

# **Exclusive photo‑ and electroproduction of vector mesons of protons**

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#### **Abstract**

We review the recent progress in the exclusive photo- and electroproduction of vector mesons off protons. The key experimental results from the CLAS, GlueX, and LEPS Collaborations are shown and compared with the theoretical calculations.

**Keywords** Photoproduction · Electroproduction · Efective Lagrangians · Regge model · GPD model

### **1 Introduction**

Exclusive photoproduction of vector mesons provides substantial contributions to the spectroscopy of hadrons. For example, the photoproduction of strange vector mesons is valuable to gain a deep understanding of baryon resonances [[1\]](#page-6-0) and to search for the missing resonances which are predicted by a quark model but not observed yet experi-mentally [\[2](#page-6-1)]. An effective Lagrangian approach and a Regge model [[3–](#page-6-2)[8\]](#page-6-3) are widely used to describe the available data (e.g., CLAS [\[9](#page-6-4)[–12\]](#page-6-5), CBELSA/TAPS [[13\]](#page-6-6), and LEPS [[14\]](#page-6-7) Collaborations) for the reactions  $\gamma p \to K^* \Lambda$  and  $\gamma p \to K^* \Sigma$ . The cross-sections of these reactions are not much suppressed relative to those of kaon photoproduction [[15](#page-6-8)[–19](#page-6-9)], indicating that  $K^*$  channel is essential in the coupled-channel analyses for the study of baryon resonances.

The diffractive scattering processes  $\gamma p \rightarrow Vp$ , where V  $= (\rho^0 \, [20, 21], \omega \, [22-24], \phi \, [25-30], J/\psi \, [31, 32]), \text{ also}$  $= (\rho^0 \, [20, 21], \omega \, [22-24], \phi \, [25-30], J/\psi \, [31, 32]), \text{ also}$  $= (\rho^0 \, [20, 21], \omega \, [22-24], \phi \, [25-30], J/\psi \, [31, 32]), \text{ also}$  $= (\rho^0 \, [20, 21], \omega \, [22-24], \phi \, [25-30], J/\psi \, [31, 32]), \text{ also}$  $= (\rho^0 \, [20, 21], \omega \, [22-24], \phi \, [25-30], J/\psi \, [31, 32]), \text{ also}$  $= (\rho^0 \, [20, 21], \omega \, [22-24], \phi \, [25-30], J/\psi \, [31, 32]), \text{ also}$  $= (\rho^0 \, [20, 21], \omega \, [22-24], \phi \, [25-30], J/\psi \, [31, 32]), \text{ also}$  $= (\rho^0 \, [20, 21], \omega \, [22-24], \phi \, [25-30], J/\psi \, [31, 32]), \text{ also}$  $= (\rho^0 \, [20, 21], \omega \, [22-24], \phi \, [25-30], J/\psi \, [31, 32]), \text{ also}$  $= (\rho^0 \, [20, 21], \omega \, [22-24], \phi \, [25-30], J/\psi \, [31, 32]), \text{ also}$  $= (\rho^0 \, [20, 21], \omega \, [22-24], \phi \, [25-30], J/\psi \, [31, 32]), \text{ also}$  $= (\rho^0 \, [20, 21], \omega \, [22-24], \phi \, [25-30], J/\psi \, [31, 32]), \text{ also}$  $= (\rho^0 \, [20, 21], \omega \, [22-24], \phi \, [25-30], J/\psi \, [31, 32]), \text{ also}$  $= (\rho^0 \, [20, 21], \omega \, [22-24], \phi \, [25-30], J/\psi \, [31, 32]), \text{ also}$  $= (\rho^0 \, [20, 21], \omega \, [22-24], \phi \, [25-30], J/\psi \, [31, 32]), \text{ also}$ have their own interest. They are governed by Pomeron exchange at high energies [\[33](#page-6-18)]. The gradually rising crosssection with the center-of-mass (c.m.) photon energy *W* is described by Pomeron exchange. Additional ingredients such as meson exchange in the *t* channel and *N*<sup>∗</sup> exchange in the *s* channel are necessary to account for the low energy data and a relevant theory capable of identifying *N*<sup>∗</sup> resonances and extracting the corresponding resonance parameters is called for. Note that, in case of  $\phi$  and  $J/\psi$  photoproduction,

because of the Okubo–Zwieg–Iizuka (OZI) rule [[34–](#page-6-19)[36](#page-7-0)], meson or  $N$ <sup>∗</sup> exchanges are highly suppressed relative to those of  $\rho^0$  and  $\omega$  photoproduction.

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Signal of the European of the E Exclusive electroproduction of  $\rho^0$  [\[37](#page-7-1)[–40\]](#page-7-2),  $\omega$  [\[41](#page-7-3)[–43](#page-7-4)], and  $\phi$  [[44–](#page-7-5)[47](#page-7-6)] light vector mesons enables us to understand the transition between the hadronic and partonic domains of the Quantum Chromodynamics (QCD) theory according to the ranges of the photon energy *W* and the photon virtuality  $Q<sup>2</sup>$ . Extending to this virtual-photon sector offers a way to understand the hadronic properties of the virtual photon and to examine to what extent of *W* and  $Q^2$  meson exchange is applicable. Figure [1](#page-1-0) shows the graphical representations of the (a) *t*-channel meson exchange and of (b) handbag diagram for  $\gamma^* p \to (\rho^0, \omega, \phi)p$ . A hadronic Regge model is successful when going from photoproduction to low *W* and  $Q^2$ ranges of electroproduction (Fig. [1a](#page-1-0)). Meanwhile, the handbag diagram of Fig. [1](#page-1-0)b takes over high ranges of *W* and *Q*<sup>2</sup>. In such a hard scattering mechanism, the transition  $\gamma_L^* \rightarrow V_L$ dominates the process and the generalized parton distributions (GPD) and factorization of scales become relevant.

In this article, we frst review recent studies of exclusive photoproduction of  $K^*$  vector meson as well as  $\rho^0$ ,  $\omega$ ,  $\phi$ , and  $J/\psi$  ones. An effective Lagrangian approach is emphasized and its theoretical framework is explained in detail. The key experimental results are shown in comparison with the theoretical calculations. The Pomeron-exchange model is explained in some detail for the difractive scattering processes  $\gamma p \to (\rho^0, \omega, \phi, J/\psi)p$ . We focus on the  $\gamma p \rightarrow (\phi, J/\psi)p$  reaction and also discuss the possible existence of the pentaquark states  $P_s^+(P_c^+)$  via the  $\phi(J/\psi)$  photoproduction. Second, we review the studies of exclusive electroproduction of light vector mesons  $\gamma^* p \to (\rho^0, \omega, \phi)p$ . We show previous and current experiments in view of the

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<span id="page-1-0"></span>**Fig. 1** Graphical representations of **a** the *t*-channel meson exchange and of **b** the handbag diagram for exclusive vector-meson electroproduction



<span id="page-1-2"></span>**Fig. 2** Feynman diagrams for  $\gamma p \to K^*Y$ , where  $Y = (\Lambda, \Sigma)$ , are drawn for the exchanges of **a** strange mesons in the *t* channel, **b** proton in the *s* channel, and **c** hyperons in the *u* channel. **d** The contact term should be included for the charged  $K^*$  production to satisfy the gauge invariance

kinematical range of  $Q^2$  and  $x_B$  and explain two relevant theoretical approaches. We also introduce other reaction processes where a GPD model is applicable.

This article is organized as follows. In Sect. [2,](#page-1-1) exclusive photoproduction of vector mesons is reviewed. Electroproduction of vector mesons is discussed in Sect. [3](#page-5-0). The summary is given in Sect. [4](#page-6-20).

### <span id="page-1-1"></span>**2 Photoproduction of vector mesons**

## **2.1 Production of K**<sup>∗</sup>  **vector mesons**

The Born diagrams for the strangeness production  $\gamma p \rightarrow K^* Y$ , where  $Y = (\Lambda, \Sigma)$ , are drawn in Fig. [2](#page-1-2). The exchanges of (a) strange mesons in the *t* channel, (b) proton in the *s* channel, and (c) hyperons in the *u* channel are considered. (d) The contact term should be included for the charged  $K^*$  production to satisfy the gauge invariance.

An effective Lagrangian approach is employed in Ref. [[3](#page-6-2)]. The photon interaction Lagrangians of strange mesons are given by

<span id="page-1-3"></span>
$$
\mathcal{L}_{\gamma K^* K^*} = -ie_{K^*} A^{\mu} \Big( K^{* \nu} K_{\mu \nu}^{* \dagger} - K_{\mu \nu}^* K^{* \dagger \nu} \Big),
$$
\n
$$
\mathcal{L}_{\gamma K K^*} = g_{\gamma K K^*} \varepsilon^{\mu \nu \alpha \beta} \Big( \partial_{\mu} A_{\nu} \Big) \Big( \partial_{\alpha} K_{\beta}^* \Big) K + \text{H.c.},
$$
\n
$$
\mathcal{L}_{\gamma K K^*} = g_{\gamma K K^*} A^{\mu \nu} K K_{\mu \nu}^* + \text{H.c.}.
$$
\n(1)

The Lagrangians for the electromagnetic (EM) interactions of baryons are written by

$$
\mathcal{L}_{\gamma NN} = -\bar{N} \left[ e_N \gamma_\mu - \frac{e \kappa_N}{2M_N} \sigma_{\mu\nu} \partial^\nu \right] A^\mu N,
$$
\n
$$
\mathcal{L}_{\gamma YY} = \frac{e \kappa_Y}{2M_N} \bar{Y} \sigma_{\mu\nu} \partial^\nu A^\mu Y.
$$
\n(2)

The strong interaction Lagrangians of strange mesons are given by

<span id="page-1-4"></span>
$$
\mathcal{L}_{K^*NY} = -g_{K^*NY}\bar{N}Y \left[ \gamma_\mu - \frac{\kappa_{K^*NY}}{2M_N} \sigma_{\mu\nu} \partial^\nu \right] K^{*\mu} \n+ \text{H.c.} ,
$$
\n
$$
\mathcal{L}_{KNY} = -ig_{KNY}\bar{N}\gamma_5 YK + \text{H.c.} ,
$$
\n
$$
\mathcal{L}_{\kappa NY} = -g_{\kappa NY}\bar{N}Y\kappa + \text{H.c.} .
$$
\n(3)

Here, the coupling constants are determined using the experimental data if the decay modes are available [\[1](#page-6-0)] or by using the theoretical models, such as the  $SU(3)$  flavor symmetry and Nijmegen potentials  $[48, 49]$  $[48, 49]$  $[48, 49]$ . For example,  $g_{\gamma K K^*}$  in Eq. [\(1](#page-1-3)) is obtained from the experimental data for the radiative decay  $\Gamma_{K^*\to K\gamma}$ , which leads to

$$
g_{\gamma K K^*}^c = 0.254 \text{ GeV}^{-1}, g_{\gamma K K^*}^0 = -0.388 \text{ GeV}^{-1}, \tag{4}
$$

where the phases of them are fxed from a quark model. The values in Eq. ([3\)](#page-1-4) from the Nijmegen potentials (NSC97a) are given by

$$
g_{K^*N\Lambda} = -4.26, g_{K^*N\Sigma} = -2.46,
$$
  
\n
$$
\kappa_{K^*N\Lambda} = 2.66, \kappa_{K^*N\Sigma} = -0.467,
$$
  
\n
$$
g_{KN\Lambda} = -13.4, g_{KN\Sigma} = 4.09,
$$
  
\n
$$
g_{KN\Lambda} = -8.31, g_{K\Sigma} = -5.32.
$$
\n(5)

It turns out that *t*-channel *K* exchange gives a dominant contribution, while the *K*<sup>∗</sup> -exchange contribution is tiny, for  $K^{*+} \Lambda$  production [\[3](#page-6-2)]. Reference [\[4\]](#page-6-21) suggests that the light  $\kappa$  meson with a mass around (600–900) MeV could play an important role for *K*<sup>∗</sup><sup>0</sup>Σ<sup>+</sup> production, while it is

supplementary in  $K^*$ <sup>+</sup> $\Lambda$  production, from the results of the parity asymmetry defned by [[50,](#page-7-9) [51\]](#page-7-10)

$$
P_{\sigma} \equiv \frac{\mathrm{d}\sigma^N - \mathrm{d}\sigma^U}{\mathrm{d}\sigma^N + \mathrm{d}\sigma^U} = 2\rho_{1-1}^1 - \rho_{00}^1,\tag{6}
$$

because *K*<sup>∗</sup> exchange is absent in *K*<sup>∗</sup><sup>0</sup>Σ<sup>+</sup> production. Here,  $\rho$ 's are the *K*<sup>\*</sup> density matrix elements and  $d\sigma^N(d\sigma^U)$  stands for the cross-section from the natural (unnatural) parity exchanges. Then, the LEPS Collaboration [[14](#page-6-7)] has confrmed that the parity asymmetry is positive at forward angles for  $\gamma p \to K^{*0} \Sigma^{+}$  as depicted in Fig. [3](#page-2-0), indicating that natural-parity exchange is a dominant process at forward angles and the exchange of  $\kappa$ (800) scalar meson is indeed essential.

Some *N*<sup>∗</sup> resonances given in the Particle Data Group (PDG) strongly couple to the *KY* channel [[1](#page-6-0)]. Thus it is reasonable to include their contributions in the *s* channel in  $\gamma p \rightarrow K^*Y$  besides the background production mechanism of Fig. [2](#page-1-2). A few  $N^*$  resonances are included in Refs. [\[5,](#page-6-22) [6\]](#page-6-23) and are found to be crucial in *K*∗Λ production, while *N*<sup>∗</sup> contributions be marginal in *K*∗Σ production in Ref. [[7](#page-6-24)]. Here the  $N^*$  couplings to  $K^*Y$  are taken from a quark model prediction [[2\]](#page-6-1). Meanwhile, the CLAS data at the Jeferson Laboratory (JLab) on the diferential cross-sections, spindensity matrices, and  $\Lambda$  recoil polarizations for  $\gamma p \to K^{*+}\Lambda$ are ftted within the Bonn-Gatchina (BnGa) partial wave analysis [\[12\]](#page-6-5). The ftted total cross-section is displayed in Fig. [4.](#page-2-1) *K* exchange (blue dot-dashed) falls off as  $\sqrt{s} = W$ 



<span id="page-2-0"></span>**Fig. 3** Parity asymmetry versus  $\cos \theta_{K*}$  in the helicity frame from the LEPS Collaboration for  $\gamma p \to K^{*0} \Sigma^+$  [[14](#page-6-7)]. The data point is averaged over photon energies from 1.85 to 2.96 GeV. Solid curve is the result from Ref.  $[4]$  $[4]$  with almost no contribution from  $\kappa$  exchange, whereas dotted curve includes substantial  $\kappa$  exchange. Figure is taken from Ref. [\[14\]](#page-6-7)



<span id="page-2-1"></span>**Fig.** 4 Total cross-section versus beam energy *W* for  $\gamma p \to K^{*+} \Lambda$ using the BnGa partial wave analysis [\[12\]](#page-6-5). The hatched regions are labeled above, and the solid curve represents the full BnGa ft. The dashed curve represents a ft which excludes the three high-mass resonances. The data are from the CLAS Collaboration [[11](#page-6-25)]. Figure is taken from Ref. [\[12\]](#page-6-5)

increases because the *t*-channel exchange model behaves as  $\sigma \sim s^{J-1}$ , where *J* is the spin of the exchanged particle. *N*(1895)1/2<sup>−</sup> (red dashed) and *N*(2100)1/2<sup>+</sup> (green dotted) provide very significant contributions to  $\gamma p \to K^{*+} \Lambda$ . Table. [1](#page-2-2) lists the branching ratios for  $N^* \to K^* \Lambda$  extracted from Ref. [[12\]](#page-6-5). For the *K*∗Σ channel, more experimental data are required to extract the main  $N^*$  decay modes.

# 2.2 Production of  $\rho^0$ ,  $\omega$ ,  $\phi$  and  $J/\psi$ , vector mesons

The Born diagrams for the photoproduction of  $\rho^0$ ,  $\omega$ ,  $\phi$ , and  $J/\psi$  vector mesons are drawn in Fig. [5](#page-3-0).

<span id="page-2-2"></span>**Table 1** *N*<sup>∗</sup> resonances and their branching ratios [%] to the *K*∗*Y* and *VN* decays given in the PDG [\[1](#page-6-0)], where  $Y = (\Lambda, \Sigma)$  and  $V = (\rho, \omega, \phi)$ 

PDG resonances	$K^*\Lambda$	$K^*\Sigma$	$\rho N$	$\omega N$	$\phi$ N
$N(1875)3/2$ <sup>-***</sup>	< 0.2		$36 - 56$	$15 - 25$	
$N(1880)1/2$ <sup>+***</sup>	$0.5 - 1.1$		$19 - 45$	$12 - 28$	
$N(1895)1/2$ <sup>-****</sup>	$4 - 9$		$14 - 50$	$16 - 40$	
$N(1900)3/2$ <sup>+****</sup>	< 0.2		$25 - 40$	$7 - 13$	
$N(2000)5/2$ <sup>+**</sup>	$1 - 3$			$\lt$ 2.	
$N(2060)5/2$ <sup>-***</sup>	$0.3 - 1.3$		$5 - 33$	$1 - 7$	
$N(2100)1/2$ <sup>+***</sup>	$3 - 11$			$10 - 25$	
$N(2120)3/2$ <sup>-***</sup>	< 0.2		$\lt$ 3	$4 - 20$	
$N(2190)7/2$ <sup>-****</sup>	$0.2 - 0.8$		< 11	$8 - 20$	



<span id="page-3-0"></span>**Fig.** 5 Feynman diagrams for  $\gamma p \to Vp$ , where  $V = (\rho^0, \omega, \phi, J/\psi)$ , for the exchanges of **a** Pomeron, **b** light mesons in the *t* channel, and **c**, **d** proton in the *s* and *u* channels, respectively

The exchanges of (a) Pomeron, (b) light mesons in the *t* channel, and (c, d) proton in the *s* and *u* channels are considered. As for the two-gluon exchange of Fig. [5a](#page-3-0), it is suggested by the Donnachie–Landshoff (DL) model  $[33, 52]$  $[33, 52]$  $[33, 52]$  $[33, 52]$  that the Pomeron couples to the nucleon like  $a C = 1$  isoscalar photon and its coupling is described in terms of the isoscalar EM form factor of the nucleon,  $F_N(t)$ . As a consequence, the Pomeronexchange amplitude for  $\gamma(q) + p(p_i) \rightarrow V(k) + p(p_f)$  can be written by

$$
\mathcal{M}_{\mathbb{P}} = G_{\mathbb{P}}(s, t) \epsilon_{\nu}^{*} T_{\mathbb{P}}^{\mu \nu} \epsilon_{\mu},\tag{7}
$$

where

$$
T_{\mathbb{P}}^{\mu\nu} = i \frac{12eM_V^2}{f_V} \beta_Q F_V(t) \beta_q F_N(t) \left(\gamma_\alpha q^\alpha g^{\mu\nu} - q^\nu \gamma^\mu\right),\tag{8}
$$

with  $t = (q - k)^2$ .  $\epsilon_{\mu}$  and  $\epsilon_{\nu}$  stand for the polarization vectors of the incoming photon and outgoing vector meson, respectively.  $f_V$  is the vector-meson decay constant and is determined through the decay width of  $\Gamma(V \to e^+e^-) = 4\pi M_V \alpha_{\rm em}/(3f_V^2)$  [[1](#page-6-0)], which leads to  $f_V = 4.94$ , 17.06, 13.38, 11.18, and 39.68 for  $V = \rho^0$ ,  $\omega$ ,  $\phi$ , *J*/ $\psi$ , and **Y**(1*s*) mesons, respectively. The coupling of the Pomeron with the quark  $Q$  (or the antiquark  $\overline{Q}$ ) in the vector meson *V* is denoted by  $\beta_Q$ , while that with the light quark in the nucleon by  $\beta_q$ . The Pomeron–vector-meson vertex is dressed by the form factor

$$
F_V(t) = \frac{1}{M_V^2 - t} \left( \frac{2\mu_0^2}{2\mu_0^2 + M_V^2 - t} \right),\tag{9}
$$

and  $F_N(t)$  is given by

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<span id="page-3-2"></span>**Fig. 6** Total cross-section versus beam energy *W* for  $\gamma p \rightarrow (\rho^0, \phi, J/\Psi, \Upsilon(1 s)) p$  [\[54\]](#page-7-13) using the DL Pomeron model [[33](#page-6-18)]. Figure is taken from Ref. [[55](#page-7-14)]

$$
F_N(t) = \frac{4M_N^2 - 2.8t}{(4M_N^2 - t)(1 - t/0.71)^2}.
$$
\n(10)

The Regge phenomenology is involved in the propagator  $G_{\mathbb{P}}(s,t)$  in Eq. ([7\)](#page-3-1):

$$
G_{\mathbb{P}}(s,t) = \left(\frac{s}{s_0}\right)^{\alpha_p(t)-1} \exp\left\{-\frac{i\pi}{2}\big[\alpha_p(t)-1\big]\right\},\tag{11}
$$

where  $\alpha_p(t) = \alpha_0 + \alpha'_p t$  is the Pomeron trajectory. The model parameters are determined by ftting to the cross-section data of  $\rho^0$ ,  $\omega$ , and  $\phi$  photoproduction:

<span id="page-3-1"></span>
$$
\mu_0 = 1.1 \text{ GeV}^2
$$
,  $\beta_q = 2.07 \text{ GeV}^{-1}$ ,  $\beta_s = 1.39 \text{ GeV}^{-1}$ ,  
\n $\alpha_0 = 1.08$ ,  $\alpha'_p = 1/s_0 = 0.25 \text{ GeV}^{-2}$ . (12)

For the heavy quark system, some values are rather different from the light quark  $(u, d, s)$  system, that is,  $\beta_c = 0.323 \,\text{GeV}^{-1}$  and  $\beta_b = 0.452 \,\text{GeV}^{-1}$  for  $J/\psi$  and  $\Upsilon(1s)$ photoproduction, respectively, and  $\alpha_0 = 1.25$  [[53\]](#page-7-12).

The total cross-sections for  $\rho^0$ ,  $\phi$ ,  $J/\psi$ , and  $\Upsilon(1s)$  production are depicted in Fig. [6](#page-3-2) as a result of Pomeron exchange and turn out to be in good agreement with the experimental data at high energies  $[54, 55]$  $[54, 55]$  $[54, 55]$  $[54, 55]$ . Meanwhile, that for  $\rho^0$ (and possibly  $\omega$ ) production implies the need for meson exchanges of Fig.  $5b$  at low energies. Also the  $N^*$  contributions could be important in the *s* channel as indicated from the values of their branching ratios for decays into  $\rho N$  and  $\omega N$  (see Table [1\)](#page-2-2) [[56](#page-7-15)[–61](#page-7-16)]. We see that the branching ratios of *N*<sup>∗</sup> to *𝜌N* and *𝜔N* are much larger than those to *K*∗Λ. Most of the values  $Br_{N^* \to \omega N}$  are extracted by including the BnGa partial wave analysis [[59](#page-7-17)]. Note that none of the decays  $N^* \rightarrow \phi N$  is firmly observed experimentally.

A prominent feature that emerged in  $\gamma p \rightarrow \phi p$  is that a bump structure is observed for  $d\sigma/dt$  at  $t = t_{min}$  around

 $E_{\nu} \sim 2$  GeV as shown in Fig. [7](#page-4-0). It is reported by the LEPS Collaboration [\[25\]](#page-6-14) and confrmed by Refs. [[27](#page-6-26)[–29\]](#page-6-27). The Pomeron plus  $(\pi^0, \eta)$  meson exchange model (green solid curve) [\[62](#page-7-18)] cannot explain this local structure. References [[63–](#page-7-19)[65](#page-7-20)] attribute it to a postulated spin-3/2 *N*<sup>∗</sup> resonance with  $M_{N^*} \approx 2.1$  GeV and  $\Gamma_{N^*} \approx 500$  MeV. Interestingly, the CLAS Collaboration [[26–](#page-6-28)[28](#page-6-29)] has found that the structure persists only in the forward angles and vanishes around  $\cos \theta \approx 0.8$ , where  $\cos \theta$  is the  $\phi$ -meson scattering angle in the c.m. frame. Thus the interpretation of it as excitation of resonances [[63–](#page-7-19)[65](#page-7-20)] seems unlikely although not totally impossible.

Meanwhile, the bump structure is interpreted as the coupled-channel effects between the  $\phi p$  and  $K^+ \Lambda(1520)$ channels [[66–](#page-7-21)[68](#page-7-22)]. However, the similarity between the charged ( $\phi \rightarrow K^+K^-$ ) and neutral modes ( $\phi \rightarrow K_S^0 K_L^0$ ) for  $\gamma p \rightarrow \phi p$  [[27](#page-6-26), [28](#page-6-29)] implies that the rescattering effect and the interference are marginal. Moreover, it is confrmed by the LEPS Collaboration [[30\]](#page-6-15) that the  $E_\nu \sim 2.0$  GeV structure is regardless of the  $\phi$ -Λ(1520) interference effect in the  $\gamma p \rightarrow K^+ K^- p$  reaction.

Although the meson and  $N^*$  contributions are expected to be small in  $\phi$  photoproduction due to the OZI rule [[34](#page-6-19)[–36](#page-7-0)], their contributions turn out to be nonnegligible for describing the abundant CLAS data [[26–](#page-6-28)[28](#page-6-29)] on the wide scattering angles of the diferential cross-sections and spin-density matrices [[55,](#page-7-14) [69\]](#page-7-23). Proton exchange is responsible for the backward angle data. Two *N*<sup>∗</sup> resonances account for the two bumplike structures around  $\sqrt{s} \sim 2.1$  and 2.3 GeV at backward angles regardless of the much larger structure illustrated in Fig. [7](#page-4-0) [\[55](#page-7-14), [69](#page-7-23)]. Keeping these in mind, more rigorous theoretical studies are called for a better understanding of the bump structure. It is also found that the efects of the fnal state interaction (FSI) are negligible in Ref. [[55\]](#page-7-14) where the gluon exchange, direct  $\phi$ *N* couplings, and the box



<span id="page-4-0"></span>**Fig. 7** Differential cross-section  $d\sigma/dt$  versus beam energy  $E_\nu$  at  $t = t_{min}$  for  $\gamma p \rightarrow \phi p$ . The blue empty circle [\[25\]](#page-6-14) and the red full circle [[29](#page-6-27)] are from the LEPS Collaboration. The black empty square [\[27,](#page-6-26) [28\]](#page-6-29) is from the CLAS Collaboration. Figure is taken from Ref. [\[29\]](#page-6-27)

diagrams arising from the couplings with  $\pi N$ ,  $\rho N$ ,  $K\Lambda$ , and *K*Σ channels are included as for the FSI terms.

The possible existence of the hidden-strangeness pentaquark state  $P_s^+$ [*uudss*<sup>]</sup>] is discussed in Ref. [\[70](#page-7-24)] as its charmed partner, i.e., three exotic charmonium-like states  $P_c^+(4312)$ ,  $P_c^+(4440)$ , and  $P_c^+(4457)$ , are observed by the LHCb Col-laboration [\[71](#page-7-25), [72\]](#page-7-26).  $P_s^+(P_c^+)$  can be examined in the *s*-channel diagram in the  $\gamma p \to \phi (J/\psi) p$  reaction as displayed in Fig. [8.](#page-4-1)

The total cross-section for  $\gamma p \rightarrow J/\psi p$  is depicted in Fig. [9.](#page-4-2) The GlueX data in Hall D at the JLab [\[31\]](#page-6-16) and previous data [[73,](#page-7-27) [74](#page-7-28)] are compared with theoretical models [\[75](#page-7-29)[–77](#page-7-30)]. The two- and three-hard-gluon exchange processes based on perturbative QCD and efective heavy quark feld theory are studied in Ref. [\[76\]](#page-7-31). The GlueX data do not consistent with the narrow peak predicted by the JPAC model [[77\]](#page-7-30) at  $E_\gamma \simeq 10$  GeV and can be used to constrain the upper limits on the branching fraction of the pentaquark *P*<sup>+</sup> *c* states. Note that the first measurements of  $d\sigma/dt$  in the range of 9.1 GeV  $\leq E_\gamma \leq 10.6$  GeV are recently reported by the Hall C experiment at the JLab [\[32](#page-6-17)] which can give us a hint on the existence of  $P_c^+$  via  $\gamma p \to J/\psi p$ .

Following the same line of reasoning, a new proposal is recently submitted to the J-PARC facility to investigate the



<span id="page-4-1"></span>**Fig.** 8 Pentaquark  $P_s(P_c)$  exchange in *s* channel diagram in the  $\gamma p \to \phi (J/\psi) p$  reaction



<span id="page-4-2"></span>**Fig. 9** Total cross-section versus beam energy  $E_\gamma$  for  $\gamma p \to J/\psi p$ . The GlueX data [[31](#page-6-16)] are compared with the previous SLAC [[73](#page-7-27)] and Cornell [\[74\]](#page-7-28) data. The theoretical predictions are from Ref. [[75](#page-7-29)] (black dashed), Ref. [\[77\]](#page-7-30) (blue solid), and Ref. [\[76\]](#page-7-31) (red dashed). Figure is taken from Ref. [\[31\]](#page-6-16)

 $\pi^- p \to \phi n$  reaction [[78\]](#page-7-32) which offers an ideal opportunity for observing *s*-channel resonances, especially the hiddenstrangeness pentaquark  $P_s$  state. Or in view of the puzzled situation related to the interpretation of the bump structure illustrated in Fig. [7](#page-4-0), the simultaneous study of  $\pi^- p \to \phi n$  to  $\gamma p \rightarrow \phi p$  will be very valuable to understand the underlying mechanism.

### <span id="page-5-0"></span>**3 Electroproduction of vector mesons**

The schematic representation of the vector-meson electroproduction  $ep \rightarrow eVp$  is displayed in Fig. [10](#page-5-1) which consists of the (a) electron scattering plane, (b) hadronic production plane, and (c) decay plane. In the hadron production plane,  $\gamma^* p \to V(\rho^0, \omega, \phi)p$ , the cross-section dependence on the angle  $\Phi$  is separated in transverse (T), longitudinal (L), and interference (TT, LT) parts as

$$
\frac{d\sigma}{d\Phi} = \frac{1}{2\pi} (\sigma + \varepsilon \sigma_{TT} \cos 2\Phi + \sqrt{2\varepsilon (1 + \varepsilon)} \sigma_{LT} \cos \Phi), \quad (13)
$$

where  $\sigma = \sigma_T + \varepsilon \sigma_L$ .  $\varepsilon$  characterizes the degree of longitudinal polarization of the virtual photon

$$
\varepsilon = \left[1 + \frac{2\mathbf{k}^2}{Q^2} \tan^2 \frac{\theta_e}{2}\right]^{-1},\tag{14}
$$

where **k** is the three-momentum of the initial particles.

Figure [11](#page-5-2) illustrates the kinematical range covered by the vector-meson electroproduction experiments. Here  $x_B = Q^2/2M_p v$  denotes for the usual Bjorken variable where  $v = E_e - E_{e'}$  is the energy transfer in laboratory frame. The HERA experiment at the ZEUS and H1 Collaborations is performed at high ranges of *W* and  $Q^2$  (e.g.,  $40 \leq W \leq 130$  GeV and  $1 \leq Q^2 \leq 15$  GeV<sup>2</sup> at H1 [[79](#page-7-33)])



Electron plane (lab) Production plane (c*.*m*.*)

<span id="page-5-1"></span>**Fig. 10** Reference frames and relevant variables for the description of  $ep \rightarrow eVp$ : **a** electron scattering plane ( $ee' \gamma^*$ ) defined in laboratory frame, **b** hadron production plane ( $\gamma^* Vp$ ) in  $\gamma^* p$  c.m. frame, and **c** decay plane ( $V \rightarrow$  decay) in *V* rest frame



<span id="page-5-2"></span>**Fig. 11** Kinematical range covered by the vector-meson electroproduction experiments. The lines indicate the total coverage in  $Q^2$  and *xB* [[41](#page-7-3)]

<span id="page-5-3"></span>and thus the GPD formulation is most applicable. Mean-while, the old experiments at the Cornell group [[44\]](#page-7-5) and HERMES Collaboration at DESY [\[39,](#page-7-34) [40](#page-7-2), [42](#page-7-35), [43\]](#page-7-4) are carried out at low ranges of *W* and  $Q^2$  (e.g.,  $3.0 \le W \le 6.3$ ) GeV and  $0.5 \le Q^2 \le 7.0 \,\text{GeV}^2$  at HERMES [[39\]](#page-7-34)) such that a hadronic Regge model is more successful.

The CLAS experiment at the JLab is more interesting. It aims to reach the highest achievable  $Q^2$  values in the valence-quark region [\[37](#page-7-1), [38,](#page-7-36) [41,](#page-7-3) [45](#page-7-37)[–47](#page-7-6)]. Thus we can test which of the two descriptions applies in the considered kinematical domain: hadronic or partonic descriptions, i.e., *t*-channel meson exchange (Fig. [1a](#page-1-0)) or handbag diagram (Fig. [1b](#page-1-0)). For example, the so-called "JML" Regge model, developed by Laget et al. [[80](#page-7-38), [81\]](#page-7-39), is widely used to describe the meson exchange diagram. In a similar approach, Ref. [\[82](#page-7-40)] has investigated the  $\gamma^* p \to \phi p$  reaction. A hadronic model is used in Ref. [[83\]](#page-7-41) to study the  $ep \rightarrow e'J/\psi p$  reaction focusing the role of the pentaquark state  $P_c(4312)$  in the *s* channel. On the other hand, the "VGG" GPD-based model, developed by M. Vanderhaeghen and collaborators [\[84](#page-7-42)[–87](#page-7-43)], is well known to describe the hard scattering mechanism.

The measurements of the interference terms  $\sigma_{TT}$  and  $\sigma_{LT}$ in Eq. ([13](#page-5-3)) are of particular importance because they are relevant to the *s*-channel helicity conservation (SCHC). If the vector meson is produced with the same helicity as the  $\gamma^*$ , SCHC is said to hold. Then,  $\sigma_{TT}$  and  $\sigma_{LT}$  vanish by definition. SCHC can be also tested by studying the spin-density matrices and decay angular distributions, e.g.,  $\rho_{00}^0 = 0$  and  $\rho_{00}^4$  = 1 if SCHC applies. More data from the upgraded 12 GeV JLab experiment [\[88\]](#page-7-44) are necessary to reach a frm conclusion concerning SCHC for  $\gamma^* p \to V(\rho^0, \omega, \phi)p$  and will need further exploration.

Meanwhile, a GPD-based model is also accessible to the processes of the deeply virtual spin-0 meson electroproduction [[89](#page-7-45)[–92\]](#page-7-46) and the deeply virtual compton scattering (DVCS) [\[93–](#page-7-47)[96](#page-7-48)]. In Ref. [[89\]](#page-7-45), the first high  $Q^2$  measurements and complete angular distributions for exclusive  $\pi^+$ 

electroproduction on protons in the *N*<sup>∗</sup> resonance region are reported. In Ref. [[90](#page-7-49)], for the frst time target and double spin asymmetries from deeply virtual  $\pi^0$  meson production are extracted over a wide range of  $Q^2$ ,  $x_B$ , and −*t*. In Ref. [[92\]](#page-7-46), light-front time-ordered amplitudes are investigated in the virtual scalar meson production process in  $(1+1)$  dimensions using the scalar field model extended from the conventional Wick–Cutkosky model. The unpolarized and beam-polarized fourfold cross-sections  $\left(d^3\sigma/dQ^2dx_Bdt d\phi\right)$  are measured for the DVCS over the widest phase space ever covered in the valence-quark region in Ref. [[93](#page-7-47)], revealing from the experiment a frst tomographic image of the nucleon.

### <span id="page-6-20"></span>**4 Summary**

Production of vector mesons via various scattering processes opens new channels to identify high-mass baryon resonances and to investigate their properties. Especially, there has been signifcant progress on the exclusive photoproduction of vector mesons over the last decade. Accurate and abundant data on the cross-sections, spin density matrices, and spin polarization observables are produced from the CLAS, GlueX, and LEPS Collaborations for *K*<sup>∗</sup> [[11](#page-6-25), [12](#page-6-5)],  $ρ$ <sup>0</sup> [\[21\]](#page-6-11),  $ω$  [[23](#page-6-30), [24](#page-6-13)],  $φ$  [[26–](#page-6-28)[30](#page-6-15)], and *J*/ $ψ$  [\[31,](#page-6-16) [32](#page-6-17)] productions.

Theoretically, an efective Lagrangian approach and a Regge model are used intensively in a single channel analysis. The BnGa partial wave analysis is used to describe *K*<sup>∗</sup>Λ [[12](#page-6-5)] and ω*N* [\[59\]](#page-7-17) photoproduction. Since Pomeron exchange is absent in photoproduction of strange mesons, its main production mechanisms is distinguished from that of light vector mesons. We review the bump structure observed at forward angles in  $\phi$  photoproduction  $[25,$ [27](#page-6-26)–[29\]](#page-6-27) in some detail. The possible existence of the hidden-strangeness  $P_s^+$  and hidden-charm  $P_c^+$  pentaquark states is discussed via  $\phi$  and  $J/\psi$  photoproduction, respectively.

We also review the exclusive electroproduction of vector mesons and compare two diferent theoretical models. A "JML" Regge model [\[80](#page-7-38), [81\]](#page-7-39) is designed to describe the *t*-channel meson exchange diagram, whereas a "VGG" GPD-based model [\[84–](#page-7-42)[87\]](#page-7-43) is adequate for the hard scattering mechanism. The upcoming data from the CLAS [\[88\]](#page-7-44) are particularly promising because they cover wide kinematical ranges of  $Q^2$  and  $x_B$  and thus provide a unique opportunity to test the two models.

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