

# **Infuence of Liquid Film Characteristics on Hot Cracking Initiation in Al–Cu Alloys at the End of Solidifcation**

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### **Abstract**

In this study, Al–4Cu alloy specimens with spherical grains and liquid flms were obtained by isothermal reheating treatment. The hot cracking of the solidifcation process was determined using a modifed constrained rod casting experimental apparatus, and the efect of liquid flm characteristics at the end of solidifcation on hot cracking initiation of Al–4Cu alloys was systematically investigated by combining molecular dynamics simulations and other methods. With the extension of soaking time, the liquid fraction (liquid flm fraction at the end of solidifcation) and grain shape factor increased with higher isothermal reheating temperatures. Additionally, the widened flling channel decreased the hot cracking initiation temperature and the critical hot cracking shrinkage stress was found to increase, thus reducing the hot cracking severity in Al–4Cu alloys. Molecular dynamics simulations revealed that with the extension of soaking time, the composition of the liquid flm changed at diferent isothermal reheating temperatures, but the short-range structure and atomic ordering of the liquid flm remained the same. The activity of the liquid flm increased in equilibrium, leading to a decrease in viscosity and an increase in fluidity, which contributed to the filling behaviour. After isothermal reheating at  $640\degree\text{C}$  for  $60\text{ min}$ , the liquid fraction reached the maximum, and the viscosity of the liquid flm was the minimum. In addition, almost no hot cracks were found.

**Keywords** Al–4Cu alloy · Liquid flm characteristics · Isothermal reheating · Molecular dynamics simulation · Hot cracking initiation mechanism

# **1 Introduction**

Al–Cu alloys have been widely used in many felds such as the aerospace industry, automobile industry and mechanical equipment, because of their low density, high specifc strength and strong corrosion resistance [[1,](#page-13-0) [2\]](#page-13-1). Despite their advantages, the limiting factor of Al–Cu alloys is their high susceptibility to various defects in castings, such as shrinkage porosity, hot cracking, segregation and microporosity, due to their wide solidifcation temperature range and large solidifcation shrinkage [[3,](#page-13-2) [4](#page-13-3)]. These defects are more

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 $\boxtimes$  Wentao Zheng wenntaozheng@163.com serious in thin-walled castings, which restricts the wide application of Al–Cu alloys [\[5](#page-13-4), [6](#page-13-5)].

Hot cracking is the most common and serious defect in Al–Cu alloys at the end of solidifcation, which leads to a drastic reduction in the mechanical properties of the castings [[7\]](#page-13-6). To reduce hot cracking and determine the mechanism of hot cracking initiation in Al–Cu alloys, a series of studies have been performed by many researchers. D' Elia et al. [[8\]](#page-13-7) investigated the infuencing factors of the hot cracking severity in cast Al–Cu alloys using constrained rod casting (CRC) experiments and found that refning the grain and increasing the mould temperature could increase the fuidity of the liquid flm at the end of solidifcation and extend the flling time, thus efectively reducing the hot cracking. D' Elia et al. [\[9](#page-13-8)] also investigated the mechanism of liquid flm feeding in a B206 Al–Cu alloy. Their results revealed that the eutectic phase rich liquid flm did not fll the hot cracks completely at the end of solidifcation. Yang et al. [[10](#page-13-9)] reported that the addition of TiC particles refned the grain size of Al–Cu alloys and improved the hot cracking resistance of Al–Cu alloys. Li et al. [[3](#page-13-2)] reported that the hot cracking severity of

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Al–Cu alloy castings decreased with increasing wall thickness using CRC experiments, while grain refnement was found to reduce the shrinkage of the liquid phase between the dendrites. Shabestari et al. [\[11](#page-13-10)] reported that hot cracks in Al–Cu alloys always formed in the mushy zone at the end of solidifcation by thermal analysis. Due to the variation in mushy zone properties for diferent cooling rates, the resistance to hot cracking was improved. Liu and Kou [[12\]](#page-13-11) reviewed that hot cracks occurred at the end of solidifcation. Thus, Liu and Kou [\[13](#page-13-12)] also revealed that hot cracks usually emerged in grain boundaries as a consequence of fewer liquid flms between grain boundaries. Collectively, the studies presented thus far provide evidence that hot cracks occurred at the residual liquid phase and extended along the grain boundaries in the final stage of solidification  $[14]$  $[14]$ , which was due to insufficient liquid film fluidity to resist solidification shrinkage at the end of solidifcation [[15,](#page-13-14) [16](#page-13-15)]. Therefore, the liquid flm is an important component in reducing hot cracks in the alloy and plays a key role in restraining the shrinkage of the alloy.

Early research on hot cracking initiation suggested that hot cracks resulted from local thermal stress concentrations [[17,](#page-13-16) [18](#page-13-17)]. Therefore, Takai et al. [[19\]](#page-13-18) determined that the grain refned structure elongation was greater than that in the coarse grain structure regardless of the solid fraction. Furthermore, Takai et al. [[20](#page-13-19)] determined the relationship between hot cracking initiation and the magnitude of tensile force by applying an active load to the mushy zone at the end of solidifcation and collected images by high-speed photography based on a CRC experiment. Matsushita et al. [[21\]](#page-13-20) established a solid–liquid two-phase fnite element model with a liquid flm skeleton structure based on the waterquenched organization of the casting at the end of solidifcation and determined the critical stress to separate the liquid and solid phases by fnite element simulations. Xu et al. [[22,](#page-13-21) [23](#page-13-22)] found that the liquid flm of the Al–Si alloy was elongated and was able to resist tensile force under active loading tension and built a hot cracking criterion model based on the nominal yield stress. The current research on the liquid flm and the mushy zone at the end of solidifcation was limited to active loading tension to determine the constitutive model and the hot cracking severity. However, the shrinkage force during solidifcation was extremely complicated, and the active loading tension could not be used on behalf of the shrinkage force.

The liquid flm characteristics play a crucial role in hot cracking during the solidifcation process. The liquid flm characteristics include the structural characteristics, radial distribution function (RDF), diffusivity coefficient (*D*) and viscosity (*η*) [\[24](#page-13-23), [25](#page-13-24)]. The liquid flm characteristics change with the solidification process and are difficult to characterize by experimental methods. Due to the rapid development of the computational material sciences, theoretical studies of the atomic structure evolution upon solidifcation from the metallic liquid have become possible. Factors that infuence metallic liquid characteristics have been explored in several studies. Roik et al. [\[26\]](#page-14-0) calculated the RDF of binary Al alloys by molecular dynamics (MD) simulation and found that the melting binary Al alloys had a short-range structure, and diferent melting binary Al alloy structures led to differences in their characteristics. Wang et al. [\[27](#page-14-1)] calculated the local structure, *D* and *η* of liquid binary Al–*x*Zr alloys by MD simulation, and demonstrated that diferent contents of Zr could afect the characteristics of liquid Al–*x*Zr alloys. Therefore, MD simulation is a reliable method to confrm the characteristics of metallic liquids and provides theoretical support for this study to calculate the characteristics of liquid flms.

As previously stated, the CRC experiment is a valid and widely used method to determine the hot cracking severity in casting alloys [[28,](#page-14-2) [29](#page-14-3)]. In this research, a modifed constrained rod casting (MCRC) experimental apparatus equipped with a load cell was developed to determine the onset temperature of hot cracks. The isothermal remelting treatment of nondendritic structure Al–4Cu alloy specimens was used to reproduce the intergranular liquid flm skeleton structure, and the solidifcation shrinkage force under different isothermal remelting conditions was measured to establish the relationship between the critical cracking stress and the liquid fraction. The infuence mechanism of liquid flms on hot crack initiation was investigated by observing the morphology of hot cracks. MD simulation was used to quantify the characteristics of the liquid flm and verify the efect of liquid flm characteristics on hot crack initiation.

# **2 Experimental**

### **2.1 Materials**

Al–4Cu alloys with a high hot cracking severity were used in this study. Al–4Cu billets with nondendritic structures were fabricated by mechanical stirring. First, high-purity Al was placed in a crucible that was preheated to 500 °C and subsequently heated to 750 °C. Al–50Cu was added to the highpurity Al melt. Until the alloy was completely melted, the refining agent, deslagging agent and deoxidizer  $(C_2Cl_6)$  were added in order and held for 10 min (the amount of each addition was 0.5–0.7 wt% of the molten metal). Finally, the alloy melt was poured into the H13 steel mould which was coated with a zinc oxide solution in the cavity and preheated to 300 °C. The microstructure was observed by optical microscopy (OM, ZEISS). The phase composition was determined by an X-ray difractometer (XRD, SHIMADZU XRD-7000) equipped with a Cu  $K\alpha$  source radiation and a transmission electron microscope (TEM, JEM-2100). XRD patterns were recorded in the 2 $\theta$  range of 20°–100° at a scan speed of 2°/ min. TEM analysis was conducted at 200 kV. The thin foil specimen for TEM analysis was ground to 50 μm thickness, and then, a 3-mm disc was punched out before ion milling.

#### **2.2 Isothermal Remelting Treatment**

A DSC-S1000 differential scanning calorimeter (DSC) apparatus was used to determine the range of isothermal remelting temperatures. The samples were heated to 700 °C at 10 °C min−1 under a nitrogen atmosphere. As indicated in Fig. [1](#page-2-0), based on the DSC curve, the solidus and liquidus temperatures of Al–4Cu alloys were 549 °C and 663 °C, respectively. The liquid fraction versus the temperature curve was obtained by integrating the DSC curve. Considering that the DSC heating rate was close to the actual isothermal reheating rate, the theoretical liquid fraction versus temperature curve of the Al–4Cu alloy specimens measured in DSC was used as a reference for determining the isothermal remelting experimental temperature [\[30](#page-14-4)].

The isothermal remelting experiment was performed using a tubular resistance furnace (1 kW, 220 V) to heat a cylindrical specimen with a diameter of 6 mm and a length of 30 mm (surface pretreatment of the specimens prior to microstructure observation). The oxide flm formed during the heating process had no efect on the experimental results, and thus, protective gas was not required. As shown in Fig. [1](#page-2-0), isothermal reheating temperatures of 620 °C, 630 °C and 640 °C, corresponding to theoretical liquid fractions of 10%, 15% and 25%, respectively, were determined from the DSC curves. The samples were soaked for 10 min, 20 min, 30 min, 40 min, 50 min and 60 min at each given temperature and then quickly quenched in cold water to preserve the microstructure obtained at the isothermal remelting stage. OM was used



<span id="page-2-0"></span>**Fig. 1** DSC curve and theoretical liquid fraction versus temperature of the Al–4Cu alloy

to observe the microstructure after water quenching. The elemental distribution of the semisolid microstructure after water quenching was analysed by electron probe microanalysis (EPMA, EPMA-1720). In this study, the experimental liquid fraction (LF) and shape factor (SF) of solid grains were measured by Image-Pro Plus 6.0 software. LF and SF were defned using Eqs. [\(1](#page-2-1)) and ([2](#page-2-2)), respectively [\[31,](#page-14-5) [32](#page-14-6)].

<span id="page-2-1"></span>
$$
LF = \frac{A_{\rm L}}{A_{\rm Total}} \times 100\%
$$
 (1)

<span id="page-2-2"></span>
$$
SF = \frac{\sum_{i=1}^{N} 4\pi A_i / P_i^2}{N}
$$
 (2)

where  $A_L$ ,  $A_{\text{Total}}$ ,  $A_i$ ,  $P_i$  and  $N$  are the area of the liquid, area of the micrograph area, area of the solid grains, perimeter of the solid grains and total number of solid grains, respectively.

#### **2.3 Liquid Film Shrinkage Stress Test Device**

In this study, the shrinkage stress of the liquid flm at the end of solidifcation was measured by an MCRC apparatus, as shown in Fig. [2a](#page-3-0). The Al–4Cu alloy specimens with spherical solid and liquid flms were obtained by isothermal reheating treatment in a tube resistance furnace. First, the temperature of the tube resistance furnace was increased to the set value and was kept for 30 min to make the interior temperature of the tube furnace uniform and stable. Then, one end of the specimen was held by a restraining rod, and the other end was connected to a connecting rod. The tube furnace was turned off after the scheduled holding time, and the stress sensor was connected to the connecting rod so that it collected the contraction stress of the liquid flm during solidifcation and cooling. The data acquisition system included the thermocouple, the stress sensor and the computer data acquisition device. The real-time data measured by the thermocouple and the stress sensor were stored on the computer through the data acquisition system, as illustrated in Fig. [2b](#page-3-0). The diameter of the specimen used to measure the shrinkage stress of the liquid flm at the end of solidifcation was the same as that in the isothermal remelting experiment to ensure that the microstructure morphology of both was the same, and the specimen size is shown in Fig. [2](#page-3-0)c. Microstructure observation and compositional analysis of hot cracks after solidifcation were performed by a scanning electron microscope (SEM, HITACHI-S3400 N) equipped with an energy-dispersive spectrometer (EDS) operating at 20 kV.



<span id="page-3-0"></span>**Fig. 2** Schematic diagram of the experimental system for liquid flm shrinkage stress: **a** isothermal reheating treatment experiment device, **b** overall experimental system and **c** size of the specimen

# **2.4 MD Simulation**

In this study, RDF, *D* and *η* were used to characterize the liquid flm. *D* was derived from Einstein's relation [[33\]](#page-14-7) through the mean square displacement (MSD) as a function of time, as shown in Eq.  $(3)$  $(3)$ ,

$$
D = \lim_{t \to \infty} \frac{\langle R^2(t) \rangle}{6t}
$$
 (3)

where *t* is time and  $\langle R^2(t) \rangle$  is the MSD as a function of time. RDF and *D* are obtained from MD simulation, and *η* of liquid flms at diferent isothermal remelting conditions can be derived from the Stokes–Einstein equation as follows [\[34\]](#page-14-8):

$$
\eta = \frac{kT}{2\pi aD} \tag{4}
$$

where the parameters of *k*, *T* and *D* are Boltzmann's constant, temperature and diffusion coefficient, respectively. The parameter *a* denotes the effective atomic diameter, which can be determined by the position of the frst peak in the RDF.

The MD simulation of the liquid flm in this work was conducted by Material Studio (version 2019) software using the Focite package based on potential function theory. A cubic  $5 \times 5 \times 5$  supercell with periodic boundary conditions was built, where the atoms were randomly distributed in the initial state. The simulations were calculated by the canonical NVT ensemble (fxed atom number, volume and temperature). The temperature was controlled by the velocity scaling method. At each isothermal remelting condition, the

liquid flm system reached an equilibrium state of 200 ps, and the evolution of the atomic structure is presented in Fig. [3.](#page-4-0)

# <span id="page-3-3"></span>**3 Results**

# <span id="page-3-1"></span>**3.1 Microstructure Evolution of Al–4Cu Alloys During Isothermal Remelting Treatment**

The microstructure of the Al–4Cu alloy billets is presented in Fig. [4](#page-4-1)a. It can be found that the grains had a nondendritic morphology and the eutectic phase was distributed at the grain boundaries. The phase composition of the Al–4Cu alloy billets was initially determined to be  $\alpha$ -Al and Al<sub>2</sub>Cu by XRD, as indicated in Fig. [4](#page-4-1)b. The eutectic phase distributed at the grain boundaries was identified to be  $Al<sub>2</sub>Cu$  with a striped shape by TEM, as shown in Fig. [4](#page-4-1)c.

<span id="page-3-2"></span>The EPMA mapping of the main alloying elements of Al–4Cu alloy billets after isothermal reheating treatment at 630 °C for 50 min is presented in Fig. [5](#page-5-0). The lighter colour of the elemental intensity scale means a greater concentration of elements and a higher elemental content at this location. The solid grains and liquid phases at the grain boundaries are observed in Fig. [5](#page-5-0)a. As shown in Fig. [5](#page-5-0)b, c, Al and Cu elements in the liquid phase were distributed between the grain boundaries, and only a few Cu elements distributed within the  $\alpha$ -Al solid grains.

The effects of the isothermal remelting treatment temperature and time on the semisolid microstructure of Al–4Cu alloys are illustrated in Fig. [6.](#page-5-1) Figure [6](#page-5-1)a–c shows the



<span id="page-4-0"></span>**Fig. 3** Atomic structure evolution of liquid flms after isothermal reheating treatment at 630 °C for 50 min: **a** 0 ps, **b** 100 ps, **c** 200 ps



<span id="page-4-1"></span>**Fig. 4** Microstructures and phase composition of the billet of Al–4Cu alloy: **a** OM, **b** XRD, **c** TEM

microstructures of Al–4Cu alloys after isothermal remelting treatment at 620 °C for diferent soaking time. As shown in Fig.  $6a$ , the eutectic phase Al<sub>2</sub>Cu at the grain boundaries was completely melted to form liquid flms with skeleton network channels and surrounding the solid grains after isothermal remelting treatment at 620 °C for 20 min. The small α-Al solid grains had a higher spheroidization degree, while the large ones had diferent sizes and shapes, and the grain edges were irregular. The lower spherization degree of α-Al solid grains was caused by few liquid flms at the grain boundaries after short-time soaking. The increase in liquid flm thickness and the form of interconnected liquid



**Fig. 5** EPMA analysis mapping results of Al–Cu alloys after isothermal reheating treatment at 630 °C for 50 min: **a** OM, **b** Al and **c** Cu

<span id="page-5-0"></span>

<span id="page-5-1"></span>**Fig. 6** Microstructures of Al–4Cu alloys after isothermal reheating treatment: **a** 620 ℃, 20 min; **b** 620 ℃, 40 min; **c** 620 ℃, 60 min; **a1** 630 ℃, 20 min; **b1** 630 ℃, 40 min; **c1** 630 ℃, 60 min; **a2** 640 ℃, 20 min; **b2** 640 ℃, 40 min; **c2** 640 ℃, 60 min

flm skeleton network channels were associated with the increased soaking time, while the spherization degree and grain sizes of  $\alpha$ -Al solid grains gradually increased, as illustrated in Fig. [6b](#page-5-1), c. The reason for the above-mentioned phenomenon was, on the one hand, Ostwald ripening (see the red boxes) which was noticed that the increase in soaking time enhanced the growth of the large grains and the small grains were observed to melt. On the other hand, the thin liquid flm reduced the distance between grains, and diferent solid grains with the same crystal orientation coalesced together (see the red ellipses), which was consistent with the results of Jiang et al. [[35\]](#page-14-9).

Figure [6a](#page-5-1)1, b1 and c1 presents the microstructures of Al–4Cu alloys after isothermal remelting treatment at 630 °C for diferent soaking time. As can be seen in Fig. [6](#page-5-1)a1, the eutectic phase  $Al<sub>2</sub>Cu$  was completely melted and formed interconnected liquid flms with skeleton network channels, and Ostwald ripening and coalescence growth were observed. In addition, at 630 °C for 20 min, the spheroidization degree of  $\alpha$ -Al solid grains increased compared to that at 620 °C for 20 min. Some large intragranular liquid drops that broke the original grain boundaries occurred within  $\alpha$ -Al solid grains, as presented by the red arrows in Fig. [6b](#page-5-1)1. These liquid drops gradually decreased and even disappeared with the extension of soaking time, which was caused by the movement of intragranular liquid drops to the grain boundaries or the migration of the liquid flm along the grain boundaries [\[36\]](#page-14-10). The interconnected liquid flm skeleton network channel thickness peaked after 60 min of soaking.

Figure [6a](#page-5-1)2, b2 and c2 indicates the microstructures of the Al–4Cu alloy after isothermal remelting treatment at 640 °C for diferent soaking time. A similar microstructure evolution can be obtained compared to that at 630 °C and 640 °C. In contrast, as presented in Fig. [6](#page-5-1)c2, the liquid drops within the  $\alpha$ -Al solid grains significantly reduced, and the skeleton network channels of the liquid flms became wider. At the same time, the spheroidization of  $\alpha$ -Al solid grains increased, and most grains were spherical and rounded rod-shaped.

The variations in SF and LF with isothermal treat-ment time at different temperatures are presented in Fig. [7](#page-6-0) using Eqs.  $(1)$  $(1)$  and  $(2)$  $(2)$ . As shown in Fig. [7a](#page-6-0), the SF always remained between 0.7 and 0.85 under diferent isothermal remelting treatment conditions, and the SF slightly increased with increasing isothermal remelting treatment temperature and soaking time, which was mainly due to Ostwald ripening. The SF value reached a maximum value of 0.822 after isothermal remelting treatment at 640 °C for 60 min. As shown in Fig. [7b](#page-6-0), the increased LF and wider liquid flm network channels were associated with the increased isothermal remelting treatment temperature and soaking time. The LF signifcantly increased and the LF value reached a maximum value of 36.68% after isothermal remelting treatment at 640 °C for 60 min.

## <span id="page-6-1"></span>**3.2 Stress–Temperature–Time Curves**

To ensure the accuracy of the experimental results, the MCRC apparatus was designed to minimize the efect of the restraining rod and connecting rod on the measured shrinkage force. On the one hand, the tube resistance furnace was designed with a short heating zone, a holding temperature zone and a transition zone. The connecting rod and restraining rod were completely exposed outside the tube resistance furnace for convective heat exchange with the air. The tube resistance furnace did not heat the connecting rod and restraining rod directly. The increased temperature of the connecting rod and restraining rod was caused by heat transfer from the Al–4Cu alloy specimens. As a result, the temperature increase of the restraining rod and connecting rod was efectively reduced. On the other hand, the connecting rod and restraining rod were made of 304 stainless steel. The thermal conductivities of 304 stainless steel and Al–Cu alloy are 12.47 W/(m K) [[37\]](#page-14-11) and 197 W/(m K) [\[38](#page-14-12)], respectively. The thermal conductivity of 304 stainless steel is much smaller than that of the Al–4Cu alloy. Therefore, the temperature of the connecting rod and restraining rod



<span id="page-6-0"></span>**Fig. 7** Variation in the **a** average shape factor, **b** liquid fraction of Al–4Cu alloys at diferent temperatures for diferent isothermal reheating treatment time

slightly increased during the experiment. Meanwhile, the temperature of the connecting rod and restraining rod ranged from 80 to 120 °C during the pre-experiment for different isothermal remelting conditions. Therefore, the increased temperature of the connecting rod and restraining rod had negligible efects on the experimental results.

The stress–time and temperature–time curves for each isothermal reheating treatment condition are presented in Fig. [8](#page-7-0). In this study, the cooling rate obtained from the temperature–time curves was approximately 0.1 °C/s. As the solidifcation commenced in the Al–4Cu alloy with near-spheroidal grains, both the liquid flm and α-Al solid grains began to shrink, and the shrinkage of the liquid flm played a major role in the entire solidifcation process, as reported by Zhou et al. [[39\]](#page-14-13) and Hao et al. [[40](#page-14-14)]. Zhong et al. [[41](#page-14-15)] and Du et al. [[42](#page-14-16)] investigated the relationship between the stress–time curves and initiated hot cracks. Their results revealed that once stress release occurred on the stress–time curves, it indicated that hot cracks initiated on the specimen. Therefore, the critical hot cracking initiation shrinkage stress value of the liquid flm and the corresponding critical hot cracking initiation temperature were obtained from the stress–temperature–time curves at each isothermal reheating treatment condition.

The stress–time and temperature–time curves for the 620 °C isothermal remelting treatment are illustrated in Fig. [8](#page-7-0)a–c, where the shrinkage stress of the liquid flm gradually increased with the progress of solidifcation. Stress releases were observed at each isothermal reheating treatment time at 620 °C, indicating that hot cracks occurred in all cases. A gradual decrease in the



<span id="page-7-0"></span>**Fig. 8** Stress–temperature–time curves after isothermal treatment: **a** 620 ℃, 20 min; **b** 620 ℃, 40 min; **c** 620 ℃, 60 min; **a1** 630 ℃, 20 min; **b1** 630 ℃, 40 min; **c1** 630 ℃, 60 min; **a2** 640 ℃, 20 min; **b2** 640 ℃, 40 min; **c2** 640 ℃, 60 min

temperature of hot cracking initiation was evident for higher soaking time; in contrast, the shrinkage stress increased.

The stress–time and temperature–time curves for the 630 °C isothermal remelting treatment are displayed in Fig. [8](#page-7-0)a1, b1 and c1. Similar to 620 °C, stress release was also observed at each isothermal reheating treatment time, confrming that hot cracking occurred at 630 °C. Two successive stress releases occurred in the stress–time curves, as shown in Fig. [8](#page-7-0)b1, implying that crack propagation or secondary hot cracks occurred in the specimen due to the insufficient feeding capacity of the liquid film. Compared with the isothermal remelting temperature of 620 °C, the hot cracking initiation temperature decreased, while the liquid flm shrinkage stress increased.

The stress–time and temperature–time curves for the 640 °C isothermal remelting treatment are displayed in Fig. [8](#page-7-0)a2, b2 and c2. The hot cracking initiation temperature signifcantly decreased, while the liquid flm shrinkage stress increased compared to the isothermal reheating temperatures of 630 °C and 620 °C, as shown in Fig. [8](#page-7-0)a2, b2 and c2. In addition, no stress release was visible on the stress–time curve, indicating that almost no hot cracks occurred at the isothermal reheating temperature of 640 °C for 60 min.

Figure [9](#page-8-0) lists the temperatures and liquid flm shrinkage stresses when hot cracking initiated for each isothermal remelting condition. As can be seen from Fig. [9](#page-8-0)a, the hot cracking initiation temperature signifcantly decreased with higher isothermal remelting treatment temperatures and longer soaking time. The hot cracking initiation temperature at 640 °C for 50 min isothermal remelting treatment was 549.84 °C, which was very close to the solidus temperature, indicating that the hot crack was not prone to form under this condition. The curve illustrates a signifcant increase in liquid flm shrinkage stress with higher isothermal remelting treatment temperature and longer soaking time when hot cracking initiate, as presented in Fig. [9](#page-8-0)b.

Combined with Fig. [7,](#page-6-0) the preliminary analysis of the results in Fig. [9](#page-8-0) is as follows. On the one hand, the diference in the feeding ability of liquid flms was likely attributed to the varied composition and characteristics of the liquid flm at each isothermal reheating treatment condition. On the other hand, with a higher isothermal remelting treatment temperature, the increased grain roundness after a longer soaking time created a wider feeding channel associated with a larger volume fraction of liquid flms, which facilitated feeding, thus making the decrease in hot cracking initiation temperature. The liquid flm characteristics were quantitatively calculated, and the mechanism of hot cracking initiation is discussed in detail in Sect. [4.](#page-10-0)

#### **3.3 Hot Cracking Morphology Analysis**

The solid fractions when hot cracking initiated in each isothermal remelting condition were measured according to Fig. [8,](#page-7-0) as listed in Table [1](#page-9-0). The range of the solid fraction for hot cracking initiation was 95.87–99.60%. The Clyne–Davies theoretical model suggested that the solid grains formed a skeleton structure when the solid fraction was between 0.9 and 0.99. The reason for this phenomenon was revealed by D 'Elia et al. [\[43](#page-14-17)]. Their research illustrated that the closed skeleton structure impeded liquid flm feeding, which easily caused intergranular hot cracking due to inadequate feeding. The range of the solid fraction for hot cracking initiation was smaller than that of the Clyne–Davies theoretical model, which was caused by the spherical solid grains during solidifcation in the present experiment. Combined with Fig. [1,](#page-2-0) no hot cracks commenced on specimens



<span id="page-8-0"></span>**Fig. 9** Variations in **a** the critical temperature, **b** critical shrinkage stress of the liquid flm of hot cracking initiation vs. isothermal treatment temperature and time

Time (min)	10	20	30	40	50	60
620	95.87	96.38	96.60	96.66	96.73	96.78
630	96.33	96.51	96.70	96.84	96.95	97.26
640	96.76	96.91	96.95	97.43	99.60	$\overline{\phantom{a}}$

<span id="page-9-0"></span>**Table 1** Critical solid fraction (%) after hot cracking initiation for diferent isothermal treatment conditions

until eutectic  $\text{Al}_2\text{Cu}$  nucleated. As a result, the shrinkage of the specimen could only be accommodated mainly by feeding with eutectic-rich liquid as the last liquid available for feeding. Figure [10](#page-9-1) shows the hot cracking morphology and EDS analysis. An increase in Cu elements and a decrease in Al elements were observed at the boundary of the hot crack (points A and B), as shown in Fig. [10](#page-9-1)a. This was attributed to the fact that the liquid flm consisted of Al and Cu elements at the beginning of solidifcation, and the Al elements nucleated along the  $\alpha$ -Al solid grains of the semisolid alloy as solidification progressed. The eutectic  $Al<sub>2</sub>Cu$  nucleated on the grain boundary where hot cracks occurred at the last stage of solidifcation. The EDS results of the alloys at the end of feeding, presented in Fig. [10b](#page-9-1), show that the

ratio of Al to Cu atoms was almost 2:1. This further verified the eutectic  $AI<sub>2</sub>Cu$ , implying that eutectic-rich liquid flms attempted to fll and subsequently heal the developing cracks. However, the eutectic-rich liquid flm was not successful at completely healing the hot cracks investigated in this research.

The hot cracking morphology after isothermal remelting for six soaking time at  $630 \degree C$  is shown in Fig. [11](#page-10-1). The morphology was characterized by hot cracks initiating through intergranular regions between two near  $\alpha$ -Al grains with the eutectic phase  $Al<sub>2</sub>Cu$  dispersed along or surrounding the propagation path. Crack propagation ended at the bridge between two solid  $\alpha$ -Al grains or the eutectic phase Al<sub>2</sub>Cu with sheet structure, as shown in Fig. [11](#page-10-1)a–d. The reason was



<span id="page-9-1"></span>**Fig. 10** Microstructures and EDS analysis of hot cracking



<span id="page-10-1"></span>**Fig. 11** Hot cracking morphologies after isothermal reheating treatment at 630 °C for **a** 10 min, **b** 20 min, **c** 30 min, **d** 40 min, **e** 50 min, **f** 60 min

that the thinner liquid flms experienced a larger shrinkage stress at the end of solidifcation, and although the insuffcient liquid flms attempted to fll and subsequently heal the developing tears at low cooling speeds, they were not successful at completely healing the developing cracks along grain boundaries investigated in this research, which was consistent with the results of Li et al. [\[44\]](#page-14-18) and Dou et al. [\[45](#page-14-19)]. As shown in Fig. [11e](#page-10-1) and f, the feeding capability was enhanced with the higher volume fraction of liquid flms, which is presented later. The hot cracking morphology was similar at the three remelting temperatures.

# <span id="page-10-0"></span>**4 Discussion**

# **4.1 Liquid Film Characteristics Simulation**

With the same isothermal remelting temperature, a longer soaking time was successful at helping Al–4Cu alloy liquid flms to complete feeding by enhancing the time available for feeding and reducing the hot cracking initiation temperature, thus limiting hot cracking. This likely resulted from the increased liquid fraction and the occurrence of Ostwald ripening. The variation in the liquid flm composition was directly attributed to Ostwald ripening, which also led to diferent liquid flm characteristics. Wang et al. [[46](#page-14-20)] used Phase-Field simulations to investigate liquid channel characteristics during columnar growth of single-crystal and bicrystal Al–Cu alloys. Their results showed that a high solute content easily formed hot cracks in the liquid flm at the end of solidifcation. Moreover, this study, with respect to the efect of liquid flm characteristics on hot cracking mechanisms, creates a novel analysis with quantitative calculation through MD simulations.

Stoichiometry numbers of liquid flm composition under diferent isothermal treatment conditions were extracted from Fig. [7b](#page-6-0), as listed in Table [2](#page-10-2). Based on the liquid flm composition and stoichiometry numbers, atoms were randomly distributed in the  $5 \times 5 \times 5$  cubic supercell with periodic boundary conditions.

RDF plays an important role in identifying the shortrange order structure and atomic number of melted alloys, as reported by Xiong et al. [\[47](#page-14-21)]. All RDF curves showed three peaks under diferent isothermal remelting

<span id="page-10-2"></span>**Table 2** Stoichiometry numbers of liquid flm composition under diferent isothermal treatment conditions

Time (min)	10	20	30	40	50	60
620	$\text{Al}_{81}\text{Cu}_{19}$	$\mathrm{Al}_{82}\mathrm{Cu}_{18}$	$\text{Al}_{87}\text{Cu}_{13}$	$Al_{87}Cu_{13}$	$\mathrm{Al}_{89}\mathrm{Cu}_{11}$	$\mathrm{Al}_{91}\mathrm{Cu}_{9}$
630	$Al_{84}Cu_{16}$	$\mathrm{Al}_{89}\mathrm{Cu}_{11}$	$\text{Al}_{90}\text{Cu}_{10}$	$\text{Al}_{90}\text{Cu}_{10}$	$\text{Al}_{91}\text{Cu}_9$	$\mathrm{Al}_{93}\mathrm{Cu}_{7}$
640	$Al_{88}Cu_{12}$	$\text{Al}_{89}\text{Cu}_{11}$	$\text{Al}_{90}\text{Cu}_{10}$	$\text{Al}_{90}\text{Cu}_{10}$	$\mathrm{Al}_{95}\mathrm{Cu}_{5}$	$\mathrm{Al}_{96}\mathrm{Cu}_{4}$



<span id="page-11-0"></span>**Fig. 12** RDFs of liquid flms under diferent isothermal treatment conditions for **a** 620 °C, **b** 630 °C, **c** 640 °C



<span id="page-11-1"></span>**Fig. 13** MSDs of liquid flms under diferent isothermal treatment conditions for **a** 620 °C, **b** 630 °C, **c** 640 °C

conditions, as demonstrated in Fig. [12](#page-11-0). The same phenomenon also appeared in the study of Christian et al. [\[48](#page-14-22)], indicating that the liquid flm exhibited a short-range order structure. The first peak value of  $g(r)$  represents the radius of the efective hydrodynamic particles. The horizontal axis value ranges of the first peak were 2.67–2.69 Å, 2.69–2.71 Å and 2.69–2.71 Å corresponding to the remelting temperatures of 620 °C, 630 °C and 640 °C, respectively, while the height of every peak remained unchanged, indicating the same short-range order structure and atomic number of liquid films with different characteristics. Therefore, the diference in the feeding capability of liquid flms was not related to the short-range order structure and atomic number.

Figure [13](#page-11-1) illustrates MSD vs. soaking time curves under diferent isothermal remelting conditions. The linear relationship between MSDs and time implied that the established MD models enabled liquid flms to reach thermal equilibrium for the selected temperature, as investigated by Wang et al. [\[49](#page-14-23)]. For the same temperature, the liquid flm activity in thermal equilibrium increased with a longer soaking time as the MSD increment increased. This resulted from Al-rich liquid flms.



<span id="page-11-2"></span>**Fig. 14** Viscosities of liquid flms under diferent isothermal treatment conditions

According to Figs. [12](#page-11-0) and [13](#page-11-1), the viscosities of liquid flms under diferent remelting conditions were calculated from Eqs.  $(3)$  $(3)$  $(3)$  and  $(4)$  $(4)$ , as depicted in Fig. [14.](#page-11-2) The viscosity of the liquid flms decreased with increasing temperature and time. Section [3.2](#page-6-1) indicates that viscosities of the liquid flms were 1.51 mPa·s and 1.03 mPa·s after 10 min and 60 min soaking time for the 620 °C remelting temperature, corresponding to hot cracking initiation temperatures of 593.52 °C and 569.32 °C, respectively. However, no cracks occurred at 640 °C for 60 min, and the viscosity reached a minimum value of 0.91 mPa·s. It was concluded that the viscosity was the key property for determining the occurrence of hot cracking. Generally, higher isothermal remelting temperatures and longer soaking time were successful at enhancing the feeding capacity of liquid flms by increasing the volume fraction and fuidity of liquid flms but reducing their viscosity and the hot cracking initiation temperature. The results further verifed the discussion in Sect. [3.2](#page-6-1).

# **4.2 Hot Cracking Initiation Mechanism**

According to the liquid flm shrinkage stress and hot crack morphology in Sect. [3](#page-3-3), the liquid film characteristics varied with the volume fraction and composition, as did the crystal morphology, under the same isothermal remelting temperature for diferent soaking time. The initiation mechanism of hot cracking in Al–4Cu alloys is presented later with respect to the effect of the crystal morphology and the volume fraction and properties of liquid flms.

Previous studies have revealed that the grain refined reduces the severity of hot cracking [[50](#page-14-24)[–53](#page-14-25)]. A schematic diagram of the hot cracking formation mechanism is shown in Fig. [15](#page-12-0). The liquid flm was inactive in the equilibrium state; however, it had high viscosity under the same isothermal remelting temperature for a shorter soaking time. The increased feeding resistance of liquid flms resulted from the coarse morphology of α-Al grains with a lower spherical degree after a shorter soaking time. The Al element melted in the liquid phase, nucleated and grew alongside α-Al grains during solidifcation, leading to a thinner feeding channel. Generally, the shrinkage of the liquid eutectic phase was larger than that of the solid phase at the last stage of solidifcation, and hot cracks were initiated by the shrinkage cavity and porosity with the presence of the solidifcation shrinkage force due to the insufficient feeding of liquid flms, as illustrated in Fig. [15a](#page-12-0). The same phenomenon also appeared in the studies of D 'Elia et al. [\[54](#page-14-26)] and Takai et al. [\[55\]](#page-14-27), indicating that the shrinkage cavity and porosity were one of the crack sources of hot cracks. However, the thickness of the liquid flm and spherical degree of grains increased, while the viscosity of the liquid flms decreased after a longer soaking time. Although the feeding channels gradually narrowed during solidifcation, they remained larger in the alloys compared with that after a shorter soaking time. The reason for this occurrence was the lower viscosity of liquid flms and the higher spherical degree of grains, as well as the wider feeding channels, after a longer soaking time. These factors facilitated the feeding behaviour, thereby inhibiting hot cracks by reducing, even eliminating, the shrinkage cavity and porosity, which is depicted in Fig. [15b](#page-12-0). The feeding capability of liquid flms peaked after 640 °C isothermal remelting temperature for 60 min,



<span id="page-12-0"></span>**Fig. 15** Schematic diagram of the hot cracking formation mechanism **a** feeding behaviour of thin liquid flm in the narrow feeding channel, **b** feeding behaviour of thick liquid flm in the wide feeding channel

and almost no hot cracks were observed, while no shrinkage cavity or porosity was generated.

The liquid phase shrinkage is larger than that of the solid phase, and the theoretical shrinkage ratio of solid to liquid is 1:3  $[56]$  $[56]$ . The insufficient liquid phase at the end of solidification did not effectively compensate for the shrinkage diferences between the solid and liquid phases, thus inducing the shrinkage cavity and porosity. The increased hot tearing severity resulted from the induced shrinkage cavity and porosity, which became the source for developing hot cracks. The increased volume fraction associated with the wider feeding channel enhanced the time available for feeding of the liquid phase, which in turn reduced the feeding resistance. Additionally, shrinkage was likely more accommodated by the feeding of the high fuidity and excellent feeding capability of low-viscosity liquid flms. Therefore, the reduction in hot cracking severity in the Al–4Cu alloy was attributed to the higher liquid fraction and grain spherical degree, as well as the lower viscosity of the liquid phase, which was beneficial for liquid films to eliminate the shrinkage diference between the solid and liquid phases.

# **5 Conclusions**

This study systematically investigated the relationship between the liquid flm volume at the end of solidifcation and hot cracking initiation using an MCRC apparatus. A further understanding with respect to the effect of liquid film characteristics on hot cracking initiation in Al–4Cu alloys at the end of solidifcation and the mechanism of hot cracking initiation was developed. The following conclusions can be drawn from this research.

- 1. A higher isothermal remelting temperature and longer soaking time were successful at helping Al–4Cu alloy liquid flms to complete feeding during the last stage of solidifcation by increasing both the liquid fraction and the grain spherical degree and widening the feeding channel. A higher isothermal remelting temperature and longer soaking time reduced the hot crack initiation temperature and increased the critical crack shrinkage stress, which, in turn, limited the severity of hot tearing.
- 2. Molecular dynamics simulation showed that the composition of liquid flms varied with isothermal remelting temperature and soaking time, while the shortrange ordered structure and atomic order of liquid flms remained the same. After a longer soaking time at a higher isothermal remelting temperature, the activity of the liquid flm in the equilibrium state increased; however, its viscosity reduced. The increase in liquid flm fuidity enhanced the flling capability.

3. The liquid fraction reached a maximum value of 36.68% at 640 °C for 60-min isothermal remelting corresponding to a valley value of liquid flm viscosity of 0.91 mPa·s, and almost no hot cracks occurred under this condition.

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## **Declarations**

**Conflict of interest** The authors declare that they have no known competing fnancial interests or personal relationships that could have appeared to infuence the work reported in this paper.

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