SHORT COMMUNICATION

In vivo relationship between bound and free insulin in patients with diabetes having anti‑insulin antibodies

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Abstract

Objective The Scatchard plot of anti-insulin antibodies is curvilinear, indicating heterogeneity in binding sites. However, the relationship between bound insulin (B) and free insulin (F) in patients with anti-insulin antibodies has not yet been elucidated. This study aimed to determine this relationship.

Methods We studied two insulin-treated patients with diabetes who had high titers of anti-insulin antibodies. The B and F levels were measured using daily blood samples. Assuming that the law of mass action is applicable to the reactions between insulin and anti-insulin antibody forms, we plotted the bound-to-free ratio (B/F) vs. B using patient data. We also performed an equilibrium binding assay in vitro.

Results Some of the B/F vs. B plots of the daily variation showed an approximately linear relationship, while the Scatchard plots of in vitro data became curvilinear.

Conclusion Our study suggests that the one-site (high-affinity site) of anti-insulin antibodies accounts, for the most part, for insulin pharmacokinetics within physiological insulin concentrations.

Keywords Anti-insulin antibodies · Scatchard plot · Bound insulin · Free insulin

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Introduction

The equilibrium binding assay [\[1](#page-5-0)] is widely used to quantify and characterize anti-insulin antibodies. In this assay, insulin is added to deinsulinized sera at various concentrations in vitro, and the affinity and capacity of anti-insulin antibodies are calculated based on bound insulin (B) and free insulin (F). The Scatchard plot, which shows the bound-to-free ratio (B/F) vs. B, is curvilinear for anti-insulin antibodies, indicating heterogeneity in binding sites [\[1](#page-5-0), [2](#page-5-1)]. However, the relationship between B and F in patients with anti-insulin antibodies has not yet been clarifed in detail.

The law of mass action should apply to the reactions between insulin and anti-insulin antibodies [\[3](#page-5-2)]. If anti-insulin antibodies have a single binding site, the Scatchard plot shows a straight line, following the equation $[3, 4]$ $[3, 4]$ $[3, 4]$ $[3, 4]$:

$$
B/F = (B_{\text{max}}-B)/K_a,
$$

where B_{max} is the binding capacity and K_a is the affinity constant.

When there are \geq 2 binding sites, a nonlinear relationship is obtained, following the equation [[4\]](#page-5-3):

$$
B = \sum (B_{\text{max}i} \times K_{ai} \times F) / (1 + K_{ai} \times F).
$$

This equation can be transformed into:

$$
B/F = \sum (B_{\text{max}i} \times K_{ai}) / (1 + K_{ai} \times F)
$$
 (1)

Assuming that the quantity and characterization of antiinsulin antibodies remains constant and the reaction of insulin and anti-insulin antibodies is at equilibrium in vivo, the relationship between B and F is represented by the equation derived from the law of mass action. Since insulin is continuously produced and used, the reaction cannot be at complete equilibrium in practice. However, the reaction proceeds toward equilibrium. Therefore, samples of B and F should be distributed according to the relationship in Eq. [1](#page-1-0). Based on this hypothesis, we evaluated the relationship between B and F in vivo.

Materials and methods

Patients

Two insulin-treated patients with diabetes, who had high titers of anti-insulin antibodies, were included in this study. The criteria of high titer of anti-insulin antibodies is unclear in general. A past study reported that it was difficult to perform Scatchard analysis when ¹²⁵I-Insulin binding rate≤50% [\[5\]](#page-5-4). Therefore, to perform the analysis we selected patients who had ¹²⁵I-Insulin binding rate \geq 70%. Written informed consent was obtained from the patients. These patients had postprandial hyperglycemia but no apparent hypoglycemic episodes, and were admitted to Kanazawa University Hospital (Kanazawa, Japan). Table [1](#page-1-1) provides the clinical information of the two patients. Patient 1 had a low titer of glutamic acid decarboxylase (GAD) antibody (2.0 U/mL). He had a history of insulin allergy and tested positive for insulin-specifc IgE antibody. His anti-insulin antibodies had not been tested before admission. He was treated for hypothyroidism with levothyroxine 75 μg, but

The bold texts represent above the reference ranges

FPG fasting plasma glucose, *F-CPR* fasting C-peptide immunoreactivity, *GAD* Ab glutamic acid decarboxylase antibody, *IA-2 Ab* insulinoma-associated antigen-2 antibody, *TPO Ab* thyroid peroxidase antibody, *Tg Ab* thyroglobulin antibody, TSH receptor *Ab* thyroid-stimulating hormone receptor antibody

had no thyroid autoantibodies. Patient 2 had received insulin therapy for 9 years, and his anti-insulin antibodies were detected 7 years ago $(^{125}I$ -Insulin binding rate 26.7%). He had subclinical hypothyroidism but no thyroid autoantibodies. Neither patient had taken sulfhydryl-containing drugs or other drugs, reportedly associated with insulin autoimmune syndrome, and had other autoimmune antibodies. Their medical history and the absence of hypoglycemic episodes suggested their anti-insulin antibodies were caused by exogenous insulin therapy.

Anti‑insulin antibodies (125I‑Insulin binding rate) and C‑peptide immunoreactivity

 125 I-Insulin binding rate was measured using a radioimmunoassay kit (Yamasa Corporation, Chiba, Japan). C-peptide immunoreactivity was determined using a chemiluminescent enzyme immunoassay with Lumipulse Presto C-peptide (Fujirebio Inc., Tokyo, Japan).

Daily variation of plasma glucose and plasma insulin

We evaluated the daily variation of plasma glucose, F, and total insulin (T) fve times daily (premeal and 2 h after meals, except after dinner) or six times daily (before and 2 h after meals). We measured F using polyethylene glycol [PEG] 6000 precipitation and T using the acid-PEG method according to a previous report $[6]$ $[6]$ $[6]$, with modifications. B was calculated as T minus F [[7\]](#page-5-6). Patient 1 took tests twice over 3 months. For the frst test, patient 1 was administered liraglutide and insulin lispro as follows: before breakfast (14 units), lunch (6 units), and dinner (4 units). Data from this test were referred to as patient 1–1. For the second test, insulin therapy was withdrawn for 21.5 days, and metformin, pioglitazone, and liraglutide were administered. Data from this test were referred to as patient 1–2. Patient 2 was withdrawn from insulin detemir for 9.5 days and treated with metformin, repaglinide, and liraglutide. Immunoreactive insulin (IRI) was measured using a sandwich enzyme immunoassay system (E test Tosoh II IRI; Tosoh Corporation, Tokyo, Japan). For patient 1–1, the IRI was measured using a chemiluminescence immunological assay (Chemilumi Insulin; Kyowa Medics, Tokyo, Japan). The conversion factor (μIU/mL to pmol/L) for IRI was 6.0.

Scatchard plot (B/F vs. B plot) and K_a and B_{max} **by the one‑site model in vivo**

Using the daily variation measurement data of B and F, we plotted B/F vs. B. We subsequently analyzed the linearity of the plot using a linear regression model. For the Scatchard analysis, the negative slope equals K_a and the

x-axis intercept equals B_{max} [[8\]](#page-5-7). However, this is not the optimal method because linearizing the transformation dis-torts experimental errors [[9\]](#page-5-8). To evaluate the K_a and B_{max} of the anti-insulin antibodies more accurately, we analyzed the saturation binding curve in vivo by nonlinear least-squares ftting of the one-site model.

Equilibrium binding assay and Scatchard plot in vitro estimated with a two‑site model

We also measured the equilibrium of binding in vitro using 125 I-labeled human insulin [\[1](#page-5-0)]. Antibody-bound insulin was removed from serum samples using dextran-coated charcoal. Then, the serum was incubated with $125I$ -labeled human insulin, along with formulations containing varying concentrations of excess unlabeled insulin. Finally, the reaction mixture was precipitated with γ -globulin and PEG, and the radioactivity of the precipitate was counted. Serum samples were collected before breakfast to measure daily variation. We calculated the K_a and B_{max} using a weighted nonlinear regression technique with a weighting factor of $1/Y^2$ fitting of the two-site model.

Statistical analyses and curve ftting

Linear regression and curve ftting were performed using GraphPad Prism ver.6.07 (GraphPad Software, Inc., La Jolla, CA, USA).

Results

Figure [1A](#page-4-0) shows the daily fasting data before breakfast. Figure [1](#page-4-0)B shows the daily variations in T, F, and plasma glucose. In both cases, T reached its lowest point before breakfast, and changes in the F level tended to follow those of the T level.

The B/F vs. B plots in vivo for patient 1–1 and patient 2 were approximately linear (Fig. [1C](#page-4-0)). The linear regression analysis results were as follows: patient 1–1 R squared = 0.770; patient 2 R squared = 0.8925. The B/F vs. B plot of patient 1–2 was distributed in a negative slope. In both cases, the Scatchard plots in vitro became curvilinear (Fig. [1D](#page-4-0)).

Discussion

Some of B/F vs. B plots in vivo showed an approximately linear relationship. This indicates that the binding reached near equilibrium in patients and the one-site of anti-insulin antibodies mainly determined insulin pharmacokinetics.

 \overline{a}

Fig. 1 The result of daily variation and an equilibrium binding assay ◂in vitro. **A** Fasting data. **B** Daily variation in total insulin, free insulin, and plasma glucose. C Scatchard plot (B/F vs. B plot) and K_a and B_{max} by the one-site model in vivo. **D** Scatchard plot and K_a and B_{max} by the two-site model in vitro. Patient 1–1 and patient 1–2 indicate patient 1's data from the frst and second test, respectively. *T-IRI* total immunoreactive insulin (pmol/L), *F-IRI* free immunoreactive insulin (pmol/L), *PG* plasma glucose (mg/dL), *BB* before breakfast, *AB* after breakfast, *BL* before lunch, *AL* after lunch, *BD* before dinner, *AD* after dinner, *B* bound insulin (10^{-8} M) *F* free insulin, *B/F* bound/free ratio, K_a affinity constant (1/10⁻⁸ M), B_{max} binding capacity (10⁻⁸ M)

Only two data points were deemed inconclusive. Therefore, we theoretically supported this fnding. Curvilinear Scatchard plots in vitro showed apparent linear regions [[1,](#page-5-0) [2](#page-5-1)]. We consider that the approximately linear B/F *vs* B plots in vivo correspond to the linear regions of the Scatchard plots in vitro because the in vivo insulin levels were limited.

In the two-site model, the relationship between B and F is defined by the equation $[4, 10]$ $[4, 10]$ $[4, 10]$ $[4, 10]$:

$$
B/F = B_{\text{max1}} \times K_{a1}/(1 + K_{a1} \times F) + B_{\text{max2}} \times K_{a2}/(1 + K_{a2} \times F)
$$
\n(2)

Equation [2](#page-4-1) can be transformed to Eq. [3:](#page-4-2)

$$
B/F = - (K_{a1} + K_{a2} + K_{a1} \times K_{a2} \times F) \times B
$$

+ $K_{a1} \times B_{max1} + K_{a2} \times B_{max2}$
+ $K_{a1} \times K_{a2} \times (B_{max1} + B_{max2}) \times F$ (3)

Equations [2](#page-4-1) and [3](#page-4-2) are both curvilinear. However, when the value of F approaches 0, Eq. [3](#page-4-2) approximates the following linear expression:

$$
B/F = -(K_{a1} + K_{a2}) \times B + K_{a1} \times B_{max1} + K_{a2} \times B_{max2}
$$
\n(4)

This may be understood using patient 1–1 in vitro data $(K_{a1}:0.381, K_{a2}:0.00258, B_{max1}:16.35, B_{max2}:37.12).$

Two-site model: $B/F = -(0.3836 + 0.0009833 \times F)$ \times B + 6.325 + 0.05256 \times F

When F approaches 0, this equation approximates the next equation:

 $B/F = -0.3836 \times B + 6.325$

We show this visually using a graph. Figure [2](#page-5-9) shows a comparison of Eqs. [2](#page-4-1) and [4](#page-4-3) using in vitro data from patient 1–1. When the value of F is lower than 1.0 (10^{-8} M), B becomes lower than 4.6 (10^{-8} M), and the two graphs become similar. We suggest that the plot line in vivo (Fig. [1](#page-4-0)C) is not a completely straight line but instead approximates the straight part of a hyperbola.

The equilibrium binding assay in vitro showed that K_{a1} > > K_{a2} and $K_{a1} \times B_{max1}$ > > $K_{a2} \times B_{max2}$. Therefore, Eq. [4](#page-4-3) is strongly affected by K_{a1} and B_{max1} , indicating that the high-affinity sites of anti-insulin antibodies have a

predominant infuence on insulin pharmacokinetics. Some previous reports have supported this fnding [\[7](#page-5-6), [11](#page-6-1)[–13](#page-6-2)].

Because of the polyclonal nature of anti-insulin antibodies, the two-site model might not be a perfect model since three or more binding sites might exist [\[2](#page-5-1), [14](#page-6-3)]. Using the three-site model, the relationship between B and F is defned by:

$$
B/F = B_{max1} \times K_{a1}/(1 + K_{a1} \times F)
$$

+ $B_{max2} \times K_{a2}/(1 + K_{a2} \times F)$
+ $B_{max3} \times K_{a3}/(1 + K_{a3} \times F)$

When the value of F approaches 0, this equation approximates the following linear expression:

$$
B/F = -(K_{a1} + K_{a2} + K_{a3}) \times B + K_{a1} \times B_{max1} + K_{a2} \times B_{max2} + K_{a3} \times B_{max3}
$$

The equation of the more binding-site model defned as Eq. [1](#page-1-0) also approaches a linear expression when F approaches 0. Therefore, our theory holds good for more binding-site models.

It is uncertain whether our results would apply to patients other than patients 1 and 2 described in this study. We suggest that the condition that the B/F vs. B plots of the daily variation become linear is as follows.

- 1. The quantity and characterization of anti-insulin antibodies remain constant and the reaction of insulin and anti-insulin antibodies is at equilibrium in vivo. This condition is necessary for the B/F vs. B plot to become a line (straight or curve line).
- 2. The binding capacity of the high-affinity site in vivo exceeds the range of insulin concentrations. When insulin concentrations exceed the binding capacity in vivo, the B/F vs. B plots should be curvilinear.

Another patient with type 1 diabetes mellitus who had a moderate titer of anti-insulin antibodies underwent the same evaluation (Supplemental Figure S1). This patient tested for evaluation of the infuence of anti-insulin antibodies because she had brittle diabetes. The B/F vs. B plot for this patient did not show a line. This may be because the binding of insulin and the antibodies did not reach equilibrium. Whether the binding reaches near-equilibrium may depend on various factors such as association and dissociation rate constants of anti-insulin antibodies [\[15](#page-6-4)], or the provided rate of endogenous and exogeneous insulin. The two patients might have unique anti-insulin antibodies that were easy to reach nearequilibrium and had a high binding capacity.

Our study had some limitations. The accuracy of the measurement of T and F levels was not guaranteed. PEG precipitation of plasma infuences the results of insulin

Fig. 2 Comparison of $B/F = B_{\text{max1}} \times K_{a1}/(1 + K_{a1} \times F) +$ $+ B_{\text{max2}} \times K_{a2}/(1 + K_{a2} \times F)$ and $B/F = -(K_{a1} + K_{a2}) \times B +$ $K_{a1} \times B_{max1} + K_{a2} \times B_{max2}$ using K_{a1} , K_{a2} , B_{max1} and B_{max2} of patient 1–1 in vitro. K_{a1} : 0.381 (1/10⁻⁸ M), K_{a2} : 0.00258 (1/10⁻⁸ M), B_{max1} : 16.35 (10⁻⁸ M), B_{max2} : 37.12 (10⁻⁸ M). Green circles: $B/F = B_{\text{max1}} \times K_{a1}/(1 + K_{a1} \times F) + B_{\text{max2}} \times K_{a2}/(1 + K_{a2} \times F).$ Red squares: $B/F = -(K_{a1} + K_{a2}) \times B + K_{a1} \times B_{max1} + K_{a2} \times B_{max2}$

immunoassay [[16\]](#page-6-5). This infuence depends on the immunoassay. And according to a previous report, the crossreaction rate for Chemilumi Insulin (IRI for patient 1–1) is 86.7% for lispro [\[17\]](#page-6-6). Therefore, the data of patient 1–1 could not be compared with other data. However, it should not infuence our main point, which is the linear relationship in the B/F vs. B plots in vivo. Additionally, F levels may have changed in the samples before measurement [\[18,](#page-6-7) [19\]](#page-6-8). It is possible that, after sampling, insulin and antiinsulin antibodies came closer to equilibrium, and B/F vs. B showed a more linear relationship. However, it is difficult to completely solve this problem because centrifugation and PEG are time-consuming [[19](#page-6-8)]. Another limitation is the small sample size. Since patients with high titers of anti-insulin antibodies are rare, we could not expand the sample size. The essential point of this article is the theoretical explanation of the latter part.

In conclusion, the two patients described in our study showed an approximately linear relationship in the B/F vs. B plots in vivo. This relationship is a novel fnding of insulin pharmacokinetics in patients with diabetes who have antiinsulin antibodies. These results indicate that the one-site (high-affinity site) of anti-insulin antibodies mainly determines insulin pharmacokinetics within physiological insulin concentrations.

Supplementary Information The online version contains supplementary material available at<https://doi.org/10.1007/s13340-023-00641-1>.

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Author contributions HA conceived and designed the study, analyzed the data, and drafted the manuscript for publication. SK designed the study and reviewed the manuscript. DC supervised the study, contributed to discussion, and reviewed and edited the manuscript. MK, MU, KY, KA, and TY reviewed the manuscript. All authors edited, reviewed, and approved the fnal version of the manuscript. HA is the guarantor of this work, and, as such, had full access to all the data in the study and takes responsibility for the integrity of the data and the accuracy of the data analysis.

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Data availability The deidentifed participant data will be shared on a request basis. Please contact Hiroyuki Asaka (daitoku@muse.ocn. ne.jp). But the data used in this study has been restricted by the Kanazawa University IRB.

Declarations

Conflict of interest None of the authors have any potential conficts of interest associated with this research.

Human and animal rights All procedures followed were in accordance with the ethical standards of the responsible committee on human experimentation (institutional and national) and/or with the Helsinki Declaration of 1964 and later versions. This study was approved by the ethics committee of Kanazawa University (approval No. 1917-1/ September 16, 2015, approval No. 1917-2/February 21, 2017).

Informed consent Written informed consent was obtained from the patients.

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