**RESEARCH PAPER**



# **Study on the estimation method for the mean stress efect on the fatigue strength of welded joints with various failure modes and joint types**

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#### **Abstract**

In compact box-shaped steel structures, partial penetration welds are frequently selected as the welding technique, and root fatigue failure might manifest in these joints. In order to ensure the structural integrity of steel structures, it is necessary to develop an assessment approach for evaluating the efficacy of post-weld heat treatment (stress relief) in enhancing the fatigue strength of root-failed welded joints. In this study, bending fatigue experiments employing stress ratios of *R*=0 and−1 have been carried out on as-welded and stress-relieved welded joint specimens. The test objects include root-failed plug weld specimens, as well as toe-failed out-of-plane gusset weld joint and T-joint specimens. The welding residual stresses near the root notch and weld toe are measured by X-ray difraction technique. The assessment of the mean stress efect on fatigue strength has been examined through the utilization of the modifed MIL-HandBook-5D equivalent stress range. The equivalent stress range is evaluated by using two fatigue assessment stresses: structural stress and elastic–plastic local stress. It has been confrmed that all fatigue test results, irrespective of the failure mode or the joint type, whether from the as-welded or stress-relieved specimens, can be closely approximated using a single S–N curve with either defnition of the equivalent stress. This outcome indicates the accomplishment of assessing the mean stress efect on the fatigue strength of welded joints with various failure modes and joint types.

**Keywords** Mean stress effect · Creep strain · Plug weld



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# **1 Introduction**

In compact enclosed compartments of box-shaped steel structures, partial penetration welds are frequently selected as the welding technique. Root fatigue failure might manifest in these joints, and employing post-weld heat treatment (stress relief (SR)) can improve the fatigue resistance of such connections. In order to ensure the structural integrity of steel structures, it is imperative to formulate a quantitative assessment approach for evaluating the efficacy of SR treatment in enhancing the fatigue strength of root-failed welded joints. In such assessments, the mean stress efect on the fatigue strength of root-failed welded joints should be clarifed. It would be of great practical value if this assessment could be performed in a uniform manner regardless of fracture type (toe failure or root failure) and joint type.

Many researchers have investigated the mean stress efect on the fatigue strength of welded joints. Baumgartner and Bruder [[1\]](#page-15-0) examined the fatigue strength of toe-failed longitudinal stifeners in as-welded and SR-treated conditions and tried to transfer the fatigue test results into a single damage parameter PSWT-N curve. Hensel [\[2](#page-15-1)] proposed to combine cyclically stabilized local residual stress with mean stress to efective mean stress and applied the fatigue design concept based on the efective mean stress to longitudinal stifeners.

Ahola et al. [\[3](#page-15-2)] and Ratfar et al. [[4\]](#page-15-3) performed fatigue analyses of welded joints with post-weld treatment by the 4R method, which is based on the cyclic behavior at the notch root accounting for local residual stress, and showed that the 4R method could improve the fatigue evaluation of weld root failure. However, no method has yet been established for evaluating mean stress efects on the fatigue strength of welded joints independent of fracture type and joint type.

The authors [\[5](#page-15-4), [6\]](#page-15-5) investigated the welding residual stress (WRS) near the root notch of plug weld (PW) specimens and carried out the fatigue tests of the as-welded (AW) and SR specimens experiencing root failure. The fndings indicated that by examining the equivalent stress range derived through the modifed MIL-Handbook-5D (MIL-HDBK-5D) method proposed by Matsuoka et al. [[7,](#page-15-6) [8](#page-15-7)], one could predict the fatigue strength of the SR specimen subjected to cyclic loadings with arbitrary stress ratio if the fatigue strength of the AW specimen is known.

Hereafter, the stress utilized in the fatigue assessment is called "fatigue assessment stress." Matsuoka's method is efective when structural hot spot stress (HSS) is chosen as the fatigue assessment stress, thereby enabling the utilization of HSS S–N diagrams for a wide range of welded joints experiencing toe failure when the HSS determination technique is established [[9\]](#page-15-8). An estimation technique for the mean stress efect on the fatigue strength of welded joints experiencing toe failure, regardless of the joint type, was established. However, in the case of joints experiencing root failure, it is essential to conduct fatigue tests on the aswelded specimen for each unique joint confguration since the methodology for estimating the fatigue strength of rootfailed joints by using HSS S–N diagrams has not been established. It is desirable to develop an estimation technique for the mean stress efect that can be applied irrespective of the fracture mode (toe and root failure) and the joint type.

In this study, the WRS measurements in the vicinity of crack initiation sites of PW, out-of-gusset weld joint (GW), and T-joint (TJ) specimens are conducted. Bending fatigue tests are performed on these specimens. The calculation of the modified MIL-HDBK5D equivalent stress range  $(\Delta \sigma_{eq})$ involves the utilization of two fatigue assessment stresses: structural stress and elastic–plastic local stress. In the former approach, HSS is employed for the toe-failed GW and TJ specimens, while the root local stress (RLS), determined by extrapolating the stress within the root gap, is employed for the root-failed PW specimen. Regarding the latter approach, the elastic–plastic local stress cycle (EPLSC), analyzed using a very fne FE mesh, is applied to both toe-failed and root-failed specimens. Based on the test results, a comprehensive evaluation is conducted to assess the effectiveness of the modifed MIL-HDBK-5D method based on structural stress in relation to root-failed PW joint. Furthermore, the validity of the modifed MIL-HDBK-5D method based on

EPLSC for joints experiencing both toe and root failures is examined.

# **2 Fatigue tests**

# <span id="page-2-2"></span>**2.1 Test specimens**

In this study, WRS measurements and bending fatigue tests are carried out on PW specimens experiencing root failure, as well as GW and TJ specimens experiencing toe failure.

Figure [1](#page-2-0) illustrates the shape and dimensions of the PW specimen. The thickness of the main plate is 16 mm, while that of the backing plate is 9 mm. The base metal is mild steel JIS: SS400, and the weld metal is JIS: YGW11. A slit is introduced at the center of the base plate and subsequently flled by MAG (100% CO2) welding, utilizing the backing plate. The welding process comprises three consecutive passes, without any inter-pass cooling duration. The mean gap between the base metal and the backing of AW specimens is approximately 1 mm, while the average radius of the root notch measures around 0.5 mm. Those gaps and radiuses are measured by photographing the cross-sections of the specimens. PW specimen exhibits the following characteristics: (1) despite the small size of the specimen, it is capable of accommodating substantial WRS; (2) it experiences root failure; (3) the WRS near the root notch can be measured by X-ray difraction (XRD) method after removing/cutting backing plate. By utilizing this specimen, one can explore the correlation between WRS and the rootfailure fatigue strength.

The shape and dimensions of the GW specimen are shown in Fig. [2](#page-2-1). The base and gusset plates are mild steel JIS: SS400 with a thickness of 16 mm. The weld metal is JIS: YGW11. The mean toe radius measures approximately 0.5 mm. This specimen shows high tensile WRS along the loading axis at the weld toe and experiences toe failure.

The shape and size of the TJ specimen are presented in Fig. [3](#page-3-0). The base and rib plates comprise a steel plate JIS: SM490A with a thickness of 19 mm. For the weld material, welding wire JIS: YGW15 is utilized. The rib is welded to the center of the base plate, measuring  $500 \text{ mm} \times 400 \text{ mm}$ , through the employment of MAG welding with Ar-20% CO2 gas. Subsequently, the specimens are extracted from that joint via electrical discharge machining. The mean toe radius measures approximately 0.5 mm. This specimen experiences toe failure in fatigue tests.

The mechanical properties and the chemical components of the base and welding materials are presented in Table [1](#page-4-0), and the welding conditions are outlined in Table [2.](#page-5-0) The mechanical properties of base and filler metals are measured by cutting a specimen from the base



<span id="page-2-0"></span>**Fig. 1** Plug weld (PW) specimen

<span id="page-2-1"></span>**Fig. 2** Out-of-plane gusset weld (GW) specimen

#### <span id="page-3-0"></span>**Fig. 3** T-joint (TJ) specimen



plate and weld bead of the welded joints. Alongside the as-welded (AW) specimens, stress-relieved (SR) specimens were fabricated for PW, GW, and TJ specimens, employing holding temperatures ranging from 500 to 600 °C, accompanied by holding durations of 1.5 h. Henceforth, the identifiers SR500, SR550, and SR600 are employed to refer to the SR specimen subjected to a holding temperature of 500, 550, and 600 °C.

#### <span id="page-3-1"></span>**2.2 WRS measurement**

Regarding each specimen prepared in Section [2.1,](#page-2-2) the WRS in the proximity of the root notch in the PW specimen, as well as that in the vicinity of the weld toe in both the GW and TJ specimens, are measured utilizing X-ray diffraction (XRD) method [[10–](#page-15-9)[12\]](#page-15-10). This measurement is conducted for both the as-welded (AW) and stressrelieved (SR) specimens.

XRD measurements are performed based on the cosα method [[13](#page-15-11)–[15](#page-15-12)] using Pulstec µ-X360s. The collimator diameter is 1 mm. The X-ray irradiation range is about 3 mm, and the distance from the toe or root notch to the nearest measurement point is 1.5 mm. The surfaces of the measurement region are smoothed by electropolishing to a metallic luster to avoid the effects of oxide scale and surface roughness.

As the weld root of the PW specimen is concealed by the backing plate, direct assessment of the WRS is unfeasible. Consequently, the overhanging section of the backing plate is removed via electrical discharge machining, as depicted in Fig. [4](#page-5-1). The presence or absence of the excised portion minimally affects the rigidity of the region adjacent to the root notch, and the impact on WRS caused by the excision is negligible [[1](#page-15-0), [2\]](#page-15-1).

#### **2.3 Fatigue tests**

In order to investigate the correlation between the WRS in the region near the root notch or the weld toe, and the fatigue strength of specimens under as-welded (AW) and stress-relieved (SR) conditions, a series of four-point bending fatigue tests are conducted. The bending fatigue tests are preferred due to the ease of controlling the local mean stress, even in the presence of welding distortion. For the cyclic loading, a Shimadzu Servo Pulser hydraulic fatigue testing machine with a capacity of 50 kN is employed. The specimen is supported by two pins at both ends, positioned at intervals of 350 mm, while two additional pins are used to drive upwards and downwards at intervals of 150 mm within the end pins, as depicted in Fig. [5](#page-5-2). A constant amplitude fully reversed sinusoidal load with stress ratio (*R*) of−1 and 0 is applied at a frequency of 8 Hz.

JSSC fatigue design guideline [[16](#page-15-13)] stipulates that the nominal stress range Δσused in fatigue assessment is calculated as  $\Delta \sigma = \Delta \sigma_m + \gamma \Delta \sigma_b$  regardless of joint type, where  $\Delta\sigma_m$  and  $\Delta\sigma_b$  are membrane and bending components of the nominal stress range. The correction factor for the bending component,  $\gamma$ , is given to be 0.8 in the guideline. The validity of this correction under the specifed test conditions  $(R = -1$  and 0) is confirmed by Araki et al. [[17\]](#page-15-14).

#### <span id="page-3-2"></span>**2.4 Thermal elastic–plastic FE analysis (TEPFEA)**

The WRS in both PW and GW specimens is examined through the utilization of thermal elastic–plastic fnite element analysis (TEPFEA). The TEPFEA is carried out employing JWRIAN-ISM, an implicit TEPFEA code based on the iterative sub-structuring method developed by Murakawa et al. [[18](#page-15-15), [19\]](#page-15-16). The fnite element (FE) meshes employed for the analysis are illustrated in Figs. [6](#page-6-0) and [7.](#page-6-1)



<span id="page-4-0"></span>**Table 1** Mechanical properties and chemical components of specimens

<span id="page-5-0"></span>**Table 2** Welding conditions of specimens

Bead	Current $(A)$	Voltage $(V)$	Welding speed (cpm)
1st pass	300	28	45
2nd pass	350	34	30
3rd pass	400	38	30
Fillet	250	28	30
Fillet	350	35	35

The shape of the weld bead is determined based on macroscopic observations. In the case of the PW specimen, a 1-mm gap is set between the base metal and the backing plate, while the radius of the root notch is set to 0.5 mm, as per the measurements. As for the GW specimen, the radius of the weld toe is also set to 0.5 mm, based on measurements. The minimum element edge length in the vicinity of the root notch or weld toe is set at 0.15 mm. This specifc length is determined through the mesh sensitivity

<span id="page-5-1"></span>**Fig. 4** WRS measurement method near the root notch analysis conducted by the authors [[20\]](#page-15-17). In the welding and SR treatment analyses, rigid motion suppression boundary conditions are applied to the FE models.

Because many researchers (e.g.,  $[21-23]$  $[21-23]$  $[21-23]$  $[21-23]$  $[21-23]$ ) have successfully implemented the assumption of elastic perfectly plastic material model in the WRS analysis, a bilinear hardening material model with Von Mises yielding criteria and small tangent modulus is adopted in this study. Bhatti et al. [[24](#page-16-0)] investigated the infuence of thermo-mechanical material properties of diferent steel grades (S355–S960) on WRS in T-fllet joints. They concluded that the temperature dependence of yield stress has the most decisive infuence on the accuracy of WRS calculations. Murakawa et al. [[18,](#page-15-15) [19\]](#page-15-16) optimized the temperature dependence of material properties so that the calculated AW WRS agreed with those measured for steel materials nearly identical to those used in this study.

From the above discussion, the material parameters for TEPFEA are determined by the following procedure: the





# <span id="page-5-2"></span>**Fig. 5** Fatigue testing setup

<span id="page-6-0"></span>

<span id="page-6-1"></span>

<span id="page-6-2"></span>**Fig. 8** Temperature dependence of yield strength

25  $= 5.7 \times 10^{-6}$  : temperature independent  $\times$  10 GPa)  $c \times 10^2$  J/kg/°C 20 Physical constants Physical constants  $-6$   $^{\circ}$ C $-1$ ) 15 10  $10^3 \text{ kg/m}^3$ 5  $\lambda$  ( $\times$ 10 J/m/s/°C) 0 0 500 1,000 1,500 Temperature, *T* (℃)

<span id="page-6-3"></span>**Fig. 9** Temperature dependence of physical constants

mechanical properties at room temperature are determined based on measurements conducted at room temperature (Table  $1(a)$  $1(a)$ ); the ratio of properties at room temperature to those at elevated temperature is approximated to be the same as that those in Refs. [[18](#page-15-15), [19](#page-15-16)]; following Refs. [[18](#page-15-15), [19](#page-15-16)], the hardening coefficient *h* is set to 1/1000 of Young's modulus.

The yield stresses  $(\sigma^Y)$  of the materials used for the PW and GW specimens are assigned temperature dependency, as illustrated in Fig. [8.](#page-6-2) The temperature dependencies of specific heat  $(c)$ , Young's modulus  $(E)$ , coefficient of thermal expansion ( $\alpha$ ), convective heat transfer coefficient ( $\beta$ ), thermal conductivity ( $\lambda$ ), Poisson's ratio ( $\nu$ ), and density ( $\rho$ ) are also considered as shown in Fig. [9.](#page-6-3)

The shapes of the fller metal regions in the FE model are determined to match the measured cross-sectional shape of the weld layer. The welding heat is applied as a moving heat source, which follows the trajectory of the welding torch. The amount of heat is determined through calculations based on the welding current, voltage, and torch speed, as provided in Table [2.](#page-5-0) The distribution of heat input is approximated by a rotating ellipsoid, where the radii difer before and after the heat source. The dimensions of the heat source and the heat input efficiency  $(\eta)$  are adjusted in order to achieve agreement between the calculated weld penetration shape and the measured ones. These adjusted parameters are documented in Table [3.](#page-7-0) As shown in Fig. [10](#page-7-1)a, the temperature histories in PW specimens are measured by K-type thermocouples with a wire diameter of 0.65 mm at four points (TC-1~4). An example of the comparison between the calculated and measured thermal cycles of a PW specimen is depicted in Fig. [10a](#page-7-1).

**Table 3** Welding heat input

<span id="page-7-0"></span>

<b>Table 3</b> Welding heat input parameters	Specimen	Bead	Heat source length (mm)	(mm)	Heat source width Heat source depth Heat input (mm)	efficiency $\eta$
	PW	1st pass	20	12		0.9
		2nd pass	35	14	10	0.9
		3rd pass	35	16	15	0.9
	GW	Fillet	20	13	b	0.9

<span id="page-7-1"></span>**Fig. 10** Thermal cycles in PW specimen during the welding process



(a) The arrangement of temperature measurement points for PW specimen



(b) Comparison of measured and calculated temperature histories

In the case of PW specimens, creep deformation is incorporated into the TEPFEA. This is due to the relatively low heat capacity of these specimens and the sustained high temperatures of 400 °C or higher in the vicinity of the weld for an extended duration. The Norton-Bailey model [\[25\]](#page-16-1) is employed to simulate the creep deformation, and the corresponding creep strain  $(\varepsilon^C)$  is calculated using Eq. ([1\)](#page-7-2).

$$
\varepsilon^{C} = C_{0} (\sigma_{VM})^{C_{1}} t^{C_{2}} \exp\left(-\frac{C_{T}}{\Theta}\right)
$$
  
\n
$$
C_{1} > 1, \ 0 \le C_{2} \le 1.0, \ \ ; \ \Theta = 273.15 + T
$$
\n(1)

where  $\sigma_{VM}$  is the von Mises stress (in MPa), *t* denotes time (in seconds), *T* signifes temperature (in degrees Celsius), and  $C_0$ ,  $C_1$ ,  $C_2$ , and  $C_T$  are the material properties associated with creep. Those properties, obtained from the references [\[5](#page-15-4)], are presented in Table [4](#page-7-3).

<span id="page-7-3"></span>

Conversely, creep is not taken into consideration for GW specimens since the elevated temperature exceeding 400 °C is of short duration.

# <span id="page-7-2"></span>**3 Experimental and analysis results**

#### **3.1 Fatigue test results**

The visual representation, fracture surface, and trajectory of fatigue crack propagation in the PW specimens are depicted in Fig. [11](#page-8-0). Likewise, Figs. [12](#page-8-1) and [13](#page-8-2) illustrate those of the GW and TJ specimens, respectively. The measurement locations for WRS in the PW and GW specimens, as detailed in Section [2.2](#page-3-1), align with the points of crack initiation. The correlation between the nominal stress range Δ*σ* and the failure life  $N_f$  is presented in Fig. [14.](#page-9-0)

The fatigue lives of the SR600 data exhibit approximately 3.5 times greater longevity than the AW data in the PW specimens and about 2.5 times greater longevity in the GW specimens, signifying an enhancement of approximately two and one classifcation grades, respectively, within the JSSC fatigue strength grade A–D. The fatigue strength at  $2 \times 10^6$ cycles (FAT value) for JSSC grade A–D is 190, 155, 125, and 100 MPa.

The test data for PW specimens with  $R=0$  is depicted using solid circle markers for AW and solid square markers for SR600. In these instances, the increment in fatigue strength resulting from SR in comparison to AW is marginal. The test data for TJ specimens with  $R = -1$  is illustrated with open diamond markers for AW and solid diamond

<span id="page-8-0"></span>**Fig. 11** PW specimen after fatigue test (**a** appearance, **b** fracture surface, **c** crack propagation path)



**Fig. 12** GW specimen after fatigue test (**a** appearance, **b** fracture surface, **c** crack propagation path)

<span id="page-8-2"></span>**Fig. 13** TJ specimen after fatigue test (**a** appearance, **b** fracture surface, **c** crack propa-

gation path)

<span id="page-8-1"></span>







markers for SR600. The fatigue strength of both cases is comparable.

# **3.2 WRS at crack initiation sites**

# **3.2.1 Root notch in PW specimens**

The X-coordinates presented in Fig. [4](#page-5-1) are utilized in the subsequent analysis. Consider *d* as the distance measured along the *X*-axis from the root notch, and let  $\sigma^{(r)}$  denote the normal component of WRS in the X-direction. The region where *d* is less than 8 mm corresponds to the interior of the root gap. Within the AW specimen, the  $\sigma^{(r)}$ <sub>x</sub> in the root gap exhibits tensile characteristics, ranging from approximately 80 to 200 MPa. Figure [15](#page-9-1) shows  $\sigma^{(r)}$  for the SR500 and SR600 specimens, where *N* is the number of test specimens with the same conditions. In this measurement, multiple specimens  $(N=2 \text{ or } 3)$  are prepared for each SR condition. WRS is measured in all specimens, and they are plotted in Fig. [15.](#page-9-1) The signifcant variation in WRS measurements is caused by a combination of individual diferences in the specimens and uncertainties in the XRD measurements. In this figure, the tensile  $\sigma^{(r)}$ <sub>x</sub> induced in AW specimens decreases through SR at a temperature of 500 °C for a duration of 1.5 h. Furthermore, it is observed that SR at a temperature of 600 °C for 1.5 h leads to complete relaxation of the stress  $(<50$  MPa). This decrease in the WRS is considered to be accountable for the enhanced root failure fatigue strength of the SR600 specimens.

# **3.2.2 Weld toe in GW and TJ specimens**

In this subsection, *d* signifes the distance measured along the *X*-axis from the weld toe. Figure [16](#page-10-0) exhibits the relation between  $\sigma^{(r)}$ <sub>x</sub> and *d* for six AW GW specimens.  $\sigma^{(r)}$ <sub>x</sub> is

Welding in the World



<span id="page-9-1"></span>**Fig. 15** Relation between WRS's X-component  $\sigma^{(r)}$ <sub>x</sub> and distance from the root notch *d* of PW specimens

tensile near the weld toe in AW specimens, with an average value of approximately 320 MPa at  $d=1.5$  mm.  $\sigma^{(r)}$ <sub>x</sub> for SR550 (six specimens) and SR600 (three specimens) cases are also plotted in this fgure. It is shown that the tensile  $\sigma^{(r)}$ <sub>x</sub> generated in AW specimens is reduced by 550  $°C$ , 1.5 h of SR, and completely relaxed (<50 MPa) by 600 °C, 1.5 h of SR. Similar to Fig.  $15$ , multiple specimens  $(N=3 \text{ to } 6)$  are prepared for each SR condition, and WRS is measured in all specimens. The signifcant variation in WRS measurements in Fig. [16](#page-10-0) is caused by a combination of individual diferences in the specimens and uncertainties in the XRD measurements.

 $\sigma^{(r)}$ <sub>x</sub> is measured at *d* = 1.5 mm along the center line of the base metal.  $\sigma^{(r)}$ <sub>x</sub> in SR600 specimens approaches insignifcance, and the disparity in WRS pre- and post-SR is negligible. The fatigue strength of AW specimens and SR600 specimens exhibit no discernible distinction.



Number of cycle to failure,  $N_f$  (cycle)

<span id="page-9-0"></span>**Fig. 14** Fatigue test results of PW, GW, and TJ specimens



<span id="page-10-0"></span>**Fig. 16** Relation between WRS's X-component  $\sigma^{(r)}$  and distance from the toe *d* of GW specimens

# <span id="page-10-3"></span>**4 Mean stress efect evaluation by hot spot stress**

Matsuoka et al. [\[7](#page-15-6)[–9](#page-15-8)] conducted an assessment of the fatigue life of weld joints that failed at the weld toe, employing the MIL-HDBK-5D method [\[18\]](#page-15-15), which incorporates the infuence of mean stress resulting from WRS. Within this methodology, the fatigue capacity is appraised using hot spot stress (HSS)-based equivalent stress range Δ*σ*eq calculated by Eq.  $(2)$  $(2)$ ,

$$
\Delta \sigma_{eq} = (\Delta \sigma)^{\alpha} \left( \frac{\Delta \sigma}{2} + \sigma_{const} + \sigma_{res} \right)^{1-\alpha}; \ \alpha = 0.6485 \tag{2}
$$

where  $\Delta \sigma$  is HSS range,  $\sigma_{\text{const}}$  is the mean stresses excluding WRS, and  $\sigma_{res}$  is the WRS near the hot spot. This formula was originally proposed in US Military Standard [[26\]](#page-16-2), and  $\alpha$  is determined by the experiments [[7,](#page-15-6) [8\]](#page-15-7).

The localized maximum and minimum stresses, accounting for both mean stress and WRS, can be computed utiliz-ing Eq. ([2\)](#page-10-1). Let  $\overline{\sigma}_{\text{max}}$  and  $\overline{\sigma}_{\text{min}}$  be the maximum and minimum in a stress cycle. In the event that the absolute value of either  $\overline{\sigma}_{\text{max}}$  or  $\overline{\sigma}_{\text{min}}$  surpasses the yield stress  $\sigma^Y$ , the WRS  $\sigma_{\text{res}}$  is updated to  $\sigma_{\text{res}}^*$  given by Eq. [\(3](#page-10-2)).

$$
\sigma_{res}^{*} = \begin{cases}\n\sigma^{Y} - \left(\sigma_{const} + \frac{\Delta\sigma}{2}\right) & (\overline{\sigma}_{\text{max}} > \sigma^{Y}) \\
\sigma_{res} & (otherwise) \\
-\sigma^{Y} - \left(\sigma_{const} - \frac{\Delta\sigma}{2}\right) \overline{\sigma}_{\text{min}} < -\sigma^{Y}\n\end{cases}
$$
\n(3)

Subsequently, we proceed to examine the equivalent stress range given by Eq. ([2](#page-10-1)) to approximate the fatigue test results through the utilization of a unifed S–N diagram encompassing various joint confgurations and failure modes (namely, root failure and toe failure). Equation  $(3)$  $(3)$  $(3)$  is derived by approximating that the material is elastic-fully plastic material. Matsuoka et al. [[7,](#page-15-6) [8\]](#page-15-7) showed experimentally that even with this simplification, the equivalent stresses in Eq. ([2](#page-10-1)) can be used to accurately estimate the mean stress efect on the fatigue strength of welded joints subject to variable amplitude loadings. In Eq. [\(3\)](#page-10-2), the external stress is evaluated by HSS. Since the WRS is an elastic–plastic stress feld and no elastic stress singularity occurs. Therefore, the stress concentrations of HSS and local WRS are comparable, and it is acceptable to use them together.

*σ*res is derived from the XRD data obtained in the vicinity of the root notch or the weld toe. The HSS of the GW and TJ samples is determined using the elastic FEA and the IIW's 0.4h-1.0h two-point extrapolation technique [\[27](#page-16-3)]. The HSS of the TJ specimen exhibits a nearly identical value to the nominal stress.

For a PW specimen, an examination is conducted on the stress distribution along the central axis of the base metal in the vicinity of the root notch using elastic FEA. The FEA results reveal that the principal direction coincides with the *X*-axis, which is the loading direction. The stress component  $\sigma_x$  exhibits an elastic singularity at  $d=0$ , gradually decreasing and converging towards the nominal stress as *d* increases. The relationship between *d* and  $\sigma_{\rm x}$ , as determined through calculations, is depicted in Fig. [17](#page-11-0).

<span id="page-10-1"></span>This stress distribution bears resemblance to that observed near the gusset end of a GW specimen. Consequently, in the context of the structural stress approach, the "root local stress (RLS)" is adopted as the fatigue evaluation stress. RLS is determined by IIW's 0.4h-1.0h two-point extrapolation method [[27\]](#page-16-3), which involves extrapolating the back face stress of the base metal to the root notch.

When calculating the  $\Delta\sigma_{\text{eq}}$ , the values of  $\Delta\sigma$  and  $\sigma_{\text{const}}$ are obtained through the computation of HSS or RLS. These values are then multiplied by the bending correction factor  $γ=0.8$ . The resulting  $Δσ<sub>eq</sub>$  is presented in Table [5.](#page-12-0)

Figure [18](#page-13-0) depicts the correlation between the structural stress-based  $\Delta \sigma_{\text{eq}}$  and  $N_f$ . It is noteworthy that the AW fatigue test results with  $R = -1$  for various specimen types, characterized by diferent joint geometries and failure modes (root failure and toe failure), can be efectively represented by a unifed S–N diagram. This indicates the validity of the IIW's extrapolation method for GW and TJ specimens, enabling the estimation of fatigue life for PW specimens experiencing root failure through the utilization of root local stress (RLS) and the HSS S–N diagram.

<span id="page-10-2"></span>Figure [18](#page-13-0) additionally illustrates the fatigue test results of SR specimens, featuring a stress ratio of  $R = -1$ , as well as those of PW specimens in AW and SR conditions with  $R=0$ . Remarkably, all test results can be efectively approximated using the same S–N diagram employed for  $R = -1$ .



<span id="page-11-0"></span>**Fig. 17** Stress X-component  $\sigma_x$  near the root notch of PW specimen by the external load

This indicates that irrespective of variations in joint geometry and failure modes (root failure or toe failure), the MIL-HDBK-5D method is capable of quantitatively assessing the infuence of mean stress caused by alterations in stress ratio (*R*) and/or WRS under the conditions chosen.

The results show that the mean stress effect due to the WRS relaxation caused by SR can be quantitatively evaluated.

Figures [16](#page-10-0) and [17](#page-11-0) demonstrate that the WRS near the root notch (for PW specimens) and the weld toe (for GW specimens) in the AW state can be reliably approximated by TEPFEA. By substituting these estimations of  $\sigma_{\text{res}}$  into Eqs. [\(2](#page-10-1)) and [\(3](#page-10-2)), the impact of mean stress can be evaluated without the need for XRD measurements. The mean value of WRS for the same SR condition is listed in Table 5, and it is used as  $\sigma_{\text{res}}$  in Eq. ([2\)](#page-10-1).

In the case of SR specimens, if the alteration in WRS caused by SR treatment can be precisely estimated by TEP-FEA, taking into account creep phenomena, the infuence of mean stress resulting from the SR treatment can be exclusively assessed through numerical simulation. This methodology proves especially advantageous for root-failed welded joints, where direct measurement of WRS poses challenges. To accomplish such an analysis, it is imperative to ascertain the creep characteristics that can replicate the creep deformations occurring during the SR process.

# **5 Mean stress efect evaluation by local elastic–plastic stress cycle**

In Section [4](#page-10-3), it is exemplified that the mean stress effect arising from variations in stress ratio and/or WRS can be assessed using the MIL-HDBK-5D equivalent stress range, relying on structural stress (HSS or RLS), irrespective of disparities in joint geometry and failure modes. Nevertheless, it is postulated that the fatigue test data cannot be approximated by the integrated S–N diagram depicted in Fig. [18](#page-13-0) when the toe profle is modifed through grinding or HFMI treatment.

In the PW specimen, the structural stress (RLS) can be determined. It is deemed that this accounts for the capability to approximate the root-failed PW specimen's test result through the HSS S–N diagram. Nevertheless, in the majority of root-failed joints, the stress distribution near the root notch deviates considerably from that observed near the weld toe, where the validity of IIW's two-point extrapolation method prevails. In such instances, the evaluation of root-failed fatigue strength becomes unattainable through the HSS S–N diagram. The regressed S–N curve with a slope of 4.049 is plotted in this figure. The Stdv of  $log(N_f)$ is fairly small at 0.033.

Let "elastic–plastic local stress cycle (EPLSC)" denote the localized stress cycle at the crack initiation site, specifcally the weld toe or root notch. This cycle is determined by employing a fne FE mesh that accurately replicates the local profle of either the weld toe or the root notch. The calculation of EPLSC involves welding TEPFEA, followed by a cyclic elastic–plastic FE analysis (EPFEA). In this analysis, the WRS in the AW condition and its relaxation during fatigue loading are thoroughly investigated. The analysis of EPLSC can be applied to any root-failed welded joint with arbitrary root geometry. It is anticipated that the fatigue test results can be approximated using a unifed S–N diagram, regardless of joint geometry and failure mode, by evaluating the MIL-HDBK-5D equivalent stress  $\Delta\sigma_{\rm eq}$  derived from the EPLSC. This fatigue assessment approach is referred to as the "EPLSC method."

In the EPLSC method, the mesh sensitivity of the local stress converges at a relatively coarse mesh size due to the occurrence of plastic deformation and the elimination of elastic stress singularity. Consequently, the EPLSC method obviates the necessity of incorporating artifcial notch geometries, as is required by the efective notch stress (ENS) approach [[28\]](#page-16-4).

In this chapter, the determination of  $\Delta\sigma_{\text{eq}}$  using the EPLSC method is carried out for both PW and GW specimens, followed by an examination of the relationship between  $\Delta \sigma_{\text{eq}}$  and  $N_f$ . The FE mesh presented in Figs. [6](#page-6-0) and [7](#page-6-1), as employed in the TEPFEA outlined in Section [2.4,](#page-3-2) serves as the model for the cyclic EPFEA. The minimum element edge length is 0.15 mm. The mesh sensitivity of EPLSC converges at this particular mesh size, under the conditions chosen. The cyclic loading analysis is conducted as a restart analysis from the AW condition, wherein a constant amplitude four-point bending load is applied, with a nominal stress range  $\Delta\sigma$  and a stress ratio

# <span id="page-12-0"></span>**Table 5** Fatigue test results and stress assessment methods





<span id="page-13-0"></span>**Fig. 18** The relation between failure lives  $N_f$  and modified MIL-HDBK-5D equivalent stress ranges  $\Delta\sigma_{\text{eq}}$  for cases with various specimens and WRS

of  $R = 0$ . In these scenarios, the maximum nominal stress experienced,  $\sigma_{\text{max}}$ , is given by  $\sigma_{\text{max}} = \Delta \sigma$ . The number of loading cycles is three.

Figure [19](#page-13-1) illustrates the computed EPLSC, specifically referring to the local stress in the x-direction  $(\overline{\sigma}_r)$ , at the point of crack initiation (the root notch for PW specimens, weld toe for GW specimens). Subsequently, Fig. [20](#page-14-0) depicts the distributions of  $\overline{\sigma}_r$  at two distinct instances: the as-welded (AW) condition and the end of the initial load cycle, both in proximity to the crack initiation sites.

In Fig. [19,](#page-13-1) the relaxation of the WRS takes place during the initial loading cycle, leading to an alteration in the WRS distribution as depicted in Fig. [20](#page-14-0). However, this alteration almost converges after the second cycle.

Based on these findings, the EPLSC is evaluated from the time history of  $\overline{\sigma}_x$  in the third cycle for each loading condition.

The EPLSC is determined for each loading condition of the fatigue tests conducted on the PW and GW specimens, employing the aforementioned procedure. For each condition, the equivalent stress ( $\Delta \sigma_{eq}$ ) is computed from the maximum and minimum  $\overline{\sigma}_r$  observed in the EPLSC, utilizing Eq. ([4\)](#page-13-2). The utilization of the bending correction factor γ mentioned in Section [4](#page-10-3) is not employed since the change in the stress gradient in the direction of thickness, as a result of bending loading, is inherently considered in the EPFEA with a very fne FE mesh.

<span id="page-13-2"></span>
$$
\Delta \sigma_{eq} = \left(\Delta \overline{\sigma}_x\right)^{\alpha} \left(\overline{\sigma}_{x,\text{max}}\right)^{1-\alpha}; \Delta \overline{\sigma}_x = \overline{\sigma}_{x,\text{max}} - \overline{\sigma}_{x,\text{min}}, \alpha = 0.6485
$$
\n(4)

where,  $\overline{\sigma}_{x,\text{max}}$  and  $\overline{\sigma}_{x,\text{min}}$  are the maximum and minimum  $\overline{\sigma}_{x}$ in a stress cycle. The difference in equivalent stress ( $\Delta \sigma_{eq}$ ) calculated using Eq. [\(4](#page-13-2)) from the EPLSC in the AW fatigue tests of the PW and GW specimens is presented in Table 5. The correlation between  $\Delta \sigma_{\text{eq}}$  and  $N_{\text{f}}$  is depicted in Fig. [21.](#page-14-1) The regressed S–N curve with a slope of 5.917 is plotted in this figure. The Stdv of  $log(N_f)$  is fairly small at 0.020. Remarkably, irrespective of variations in joint geometry, failure modes, stress ratio (*R*), and the WRS employed, the relationship between  $\Delta \sigma_{\text{eq}}$  and  $N_{\text{f}}$  can be approximated by a single S–N diagram, analogous to Fig. [18](#page-13-0). This outcome demonstrates the validity of the EPLSC-based mean stress efect evaluation for the AW specimens with diferences in joint geometry and failure modes under the conditions chosen.

Once the creep characteristics of the material are established, it becomes feasible to assess the impact of stress relief (SR) on the enhancement of fatigue strength



<span id="page-13-1"></span>Fig. 19 The calculated time histories of  $\bar{\sigma}_x$  at the root notch of the PW specimen and that at the weld toe of the GW specimen subject to the cyclic loadings with the load amplitude of  $\Delta P_{\text{max}}$  ( $R = -1$ )

<span id="page-14-0"></span>**Fig. 20** The distributions of  $\vec{\sigma}_r$  near the root notch the PW specimen and that near the weld toe of the GW specimen in AW condition and at the end of the 1st loading cycle  $(R = -1; \text{unit},$ MPa)



i) AW ii) The end of the 1<sup>st</sup> cycle





<span id="page-14-1"></span>**Fig. 21** The relation between failure lives  $N_f$  and modified MIL-HDBK-5D equivalent stress ranges Δ*σ*eq estimated from the calculated elastic–plastic local stress cycles

through the EPLSC method. Moreover, the application of the EPLSC method can be extended to evaluate the fatigue strength improvement resulting from variations in the toe profle and the compressive WRS induced by high-frequency mechanical impact (HFMI). The comprehensive validation of these analyses will be the focal point of future investigations.

# **6 Conclusions**

The measurement of the welding residual stress (WRS) in the vicinity of crack initiation sites of specimens with different types of joints, such as plug weld (PW), out-of-gusset weld (GW), and T-joint (TJ) specimens, is conducted. Bending fatigue tests are performed on these joint specimens. The calculation of the modifed MIL-HDBK5D equivalent stress range ( $\Delta \sigma_{\text{eq}}$ ) involves the utilization of two fatigue assessment stresses: structural stress and elastic–plastic local stress. In the former approach, the structural hot spot stress (HSS) is employed for the toe-failed GW and TJ specimens, while the root local stress (RLS), determined by extrapolating the stress within the root gap, is employed for the root-failed PW specimen. Regarding the latter approach, the elastic–plastic local stress cycle (EPLSC), analyzed using a very fne FE mesh, is applied to both toe-failed and rootfailed specimens. Based on the test results, a comprehensive evaluation is conducted to assess the efectiveness of the modifed MIL-HDBK-5D method based on structural stress in relation to root-failed PW joint. Furthermore, the validity of the modifed MIL-HDBK-5D method based on EPLSC for various joints experiencing both toe and root failures is examined.

The fndings of this study can be summarized as follows:

- (1) Under the conditions chosen, all fatigue test results can be approximated by a unifed S–N diagram regardless of the joint type, failure mode, and stress ratio when the fatigue assessment stress is evaluated by the  $\Delta\sigma_{\rm eq}$  based on structural HSS (for toe-failed joints) or RLS (for rootfailed joints). The Stdv of  $log(N_f)$  is fairly small at 0.033.
- (2) Under the conditions chosen, fatigue test results of PW and GW specimens in AW condition with a stress ratio of *R*≤0 can be approximated by a unifed S–N diagram regardless of the joint type, failure mode, and stress ratio *R*≤0 when the fatigue assessment stress is evaluated by the  $\Delta\sigma_{\text{eq}}$  based on EPLSC. The Stdv of  $log(N_f)$  is fairly small at 0.020.

The aforementioned fndings indicate that the modifed MIL-HDBK-5D methodology can accomplish an assessment of the infuence of mean stress on weld fatigue, regardless of the geometry of the joint and the mode of failure.

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**Data availability** The data that support the fndings of this study are available from the corresponding author, N.O., upon reasonable request.

#### **Declarations**

**Conflict of interest** The authors declare no competing interests.

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