TECHNICAL PAPER

Strain rate efect on CRALL under high‑velocity impact by diferent projectiles

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Abstract

A fber–metal laminate (FML) is a hybrid laminate that is mostly used for aircraft, automobiles, and defense industry applications. The carbon fber-reinforced aluminum laminate (CRALL) is an advanced FML and has a very high specifc strength. To investigate the efects of strain rate and projectiles' nose shape on the ballistic limit of the CRALL, a series of dynamic explicit analyses were performed at high-velocity impact (HVI) by using fat, hemispheric, and sharp-nosed projectiles at three distinct strain rates $(1 \text{ s}^{-1}, 100 \text{ s}^{-1}, \text{ and } 1000 \text{ s}^{-1})$. A progressive damage model based on damage initiation and damage propagation was developed for this numerical study and implemented in the ABAQUS software. At HVI, the damage modes and failure processes of the carbon fber-reinforced polymer (CFRP) in the CRALL were investigated using Yens' criteria. The damage behavior of aluminum (Al) plates in the CRALL under HVI was determined by the Johnson–Cook (J-C) model. A cohesive surface based on bi-linear traction–separation law was utilized in between the Al plate and CFRP composite lamina to investigate the delamination in inter-laminar. The obtained results reveal that the CRALL has a high ballistic limit, either for high strain rates or for fat-nosed projectiles. The strain rate has signifcant infuence on the CRALL ballistic limit velocities for the fat-nosed projectile as compared to other projectile confgurations.

Keywords Ballistic · CRALL · FML · HVI · Projectile · Strain rate

1 Introduction

Fiber–metal laminates (FMLs) are combinations of monolithic metallic plates and composite laminates. The FMLs have abroad area of applications in various industries for technical as well as general purpose applications due to their good resistance to fatigue, impact, and fre resistance [\[1](#page-13-0)]. These industries may be the aerospace, automotive, and defense industries. In comparison to conventional plates and composite laminates, the use of FMLs reduces the weight of the structure while gaining excellent strength and corrosion resistance [[2\]](#page-13-1). The FML materials currently used are Aramid fber-reinforced aluminum laminates (ARALLs),

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 \boxtimes Shivdayal Patel shivdayal@iiitdmj.ac.in glass-laminated aluminum-reinforced epoxy (GLARE), CRALLs, etc. [\[3](#page-13-2)].

Song et al. [[4](#page-13-3)] experimentally and numerically investigated the energy absorption of CRALL through a dropweight impact test. They showed that the object hit by 9.40 J exhibited matrix and fber failures, whereas the object hit by 2.35 J exhibited no signifcant damage behavior appearing in CFRP layers but a shear fracture appearing on the Al layer. Naik et al. [\[5](#page-13-4)] observed that the glass fiber-reinforced plastic (GFRP) tensile strength increased by up to 88% at high strain rates as compared to the tensile strength at quasi-static loading. Rajkumar et al. [\[6](#page-13-5)] focused on the strain rate and lay-up confguration efects of the CRALL. They performed both tensile and fexural tests. They discovered that as the strain rate increased, the tensile strength increased but the fexural strength decreased. Naresh et al. [[7](#page-13-6)] studied the efect of strain rates from 10 s⁻¹ to 1000 s⁻¹ to determine the sensitivity of the strain rate, tensile characteristics, and strain rate parameters. They also found that the tensile strength was proportional to the strain rate. Xia et al. [\[8](#page-13-7)] also found that CRALL tensile strength increases with respect to strain rate. Wen [\[9](#page-13-8)] studied the FMLs' impact behavior, which

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was perforated and pierced by oval as well as conical-nosed impactors at high velocities. He recorded that the truncated conical-nosed projectile provided the highest ballistic limit. Kpenyigba et al. [[10](#page-13-9)] analyzed the impact behavior of an isotropic metal sheet under blunt, hemispheric, and conicalnosed projectiles of the same mass. As a result, the highest ballistic limit was observed for a hemispherical-nosed projectile, among others. Tirillo et al. [[11](#page-14-0)] evaluated CFRP's ballistic limit at HVI and observed that hybridization of CFRP with basalt improved the ballistic limits. Xu et al. [\[12\]](#page-14-1) experimentally reported that the CRALL has better penetration resistance against the HVI in comparison with the Al sheet and the CFRP laminate. Zhu et al. [\[13\]](#page-14-2) numerically validated the Xu et al. [[12](#page-14-1)] experimental results of ballistic limit and describe the damage behaviors of the CRALL under various projectile configurations impact. Many researchers [[14,](#page-14-3) [15\]](#page-14-4) implemented a continuum damage model via a VUMAT user-defned subroutine in ABAQUS to analyses composite laminate failures under impact loadings. Sierakowski [[16](#page-14-5)] and Groves et al. [[17](#page-14-6)] describe the infuence of the strain rate on the mechanical behavior of the composite material. Yen [\[18\]](#page-14-7) provided a numerical model to predict the strain rate impact on the composite material. Al-Hassaniand Kaddour [\[19](#page-14-8)]describe the strain rate effect of GFRP, CFRP and Kevlar fber-reinforced polymer dynamic failure within the range of $5 s⁻¹$ to $400 s⁻¹$. Hsiao and Daniel [[20](#page-14-9)] discovered the composite stifening follows a linear trend within the strain rate, which varies from 1 s^{-1} to 1800s−1. Ma et al. [[21](#page-14-10)] experimentally and Ma et al. [[22\]](#page-14-11) numerically represents the effect of strain rate on the ballistic limit of the GFRP composite. In these studies, they found the ballistic limit improved with an enhancement in the strain rate. To perform the numerical analysis, they used the material properties of strain rates ranging from 0.0001 to 0.01. Xiao et al. [[23](#page-14-12)] numerically discovered the strain rate effect on the mild steel impact behavior subjected single particle impact. They have used the material properties of steel from 0.001 s⁻¹ to 315 s⁻¹. They found the yield strength of the material increased with the rise in strain rate.

The experimental work on the FMLs subjected to HVI has been described in literature with various projectile shapes. The limited works on fnite element simulation available for HVI with various nose-shaped projectiles with varying strain rates. However, in this numerical study, the efects of diferent-nosed (sharp, fat, and hemisphere) projectiles at strain rates of 1 s^{-1} , 100 s⁻¹, and 1000 s⁻¹ have been analyzed on the CRALL's ballistic limit, residual velocity, damage behavior, and energy absorption under HVI. The progressive damage modeling of the CRALL materials has been developed using the damage initiation and damage evaluation model. The developed model has been implemented in the ABAQUS software to investigate the composite failures and validate the literature experimental results. An instantaneous elastic constant reduction approach has been utilized in this work to discover the material degradation during ballistic penetration, stress–strain characteristics, and type of failure.

2 Finite element modeling

2.1 Modeling of geometry

The geometry details of fat, hemispherical, and sharp-nosed projectiles of the same mass (30 g) are shown in Fig. [1.](#page-1-0) The fnite element models of the CRALL with three diferent types of projectiles are shown in Fig. [2.](#page-2-0) All these confgurations are taken from the literature [[12](#page-14-1), [13\]](#page-14-2). The CRALL has 2.4 mm thickness with 0.1 m in diameter. The CRALL and projectiles are discretized by using C3D8R and R3D4 elements, respectively. The CRALL has two 0.8 mm thick Al sheets and one 0.8 mm CFRP laminate [[12\]](#page-14-1). The CFRP laminate has 8 plies of uniform thickness and ply orientations of $[0/90/0/90]_s$. The contact surfaces of each Al plate and each CFRP lamina are connected using cohesive modeling. The general contact modeling is used for connecting the CRALL and projectiles.

The circumferential edges of the CRALL's are fixed (arrest all degree of freedom) in all directions (*x*, *y*, *z*). This was done in simulations by employing a present velocity boundary condition. The friction coefficient of 0.3 is used between the CRALL and projectiles [\[13](#page-14-2)].

Fig. 1 Dimensions (in mm) of projectiles with **a** fat nose; **b** hemisphere nose; and **c** sharp nose

Fig.2 FE model of CRALLs with **a** fat nose; **b** hemispherical nose; and **c** sharp nose projectiles

2.2 Modeling of materials

2.2.1 J‑C plasticity and damage model

The J–C model is generally applied to metals to predict the plastic damage during impact simulation problems like collisions and sudden weight drops from heights. The J–C model gives the coupled efect of strain, strain rate, and temperature [\[24\]](#page-14-13). The J-C plasticity model is expressed as:

$$
\sigma = (A + B\epsilon^n) \left[1 + \text{Cln}\left(\frac{\dot{\epsilon}}{\dot{\epsilon}_o}\right) \right] \left[1 - \left(\frac{T - T_r}{T_m - T_r}\right)^m \right] \tag{1}
$$

where; A , B , n , C , and m are material constants. T , T_m , and *T*r are working, melting, and room temperature, respectively. *ε* is working strain rate and ϵ ⁰ is reference strain rate. *ε* is equivalent plastic strain.

It not only depicts the build-up of the deformation process during failure but also the change in failure strain. The stress state, strain rate, and temperature are used to calculate the plastic failure strain ε*^f* .

$$
\varepsilon_f = \left[D_1 + D_2 \exp(D_3 \sigma^*)\right] \left[1 + D_4 \ln\left(\frac{\dot{\varepsilon}}{\dot{\varepsilon}_o}\right)\right] \left[1 + D_5\left(\frac{T - T_r}{T_m - T_r}\right)\right]
$$
\n(2)

where D_i ($i = 1, 2, \ldots, 5$) are known as failure damage parameters. The curve ftting of the calibrated relationship between failure strain and stress tri-axiality at room temperature can be used to find the values D_1 , D_2 , D_3 , and D_4 . For D_5 least square method can be used. An accumulation of damage parameter is determined by Eq. ([3\)](#page-2-1)

$$
D = \sum \frac{\Delta \epsilon_f}{\epsilon_f} \tag{3}
$$

For an integration cycle, the equivalent plastic strain increment is denoted here by $\Delta \varepsilon_f$.

The properties with all these J-C parameters of Al plate are represented in Table [1](#page-2-2).

2.2.2 Constitutive relation of CFRP

In this analysis, to fnd the modulus at a high strain rate, Karim's [\[25](#page-14-14)] rules of mixture for a unidirectional composite are used, as given by:

$$
E_{11}(t) = E_{f1}V_f + V_m[E_m + Qe^{-Mt} + Re^{-Nt}]
$$

\n
$$
E_{22}(t) = \frac{E_{f1}V_f}{E_{f2}V_m + E_{f1}V_f} + Qe^{-Mt} + Re^{-Nt}
$$

\n
$$
G_{12}(t) = \frac{G_{f12}G_m}{G_{f12}V_m + G_mV_f} + Q_{12}e^{-Mt} + R_{12}e^{-Nt}
$$

\n
$$
G_{23}(t) = \frac{G_{f23}G_m}{G_{f23}V_m + G_mV_f} + Q_{23}e^{-Mt} + R_{23}e^{-Nt}
$$

\n(4)

The details about these parameters are provided in the literature [[25](#page-14-14)]. The above relationships are used to obtain the values of all elastic moduli at constant strain rate. The values of these parameters for CFRP are shown in Table [2,](#page-3-0) where E_1 and E_2 are Maxwell elements.

2.2.3 Damage model of CFRP

Damage initiation criteria developed by Yen [[18\]](#page-14-7) have been employed by VUMAT in ABAQUS to predict the types of failure modes for unidirectional composites. These criteria are an extension of Hashins' composite failure model. Failure criteria are given for fber and matrix damages by Yen [[18\]](#page-14-7) are represented in Eqs. $(5)-(9)$ $(5)-(9)$ $(5)-(9)$ $(5)-(9)$ $(5)-(9)$:

Fiber damage:

Uniaxial tension and transverse shear;

Table 2 CFRP engineering Properties *ρ* (kg/m³)

	Properties ρ (kg/m ³) E_1 (GPa) E_2 (GPa)				$E_{\rm m}$ (GPa) $G_{\rm m}$ (GPa) v_{23}		$v_{12} = v_{13}$
Value	1570	0.971	0.104	2.31	0.857	0.38	0.25
			Properties E_{f1} (GPa) E_{f2} (GPa) $G_{f12} = G_{f13}$ (GPa) G_{f23} (GPa) θ_{e1} (ms)				θ_{g1} (ms) $\theta_{e2} = \theta_{g2}$ (ms)
Value	230	LD.	2.35	24	0.041	0.077	121,000

$$
f_1 - r_1^2 = \left(\frac{E_{11}\langle \varepsilon_{11}\rangle}{S_{XT}}\right)^2 + \frac{G_{12}^2 \varepsilon_{12}^2 + G_{13}^2 \varepsilon_{13}^2}{S_{FS}^2}
$$

- $r_1^2 = \begin{cases} < 1 & \text{no failure} \\ \ge 1 & \text{failure} \end{cases}$ (5)

Uniaxial compression;

$$
f_2 - r_2^2 = \left(\frac{E_{22}\langle \epsilon'_{11}\rangle}{S_{XC}}\right)^2 - r_2^2 = \begin{cases} < 1 & \text{no failure} \\ \ge 1 & \text{failure} \end{cases}
$$
 (6)

Transverse compression;

$$
f_3 - r_3^2 = \left(\frac{E_{22}\langle -\epsilon_{22}\rangle}{S_{FC}}\right)^2 + \left(\frac{E_{33}\langle -\epsilon_{33}\rangle}{S_{FC}}\right)^2
$$

$$
-r_3^2 = \begin{cases} < 1 \text{ no failure} \\ \ge 1 \text{ failure} \end{cases}
$$
 (7)

Matrix damage: Perpendicular direction;

$$
f_4 - r_4^2 = \left\{ \left(\frac{E_{22} \langle \varepsilon_{22} \rangle}{S_{\text{Yut}}} \right)^2 + \left[\frac{G_{23} \varepsilon_{23}}{S_{\text{YZ0}} + S_{\text{YSR}}} \right]^2 + \left[\frac{G_{12} \varepsilon_{12}}{S_{\text{XY0}} + S_{\text{YSR}}} \right]^2 \right\}
$$

$$
- r_4^2 = \left\{ \begin{array}{ll} < 1 & \text{no failure} \\ \geq 1 & \text{failure} \end{array} \right\} \tag{8}
$$

Parallel direction (delamination);

$$
f_5 - r_5^2 = \left\{ \left(\frac{E_{33} \langle \varepsilon_{33} \rangle}{S_{2ut}} \right)^2 + \left[\frac{G_{23} \varepsilon_{23}}{S_{YZ0} + S_{YSR}} \right]^2 + \left[\frac{G_{13} \varepsilon_{13}}{S_{XZ0} + S_{ZSR}} \right]^2 \right\}
$$

- $r_5^2 = \left\{ \begin{array}{c} < 1 \text{ no failure} \\ \ge 1 \text{ failure} \end{array} \right\}$ (9)

Here;

$$
\epsilon_{11}^{'} = \max\left\{-\epsilon_{11} - \langle \epsilon_{22} \rangle \frac{E_{22}}{E_{11}}, -\epsilon_{11} - \langle \epsilon_{33} \rangle \frac{E_{33}}{E_{11}}\right\}
$$

Here; $\epsilon_{11}, \epsilon_{22}, \epsilon_{33}, \epsilon_{12}, \epsilon_{23}$, and ϵ_{13} are ply-level engineering strains. E_{11} , E_{22} , E_{33} , G_{12} , G_{23} , and G_{13} are associated elastic moduli. Macaulay brackets represented here by⟨⟩.Tensile strength, compressive strength, fber layer shear strength, and crush failure strength are represented by S_{XT} , S_{XC} , S_{FS} , and *S*_{FC}, respectively. For the initial damage-free material, damage thresholds r_i ($i = 1,2,3,...$) are set to 1.

For damage evolution, to quantify six damage variables $\overline{\omega}$. with $i=1, 2, \ldots$ 6 are assumed and corresponding compliance matrix has been developed as:

$$
\begin{bmatrix} S \end{bmatrix} = \begin{bmatrix} \frac{1}{(1-\overline{\omega}_1)E_{11}} & \frac{-\upsilon_{21}}{E_{22}} & \frac{-\upsilon_{31}}{E_{33}} & 0 & 0 & 0\\ \frac{-\upsilon_{12}}{E_{11}} & \frac{1}{(1-\overline{\omega}_2)E_{22}} & \frac{-\upsilon_{32}}{E_{33}} & 0 & 0 & 0\\ \frac{-\upsilon_{13}}{E_{11}} & \frac{-\upsilon_{23}}{E_{22}} & \frac{1}{(1-\overline{\omega}_3)E_{33}} & 0 & 0 & 0\\ 0 & 0 & 0 & \frac{1}{(1-\overline{\omega}_4)G_{12}} & 0 & 0\\ 0 & 0 & 0 & 0 & \frac{1}{(1-\overline{\omega}_5)G_{23}} & 0\\ 0 & 0 & 0 & 0 & 0 & \frac{1}{(1-\overline{\omega}_6)G_{13}} \end{bmatrix}
$$
(10)

Stifness matrix is the inverse of compliance matrix and is obtained by inverting them

$$
[C] = [S]^{-1}
$$
 (11)

The growth rate is defned by damage evolution law as given below

$$
\overline{\omega}_i = \sum_j \dot{\psi}_j q_{ji} \tag{12}
$$

where; ψ_j ($i = 1, 2 ...$) is the scalar function, '*j*' is growth rate, and q_{ij} couples both the damage variable and scalar function.

2.2.4 Formulations for strain rate dependence

The significant effects of strain rate on the composite laminate properties during the HVI are observed. When this infuence is considered, the strength and stifness of unidirectional composites alter. The unidirectional CFRP composite strengths are modifed with respect to changes in strain rate as per the following equation [\[18](#page-14-7)]:

$$
\{S_{RT}\} = \{S_0\} \left(1 + \text{cln}\frac{\{\epsilon\}}{\dot{\epsilon}_0}\right) \tag{13}
$$

Properties of CRALLs		$1\ \mathrm{s}^{-1}$	$100 s^{-1}$	$1000 s^{-1}$
Stiffness (GPa)	E_{11}	139.32	203.407	235.450
	E_{22}	3.1	4.526	5.239
	E_{33}	3.1	4.526	5.239
	G_{12}	0.95	1.387	1.605
	G_{13}	0.95	1.387	1.605
	G_{23}	1.3	1.898	2.197
Strength (MPa)	$X_{\rm T}$	2050	2994	3464
	$X_{\rm C}$	1050	1534	1774
	$Y_{\rm T}$	71	104	120
	$Y_{\rm C}$	132	193	223
	$S_{\rm L}$	75	110	126
	S_{T}	34	54	57
Fracture energy (N/m)	G_{1T}	48,400	19,910.43	23,038
	G_{1C}	60,300	10,198.04	11,800
	G_{2T}	4500	68,953.85	79,793
	$G_{\rm 2C}$	8500	128,198.7	148,348

Table 3 Properties of unidirectional CFRP at diferent strain rates

Here;
$$
\{S_{RT}\} = \begin{cases} X_T \\ Y_C \\ Y_T \\ Y_C \\ S_L \\ S_T \end{cases}
$$
 and $\{S_O\} = \begin{cases} X_T \\ Y_C \\ Y_C \\ Y_C \\ S_L \\ S_T \end{cases}$ where

 $c = 0.1$ is the strain rate constant, $\{S_0\}$ and $\{S_{RT}\}$ are the strengths at reference strain rate $(\dot{\epsilon}_0)$ and current strain rate $(\dot{\varepsilon})$, respectively.

The strain rate impacts on elastic moduli are extracted in the same way as:

$$
\{E_{RT}\} = \{E_0\} \left(1 + \text{cln}\frac{\{\epsilon\}}{\epsilon_0}\right)
$$
\n
$$
\text{Here: } \{E_{RT}\} = \begin{cases} E_{11} \\ E_{22} \\ E_{33} \\ G_{12} \\ G_{13} \\ G_{23} \end{cases} \text{ and } \{E_O\} = \begin{cases} E_{11} \\ E_{22} \\ E_{33} \\ G_{12} \\ G_{13} \\ G_{23} \end{cases}
$$
\n
$$
(14)
$$

Here, ${E_0}$ and ${E_{RT}}$ are the elastic moduli at reference strain rate $(\dot{\epsilon}_0)$ and current strain rate $(\dot{\epsilon})$, respectively. During HVI, the composite laminates show a noticeable strain rate effect. Considering the 1 s⁻¹,100 s⁻¹, and 1000 s⁻¹ strain rates' effect on the CFRP strengths, the rate-dependent parameters of strength are calculated by using Eqs. [13](#page-3-3) and [14](#page-4-0). By increasing the strain rate, increases in the strength and stifness properties of composite (CFRP) were obtained. All calculated properties are given in tabular form in Table [3](#page-4-1)

Fig.3 Residual velocity versus initial velocity curves for various projectiles

and used to fnd residual velocity, ballistic velocity, stresses, and energy absorption. The fracture energies at diferent strain rates are also listed in Table [3.](#page-4-1)

2.2.5 Damage mode of interface

For interfaces, delamination is the crucial failure mechanism of FMLs when they are subjected to HVI. An energy-based Benzeggagh–Kenane (B–K) power law was employed [[26\]](#page-14-15) to analyses the delamination behavior.

The interface is very thin, with only two shear tractions and normal traction acting. The delamination is unavoidable under mixed-mode conditions. Nominal stress criterion for mixed-mode conditions is given by:

$$
\left(\frac{\sigma_n}{N}\right)^2 + \left(\frac{\sigma_s}{S}\right)^2 + \left(\frac{\sigma_t}{T}\right)^2 = 1\tag{15}
$$

Here, *S*, *T*, and *N* are defned as maximum stress values for the corresponding two shear and one normal direction, respectively, while σ_n , σ_s , and σ_t denote the traction stress in those directions. The cohesive properties are taken from literature [[26,](#page-14-15) [27\]](#page-14-16).

2.3 Validation of numerical model

The Yens' criteria and J-C damage modeled are employed for CFRP composite laminate and metallic Al plates, respectively, to validate the present numerical results with literature [[12](#page-14-1)] experimental results for ballistic limit of CRALL under the velocity range from 60 to 150 m/s. A ballistic velocity is the highest impactor's starting velocity at which it fails to perforate the target plate. The ballistic velocities as predicted by the present numerical models of

Table 4 Experimental [\[12\]](#page-14-1) and present numerical results comparisons for ballistic limit of CRALLs

Model	Experiment [12] (m/s) (p)	Prediction $[13]$ (m/s) $\left(q\right)$	Present simulation (m/s)(r)	$%$ Error between (p) and (r)
CRALL/F	85.2	108.7	90.02	5.8
CRALL/H	80.9	84.4	83.2	2.8
CRALL/S	70.5	67.8	68	3.5

CRALL for three distinct projectile combinations named CRALL/Flat (CRALL/F), CRALL/Hemispherical (CRALL/H), and CRALL/Sharp (CRALL/S) are shown in Fig. [3](#page-4-2). The CRALL/S and CRALL/F versions have somewhat more nonlinear behavior than the CRALL/H. Table [4](#page-5-0) shows the CRALLS' ballistic limit comparisons of the current study with both the experimental and numerical results of Xu et al. [[12\]](#page-14-1) and Zhu et al. [\[13\]](#page-14-2), respectively, at $1 s⁻¹$ strain rate for distinct nose projectile impacts. Small percentage errors are seen between the obtained results and the literature $[12]$ experimental results. By applying fine meshing only in the impact zone (as shown in Fig. [2\)](#page-2-0), we were able to save computational time while maintaining the accuracy of the results. After validation at a strain rate of $1 s^{-1}$, FE modeled CRALL with various nose-shaped projectiles are utilized to explore the ballistic limit in greater depth throughout the ballistic penetration process at higher strain rates.

The numerically obtained failure behavior of the various CRALL configurations at the reference strain rate (1 s^{-1}) is compared with the experimentally [[12\]](#page-14-1) deformed CRALL configurations. The modes of failure of the top Al plate, followed by the top CFRP laminate and the bottom Al plate, are compared for the present numerical and literature experimental [[12\]](#page-14-1) case. These comparisons are illustrated in Fig. [4.](#page-6-0) This figure clearly shows the numerically fractured Al plates and CFRP laminate patterns are matched with the experimental fracture modes for all configurations. For the case of CRALL/F at velocity of V_{110} , the top and bottom Al plates are subjected to shear damage and both tensile and shear damage, respectively. Similarly, for the CRALL/H configuration at velocity of V_{107} , only a ductile fracture hole is seen in the top Al plate. CFRP and the bottom Al plate are subjected to two orthogonal cracks and two orthogonal fractured holes, respectively. The CRALL/S fracture behaviors are the same as the CRALL/H configuration, but due to the smaller contact area of the sharp-nosed projectile as compared to the hemisphere-nosed projectile, a small hole is created on the top al plate.

3 Results and discussion

Dynamic explicit analysis on the CRALL is performed using the diferent projectile's nose shapes with strain rate efect consideration. The ballistic limits and residual velocities of the CRALL are determined using progressive damage modeling. The Yen criteria and J–C model are used for damage behavior prediction of CFRP and Al respectively. The obtained results for the ballistic limit, residual velocity, damage failure behavior, and energy absorption are discussed in the below sections.

3.1 Efect of strain rate on the ballistic limit of CRALL

The projectile's nose shape at various strain rates infuences the ballistic limit as well as the residual velocity of the CRALL. To evaluate the ballistic velocity of the CRALL/F configuration, ten successive hits for each strain rate (1 s⁻¹, 100 s⁻¹, and 1000 s⁻¹) were applied to the CRALL by a fat-nosed projectile. The projectile starting velocities ranging from 80 to 180 m/s were used to perform this study. Figure [5](#page-7-0)a illustrates a fat-nosed projectile's residual velocities (terminal velocity) variation with respect to fat-nosed projectile starting velocity at 1 s⁻¹, 100 s⁻¹, and 1000 s⁻¹ strain rates. The starting velocity varies from 80 m/s to 180 m/s, with the highest ballistic limit of 122 m/s obtained at 1000 s−1 strain rate. The ballistic limits of the CRALL/F confguration at $1 s^{-1}$ and $100 s^{-1}$ are obtained at 90.02 m/s and 120 m/s, respectively. At a projectile starting velocity of 130 m/s (V_{130}) , the residual velocities are 45 m/s, 34.02 m/s, and 30.52 m/s for 1 s⁻¹, 100 s⁻¹, and 1000 s⁻¹ strain rates, respectively. The residual velocities at V_{150} are 90.26 m/s, 85.43 m/s, and 82.97 m/s for 1 s⁻¹, 100 s⁻¹, and 1000 s⁻¹, respectively. As a result, at 1000 s^{-1} strain rate, the residual velocity is the smallest, followed by $100s^{-1}$ and 1 s−1strain rates. This increase in ballistic limit and decrease in residual velocity with an increase in strain rate is due to the enhancement in the stifness of both Al plates and CFRP laminate [\[16,](#page-14-5) [17](#page-14-6), [28](#page-14-17), [29](#page-14-18)]. In the case of a higher strain rate, the CRALL strength increases due to the restriction of dislocation movements. However, the CRALL/F confguration gives the highest ballistic limit and the smallest residual velocity for $1000 s⁻¹$ strain rate.

Similarly, a series of nine successive impacts applied by a hemisphere-nosed projectile of diverse strain rates $(1 s⁻¹,100 s⁻¹,$ and 1000 s⁻¹) on the CRALL at various starting velocities. The starting velocities of hemispherenosed projectile ranging from 60 to 150 m/s to determine the ballistic limit and residual velocities behavior of the

Fig. 4 Modes of CRALLs fracture under HVI by various projectiles

Fig.5 Residual-initial velocity curves for diferent projectiles at diferent strain rates

CRALL/H confguration as illustrated in Fig. [2](#page-2-0)b. Figure [5](#page-7-0)b represents the variation of residual velocity with respect to hemisphere-nosed projectile starting velocity at various strain rates. At 1 s^{-1} , 100 s^{-1} , and 1000 s^{-1} strain rates, the ballistic limits of the CRALL/H configuration are obtained as 83.2 m/s, 105 m/s, and 107 m/s, respectively. The strain rate infuences the residual velocities of the projectile. The projectile residual velocity is also a function of the starting projectile velocity. From Fig. [5](#page-7-0)b, it is observed that for $1 s^{-1}$, 100 s⁻¹, and 1000 s⁻¹ strain rates, the hemispherenosed projectile residual velocities at V_{130} are 58.66 m/s, 42.93 m/s, and 39.25 m/s, respectively. Similarly, at V_{150} these are recorded as 94.15 m/s, 84.73 m/s, and 83.81 m/s, respectively, for 1 s^{-1} , 100 s^{-1} , and 1000 s^{-1} strain rates. This could be because the CRALL stifens at high strain rates as the yield strengths of both Al and CFRP increase. The stifer CRALL restricts the projectile's ability to pass through it under high strain rate conditions. However, the residual velocity varies in inverse proportion to the strain rate [[22](#page-14-11)].

To determine the ballistic velocity of the CRALL/S confguration depicted in Fig. [2c](#page-2-0), eight successive impacts on the CRALL were applied for each strain rate by a sharpnosed projectile. The sharp-nosed projectile's starting velocity varies between 60 and 150 m/s to identify the ballistic limit of the CRALL/S confguration. Figure [5](#page-7-0)c represents the relation between residual and starting velocities of the CRALL/S at diferent strain rates. The ballistic limits recorded at 1 s^{-1} , 100 s^{-1} , and 1000 s^{-1} strain rates for the CRALL/S confguration are 68 m/s, 103 m/s, and 104 m/s, respectively. The ballistic limit obtained at 1 s^{-1} is the smallest, followed by $100s^{-1}$ and $1000 s^{-1}$. At V₁₃₀, the residual velocities of 59.14 m/s, 45.91 m/s, and 41.58 m/s are recorded for 1 s⁻¹, 100 s⁻¹, and 1000 s⁻¹ strain rates, respectively. For a starting velocity of 150 m/s, the highest residual velocity of 97.04 m/s obtained at 1 s^{-1} strain

Fig. 6 CRALL ballistic limit at diferent strain rates

rate, followed by 87.13 m/s at 100 s⁻¹, and 85.24 m/s at 1000 s^{-1} , as seen in Fig. [5](#page-7-0)c. Fig. [5](#page-7-0) clearly indicates that the residual velocity of a projectile is a function of both the starting velocity of the projectile and the strain rate. Strain rate has a signifcant infuence on residual velocity and ballistic limit, as revealed in Fig. [5](#page-7-0). A sharp-nosed projectile has the highest residual velocity for a fxed projectile starting velocity due to its small initial contact area with the CRALL at all strain rates, followed by hemisphere and fat-nosed projectiles. The higher contact area of the projectile with the CRALL increases the friction between them. However, the fat-nosed projectile's residual velocity is the smallest among the other projectile confgurations [[13\]](#page-14-2). The increase in the strain rate strengthens the CRALL, which causes the perforation capacity of the projectile to reduce. Therefore, at high strain rate, residual velocity is minimum for all projectile shape [\[19](#page-14-8), [30](#page-14-19)].

The comparisons of the ballistic limit velocity are demonstrated in Fig. [6](#page-7-1) for three separate projectiles at three different strain rates. The results plotted in Fig. [6](#page-7-1) show that the ballistic velocity of the CRALL increases for all three projectile models with raising in strain rate. Sharp and fat

Fig. 7 Stress–strain curves for CRALL at diferent strain rates and projectiles

projectiles demonstrated that the CRALLs ballistic velocities are lowest and maximum, respectively. This could be due to the nose contact area of the fat projectile is higher followed by hemisphere and sharp-nosed projectile. The larger contact area of the projectile has less perforation capacity in comparison with the smaller contact area of the nosed projectile. However, the CRALL/H confguration shows an intermediate nature as compared to the CRALL/F and CRALL/S confgurations. The CRALL ballistic limit velocity for hemisphere projectile changes relatively little (28.6%) with regard to the varied strain rates $(1 \text{ to } 1000 \text{ s}^{-1})$ followed by flat (35.52%) and sharp (52.94%) and identifed the low residual velocity at high strain rate. Due to an increase in the strength of both the Al and CFRP of the CRALL for increased strain rate, the ballistic limit of the CRALL improved for all projectile confgurations. This mechanism of strengthening the CRALL with a high strain rate is discussed in Sect. [3.2](#page-12-0).

3.2 Strain rates efects on stress–strain characteristics

Stress–strain behavior of both the Al plate and the CFRP laminate is infuenced by the rate of strain applied. The efect of strain rate on the stress–strain characteristics of various CRALL confgurations is illustrated in Fig. [7](#page-8-0). At low strain rates, ductile material (Al plates) has time to stretch before breaking. The maximum load is therefore limited. However, a material has less time to deform at a high strain rate, which results in a larger measured load. Dislocation glide or twinning is the two types of atomic mobility that determine the yield phenomenon for ductile materials. The dislocation glide is disrupted by a high strain rate, which prevents twinning. This method has a higher yield point since it takes more energy to shift atoms. As the strain rate rises, the overall elongation decreases during the projectile's impact [[23,](#page-14-12) [29](#page-14-18)[–32](#page-14-20)]. Similarly, in the case of CFRP composite laminate, the material stifens as the strain rate rises (with a decrease in matrix ductility). This stifening behavior has a substantial impact on the ballistic limit. There are diferent proposed explanations for this phenomenon. The viscoelastic properties of the polymeric matrix itself make up the frst, while the time-dependent nature of accumulated damage makes up the second [[20](#page-14-9)]. When damage happens more gradually and at slower rates, a clearly defned nonlinear zone appears close to the stress–strain curve's terminus. This behavior can be clearly seen in Fig. [7](#page-8-0) for all CRALL confgurations. Since the loading period is brief enough for material failure to occur before the commencement of fber initiation failure, the Young's modulus of elasticity rises with strain rate [[33\]](#page-14-21). This implies that when the strain rate rises, the failure modes shift. Materials that are lightly cross-linked will experience signifcant elastic deformation before breaking, whereas uncross-linked polymers will exhibit viscoelastic behavior. The behavior before breaking will depend on the crosslink and entanglement densities [\[18](#page-14-7), [19](#page-14-8)]. However, for high strain rates, the CRALL has high yield strength for all impact cases with various nose-shaped projectiles. During the impact on the CRALL, plug formed on the CRALL and is more at the high strain at the same time instant. Figure [7a](#page-8-0) depicts the stress–strain relation at various strain rates for the CRALL/F confguration. From Fig. [7a](#page-8-0), it is noted that the rate of strain is increased from 1 to 100 s^{-1} , the modulus of elasticity rises by 45.99%, resulting in a 12.40% increase in yield strength, and the maximum strength rises by 41.58%. Similarly, as the strain rate is raised from 100 to 1000 s^{-1} , the modulus of elasticity increases by 15.75%, resulting in enhanced yield strength and maximum strength of 9.97% and 40.25%, respectively.

The stress–strain curves for the CRALL/H are shown in Fig. [7b](#page-8-0). For the CRALL/H, the modulus of elasticity increases by 45.99% when the strain rate is raised from 1 to 100 s −1, resulting in a 67.75% increase in yield strength and a 46.48% increase in maximum strength. The modulus of elasticity rises by 15.75% as the strain rate is increased from 100 to 1000 s−1, resulting in increased yield strength and maximum strength of 13.88% and 7.58%, respectively. From Fig. [7c](#page-8-0), it revealed that for the CRALL/S, when the rate of

Fig. 8 Damages at 100 s^{-1} and 1000 s^{-1} strain rates in CRALLs

Fig. 9 Damaged area of CRALL at high strain rates

strain is increased from 1 to 100 s^{-1} , the modulus of elasticity rises by 45.99%, resulting in a 0.51% increase in yield strength and a 26.46% increase in maximum strength. When the rate of strain is raised from 100 to $1000 \, \text{s}^{-1}$, the modulus of elasticity increases by 15.75%, resulting in enhanced yield strength and maximum strength of 36.60% and 14.75%, respectively. These improvements in the CRALLs' strength are due to a rise in the strain rate [\[22](#page-14-11), [25](#page-14-14), [29\]](#page-14-18).

3.3 CRALL failure analysis

The tensile, shear, and delamination failures operated on the all CRALL models in both $100 s⁻¹$ and $1000 s⁻¹$ strain rates shown in Fig. [8.](#page-9-0) The delamination criterion worked appropriately in both strain rate models without reducing the strain rate impact. For the CRALL/F model, increased strain rates have a little infuence on fber and matrix tensile failures in CFRP. The enhanced strain rate $(100-1000 \text{ s}^{-1})$ increases the shear effect. For a high strain rate, the delamination in CFRP laminate of the CRALL is greater than the low strain rate delamination. The laminate shows the tensile cracks caused by fat-nosed projectile impacts at high strain rates. Fiber tensile, matrix tensile, and shear failure

occurred in the CRALL/H model at both strain rates, as shown in Fig. [8b](#page-9-0). Increased strain rate had little infuence on fber and matrix tensile in the CFRP composite laminate. However, the enhanced strain rate increased the shear effect on the CRALL's CFRP laminate. A diamond-shaped bulge formed due to impact by a hemisphere-nosed projectile. This bulge size is higher for $1000 s⁻¹$ strain rate as compared to 100 s −1. Figure [8](#page-9-0)c depicts the tensile fber and matrix failure as well as shear and delamination in the CFRP laminate during impact by a sharp-nosed projectile. The CRALL/S confguration also shows a similar type of failure as seen for the CRALL/H confguration. In the CRALL/S confguration, the damage area is smaller than the damage area of the CRALL/H confguration. This could be due to the smaller contact area of a sharp-nosed projectile. For all CRALL confgurations, the damage in the CFRP is a little bit higher for high strain rates. This could be due to the fact that the crack formed during the projectile's impact propagates faster for the high strain rate. Figure [8](#page-9-0) represents the shear damage is the major failure of the CFRP laminate followed by the matrix tensile failure and fber tensile failure, respectively, in the entire CRALL confguration.

Fig. 10 Ballistic penetration process of CRALL

Fig. 11 Energy absorption for various confgurations

3.4 Analysis of ballistic penetration process

Figure [10](#page-11-0) shows the various nosed projectiles' ballistic penetration process (at $100 s^{-1}$ and $1000 s^{-1}$ strain rate) in the CRALL at diferent times. As shown in Fig. [10](#page-11-0)a for flat-nosed projectile, penetration is the largest at $t = 100 \,\mu s$ because its impacted face contacts area is very large as compared to sharp and hemisphere nose.

The plasticity of the composite plate is lower as compared to aluminum sheets. As we increase strain rate, deformation will be increased at the same time instant. Therefore, at $t = 250$ μs it can be easily see, a plug column is started. This plug formation is a plugging part of CRALL but is more at the high strain at the same time instant. Due to high shearing in the case of a fat-nosed projectile, no plug ejection is seen in Fig. [9.](#page-10-0) In the composite layers, tensile shear failure and delamination occur between the Al layer and composite layer. Shear failure dominated due to the edge of the flat nose. At $t = 400 \text{ }\mu\text{s}$ afterward, since the projectile no longer deformed the CRALL plate, and perforated area no longer increased after increasing the time $(>400 \,\mu s)$. The depth of penetration of a projectile increases as we increase the strain rate $100 s^{-1}$ to $1000 s^{-1}$ at the respective instant due to which the plug column will also be increased.

In Fig. [10b](#page-11-0), at 100 μs, the impacted shape is formed like a spherical concave on the top layer of Al, and a convex surface appears on the backside of the Al layer due to the hemisphere nose of the projectile. At $t = 250 \text{ }\mu\text{s}$, the middle part of the target plate appears at the backside of the target due to the shear failure of the Al sheet, and a small plug column form. The deformation of the CRALL increases as the contact area of the projectile increases during continuous ballistic penetration. Fiber tensile failure and shear failure happen in the CFRP composite layers. The delamination criterion occurs between the Al layer and the composite layer. In Fig. [9](#page-10-0), the plug ejection failure mode is observed at the CRALL due to circumferential necking of shear. More shear deformation happens at a high strain rate. The perforated area remains constant after increasing the time *t*>400 μs. The projectile's depth of penetration increases as the strain rate increases from 100 to 1000 s⁻¹ at a time.

Similarly, Fig. [10c](#page-11-0) shows that at $t = 100 \mu s$, fiber tensile and matrix tensile failures are dominated by shear failure in the composite layer and tension failure occurs in the Al layers, resulting in a limited afected area and a considerable stress. At $t = 250 \,\mu s$ and 400 μs , a sharp nose tip develops, indicating that the composite and both layers of Al have failed. As we increased the strain rate from 100 to 1000 s−1, the rapid penetration process occurred at the same time. As seen in Fig. [9](#page-10-0), the sharp-nosed projectile petalling failure mode is detected owing to redial tension in Al layers. However, petalling happens quickly when the rate of strain is increased. The depth of penetration of the bullet grows as the strain rate rises from 100 to 1000 s⁻¹ at the corresponding instant, resulting in no plug column formation.

3.5 Energy absorption for the CRALL material

Energy absorption (internal energy) study of the CRALL/F, CRALL/H, and CRALL/S confgurations is performed using the three diferent strain rates of 1, 100 and 1000 s^{-1} at a constant impactor velocity of 150 m/s, as shown in Fig. [11](#page-12-1). It is observed that all the three cases (CRALL/F, CRALL/H, and CRALL/S) energy absorption are increasing with increases the strain rate from 1 to 1000 s^{-1} . The flat-nosed projectile has the highest energy absorption at $1000 s^{-1}$ strain rate when compared to other projectiles such as CRALL/H and CRALL/S at the same strain rate. It is due to the geometry of the projectile and higher strain rate efect. The CRALL/H material represents that the maximum and minimum energy absorptions

are 11.8 J and 7.2 J for 1000 s⁻¹ and 1 s⁻¹, respectively, at 0.4 ms. Similarly, the fat-nosed projectile impacted with CRALL material is also investigated, and the maximum and minimum energy absorptions are 60 J and 14 J for 1000 s⁻¹and 1 s⁻¹, respectively, at 0.8 ms. The sharp projectile impacted with CRALL material shows that the maximum and minimum energy absorptions are 10 J and 7 J for 1000 s⁻¹and 1 s⁻¹ strain rates at 0.4 ms, respectively. Hence, it is concluded from these energy graphs that the energy absorption of the CRALL is proportional to the strain rate. This is the highest for the fat-nosed projectile, followed by the hemisphere and sharp projectiles.

4 Conclusion

The different projectile shapes and strain rate effects are numerically investigated for the CRALL under the HVI. From this numerical study, the major fndings are as follows:

- The ballistic limit of the CRALL for all projectile impacts increases as the strain rate goes from 1 to 1000 s^{-1} . The residual velocity shows an inverse efect. This is due to the CRALL stifening as a result of strain rates.
- For the fat-nosed projectile impact case, the CRALLs ballistic limit velocities are the highest at all strain rates, followed by hemisphere and sharp-nosed projectiles. This is because the fat-nosed projectile has the greatest initial contact area with the CRALL, followed by the hemisphere- and sharp-nosed projectiles.
- Raising the strain rate causes the yield strength and maximum strength to grow exponentially due to an increase in the Young modulus of elasticity.
- For the fat, hemisphere, and sharp-nosed projectiles, the CRALL failure patterns are shear, orthogonal cracks with a large hole, and orthogonal cracks with a small hole, respectively. This occurs as a result of their various interactions with the CRALL.
- At a $1s^{-1}$ strain rate, the yield strength of the CRALL is high for sharp-nosed projectiles and low for fat-nosed projectiles. At a high strain rate of 1000 s^{-1} , the yield strength of the target is high for hemisphere-nosed projectiles and low for fat-nosed projectiles. The maximum strength of the CRALL is the highest for fat-nosed projectiles at all strain rates.
- The flat-nosed projectile requires high velocity to perforate the target at both low and high strain rates and also showed the maximum energy absorption in comparison to other projectiles such as the CRALL/H and CRALL/S confgurations.
- When the strain rate of the ballistic penetration process rises, the depth of penetration of the projectile increases. Increased strain rate had no signifcant infuence on fber

tensile, matrix tensile, and delamination failures for the CRALL.

- The damage area is the largest for the CRALL/F configuration, followed by the CRALL/H and CRALL/S confguration.
- High tensile failure occurs at high strain rate for the CRALL/S, causing petalling in the CRALL for using the sharp projectiles.

Declarations

Conflict of interest The authors declare that they have no conficts of interest.

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