RESEARCH ARTICLE - MECHANICAL ENGINEERING

# **Flow Behavior of Lead-Free Machinable Brass During Hot Compression Deformation**

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**Abstract** Hot compression tests were carried out to study the deformation behaviors of a lead-free machinable brass using Gleeble-1500 thermal simulator in the temperature range of 823–973 K and the strain rate range of  $0.01-10 s^{-1}$ . The results show that the flow behavior of the lead-free machinable brass is strongly influenced by strain rate and temperature, and the flow stress increases with increasing strain rate and decreasing temperature. The constitutive equations incorporating the effects of strain rate and temperature have been established to model the hot deformation behavior of this alloy. The reliability of the developed constitutive model was demonstrated by the mean percentage error of 10.82% and the correlation coefficient of 0.98. Moreover, the flow stability/instability of the lead-free machinable brass was carefully investigated on the basis of dynamic material modeling approach. It was found that plastic deformation was stable for processing conditions in which the strain rate range was  $1-10 s^{-1}$  within the temperature range of 823–923 K.

**Keywords** Lead-free machinable brass · Hot compression deformation · Flow behavior · Constitutive model

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### الخلاصة

لقد أجريت اختبارات الضغط الساخن لدراسة سلوكيات التشوه من النحاس المشكل الخالي من الرصاص باستخدام محاكاة جليبل-1500 الحرارية في درجات حرارة تتراوح بين 823-973 كيلفن ونطاق معدل إجهاد من0.01\_10 / ثانية. وبينت النتائج أن سلوك تدفق النحاس المشكل الخالي من الرصاص يتأثر بشدة بمعدل الإجهاد ودرجة الحرارة ، ويزداد النونرَ مع زيادة معدل ندفق الإجهاد وخفض درجة الحرارة. وتم إنشاء المعادلات التأسيسية المتضمنة لآثار معدل الإجهاد ودرجة الحرارة لنمذجة سلوك التشوه الساخن من هذه السبائك. وقد أثبتت موثوقية النموذج التأسيسي المطور من خلال متوسط خطأ نسبي من 10.82٪ ومعامل ارتباط منّ 0.98. وعلاوة على ذلك، فقد تم التحقيق في استقرار / عدم استقرار تدفق النحاس المشكل الخالي من الرصاص بعناية على أساس نهج نمذجة المواد الديناميكي وقد وجد أن تشوه البلاستيك كان مستقرأ لظروف المعالجة التي تضمنت نطاق معدل الإجهاد من 1-10 / ثانية ضمن در جات حر ار ة تتر او ح بين 823-923 كيلفن.

### **1 Introduction**

Lead-free machinable brasses have attracted great attentions at various industries due to the growing environmental concerns. Development of easily machinable lead-free brass has been considered by many researchers [\[1](#page-6-0)[–4\]](#page-7-0). However, different deformation behaviors of this series of alloys may easily cause the defects of microstructure and property after hot deformation, which can limit the further development of these materials. Therefore, it is necessary to understand hot deformation behavior and flow characteristic of this series of alloys in more details. So far, great attention is given to study machinability, tensile properties and corrosion properties of lead-free machinable brasses in the current scientific literature [\[5](#page-7-1)[–7](#page-7-2)]. However, there is still a lack of in-depth knowledge on the high temperature flow behavior of leadfree machinable brasses.



Flow behavior of materials during hot deformation processes is rather complex, because it is significantly affected by various working parameters such as the deformation degree, temperature and strain rate [\[8](#page-7-3)[–10\]](#page-7-4). Hence, the understandings of hot deformation behavior of metals or alloys are of vital importance for designing the forming processes. The constitutive relation which can relate the flow stress, strain rate and temperature may generally be used to describe the plastic flow behaviors of metals or alloys. The constitutive model was capable to predict and characterize the flow behavior of materials in different regions of the hot compression stress–strain curves which included work hardening, dynamic recovery, dynamic recrystallization and flow instability [\[11\]](#page-7-5). Investigation on the flow behavior of lead-free machinable brasses at elevated temperatures is thus essential for optimization of the hot working process.

The main objective of this study was to evaluate the flow behavior of the lead-free machinable brass by hot compression tests under various deformation conditions. Based on the experimental data, constitutive equations for the flow stress dependence on strain rate and temperature are applied to describe the plastic flow property of the material. The reliability of the constitutive equation is assessed by the mean error of the peak flow stress between the predicted and experimental results. The flow stability was also investigated using a dynamic material modeling approach. The results will provide useful guidelines for the optimization of processing parameters of this lead-free machinable brass.

### **2 Material and Experimental Procedure**

### 2.1 Material

The material used in this study is newly developed in our lab, and its nominal chemical composition (wt%) is Cu–36.3Zn– 1.76Mg–0.5Bi–0.5Sb. In addition, the original microstructure of the as-received lead-free brass consisting of  $\alpha$  phase,  $\beta$  phase and machinable particles is exhibited in Fig. [1.](#page-1-0)

### 2.2 Experimental Procedures

The hot compression tests were conducted on a Gleeble-1500 thermal simulator in the strain rate range of  $0.01-10 s^{-1}$  and the temperatures range of 823–973 K. Cylindrical specimens with 15 mm height and 10 mm diameter were prepared to carry out compression tests. In order to minimize the friction between the specimen and die during hot deformation, the flat ends of the specimen were recessed to a depth of 0.2 mm deep to entrap the lubricant of graphite mixed with machine oil, as shown in Fig. [2.](#page-1-1) The specimens prior to isothermal compression were heated to the designed temperature and held for 3 min in order to obtain a homogeneous heat dis-



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**Fig. 1** Microstructure of the as-received lead-free machinable brass

<span id="page-1-0"></span>

**Fig. 2** Typical appearance of the specimens of the lead-free machinable brass before the hot compression tests

<span id="page-1-1"></span>tribution. The reduction in height is 60% at the end of the compression tests. During preheating and testing, a positive argon gas pressure was maintained in the heating chamber to avoid oxidation.

## **3 Results and Discussion**

### 3.1 Flow Behavior

Typical true stress–true strain curves obtained from the hot compression tests of the lead-free machinable brass in a wide range of deformation temperature and strain rate conditions are depicted in Fig. [3.](#page-2-0) As is seen, the flow stress level is significantly affected by the temperature and strain rate. The flow stress decreases with the increase in temperature and the decrease in strain rate. Meanwhile, the flow curves exhibit the obvious flow softening phenomena. The



<span id="page-2-0"></span>**Fig. 3** True stress–true strain curves for the lead-free machinable brass alloy under different deformation temperatures. **a** 823 K, **b** 873 K, **c** 923 K, **d** 973 K

higher the deformation temperature and the lower the strain rate, the greater the flow softening tendency becomes. The cause can lie in the fact that the higher temperature and lower strain rate promote the higher mobility of grain boundary and growth of dynamically recrystallized grains. The peak stresses on the true stress–strain curves further suggest that the dynamic recrystallization and dynamic flow softening of the lead-free machinable brass occurs during hot compression.

### 3.2 Constitutive Analysis of the Flow Stress

Based on these flow curves obtained in the hot compression tests, a material constitutive equation was developed to further understand the plastic flow behavior of the experimental lead-free machinable brass. To formulate the constitutive equation of the alloy, the Arrhenius equation which was widely used to describe the relationship between the strain rate, temperature and flow stress was utilized in this study [\[12](#page-7-6)[–14](#page-7-7)]. Three types of Arrhenius equations are shown as follows:

$$
\dot{\varepsilon} = A\sigma^{n_1} \exp\left(-\mathcal{Q}/R_0 T\right) \tag{1}
$$

<span id="page-2-1"></span>
$$
\dot{\varepsilon} = A \exp(\beta_1 \sigma) \exp(-Q/R_0 T) \tag{2}
$$

$$
\dot{\varepsilon} = A \left[ \sinh \left( \alpha_0 \sigma \right) \right]^n \exp \left( -\frac{Q}{R_0 T} \right) \tag{3}
$$

where  $R_0$  denotes the universal gas constant (8.314 J mol<sup>-1</sup> K<sup>-1</sup>),  $\dot{\varepsilon}$  is strain rate (s<sup>-1</sup>),  $\sigma$  is the flow stress (MPa) for a given true stain, *Q* is the deformation activation energy (kJ mol<sup>-1</sup>) and *T* is temperature (K).  $\beta_1$ ,  $n_1$ ,  $\alpha_0$ , *n* and *A* are the material constants, where  $\alpha_0 = \beta_1/n_1$ . It is worth to say that since the peak stress is more commonly applied due to easy identifiability on the flow curve [\[15\]](#page-7-8),  $\sigma$  is considered to be the peak flow stress in the present study. It has been reported that Eqs.  $(1)$ – $(3)$  are the most frequently used equations describing the thermally activated process during hot deformation. Equations [\(1\)](#page-2-1) and [\(2\)](#page-2-1) are suitable for low stress regime (i.e.,  $\alpha_0 \sigma < 0.8$ ) and high stress regime (i.e.,  $\alpha_0 \sigma > 1.2$ ), respectively, whereas Eq. [\(3\)](#page-2-1) is a more general form which can be applied to stresses over a wider range. Because Eq. [\(3\)](#page-2-1) is found to be more representative and most suitable form for explaining the deformation behavior, the hyperbolic sine law equation was applied in the present work.







<span id="page-3-1"></span>**Fig. 4** Relationships between **a** ln ( $\dot{\epsilon}$ ) and ln( $\sigma$ <sub>p</sub>); **b** ln ( $\dot{\epsilon}$ ) and  $\sigma$ <sub>p</sub>



<span id="page-3-2"></span>**Fig. 5** Evaluating the values of **a** *n* by fitting ln[sinh( $\alpha_0\sigma_p$ )] – ln ( $\dot{\epsilon}$ ) and **b** Q by fitting ln[sinh( $\alpha_0\sigma_p$ )] – 1/*T* 

### *3.2.1 Determination of Material Parameters for Hot Deformation Conditions*

The true stress–strain data obtained from compression tests under different strain rate and temperature conditions were used to determine the material constant of the aforementioned constitutive equation. To achieve this purpose, the flow stress value at the curve maximum is taken as an example for demonstrating solution procedure of the involved material constants.

For low and high stress levels, Eqs. [\(1\)](#page-2-1) and [\(2\)](#page-2-1) result in the following relationships, respectively:

<span id="page-3-0"></span> $\ln \dot{\varepsilon} = n_1 \ln \sigma_p + \ln A - Q/R_0 T$  (4)

$$
\ln \dot{\varepsilon} = \beta_1 \sigma_{\rm p} + \ln A - Q/R_0 T \tag{5}
$$

Taking the partial differentiation of Eqs. [\(4\)](#page-3-0) and [\(5\)](#page-3-0) with respect to the peak flow stress  $(\sigma_{p})$  at constant temperature, one would get

<span id="page-3-4"></span>
$$
\left[\frac{\ln\left(\sigma_{\rm p}\right)}{\ln\dot{\varepsilon}}\right]_{T} = \frac{1}{n_1} \tag{6}
$$

$$
\left[\frac{\sigma_{\rm p}}{\ln \dot{\varepsilon}}\right]_T = \frac{1}{\beta_1} \tag{7}
$$

Figure [4a](#page-3-1), b shows that the values of  $1/n_1$  and  $1/\beta_1$  are obtained from the slope of the lines in the plots of  $\ln (\sigma_{p})$  – ln ( $\dot{\epsilon}$ ) and  $\sigma_p$  – ln ( $\dot{\epsilon}$ ). The mean value of the slopes was considered as the values of  $n_1$  and  $\beta_1$ , which was found to be 5.4389 and 0.1196MPa, respectively. This gives the value of  $\alpha_0 = \beta_1/n_1 = 0.02199 \text{ MPa}^{-1}.$ 

<span id="page-3-3"></span>For the whole stress values including low and high stress levels, taking the logarithm on both sides of the above Eq. [\(3\)](#page-2-1) gives

$$
\ln\left[\sinh\left(\alpha_0\sigma_p\right)\right] = \frac{1}{n}\ln\dot{\varepsilon} + \frac{Q}{nR_0T} - \frac{1}{n}\ln A\tag{8}
$$

At a constant temperature during the hot deformation process, the value of *n* can be acquired by making a liner fitting of  $\ln[\sinh(\alpha_0 \sigma_p)] - \ln(\dot{\varepsilon})$ , that is:

$$
\left[\frac{\partial \ln \left[\sinh\left(\alpha_0 \sigma_p\right)\right]}{\partial \left(\ln \dot{\varepsilon}\right)}\right]_T = \frac{1}{n} \tag{9}
$$



<span id="page-4-1"></span>**Table 1** Determined materials parameters for the lead-free machinable brass

| Material                         | $\alpha_0 \, (\text{MPa}^{-1})$ n | $Q$ (kJ/mol) $A (s^{-1})$                                |  |
|----------------------------------|-----------------------------------|--|--|
| Lead-free<br>machinable<br>brass | 0.02199                           | 3.5472 426.817 $\pm$ 20 3.4307 $\times$ 10 <sup>23</sup> |  |

From a group of parallel and straight lines in Fig. [5a](#page-3-2), it can be easily evaluated for the *n*-values, by averaging the values of *n* under different temperatures. The average of *n* value was found to be 3.5472. In the same way, for a particular strain rate, differentiating Eq. [\(8\)](#page-3-3) gives

<span id="page-4-0"></span>
$$
\left[\frac{\partial \ln \left[\sinh\left(\alpha_0 \sigma_p\right)\right]}{\partial \left(T^{-1}\right)}\right]_{\hat{\varepsilon}} R_0 n = Q \tag{10}
$$

Equation [\(10\)](#page-4-0) gives the value of *Q* from the variations of flow stress with strain rate and temperature according to the hyperbolic sine function. Therefore, by substituting the values of temperatures and flow stresses obtained at fixed strain rate into Eq. [\(10\)](#page-4-0), the value of *Q* can be derived from the slope of plotting  $\ln[\sinh(\alpha_0\sigma_p)]$  as a function of  $1/T$ , as shown in Fig. [5b](#page-3-2). It can be seen that the linear correlation between ln[sinh( $\alpha_0 \sigma_p$ )] and  $1/T$  is relatively high; thus, the value of activated energy  $(Q)$  can be obtained as  $426.817 \pm 20$  kJ/mol.

Since the value of *Q* has been obtained, it is easy to evaluate the value of the material constant *A* in Eq. [\(7\)](#page-3-4) to be  $3.4307 \times 10^{23}$  s<sup>-1</sup> according to the linear regression of the ln[sinh( $\alpha_0 \sigma_p$ )] – ln ( $\dot{\epsilon}$ ) plots at each temperature as shown in Fig. [5a](#page-3-2).

Table [1](#page-4-1) shows the calculated values of all material parameters required for the flow stress prediction of the lead-free machinable brass. It was found that the activation energy of  $426.817 \pm 20$  kJ/mol was similar to those reported values of other copper based alloys, in which the activation energies were typically in the range of 214–572 kJ/mol [\[16](#page-7-9)[–18\]](#page-7-10).

#### *3.2.2 Comparison of the Peak Flow Stresses*

In order to test the adequacy of the developed equation, a comparison between the measured and predicted results from the above-mentioned computation is carried out. According to Eq. [\(3\)](#page-2-1) at constant temperature and strain rate, a general expression for the peak flow stress can be written as

<span id="page-4-2"></span>
$$
\sigma_{\rm p} = \frac{1}{\alpha_0} \ln \left\{ \left( \dot{\varepsilon} \exp\left(\frac{Q}{R_0 T}\right) / A \right)^{1/n} + \left[ \left( \dot{\varepsilon} \exp\left(\frac{Q}{R_0 T}\right) / A \right)^{2/n} + 1 \right]^{1/2} \right\}
$$
(11)



<span id="page-4-4"></span>**Fig. 6** Correlation between the experimental and predicted peak flow stresses data from the developed constitutive equation of the lead-free machinable brass alloy

When the values of material constants from Table [1](#page-4-1) are substituted into Eq.  $(11)$ , the following expression to predict peak flow stress of the investigated lead-free machinable brass at a given temperature and strain rate can be obtained:

<span id="page-4-3"></span>
$$
\sigma_{\rm p} = \frac{1}{0.02199} \ln \left\{ \left( \frac{\dot{\varepsilon}}{3.4307 \times 10^{23}} \right)^{1/3.5472} + \left[ \left( \frac{\dot{\varepsilon}}{3.4307 \times 10^{23}} \right)^{2/3.5472} + 1 \right]^{1/2} + 1 \right\}
$$
(12)

The comparison of the measured and predicted peak flow stresses by Eq. [\(12\)](#page-4-3) under all the experimental conditions is shown in Fig. [6.](#page-4-4) In most cases, the predicted flow stresses show a high agreement with the experimental flow stresses at lower rates compared with those at higher rates. The mean percentage error of all peak flow stresses shown in Fig. [6](#page-4-4) is 10.82% with the square of the correlation coefficient  $R^2$  = 0.98. This suggests that the proposed deformation constitutive model can agree well with the experimental values and can be employed to analyze the flow behavior during the hot forming process of the lead-free machinable brass.

#### **4 Flow Stability During Hot Deformation**

It has shown that the hot flow behavior of the investigated lead-free machinable brass is obviously sensitive to strain rate and temperature. For example, an increase of strain rate greatly enhances the flow stress, whereas the flow stress is apparently decreased due to an increase in temperature. At higher deformation rate, large amount of heat is often pro-





<span id="page-5-0"></span>**Fig. 7** Evaluating the value of m by plotting log  $\sigma_p$  versus log ( $\dot{\epsilon}$ )

duced. As a result, the material exhibits flow softening behavior and ultimately material instability can occur. Dynamic material modeling [\[19](#page-7-11)[–21](#page-7-12)] was widely used to characterize the deformation behavior. This method has been successful in correlating flow stability/instability condition and the plastic flow behavior through the strain rate sensitivity *m* and the temperature sensitivity *s* at specific temperature and strain rate. In order to effectively evaluate the flow stability of the lead-free machinable brass during hot deformation, the dynamic material modeling stability criteria developed by Malas and Seetharaman [\[22\]](#page-7-13) were used in the present study.

In terms of the principles of the dynamic material modeling, the plastic stable zones can be established during the steady energy dispersion processes, if and only if the following four criteria are met for stable flow simultaneously:

<span id="page-5-3"></span>
$$
0 < m < 1 \tag{13}
$$

$$
\frac{\partial m}{\partial (\log \dot{\varepsilon})} \le 0 \tag{14}
$$

$$
s > 1 \tag{15}
$$

$$
\frac{\partial s}{\partial (\log \dot{\varepsilon})} \le 0 \tag{16}
$$

where the strain rate sensitivity  $m = [\partial \log(\sigma_p)/\partial \log \dot{\varepsilon}]_T$  can be determined from the slopes of the flow peak stress versus strain rate at different temperatures as shown in Fig. [7,](#page-5-0) and the temperature sensitivity  $s = 1/T[\partial \log(\sigma_p)/\partial(1/T)]_{\varepsilon}$  can be obtained according to the slopes of the  $ln(\sigma_p)$  versus  $1/T$ graph at different temperatures as shown in Fig. [8.](#page-5-1) The two material parameters are considered to be related to the manner of the energy dispersion during hot deformation.

The strain rate sensitivity *m* is an important material property, which can significantly influence hot workability of metals or alloys. Figure [9](#page-5-2) shows the variation of *m* versus the strain rate at given temperatures. It could be found that the strain rate sensitivity *m* varied from 0.13 to 0.21 and hence





**Fig. 8** Evaluating the value of n by plotting  $\ln(\sigma_n)$  versus 1/T

<span id="page-5-1"></span>

<span id="page-5-2"></span>**Fig. 9** The strain rate sensitivity *m* versus  $log(\dot{\epsilon})$  at different temperatures

the criterion in Eq. [\(13\)](#page-5-3) was always satisfied for all temperatures and strain rates. However, the rate of change of *m* with respect to  $log(\dot{\varepsilon})$  is relatively complex. The rate of change of *m* was always negative or equal to zero for the temperatures of 823 and 873 K in the strain rate range of  $0.01-10 s^{-1}$ , which implied that the criterion in Eq. [\(14\)](#page-5-3) was fully satisfied. For the temperature of 923 K, the criterion in Eq. [\(14\)](#page-5-3) was not satisfied in the strain rate range of  $0.01-0.1$  s<sup>-1</sup>, whereas the criterion was enough satisfied in the strain rate range of 0.1–10 s−<sup>1</sup> due to the negative or zeroth rate of change of *m*. When the temperature was further increased to 973 K, the rate of change of *m* was always positive for all strain rates and hence the criterion in Eq. [\(14\)](#page-5-3) was not satisfied. This indicated that material instability might occur during hot deformation.

The other important factor affecting hot deformation behavior is the temperature sensitivity *s* in Eq. [\(15\)](#page-5-3), which indicates that the rate of net entropy production is always positive as required for stable flow conditions in an irreversible process [\[23](#page-7-14)]. The variation of *s* versus the strain rate for



<span id="page-6-1"></span>**Fig. 10** The temperature sensitivity *s* versus  $log (ε)$  at different temperatures

<span id="page-6-2"></span>Table 2 Conditions of satisfaction for each criterion according to dynamic material modeling approach for the lead-free machinable brass

|  |                    | Criteria $T(K)$ $\dot{\varepsilon}$ (0.01-0.1 s <sup>-1</sup> ) $\dot{\varepsilon}$ (0.1-1 s <sup>-1</sup> ) $\dot{\varepsilon}$ (1-10 s <sup>-1</sup> ) |          |          |
|--|--------------------|--|----------|----------|
| $0 \le m \le 1823 - 973$   |                    |  | $\circ$  | $\circ$  |
| $\frac{\partial m}{\partial (\log \dot{\varepsilon})} \leq 0$ 823–873 $\times$ |                    |  | $\circ$  | $\circ$  |
|  | $873 - 923 \times$ |  | $\circ$  | $\circ$  |
|  | $923 - 973 \times$ |  | $\times$ | $\times$ |
| $s > 1$ 823-973 o  |                    |  | $\circ$  | $\circ$  |
| $\frac{\partial s}{\partial (\log \varepsilon)} \leq 0$ 823–873 $\times$       |                    |  | $\times$ | $\circ$  |
|  | $873 - 923 \times$ |  | $\times$ | $\Omega$ |
|  | $923 - 973 \times$ |  | $\times$ | $\circ$  |

The symbols such as "∘" and "×" denote satisfied or unsatisfied condition for each criterion

different temperatures is plotted in Fig. [10.](#page-6-1) It is clear that the temperature sensitivity *s* varied from 7 to 11 and hence the criterion in Eq.  $(15)$  was always satisfied for the entire experimental range. However, the rates of change of the temperature sensitivity *s* with respect to  $log(\epsilon)$  were positive for the strain rate range of  $0.01-1$  s<sup>-1</sup> within the temperature range of 823–923 K and the strain rate range of 0.01–0.1 s<sup>-1</sup> at the temperature of 973 K. These deformation conditions did not satisfy the criterion in Eq. [\(16\)](#page-5-3). Only when the strain rate range was  $1-10 s^{-1}$  within the temperature range of 823– 923 K and the strain rate range of  $0.1-10 s^{-1}$  for the temperature of 973 K, the criterion in Eq. [\(16\)](#page-5-3) was satisfied.

The state of satisfaction for each criterion at different range of temperatures and strain rates is further summarized in Table [2.](#page-6-2) It has been known that only when all four criteria of the dynamic material modeling are verified simultaneously, the flow stability can be determined. Therefore, it can be reasonably concluded that plastic deformation of the lead-free machinable brass is stable at strain rates between 1 and  $10 s^{-1}$  and the temperature range of 823–923 K.

### **5 Conclusions**

The hot deformation behaviors of the lead-free machinable brass were investigated by the compression tests in the temperature range of 823–973 K and the strain rate range of  $0.01-10 s^{-1}$ . The main conclusions can be obtained as follows:

- 1. The flow behavior strongly depends on strain rate and temperature, and the flow stress increases with the increase of strain rate and the decrease of temperature.
- 2. On the basis of the experimental data from the hot compression tests, the material constants (i.e.,  $\alpha_0$ , *n*,  $Q$  and *A*) of the Arrhenius equation with hyperbolic sine law were obtained. The activation energy *Q* for the investigated strain rate and temperature ranges was  $426.817 \pm$ 20 kJ/mol, which was in reasonable agreement with copper alloys reported before.
- 3. The constitutive equation incorporating the effects of temperature and strain rate was developed to describe the flow stress behavior of the lead-free machinable brass. The high correlation coefficient  $(R^2 = 0.98)$ and the mean percentage error  $(10.82\%)$  for the flow stress obtained from the established model indicate that the model can be used to numerically simulate the hot deformation behavior of the lead-free machinable brass.
- 4. Dynamic material modeling can be effectively utilized to summarize flow stability/instability of the lead-free machinable brass. In the investigated range, the optimal conditions for hot working of this alloy can be the strain rate range of  $1-10 s^{-1}$  and between 823 and 923 K, where the plastic flow is considered to be stable.

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