RESEARCH ARTICLE-MECHANICAL ENGINEERING

Process Parameters Efect Investigations on Viscosity of Water‑ethylene Glycol‑based α‑alumina Nanofuids: An Ultrasonic Experimental and Statistical Approach

R. Prakash¹ · L. Chilambarasan1 · K. Rajkumar1

Received: 23 February 2021 / Accepted: 29 May 2021 / Published online: 8 June 2021 © King Fahd University of Petroleum & Minerals 2021

Abstract

Stable α-alumina-water-ethylene glycol (WEG) based nanofuids with a low viscosity requirement are preferable for promising engineering applications. Viscosity of nanofuids is a signifcant parameter that decides the fow characteristics and pumping pressure requirements. In this study, α-alumina nanoparticles (spherical morphology with 40 nm) dispersed in WEG mixture in a ratio of 50:50 (v/v) using an ultra-sonication process. Further analysis of the effects of process parameters on the viscosity of prepared nanofuid, including volume concentrations (0.01%–0.2%), temperatures (30-45 °C), and sonication times (0–4 h). A decrease in viscosity of 11.36% was observed for 0.2% volume concentration as sonication time increased from 0 to 3 h at a process temperature of 45 $^{\circ}$ C. The viscosity value of nanofluids approaches a stable value at 3 h of sonication. No signifcant sonication 'null efect' was required for lower concentrations irrespective of the temperature and sonication time, yielding low viscosity. At the same time, clusters were observed at a higher volume concentration under a minimal sonication time (1 h) resulting in a higher viscosity. On the other hand, the viscosity of nanofuid was reduced with the help of an increase in sonication duration and process temperature. Statistical analysis ranks a higher degree to volume concentration of nanoparticles.

Keywords Nanofuid · Water-ethylene glycol · Viscosity · Statistical analysis · Ultrasonication · Particle cluster

1 Introduction

Conventional heat transfer fuids are considered energyintensive and demanding costly thermal management systems and can cause environmental concerns. The concept of nanofuids started at the beginning of the nineteenth century, but there is still a need for comprehensive research, as the development of new types of nanoparticles and their exotic properties offer a solution for emerging engineering applications. Choi and Eastman [\[1](#page-10-0)] introduce the concept of nanofuids by suspending nanoparticles in the base fuid in order to create advantages over conventional fuids. Nanofuids are new-generation heat transfer fuids synthesized by dispersing metallic like copper, aluminium, etc., or non-metallic

 \boxtimes L. Chilambarasan chilambarasanl@ssn.edu.in nanoparticles such as various forms of carbide, ceramics, and semiconductors or nanofbers/nanotubes of less than or equal to 100 nm size in base fluids $[2-4]$ $[2-4]$.

Zarei et al. [[5\]](#page-10-3) have suggested the prospects of nanofuids as a working fuid for various heat transfer applications. Nanofuids have boosted thermal properties with better longterm stability, and offer low pressure drops and erosion during fuid pumping [\[2](#page-10-1)]. Nanofuids are prepared using either one-step or two-step techniques without/with the addition of a surfactant to increase its stability and prevent sedimentation. Generally, heat transfer fuids such as water, ethylene glycol, propylene glycol [[6\]](#page-11-0), tri-ethylene glycol [\[5](#page-10-3)], glycerol [[7\]](#page-11-1), and engine oil [[8\]](#page-11-2) are explored as base fuid. However, a mixture of water and ethylene glycol is widely used as a heat exchange medium in both heating and cooling systems to maximize the boiling point and minimize the freezing point, respectively [[9\]](#page-11-3). In a nanoparticle group, alumina $(\alpha$ -Al₂O₃) is one of the non-metallic nanoparticles having unique favourable characteristics for the requirement of many heat transfer applications. Alumina $(\alpha - Al_2O_3)$ nanoparticle is a thermodynamically stable metal oxide with

¹ Department of Mechanical Engineering, Sri Sivasubramaniya Nadar College of Engineering, Kalavakkam, Chennai 603110, Tamilnadu, India

attractive features such as better specifc heat, high thermal conductivity, and lower density [\[10](#page-11-4)].

Characteristics of nanofuid are governed by four essential thermophysical properties, such as thermal conductivity, viscosity, density, and specifc heat [[11\]](#page-11-5). Also, these properties are directly related to parameters such as type of nanoparticles, their volume concentration, mixture of base fuids, and process temperature [[2\]](#page-10-1).

A suitable combination of above-mentioned parameters is to be controlled to tailor the required properties of nanofuids. Thermal conductivity and viscosity of nanofuids are the most signifcant characteristics that describe the application of nanofuids in heating and cooling systems, nuclear reactors, pool boiling, solar heater, lubricant for machining processes, automotive cooling system, medical, and food industries [\[6\]](#page-11-0). Thermal conductivity and viscosity of the nanofuid increase with the addition of nanoparticles is unavoidable. However, the required heat transfer fuids must be balanced as low viscosity and high thermal conductivity for efficient use as coolants $[12]$ $[12]$. In terms of flow and heat transfer properties, viscosity is one of the essential properties of fuids and determines the selection of nanofuids for various applications [\[13\]](#page-11-7). Much research has been conducted on the thermal properties of nanofluids $[14–16]$ $[14–16]$ $[14–16]$, especially thermal conductivity, stability and specifc heat, with regard to the morphology and size of added nanoparticles. Few research studies have reported on the viscosity of nanofuids which consist mainly of a mono-type fluid [\[3](#page-10-4)]. Viscosity is also referred to as dynamic viscosity, which is an important behaviour of thermophysical properties of colloidal suspensions like nanofluid $[17, 18]$ $[17, 18]$ $[17, 18]$ $[17, 18]$. However, there has been gradually increasing interest in the viscosity of nanofuids due to its impact on several other characteristics of nanofuid such as heat transfer, fluid flow, resistance to flow, specific heat capacity, and pumping pressure [\[19–](#page-11-12)[22\]](#page-11-13). Several factors infuence the viscosity of nanofuids, either directly or indirectly, including particle shape and size, volume concentration, base fuid properties, process temperature, and added surfactants [[23,](#page-11-14) [24](#page-11-15)]. Usually, nanofuids have a higher viscosity as compared to their respective base fuids but the requirement of any nanofuid has as much as low viscosity to facilitate the fuid fow [\[3](#page-10-4)].

Likewise, temperature is a signifcant parameter that infuences the viscosity of nanofuids. Normally, an increase in temperature signifcantly decreases the viscosity of nanofuids [[25,](#page-11-16) [26\]](#page-11-17). In addition, Asadi et al. [[27\]](#page-11-18) stated in a study that nanofuids show a gradual reduction in viscosity up to critical temperature, after that the viscosity is dramatically reduced to a lower extent. Moreover, the prospect of nanofuid is also related to its processing conditions, which may extend stability of nanofuid.

The effect of the ultrasonication process on the thermal conductivity and viscosity of nanofuid has been studied in order to understand its positive impact on the studying fuids [\[28,](#page-11-19) [29\]](#page-11-20). Ultrasonication can prevent the formation of agglomeration of nanoparticles and facilitate its uniform dispersion in the base fuid. Ultrasonication process controlled by parameters of power, duration, and frequency to make a dispersion efectively. However, sonication duration is an ultrasonication process parameter that efectively controls the nanofuid properties by a uniform dispersion of nanoparticles and its stability in a base fuid [[30\]](#page-11-21). Further to understand the ultrasonication process, Mahbubul et al. [[31\]](#page-11-22) investigated the effect of ultrasonication energy on the viscosity of A_1O_3 water nanofluid and reported the decrease in the number of clusters with an increase in ultrasonication duration but not considered to have a concentration efect and a process temperature.

As compared to low viscosity base fuids, higher viscosity base fuids containing nanoparticles need more sonication time (energy) to become homogeneous [\[32](#page-11-23)]. Kwak and Kim [[33\]](#page-11-24) found that an optimal duration as 9 h required to complete dispersion of nanoparticles for ethylene glycol-based CuO nanofuid from the experimental sonication duration of 1 to 30 h. Lee et al. $[25]$ $[25]$ conducted the sonication of aqueous-based Al_2O_3 (30 nm) nanofluids up to 30 h and found that 5 h of sonication was an optimum. They asserted that an optimal ultrasonication period for the nanofuids depends on the size and zeta potential of alumina nanofuids. Buonomo et al. [\[34](#page-11-25)] and Gangadevi et al. [[35\]](#page-11-26) found optimum sonication duration for water based Al_2O_3 nanofluid as 2 h (40 nm) and 4 h (50 nm), respectively. At the same time, Adio et al. [\[36](#page-11-27)] conducted experiments with Al_2O_3 nanoparticles of different sizes such as 30, 80 and 100 nm in glycerol as base fuid and reported that nanofuid prepared with smaller particle size (30 nm) shows higher viscosity and requires more sonication energy when compared with nanofuid prepared with larger particle size (80 nm and 100 nm). He et al. [[37\]](#page-11-28) investigated the viscosity of $TiO₂$ nanofluids with particle sizes ranging from 95 to 210 nm and found that the viscosity increases with increasing nanoparticle size; however, their experimental results contradicted Adio et al. fndings.

Considering the above discussions, the requirement of efficient heat transfer nanofluids with optimum viscosity is required for the heat transfer applications. The present investigation aimed to study the efect of ultra-sonication duration, volume concentration of nanoparticles, and temperature on the dynamic and relative viscosity of the WEG based Al_2O_3 nanofluid to suit different engineering applications. Further, statistical analysis on viscosity of nanofuid has been performed to study the effect of considered parameters to determine its signifcance and their ranking.

2 Experimental Procedure

2.1 Source and Characteristics of Alumina Nanoparticles

 Al_2O_3 nanoparticles are chemically stable, less toxic, cheaper, and commercially available. α -Al₂O₃ nanoparticles of less than 50 nm were purchased from Sigma-Aldrich, Germany. High-Resolution Transmission Electron Microscope (HR-TEM) was employed to study the morphological characteristics of $A₁O₃$ nanoparticles.

The morphology and average size of the nanoparticles, as shown in Fig. [1a](#page-2-0), were almost spherical, and 40 nm. XRD analysis on the Al_2O_3 nanoparticles was carried out with an Empyrean X-ray difractometer (PANalytical, Netherlands) with Cu anode (line and point focus) to confrm the crystalline structure of metal oxide. Figure [1](#page-2-0)b reveals the rhombohedral structure of Al_2O_3 nanoparticles and confirmed peaks with the help of JCPDS card number 1040LQS. Major XRD refections observed were listed as follows: 25.59°, 35.14°, 37.78°, 43.36°, 52.55°, 57.52°, 59.8°, 61.23°, 66.55°, 68.20°, and 77.2° . The morphology, size, and structure of Al_2O_3 nanoparticles were identifed to be suitable for the preparation of WEG based alumina nanofuid.

2.2 Calculation of Volume Fraction of Nanoparticle

The formula used to fnd the volume concentration of the nanoparticle $[38]$ $[38]$ $[38]$ in the nanofluid is mentioned below Eq. ([1](#page-2-1)).

Volume concentration,
$$
\phi
$$
 $\varphi = \begin{bmatrix} \frac{V_{\text{Al2O3}}}{\rho_{\text{Al2O3}}} \\ \frac{V_{\text{Al2O3}}}{\rho_{\text{Al2O3}}} + \frac{V_{\text{bf}}}{\rho_{\text{bf}}} \end{bmatrix} \times 100$ (1)

where,

ϕ is the volume fraction of the nanoparticle.

 V_{Al2O3} and V_{WEG} are the weights of nanoparticle and WEG fluid, respectively.

 ρ_{Al2O3} and ρ_{WEG} are the densities of nanoparticles and WEG fluid, respectively.

2.3 Preparation of Nanofuids

The two-step procedure is the most widely used method for nanofuid preparation. Ethylene glycol has anti-freezing properties [[39\]](#page-12-0) and is miscible with water. Yu et al. [[40\]](#page-12-1) suggested that the suitable proportion of water and ethylene glycol (WEG) is 50: 50 for anti-freezing or anti-boiling applications. It is therefore considered to be a good base fluid for nanofluid preparation [[41\]](#page-12-2). Nanofluid was prepared by dispersing the Al_2O_3 nanoparticles in the WEG fluid in the ratio of 50:50 (Ethylene glycol: water) using a two-step method [\[42](#page-12-3)], as follows:

- 1. 100 ml of a mixture of deionized water and ethylene glycol was stirred well over a magnetic stirrer (REMI 5MLH) at a constant speed of 420 rpm. Al_2O_3 nanoparticles were then added to the mixture and the stirring process continued at the same speed.
- 2. Finally, the obtained suspension was again sonicated to required stability with an ultrasonication method (RS PRO Ultrasonic) with a facility to precisely control the temperature of the bath.

2.4 Examination of Stability of Al₂O₃ Nanofluids

 Al_2O_3 nanoparticles were dispersed in the volume concentration of 0.01%, 0.05%, 0.1%, and 0.2% in ethylene

Fig. 1 HR-TEM image and XRD pattern of AI_2O_3 nanoparticle

glycol–water mixture. Prepared nanofuid samples were stored for one month in glass vials to determine the stability through visual observation. Figure [2](#page-3-0)a shows the photograph of nanofuid samples at the time of preparation. After one month, the photograph of samples was taken and is presented in Fig. [2](#page-3-0)b. No visual sediments were observed in all studied samples but there was a presence of slight sedimentation for higher volume concentration samples.

2.5 Particle Size Determination in Alumina Nanofuids

Dynamic Light Scattering (DLS) is the most common method that can be used to fnd the size of particles in the suspension or nanofuids. The alumina particle/cluster size of the prepared nanofuids was determined using a Dynamic Light Scattering (Model: Nanotrac Wave II) analyzer. After 3 days of nanofuid preparation, particle size analysis was performed at room temperature for lower (0.01%) and higher (0.2%) volume concentrations.

2.6 Viscosity Measurements

A rotational type digital viscometer (VISCO-895, ATAGO, Japan) was used to measure the dynamic viscosity of prepared samples. Some advantages of using this type over other viscometers were high accuracy $(\pm 1\%)$, small sample amount (16 mL), least count $($ - 1mPas), and variable speed (0.5–250 rpm). The digital viscometer measures the viscosity of the liquid sample directly using the theory of measuring the shear stress (torque) between the cylindrical surface of the spinning cylinder immersed in the sample. The viscosity of samples was taken at a constant rotation speed of 250 rpm.

Prior to measurement, the instrument was calibrated using a standard liquid with known viscosity. The dynamic viscosity of WEG (50:50) is measured three times for the validation of the instrument, and the same is compared with the values of ASHRAE [[43](#page-12-4)]. A k-type thermocouple was used to monitor changes in the temperature of nanofuids during viscosity measurements. Figure [3](#page-3-1) shows a comparison of the WEG experimental results with the ASHRAE data. The observed results were in good agreement with ASHRAE data showing a variance of \pm 5 per cent and thus verifed the validity of the measurements.

For experimentation, process parameters such as ultrasonication time (0–4 h), temperature (30–45 °C), volume concentration $(0.01\%, 0.05\%, 0.1\%, 0.2\%)$ of nanoparticles were considered to investigate the change in viscosity of WEG -based Al_2O_3 nanofluid. The selection of process parameters was based on the previous literature [[19](#page-11-12), [21](#page-11-30)]. This study is used to determine the variation in viscosity

Fig. 3 Validation of the digital rotational viscometer

 $0.1%$ $0.2%$ $0.05%$ $0.01%$ $0.1%$ $0.01%$ 0.05%

(a) Samples at the time of preparation

(b) Samples after one month

 $0.2%$

Fig. 2 a Samples at the time of preparation. **b** Samples after one month

of WEG -based Al_2O_3 nanofluids without surfactant. The viscosity of each sample was measured every hour after sonication under investigation conditions and repeated an average of three trials.

2.7 Taguchi's Statistical Design and Analysis for Ranking

Statistical analysis was conducted using a Taguchi method for ranking of considered parameters that are infuencing the viscosity of nanofuids [[44\]](#page-12-5). The present work aims to acquire minimum viscosity as the desired property of nanofluid, therefore the 'smaller is better' condition was chosen to obtain the optimum results. Experimentally obtained viscosity values and their corresponding parameters were used to construct the orthogonal array (L16) design. Experimental parameters and their levels for the L16 orthogonal model are shown in Table [1](#page-4-0).

The ranking of the infuencing parameters, such as temperature, nano-aluminium concentration and sonication time, and their optimum levels for achieving the minimum viscosity of the prepared nanofuid, were analysed using the Signal-to-Noise (S/N) ratio.

3 Results and Discussion

Experimental fndings of the viscosity of WEG based alumina nanofuids were presented in this section, with the efect of ultrasonication time, volume concentration of nanoparticles, and process temperatures.

3.1 Efect of Ultra‑sonication Time

The effect of ultrasonication time on dynamic viscosity of water-ethylene glycol (WEG)-based Al_2O_3 nanofluids is presented in Fig. [4a](#page-5-0)–d, as a function of various volume concentrations and process temperatures. It is noted that the dynamic viscosity of the nanofuid increases marginally for 1 h of sonication time. Thereafter, there is a decreasing trend with the sonication duration at all volume concentrations. A similar pattern in viscosity with a sonication duration has been observed for deionized water-based multi-walled carbon nanotubes nanofuid [\[45\]](#page-12-6) and ethylene glycol-based carbon nanotubes nanofluid $[46]$ $[46]$. A small rise in viscosity

was attributed to the presence of clusters of nanoparticles that provide resistance to the viscometer spindle. Later, it decreases due to the de-clustering of agglomerates with a sonication duration. At volume concentration of 0.01%, the rate of increment in viscosity for the sonication time of 1 h is lower at 45 °C compared to 30 °C. An increase in process temperature certainly reduces the increment of viscosity due to particle clusters. For given volume concentrations and temperatures, nanofuid viscosity values without sonication are referred to as the baseline values.

The baseline viscosity was 3.42 cP for 0.01% (lower volume concentration) at 30 \degree C, as the sonication time increased to 3 h the viscosity decreased by 1.75% to 3.36 cP. It is shown that ultrasonication does not alter the nanofuid viscosity considerably. Similarly, the decrease in viscosity was 10.6% for 0.2% (higher volume concentration). Ultrasonication has a major impact on the viscosity of WEGbased Al_2O_3 nanofluids. It is noted that there is an interrelation between the volume concentration of nanoparticles and the ultrasonication duration.

Likewise, at 45 \degree C, the sonication time increased from 0 to 3 h, and the viscosity value decreased by 3.8% for 0.01% (lower volume concentration). Similarly, a decrease in viscosity of 11.36% was observed for 0.2% (higher volume concentration). It is shown that concentration increased from 0.01 to 0.2%, at a higher temperature, the rate of reduction in viscosity was a combined effect of increased process temperature and ultrasonication duration. This combined efect apparently causes mobility of the particles and weakens the cohesive force between the particles [[47\]](#page-12-8).

In addition, there is an insignifcant decrease in viscosity value with sonication time for 0.01% and 0.05%. Despite using ultrasonic energy to disperse nanoparticles, a large volume of base fuid with a low fraction of nanoparticles absorbs ultrasonic energy. Sonication was more benefcial by adding more nanoparticles to the base fuid. In particular, a higher volume concentration (0.2%) shows a substantial shift in viscosity with sonication time compared to lower volume concentrations.

Continuous reduction in nanofuid viscosity is observed up to a sonication duration of 3 h. It was evident that the de-clustering of agglomerates stimulates the mobility of nanoparticles, leading to a reduction in viscosity. After that, viscosity is approached by a stable value for a higher sonication duration. It's because nanofuids reach their level of

Table 1 L16 Orthogonal array and parameter levels

Fig. 4 a–d Effect of ultrasonication duration on the viscosity of WEG-based AI_2O_3 nanofluid

homogeneity. It is observed that the prolonged sonication of nanofuid does not produce any desirable efect on viscosity. A similar pattern of viscosity is observed for the various processing temperatures and concentrations. Comparing all the results, the optimal sonication time to obtain the lowest nanofuid viscosity for the volume concentrations considered is 3 h.

3.2 Efect of Temperature

The effect of temperature on dynamic viscosity of waterethylene glycol (WEG)-based Al_2O_3 nanofluids under various sonication times and volume concentrations is shown in Fig. [5a](#page-6-0)–d. All samples of WEG-based Al_2O_3 nanofluids show a steady decrease in viscosity with a rise in temperature from 30 to 45 °C. The increase in processing temperature

of nanofuids reduces the strength of intermolecular attraction between base fuid and nanoparticles [\[3](#page-10-4)] and increases the Brownian motion of nanoparticles [\[45](#page-12-6)]. The addition of particles increases viscosity, but the decrease in viscosity is related to temperature. The increase in thermal energy of nanofuid helps to encourage Brownian motion, which leads to a decrease in the attractive forces of inter-particles and thus decreases viscosity of nanofuids.

For a volume concentration of 0.01%, a negligible shift in viscosity values with a volume concentration of 0.05% in volume at all temperatures for a sonication duration of 1 h is observed, as shown in Fig. [5a](#page-6-0). It shows that an increase in temperature decreases the viscosity for all concentrations. However, for 0.01% and 0.05%, the diference in viscosity would be almost the same, but little change is observed due to a small amount of nanoparticles added. Conversely,

Fig. 5 a–**d** Efect of temperature on dynamic viscosity for diferent nanoparticle concentrations

there is a considerable increase in the viscosity of nanofuid with addition of nanoparticles (0.1% and 0.2%). This is due to an increase in the volume concentration of the number of dispersed nanoparticles in the base fuid, which contributes to an increase in viscosity regardless of the increase in temperature. It is noteworthy that the decrement trend of viscosity of nanofuid was observed with an increase in process temperature. It may reduce the viscosity, which has been increased by added nanoparticles. Thus, it brings the viscosity values down to desired value. Ruan and Jocabi [\[46](#page-12-7)] performed experiments with ethylene glycol nanofluids based on carbon nanotubes and reported similar efects of temperature on viscosity.

Decreased viscosity with processing temperature was observed for all concentrations regardless of the sonication time, as shown in Fig. [5](#page-6-0)b. As compared to Fig. [5a](#page-6-0), b indicates a decrease in the magnitude of the viscosity due to the de-clustering of agglomerated nanoparticles in the base fuid. Further sonication time increased to 3 h, and the magnitude of the viscosity decreased to a certain level to all temperatures considered as shown in Fig. [5c](#page-6-0). It seems that an efective sonication realized at 3 h. It is noted that the sonication efect was not much realized, but a small shift in the magnitude of viscosity is observed at lower concentrations. At the same time, the viscosity value of 0.2% volume concentration is moved further downwards and reached a closer viscosity value of 0.1% for studied temperatures. Sim-ilar pattern is also observed in Fig. [5](#page-6-0)d. This figure shows a negligible change in magnitude of the viscosity between 0.1 and 0.2% for the 4 h sonication duration. Experimental results show that there is a substantial decrease in the viscosity magnitude of WEG-based Al_2O_3 nanofluid for a

3 h sonication period. This means that WEG-based Al_2O_3 nanofuid achieves homogeneity at a sonication time of 3 h leading to a signifcant declustering of agglomerates. Asadi and Alarif [\[30](#page-11-21)] found that extended sonication time might not have had any benefcial impact on nanofuid dispersion. It is derived from experimentation that the ultrasonication process was much needed to achieve lower viscosity for higher concentrations added nanofuid as compared to lower concentrations.

The distribution of nanoparticles in nanofuid under different conditions is presented schematically in Fig. [6.](#page-7-0) Null efect is characterized as an infnitesimal efect on the dispersion of nanoparticles due to sonication. Null efect was observed for lower concentrations of nanoparticles under 1 h and 3 h, irrespective of processing temperatures. Low-volume concentration does not take longer sonication time for dispersion of nanoparticles. At the same time, clusters were observed at a higher volume concentration under a minimal sonication time. This implies that the importance of the sonication efect would be needed to disperse higher concentrations of nanoparticles. This concludes that the concentration of alumina has a higher impact on the viscosity of nanofuids compared to process temperature and sonication time.

3.3 Efect of Cluster Size on Viscosity of Nanofuids

In order to study the efect of alumina cluster particle distribution on viscosity of WEG-based Al_2O_3 nanofluids, lower volume concentration (0.01%) and higher volume concentration (0.2%) at 1 h and 3 h sonicated conditions were considered. Figure [7](#page-8-0)a–d depicts the particle/cluster size of alumina-WEG nanofuids measured at room temperature by DLS method for sonication durations (1 h and 3 h) and volume concentrations (0.01 and 0.2%).

The mean cluster size of 0.01% nanofuid at 1 h of sonication was 150 nm, which decreased to 135 nm as the sonication time increased to 3 h. As the concentration of nanoalumina increased to 0.2%, the mean cluster size at 1 h of sonication was 215 nm, which decreased substantially to 175 nm after 3 h of sonication. Similarly, the observed viscosity of nanofuid was higher for 1 h sonicated samples relative to 3 h sonicated samples, as previously shown in this study. The obtained results suggest that increasing the cluster size of nanoparticles increases the dynamic viscosity of prepared nanofuids. This result is consistent with the fndings of Nguyen et al. [[26](#page-11-17)] and Jarahnejad et al. [\[48](#page-12-9)], who analysed the viscosity of $Al_2O_3/water$ nanofluids with cluster/particle sizes ranging from 36 to 300 nm and found that the viscosity of the nanofuid increased with the size of the nanoparticles. This may be because the molecular structure of nanofuids has changed. It is noted that the mean cluster size of nanofuids was substantially bigger than the primary nanoparticle size (average size 40 nm).

3.4 Relative Viscosity of WEG Based Al₂O₃ Nanofluid

Figure [8](#page-9-0)a–d describes the relative viscosity of WEG (50:50) based Al_2O_3 nanofluids with different volume concentrations, temperatures, and sonication durations. Loading nanoparticles in the base fluid increases the density of nanofluids, which increases the viscosity of nanofluids [\[8](#page-11-2)]. Generally, higher nanoparticle loading reduces the interparticle distance resulting in increased interaction between the nanoparticles.

From the observation, a maximum rise in relative viscosity is observed at a volume concentration of 0.2% under all considered sonication durations and temperatures. This indicates that the volume concentration contribution to the

Fig. 6 Sonication effect on the viscosity of Al_2O_3 nanofluids

Fig. 7 Alumina particle size of WEG based Al2O3 nanofuids **a** Concentration 0.01% @ 1 h sonication, **b** Concentration 0.01% @ 3 h sonication, **c** Concentration 0.2% @ 1 h sonication, and **d** Concentration 0.2% @ 3 h sonication

viscosity was large compared to other variables, including process temperature and ultrasonication time. Esfe and Saedodin [\[49\]](#page-12-10) and Kole and Dey [[50](#page-12-11)] have reported that the viscosity of nanofuids increases linearly with an increase in the volume fraction or concentration of nanoparticles.

It can also be shown from Fig. [8a](#page-9-0)–d that the relative viscosity decreases linearly with an increase in sonication time. This is the outcome of the ultrasonication efect on nanofuids arising from the de-clustering of nanoparticle agglomerates in WEG nanofuid. By comparing all cases, the minimum relative viscosity observed was 1.13, 1.14, 1.29, and 1.32 for 0.01%, 0.05%, 0.1%, and 0.2% of the volume concentration at 3 h and 45 °C, respectively.

3.5 S/N Ratios for Viscosity Measurements

The S/N ratio was used to determine the statistical parameters affecting the viscosity of WEG-based Al_2O_3 nanofluid. Table [2](#page-9-1) presents the S/N ratio of parameters considered for dynamic viscosity of nanofuids including their ranks.

Figure [9](#page-9-2) shows the main efect plot of the viscosity of WEG -based AI_2O_3 nanofluid for the considered parameters using an L16 Orthogonal design. The goal of the present work is to minimize the viscosity of the prepared nanofuid, which can be done at a temperature of 45 °C with a S/N ratio of-10.81. The addition of heat energy to nanofuid increases the random motion of nanoparticles and reduces the resistance of fuids, thus increasing the distance between particles. This leads to a major decrease in nanofuid viscosity. The fndings obtained are similar to previous experimental studies on nanofluids $[51, 52]$ $[51, 52]$ $[51, 52]$ $[51, 52]$. The minimum viscosity of the prepared nanofuid was achieved at a S/N ratio of -10.23 for the lowest aluminium concentration of 0.01%. Normally, a smaller quantity of nanoparticles may not have had a significant efect on the viscosity of the base fuid. Ultrasonication process offers good dispersion of nanoparticles by invoking de-clustering of agglomerates in an alumina based WEG nanofuid. Based on the results, the minimum viscosity of nanofuid was achieved at a S/N ratio of -10.88 for a sonication period of 3 h. The optimal sonication time was 3 h from both experimental and statistical analysis.

Based on the present statistical design, the desired combination of parameters to obtain a minimum nanofuid viscosity was a high processing temperature (45 °C), a low aluminium concentration (0.01%) and an intermittent sonication time (3 h). Other thermophysical properties have

Fig. 8 a–**d** Variation of relative viscosity with various temperature for each sonication duration

also been considered during the selection of parameters for the preparation of nanofuids for specifc engineering applications. However, the present research is limited to

Fig. 9 S/N ratio plot for the viscosity of Al_2O_3 based nanofluids

the investigation of viscosity, which is one of the essential characteristics of nanofuids.

The delta value for each parameter was determined by the diference in the maximum and minimum S/N ratio values. Based on delta value, rank for infuencing parameters on viscosity of nanofuid was determined. The current statistical study lists the order of parameters that follows alumina $concentration > temperature > sonication time.$

4 Conclusion

The present study reveals the variation in viscosity of α -Al₂O₃-WEG based nanofluids without surfactant. Influence of parameters such as ultra-sonication duration (0–4 h), process temperature (30–45 °C), and volume concentration $(0.01\%, 0.05\%, 0.1\%, 0.2\%)$ of nanoparticles on the dynamic viscosity and relative viscosity of α -Al₂O₃-WEG based nanofuids was studied through experimental and statistical analysis. The following observations are made from this study:

- 1. TEM results of α -Al₂O₃ reveal spherical morphology and are free from impurities. XRD results of α -Al₂O₃ show the characteristic peaks of rhombohedral Al_2O_3 structure.
- 2. Dynamic viscosity of the nanofuid increases as a result of nanoparticle clusters due to the nature of inter-particle attraction requiring strong ultrasonication. However, viscosity decreases with an increase in sonication duration due to the de-clustering effect of agglomerates, increasing inter-particle distance.
- 3. Sonication time increased from 0 to 3 h, a decrease in viscosity of 11.36% was observed for 0.2% volume concentration with precondition of higher process temperature (45 °C). After sonication time of 3 h, viscosity value becomes almost stable and nanofuids reach homogeneity for all considered temperatures and volume concentrations.
- 4. A low concentration nanoparticle-containing nanofuid requires a smaller ultrasonication, in other words, null efect was seen for lower concentrations irrespective of the temperature and sonication time. At the same time, clusters were observed at a higher volume concentration under a minimal sonication time (1 h).
- 5. Sonication efect was much required to disperse higher concentrations of nanoparticles efectively. This concludes that the concentration of alumina has a higher impact on the viscosity of nanofuids compared to process temperature and sonication time.
- 6. The addition of heat energy to nanofuid by increasing process temperature reduces the resistance of fuids

which decrease the viscosity of nanofuid for all concentrations, regardless of the sonication time.

- 7. The current study revealed that the clustering efect of alumina nanoparticles increases the viscosity of Al_2O_3 -WEG based nanofluids.
- 8. The minimum relative viscosity observed was 1.13, 1.14, 1.29, and 1.32 for 0.01%, 0.05%, 0.1%, and 0.2% of the volume concentration at 3 h and 45 °C, respectively. Since the loading of nanoparticles in WEG base fuid increases the interaction between nanoparticles and clustering resulting in increased relative viscosity of nanofuid.
- 9. In addition, based on the S/N ratio, the order of parameters afecting the viscosity value was the alumina con $centration > temperature > sonication time. The infer$ ence obtained from the statistical analysis is in line with experimental results.

Acknowledgements The authors would like to thank Sri Sivasubramaniya Nadar College of Engineering, Chennai for providing fnancial support through the SSN internal funding. We also acknowledge the technical support given by Prof. Dr. P. Ramasamy, Dean, SSN Research Centre.

Author Contributions RP—Resources, Supervision, Validation and Visualization; LC—Conceptualization, Investigation, Data acquisition; KR—Supervision, Writing- Review and Editing.

Funding This work is not funded by any agency.

Declarations

Conflict of interest The authors declare that they have no confict of interest. The authors declare that they have no known competing financial interests or personal relationships that could have appeared to infuence the work reported in this paper.

References

- 1. Choi, S.U.S.; Eastman, J.A.: Enhancing thermal conductivity of fuids with nanoparticles. Am. Soc. Mech. Eng. Fluids Eng. Div. FED. **231**, 99–105 (1995)
- 2. Ghadimi, A.; Saidur, R.; Metselaar, H.S.C.: A review of nanofuid stability properties and characterization in stationary conditions. Int. J. Heat Mass Transf. **54**, 4051–4068 (2011). [https://](https://doi.org/10.1016/j.ijheatmasstransfer.2011.04.014) doi.org/10.1016/j.ijheatmasstransfer.2011.04.014
- 3. Murshed, S.M.S.; Estellé, P.: A state of the art review on viscosity of nanofuids. Renew. Sustain. Energy Rev. **76**, 1134–1152 (2017).<https://doi.org/10.1016/j.rser.2017.03.113>
- 4. Gbadeyan, J.A.; Titiloye, E.O.; Adeosun, A.T.: Efect of variable thermal conductivity and viscosity on Casson nanofuid fow with convective heating and velocity slip. Heliyon **6**, e03076 (2020).<https://doi.org/10.1016/j.heliyon.2019.e03076>
- 5. Zarei, J.M.; Keshavarz, P.; Zerafat, M.M.; Sabbaghi, S.: Experimental investigation on the thermal conductivity of Triethylene

Glycol-Water-CuO nanofuids as a desiccant for dehydration process. Int. J. Nano Dimens. **11**, 74–87 (2020)

- 6. Babar, H.; Sajid, M.; Ali, H.: Viscosity of hybrid nanofuids: a critical review. Therm. Sci. **23**, 1713–1754 (2019). [https://doi.](https://doi.org/10.2298/tsci181128015b) [org/10.2298/tsci181128015b](https://doi.org/10.2298/tsci181128015b)
- 7. Sharifpur, M.; Adio, S.A.; Meyer, J.P.: Experimental investigation and model development for efective viscosity of Al2O3–glycerol nanofuids by using dimensional analysis and GMDH-NN methods. Int. Commun. Heat Mass Transf. **68**, 208–219 (2015)
- 8. Mishra, P.C.; Mukherjee, S.; Nayak, S.K.; Panda, A.: A brief review on viscosity of nanofuids. Int. Nano Lett. **4**, 109–120 (2014).<https://doi.org/10.1007/s40089-014-0126-3>
- 9. Sekrani, G.; Poncet, S.: Ethylene- and propylene-glycol based nanofuids: a litterature review on their thermophysical properties and thermal performances. Appl. Sci. (2018). [https://doi.org/](https://doi.org/10.3390/app8112311) [10.3390/app8112311](https://doi.org/10.3390/app8112311)
- 10. Saleemi, M.; Vanapalli, S.; Nikkam, N., et al.: Classical behavior of alumina (Al2O3) nanofuids in antifrogen N with experimental evidence. J. Nanomater. **2015**, 1–7 (2015)
- 11. Okonkwo, E.C., Wole-Osho, I., Almanassra, I.W. et al.: An updated review of nanofuids in various heat transfer devices. J. Therm. Anal. Calorim. 1–56 (2020)
- 12. Aishwarya, V.; Suganthi, K.S.; Rajan, K.S.: Transport properties of nano manganese ferrite-propylene glycol dispersion (nanofuids): New observations and discussion. J. Nanoparticle Res. (2013).<https://doi.org/10.1007/s11051-013-1774-3>
- 13. Patra, A.K.; Nayak, M.K.; Misra, A.: Viscosity of nanofuids-a review. Int. J. Thermofuid Sci. Technol. **7**, 70202 (2020)
- 14. Thomas, S.; Sobhan, C.B.P.: A review of experimental investigations on thermal phenomena in nanofuids. Nano Res. Lett. **6**, 377 (2011)
- 15. Murshed, S.M.S.; De. Castro, C.A.N.: Superior thermal features of carbon nanotubes-based nanofuids–a review. Renew Sustain. Energy Rev. **37**, 155–167 (2014)
- 16. Aybar, H.Ş; Sharifpur, M.; Azizian, M.R., et al.: A review of thermal conductivity models for nanofuids. Heat Transf. Eng. **36**, 1085–1110 (2015)
- 17. Estellé, P.; Halelfadl, S.; Maré, T.: Lignin as dispersant for waterbased carbon nanotubes nanofluids: impact on viscosity and thermal conductivity. Int. Commun. Heat Mass Transf. **57**, 8–12 (2014)
- 18. Qiu, L.; Zhu, N.; Feng, Y., et al.: A review of recent advances in thermophysical properties at the nanoscale: from solid state to colloids. Phys. Rep. **843**, 1–81 (2020). [https://doi.org/10.1016/j.](https://doi.org/10.1016/j.physrep.2019.12.001) [physrep.2019.12.001](https://doi.org/10.1016/j.physrep.2019.12.001)
- 19. Bashirnezhad, K.; Bazri, S.; Safaei, M.R., et al.: Viscosity of nanofuids: a review of recent experimental studies. Int. Commun. Heat Mass Transf. **73**, 114–123 (2016). [https://doi.org/10.](https://doi.org/10.1016/j.icheatmasstransfer.2016.02.005) [1016/j.icheatmasstransfer.2016.02.005](https://doi.org/10.1016/j.icheatmasstransfer.2016.02.005)
- 20. Meyer, J.P.; Adio, S.A.; Sharifpur, M.; Nwosu, P.N.: The Viscosity of nanofuids: a review of the theoretical, empirical, and numerical models. Heat Transf. Eng. **37**, 387–421 (2016). [https://doi.org/10.](https://doi.org/10.1080/01457632.2015.1057447) [1080/01457632.2015.1057447](https://doi.org/10.1080/01457632.2015.1057447)
- 21. Yang, L.; Xu, J.; Du, K.; Zhang, X.: Recent developments on viscosity and thermal conductivity of nanofuids. Powder Technol **317**, 348–369 (2017). [https://doi.org/10.1016/j.powtec.2017.04.](https://doi.org/10.1016/j.powtec.2017.04.061) [061](https://doi.org/10.1016/j.powtec.2017.04.061)
- 22. Routbort, J.L.; Singh, D.; Timofeeva, E.V.; Yu, W.; France, D.M.: Pumping power of nanofluids in a flowing system. J. Nanoparticle Res. **13**, 931–937 (2011). [https://doi.org/10.1007/](https://doi.org/10.1007/s11051-010-0197-7) [s11051-010-0197-7](https://doi.org/10.1007/s11051-010-0197-7)
- 23. Soto, A.; Gaster, T.; Golden, C.; Vafaei, S.: Theoretical investigation of thermal conductivity and viscosity of nanofuids. Proc. Therm. Fluids Eng. Summer Conf. (2020). [https://doi.org/10.](https://doi.org/10.1615/TFEC2020.nma.032014) [1615/TFEC2020.nma.032014](https://doi.org/10.1615/TFEC2020.nma.032014)
- 24. Suganthi, K.S.; Anusha, N.; Rajan, K.S.: Low viscous ZnO–propylene glycol nanofuid: a potential coolant candidate. J. Nanoparticle Res. **15**, 1–16 (2013)
- 25. Lee, J.H.; Hwang, K.S.; Jang, S.P.; Lee, B.H.; Kim, J.H.; Choi, S.U.S.; Choi, C.J.: Efective viscosities and thermal conductivities of aqueous nanofuids containing low volume concentrations of Al2O3 nanoparticles. Int. J. Heat Mass Transf. **51**, 2651–2656 (2008)
- 26. Nguyen, C.T.; Desgranges, F.; Roy, G., et al.: Temperature and particle-size dependent viscosity data for water-based nanofuids–hysteresis phenomenon. Int. J. heat fuid fow. **28**, 1492–1506 (2007)
- 27. Asadi, A.; Pourfattah, F.; Miklósszilágyi, I., et al.: Efect of sonication characteristics on stability, thermophysical properties, and heat transfer of nanofuids: a comprehensive review. Ultrason. Sonochem. (2019). [https://doi.org/10.1016/j.ultsonch.2019.](https://doi.org/10.1016/j.ultsonch.2019.104701) [104701](https://doi.org/10.1016/j.ultsonch.2019.104701)
- 28. Chen, Z.; Shahsavar, A.; Al-Rashed, A.; Afrand, M.: The impact of sonication and stirring durations on the thermal conductivity of alumina-liquid paraffin nanofluid: an experimental assessment. Powder Technol. **360**, 1134–1142 (2020). [https://doi.org/](https://doi.org/10.1016/j.powtec.2019.11.036) [10.1016/j.powtec.2019.11.036](https://doi.org/10.1016/j.powtec.2019.11.036)
- 29. Sonawane, S.S.; Khedkar, R.S.; Wasewar, K.L.: Efect of sonication time on enhancement of efective thermal conductivity of nano TiO2-water, ethylene glycol, and paraffin oil nanofluids and models comparisons. J. Exp. Nanosci. **10**, 310–322 (2015). [https://](https://doi.org/10.1080/17458080.2013.832421) doi.org/10.1080/17458080.2013.832421
- 30. Asadi, A.; Alarif, I.M.: Efects of ultrasonication time on stability, dynamic viscosity, and pumping power management of MWCNTwater nanofuid: an experimental study. Sci. Rep. **10**, 1–10 (2020). <https://doi.org/10.1038/s41598-020-71978-9>
- 31. Mahbubul, I.M.; Chong, T.H.; Khaleduzzaman, S.S.; Shahrul, I.M.; Saidur, R.; Long, B.D.; Amalina, M.A.: Effect of ultrasonication duration on colloidal structure and viscosity of aluminawater nanofuid. Ind. Eng. Chem. Res. **53**, 6677–6684 (2014). <https://doi.org/10.1021/ie500705j>
- 32. Yang, J.C.; Li, F.C.; Zhou, W.W.; He, Y.R.; Jiang, B.C.: Experimental investigation on the thermal conductivity and shear viscosity of viscoelastic-fuid-based nanofuids. Int. J. Heat Mass Transf. **55**, 3160–3166 (2012). [https://doi.org/10.1016/j.ijheatmasstrans](https://doi.org/10.1016/j.ijheatmasstransfer.2012.02.052) [fer.2012.02.052](https://doi.org/10.1016/j.ijheatmasstransfer.2012.02.052)
- 33. Kwak, K.Y.; Kim, C.Y.: Viscosity and thermal conductivity of copper oxide nanofuid dispersed in ethylene glycol. Korea-Australia Rheol. J. **17**, 35–40 (2005)
- 34. Buonomo, B.; Manca, O.; Marinelli, L.; Nardini, S.: Efect of temperature and sonication time on nanofuid thermal conductivity measurements by nano-fash method. Appl. Therm. Eng. **91**, 181–190 (2015). [https://doi.org/10.1016/j.applthermaleng.2015.](https://doi.org/10.1016/j.applthermaleng.2015.07.077) [07.077](https://doi.org/10.1016/j.applthermaleng.2015.07.077)
- 35. Gangadevi, R.; Vinayagam, B.K.; Senthilraja, S.: Efects of sonication time and temperature on thermal conductivity of CuO/ water and Al2O3/water nanofuids with and without surfactant. Mater. Today Proc. **5**, 9004–9011 (2018). [https://doi.org/10.](https://doi.org/10.1016/j.matpr.2017.12.347) [1016/j.matpr.2017.12.347](https://doi.org/10.1016/j.matpr.2017.12.347)
- 36. Adio, S.A.; Sharifpur, M.; Meyer, J.P.: Infuence of ultrasonication energy on the dispersion consistency of Al_2O_3 –glycerol nanofluid based on viscosity data, and model development for the required ultrasonication energy density. J. Exp. Nanosci. **11**, 630–649 (2016).<https://doi.org/10.1080/17458080.2015.1107194>
- 37. He, Y.; Jin, Y.; Chen, H.; Ding, Y.; Cang, D.; Lu, H.: Heat transfer and fow behaviour of aqueous suspensions of TiO2 nanoparticles (nanofuids) fowing upward through a vertical pipe. Int. J. Heat Mass Transfer. **50**, 2272–2281 (2007). [https://doi.org/10.1016/j.](https://doi.org/10.1016/j.ijheatmasstransfer.2006.10.024) [ijheatmasstransfer.2006.10.024](https://doi.org/10.1016/j.ijheatmasstransfer.2006.10.024)
- 38. Hamed Mosavian, M.T.; Zeinali Heris, S.; Etemad, S.G.; Nasr Esfahany, M.: Heat transfer enhancement by application of

- 39. Ashrae, A.: Handbook-Fundamentals. Atlanta, USA (2005)
- 40. Yu, W.; Xie, H.; Chen, L.; Li, Y.: Enhancement of thermal conductivity of kerosene-based Fe3O4 nanofuids prepared via phasetransfer method. Colloids Surf. A Physicochem. Eng. Asp. **355**, 109–113 (2010)
- 41. Sawicka, D.; Cieśliński, J.T.; Smolen, S.: A comparison of empirical correlations of viscosity and thermal conductivity of water-ethylene glycol-Al2O3 nanofuids. Nanomaterials **10**, 1–24 (2020).<https://doi.org/10.3390/nano10081487>
- 42. Beck, M.P.; Yuan, Y.; Warrier, P.; Teja, A.S.: The thermal conductivity of alumina nanofuids in water, ethylene glycol, and ethylene glycol + water mixtures. J. Nanoparticle Res. **12**, 1469–1477 (2010).<https://doi.org/10.1007/s11051-009-9716-9>
- 43. Afrand, M.; Abedini, E.; Teimouri, H.: How the dispersion of magnesium oxide nanoparticles efects on the viscosity of waterethylene glycol mixture: experimental evaluation and correlation development. Phys. E Low-Dimensional Syst. Nanostruct. **87**, 273–280 (2017).<https://doi.org/10.1016/j.physe.2016.10.027>
- 44. Abadeh, A.; Passandideh-Fard, M.; Maghrebi, M.J.; Mohammadi, M.: Stability and magnetization of Fe3O4/water nanofuid preparation characteristics using Taguchi method. J. Therm. Anal. Calorim. **135**, 1323–1334 (2019)
- 45. Sadri, R.; Ahmadi, G.; Togun, H.; Dahari, M.; Kazi, S.N.; Sadeghinezhad, E.; Zubir, N.: An experimental study on thermal conductivity and viscosity of nanofuids containing carbon nanotubes. Nanoscale Res. Lett. **9**, 4–13 (2014). [https://doi.org/10.1186/](https://doi.org/10.1186/1556-276X-9-151) [1556-276X-9-151](https://doi.org/10.1186/1556-276X-9-151)
- 46. Ruan, B.; Jacobi, A.M.: Ultrasonication effects on thermal and rheological properties of carbon nanotube suspensions.

Nanoscale Res. Lett. **7**, 1–14 (2012). [https://doi.org/10.1186/](https://doi.org/10.1186/1556-276X-7-127) [1556-276X-7-127](https://doi.org/10.1186/1556-276X-7-127)

- 47. Mahbubul, I.M.; Saidur, R.; Amalina, M.A.; Niza, M.E.: Infuence of ultrasonication duration on rheological properties of nanofuid: an experimental study with alumina–water nanofuid. Int. Commun. Heat Mass Transf. **76**, 33–40 (2016)
- 48. Jarahnejad, M.; Haghighi, E.B.; Saleemi, M.; Nikkam, N.; Khodabandeh, R.; Palm, B.; Toprak, M.S.; Muhammed, M.: Experimental investigation on viscosity of water-based Al2O3 and TiO2 nanofuids. Rheol. Acta. **54**, 411–422 (2015). [https://doi.org/10.](https://doi.org/10.1007/s00397-015-0838-y) [1007/s00397-015-0838-y](https://doi.org/10.1007/s00397-015-0838-y)
- 49. Hemmat Esfe, M.; Saedodin, S.: An experimental investigation and new correlation of viscosity of ZnO-EG nanofuid at various temperatures and diferent solid volume fractions. Exp. Therm. Fluid Sci. **55**, 1–5 (2014). [https://doi.org/10.1016/j.expthermf](https://doi.org/10.1016/j.expthermflusci.2014.02.011) [usci.2014.02.011](https://doi.org/10.1016/j.expthermflusci.2014.02.011)
- 50. Kole, M.; Dey, T.K.: Efect of aggregation on the viscosity of copper oxide-gear oil nanofuids. Int. J. Therm. Sci. **50**, 1741–1747 (2011).<https://doi.org/10.1016/j.ijthermalsci.2011.03.027>
- 51. Hemmat Esfe, M.; Rahimi Raki, H.; Sarmasti Emami, M.R.; Afrand, M.: Viscosity and rheological properties of antifreeze based nanofuid containing hybrid nano-powders of MWCNTs and TiO2 under diferent temperature conditions. Powder Technol. **342**, 808–816 (2019). [https://doi.org/10.1016/j.powtec.2018.10.](https://doi.org/10.1016/j.powtec.2018.10.032) [032](https://doi.org/10.1016/j.powtec.2018.10.032)
- 52. Toghraie, D.; Mokhtari, M.; Afrand, M.: Molecular dynamic simulation of copper and platinum nanoparticles Poiseuille fow in a nanochannels. Phys. E Low-dimensional Syst. Nanostruct. **84**, 152–161 (2016)

