ORIGINAL PAPER

Numerical simulations of streamwise vortices on a high-lift wing

T. Landa¹ · R. Radespiel¹ · J. Wild²

Received: 25 November 2015 / Revised: 1 September 2016 / Accepted: 23 September 2016 / Published online: 7 October 2016 © Deutsches Zentrum für Luft- und Raumfahrt e.V. 2016

Abstract This contribution presents results of numerical simulations on a generic high-lift configuration. Properties of the computational grid are briefly described. The numerical simulations are performed with the DLR-TAU-Code at different angles of attack up to stall. The Menter-SST eddy viscosity turbulence model and the JHh-v2 Reynolds stress model are applied. Streamwise vortices arise at the edge of a slat, which is cut off in the spanwise direction, and the corresponding edge of the clean nose. These vortices interact with the flow along the suction side of the wing. While proceeding downstream, a strong interaction between the vortices is observed for high angles of attack. The behavior of the vortex system and the influence on the high-lift performance of the configuration is characterized. In particular, the effect of the applied turbulence models of different types on the prediction of the vortex behavior is shown within this contribution.

Keywords High-lift aerodynamics - Longitudinal vortices - Computational fluid dynamics - Turbulence modeling

List of symbols

 b Span (m)

 C_{D} Drag coefficient (–)

This paper is based on a presentation at the German Aerospace Congress, September 22–24, 2015, Rostock, Germany.

 \boxtimes T. Landa t.landa@tu-braunschweig.de

¹ Institute of Fluid Mechanics, TU Braunschweig, Hermann-Blenk-Str. 37, 38108 Brunswick, Germany

² DLR Institute of Aerodynamics and Flow Technology, Lilienthalplatz 7, 38108 Brunswick, Germany

Subscript

n Normal to leading edge

1 Introduction

Modern aircraft operate within a large range of velocities. To obtain the required lift at low speeds during take-off and landing, the lift coefficient is increased by high-lift devices, such as leading edge and trailing edge devices. Nowadays, common high-lift systems consist of a single slotted slat (leading edge) and a single slotted Fowler flap (trailing edge) [\[1](#page-12-0)]. Compared to multi-slotted high-lift devices, such a configuration is a good compromise between aerodynamic high-lift performance and the complexity and the weight of the high-lift system. The basic aerodynamic effects of slotted multi-element high-lift configurations are well understood [[2\]](#page-12-0). Nevertheless, the prediction of maximum lift of realistic configurations requires to consider details of the three-dimensional high-lift device.

A significant influence on the aerodynamic behavior is observed due to (underwing) engine integration. At the position of the engines pylon, the slat is cut out. At the spanwise end faces of the intercepted slat and at the corresponding faces of the clean nose part above, the pylon vortices are induced. Moreover, the flow around the engine causes two additional vortices. The result is a complex system consisting of different vortices trailing downstream close to the suction side of the wing. The vortex system strongly influences the flow behavior in this region, which generally leads to a significant loss of maximum achievable lift [\[3](#page-12-0)]. These losses can be compensated by a nacelle strake, which is mounted at the engine. The nacelle strake causes a particular vortex. This vortex positively influences the flow field downstream causing an increase in maximum lift.

In recent years, much effort has been taken to investigate the effects of vortex systems on the high-lift behavior of realistic configurations. Aiming at a better understanding of the complex vortex behavior, numerous experimental and numerical investigations have been performed in various research projects. Important contributions in this area of research are provided within the European projects EUROLIFT and EUROLIFT II [\[4–8](#page-12-0)]. These projects include extensive numerical and experimental studies of different high-lift configurations with different levels of complexity, which provides a deep understanding of the influence of different components on the lift and drag behavior. Particularly, the effects on maximum lift were analyzed. Another remarkable work is the research project high-lift inflight validation (HINVA) [[9\]](#page-12-0). Within this project, numerical and experimental investigations with detailed models of an Airbus A320 and large-scale flight tests have been performed, to improve the prediction of the aerodynamic performance at maximum lift. However, the prediction of the aerodynamic effects at maximum lift including the behavior of the vortex system with numerical methods is still a challenging task [\[10](#page-12-0)]. Similar findings derive from the NASA High-lift prediction workshop. The main focus was to predict the correct flow behavior with modern numerical methods at a generic three-element high-lift configuration without slat interception and engine. At this configuration, a vortex system in the streamwise direction occurs at the wing tip. Results of various numerical simulations showed significant differences compared to experimental results [\[11](#page-12-0)]. Particularly, the behavior of the streamwise vortex system differed. It was shown that the applied turbulence model has a large influence on the prediction of the behavior of the vortex system [\[12](#page-12-0)].

Further studies dealt with the influence of different turbulence models on the prediction of streamwise vortices by analyzing the tip vortex of a half-wing model without high-lift devices. Significant differences in the behavior of the vortex occur. Simulations with eddy viscosity models show a rapid decay of the vortex that does not correspond to experimental data. In contrast, the decay of the streamwise vortex predicted with Reynolds stress models is significantly lower. The results with Reynolds stress models (RSMs) are in good agreement with the experimental data [\[13](#page-12-0), [14\]](#page-12-0).

To approach a better prediction of the vortex systems and their influence on wing stall, in this contribution, the vortex system at a slat end is investigated in a generic setup. Particularly, the effect of the applied turbulence model on the behavior of the vortex system is of great interest. For the fundamental studies herein, we use a simplified configuration, which is a generic high-lift configuration without an engine. The slat is finite, representing half of a slat cut-out for engine integration on commercial aircraft. With this geometry, it is possible to investigate one part of the vortex system in detail, which is still relevant for realistic configurations. A detailed description of the geometry is shown in Sect. [2.2](#page-2-0).

Recently, the authors presented results of simulations with the Menter-SST turbulence model [\[15](#page-12-0)]. Based on these results, the computational grid has been improved. With this modified grid, simulations with the Menter-SST eddy viscosity model and the JHh-v2 RSM turbulence model are performed. The results of these simulations are presented in this contribution. The investigations aim at a deeper understanding of the interaction between longitudinal vortices and the suction side of the high-lift wing at different angles of attack. Particularly, the effects on stall behavior and maximum lift are of great interest. The numerical methods, the geometry and the computational grid used for the simulations herein are described in detail in the first part of this contribution. In addition, an overview of the performed simulations is given. The results are presented and discussed. The global flow field and the characteristics of the vortex system are shown. In the last part, the results are summarized, and an outlook to future work is given.

2 Numerical setup

2.1 Methods

For the simulations presented in this contribution, the DLR TAU-Code (Release 2014.2.0) is used as flow solver [\[16](#page-12-0), [17](#page-12-0)]. With this software package, it is possible to compute flow fields on structured, unstructured or hybrid grids by solving the Reynolds-averaged Navier–Stokes equations based on a finite volume method. To compute the fluxes, central and different upwind spatial discretization

schemes are available. For time-stepping, either a semiimplicit LU-SGS scheme or explicit Runge–Kutta schemes can be applied. The TAU-Code offers different convergence acceleration techniques like local time-stepping, residual smoothing, and a multigrid approach. To accelerate the numerical solution process at nearly incompressible flow conditions, low Mach number preconditioning is applied. For the simulations presented in this contribution, the central discretization scheme to calculate fluxes and the LU-SGS scheme for time-stepping were used. The previously described acceleration techniques have been applied.

To simulate turbulent flows, the TAU-Code follows the Reynolds-averaged Navier–Stokes (RANS) approach combined with a turbulence model. Various turbulence models of different types are implemented. Here, the twoequation Menter-SST (Shear Stress Transport) and the JHhv2 (Jakirlić Hanjalić homogeneous) turbulence models are applied. The Menter-SST model $[18]$ $[18]$ is based on the hypothesis of Boussinesq and belongs to the class of eddy viscosity models. Although the ability of these models to accurately simulate vortices is known to be limited [\[13](#page-12-0), [14\]](#page-12-0), the robustness of this model is of great advantage to create a fundamental understanding of the flow around this geometry. Furthermore, the results serve as a basis for comparison with the applied Reynolds stress model. The JHh-v2 RSM model follows a second-moment closure approach, which means that a transport equation is solved for each component of the Reynolds stress tensor. This model is based on the JHh turbulence model developed by Jakirlić and Hanjalić [[19\]](#page-12-0) and has been extended by Probst [\[20](#page-12-0)]. Recent work shows promising results in vortex prediction using the JHh-v2 turbulence model [[14,](#page-12-0) [21\]](#page-12-0).

2.2 Geometry

The generic three-dimensional configuration is based on the DLR F15 high-lift airfoil. In recent years, this airfoil has been extensively investigated both in experimental and numerical studies, and thus, a high level of knowledge is achieved [\[21](#page-12-0), [22\]](#page-12-0). The following parameters define the position of the slat and the Fowler flap related to the airfoil geometry normal to the leading edge.

- Slat: 28.8 $^{\circ}$ deflection, 2.09 % overlap, 2.61 % gap,
- Fowler flap: 30.3° deflection, 1.52 % overlap, 0.968 % gap.

The generic high-lift configuration is a swept wing $(\varphi = 25^{\circ})$ without twist and dihedral. The span is $b = 1.7525$ m and the chord is constant for the whole wing. With retracted flaps, the chord normal to the leading edge is $c_n = 0.6$ m. This value corresponds to a chord in the streamwise direction of $c_{ref} = 0.662$ m, which is taken as the reference chord length for the evaluation. At the

Fig. 1 Top view on the high-lift configuration

inner part of the wing ($\eta = 0$ –62.6 %), the slat is retracted resulting in a two-element configuration with a clean. Outboard, the slat is extended with the geometric parameters mentioned above. The flap is extended along the whole span. At the spanwise end, the wing is cut off in line of flight, and no additional wingtip-device is mounted. Figure 1 shows the geometry of the three-dimensional high-lift configuration.

2.3 Grids

For the generation of the computational grids, the commercial software Gridgen (V 15.18, Pointwise, Inc.) has been used. The reference grid is a hybrid grid consisting of structured and unstructured parts. The surface grid contains mostly structured areas, only the spanwise end faces of slat, wing, and the Fowler flap are discretized with an unstructured surface grid. The structured volume part of the grid consists of 60 layers to ensure a good resolution of the boundary layers by structured cells. The initial wall spacing is $\Delta s_{init} = 0.003$ mm, such that dimensionless wall distances of y^+ < 1 are obtained largely, which is required to accurately predict the boundary layer. Only in regions of suction peaks or strongly vortex-influenced regions, y^+ values are slightly greater than 1. The expansion rate in the wall-normal direction within the structured layers to resolve the boundary layer is lower than 1.18 globally. Thus, the boundary layer is resolved with more than 35 cells at a chordwise position of $x/c_{\text{ref}} = 0.1$ and more than 40 cells at a chordwise position of $x/c_{\text{ref}} = 0.8$. The maximum aspect ratios close to the wall are $(\Delta x/\Delta s_{\text{init}})$ - $_{\text{max}} \approx 2000$ in the chordwise direction and $(\Delta y/$ Δs_{init} _{max} \approx 3333 in the spanwise direction. The latter one

occurs at an undisturbed position inboard at the wing. Within the vortex-influenced region, the spanwise aspect ratio is significantly lower ($\Delta y/\Delta s_{\text{init}} \approx 666$). Structured blocks have also been used for the wake region behind the flap and in the slat and wing cove. In addition, the region downstream of the slat cut-off is also resolved with additional structured cells above the structured part to resolve the boundary layer. Here, a rectangular box with constant cell spacing in the y- and z-directions is used to account for the presence of streamwise vortices. The box is directly connected to the structured cells above the surface. Hence, numerical smearing of vortices due to tetrahedral cells is minimized using equally spaced hexahedral cells. An improvement of capturing the behavior of vortices using a hexahedral box has already been shown by Eliasson et al. [\[4](#page-12-0)].

The whole computational domain has the shape of a hemisphere. Outside the previously described structured areas, unstructured tetrahedral cells are used. The resolution decreases to the outer edge. The high-lift configuration is fixed at the plane of symmetry, which is assumed to be an Eulerian wall without viscous effects. The spherical farfield boundary has a distance of 100 m (\approx 150 \times c_{ref} , respectively, $\approx 58 \times b$) to the origin, which is located at the leading edge of the wing at $\eta = 0$. In total, the grid consists of about 60 million points.

In addition, two other computational grids were derived from the reference grid. The overall structure (structured parts, vortex box, and computational domain) is maintained, whereas the spatial resolution varies between the grids. For the coarse grid, the number of cells in the structured part is halved in each direction (x, y, z) and the unstructured part is adapted. Furthermore, a grid with a local refinement in the region of the vortices was created. RANS simulations with this grid provide information about the influence of the spatial discretization on the prediction of the vortices. Table 1 shows the spacing of the grids in the box to capture the vortices and the total number of grid points.

2.4 Flow conditions

The flow conditions and the model size correspond to common experimental settings of the DLR F15 airfoil. Various wind-tunnel experiments [\[22–24](#page-12-0)] and numerical

Table 1 Spacing of the hexahedral cells within the vortex box and total grid points of the different grids

Grid		$\Delta y/\Delta z$ (mm) max. Δx (mm) Total points (mio.)
Coarse	11.5	~ 8.2
Reference	5.75	\sim 60
Locally refined 0.5		\sim 113

studies [[21,](#page-12-0) [24](#page-12-0)] have been performed at $Re_n = 2.096 \times 10^6$ and $Ma_n = 0.15$. For the simulations performed at the swept wing ($\varphi = 25^{\circ}$), it is desired to have comparable flow conditions normal to the leading edge, where the two-dimensional airfoil is present. With the following equations, the freestream values of Re and Ma are calculated for the swept wing without dihedral at an angle of attack of $\alpha = 6^{\circ}$ [[25\]](#page-12-0):

$$
Ma = \frac{Ma_n}{\cos \phi \sqrt{1 + \sin^2 \alpha \times \tan^2 \phi}}
$$
 (1)

$$
Re = \frac{Re_{\rm n}}{\cos^2 \phi \sqrt{1 + \sin^2 \alpha \times \tan^2 \phi}}.
$$
 (2)

The resulting values of Re and Ma are assumed to be constant to have comparable conditions for all simulations, although the component normal to the leading edge differs depending on the angle of attack. Simulations have been performed at different angles of attack with the following freestream conditions.

- $Re = 2.546 \times 10^6$ (related to $c_{ref} = 0.662$ m)
- $Ma = 0.1653$
- $V_{\infty} = 56.735 \text{ m/s}$
- $\alpha = 6^{\circ}/8^{\circ}/10^{\circ}/12^{\circ}/12.5^{\circ}/13^{\circ}/13.5^{\circ}.$

Turbulent flow is assumed for all simulations performed with the Menter-SST turbulence model. The JHh-v2 model requires defining transition positions. Based on the Menter-SST results, the location of transition on the lower surface is defined closely downstream of the stagnation line. The transition of the upper surface is set close to the suction peak of each component. These artificial transition positions do not necessarily represent the physical position, which cannot be exactly determined in the absence of corresponding experiments. Nevertheless, the applied strategy to define the transition for the simulation is common practice in many applications of high Reynolds number flows. A detailed description how transition is modeled within the JHh-v2 model can be found in [[26\]](#page-12-0).

The simulations with both turbulence models started at $\alpha = 6^{\circ}$ without a restart solution. Based on these solutions, the angle of attack has been increased gradually. In addition to the simulations with the steady solver, an unsteady simulation (uRANS) with the JHh-v2 model has been performed at $\alpha = 6^{\circ}$.

2.5 Validation of the numerical approach

DLR F-15 model has been extensively investigated with various experiments, including different sweep angles, flap and slat settings, and flow conditions. Unfortunately, a configuration with a slat cut-out or cut-off, where a vortex system interacts with the suction side has not been tested yet. Hence, no experimental reference data are available for a comparison with the presented simulations. Nevertheless, the applied turbulence models have been tested on a related test case. Cécora investigated the ability of different turbulence models to predict streamwise vortices on an NACA 0012 half-wing model [[27](#page-12-0)]. At this configuration, a streamwise vortex develops at the tip of the inclined wing $(\alpha = 10^{\circ})$. The computational grid consists of 13.2 million grid points in total. Again, structured blocks with hexahedral cells are used to capture the vortex accurately. The simulations were performed at a Mach number of $Ma = 0.16$ and a Reynolds number of $Re = 4.35 \times 10^6$. Cécora used different turbulence models and compared the predicted vortices with experimental data at the same conditions. Figure 2 shows the streamwise velocity component of the vortex core above and behind the NACA 0012 half-wing.

In the phase of axial acceleration on the wing $(x_a/c \lt 0)$, the applied eddy viscosity models (Menter-SST and SAO) underestimate the core velocity. The Reynolds stress models (JHh-v2 model with linear or quadratic redistribution term) predict core velocities, which are in good agreement with the experimental data. Furthermore, the dissipation of the vortex behind the wing $(x_a/c>0)$ differs strongly among the applied turbulence models. Both eddy viscosity models show a strong decay of the axial velocity behind the trailing edge of the wing. In contrast, the Reynolds stress models predict a slow decrease of the core velocity, which again matches the experimental data. One finds that the Reynolds stress models capture the observed vortex behavior, while the eddy viscosity models show a rapid dissipation of the vortex.

With the present work, the findings of Cécora are transferred to a more complex, practically relevant test

Fig. 2 NACA 0012 half-wing. Streamwise velocity component along the vortex core [\[27\]](#page-12-0)

case. Again, the effect of the applied turbulence model on the vortex prediction is investigated. Based on the results of Cécora, the JHh-v2 RSM model with a linear redistribution term is used here. As an eddy viscosity model, the established Menter-SST model is applied (q.v. 2.1.).

3 Results

This section presents the results of the simulations on the high-lift configuration. The convergence behavior of the simulations and the global flow results are presented. Particularly, the main focus of this contribution is on the behavior of the streamwise vortices. The vortex system is analyzed in detail, and the effect on the high-lift behavior of the configuration is shown.

3.1 Convergence behavior

For the simulations presented in this contribution, the major criterion to decide whether convergence is reached is the behavior of the aerodynamic coefficients. After a transient period for each angle of attack, an oscillating behavior around a constant value with limited amplitude is observed for both turbulence models. Nevertheless, the fluctuations are smaller for the Menter-SST simulations. When this behavior is observed, the normalized density residual is in a range between 10^{-4} and 10^{-3} , and no further decrease is obtained. This indicates an unsteady flow resulting from the complex flow phenomena of this configuration, namely, separated flow on the Fowler flap, wingtip vortex, and vortices at the slat and clean nose edges. To investigate the effect of the unsteady flow phenomena on the solution, an unsteady simulation (uRANS) with the JHh-v2 model has been performed at $\alpha = 6^{\circ}$. Based on the results of the steady simulation, the timespan of six convective time steps ($t_{\text{conv}} = c_{\text{ref}}/V_{\infty}$) was simulated. The history of the aerodynamic coefficients of both types of simulations is shown in Fig. [3](#page-5-0).

It appears that the variation of the aerodynamic coefficients is lower for the unsteady simulation. Nevertheless, the level remains constant and is similar compared to the level predicted with steady simulations. It can be concluded that although the flow is unsteady, the results of the steady simulations are rather reliable in predicting the aerodynamic coefficients. The effect of steady and unsteady simulations on the prediction of the vortex system will be shown in Sect. [3.3.](#page-6-0)

3.2 Global characteristics

In this section, the aerodynamic performance and the global flow characteristics of the generic high-lift

Fig. 3 History of aerodynamic coefficients of the JHh-v2 simulations at $\alpha = 6^{\circ}$, *left* steady simulation (last 10 k iterations), *right* unsteady simulation

configuration are presented. Figure 4 shows the lift curve and the Lilienthal polar predicted with both turbulence models. It has to be mentioned that the presented values are averaged values of the last 5000 iterations of the steady simulations for each angle of attack.

The simulations with the Menter-SST turbulence model exhibit a linear behavior of the lift coefficient up to an angle of attack of $\alpha = 12^{\circ}$. A further non-linear increase is observed up to $\alpha = 13.5^{\circ}$. At even larger angles of attack $(\alpha = 14^{\circ})$, no steady solution could be achieved, but the lift coefficient dropped down within the simulation. A transient solution illustrates large regions of separated flow downstream of the slat cut-off and on the inner part of the wing.

Fig. 4 Aerodynamic coefficients predicted with Menter-SST and JHh-v2 turbulence models, top lift curve, bottom Lilienthal polar

Steady simulations with the JHh-v2 turbulence model have also been performed up to $\alpha = 13.5^{\circ}$. The lift coefficients are slightly larger compared to the Menter-SST results up to $\alpha = 10^{\circ}$. At higher incidences, the lift is lower. This behavior is explained by the pressure distributions. Figure 5 shows pressure distributions on the flap at $\alpha = 10^{\circ}$ and $\alpha = 12.5^{\circ}$.

At $\alpha = 10^{\circ}$, the pressure distributions of the Menter-SST and JHh-v2 models at an inboard position ($y = 0.6$ m, two elements) are almost equal. At the outboard position $(y = 1.4 \text{ m}$, three elements), the suction peak is predicted slightly stronger with the JHh-v2 model. The same behavior is observed for the main element (not shown). Hence, a larger lift coefficient is predicted with the JHh-v2 model at $\alpha = 10^{\circ}$. In contrast, the suction peaks over the whole span at $\alpha = 12.5^{\circ}$ are weaker compared to the Menter-SST model, resulting in a lower lift coefficient. Another effect becomes apparent at the rear part of the flap. At $\alpha = 10^{\circ}$, the pressure is almost constant at the downstream third of the flap, indicating a flow separation. At $\alpha = 12.5^{\circ}$, the pressure further recovers toward the trailing edge. The behavior of the separation on the flap will be discussed later.

Although the lift curve differs between both turbulence models, the ratio of lift and drag is predicted similarly, resulting in a good agreement of the Lilienthal polars. Nevertheless, it has to be mentioned that the fluctuations of lift and drag are increased in the simulations at $\alpha = 13^{\circ}$ 13.5. To receive reliable results near maximum lift conditions, unsteady simulations at these angles of attack are in progress. Hence, the following evaluation of the global flow field and the behavior of the vortex system will focus

Fig. 5 Pressure distributions on the fowler flap at two spanwise positions, left $\alpha = 10^{\circ}$, right $\alpha = 12.5^{\circ}$

on $\alpha = 6^{\circ}$ (low, linear), $\alpha = 10^{\circ}$ (medium, linear) and $\alpha = 12.5^{\circ}$ (high, pre-stall).

To illustrate different flow effects, which occur at the generic high-lift configuration, Fig. 6 shows wall streamlines and the skin friction coefficient in the x-direction for the above-mentioned angles of attack for both turbulence models.

Figure 6 reveals different flow phenomena, which occur on the high-lift configuration. An important flow feature is the flow on the Fowler Flap. While the flow on the main wing and the slat is attached for the considered incidences, separated flow becomes visible on the rear part of the Fowler flap (1). The size and the location of the separated flow depend on the angle of attack and the turbulence model. At $\alpha = 6^{\circ}$, both turbulence models show separated flow along the whole span. The Menter-SST turbulence model predicts a separation at about the last 40 % of the flap, whereas the size is slightly smaller with the JHh-v2 model. Both turbulence models exhibit a decreasing size of the separation with increasing angle of attack. At $\alpha = 12.5^{\circ}$, using the Menter-SST model, a small part of the flap downstream of the slat cut-off shows fully attached flow. At the rest of the flap, only small regions show separated flow. With the JHh-v2 model, nearly the whole flow on the flap is attached.

Fig. 6 Wall streamlines and skin friction distribution $(x\text{-direction})$ on the upper side of the generic high-lift configuration at different angles of attack

Another remarkable flow effect occurs at the tip of the wing. At this location, the wall streamlines are curved inwards, representing the footprint of the wingtip vortex (3). At higher angles of attack, the values of the skin friction coefficient (x-direction) become larger in the influenced region due to a stronger tip vortex. For all incidences, the wingtip vortex is a local phenomenon and does not considerably affect other parts of the configuration. Since this vortex is of no relevance for this contribution, no further evaluation will be performed. In contrast, the streamwise vortices arising at the edges of the slat and the clean nose are of great interest. These vortices likewise create distinct footprints downstream of the slat cut-off (2). The behavior of this vortex system varies depending on the turbulence model and the angle of attack. A detailed evaluation of the characteristics of the vortices is performed in the next part of this contribution.

3.3 Characteristics of streamwise vortices

At the generic high-lift configuration, a system consisting of streamwise vortices develops and proceeds along the suction side. The development of these vortices is shown in Fig. 7.

It becomes apparent that two vortices arise. The first vortex develops at the edge of the spanwise cut-off slat (slat vortex). At the edge of the clean nose, a compensating flow occurs due to high pressure differences between the suction and the pressure side. This flow generates another vortex, which proceeds on the suction side of the high-lift configuration (clean nose vortex). For further evaluation of these vortices, slices at different chordwise positions will be evaluated. The slices with their corresponding position on the wing are also shown in Fig. 7.

In the first step, the influence of the computational grid on the prediction of the vortices is investigated. For the

Fig. 7 Development of vortex system on the suction side of the highlift wing. Contour plots of non-dimensional vorticity at different positions on the wing simulated with Menter-SST model at $\alpha = 6^{\circ}$

grid-dependence tests, three grids with a different grid resolution within the vortex region are used (details in Sect. [2.3](#page-2-0)). Figure 8 shows results of the simulations with the Menter-SST model on the different grids at $\alpha = 10^{\circ}$.

Significant differences in the prediction of the vortices occur between the coarse and reference grids. At a chordwise position of $x/c_{\text{ref}} = 0.1$, the slat vortex is predicted clearly stronger on the reference grid. However, the clean nose vortex is predicted in a similar manner on both grids at this position. Further downstream $(x/c_{\text{ref}} = 0.4)$, both vortices dissipate rapidly on the coarse grid. The structure and the strength differ from the vortices predicted on the reference grid. Obviously, the coarse grid is not able to predict the vortices accurately. In contrast, the differences between the reference grid and the locally refined grid are much smaller. The vortices predicted on both grids show the same structure and the same strength at both chordwise positions. Although the resolution has been quadrupled for the locally refined grid, almost no effect on the prediction of the vortices is visible. Hence, it can be concluded that the spatial resolution of the vortices is sufficient on the reference grid. For this reason, the following results arise from simulations on the reference grid.

In Sect. [3.1,](#page-4-0) it has been shown that fluctuations of the aerodynamic coefficients appear within the steady simulations. Hence, the influence of the solver type (steady, respectively, unsteady simulation) on the prediction of the vortices is analyzed. Therefore, the steady solution and a time-averaged solution with the unsteady solver at two different chordwise positions simulated with the JHh-v2

simulated with the Menter-SST model at $\alpha = 10^{\circ}$ with different grids

Fig. 9 Contour plots of non-dimensional vorticity at two chordwise positions (JHh-v2 turbulence model, $\alpha = 6^{\circ}$), *left* steady simulation, right unsteady simulation (time-integrated between $t/t_{\text{conv}} = 5{\text -}6$)

model are shown in Fig. 9 for an angle of attack of $\alpha = 6^{\circ}$. The averaging has been performed for one convective time step between $t/t_{\text{conv}} = 5$ and $t/t_{\text{conv}} = 6$.

It arises that the vortices predicted with the steady and the unsteady solver are similar. Both types of simulation show vortices of about the same size at the both slices. The most noticeable difference between the solutions occurs at a chordwise position of $x/c_{\text{ref}} = 0.1$. At this point, the slat vortex predicted with the unsteady solver is slightly weaker compared to the steady solver. Nevertheless, the size, the position, and the appearance of the slat vortex is predicted similarly. In addition, the steady and unsteady solvers show secondary vortices in the region of the slat vortex. The appearance and strength of these vortices slightly differs between both solvers. At the slice located downstream (x) $c_{\text{ref}} = 0.4$, the differences between both solutions are smaller. The steady solver and unsteady solver predict vortices of almost the same size, strength, and position. Although slight differences occur at both chordwise positions, it can be concluded that the steady solver captures the important effects of the vortex system, namely, the strength, position, and the size. For this reason, the results of the steady simulations with the Menter-SST and JHh-v2 turbulence models are used to analyze the influence of turbulence model and the incidence on the behavior of the vortex system. Nevertheless, it has to be noted that these results come from unconverged solutions, which still show oscillations in the aerodynamic coefficients (q.v. 3.1). Figure [10](#page-8-0) shows the development of the vortex system at $\alpha = 6^{\circ}$ for both turbulence models.

At the first presented position at $x/c_{\text{ref}} = 0.1$, different regions of increased non-dimensional vorticity become apparent. Both turbulence models show distinct regions of increased vorticity between $y/b = 0.63-0.64$. At this angle Fig. 8 Non-dimensional vorticity at different chordwise positions of attack, the aerodynamic loads of the slat are very low

Fig. 10 Non-dimensional vorticity at different chordwise positions at $\alpha = 6^{\circ}$, *left* Menter-SST turbulence model, *right* JHh-v2 RSM

and different vortical structures arise at the edges of the slat. Furthermore, the formation of vortical structures through the flow around the clean nose is observed (y/ $b = 0.61 - 0.62$. While proceeding downstream, the vortical structures behind the slat merge. The same holds for the structures behind the clean nose. Finally, at a chordwise position of $x/c_{\text{ref}} = 0.3$, two distinct vortices have formed. The positions $x/c_{\text{ref}} = 0.4$ and $x/c_{\text{ref}} = 0.5$ reveal a further decrease of the maximum non-dimensional vorticity with a simultaneous widening of both vortices. The spanwise position (y/b) and the position above the suction side of the wing remain nearly constant. This behavior and the appearance of the vortex system are predicted by both turbulence models. Nevertheless, the results differ between the Menter-SST and the JHh-v2 turbulence model regarding the strength of the vortices. The JHh-v2 model predicts significant stronger vortices already closely behind the origin. Furthermore, the JHh-v2 model is able to conserve the vortices for a longer distance. This behavior is also

Fig. 11 Iso-surfaces of non-dimensional vorticity $\omega \times c_{ref}/V_{\infty} = 35$ at $\alpha = 6^{\circ}$, top Menter-SST, bottom JHh-v2

shown in Fig. 11, which visualizes the vortices using isosurfaces of the non-dimensional vorticity.

Figure 11 clearly shows the formation of the vortices at the edges and the development along the suction side of the wing. This visualization reveals the conservation of the vortices with the JHh-v2 model, since the iso-surfaces proceed along the whole suction side. This result is in good agreement with the results of Craft $[13]$ $[13]$ and Cécora $[14]$ $[14]$, who also observed the effects of stronger vortices and a longer conservation with Reynolds stress models compared to eddy viscosity models.

At an angle of attack of $\alpha = 6^{\circ}$, no interaction between the slat vortex and the clean nose vortex is observed. A different situation appears at $\alpha = 10^{\circ}$, which is shown in Fig. [12](#page-9-0).

It becomes apparent that the mechanism of the formation of the clean nose vortex is similar. However, the appearance of the slat vortex differs. A distinct circular region of increased vorticity already appears at a chordwise position of $x/c_{ref} = 0.1$ due to a higher aerodynamic load of the slat at this incidence. This vortex is slightly away from

Fig. 12 Non-dimensional vorticity at different chordwise positions at $\alpha = 10^{\circ}$, *left* Menter-SST turbulence model, *right*: JHh-v2 RSM

the surface. While proceeding downstream, this vortex is drifting inwards without changing the appearance. At x/ $c_{\text{ref}} = 0.3$, the slat vortex interacts with the clean nose vortex. The clean nose vortex is displaced by the slat vortex and a change of the appearance of the clean nose vortex is observed. Further downstream, this behavior continues. Although the general behavior is captured by both turbulence models, larger differences between the Menter-SST model and the JHh-v2 turbulence model emerge. The results of the Menter-SST turbulence model show quite weak vortices at a position of $x/c_{\text{ref}} = 0.3$ due to the rapid decay of the strength. Hence, the interaction between the slat and the clean nose vortex is smaller compared to the JHh-v2 model, which can be observed most clearly at a position $x/c_{\text{ref}} = 0.5$. At this position, the vortices predicted with the Menter-SST model have already lost most of the strength and the slat vortex is nearly above the remaining part of the clean nose vortex. Compared to the Menter-SST model, the JHh-v2 model

predicts stronger vortices at this position. In addition, the position of the vortices relative to each other changed. The slat vortex is at an inboard position, while the remaining vortical structures of the clean nose vortex are on the outer side. This behavior is again shown in Fig. 13.

The iso-surfaces of non-dimensional vorticity demonstrate the differences between the prediction of the vortex system of the Menter-SST model and the JHh-v2 turbulence model. The weak interaction predicted with the Menter-SST model at $x/c_{\text{ref}} = 0.3$ becomes visible. Although the clean nose vortex is displaced by the slat vortex, the weak vortex withstands the displacement. In contrast, the results of the JHh-v2 model expose a different behavior of the interaction. When both vortices interact, the clean nose vortex changes its appearance. Due to the displacement of the slat vortex, the clean nose vortex spreads out in the spanwise direction and decomposes. This decomposition takes place in a region of an adverse pressure gradient on the suction side of the high-lift configuration, which favors a breakdown of the vortex. It is not clearly determined if the adverse pressure gradient or the

Fig. 13 Iso-surfaces of non-dimensional vorticity $\omega \times c_{ref}/V_{\infty} = 35$ at $\alpha = 10^{\circ}$, top Menter-SST, bottom JHh-v2

influence of the slat vortex is primarily responsible for the decomposition of the clean nose vortex. For this reason, a vortex breakdown in the classical sense is questionable and therefore marked with a $(?)$ in Fig. [13](#page-9-0). Another effect is observed for the slat vortex. The appearance of this vortex is constant up to a chordwise position of $x/c_{\text{ref}} = 0.5$. Nevertheless, Fig. [13](#page-9-0) shows a changing behavior downstream. Still, at this position, an adverse pressure gradient is present. The slat vortex breaks down in a spiral movement. At positions further downstream, decomposed structures of increased vorticity are present.

Compared to $\alpha = 10^{\circ}$, the behavior of the vortex system at $\alpha = 12.5^{\circ}$ exhibits strong similarities. The contour plots of non-dimensional vorticity are shown in Fig. 14.

It appears that the mechanism of the formation of the slat and the clean nose vortex at $\alpha = 12.5^{\circ}$ is similar compared to $\alpha = 10^{\circ}$. Nevertheless, the strength of both vortices at $x/c_{\text{ref}} = 0.1$ is higher due to higher aerodynamic loads at this angle of attack. Furthermore, the interaction between both vortices occurs earlier. At x/ $c_{\text{ref}} = 0.2$, the Menter-SST model shows a widened clean nose vortex, which is already influenced by the slat vortex. The JHh-v2 model likewise reveals an interaction of the vortices, but in contrast to the Menter-SST model, the clean nose vortex already decomposes. Spots of increased vorticity are visible at this position. Further downstream, the interaction predicted with the Menter-SST model is similar to $\alpha = 10^{\circ}$. The interaction between the vortices is dominated by a displacement of the clean nose vortex. A decomposition or breakdown is not observed. In contrast, the interaction predicted with the JHh-v2 model is of a fundamentally different character. Downstream of the observed decomposition of the clean nose vortex, a reformation of this vortex occurs. Between x/ $c_{\text{ref}} = 0.4{\text{-}}0.5$, a nearly circular region has formed again. Compared to upstream positions, the maximum non-dimensional vorticity is increased again. To illustrate this effect, iso-surfaces of non-dimensional vorticity are shown in Fig. [15.](#page-11-0)

For both turbulence models, a widened clean nose vortex is visible. Again, the visualization of the vortex system predicted with the Menter-SST model shows a displacement of the clean nose vortex without decomposition or breakdown. The results of the JHh-v2 model show the displacement of the clean nose vortex at an earlier position compared to $\alpha = 10^{\circ}$. The reason for this is the strong interaction with the slat vortex, which occurs at an upstream location. Furthermore, the adverse pressure gradient is stronger at higher incidences. This effect is also responsible for the breakdown of the slat vortex, which again is observed at an upstream position compared to $\alpha = 10^{\circ}$. The visualization of the vortices also

Fig. 14 Non-dimensional vorticity at different chordwise positions at $\alpha = 12.5^{\circ}$, *left* Menter-SST turbulence model, *right* JHh-v2 RSM

demonstrates that distinct vortical structures reformate after the clean nose vortex decomposes.

At $\alpha = 12.5^{\circ}$, regions of a negative skin friction coefficient occur close behind the edge of the clean nose (compare Fig. [4](#page-5-0)). Here, the upwards directed velocity components of the outboard side of the clean nose vortex destabilize the boundary layer. Local limited regions of separated flow occur. This effect is stronger for the Menter-SST model, where the clean nose vortex is only displaced and not decomposed. Further downstream, a stronger effect is observed for the JHh-v2 model. Here, the clean nose vortex reformates and influences the boundary layer. The Menter-SST model is not able to preserve the strength of the vortex, and thus, the effect on the boundary layer is lower. Nevertheless, the influenced region behind the cut-off is small for both turbulence models, and for that reason, the overall aerodynamic

Fig. 15 Iso-surfaces of non-dimensional vorticity $\omega \times c_{ref}V_{\infty} = 35$ at $\alpha = 12.5^{\circ}$, top Menter-SST, bottom JHh-v2

behavior of the high-lift configuration at this angle of attack is not influenced significantly.

4 Conclusion

Results of flow simulations of streamwise vortices on a generic three-dimensional high-lift configuration at different angles of attack have been presented. The simulations were performed with the DLR TAU-Code as flow solver applying the Menter-SST eddy viscosity and the JHh-v2 RSM turbulence model. Two vortices develop at the edges of the slat and the clean nose, proceeding downstream on the suction side of the wing.

Steady simulations expose slight fluctuations of the aerodynamic coefficients. However, a comparison with an unsteady simulation shows that the results produced with a steady solver are similar concerning the level of the aerodynamic coefficients and the behavior of the vortices. Nevertheless, at incidences close to stall, it becomes necessary to perform unsteady simulations.

The results at all considered angles of attack reveal a different behavior of the vortices for both turbulence models. In general, the vortices predicted with the JHhv2 model are stronger compared to the Menter-SST model. In addition, a strong decay of the vortices is observed for the Menter-SST turbulence model. The JHh-v2 RSM model preserves the vortices better while proceeding downstream. This observation corresponds to results from the literature [[13](#page-12-0), [14\]](#page-12-0). Furthermore, differences between the Menter-SST model and the JHh-v2 model occur concerning the interaction of the vortices. At $\alpha = 6^\circ$, no interaction is observed for both turbulence models. In contrast, at $\alpha = 10^{\circ}$ and $\alpha = 12.5^{\circ}$ the slat vortex drifts inwards and displaces the clean nose vortex. For these angles of attack, the results of the JHh-v2 model exhibit a decomposition of the clean nose vortex when the interaction takes place. This decomposition is not observed with the Menter-SST model, where the clean nose vortex is simply deformed. Furthermore, at downstream positions, the JHh-v2 model predicts a breakdown of the slat vortex. Again, this effect is not captured by the Menter-SST model.

The vortex behavior influences the boundary layer on the suction side of the wing. The wall streamlines are curved by the vortices close to the surface. Particularly, at high angles of attack, differences between the Menter-SST and the JHh-v2 model become visible. The reason for this is the behavior of the interacting vortices. Here, the different structures of the predicted interaction are represented at the skin friction distribution. To identify the effect of the vortex interaction and breakdown on the stall behavior of the high-lift configuration, unsteady simulations at the corresponding angles of attack have to be performed, which will be part of future research within this project. Further plans of future work include an improved delayed detached eddy simulation (IDDES). This simulation will show whether an RANS simulation can capture the important flow mechanisms or whether a scale-resolving simulation is required to capture the complex flow features. In addition, a wind-tunnel experiment with the presented configuration is planned. These experiments will deliver a data base for a comparison and allow a quantitative evaluation of the simulations presented in this contribution.

Acknowledgments The authors wish to acknowledge the German Federal Ministry for Economic Affairs and Energy (BMWi) for funding this research activity (Grant Number: 20A1301B). The views and conclusions contained herein are those of the authors and should not be interpreted as necessarily representing the official policies or endorsements. Furthermore, the authors would like to thank the North-German Supercomputing Alliance (HLRN) for providing computational resources within the project nii00091.

Gefördert durch:

Bundesministerium für Wirtschaft
und Energie

aufgrund eines Beschlusses des Deutschen Bundestages

References

- 1. Rudolph, P.K.C.: High-lift systems on commercial subsonic airliners. NASA CR 4746 (1996)
- 2. Smith, A.M.O.: High lift aerodynamics. J. Aircr. 12(6), 501–530 (1975)
- 3. Haines, A.B., Young, A.D.: Scale effects on aircraft and weapon aerodynamic. AGARDograph 323, 27–65 (1994)
- 4. Eliasson, P., Catalano, P., Le Pape, M.-C., Ortmann, J., Pelizzari, E., Ponsin, J.: Improved CFD predictions for high lift flows in the european project EUROLIFT II. AIAA 2007-4303, Miami (2007)
- 5. Frhr von Geyr, H., Schade, N., van der Burg, J.W., Eliasson, P., Esquieu, S.: CFD prediction of maximum lift effects on realistic high-lift-commercial-aircraft-configurations within the European project EUROLIFT II. AIAA 2007-4299, Miami (2007)
- 6. Rudnik, R., Frhr van Geyr, H.: The European high lift project EUROLIFT II—objectives, approach, and structure. AIAA 2007-4296, Miami (2007)
- 7. Rudnik, R.: Stall behavior of the EUROLIFT high lift configurations. AIAA 2008-836, Reno (2008)
- 8. Wild, J., Brezillon, J., Amoignon, O., Quest, J., Moens, F., Quagliarella, D.: Advanced high-lift design by numerical methods and wind tunnel verification within the European project EUROLIFT II. AIAA 2007-4300, Miami (2007)
- 9. Rudnik, R., Reckzeh, D.. Quest, J.: HINVA—high lift INflight validation—project overview and status. AIAA 2012-0106, Nashville (2012)
- 10. Bier, N., Rohlmann, D., Rudnik, R.: Numerical maximum lift prediction of a realistic commercial aircraft in landing configuration. AIAA 2012-0279, Nashville (2012)
- 11. Sclafani, A.J., Slotnick, J.P., Vassberg, J.C., Pulliam, T.H., Lee, H.C.: OVERFLOW analysis of the NASA trap wing model from

the first high lift prediction workshop. AIAA 2011-866, Orlando (2011)

- 12. Crippa, S., Melber-Wilkending, S., Rudnik, R.: DLR contribution to the first high lift prediction workshop. AIAA 2011-938, Orlando (2011)
- 13. Craft, T.J., Gerasimov, A.V., Launder, B.E., Robinson, C.M.E.: A computational study of the near-field generation and decay of wingtip vortices. Int. J. Heat Fluid Flow 27, 684–695 (2006)
- 14. Cécora, R.-D., Radespiel, R., Eisfeld, B., Probst, A.: Differential Reynolds-stress modeling for aeronautics. J. Aircr. 53(3), 739–755 (2015)
- 15. Landa, T., Wild, J., Radespiel, R.: Simulation of longitudinal vortices on a high-lift wing. In: Radespiel, R., et al. (eds.) Advances in simulation of wing and nacelle stall, notes on numerical fluid mechanics and multidisciplinary design, vol. 131, pp. 351–366, Springer, Heidelberg, New York, London, ISBN 978-3-319-21126-8 (2015)
- 16. Schwamborn, D., Gerhold, T., Heinrich, R.: The DLR TAU-Code: recent applications in research and industry. ECCOMAS CFD 2006, Egmond aan Zee (2006)
- 17. Schwamborn, D., Gardner, A.D., von Geyr, H., Krumbein, A., Lüdeke, H., Stürmer, A.: Development of the DLR TAU-Code for aerospace applications. ICASAT 2008, Bangalore (2008)
- 18. Menter, F.R.: Zonal two equation $k-\omega$ turbulence models for aerodynamic flows. AIAA 93-2906, Orlando (1993)
- 19. Jakirlic, S., Hanjalic, K.: A new approach to modelling near-wall turbulence energy and stress dissipation. J. Fluid Mech. 459, 139–166 (2002)
- 20. Probst, A., Radespiel, R.: Implementation and extension of a near-wall reynolds-stress model for application to aerodynamic flows on unstructured meshes, AIAA 2008-770, Reno (2008)
- 21. Reuß, S., Probst, A., Knopp, T.: Numerical investigation of the DLR F15 two-element airfoil using a Reynolds stress model. Third symposium ''Simulation of Wing and Nacelle Stall'', Braunschweig (2012)
- 22. Wild, J.: Mach and Reynolds number dependencies of the stall behavior of high-lift wing-sections. J. Aircr. 50(4), 1202–1216 (2013)
- 23. Hahn, D., Scholz, P., Radespiel, R.: Experimental evaluation of the stall characteristics of a two-element high-lift airfoil. Second symposium "Simulation of Wing and Nacelle Stall", Braunschweig (2010)
- 24. Hühne, C.-P., Mahmood, S., Scholz, P., Radespiel, R.: Active flow control at a swept wing: a comparison of numerical and experimental results. AIAA 2013-2798, San Diego (2013)
- 25. Büscher, A., Radespiel, R.: A method for the aerodynamic analysis and design of nonplanar lifting configurations at transonic speeds. Jahrbuch DGLR 1, 603–612 (2003)
- 26. Probst, A., Radespiel, R., Rist, U.: Linear-stability-based transition modeling for aerodynamic flow simulations with a near-wall reynolds-stress model. AIAA J. 50(2), 416–428 (2012)
- 27. Cécora, R.-D.: Reynolds-Spannungsmodell der Turbulenz für Anwendungen der Flugzeugaerodynamik. NFL Forschungsbericht 2015-27, Braunschweig (2015)