#page-19-1), Sect. [3](#page-16-0).

<span id="page-24-3"></span> $23$  Analytical results and numerical simulations are available from the authors upon request.

## <span id="page-25-0"></span>**6 Main conclusions**

We contribute to the debate on trade liberalization for abatement goods and services by comparing diferent equilibrium confgurations occurring in a developing country, one of them involving also domestic production of the abatement technology.

With this aim in mind, we developed a two-country model with two downstream frms and one upstream eco-sector, which is consistent with several stylized facts about environmental goods provision and consumption in developing countries. We obtain that fully relying on EGs supplied by an external foreign innovator is not always desirable if policy makers in the developing country want to promote environmental quality and enhance social welfare.

Under rather general conditions, increasing the emissions tax rate and switching from the *N*, *L* to the *E*, *L* equilibrium would lead to a fall in total emissions. Hence there is scope for climate policy to become a driver for in-house production of the abatement technology by the more efficient firms, being also effective in terms of emissions reduction. In other words, efforts for trade liberalization in EGs could imply—making the abatement technology more easily available and inducing a more stringent emissions taxation—the transition to an equilibrium where some local frms in developing countries engage in environmental innovation with an improvement in environmental quality.

Nevertheless, the effects on aggregate welfare are not clear-cut, as they heavily depend on frms' heterogeneity: only if the cost asymmetry is low enough the transition to the  $E$ ,  $L$  equilibrium would make the society better off. Thus one should carefully consider the specifc industrial structure of a developing country before embarking in policy prescriptions.

In our view, the paper also sheds light on the importance of additional conditions affecting over time the outcome of trade-liberalization efforts, notably market size, learning-by-doing processes resulting in frms' costs diminishing over time and technological spillovers enhancing the transfer of knowledge across frms. On this regard, an interesting case is represented by Chile, as reported in Sauvage ([2014](#page-29-24)), where a relatively open trade and foreign investment regime *along with* a commitment to environmental protection have been in place since the second half of the 1990s. This induced foreign frms in the EG sector to invest and open local subsidiaries, including partnerships with Chilean frms. The country initially experienced an increase in imports of abatement technologies and higher FDI infows. But over time this stimulated production of EGs by local frms, which succeeded in accumulating know-how and expertise, so that nowadays Chile is a regional hub for Latin America and a regional leader in the provision of these goods and services.

To conclude, we are aware of the simplifying hypotheses adopted in our study, in particular the fact that the contract for the licensed technology always involves a fxed fee. A more careful modelling of the foreign market for imported EGs, introducing monopolistic competition (for instance a dominant frm along with a competitive fringe) would enrich the analysis. Moreover, we focussed on the impact of climate policy assuming an exogenous tax rate. Needless to say, the model should

be extended endogenizing environmental policy. Besides, it would be interesting to hypothesize the presence of foreign subsidiaries producing EGs in the developing country and interacting through knowledge spillovers with local frms. These issues are left for future research.

## **Appendix A**

Let  $\vartheta$  be the difference between the value of the two licenses,  $f_1(1)$  and  $f_2(2)$ 

$$
\theta = f_1(1) - f_2(2)
$$
\n
$$
= \left( -\frac{216 t^6 + 1140 t^5 + 2236 t^4 + 2013 t^3 + 846 t^2 + 135 t}{600 t^6 + 3920 t^5 + 10206 t^4 + 13482 t^3 + 9504 t^2 + 3402 t + 486} \right) c_2^2
$$
\n
$$
+ \frac{288 A t^6 + 1572 A t^5 + 3280 A t^4 + 3234 A t^3 + 1512 A t^2 + 270 A t}{600 t^6 + 3920 t^5 + 10206 t^4 + 13482 t^3 + 9504 t^2 + 3402 t + 486} c_2 + \frac{46 A^2 t^6 + 198 A^2 t^5 + 307 A^2 t^4 + 198 A^2 t^3 + 45 A^2 t^2}{600 t^6 + 3920 t^5 + 10206 t^4 + 13482 t^3 + 9504 t^2 + 3402 t + 486}
$$

We want to assess whether  $\gamma > 0$ . Solving  $\gamma$  w.r.t  $c_2$  we obtain two different solutions of  $c_2$ , say  $c_f(-)$  and  $c_f(+)$ .

$$
c_f = \begin{cases} \frac{135A+756A\,t+1617A\,t^2+1640A\,t^3+786A\,t^4+144A\,t^5-9A\,\sigma-21A\,t-10A\,t^2\,\sigma}{216\,t^5+1140\,t^4+2236\,t^3+2013\,t^2+846\,t+135} \\ \frac{135A+756A\,t+1617A\,t^2+1640A\,t^3+786A\,t^4+144A\,t^5+9A\,\sigma+21A\,t\,\sigma+10A\,t^2\,\sigma}{216\,t^5+1140\,t^4+2236\,t^3+2013\,t^2+846\,t+135} \end{cases}
$$

where  $\sigma = \sqrt{(3 t + 5) (2 t^2 + 6 t + 3) (18 t^3 + 59 t^2 + 54 t + 15)}$ . Let us label *c<sub>f</sub>*(−) the solution with the minus and  $c_f$ (+) the solution with the plus. In our work we focus only on  $c_f(-)$  as it implies feasible values of  $c_2$ . In particular the solution  $c_f(+)$ does not satisfy the condition  $c_2 < A/2$ . In the interval within  $c_f(-)$  and  $c_f(+)$  we have that  $\gamma > 0$ , and then  $f_1(1) > f_2(1)$ , while below  $c_f(-)$  and above  $c_f(+)$  we have that  $f_2(1) > f_1(2)$ .

## **Appendix B**

We want to prove that  $f_1(2) > f_2(2)$ . We define  $\gamma = f_1(2) - f_2(2)$ , that is:

$$
\gamma = \frac{\left(23A^2 + 46A c_2 + 23 c_2{}^2\right) t^2 + \left(15A^2 + 30A c_2 + 15 c_2{}^2\right) t}{450 t^2 + 540 t + 162} +
$$
  
 
$$
-\frac{\left(18A^2 - 72A c_2 + 72 c_2{}^2\right) t^4 + \left(48A^2 - 228A c_2 + 255 c_2{}^2\right) t^3}{162 t^4 + 756 t^3 + 1206 t^2 + 756 t + 162} + (39)
$$
  
 
$$
-\frac{\left(26A^2 - 194A c_2 + 266 c_2{}^2\right) t^2 + \left(3A^2 - 48A c_2 + 84 c_2{}^2\right) t}{162 t^4 + 756 t^3 + 1206 t^2 + 756 t + 162}
$$

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We want to demonstrate that  $\gamma > 0$ ,  $\forall t$ . Knowing that  $\frac{A}{2} > c_2$ , we can substitute in the above equation  $A = 2c_2$  obtaining that:

<span id="page-27-0"></span>
$$
\frac{621 \, c_2{}^2 \, t^6 + 3378 \, c_2{}^2 \, t^5 + 6753 \, c_2{}^2 \, t^4 + 6120 \, c_2{}^2 \, t^3 + 2565 \, c_2{}^2 \, t^2 + 405 \, c_2{}^2 \, t}{1350 \, t^6 + 7920 \, t^5 + 18096 \, t^4 + 20628 \, t^3 + 12528 \, t^2 + 3888 \, t + 486} \tag{40}
$$

It is easily found that Eq. [\(40](#page-27-0)) is always strictly positive. Moreover  $\gamma(A, t, c_2) > 0$ for feasible parameter values: a sufficient condition for this condition to hold is that  $0 < t < c_2$ .

## **Appendix C**

Let  $\lambda$  be the difference between  $\pi_{\text{NO}}^M(1)$  in Eq. [\(11](#page-8-0)) and  $\pi_{\text{end}}^M(1)$  in Eq. [\(24](#page-12-1)). By assumption we have that  $\frac{A}{2} > c_2$ . If we minorate the function  $\lambda$  substituting  $\frac{A}{2}$  with  $c_2$ , we obtain the expression:

$$
\frac{432 c_2^2 t^{10} + 5137 c_2^2 t^9 + 26350 c_2^2 t^8 + 75946 c_2^2 t^7}{\Gamma}
$$
  
+ 
$$
\frac{134730 c_2^2 t^6 + 151947 c_2^2 t^5 + 108774 c_2^2 t^4 + 47709 c_2^2 t^3}{\Gamma}
$$
  
+ 
$$
\frac{11664 c_2^2 t^2 + 1215 c_2^2 t}{\Gamma}
$$

where  $\Gamma = 2(5t + 3)^2(3t^2 + 7t + 3)^2(3 + t)^2(1 + t)^2$ . This expression is strictly positive provided  $t > 0$  and  $c_2 > 0$ . It is easily found that  $\frac{\partial \lambda}{\partial A} > 0$ . Thus it always holds that  $\lambda > 0$ .

Besides, let  $\theta$  be the difference between  $\pi_{\text{NO}}^M(1)$  in Eq. [\(11](#page-8-0)) and  $\pi_{\text{end}}^M(1)$  in Eq. [\(25\)](#page-12-2). By simple calculations, we have that:

$$
\theta = \frac{t^2(5t+3)^2(3t^4+47t+20t^3+15+48t^2)[A(1+t)+c_2]^2}{\Gamma}
$$

which is clearly strictly positive. Finally, letting  $\epsilon = \pi_{\text{NO}}^M(2) - \pi^M(2)$ , where  $\pi^{M}(2) = 2f_{2}(2)$  and  $f_{2}(2)$  is as in Eq. [\(26](#page-13-1)), we obtain that

$$
\epsilon = \frac{t(t+2)(A(1+t)+c_2)}{(3+2t)^2(3t^2+7t+3)^2}[A(7t^2+15t+6)-c_2(12t^2+27t+12)]
$$

Substituting for  $A = 2c_2$ , the numerator in  $\epsilon$  boils down into  $tc_2(2t + 3) > 0$ . Since  $\epsilon$  is clearly increasing in *A*, the result follows, i.e.  $\epsilon > 0$ , provided  $t > 0$  and  $c_2 > 0$ .

## **Appendix D**

For the sake of exposition, when  $k = 1$ , we refer to the case with  $0 \leq c_2 < c_f$ , where the *E*, *L* equilibrium confguration arises, as to "Scenario A". Likewise, when  $c_2 > c_f$ , i.e. the equilibrium configuration without endogenous effort (*L*, *N*) may

occur, we refer to "Scenario B". In Scenario A, where the case *E*, *L* may arise, we have that  $\pi^M(2) = \pi^M(1)$ , with  $\pi^M(1) = \pi^M_{\text{end}}(1)$  as in Eq. ([24\)](#page-12-1), for a value of  $c_2$ , say  $c_h$ , with:

$$
c_h = \frac{162A + 1269A t + 3798A t^2 + 5381A t^3 + 3540A t^4 + 828A t^5}{\Delta} + \frac{81A\Gamma + 324A t\Gamma + 396A t^2 \Gamma + 135A t^3 \Gamma}{\Delta}
$$

where  $\Gamma = \sqrt{8t^4 + \frac{436t^3}{9} + \frac{856t^2}{9} + 68t + 16}$  and  $\Delta = 2142t^5 + 10347t^4 + 18502t^3$ +15579  $t^2$  + 6264 *t* + 972. It is easily shown that, if  $0 \le c_2 < c_h$ , then  $\pi^{M}(2) - \pi^{M}(1) > 0$  and the innovator will provide two licenses (*L*, *L* case). If  $c_2 > c_h$ then  $\pi^{M}(2) - \pi^{M}(1) < 0$  and he will provide only one license (*E*, *L* case).<sup>[24](#page-28-0)</sup>

In Scenario B, when the efficient firm buys the license  $(L, N \text{ case})$ , we have that  $\pi^{M}(2) = \pi^{M}(1)$ , with  $\pi^{M}(1) = \pi^{M}(1)$  in Eq. [\(25](#page-12-2)), for  $c_{2} = c_{g}$  with

$$
c_g = \frac{567A + 2808A t + 5175A t^2 + 4466A t^3 + 1830A t^4 + 288A t^5}{\Delta} + \frac{81A\Gamma + 243A t\Gamma + 207A t^2\Gamma + 54A t^3\Gamma}{\Delta}
$$

where  $\Gamma = \sqrt{\frac{32t^4}{3} + \frac{220t^3}{3} + \frac{1624t^2}{9} + 186t + 66}$  and  $\Delta = 576t^5 + 3768t^4 + 9490t^3$  $+11394 t^2 + 6453 t + 1377$ . Moreover,  $\pi^M(2) > \pi^M(1)$  when  $0 \le c_2 < c_g$ , and then the external innovator sells two licenses. On the other hand,  $\pi^{M}(2) < \pi^{M}(1)$  when  $c_2 > c_g$ , and he will sell only one license to the more efficient firm.

Regarding the ranking between  $c_f$ ,  $c_g$  and  $c_h$ , evaluating  $c_f(A, t)$ ,  $c_h(A, t)$  and  $c_g(A, t)$ for  $t = 0$ , and for a given value of *A*, we obtain that  $c_f(\bar{A}, 0) > c_g(\bar{A}, 0) > c_h(\bar{A}, 0)$ , with  $c_f(A, 0) = 0$ ,  $\forall A$ , and  $c_h(\bar{A}, 0) < c_g(\bar{A}, 0) < 0$ . Also  $c_h(A, 0)$  and  $c_g(A, 0)$  are decreasing in *A*. So the ranking  $c_f(A, 0) > c_g(A, 0) > c_h(A, 0)$  holds for *any* value of *A*. It is possible to show that all these functions are increasing in *t*, though at a decreasing rate. In particular, for a given *A*, it holds that  $\frac{\partial c_h(A,t)}{\partial t} > \frac{\partial c_g(A,t)}{\partial t} > \frac{\partial c_f(A,t)}{\partial t}$ , and that  $\frac{\partial^2 c_h(A,t)}{\partial t^2} < \frac{\partial^2 c_g(A,t)}{\partial t^2} < \frac{\partial^2 c_f(A,t)}{\partial t^2} < 0$ . Accordingly,  $c_f(\overline{A},t) > c_g(\overline{A},t) > c_h(\overline{A},t)$ for  $0 \le t < t^*$ , while  $c_h(\overline{A}, t) > c_g(\overline{A}, t) > c_f(\overline{A}, t)$  for  $t \ge t^*$ . This ranking is found to be robust to changes in the parameter  $A$ . Being the value of  $t^*$  quite high (around 6.5, irrespective of the value of *A*) and unrealistic in the context of developing countries, in our analysis we focussed on the former scenario. Thus, for  $t < t^*$ , combining the results in Propositions [4](#page-14-2) and [5](#page-14-3), the *E*, *L* equilibrium occurs for  $c_h < c_2 < c_f$ , while for  $c_2 > c_f$  the equilibrium is given by *L*, *N*, and finally for  $c_2 < c_h$  the equilibrium is *L*, *L*. Instead, for a high level of *t*, namely for  $t > t^*$ , the *L*, *N* equilibrium would arise for  $c_2 > c_g$ , while the equilibrium configuration would be given by *L*, *L* whenever  $c_2 < c_g$ .

<span id="page-28-0"></span><sup>&</sup>lt;sup>24</sup> In order to guarantee feasible values of  $c<sub>h</sub>$  we consider only the solution with the minus.

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