**TECHNICAL PAPER**



# **Infuence of blade profle on energy loss of sewage self‑priming pump**

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Received: 20 July 2018 / Accepted: 21 September 2019 / Published online: 3 October 2019 © The Brazilian Society of Mechanical Sciences and Engineering 2019

#### **Abstract**

Sewage self-priming pumps are widely used in municipal sewage treatment and agricultural irrigation. The impeller is the key component to determine the hydraulic performance of sewage self-priming pump. In this study, the ZW100-100-15 sewage self-priming pump was selected as a research object. Five double-channel impellers with diferent blade profles were designed based on the same meridional shape. The ANSYS CFX 16.2 and shear stress transport *k*–*ω* turbulence model were conducted to investigate the sewage pump models with fve diferent impellers numerically. The entropy production theory was applied to analyze the internal energy losses of diferent sewage pump models. The mechanism of infuence of blade profles on the energy losses was investigated systematically. The results indicated that under diferent fow rate conditions, the hydraulic efficiency of S5 scheme with a concave blade angle distribution profile is higher than that of other schemes. At the design fow rate, the head of S5 was the highest, the fow state inside the impeller was the most stable and the energy loss inside the impeller was the least. In non-design conditions, the fow distribution and entropy production rate distribution of S5 were signifcantly better than those of other schemes. Results illustrated that fow separation, backfow, shock efect, vortex and rotor–stator interaction were the main inducers for the formation of entropy production. This research indicated that the entropy production theory can predict the irreversible energy loss in pump accurately and the blade profle optimization can efectively improve the sewage self-priming pump hydraulic performance and weaken the unstable fow and its internal energy loss.

**Keywords** Blade profle · Sewage self-priming pump · Entropy production · Energy loss

## **1 Introduction**

With the development of "five water treatment" in China [\[1](#page-12-0)], as a general centrifugal pump, the sewage self-priming pump has been widely used in municipal wastewater treatment. At present, the sewage self-priming pumps are generally characterized by low efficiency and high energy consumption

Technical Editor: Jader Barbosa Jr., PhD.

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[[2\]](#page-12-1). Therefore, it is great practical signifcance to improve the performance of sewage self-priming pump to reduce its energy consumption and realize the energy saving and emission reduction. As a core component of a centrifugal pump, the impeller blade profile is one of the important factors afecting the performance of a centrifugal pump, because it can change the hydraulic load on blades and afects the conversion efficiency of pressure energy in the impeller. It is known that there are many factors infuencing blade profle, including blade trailing edge thickness and outlet placement angle  $[3-7]$  $[3-7]$  and blade wrap angle  $[8, 9]$  $[8, 9]$  $[8, 9]$  $[8, 9]$ . Also the Bezier's curve method was utilized to design the blade profles [\[10](#page-12-6)], or a three-dimensional blade inverse method based on freeform surface deformation method was proposed to optimize the impeller blade [\[11\]](#page-12-7). Recently, computational fuid dynamics (CFD) has been applied to analyze the fow felds in pump, the distribution of static pressure, fuid velocity and turbulent kinetic energy of the internal fow feld of the pump which were obtained by numerical simulation [\[12–](#page-12-8)[14\]](#page-12-9). As we know, it has some limitations for the traditional method for evaluating



<span id="page-1-0"></span>**Fig. 1** Blade placement angle distribution of fve impeller schemes. **a** S1 blade, **b** S2 blade, **c** S3 blade, **d** S4 blade, **e** S5 blade

<span id="page-1-1"></span>



the hydraulic loss in pump based on the pressure drop. Therefore, some researchers adopted the entropy production theory to quantitatively evaluate the energy loss features inside pump and provide accurate and intuitive information for subsequent improvement and optimization for pump [[15](#page-12-10)[–18\]](#page-12-11). In addition, entropy production theory was also widely used in heat transfer, microscopic particle motion and other felds [\[19](#page-12-12)[–22\]](#page-13-0).

In the present study, in order to understand the infuence of impeller blade profle on the performance of centrifugal pump in-depth, fve diferent blade schemes were obtained by adjusting the hub, middle and shroud profles of the blade. Based on the numerical method and entropy production theory, the sewage self-priming pump models under diferent blade schemes were studied and the fow states and energy losses inside the pump were analyzed quantitatively.

# **2 Entropy production theory**

It is well known that entropy is produced in an irreversible process. Any real fuid system features entropy production phenomena under the second law of thermodynamics. The entropy production method can be used to predict the hydraulic loss of centrifugal pumps accordingly [[23\]](#page-13-1).

The flow state of a centrifugal pump is turbulent. Time-averaged movement and velocity fuctuation together form the turbulent flow responsible for the rate of entropy production. The entropy production rate (EPR, *S*<sup>*i*</sup>') is calculated as follows [\[24](#page-13-2)]:

$$
\dot{S}^{\prime\prime\prime} = \dot{S}^{\prime\prime\prime}_{D} + \dot{S}^{\prime\prime\prime}_{D^{\prime}} \tag{1}
$$

<span id="page-2-3"></span>

The time-averaged movement part is presented in Eq. ([2\)](#page-2-0) and the velocity fuctuation part is presented in Eq. ([3](#page-2-1)):

$$
\dot{S}_{D}''' = \frac{2\mu}{T} \left[ \left( \frac{\partial \bar{u}}{\partial x} \right)^2 + \left( \frac{\partial \bar{v}}{\partial y} \right)^2 + \left( \frac{\partial \bar{w}}{\partial z} \right)^2 \right] \n+ \frac{\mu}{T} \left[ \left( \frac{\partial \bar{v}}{\partial x} + \frac{\partial \bar{u}}{\partial y} \right)^2 + \left( \frac{\partial \bar{w}}{\partial x} + \frac{\partial \bar{u}}{\partial z} \right)^2 + \left( \frac{\partial \bar{v}}{\partial z} + \frac{\partial \bar{w}}{\partial y} \right)^2 \right]
$$
\n
$$
\dot{S}_{D}''' = \frac{2\mu_{\text{eff}}}{T} \left[ \left( \frac{\partial u'}{\partial x} \right)^2 + \left( \frac{\partial v'}{\partial y} \right)^2 + \left( \frac{\partial w'}{\partial z} \right)^2 \right]
$$
\n(2)

$$
\dot{S}_{D'}^{"'} = \frac{2\mu_{\text{eff}}}{T} \left[ \left( \frac{\partial u'}{\partial x} \right) + \left( \frac{\partial v'}{\partial y} \right) + \left( \frac{\partial w'}{\partial z} \right) \right] \n+ \frac{\mu_{\text{eff}}}{T} \left[ \left( \frac{\partial v'}{\partial x} + \frac{\partial u'}{\partial y} \right)^2 + \left( \frac{\partial w'}{\partial x} + \frac{\partial u'}{\partial z} \right)^2 + \left( \frac{\partial v'}{\partial z} + \frac{\partial w'}{\partial y} \right)^2 \right]
$$
\n(3)

where  $S_D^{\prime\prime\prime}$  is the entropy production rate caused by time-averaged movement;  $\dot{S}^{\prime\prime\prime}_{D^\prime}$  is the entropy production rate caused by velocity fluctuation;  $\mu$  is the dynamic viscosity;  $\bar{u}$ ,  $\bar{v}$  and  $\bar{w}$ are the time-averaged velocity components (m/s); *u*′ , *v*′ and *w*′ are the fuctuation velocity components (m/s); *T* is the temperature; the constant value of 293 K is set for calculation;  $\mu_{\text{eff}}$  is the effective dynamic viscosity and is defined in Eq. ([4\)](#page-2-2):

$$
\mu_{\text{eff}} = \mu + \mu_{t} \tag{4}
$$

in which  $\mu_t$  is the turbulent dynamic viscosity (Pa s).

 $S_{p}$ <sup> $\prime\prime\prime\prime$ </sup> can be calculated directly by simulation; however, the  $\tilde{S}^{\prime\prime\prime}_{D^{\prime}}$  is not calculated directly; instead, it can be calculated as follows [[25](#page-13-3)]:

$$
\dot{S}_{D'}''' = \alpha \frac{\rho \omega k}{T} \tag{5}
$$

where  $\alpha$  = 0.09,  $\omega$  is the turbulent eddy frequency (s<sup>-1</sup>) and *k* is the turbulent energy  $(m^2/s^2)$ .

The total EPR  $S_{\text{pro}}$  is an integration of the local EPR volumes:

$$
S_{\rm pro} = \int_{V} \dot{S}_{D}^{\prime\prime\prime} dV + \int_{V} \dot{S}_{D}^{\prime\prime\prime} dV \tag{6}
$$

<span id="page-2-0"></span>where  $V$  is the volume of flow passage in each hydraulic component.

# **3 Calculation model and calculation method**

#### <span id="page-2-1"></span>**3.1 Basic parameters of model pump**

In the present study, a ZW100-100-15 sewage selfpriming pump was employed as the research object. The design parameters of pump are flow rate  $Q_d = 100 \text{ m}^3/\text{h}$ , head  $H_d = 15$  m, speed  $n = 2900$  r/min, inlet diameter  $D_1 = 98$  mm, outlet diameter  $D_2 = 142$  mm, number of blades  $Z = 2$  and blade outlet height  $b<sub>2</sub> = 68$  mm. The inlet and outlet placement angle of blade profle on shroud surface is  $\beta_{1s}=20^\circ$  and  $\beta_{2s}=22^\circ$ , respectively; the inlet and outlet placement angle of blade profle on middle surface is  $\beta_{1m} = 22.5^{\circ}$  and  $\beta_{2m} = 22^{\circ}$ , respectively; the inlet and outlet placement angle of blade profle on hub surface is  $\beta_{1h}$ =25° and  $\beta_{2h}$ =22°. In addition, the blade inlet thickness is 5 mm and the outlet thickness is 6 mm.

<span id="page-2-2"></span>Figure [1](#page-1-0) shows the blade placement angle profiles for different impellers in which the blade angle distribution profile on hub surface of S1, S2, S3, S4 and S5 was arranged in a convex shape, a saddle shape, a linear drop shape, an inverse saddle shape and a concave shape, respectively. The shroud profile and the middle profile were adjusted according to the shape of hub profile by the Bezier control points automatically, and the blade wrap angle of each scheme also changes accordingly.

Table [1](#page-1-1) shows the wrap angle of the blade profiles for five different impeller schemes. Moreover, the shapes of

<span id="page-3-0"></span>



<span id="page-4-0"></span>**Fig. 3** Computational domains of a pump model. **a** Fluid domains, **b** calculation meshes



<span id="page-4-1"></span>**Fig. 4** Grid sensitivity validation  $(1.0Q_d)$ 

blade without thickness of five different impeller schemes are presented in Fig. [2.](#page-2-3) And the detail information of blade radius distributions of five impeller schemes is given in Table [2](#page-3-0).

#### **3.2 Fluid domains and mesh**

The fuid domains of pump included the inlet pipe, suction, impeller, volute, chamber, outlet pipe, seal ring and recir-culation hole (Fig. [3a](#page-4-0)). The leakage flow effect on hydraulic performance was considered by involving the seal ring during the modeling process. The lengths of inlet pipe and outlet pipe were set as ten times of the pipe diameter. The fuid domains of pump were constructed by 3D software and



<span id="page-4-2"></span>**Fig. 5** Validation for performance data of S5

meshed into hexahedral grids by using commercial software GridPro (Fig. [3](#page-4-0)b). The blades and tongue were well refned to keep high mesh quality. Taking S5 as an example, the grid sensitivity test was performed by ANSYS CFX with SST *k*–*ω* turbulence model. The grid sensitivity analysis was carried out to determine the appropriate number of grids. Figure [4](#page-4-1) shows that as the number of grid is about 3.9 million, the head (*H*), torque (*T*) and total entropy production rate  $(S_{\text{pro}})$  basically remain stable and their value is about 16.9 m, 19.4 N m and 3.8 W/K, respectively, under designed flow rate condition. In order to balance the calculation accuracy and calculation time, the total mesh number of the fnal model is set at 3,931,964, in which the number of grids of impeller, volute, chamber and suction is 555,532, 461,312,



<span id="page-5-0"></span>**Fig. 6** Performance curves of fve diferent impellers under diferent flow rate conditions

2,157,056 and 170,000, respectively, and the grid number of other computing domains is 588,064.

#### **3.3 Numerical approach**

Performance data and flow fields of the sewage self-priming pump were calculated numerically. The SST *k*–*ω* turbulence model was applied to solve the calculation. The boundary condition was set as the total pressure inlet and its relative pressure was 0 bar, and the outlet was set as the mass fow outlet. The wall of the fuid domain was divided into two types: rough wall surface and smooth wall surface. The impeller and pump casing were made by sand casting process; therefore, those were set as no-slip rough surfaces with a roughness of 0.04 mm, while the other parts were set as no-slip smooth walls. The rotating and static couplings of the interface between the impeller and the suction, and the interface between the impeller and the volute were set as the frozen rotor interface. Since both sides of the interface have disconnected meshes and nodes, the general grid interface was applied to transfer information from one side to another. The high-order solution was set for calculation with the convergence residual RMS below  $10^{-5}$  for all equations.



<span id="page-5-1"></span>**Fig. 7** Static pressure loads of fve diferent impellers at span 0.5 under diferent fow rate conditions

<span id="page-6-0"></span>



# **3.4 Validation of numerical method**

Figure [5](#page-4-2) shows the performance curve comparison between the experimental results and the numerical results of S5. As can be seen from the fgure, the maximum deviation of head under the part-load conditions is about 8%. It is because the existing numerical method is incapable to predict pump performance accurately at small fow rate conditions for the high complex turbulent flows inside pump. At the designed flow rate  $Q_d = 100 \text{ m}^3/\text{h}$ , the calculated head is 16.9 m, while the experimental head is 16.58 m. Therefore, its error is 0.32 m, and the relative error is 1.93%, which meets the calculation accuracy requirements. As the fow rate moves to the over-load conditions, the head error slightly increases. Furthermore, as for the efficiency curve, the consistency between the experimental value and the calculated value is relative well. However, at high flow rate conditions, there is a certain deviation between the two. It is due to the mechanical and leakage losses which are not considered in the efficiency calculation. Based on the above analysis, the

numerical calculation model has better accuracy and can meet the following calculation and verifcation requirements.

# **4 Results and discussion**

#### **4.1 Performance curves of diferent blade profles**

Figure [6](#page-5-0) shows the hydraulic performance calculation results for the sewage self-priming pump models with fve diferent impellers.

It is obviously found that the relative diference among the performance curves of S2, S3 and S4 is small. Looking at the *Q*–*H* curve only, the head of S1 is the lowest at any fow rate, and a local hump phenomenon occurs in the small flow rates area. As the flow rate increases up to the design and overfow operating points, the head value of S5 is higher than that of the others. In addition, as for the S5, the head at the design flow rate of  $100 \text{ m}^3/\text{h}$  is  $16.9 \text{ m}$ , which is higher than the target design head and the head of

<span id="page-7-0"></span>**Fig. 9** EPR distribution and streamlines at middle-span surface of diferent impellers at  $0.7Q_d$ 



S2, S3 and S4 basically meets the target, while the S1 has a low head at design fow rate and fails to meet the target. Furthermore, for the *Q*–*η* curve, it is observed that at any flow rate, the efficiency of S5 is higher than that of the others, while the efficiency of S1 is the lowest. At the design flow rate, the maximum efficiency of  $S5$  is  $67.57\%$ , the maximum efficiency of S2, S3 and S4 is relatively close, which is 59.05%, 59.45% and 59.61%, respectively, and the efficiency of S1 is smallest whose value is  $50.68\%$ . Therefore, it can be concluded that the blade profle has a greater infuence on pump performance. It is noted that the blade of S5 has a large wrap angle, which takes a good government on the fuid inside the impeller in the purpose of reducing the scale of fow slip and fow separation phenomenon greatly. It is therefore the mechanical energy can be largely converted into the potential energy. In the other hand, the blade of S1 has a smaller wrap angle, so the fuid is not controlled well in the channels, and the slip and fow separation phenomena are easier to generate. Therefore, as for S1, a high energy loss is generated and its head and efficiency are relatively low.

#### **4.2 Blade loads of diferent blade profles**

Figure [7](#page-5-1) shows the static pressure load curves of five different impellers at middle-span surface (span 0.5). The abscissa indicates the normalization distance from the inlet to the outlet of blade, and the ordinate indicates the static pressure load of blade. The upper curve illustrates the pressure load of the pressure side of blade, and the lower curve presents the pressure load of the suction side of blade.

It is illustrated that the static pressure loads on the blade gradually increase from the leading edge of blade to the trailing edge of blade. However, in the flow conditions of  $0.1Q_d$ and  $0.3Q<sub>d</sub>$ , it is obviously found that, for S1 impeller, a peak pressure value appeared at middle of pressure side of blade, which is because a large blade placement angle is given for S1 at mid-length of blade. The static pressure distribution curves of the S2, S3 and S4 impellers are basically consistent and relatively stable. With the continuous increase in fow rate, the static pressure loads of the impellers tend to be stable and evenly distributed. It can be seen clearly from the curves that the static pressure value of the pressure surface

<span id="page-8-0"></span>



on the blade is basically higher than that of the suction surface, and only in the case of too low flow rates, the static pressure value of pressure side is lower than the value of the suction side appearing in a small area near the leading edge of the blade. This results from high incidence angle of fow at part-load conditions, because the high incidence angle makes the flow velocity near the pressure side of leading edge is higher that of suction side. By following the Bernoulli's principle, it determines higher pressure near suction side of blade leading edge. From the above discussion, it is concluded that the blade profle signifcantly infuenced the fow state and pressure distribution of impeller. In addition, it is illustrated that the pressure load of the impeller at design fow rate condition is more stable than that of the non-design conditions.

# **4.3 Internal fow features of impellers with diferent blade profles**

Figures [8,](#page-6-0) [9](#page-7-0), [10](#page-8-0) and [11](#page-9-0) show the EPR distribution and velocity streamlines of the impeller with diferent blade profles on the middle-span surface (span 0.5) under four typical fow conditions. It is observed that when  $Q = 0.1 Q_d$ , large flow separation and low-speed vortex zones are generated close to the suction side of the impellers and high energy losses are produced. This is due to the high angle of incidence of flow for a too low flow rate condition. In such a flow condition, the relative fow angle is smaller than the blade inlet placement angle, and the fuid enters the impeller as a positive incidence angle, so that the fuid velocity at the suction side of the blade is lower than that of at the middle flow across channel. The flow velocity difference enlarges the shear effect and produces the flow separation and vortex. However, as the fow rate increases, the relative fow angle is increasing and the incidence angle is decreasing; as a result, these two angles are matched, so that it makes the fow state more stable. Meanwhile, the low-speed vortex areas are also reduced significantly. At the operating points of  $1.0Q<sub>d</sub>$  and 1.3 $Q_d$ , it can be seen that the flow angle is basically the same as the blade inlet placement angle, so that the fow entering into the blade is quite stable. There is only a local small

<span id="page-9-0"></span>**Fig. 11** EPR distribution and streamlines at middle-span surface of diferent impellers at  $1.3Q_d$ 



vortex area found at the outlet of blade, and the local energy losses are reduced more.



<span id="page-9-1"></span>**Fig. 12** Total EPR distributions of diferent impellers

Figure [12](#page-9-1) shows the total EPR  $(S_{\text{pro}})$  of the impellers with diferent blade profles under four typical fow conditions. It can be obtained that total EPR of S1 impeller is higher than that of other impellers and its maximum value is about 10.5 W/K at 0.1 $Q_d$ . However, S5 impeller has minimum total EPR values and its minimum value is 1.84 W/K at  $1.0Q<sub>d</sub>$ . With the increase in the flow rate, the total EPR of impeller, except S1 impeller, decreases frst and then increases slightly and reaches the minimum at  $1.0Q_d$ . Based on the above analysis, it is presented that the fow state of the S5 impeller is the most stable and strength of vortex is the weakest; therefore, its total EPR and internal energy loss are the smallest.

# **4.4 Energy losses of pump with diferent blade profles**

Figures [13](#page-10-0), [14](#page-10-1), [15](#page-11-0) and [16](#page-11-1) illustrate EPR distribution of pumps with five different impellers under different flow conditions. It is presented that under part-load flow conditions, high EPR values are mainly concentrated on impeller, volute and suction areas and the less energy losses are found

<span id="page-10-1"></span><span id="page-10-0"></span>

in chamber area. This is quite expected outcome, as a result of the strong hydraulic and impact losses, which induced from the backflow, flow separation, vortex and rotor-stator interactions in these fow domains. When the fow rate increases, the EPR values reduce largely and the hydraulic loss inside the impeller is signifcantly decreased. For the volute area, the energy loss is transferred to the difusion section of volute, and the high EPR values appear at the upper part of the chamber. At the design and over-load flow conditions, high EPR values are observed in the impeller

S1 S2 S3 S4 S5

<span id="page-11-0"></span>**Fig. 15** Total EPR distribution in the pump with diferent impellers at  $1.0Q_d$ 



<span id="page-11-1"></span>**Fig. 16** Total EPR distribution in the pump with diferent impellers at  $1.3Q_d$ 



outlet, and this energy loss is mainly caused by the shearing efect between the blade trailing edge and fuid. In addition, high EPR values are also found in the volute tongue area, the difusion section and the upper left area of the chamber. This is due to the fact that, as the fow rate increases, the high-speed jet flows pumping out from the impeller and volute enhance the shear and impact losses inside the pump.

Comparing the EPR distribution of diferent impeller schemes at the same flow rate condition, it is illustrated that the EPR values of S5 are lower than those of other schemes,

which indicates that the internal energy loss of S5 is the smallest and the hydraulic efficiency is the highest.

# **5 Conclusions**

Based on the numerical calculation and entropy production theory, this paper investigated the internal flow characteristics and loss mechanism of a sewage self-priming pump with five different blade profile impellers. The following conclusions were obtained:

In comparison with the other blade profle impellers, it was found that the S5 impeller with the concave blade angle profle had the most stable internal fow and the lowest total EPR values. The blade with a larger blade wrap angle efectively governed the fow inside the impeller, which made the flow in the impeller channels not easy to slip and separate. Eventually, it weakened the energy losses caused by the slip and separation phenomena inside pump.

The relative fow angle of fuid inside the impeller was controlled by blade profles. Unsuitable blade profle led to the occurrence of negative incidence angle of fuid fow in the impeller, which enlarged the impact loss and the shearing action between the fuids. And the local vortex appeared in the inlet area of the blade. Therefore, the blade profles could determine the fow states, pressure loads and hydraulic losses of the impeller.

The entropy production theory was used to deeply analyze the distribution of energy loss inside pump with diferent impellers. Under small fow rate conditions, the large shear and impact effects were caused by the interferences between the high-speed jet fow from the outlet of the blade and the low-speed fuid inside the volute. The rotor and stator interactions of the impeller and volute strengthened the energy loss inside the impeller and volute. With the increase in the fow rate, the internal energy loss of the impeller was signifcantly reduced, and the energy loss was transferred to the difusion section of the volute and the upper part of the chamber. This was due to the high-speed jet fows pumping out from the impeller and volute enhanced the shear and impact losses inside the volute and chamber.

**Acknowledgements** The authors gratefully acknowledge the support from the National Natural Science Foundation of China (No. 51606167 and 51609212), the Open Foundation of Zhejiang Provincial Top Key Academic Discipline of Mechanical Engineering (No. ZSTUME02A04) and Postdoctoral Research Foundation of Zhejiang Province (CN) titled with "Studies on the inner fow mechanism in the centrifugal pump impeller at lower fow rate conditions based on anisotropic LES analysis."

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