ORIGINAL RESEARCH

Evaluating the dependency of polymer/particle interphase thickness to the nanoparticles content, aggregation/agglomeration factor and type of the exerted driving force

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Abstract

The physical/mechanical characteristics of the polymer/particle interphase region have been always considered to be dependent on the surface chemical structure of the nanoparticles and their interactions with the polymer chains. In addition, it is repeatedly reported that the interphase-related parameters (e. g., thickness, tensile modulus and strength, yield strength, thermal conductivity) can be considered constant under any process conditions. Accordingly, in this study, a comprehensive investigation was performed to defne the efects of nanoparticles content, aggregation/agglomeration factor and type of the exerted driving force on the characteristics of the polymer/particle interphase region. To this end, diferent experimental/ analytical approaches were adapted by which it was possible to precisely characterize the internal structure of PS/silica and PMMA/silica nanocomposite samples based on their thermal and mechanical properties. The mechanical characteristics were evaluated using a developed form of Zare's model and in the case of thermal characteristics, two new analytical models were proposed based on equivalent box model (EBM). According to the results, it was revealed that the increment of the nanoparticle content increased the thermal conductivity of the interphase while decreased its thickness and yield strength. Moreover, it was found that the aggregation/agglomeration of nanoparticles had negative efects on the interphase thermal properties which were negligible at low contents.

Graphic abstract

Keywords Polymer/particle interphase · Aggregation/agglomeration · Polymer nanocomposites · Thermal/mechanical characteristics · Thermal conduction

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Introduction

Investigation of the mechanical properties and thermal conductivity of polymer composites/nanocomposites has been always considered a very important feld due to the wide

application of this family of materials in diferent industries $[1-3]$ $[1-3]$ $[1-3]$. Polymer composites are expected to have the best consistency with the process conditions which is crucial to utilize the most precise methods in their designing stage $[4, 5]$ $[4, 5]$ $[4, 5]$. In general, there are two main procedures: (I) direct application under simulated environmental conditions and (II) modeling approaches to evaluate the performance of the designed products $[6–8]$ $[6–8]$ $[6–8]$ $[6–8]$. The direct application of the composites/nanocomposites, to evaluate their probable consistency with the conditions, is not a cost/time efective method, while the modeling approach can provide valuable and practical results very fast and with almost no cost. There are many theoretical, semi-empirical and empirical models which have been developed so far. They consider a variety of assumptions to aim to elevate the level of understanding of how the thermal/mechanical characteristics of polymer composites/nanocomposites are dependent on diferent factors [[9](#page-8-6)[–11](#page-8-7)].

In the case of polymer nanocomposites, regardless of the shape and content of the nanoparticles, presence of the polymer/particle interphase regions somewhat complicates the modeling process $[12-14]$ $[12-14]$. It is well-understood that the characteristics of the interphase region drastically afect the network properties of the system due to the relatively large size of the region compared to the size of the fillers [[13,](#page-8-10) [15](#page-8-11)]. Though it is impossible to defne the characteristics of the polymer/particle interphase regions via direct measurement methods and, therefore, using the indirect methods, modeling approaches, is the only choice to obtain information about this important part of the nanocomposites [[16](#page-8-12), [17](#page-8-13)]. The polymer/particle interphase regions are formed based on the adsorption of the polymer molecules onto the surface of the nanoparticles [\[12,](#page-8-8) [13,](#page-8-10) [18\]](#page-8-14). This can be ascribed to the mutual interaction between the chemical sites on the surface of the nanoparticles with specifc groups of the polymer chains [[12](#page-8-8), [17](#page-8-13)]. Jain et al. have reported that the nanoparticles selectively adsorb the highest molar mass polymer chains, during the production process, while the surrounding matrix contains low molar mass polymer chains [[18\]](#page-8-14). In addition, according to De Genne's scaling theory of polymer adsorption, the density of the interphase region decreases with the distance from the surface of the nanoparticles until it equals the density of the polymer matrix [[19–](#page-8-15)[21](#page-8-16)].

Accordingly, the inevitable formation and thermal/ mechanical characteristics of the polymer/particle interphase regions signifcantly afect the heat transfer and stress transfer in polymer nanocomposites [[22,](#page-8-17) [23\]](#page-8-18). Moreover, the aggregation/agglomeration of the nanoparticles can be introduced as another important parameter that drastically afects their performance in the system [[24–](#page-8-19)[26\]](#page-8-20).

Diferent variation patterns, as a function of distance from the surface of the nanoparticle, can be considered for physical/mechanical properties inside the interphase regions (e.

g., linear and exponential) [[14,](#page-8-9) [27,](#page-9-0) [28](#page-9-1)]. All of the mentioned patterns have one thing in common according to which the variation starts from a maximum value, on the surface of the nanoparticle, and ends to a minimum value, equal to the value of the corresponding property in the polymer matrix [[14,](#page-8-9) [27](#page-9-0)]. As it is clear, the thickness of the interphase is a very important parameter by which it is possible to determine the average value of the physical/mechanical properties for the interphase region. For instance, Ji et al. have proposed the following equation to calculate the tensile modulus of the interphase region [[14](#page-8-9)]:

$$
dE_i = \frac{E_{i0} - E_m}{\tau} dl,
$$
\n(1)

where E_{i0} denotes the maximum tensile modulus on the surface of the nanoparticles, E_m is the tensile modulus at end of the interphase region $(E(\tau))$, τ represents the thickness of the interphase and *l* is the distance from the surface of the nanoparticles.

The effects of the polymer/particle interphase region on the physical/mechanical properties of the polymer nanocomposites have been widely investigated. Zare et al. have investigated the efects of the interphase and fller size on the percolation threshold of carbon nanotubes in nanocomposites [\[21](#page-8-16)]. Maghami et al. have proposed a new method to characterize the polymer/particles interphase using the gas permeability method [\[17](#page-8-13)]. In another study by Wan et al., the combination of microstructure characterization and micromechanical modeling methods has been used to evaluate the efects of the polymer/particle interphase region on the mechanical properties of the polymer/graphene oxide nanocomposites [[17\]](#page-8-13). Furthermore, we have previously proposed many methods to characterize the physical/mechanical properties of the polymer/particle interphase regions in diferent nanocomposite systems [\[26](#page-8-20), [29,](#page-9-2) [30\]](#page-9-3).

In almost all related studies, the interphase region is introduced as a specifc solid part of the nanocomposite, with specifc characteristics, whose formation is not dependent on other system parameters [\[13](#page-8-10), [14,](#page-8-9) [31](#page-9-4)]. Accordingly, a comparative study was performed to evaluate and compare the obtained values for the polymer/particle interphase thickness based on the thermal and mechanical characteristics of the interphase. The thermal characterization of the interphase was performed using the thermal test results of diferent prepared nanocomposites samples and a new thermal conduction model considering the efect of the nanoparticle content and aggregation/agglomeration factor. The model was designed based on the combination of series and parallel forms of equivalent box model (EBM) with the corresponding geometrical structure of the nanocomposite system. The mechanical characteristics of the polymer/particle interphase region were determined using a developed form of Zare's model, on the tensile strength of the polymer nanocomposites.

Fig. 1 a Structure of polymer nanocomposites containing spherical nanoparticles, **b** corresponding geometrical structure of the system and **c** 2D view of 1/8 of the model structure with distinguished parts

Moreover, tensile, rheology and thermal conduction tests were performed to provide sufficient experimental data for a comprehensive comparison. The tested PS and PMMA nanocomposites, containing 1, 2, 3 and 4 vol% of silica nanoparticles were prepared via melt mixing. Before the mixing process, the nanoparticles were subjected to the chemical surface modification process using (3-aminopropyl)triethoxysilane (APTES) and hexadecyltrimethoxysilane (HDTMS) to enhance their compatibility with PS and PMMA phases, respectively. Thermal conduction and tensile tests were conducted to provide the required experimental results.

Fig. 2 Structures of **a** EBMp and **b** EBMs and their relation with their geometrical model structure

Modeling background

posite containing spherical nanoparticles that are perfectly dispersed in the matrix. Based on the fundamentals of Ji's model [[14\]](#page-8-9), it is possible to represent the entire nanocomposite structure as a cube, with unit side length, containing a core and shell at its center (Fig. [1](#page-2-0)b). This geometrical structure is also used by Boutaleb et al. to evaluate the mechanical properties of the polymer nanocomposites containing spherical nanoparticles [[32\]](#page-9-5). It should be noted that the diameter of the sphere (*z*) and the thickness of the shell (*e*/2–*z*/2) are the representatives of the diameter of the nanoparticles and thickness of the actual polymer/particle interphase region, respectively. Accordingly, parameters *z* and *e* can be defned using Eqs. ([2\)](#page-2-1) and ([3\)](#page-2-2), respectively:

$$
z = \sqrt[3]{\frac{3\varphi_d}{\pi 4}}\tag{2}
$$

$$
e = \sqrt[3]{\frac{3\varphi_d}{4\pi r^3} ((r+\tau)^3 - r^3) + z^3},
$$
\n(3)

where τ is the thickness of the polymer/particle interphase region, φ_d denotes the actual volume fraction of the applied nanoparticles in the nanocomposite samples and *r* is the radius of the spherical nanoparticles.

As it is illustrated in Fig. [1](#page-2-0)c, the corresponding geometrical structure of the nanocomposite system (Fig. [1b](#page-2-0)) can be represented as 1/8 of the main structure which helps to simplify the modeling process. To be more precise, the model structure can be divided into 8 similar and symmetrical parts in which the volume fraction of the constituents is similar to that of the main structure. To evaluate the interaction between the model constituents, it is possible to use two diferent arrangements of the EBM, as illustrated in Fig. [2.](#page-2-3)

In general, EBM constructs a combination of series and parallel boxes, representing model structural constituents, through which it is possible to study the response mechanism of the system against the exerted driving force (e. g., stress, heat, etc.) $[14, 26]$ $[14, 26]$ $[14, 26]$ $[14, 26]$ $[14, 26]$. Each box in the EBM has a specific volume fraction which in this study should be calculated using the main model structure (Fig. [1b](#page-2-0), c) as follows:

$$
\varphi_{\rm N} = 4/3\pi z^3 \tag{4}
$$

$$
K_T = \varphi_I K_I + \varphi_{II} K_{II} + \varphi_{III} K_{III},\tag{15}
$$

where K_I and K_{II} can be calculated using Eqs. ([16\)](#page-3-0) and [\(17](#page-3-1)), respectively:

$$
\frac{1}{K_{\rm I}} = \frac{\varphi_{m\rm I}}{K_m} + \frac{\varphi_{i\rm I}}{K_i} + \frac{\varphi_{\rm N}}{K_{\rm N}} (1 - \mu) \tag{16}
$$

$$
\frac{1}{K_{\rm II}} = \frac{\varphi_{m\rm II}}{K_m} + \frac{\varphi_{i\rm II}}{K_i},\tag{17}
$$

$$
\varphi_{\text{ill}} = 4/3\pi e^3 - 2\left\{\pi \left(e - \sqrt{e^2 - z^2}\right)^2 / 3 \times \left(3\left(e - \sqrt{e^2 - z^2}\right) - e\right)\right\} - 2\pi^2 \sqrt{e^2 - z^2} \tag{5}
$$

$$
\varphi_{i\text{II}} = 4/3\pi \left(e^3 - z^3\right) - \varphi_{i\text{II}} \tag{6}
$$

$$
\varphi_{m\text{III}} = 1 - \pi e^2 \tag{7}
$$

$$
\varphi_{mII} = \pi \left(e^2 - z^2 \right) - \varphi_{iII} \tag{8}
$$

$$
\varphi_{mI} = \pi z^2 - \varphi_N - \varphi_{iI} \tag{9}
$$

$$
\varphi_1 = \pi z^2 \tag{10}
$$

$$
\varphi_{\text{II}} = \pi \left(e^2 - z^2 \right) \tag{11}
$$

$$
\varphi_{III} = \varphi_{mIII}.\tag{12}
$$

The thermal resistance along the fux direction is additive [\[33\]](#page-9-6), and therefore, the effective thermal conduction coefficient of the series component (K_{es}) of the EBMs is

$$
R_{\text{Ts}} = \sum R_j \to \frac{1}{K_{\text{es}}} = \sum \frac{\varphi_j}{K_j},\tag{13}
$$

where φ_j , K_j and R_j are the volume fraction, conduction coefficient and resistance of the component j_{th} . R_{Ts} denotes the overall resistance in the series state.

On the other hand, considering the additive thermal conductance $(C_{TP} = 1/R_{TC})$ for parallel components it is possible to calculate the effective thermal conduction coefficient of the parallel components (K_{en}) of the EBMs as follows [[33\]](#page-9-6):

$$
C_{\text{Tp}} = \sum C_j \to K_{\text{ep}} = \sum \varphi_j K_j. \tag{14}
$$

In the case of the parallel state of parts I, II and III of the EBM (Fig. $2a$ $2a$), the thermal conduction coefficient of the nanocomposite (K_T) can be calculated using the following equation:

In the case of the series state of parts I, II and III (Fig. [2b](#page-2-3)) the thermal conduction coefficient of the nanocomposite is

$$
K'_{T} = \left(\frac{\varphi_{\rm I}}{K'_{\rm I}} + \frac{\varphi_{\rm II}}{K'_{\rm II}} + \frac{\varphi_{\rm III}}{K_{\rm III}}\right)^{-1},\tag{18}
$$

where K_I and K_{II} can be calculated using Eqs. ([19\)](#page-3-2) and [\(20](#page-3-3)), respectively:

$$
K'_{\rm I} = \varphi_{m\rm I} K_m + \varphi_{\rm i\rm I} K_i + \varphi_{\rm N} K_{\rm N} (1 - \mu) \tag{19}
$$

$$
K'_{\text{II}} = \varphi_{m\text{II}} K_m + \varphi_{i\text{II}} K_i. \tag{20}
$$

Hereinafter, the EBM model with parallel and series I, II and III parts will be referred to as EBMp and EBMs, respectively.

Experimental

Materials

Aerosil fumed silica was kindly provided by Degussa (OX-50, *D* =40 nm, France). (3-Aminopropyl)triethoxysilane (APTES), hexadecyltrimethoxysilane (HDTMS) and ethanol (>99%) were purchased from Merck Co. (Germany) and used without further treatments. Polystyrene (PS) [Grade 1160 GPPS, $\rho = 1.04$ (g/mL)] and poly(methyl methacrylate) [Grade IH830, $\rho = 1.18 \text{ (g/mL)}$] were purchased from Tabriz Petrochemical (Iran) and LG Co. (South Korea), respectively.

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Sample preparation

Surface modifcation of the nanoparticles to enhance the compatibility with PS and PMMA.

The nanoparticles were added to ethanol and sonicated for 30 min at room temperature, to obtain a well-dispersed suspension, and then APTES was added and the mixture stirred for 24 h. The surface-modifed nanoparticles were then collected by centrifugation and washed with water several times to remove extra APTES molecules. Finally, the nanoparticles were dried at 50 °C under vacuum for 24 h. The same method was repeated with HDTMS. The silica nanoparticles modified with APTES and HDTMS were addressed as OXA and OXH, respectively.

Nanocomposite sample preparation

Melt mixing process was performed in an internal mixer (Brabender Plasticorder W50EHT, Germany) (60 rpm, 8 min, 200 °C) to prepare PMMA nanocomposite samples containing 1–4 vol% of OXH nanoparticles. The samples were then transferred to a vacuum oven at 60 °C and after 72 h molded according to ISO-527 using a hot-press device (200 °C, 40 bar). A diferent mold (thickness: 2 mm, diameter: 20 mm) was also used to prepare suitable samples for thermal conduction and rheology tests. The same method was used to prepare PS nanocomposite samples containing 1–4 vol% of OXA nanoparticles.

Characterization

Rheology test

The frequency sweep rheology tests were conducted using an Anton Paar MCR 301 device (Austria) at 200 °C. The complex and zero shear rate viscosities of the PS-OXA samples were used to interpret the results of the heat conduction tests.

Tensile tests

The tensile tests were performed using a Zwick/Roell tensile testing machine (Z 010, Germany) at room temperature according to ISO-527. At least 3 samples of each composition were tested and the averaged results were used to determine the characteristics of the interphase region based on the developed form of Zare's model.

Heat conduction tests

The thermal conduction coefficient of the tablet-shape nanocomposite samples was measured by placing them between the heated and cooled metal sections of a heat conduction unit (H940, P.A. Hilton, UK). The heat fux was set at 2 W/ $m²$ and then the temperatures at the sides of each sample were read. Finally, Fourier's law [Eq. [\(21](#page-4-0))] was used to calculate the conduction coefficient of the samples $[34]$ $[34]$:

$$
q_x = -k \frac{\Delta T}{\Delta x},\tag{21}
$$

where q_x denotes the heat flux (W m⁻²), ΔT and Δx represent the temperature diference and thickness of the samples, respectively. At least 3 samples of each composition were tested and averaged results \pm STD were reported.

Results and discussion

Table [1](#page-5-0) represents the model results regarding the interpreted thermal characteristics of the polymer/particle interphase region based on EBMp (Fig. [2a](#page-2-3)). As it is clear, the conduction coefficient of the interphase region (K_i) was lower than that of the polymer matrix, in all samples, and decreased with nanoparticles content. This can be ascribed to the higher compactness of the polymer molecules in the region, compared to the surrounding polymer bulk, which decreased the heat transfer $[20, 22, 35]$ $[20, 22, 35]$ $[20, 22, 35]$ $[20, 22, 35]$ $[20, 22, 35]$. It can be also seen that the thickness of the interphase (τ) and K_i decreased with the nanoparticles content, in both PS-OXA and PMMA-OXH groups, which can be attributed to the selective adsorption of the high molar mass polymer molecules onto the surface of the nanoparticles [\[18,](#page-8-14) [35](#page-9-8)]. The reported values of the aggregation/agglomeration factor (μ) were interpreted from the experimental results via optimizing Eqs. ([15\)](#page-3-4) and ([18\)](#page-3-5) [[15\]](#page-8-11).

In general, it is reported that the adsorbed high molar mass polymer chains form a shell around the nanoparticles, while the low molar mass chains stay in the surrounding molten matrix $[18]$ $[18]$. As a result, the increment of the nanoparticle content should decrease the viscosity of the molten nanocomposite. This concept was evaluated via the rheology test using the prepared PS-OXA nanocomposite samples.

As it is demonstrated in Fig. [3a](#page-5-1), the complex viscosity $(\eta^*(\omega))$ of the tested samples was decreased with the content of the nanoparticles, whose surfaces were completely compatible with the surrounding polymer phase, at any frequency. Besides, Fig. [3b](#page-5-1) clearly shows the decrement of the zero-shear rate viscosity with the content of the nanoparticles. These fndings are completely similar to those reported in literature [[22](#page-8-17)] and accordingly, it can be concluded that τ is directly dependent on the number and length of the attached polymer chains [[18\]](#page-8-14).

Figure [4](#page-6-0) represents the schematic of the selective adsorption of the relatively high molar mass polymer chains and its dependency on the nanoparticle content. As it is clear, at

	φ_d (vol%)	(τ) (nm)	(K_i) (W m ⁻¹ k ⁻¹)	(μ) $(\%)$	Experimental conduc- tion coefficient $(K_{\text{exp.}})$ $(W m^{-1} k^{-1})$	Theoretical conduc- tion coefficient (K_{the}) $(W m^{-1} k^{-1})$	Error $(\%)$
PS-OXA	$\mathbf{0}$				0.163 ± 0.015		
	1	89	0.143	$\mathbf{1}$	0.196 ± 0.012	0.193	1.5
	2	66	0.148	1.7	0.224 ± 0.016	0.216	3.5
	3	53	0.15	2.6	0.251 ± 0.02	0.241	3.9
	4	43	0.152	3.2	$0.283 + 0.019$	0.277	2.1
Average		62.7	0.148	2.05			
PMMA-OXH	Ω				0.290 ± 0.011		
	1	74	0.23	$\mathbf{1}$	0.425 ± 0.016	0.413	2.8
	\overline{c}	49	0.241	1.6	0.514 ± 0.014	0.504	1.9
	3	36	0.262	2.8	0.607 ± 0.008	0.598	1.4
	$\overline{4}$	26	0.279	3.7	0.698 ± 0.014	0.683	2.1
Average		46.2	0.253	2.275			

Table 1 Thermal characteristics of the PS-OXA and PMMA-OXH nanocomposite samples based on EBMp

Fig. 3 Rheology test results of PS-OXA nanocomposite samples: **a** variation of the complex viscosity with frequency and **b** variation of zero-shear rate viscosity with the nanoparticle content

frst the two big polymer chains were selectively adsorbed (Fig. [4](#page-6-0)a), while the chains with lower molar mass were not allowed inside the interphase region. However, after the duplication of the available nanoparticles surfaces (Fig. [4](#page-6-0)b), the increment of the nanoparticles content, there was enough space for other polymer chains, with relatively high molar

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mass compared to other unattached molecules, to enter the interphase region. This increased the length range of the attached chains onto the surface of the nanoparticles and consequently, according to the results of Table [1,](#page-5-0) decreased the interphase thickness.

The same trends can be also seen for τ and K_i in Table [2,](#page-6-1) where the interpreted thermal characteristics of the interphase region are represented based on EBMs. Though, it is noteworthy to mention that the average value of K_i was almost the same for PS-OXA or PMMA-OXH samples based on the results of EBMp and EBMs. We have previously proved that the aggregation/agglomeration of the nanoparticles was an inevitable phenomenon, even at very low nanoparticles content $(<1\%)$ [[30\]](#page-9-3). Similar results were also obtained in the present study (Tables [1](#page-5-0) and [2\)](#page-6-1). In addition, very low error values of the proposed conduction model, based on both EBM approaches, indicated its acceptable accuracy.

The effects of the variation of parameters τ , K_i and μ on the conduction coefficient of PS-OXA nanocomposite samples [Eqs. [\(15](#page-3-4)) and ([18\)](#page-3-5)] are represented in Fig. [5](#page-7-0). According to both EBM approaches, the increment of K_i at any nanoparticles content increased the conduction coefficient of the nanocomposite (*K* or *K'*) (Fig. [5b](#page-7-0), e). The impact of the aggregation/agglomeration factor (μ) on EBMp was negligible (Fig. [5c](#page-7-0)), while it drastically affected the results of EBMs (Fig. [5](#page-7-0)f). On the other hand, according to EBMp the thermal conduction coefficient of the nanocomposite samples follows an increasing trend with the increment of the interphase thickness (Fig. [5a](#page-7-0)), while EBMs were very sensitive to the variation of τ and did not follow any specific trend (Fig. [5](#page-7-0)d).

Moreover, the yield strength and thickness of the polymer/ particle interphase region were also determined using the developed form of Zare's model based on the obtained results from the

performed tensile tests [\[36](#page-9-9)]. It should be noted that development of procedure was comprised by adding the parameter μ to the computational structure of the model to involve the efects of the aggregation/agglomeration of the nanoparticles. According to the developed model, the thickness of the polymer/particle interphase region can be calculated as follows:

$$
\tau = \frac{r}{3} \left(\frac{\ln \left(\frac{\sigma_{\exp} \left(1 + 2.5 \left(\mu \varphi_d \right)^{2/3} \right)}{\sigma_m \left(1 - \left(\mu \varphi_d \right)^{2/3} \right)} \right) \left(\mu \varphi_d \right)^{-2/3}}{\ln \left(\frac{\sigma_i}{\sigma_m} \right)} - 1 \right), \tag{22}
$$

where σ_{exp} and σ_m are the experimental yield strength of nanocomposite and polymer matrix, respectively, *r* is the radius of the spherical nanoparticles, σ_i represents the yield strength of the polymer/particle interphase region and μ is the aggregation/agglomeration factor (Tables [1](#page-5-0) and [2](#page-6-1)). Based on the nature of the tensile and heat conduction tests there is no need to discriminate the aggregation (strong bonding) or agglomeration (loose bonding) phenomena, since they were considered to have similar efects on the models. The increment of the nanoparticle content increased parameter μ and accordingly, at high nanoparticles content a major deviation could be seen from the ideal state, where

Table 2 Thermal characteristics of the PS-OXA and PMMA-OXH nanocomposite samples based on EBMs

Fig. 5 Efects of the variation of parameters τ , K_i and μ on the thermal conduction coefficient of PS-OXA nanocomposite samples based on **a–c** EBMp and **d–f** EBMs structures

 $\mu = 0$. Though, both mechanical and thermal models were designed in a way that they could minimize the fnal errors and offered the closest results to the actual values considering the aggregation/agglomeration factor.

We have previously proved that σ_i/σ_m was 5.9 and 4.3 for PMMA-OXH and PS-OXA nanocomposites, respectively [[7,](#page-8-22) [30](#page-9-3)]. However, the variable mechanical characteristics of the interphase region, based on the aggregation/agglomeration factor of EBMs are represented in Table [3](#page-7-1).

As can be seen in Table 3 , τ decreased with the nanoparticles content, similar to the reported results in Tables [1](#page-5-0) and [2](#page-6-1) which also proved the efects of the nanoparticles content on the selective adsorption of the high molar mass polymer chains. It should be also noted that the relatively higher values of τ in the case of PS-OXA samples (>100 nm) could be attributed to the stronger interaction between APTES molecules and PS chains compared to that of HDTMS molecules and PMMA chains.

It is noteworthy to mention that, we have also reported 194 nm and 21.5 nm as the average thicknesses of the interphase region based on the tensile strength results of PS-OXA and PMMA-OXH nanocomposites, respectively [[7,](#page-8-22) [30](#page-9-3)]. Comparing all of the represented results clearly showed that the thickness of the polymer/particle interphase region was completely depended on the nanoparticles content, aggregation/agglomeration factor and the type of the exerted driving force.

Conclusion

The thermal and mechanical characteristics of the polymer/ particle interphase region were interpreted from the thermal conduction and tensile tests, respectively. It was proved that the combination of EBMp and EBMs with the corresponding geometrical structure of the nanocomposites was completely capable of defning the thickness and thermal conduction coefficient of the interphase region as a function of φ_d and μ . Though, EBMs was more sensitive to the variation of μ and τ , it introduced a better choice for interpreting the thermal characteristics of the interphase region. On the other hand, the mechanical characteristics of the polymer/ particle interphase region were interpreted from the tensile test results (yield strength) of the prepared PS-OXA and PMMA-OXH nanocomposites using a developed form of Zare's model. Comparing the results revealed that the interphase thickness in a nanocomposite system was dependent on the nanoparticle content, aggregation/agglomeration factor and type of the exerted driving force, and therefore, it should not be considered as a specifc part of the nanocomposite system with constant characteristics (e. g. thickness, thermal conduction, tensile modulus, yield strength, etc.).

Declarations

Conflict of interest The authors declare that they have no conficts of interest.

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