

A Review on Computational Fluid Dynamics Modelling in Human Thoracic Aorta

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Abstract—It has long been recognized that the forces and stresses produced by the blood flow on the walls of the cardiovascular system are central to the development of different cardiovascular diseases (CVDs). However, up to now, the reason why arterial diseases occur at preferential sites is still not fully understood. This paper reviews the progress, made largely within the last decade, towards the use of 3D computational fluid dynamics (CFD) models to simulate the blood flow dynamics and its interaction with the arterial wall within the human thoracic aorta (TA). We describe the technical aspects of model building, review methods to create anatomic and physiologic models, obtain material properties, assign boundary conditions, solve the equations governing blood flow, and describe the assumptions used in running the simulations. Detailed comparative information is provided in tabular format about the model setup, simulation results, and a summary of the major insights and contributions of each TA article reviewed. Several syntheses are given that summarize the research carried out by influential research groups, review important findings, discuss the methods employed, limitations, and opportunities for further research. We hope that this review will stimulate computational research that will contribute to the continued improvement of cardiovascular health through a strong interaction and cooperation between engineers and clinicians.

Keywords—Blood flow, Computational fluid dynamics, Hemodynamics, Human thoracic aorta.

INTRODUCTION

Aorta, the largest artery found in the human body, is the main vessel through which oxygenated blood pumped

out of the left ventricle (LV) enters the systemic circulation. Thoracic aorta (TA) refers to the region that consists of the ascending aorta, aortic arch and descending aorta. This segment also includes three main branches stemming from the arch, namely brachiocephalic artery (BA), left common carotid artery (LCA) and left subclavian artery (LSA), which channel blood supply to the upper parts of the body. TA has one of the most complex anatomies amongst all arteries; in addition to bending severely, the centerline of the arch twists, thus it doesn't lie in a plane (non-planar). Additionally, TA has branching, tapering of the lumen and distensible arterial walls.

Despite significant progress in clinical care and public education, cardiovascular diseases (CVDs) remain the leading single cause of morbidity and mortality worldwide. According to a prediction by World Health Organization, by year 2030 approximately 23.6 million people will die from CVDs.¹⁹ TA with its complex anatomy is subjected to typical CVDs which often manifest in forms of atherosclerosis, aneurysm, and dissection. Atherosclerosis, the most common manifestation of arterial disease, is characterized by the thickening of the arterial wall caused by a build-up of fatty plaque in the inner lining of the artery. Aortic aneurysm occurs when there is progressive enlargement and dilation due to weakening of the aortic wall. Dissection, on the other hand, refers to a disruption of the aortic wall, forming an intimal flap and therefore separating a true from a false lumen. The above conditions are life-threatening due to their potential of rupture at the weakened aortic sections, therefore, the need for elucidating the mechanisms involved in the development and progression of these diseases is critical and has been the subject of active research in the past decades.

Development of computational fluid dynamics (CFD) in recent years has enabled the use of 3D numerical

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simulations to investigate patient-specific hemodynamics and to understand the origin and development of different CVDs; mainly due to its capability of quantifying variables not measurable *in vivo*, its reproducibility, and its role as diagnostic and treatment tool for different CVDs conditions. In contrast to *in vitro* studies, CFD is more convenient for altering model parameters such as boundary conditions, and given the complexity of blood flow in intricate geometries, the combination between high resolution simulation techniques and image-based measurements data has proven to be a reliable tool for realistic modelling of arterial blood flow. Limitations in the use of CFD simulations are related primarily to the model assumptions that are made when these simulations are performed, e.g., geometry, viscosity, distensibility, flow conditions. Simplified interpretations, however, have always been the cornerstone of understanding the physical world.

In spite of the last decade history of CFD studies related to the TA, this literature has never been comprehensively reviewed. For new researchers entering the field, a critical review would be invaluable, and experienced researchers who are focusing on a particular sub-problem may benefit from an overview exposure to the work of other researchers. Thus, the goal of this paper is to review the current state of the art of CFD modelling in human TA, including the main steps involved in simulating blood flow and its interaction with the arterial wall, namely, problem identification, pre-processing, solving, and post-processing. The article is organized as follows. “**Problem Identification**” begins by focusing on what is known about the biomechanical factors that play a role in the cardiovascular health as well as in the progression and treatment of cardiovascular diseases. “**Pre-processing**” section introduces the approaches of obtaining TA geometric models, discretization and meshing schemes. Material properties, boundary conditions and turbulence models are also discussed. Particular attention is paid to the assignment of boundary conditions, as this point is of critical importance in the current area of research. “**Governing Equations and Blood Flow Mechanics**” section describes the governing equations and important aspects of the mechanics of blood flow. “**Post-processing**” section describes the post-processing, including Table 1, which summarizes the major insights and contributions of each TA study included in this review. Validation and verification of the computational results are also discussed. Finally, “**Conclusions and Future Challenges**” section contains concluding remarks and future challenges.

PROBLEM IDENTIFICATION

The fact that mechanics plays a vital role in the development and maintenance of cardiovascular

health, as well as in the initialization and localization of CVDs has been known since long; however, it has only been since the mid-1970s that we have understood why mechanics are truly important. Hemodynamic factors that have been suggested to influence cellular development on the arterial wall are derived from the velocity field and involve several different forms, such as flow separation, secondary flow, wall shear stress (WSS), and spatial and temporal shear stress gradients. The relationship between shear stress distribution and cellular development has been shown to be linked *via* the mechano-transduction process.³³ Particularly, endothelial cells (ECs), which form the innermost layer of the arterial wall and are in direct contact with flowing blood, can change their responses due to local flow conditions.³² Several studies had shown that endothelial dysfunction and arterial wall remodelling are correlated with complex flow dynamics; especially with low and oscillatory shear stress.^{60,161,215} The long term interaction between the ECs and the blood flow results in changes of arterial wall thickness, structure and morphology, processes directly linked to a variety of CVDs.

Today, there is accumulating evidence that atherosclerotic lesions occur predominantly at regions of low and oscillatory shear.^{22,24,88,116} Moreover, it is known that these lesions tend to localize in regions of complex arterial geometry, such as bends, tapering, and branching.^{31,49,85,207} Based on these studies, the human TA with its complex anatomy can be considered as one of the most susceptible arteries for the development of atherosclerosis. Bogren *et al.*, Kilner *et al.* and Bogren *et al.*^{12,13,78} observed helical and retrograde (reversing) flow patterns prevailing in the aortic arch. In these studies, the curvature and the non-planarity of the aortic arch were thought to be the reasons for the helical nature of the blood flow. Later, Utepov *et al.*¹⁹⁸ demonstrated that the tapering of the descending aorta is correlated with the progression of plaque in this part of the aorta. Hence, besides hemodynamics factors, the global and local anatomy of an artery significantly influences and plays a role in the initialization and localization of arterial diseases, especially atherosclerosis.

Nevertheless, given the fact that early events leading to the pathogenesis of atherosclerosis is the accumulation of lipids within the arterial wall, in recent years some researchers have been paying more attention to mass transport phenomena in the cardiovascular system and the interaction of red blood cells (RBCs) with the arterial wall.^{82,190,206} An increased level of low-density lipoprotein (LDL) has been shown to promote the accumulation of cholesterol within the intima layer of large arteries.^{67,165} There is an exchange of water from the blood to the arterial wall, driven by the

arterial pressure difference, which can transport LDL to the arterial wall. However, the ECs present a barrier to LDL creating a flow-dependent concentration boundary layer. This concentration polarization is interesting, as regions with elevated LDL are co-located with low shear regions,³⁹ suggesting a relationship between LDL accumulation and blood flow dynamics. Studies in animals and humans have indicated that the flux of LDL from the blood into the arterial wall depends both on the flow-dependent LDL concentration and the LDL permeability at the blood–wall interface.¹³³

Oxygen transport in the arterial wall is probably another important factor involved in the pathogenesis of atherosclerosis. Santilli *et al.*¹⁷¹ observed that oxygen tension was significantly lower at the atherosclerotic lesion-prone sinus region of the canine carotid sinus when compared with that in the common carotid artery. In addition, hypoxia has been shown to cause damage to the endothelial barrier and result in inter-endothelial gaps, hence leading to increased arterial wall permeability to macromolecules.¹³⁵ Recently, Sluimer *et al.*¹⁷⁸ directly observed the existence of hypoxia in human atherosclerotic carotid arteries for the first time. On the contrary, hyperoxia has been shown to have the effect on the regression of atherosclerotic plaques.¹³⁷ Clearly, the role of LDL and oxygen transport and its connection to atherosclerosis is a complex phenomenon, present not only at two very different time scales but also at two very different spatial scales. To this day, the reason why atherosclerosis development occurs at preferential sites is still not fully understood, but these regions coincide with complex flow and low and oscillating shear stress. These findings have motivated a large volume of research to try to elucidate the blood flow dynamics in the human TA and to quantify the links between flow environment and CVDs pathways.

PRE-PROCESSING

Geometry: Definition of the Computational Domain

The first step on simulating blood flow is to obtain the geometry, or physical bounds of the artery. There have been several experimental and computational studies in curved tubes, both in steady and unsteady flow conditions, that have aimed to elucidate the flow dynamics in the aortic arch.^{63,83,129,170,186,211} These studies have provided great insight into the complexity of flow patterns in curved tubes, established the influence of arch curvature, and documented the resulting skewness in velocity profiles as well as the structure of secondary flow patterns within these geometries.

More recently, idealized geometries of the TA were also used in CFD studies (see Table 1). Although the

majority of these geometries were based on medical imaging data, some simplifications were made, such as setting circular cross-sections, applying constant diameter throughout the lumen or neglecting the arch branches. Mori and Yamaguchi¹²¹ were amongst the first researchers that used a magnetic resonance imaging (MRI) image-based geometry to simulate blood flow in the TA. As a result, flow dynamics were more realistic in comparison to earlier works with curved tubes. Later, Shacheraghi *et al.*¹⁷⁴ used a computed tomography (CT) image-based geometry, and even though the TA model considered the arch branches and a minimal out-of-plane curvature, it had a circular cross-section. While a major cause of complex flow dynamics in large arteries is its local anatomy, the above idealized geometries captured important anatomical features of the TA and were used to understand the extent of the idealization. Furthermore, these studies in curved tubes and idealized geometries established the dependence of blood flow dynamics on various geometric and model parameters, including the non-Newtonian behavior of blood, fluid–structure interaction (FSI), mass transport phenomena, the flow Reynolds and Dean numbers, and in the case of unsteady flow, the Womersley number.

While initially TA simulations were performed using idealized geometric models, in recent years the majority of these studies have used image-based patient-specific geometries (see Table 1). Currently, the most common medical imaging techniques used to reconstruct arterial geometries are MRI and CT. On the one hand, CT is a technique used to obtain high resolution X-ray images of the inside of a body with a very thin slice thickness. These images have high contrast which makes it possible to see each part of a body distinctly by a slight adjustment of contrast. On the other hand, MRI does not require the use of ionizing radiation; instead, contrast is achieved by exploiting differences in the magnetic spin relaxation properties of the various bodily tissues and fluids. For the purposes of imaging arteries, MRI is particularly attractive since the blood itself can be used as a contrast agent. In addition, phase-contrast MRI (PC-MRI) may also be used to measure time-varying blood flow rates waveforms to provide the necessary velocity boundary conditions at the CFD model's inlets and outlets

In general, after image acquisition, the 3D model reconstruction includes two major steps: image segmentation and surface modelling. Many of the early tools for image-based reconstruction were based on 2D segmentation.^{185,194} This approach is based on re-sampling the 3D image data on 2D image planes, segmenting the lumen boundary on this plane to obtain a closed-curve, lofting adjacent curves to create a tubular model of the artery, and then using geometric

union operations to create the complete model. Although 2D segmentation can be used to create complex geometric models and works particularly well for image data within regions of poor contrast, this approach is largely manual and thus very time-consuming. More recently, a less time consuming, robust and more automated alternative is 3D segmentation,^{1,8} as is used in commercial and open source software packages. This approach uses intensity thresholding to automatically detect the imaging area to be used in the model, thus it can present challenges with image data where contrast with adjacent tissues is poor. These techniques can be performed with variants depending on the software, with more or less automation as dictated by the resolution of the data.

Discretization: Mesh Generation

Once the anatomy has been translated into a 3D geometric model, it is discretized into a finite number of smaller sub-domains called elements or cells, over which the governing Navier–Stokes equations are then solved. The number and distribution of these elements largely govern the accuracy of the simulation results; smaller elements must be used to resolve complex flow regions, but the computational costs (time and memory) scale with the number of elements used, thus a critical balance must be achieved between computational resources and solution accuracy.

In generating a spatial discretization of the computational domain, we are faced with the choice between structured (hexahedral) or unstructured (tetrahedral) meshes. For curved tubes or idealized TA geometries, structured meshing has been the preferred option, since is fairly straightforward and can be easily automated by dividing the symmetric geometry into a fixed number of points around the circumference and along the tube axis. Such structured meshes may also be generated for the arch branches using block-structured meshes, though considerably more effort is required to ensure the quality of the elements. In patient-specific TA simulations, the most common approach has been the use of unstructured meshes produced by commercial meshing software, in which distributions of tetrahedral, prismatic and pyramid elements are generated using a variety of sophisticated algorithms. An unstructured computational domain is often preferred for its potential of effortless grid generation over complex geometries, even though, structured meshes may also be generated for patient-specific geometries.

A comparative CFD study between different mesh types in the TA is not yet available; however, De Santis *et al.*³⁴ recently conducted a similar study in a left coronary artery. The results showed that unstructured

meshes needed much higher resolution than structured meshes to reach mesh independency; with higher computational costs. Such differences are also reported in other studies and are attributed to the poor alignment with the primary flow direction and to the high numerical diffusion error associated with unstructured meshes.¹⁰⁷ Hexahedral meshes are known to provide higher accuracy but are generally more difficult to generate in complex and branching geometries, and the associated user intervention time can be excessively expensive. Figure 1 presents an example of MRI data at maximum intensity projection (a) used to derive a patient-specific TA coarctation 3D geometric model (b) in combination with an unstructured mesh with five prism layers adjacent to the arterial wall (c). Note that due to the nature of the imaging data, the exact shape of the artery may differ from the one seen on MRI.

Mesh independence studies are a vital part of CFD work since they show the extent to which the results depend on mesh parameters, and quantify the error associated with spatial discretization. However, as noted by Prakash & Ethier,¹⁵² mesh refinement studies are rarely reported in the literature. Where the results of a study are given, they are sometimes ambiguous, with simple statements of the percentage error compared to a finer mesh. Without the densities of the two meshes these statements give the reader no information about how well converged the solution is, since by making a mesh which is only a little finer it is clearly possible to achieve a tiny percentage difference between the two solutions.¹⁶³ Adaptive meshing techniques were recently described for CFD studies. Muller *et al.* and Sahni *et al.*^{125,168} discuss a method in which a posteriori error estimators, provide necessary information to adaptively refine the mesh. Furthermore, because the resolution of WSS is often of interest, boundary layer mesh generation techniques can be used to increase mesh density near the arterial wall.¹⁶⁷ In retrospect, a valid computational mesh should accurately resolve both the complex geometry and the physiologically relevant flow features, and should take the user, the solver and the computational resources out of the loop.

Material Properties

Human Blood

Human blood which exhibits a highly complex, flow-dependent physical and chemical constitution, is a non-Newtonian fluid in which its viscosity depends on the shear rate. Blood viscosity is shear-thinning because of the disaggregation of the rouleaux (stacks of RBCs) and the orienting of individual RBCs.²⁵ Experimental evidence has also shown that blood

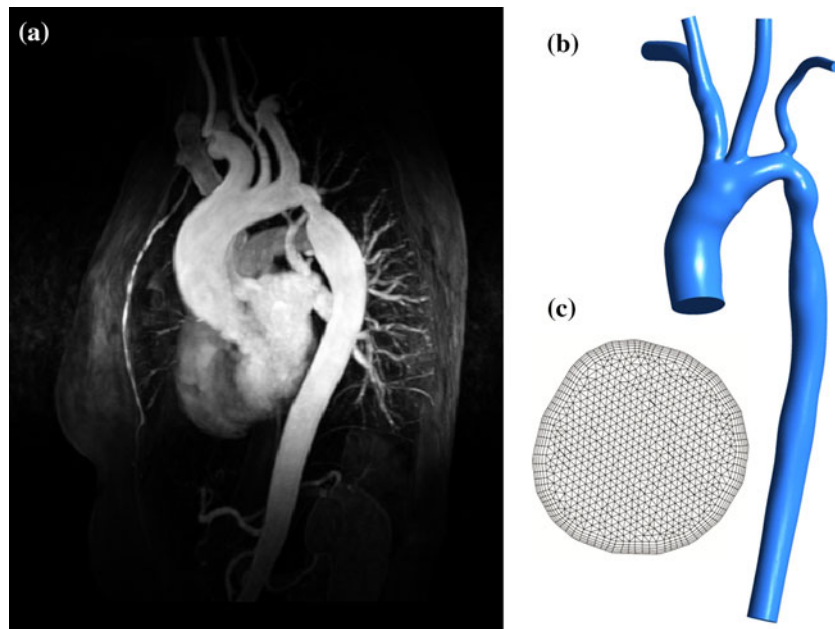


FIGURE 1. MRI data at maximum intensity projection (a), Patient-specific TA coarctation 3D model (b), and unstructured mesh with five prism layers adjacent to the arterial wall (c) (Open Source Medical Software Corporation. <http://www.vascularmodel.org>).

under certain conditions behaves as a non-linear viscoelastic fluid, resulting from the elastic membranes of its constituents.¹⁹⁵ Finally, blood is thixotropic; its viscosity can vary with time at constant low shear mainly due to rouleaux aggregation and disaggregation. Although blood has been usually considered as a Newtonian fluid in CFD studies of large arteries, its viscosity is strongly influenced by two factors: hematocrit (volume percentage of RBCs in whole blood) and temperature. As hematocrit increases, there is an increase in viscosity, as temperature decreases, viscosity increases.⁶

It can be seen that most of the rheological models proposed in the literature to predict the stress vs. strain rate relationship of blood fall into two categories: (i) models which predict shear-thinning effects: the Cross model,¹³⁶ the non-Newtonian Power law model,⁴ the Carreau model²⁶ and the Second-grade model,¹⁰⁹ (ii) models which exhibit yield stress: the Casson model⁶¹ and the Herschel–Bulkley model.¹⁶⁹ Moreover, complex constitutive models in which blood is modeled as a viscoelastic fluid have also been introduced.¹⁴¹ Although constitutive equations from the Oldroyd-B type model have the best potential to capture with reasonable accuracy the rheological behavior of blood in large arteries,²¹⁹ the remaining challenge is to determine and develop more sophisticated non-Newtonian models that capture blood real behavior under complex flow conditions.

Experimental studies have shown that at high shear rates (above 100 s^{-1}) and in large and medium arteries,

the viscosity of human blood with 45% hematocrit reaches a constant value of $3.0\text{--}4.0 \text{ mPa s}$,¹⁴⁷ thus justifying somewhat the choice of a Newtonian model. However, there does not appear to be a consensus in the literature on the importance of the non-Newtonian effects of blood in large arteries, including the TA. While some studies have found significant differences between their results calculated with and without the non-Newtonian models,^{23,74,101} others have found that the Newtonian approach is a reasonably good approximation.^{16,75} The main argument to ignore the non-Newtonian behavior of blood is that shear rates in large arteries are predominantly high. Still, in transient flow conditions, especially when the blood flow slow or reverses direction, there are periods of time and local regions where the shear rate may be below 100 s^{-1} and it would be reasonable to expect that the non-Newtonian effects may be important. The question that is important to address is; to what extent are these effects important over an entire cardiac cycle?

A recent study by Liu *et al.*¹⁰⁵ investigated the effect of both non-Newtonian and pulsatile blood flow conditions on mass transport phenomena in a patient-specific TA model. It was found that under steady flow conditions, although the WSS distribution is similar for both the Newtonian and the non-Newtonian simulations, the WSS magnitude for the non-Newtonian simulation is generally higher than that for the Newtonian simulation, especially in areas with low WSS. The steady results also revealed that when compared to the Newtonian simulation, the shear thinning

non-Newtonian behavior of blood (Carreau model) has little effect on LDL and oxygen transport in most regions of the TA, but in atherogenic-prone areas (areas with flow disturbance) where the luminal surface LDL concentration is high and oxygen flux is low, its effect is apparent. The effect of flow pulsation on the transport of LDL has a similar trend. But pulsatile flow can apparently enhance oxygen flux in the TA, especially in areas predisposed to flow disturbance (low oxygen flux). Therefore, it was suggested that the shear thinning non-Newtonian behavior of blood may be pro-atherogenic, while the pulsation of blood flow may be anti-atherogenic.

Arterial Wall—FSI

The arterial wall deforms under loads, and in particular for some arteries such as the TA, this deformation is large and might not be approximated by a rigid wall. In fact, the motion of the arterial wall and surrounding tissues affects the blood flow dynamics and vice versa, both in healthy and diseased conditions. Furthermore, wave propagation phenomena in the cardiovascular system can only be modelled by taking the vessel wall deformability into account. Devising an accurate model for the mechanical behavior of the arterial wall is a challenging task, since the vessel wall is anisotropic, heterogeneous, and composed of three layers (intima, media and adventitia) with different biomechanical characteristics.⁶⁸ An accurate model for the arterial wall should take into account the effects of anisotropy due to the distribution of the collagen fibers, the three-layer structure, the nonlinear behavior due to collagen activation, the incompressibility constraint, the surrounding tissues and the spatial variations in the vessel wall properties.

Modelling the interaction between the blood flow and the arterial wall represents one of the major challenges in the field of CFD hemodynamics. Prior to 2005, with the exception of the work developed by,^{66,73,100,148,153} and due mainly to the difficulties in formulating and solving the coupled problem of fluid and solid, nearly all blood flow simulations were conducted in rigid-wall models. However, in recent years, significant progress has been made in the area of FSI. Traditional FSI techniques can be divided into four categories on the basis of the utilized computational framework: linearized kinematics,^{37,41} coupled momentum method (CMM),⁴² immersed boundary method,^{80,151} and the arbitrarily Lagrangian–Eulerian (ALE) formulation.^{38,69}

Several authors have successfully simulated blood flow in TA models using ALE methods and non-ALE methods (see Table 1). To the best of our knowledge, the first full FSI simulation of blood flow in the TA

was performed by Gao *et al.*⁵⁶ on an idealized three-layer structure. The FSI system was formulated in an ALE frame and solved under unsteady flow conditions. Despite the predictions of blood flow dynamics utilizing an FSI technique, there were limitations to the present study. Among these were neglecting the arch branches, the aortic arch's non-planarity and the approximation of wall thickness. In general, ALE formulations are computationally expensive when considering large models of the vasculature, and less robust than linearized kinematics methods, since the mesh is deformed dynamically to always conform to the boundaries of the computational domain, requiring the continual update of the geometry of the fluid and the structural elements.

Later, Kim *et al.*⁸¹ presented a comprehensive FSI simulation in a patient-specific healthy TA model under rest and exercise conditions and a in a TA coarctation model under pre and post-intervention. The study used the CMM to describe the deformable wall properties and a coupled lumped parameter (zero-dimensional) heart model as an inlet boundary condition. The structure was mechanically constrained with fixed supports at the inlet and uniform deformable wall properties were considered, despite the fact that the arterial wall properties vary spatially. Although previous studies^{48,173} have used lumped parameter heart models, these studies were developed with the assumption of rigid arterial walls. In particular, the CMM shows good results in many physiological situations and it has the advantage of being computationally inexpensive because the mesh is fixed. Although the CMM is well suited for small displacements, this approach can be inappropriate when the displacements become large. Furthermore, as the fixed control volume where the fluid equations are solved allows the fluid to pass through the interface, the quantities computed at the boundary, such as the WSS, are subject to a further approximation.

Most recently, Brown *et al.*¹⁷ reported an alternative middle-ground approach to a full FSI simulation. It employed a compressible fluid model tuned to elicit a response analogous to the compliance of the TA wall, and thus to capture the wave propagation characteristics. It was stressed that changes in fluid density represent the capacity for changes of fluid mass within a cross-section, analogous to vessel wall compliance. The results showed that the use of a compressible fluid model, set to produce the desired wave speed, was able to capture the gross effects of the propagating waves. Furthermore, the results were significantly closer to those obtained from a full FSI simulation than those produced by a rigid wall model, but at relatively low computational costs. Although the compressible flow analysis over-estimates the WSS during systole, it does

capture the relative distribution of WSS and may offer a computationally viable alternative to a full FSI model.

Without question, FSI in the arterial system depend strongly on the tissue and organs outside the vessel of interest. Thus, a critical prerequisite for simulating realistic TA hemodynamics is the development of patient-specific constitutive models for the cardiac tissue that account for the complex interaction of the blood flow with the compliant and continuously deforming heart walls. The development of patient-specific FSI simulations is a formidable task since total heart function emerges as the result of the coupled interaction of the blood flow with a molecular, electrical and mechanical processes that occur across a wide range of scales.⁷² The first attempt to develop 3D models with coupled FSI simulation of blood flow and tissue mechanics was the pioneering work by Peskin.^{149,150} In this model the heart was assumed to be embedded in a periodic domain filled with fluid and the simulations were carried out under conditions that were not physiologic. More recently, different versions of this model have been able to carry out simulations at higher cardiac volume flow rate,^{62,110} and other models have attempted to raise the degree of patient-specific modelling realism by incorporating information acquired from non-invasive imaging techniques.^{84,134} The main challenges confronting this class of models stem from the limitations in the resolution of imaging modalities, as well as the extensive simplifying assumptions that need to be incorporated in the FSI model. To yield clinically relevant results, these models need to be drastically enhanced by incorporating into the modelling framework multi-physics elements of cardiac function along with inputs from modern imaging technologies and *in vivo* measurement techniques. Modelling the entire heart system would necessitate a modelling effort as complex as for the problem at hand, i.e., FSI in the TA.

In conclusion, compared to a rigid wall model, FSI can provide a more accurate and physiologic description of the hemodynamics as well as the arterial wall stresses and strains. Nevertheless, this comes at the cost of requiring more complex numerical algorithms, higher computational costs, and determination of patient-specific arterial wall properties, which are difficult to obtain experimentally or are often unknown. As noted by Taylor & Figueroa,¹⁹² new imaging techniques enable the characterization of the motion and thickness of the arterial wall; however, it remains a challenge to incorporate this *in vivo* data into FSI formulations. A new class of image-based FSI problems will require the development of non-invasive methods to assign tissue properties to the computational model from the medical imaging data, *via* the

solution of an inverse problem. Any CFD model that is intended for clinical application should capture the important physical characteristics, but should be no more complex than it needs to be. Whether or not FSI is included, the equations can only be solved if appropriate boundary conditions are given.

Boundary Conditions

The cardiovascular system is a closed network with millions of vessels interacting with each other. Since the input parameters to the CFD simulation are the boundary conditions, its choice plays a major role in modelling the upstream and downstream vasculatures absent in the computational domain of interest and must be carefully tuned to match clinical data. The question of where to cut this domain is not trivial: the further the boundary is from the area of interest, the less influence this artificial boundary will have on the local results, but the larger the computational domain will be. Inappropriate boundary conditions would result in non-physical solutions.

Inlet Boundary Conditions

Usually, at the upstream side of the artery of interest a velocity boundary condition is prescribed at the inlet, with an idealized profile such as a flat (plug), fully developed (parabolic) or Womersley flow pattern, or based on time-varying velocity data obtained with PC-MRI or ultrasound (see Table 1). Particularly, a flat velocity profile used together with a pulsatile waveform is often the preferred inlet boundary condition in transient TA studies. This pulsatile waveform is generally based on experimental data reported by Pedley,¹⁴⁷ and it is characterized by accelerating, decelerating, reversed, and zero flow regions (Fig. 2). The assumption of a flat velocity profile at the aortic inlet has been verified by various *in vivo* measurements using hot-film anemometry on different animal models, which have demonstrated that the velocity profile distal to the aortic valve is essentially flat in the ascending aorta, skewed towards the inner wall with respect to the aortic arch and only consisted of a weak helical component.^{40,131,172}

However, the fact is that the blood flowing into the TA pumped by the LV exhibits a complex 3D nature. Blood flow patterns in the healthy TA range from axial during the early portion of systole, to helical during mid-to-late systole, and complex flow recirculation during end systole and diastole (Fig. 3).⁷⁸ The development of helical flow patterns during peak to late systole is thought to be produced by several factors: (i) due to the arrangement of the muscle fibers, the LV undergoes a significant torsional deformation, twisting

in a counterclockwise direction during systole and then returning in a clockwise direction during diastole, resulting in diastolic recoil; (ii) the opening and closing dynamics of the aortic valve leaflets and their asymmetric configuration; and (iii) the curvature and the non-planarity of the TA. As aortic helical flow is a common feature in normal individuals as the consequence of the natural optimization of fluid transport processes in the cardiovascular system,^{78,119} and it is strictly related to transport phenomena of oxygen and LDL,^{98,104–106} great attention should be put when idealized velocity profiles are applied at the inlet boundaries of TA computational models.

On the other hand, time-varying pressure waveforms, usually available from catheterization based pressure acquisition technologies, are less frequently prescribed as inlet boundary conditions.^{143,202} Although it is claimed that the driving force for the blood flow in an artery is the pulsatile pressure gradient along the artery, the amount of blood flowing in the computational model is very sensitive to pressure gradients between inlet and outlets. As the pressure differences between these boundaries are only a small percentage of the systolic-diastolic pulse amplitude,

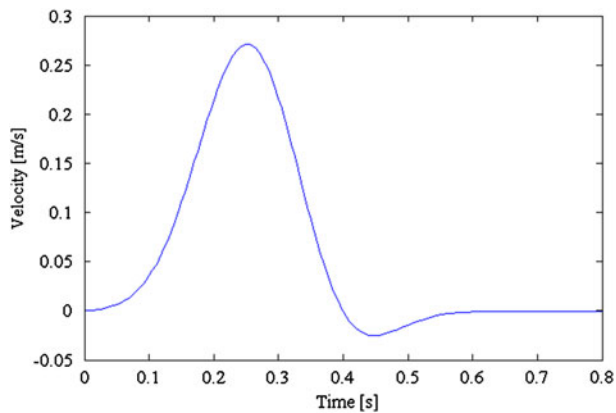


FIGURE 2. Inlet velocity pulsatile waveform at ascending aorta.

this imposes the problem of accurately determine the pressure, a condition that is difficult to reach in practice. Thus, small errors in the imposed pressure data could lead to great departure of the velocities from the actual values. Moreover, patient-specific pressure data is not currently acquired with enough precision to serve this purpose since an invasive approach could introduce sources of error and artefacts such as deterioration in frequency response, catheter whip artefact, end-pressure artefact, and systolic pressure amplification in the periphery, among others.⁷⁶

In contrast to several developments made in the area of outlet boundary conditions, little progress has been reported for the influence of inlet boundary conditions in CFD studies of large arteries, despite the fact that proximal to the inlet boundary there is also an upstream part of the cardiovascular system that interacts with the computational domain. Additionally, and with the exception of,^{117,160} no studies have investigated the effect of different inlet velocity profiles in the TA, and few have reported its effect in other large arteries.^{18,123,124,127} Morbiducci *et al.*¹¹⁷ studied how flat and fully developed inlet velocity profiles affect patient-specific simulated hemodynamics in the TA when compared to simulations employing PC-MRI measured 3D and axial (1D) velocity profiles of the patient's own *in vivo* measured flow data. The obtained results were compared in terms of WSS distribution and helical flow structures. It was found that the imposition of PC-MRI measured axial velocity profiles at the inlet may capture disturbed shear with sufficient accuracy, without the need to prescribe (and measure) realistic fully 3D velocity profiles. Likewise, attention should be put in setting idealized or PC-MRI measured axial velocity profiles at the inlet of the TA computational model when transport phenomena are investigated, since helical flow structures are markedly affected by the boundary condition prescribed at the inlet.

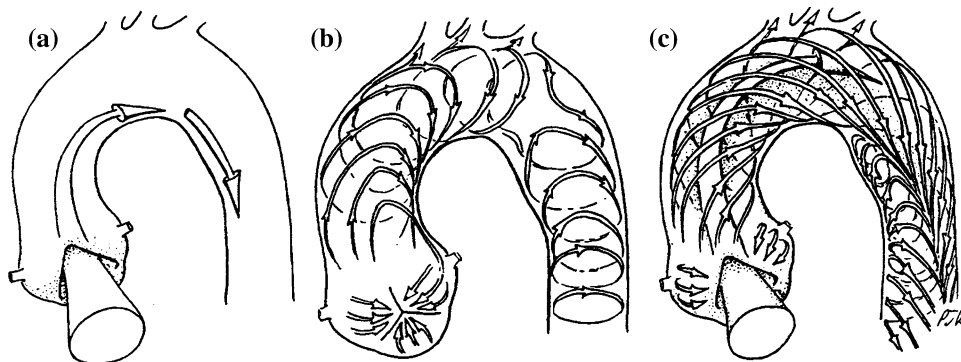


FIGURE 3. Schematic drawing delineating blood flow patterns in TA during early systole (a), mid-to-late systole (b), and end systole and diastole (c) (Copy from Kilner *et al.*, 1993).

While the above TA studies used inlet boundary conditions only valid for one particular physiologic state, thus, ignoring the bidirectional interactions between the computational domain and the heart, other TA studies have implemented reduced-order heart models as inlet boundary conditions (see Table 1). Particularly, Kim *et al.*⁸¹ developed and implemented a boundary condition that coupled a zero-dimensional (lumped parameter) heart model to the inlet of a patient-specific TA model, where the shape of the velocity profile of the inlet boundary were constrained. It was stated that in order to study how the changes in the cardiac properties and the cardiovascular system influence each other, the inlet boundary condition should model the interactions between them. While the aortic valve is open, the aortic flow and pressure, and the ventricular pressure and volume are computed through the coupling between the heart model and the TA model. When the aortic valve closes, the inlet boundary condition switches to a zero velocity boundary condition. Lumped parameter heart models approximate global characteristics of the heart using simple hydraulic models of resistance, capacitance, inductance parameters, pressure source and diode, resulting in time varying ordinary differential equations of flow and pressure.

Outlet Boundary Conditions

For the downstream side of the artery of interest, the boundary conditions have been a topic of debate and continuous development in the last years. In physiological conditions, arteries are branched and connected to smaller vessels, it is impossible to trace all the branching in the simulation and the model must be terminated at some point, depending on the specific aim of the study. Furthermore, these branches have to be lumped into a suitable terminal description, so that wave propagation and artery impedance characteristics can be reasonably represented.

Previously, the most common outlet boundary conditions for CFD simulations of large arteries were prescribed constant or time-varying pressures, constant (generally zero) traction and velocity profiles (see Table 1). Such boundary conditions are limiting in that they do not accurately replicated the fluid impedance of the downstream vasculatures. Particularly, if zero or equal pressures or tractions are used for different outlets, the flow split will be dictated solely by the resistance to flow in the branches of the domain of interest, neglecting the dominant effect of the resistance of the downstream vasculatures.^{140,193} Additionally, with constant pressure, zero traction, and velocity as outlet boundary conditions, computed blood pressure is not in the physiologic range and simulations could not be

performed where the flow distribution and pressure field are part of the desired solution.^{59,199}

In the case of time-varying velocity or pressure boundary conditions, first, obtaining such data for a model with multiple outlets is impractical. Second, even if this data was acquired simultaneously for each outlet, it would be very difficult to synchronize these waveforms in a manner consistent with the wave propagation phenomena in the arterial wall. Yet, with electrocardiogram gated measurements, there is likely to be a mismatch between the real and simulated wave speeds, which may results in spurious reflections within the computational domain. Finally, prescribing time-varying data is not relevant for treatment planning applications, where the quantity of blood flow exiting and the distribution of pressure are unknown and are part of the desired solution. Nevertheless, Gallo *et al.*⁵² recently investigated how the imposition of personalized PC-MRI measured blood flow rates as outlet boundary conditions influences the simulation results in a TA model. From six different outlet strategies to manage the acquired flow data, it was concluded that in order to obtain physiologically realistic results, the measured flow rates needed to be imposed at three of the four outlets of the TA model.

Another approach widely described in the literature is to prescribe outflow boundary conditions at the outlets as constant fractions of the inflowing blood (see Table 1). According to Middleman,¹¹¹ approximately five percent of the blood flow is assumed to leave the TA through each of the three arch branches, though some CFD studies have recalculate these percentages based on the specific outlet area of each arch branch or have used a modified version of the Murray's Law.¹²⁶ However, this flow ratio is not a realistic approximation for patient-specific FSI models, and there is no reason to believe that the flow division through the arch branches is constant during the entire cardiac cycle.¹⁹¹

To overcome the shortcomings of the above boundary conditions, other studies have used simplified boundary conditions that include either resistance or impedance models.^{15,112} In the TA study developed by Park *et al.*,¹⁴³ organs and body parts were assumed to be likened to cylindrically shaped porous media, so-called "pseudo-organs", and treated in the computational domain as forms of hemodynamic resistance. Permeability functions were determined from two-dimensional axisymmetric computations of each aortic branch. It was stated that there is a close similarity between blood flow through small vessels and the fluid flow through a porous medium. Thus, a proper permeability function could mimic flow through organs and body parts. Although resistance boundary condition do not require the specification of either flow rate or pressure data, it severely impacts wave propagation

phenomena, since it forces the blood flow and pressure waves to be in phase at the outlet and it can generate abnormal pressure values in situations of flow reversal.²⁰⁴

Increasingly, more sophisticated zero-dimensional (lumped parameter) models and 1D (distributed parameter) models have been used in multiscale (or multidimensional) models, in which their primary role is to provide boundary conditions for 3D computational simulations. For the 1D network models, branching patterns, length, diameter, and material properties of vessel segments are assigned; whereas for the lumped-parameter models, resistance, capacitance and inductance parameters are set to achieve the desired hemodynamic characteristics of the downstream domain. The coupling between these models can be solved in an explicit, staggered manner, or by embedding the reduced-order model into the equations of the 3D computational domain. A lumped parameter model is a dynamic description of the physics neglecting the spatial variation of its parameters and variables. If the model is distributed, these parameters and variables are assumed to be constant in each spatial compartment. Therefore, a lumped parameter model is governed by a group of ordinary differential equations that assume a uniform distribution of the fundamental variables (pressure, blood flow and volume) within any particular compartment of the cardiovascular system at any instant in time, whereas a distributed parameter model can be described by hyperbolic partial differential equations that recognise the variation of these parameters in space. This is illustrated in Fig. 4. A comprehensible review of zero-dimensional and 1D models of blood flow in the cardiovascular system can be found in.¹⁷⁷

Several studies have successfully coupled distributed parameter models to 3D models,^{10,46,142,197} including some TA studies (see Table 1). However, solving the transient nonlinear 1D equations of blood flow in the millions of downstream vessels is an intractable problem, and therefore linearized 1D models are needed. These simplified linear methods usually assume periodicity of the solution.^{139,183,204} Yet, blood flow and pressure in large arteries are not always periodic in time due to heart rate variability, respiration, physiological changes or complex transitional flow.¹⁷⁶ On the other hand, some studies have successfully coupled lumped parameter models to 3D models,^{7,94,113,181} including some TA studies (see Table 1). Different strategies for coupling the 3D equations with lumped parameter models have been presented in.^{155,156} However, in the majority of these studies the coupling has been performed iteratively, which can lead to stability and convergence issues, and has been generally applied to geometries with one or two outlets, rigid walls and low

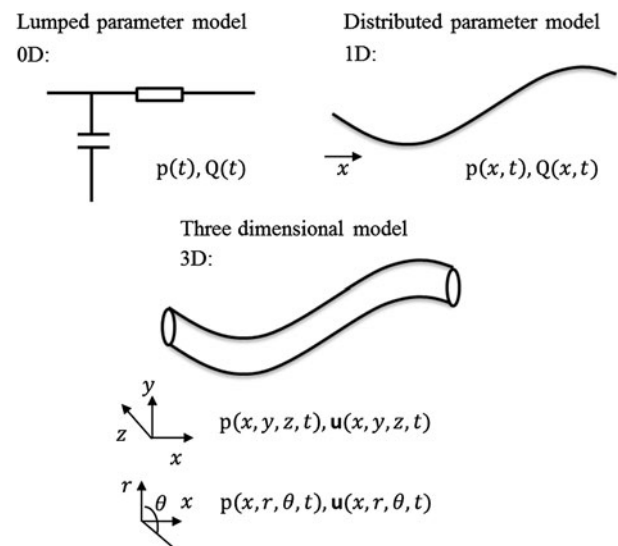


FIGURE 4. Different scales of modelling.

resistances (as seen in the pulmonary vasculature). In contrast, a recent work presented by Vignon-Clementel *et al.*²⁰⁵ extended the multiscale modelling to include boundary conditions that accommodate the non-periodic or transient phenomena using lumped parameter outlet boundary conditions. This approach considered the arterial wall response to blood flow and pressure on patient-specific multi-branched geometries.

Although with multiscale models, outlet boundary conditions are derived naturally through the coupling of the 3D computational domain and the downstream reduced-order models, the relationship between flow and pressure at each interface is generally enforced weakly, as a result of the coupling between a numerical domain and analytic domain; which usually results in diverging simulations. This coupling usually does not include any constraints on the shape of velocity profiles nor on the pressure distribution at the interface. Yet, reduced-order models are derived based on an assumed shape of the velocity profile and the assumption of uniform pressure over the cross section.^{27,70} As a result, some remaining challenges persist; these include problems where flow is complex, with significant flow reversal during part of the cardiac cycle, and with complex flow structures developing at the outlet boundaries due to vessel curvature or branches immediately upstream of the boundary.

A common but rather rudimentary workaround to this problem has consisted of extending the outlet branches using long straight segments to regularize the blood flow. Recently, new formulations have been developed to resolve this issue numerically. Formaggia *et al.*⁴⁷ implemented a total pressure boundary condition to control the energy flux entering and exiting the computational domain and to stabilize problems with

complex flows near boundaries. However, this approach requires an unconventional formulation of the Navier–Stokes equations and has not yet been proven to resolve boundary instability issues in complex hemodynamic simulations. An alternate solution to this problem has been proposed by Kim *et al.*,⁸¹ where an Augmented Lagrangian formulation was used to constrain the shape (but not the magnitude) of the velocity profile at the inlet or outlet boundaries, rendering stable solutions regardless of the complexity of the blood flow.

Arterial Wall Boundary Conditions

Whereas much work has already been accomplished concerning outlet boundary conditions, few CFD studies have taken into account the external tissues surrounding the TA to derive adequate boundary conditions for the arterial wall domain (see Table 1). Large arteries subject to a high load, as it is the case in the TA, undergoes large deformations concerning both the luminal radius and the vessel displacement displacements, and experiences a complex coupling with surrounding tissues and organs, namely interactions with the spine on the outer wall and with the heart in the ascending aorta. However, in the majority of the FSI studies we are aware of, a free stress condition with a constant (frequently zero) pressure has been applied on the outer part of the arterial wall. This simple boundary condition is not able to sustain the artery and typically results in non-physiological motion patterns of the arterial wall. In fact, this motion induces inaccuracies much greater than those introduced by spurious reflections caused by inconsistent inlet and outlet boundary conditions.

To take into account the influence of the heterogeneous tissue surrounding the TA, Crosetto *et al.*³⁰ introduced a Robin condition¹⁵⁴ at the outer arterial wall. This condition consisted of a pressure–displacement linear constitutive relation; relation previously investigated *in vivo* and *in vitro* by Liu *et al.*¹⁸¹ In the latter work, the intraluminal pressure was shown to be proportional to the radius of the lumen only when the surrounding tissue was taken into account. The main difficulty encountered by Crosetto *et al.*³⁰ was to configure a suitable choice of one of the models parameter. Though this choice was empirical, the results led to physiological displacements and fitted qualitatively with the plot reported by Liu *et al.*¹⁰³ It was found that the pulse wave velocity, WSS, mean pressure, velocity and intraluminal radius at different axial sections along the artery were in the physiological range, though many parameters have to be adapted on a patient-specific basis. To the authors' knowledge, this was the first FSI study that addresses the formulation

of an adequate boundary condition for the external tissue when studying the TA.

Similarly, Moireau *et al.*¹¹⁵ introduced a boundary condition along the TA outer wall that consisted of a viscoelastic term representing the support provided by the surrounding tissues and organs. A forcing term was used at the inlet boundary of the arterial wall to account for the heart motion. This simple model corresponds to a generalized Robin condition on the walls and relies on two adjustable parameters to mimic the response of various physiological tissues. Time-varying medical imaging data was used to obtain information on the apparent motion of the wall. In order to illustrate the versatility of this approach, two different patient-specific modelling cases were implemented, using a distinct FSI technique for each (ALE and CMM). When applied to an inlet or outlet arterial wall boundary, the viscoelastic term represents the truncated arterial tree extending from the geometric model. Comparably, when applied along the exterior surface of the arterial wall, the viscoelastic term models tethering to the external organs. This approach was shown to improve the quality of the simulations by providing accurate deformation patterns of the arterial tree. However, this required a careful manual calibration process of the parameters in the boundary support model. More recently, Moireau *et al.*¹¹⁴ proposed a method to automate and refine this calibration process. A complete methodological chain for the identification of boundary support parameters in a TA model based on well-adapted sequential data assimilation procedures^{11,130} was presented.

In summary, blood flow dynamics in the domain of interest cannot be simulated in isolation from the rest of the cardiovascular system. Physiologically accurate boundary conditions that are robust as well as simple to implement must be carefully considered for each particular problem. Ideally, patient-specific measurements data should be implemented as boundary conditions, however such information is not always available, and hence reasonable assumptions must be made. With the development of computer hardware and numerical analysis techniques, it now is possible to build multiscale models coupling reduced-order models with the 3D computational domain. However, the treatment of the domain boundaries among the different dimensional models within an overall framework still needs further improvement. This includes not only the matching of the mean pressure/flow values and their distribution information on the interfaces, but also the correct wave reflection description. Therefore, in order to perform multiscale blood flow simulations efficiently, the next step would be to develop numerical optimization algorithms that automatically tune the best parameter values for obtaining

experimentally measured data. Breakthroughs to be made on this issue will be extremely helpful to the improvement of simulation accuracy.

Turbulence Models

The characteristic dimensionless parameter that describes viscous flows is the Reynolds number Re , defined as:

$$Re = \frac{\rho \mathbf{u} D}{\mu} \quad (1)$$

where D is the artery diameter, \mathbf{u} is the characteristic fluid velocity (mean cross-sectional velocity), ρ is the density of blood (Newtonian fluid) and μ is the blood dynamic viscosity. A typical density for blood is 1050–1060 kg/m³ (at 37 °C). The Reynolds number is a measure of the ratio of inertial forces ($\rho \mathbf{u}^2$) to viscous forces ($\mu \mathbf{u}/D$). Hence, at high Reynolds numbers ($Re > 4000$), inertial forces are dominant, whereas viscous forces become significant only at low Reynolds values ($Re < 2300$). The transitional regime from laminar to turbulent flow occurs in the interval between 2300 and 4000. Generally, blood flow in the large arteries has been assumed to be laminar both in steady and unsteady flow conditions, since the mean flow velocity has been predicted low enough to result in relatively low Reynolds number.^{50,102,132} For pulsatile flow, turbulence may occur for a Reynolds number much larger than expected for steady flow, due to the fact that accelerating flows tend to be more stable than steady flows.^{51,64}

However, some studies have found that the pulsatile flow in the TA has Reynolds numbers in the transitional regime, which creates a very complex 3D flow field.^{118,182} While systolic acceleration normally has a stabilizing effect on the blood flow, flow disturbances might appear during the deceleration phase. Stein and Sabbah¹⁸⁴ measured blood velocity in both healthy and diseased patients and found highly disturbed flow patterns during systole and the early part of diastole in healthy patients, and fully turbulent flow in patients with aortic insufficiency. Likewise, Peacock *et al.*¹⁴⁶ conducted an experimental study where the critical Reynolds number for the onset of turbulence under physiological conditions in a straight pipe was measured. It was found that the critical Reynolds number normally found in the aorta was on the order of 5500, and since the peak Reynolds number is usually higher, their results predicted the existence of disturbed aortic flows. More recently, Stalder *et al.*¹⁸² used MRI data to study the TA blood flow in a large cohort of 30 young healthy patients, it was concluded that flow instabilities were present in healthy subjects at rest, but not necessarily a fully turbulent flow. According to the

calculated critical Reynolds numbers, flow instabilities were prominent in the ascending (14/30 volunteers) and descending aorta (22/30 volunteers) but not in the aortic arch (3/30 volunteers). They expected that turbulence effects might be more pronounced for higher cardiac outputs, or in the presence of CVDs.

Model blood flow is complex due to its transitional and disturbed nature, and might be best treated with a turbulence model that can account for these effects. Several authors have implemented turbulence models in TA simulations (see Table 1). Early works predominantly employed the Reynolds averaged Navier–Stokes (RANS) equations, which provide a time averaged solution of the flow and some estimates of its fluctuating behavior.^{5,166,200} RANS turbulence models thus provide a somewhat limited representation of the blood flow, lacking the dynamics of the turbulence and are not the ideal choice for simulating complex blood flow.²¹⁸ Direct numerical simulation (DNS) resolves all spatial and temporal scales of the flow, but is greatly expensive in terms of computational costs. In addition, the use of complex geometries is strongly limited due to the high order numerical schemes. A scale-resolving turbulence model such as large eddy simulation (LES) on the other hand, may be more suitable, due to the finer resolution and its ability to handle transitional effects. Also, the computational costs compared to a DNS are significantly reduced, while most of the dynamics are captured in the numerical calculations.

There have been a number of numerical studies using LES on idealized arterial geometries,^{57,145,189,201} including some TA studies (see Table 1). The results have been in good agreement with experimental data, demonstrating the potential for modelling physiological low-Re transitional flows using LES models. More recently, Lantz *et al.*^{97,98} conducted scale resolving blood flow simulations in patient-specific TA models under pulsatile flow conditions. The objective of these studies was to characterize the disturbed flow field and to investigate the relationship between WSS and LDL surface concentration using a LES model. They found that disturbed flow was present in the aorta when the peak Reynolds numbers was on the order of 5000–6000, and that the disturbances had a significant effect on the LDL surface concentration. The disturbances formed predominantly in the descending aorta during the latter part of systole, but were still present in the beginning of diastole. Also, it was found that the accumulation of LDL was inversely correlated to WSS. In general, regions of low WSS corresponded to regions of increased LDL concentration and vice versa. Therefore, the near-wall velocity field was investigated at four representative locations. It was concluded that in regions with disturbed blood flow the LDL concentration had significant temporal changes, indicating that

LDL accumulation is sensitive to not only to WSS but also near-wall flow patterns, such as disturbances and high near-wall velocities. The fact that blood flow can exhibit high frequency fluctuations in the range of transitional flow in healthy patients is probably not a coincidence, but an effect of evolution. Thus, care must be taken to accurately compute the flow field, which has important implications for the pathophysiology of CVDs and the design of cardiovascular devices. A new perspective about turbulence in blood flow is discussed in.²

GOVERNING EQUATIONS AND BLOOD FLOW MECHANICS

Navier–Stokes Equations

3D fluid flows can be sufficiently described in a mathematical form by a group of partial differential equations known as the Navier–Stokes equations. These are based on the laws of motion (momentum equation), conservation of mass (continuity equation) and conservation of energy (energy equation). Under the assumptions of an incompressible, homogenous, Newtonian fluid, the Navier–Stokes equations can be described as:

$$\rho \frac{\partial \mathbf{u}}{\partial t} + \rho(\mathbf{u} \cdot \nabla)\mathbf{u} = -\nabla p + \mu \nabla^2 \mathbf{u} \quad (2)$$

$$\nabla \cdot \mathbf{u} = 0 \quad (3)$$

where the primary variables are the velocity vector $\mathbf{u} = [u, v, w]$ and the pressure p that vary in space x, y, z and time t . Note that taking into account non-Newtonian effects is possible, provided that the above equations are changed appropriately. For simple cases, these partial differential equations have an analytical solution.^{128,208} However, for more general flows involving complex geometries and/or complex boundary conditions, it is necessary to solve the system of Navier–Stokes equations by numerical methods.

Two numerical methods for solving the Navier–Stokes equations are available: finite element method (FEM) and finite volume method (FVM). The FEM uses simple piecewise polynomial functions on local elements to describe the variations of the unknown flow variables. When these approximate functions are substituted into the governing equation, they will not hold exactly, and the concept of a residual is introduced to measure the errors. These residuals are then minimized by multiplying by a set of weighting functions and then integrating. This yields a set of algebraic equations for the unknown terms of the approximating

functions. On the other hand, the FVM employs an integral form of the conservation laws directly into a finite number of smaller sub-domains called control volumes. Finite difference type approximations are then substituted for the terms of the integrated equations, forming algebraic equations that are solved by an iterative method. One of the advantageous features of FVM is its conservation properties, since it is based on applying conservation principles over each control volume, global conservation is ensured. Another advantage of FVM is that is not limited to a single grid type; it gives freedom to use both structured and unstructured meshes.

The majority of TA studies have been conducted using several commercially CFD software packages, such as CFD-RC, FIDAP and STAR-CD. Fluent and CFX, both available from ANSYS Inc., are the CFD commercial products most often used for modelling blood flow. In addition, open-source toolkits like LifeV and SimVascular have also been used. Other research groups have developed their own CFD solvers to suit their specific problems. Since CFD uses iterative methods to solve the governing equations, convergence is an important consideration. Different researchers use different measures of convergence, but it is common to look at the residuals, which should decrease below a threshold value, and some local and global flow parameters which should reach a steady state. The convergence criterion for the residuals should be determined by examining how much the important flow characteristics change between different values. For novice CFD users who, whilst developing CFD skills by using commercially available software, need a detailed discussion on how CFD code would enable to solve the Navier–Stokes equations rather than relying on the commercialized CFD codes, please refer to.²⁰³

Blood Flow Mechanics in Large Arteries

Basic aspects of the mechanics of blood flow in idealized anatomies are presented. Arteries are modeled as rigid-wall tubes of uniform circular cross-sections, and the blood is assumed as a homogeneous incompressible Newtonian fluid. For a detailed analysis of these concepts refer to.^{20,144,147}

WSS

Wall shear stress, τ , is the tangential force exerted on the arterial wall by the blood flow. For a Newtonian fluid, WSS is proportional to the gradient of the velocity, du/dr (shear rate), and is given by:

$$\tau = \mu \frac{du}{dr} \quad (4)$$

where μ is the blood dynamic viscosity and r is the radial direction perpendicular to the arterial wall. For blood flow moving next to solid boundaries the no-slip condition applies, which states that the velocity of the blood is zero at the rigid arterial wall. The total shear stress exerted on the wall throughout an entire cardiac cycle can be evaluated using the time-averaged WSS (TAWSS) which can be expressed as:

$$\text{TAWSS} = \frac{1}{T} \int_0^T |\bar{\tau}| dt \quad (5)$$

where $|\bar{\tau}|$ is the magnitude of the instantaneous WSS vector and T is the temporal period (cardiac cycle). Another hemodynamic parameter that is often used in the literature to describe the cyclic variation of WSS is the Oscillatory Shear Index (OSI), defined according to He and Ku⁶⁵ as:

$$\text{OSI} = \frac{1}{2} \left(1 - \frac{\left| \frac{1}{T} \int_0^T \bar{\tau} dt \right|}{\frac{1}{T} \int_0^T |\bar{\tau}| dt} \right) \quad (6)$$

where $\bar{\tau}$ is the instantaneous wall shear stress vector. The oscillatory shear index is a measure of the deviation of the WSS vector from its predominant axial direction of the flow over one cardiac cycle, thus characterizes flow separation from the arterial wall. It takes values in the range of 0 to 0.5, where lower OSI values indicate WSS is oriented predominately in the primary direction of the blood flow while a value of 0.5 means that the instantaneous vector never is aligned with the time-averaged vector, which indicates a very oscillatory behavior. OSI is insensitive to shear magnitude and must therefore be used with caution; a large OSI value can indicate a disturbed flow region with high or low WSS magnitudes.

Womersley Number

Blood flow in large arteries is driven by the heart, and accordingly it is highly pulsatile. The dimensionless parameter that is usually used to describe unsteady flows is the Womersley number, α (or Wo), defined by Womersley²¹⁷ for flow in a straight tube:

$$\alpha = \frac{D}{2} \sqrt{\frac{\omega}{\nu}} \quad (7)$$

where $\omega = 2\pi/T$ is the oscillatory frequency (angular frequency) and $\nu = \mu/\rho$ is the kinematic viscosity. The Womersley number is essentially a frequency parameter that measures the instability of the flow in relationship to its viscous forces. For low frequencies ($\alpha < 1$), the viscous forces govern, the velocity and pressure waveforms are in phase and the velocity

profile is parabolic (quasi-steady flow). For high frequencies, the unsteady inertial forces dominate, there is a phase lag between the velocity and pressure waveforms and the flow assumes the shape of a flat velocity profile, i.e., disturbed flow. The Womersley number in the human aorta can take values between 10 and 20,²¹ implying that the unsteady flow plays a role in large arteries.

Flow in a Straight Tube

Figure 5 shows the development of a steady laminar flow in a straight tube. At the entrance of the tube the velocity profile is almost flat. Due to the no-slip condition, the velocity is zero at the walls and a velocity gradient is immediately generated with the adjacent moving fluid. As a result of this traction, high WSS appears on the wall and a viscous boundary layer grows. The boundary layer progressively decelerates the near-wall fluid, while acceleration occurs at the center of the tube. The shear stress is gradually reduced on the wall until it becomes constant when the boundary layer has filled the tube and a parabolic velocity profile has been established. This is the well-known steady fully-developed laminar flow (Poiseuille flow).

Flow in a Curved Tube

In order to measure and interpret the flow dynamics in the complex geometry of the human aortic arch, it is important to understand the effect of curvature on the flow development. In curved tubes the fluid particles are forced to change direction and accelerate in order to preserve the axial flow. The large pressure gradient that is developed is what drives this acceleration. If the initial flow is fully developed, the central highest velocities have high inertia and cannot be easily deflected. Fluid near the wall has less inertia and therefore is greatly displaced. Consequently, the highest velocities do not occur in the center but are found closer to the outer wall of the curvature. The displacement also generates secondary motions in the transverse plane in the form of two counter-rotating vortices (Dean vortices) moving from the outer bend to the inner bend along the walls of the tube (Fig. 6), as occur when there is a flow around a pipe bend.⁹⁵ The

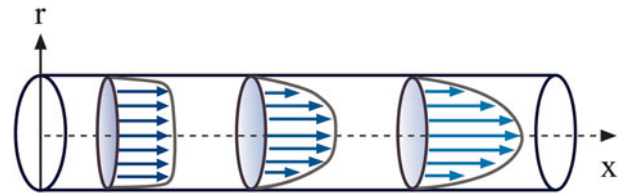


FIGURE 5. Development of steady laminar flow at the entrance of a straight tube (Reproduced after Caro *et al.*, 1985).

skewness of the velocity profile implies that in a curved tube high shear stress is developed on the outer wall, and low shear stress on the inner wall.

Dean^{35,36} developed the analytical solution for a fully developed, steady viscous flow in a curved tube of circular cross section, and demonstrated that the degree of influence of curvature on a steady streamlined flow can be expressed by the dimensionless Dean number:

$$De = Re\sqrt{\frac{r}{R}} \quad (8)$$

where r is the tube radius and R is the radius of curvature. The Dean number is a measure of the ratio of centrifugal inertial forces to viscous forces, analogous to the definition of the Reynolds number. With an increasing Dean number, the effects of the centrifugal forces become stronger and increase the secondary motions. Dean number can be used to assess the variation due to the radius of curvature effects along the aortic arch.

Flow in a Bifurcation

When a steady fluid flow arrives at a bifurcation, it is forced to divide into the branches (Fig. 7). Due to its high inertia, the acting pressure gradient cannot displace it immediately into the axial directions of the branches and, hence, the flow moves next to the inner walls of the bifurcation. High shear is developed, as a result, on the flow divider. On the contrary, near-wall fluid in the parent vessel has less inertia and can be greatly deflected. This generates secondary motions in

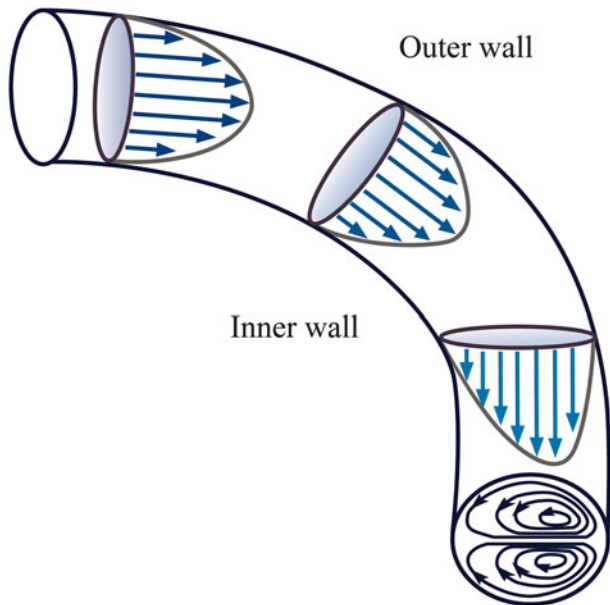


FIGURE 6. Steady flow in a curved tube with the presence of skewed axial velocity profile and secondary motions (Reproduced after Caro *et al.*, 1985).

the transverse plane, while low shear regions develop on the outer walls of the bifurcation. New boundary layers develop along the inner walls that eventually reestablish the Poiseuille flow type in both daughter branches further downstream. At very high initial velocities and sharp angles, large pressure gradients may cause separation of the flow and the formation of a separation zone or flow reversal at the outer walls. Such zones are characterized by high particle residence times and low values of WSS.

POST-PROCESSING

After the governing equations are solved and the convergence criterion is reached, the simulation results are analyzed and visualized at different locations and time instants. Additional hemodynamic parameters of interest computed from the basic flow fields, such as WSS, energy losses, pressure wave propagation, wall compliance, mass transport phenomena and particle residence time, are usually interpreted by means of contour and vector plots, streamlines and particle tracking, or 2D and 3D surface plots. A significant challenge of patient-specific modelling is making sense of the large amount of numerical data that can—and should—be extracted. Also, this data must be analyzed at different levels of detail for different purposes; maps of quantities of biological significance may be of interest to a clinical audience, while other quantities must be considered if the computational model was integrated with a reduced-order model.

In order to organize in a detailed manner the findings of the TA studies included in this review, comparative information is provided in tabular format. Table 1 is organized chronologically and provides the model setup, simulation results and a summary of the major insights and contributions of each article reviewed.

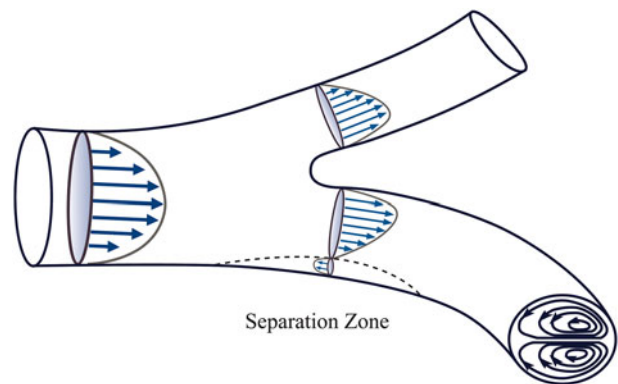


FIGURE 7. Steady flow in a bifurcation with a separation zone, secondary flow, and skewed axial profile (Reproduced after Caro *et al.*, 1985).

Conference papers were not included. In general, most TA studies focused on surface-based parameters, which are thought to be most closely linked to the pathogenesis of different CVDs. WSS, TAWSS and OSI remain the most commonly reported hemodynamic wall parameters in CFD studies (Fig. 8). Traditionally, these quantities have been presented as spatial maps or trends at a particular spatial location. As TA studies have moved from idealized to patient-specific cases, several groups have encouraged a more statistical treatment of these parameters. Besides from surface-related quantities, velocity fields and volumetric parameters also have much to tell. Velocity iso-contours are ideal for visualizing or quantifying regions of slow recirculating and retrograde flow at branches. Simulated dye studies are attractive for visualizing the complexities of pulsatile flows but also for facilitating indirect comparisons against *in vivo* image-based data. It is likely that a variety of other quantities -yet to be identified - will need to be interrogated as new biological mechanisms are identified and new numerical models are developed to understand them. Discussions between the clinician and the scientist are then the key to choose such parameters and to interpret the results.

Verification and Validation

An acute aspect of CFD hemodynamic studies is their verification and validation. Verification is defined as the assessment of the numerical accuracy with which the computational model was implemented. This process usually relies on the existence of an analytical solution for the model. By contrast, validation is the process of determining the degree to which the computational model is an accurate representation of the real world, and quantifying its uncertainty. A simulation is considered to be validated if the differences between its results and experimental data are small and if the uncertainties in the experimental results are also small.²⁰³ It is clear that when developing new models for hemodynamic modelling, the verification should precede any attempt of validation. A clear distinction between verification and validation is given by Roache and Babuska & Oden,^{3,164} who describe verification as “solving the equations right”, whereas validation is “solving the right equations.”

Traditionally, CFD validation studies have primarily used *in vitro* models.^{45,87,91} Kung *et al.*⁹⁰ compared numerical simulations of flow and pressure incorporating deformable walls using *in vitro* flow phantoms under physiological flow and pressure conditions. Regarding *in vivo* validation, relatively few studies have been published comparing patient-specific hemodynamics simulations with *in vivo* measurements.^{44,86,158} Boussel *et al.*¹⁴ compared CFD data and

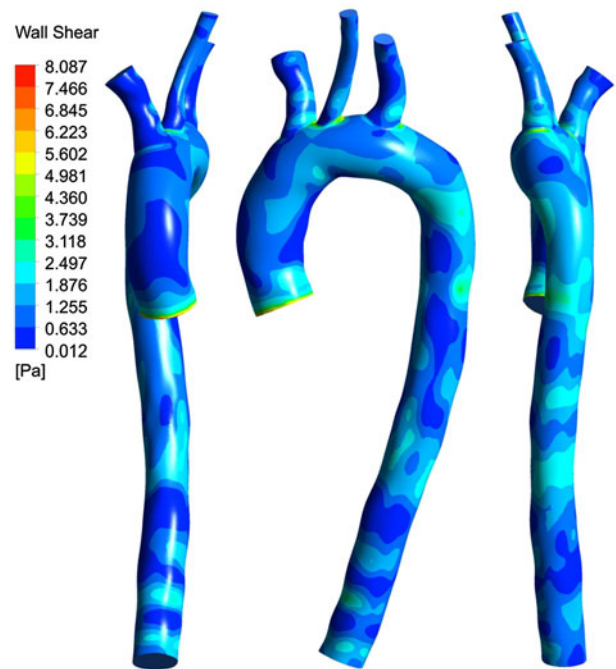


FIGURE 8. Example of WSS (Pa) distribution in a healthy TA 3D model in steady state simulation.

in vivo PC-MRI measurements in patient-specific intracranial aneurysms models. They reported favorable agreement for flow patterns and velocities, but poor agreement for WSS due to the incapability of PC-MRI to capture near-wall velocity gradients.

To the authors' knowledge, full validation TA studies comparing patient-specific simulations with *in vivo* data have not been published. In^{73,99,100,159,188,213} some velocity results were slightly compared with PC-MRI data measured at different sections of the TA that were not used as boundary conditions. Though the simulation results reported good qualitative agreement between computed and PC-MRI *in vivo* velocity patterns, this does not show that flow field details are being correctly predicted, but it does give some assurance and is a first step towards validation. Although initial results are encouraging, *in vivo* validation studies remain in their infancy. PC-MRI offers the greatest promise as an *in vivo* gold standard, but still provides a comforting but inconclusive evidence that simulations are physiological faithful. In addition, it is likely that validation studies may require the acquisition of extra data; however, this additional cost is critical if we are to rely on simulation-based results in the future. In the context of predictive simulations, establishing a database of experimental results which could act as test cases for research groups wishing to validate their computational models would be useful, and may call for novel clinical protocols.

TABLE 1. Summary of the major insights and contributions of each TA article.

ID	B. Conditions							Major insights and contributions	
	Geometry	Blood	A. Wall	Inlet	Outlet	Time	Flow		
121	I-M	Water	R	FV-SW	Z	B	L	WSS, velocity	First study that used an idealized MRI-based TA geometric model (no arch branches)
120	I-M	Water	R	FV	Z	S	L	WSS, velocity	First study that used an idealized MRI-based TA geometric model with arch branches
174	I-C	N	R	FV-PW	O	U	L	WSS, velocity, tracer distribution, pressure	A passive scalar (tracer) was used to visualize the pulsatile blood flow. First detailed TA study
73	P-M	N	FSI	MV	MV + O	U	L	WSS, velocity	First study that used a patient-specific TA geometric model. Radial expansion–contraction and translational motion in the ascending aorta was prescribed. Rigid wall elsewhere. Measured velocity at descending aorta, outflow at branches. Comparison with MRI data measured at ascending aorta
100	P-M	N	ALE	MV	Z	U	L	WSS, velocity	Study only considered the ascending aorta geometry. Comparison between blood flow distal to an artificial heart valve and native flow of a healthy patient. Comparison with MRI data measured at aortic arch
79	I-C	N	R	FV-PW	O	U	L	Womersley number, Schmidt number, tracer distribution, velocity	Tracer visualization method was analyzed in more detail compared to ¹⁷⁴
122	I-C	N	R	FV-PW		B	L	Velocity, WSS	Three TA geometric model variations were simulated (no arch branches)
56	I	N	ALE	FV-PW	Z	U	L	Pressure, wall stress distribution	First full FSI study. A three-layered TA model (no arch branches) was used to study the influence of medial wall stiffness on wall stress distribution
54	I	N	ALE	FV-PW	Z	U	L	Pressure, wall stress distribution, velocity, wall deformation	Blood flow dynamics was analyzed in more detail compared to ⁵⁶
53	I	N	ALE	FV	Z	S	L	Velocity, pressure, WSS, wall deformation, wall stress distribution	Blood flow dynamics was analyzed under steady flow conditions
58	P-M	N	R	MV + PV-PW	O	U	L	WSS, velocity	Two velocity inlet boundary conditions were simulated to compare the WSS distribution
143	I	N	R	MP	-	U	L	Pressure, velocity	Pseudo-organs were connected at outlets. Power Law permeability functions derived from 2D computations were used in 3D simulations as outlet boundary conditions

TABLE 1. Continued.

ID	B. Conditions					Major insights and contributions			
	Geometry	Blood	A. Wall	Inlet	Outlet		Time	Flow	Simulation results
55	I	N	ALE	FV	Z	S	L	Pressure, velocity, wall stress distribution	A three-layered healthy and diseased TA models (no arch branches) were used to investigate the combined effects of arch aneurysm and medial wall stiffness on wall stress distribution
96	I	N	R	FV-PW	PP	U	L	Velocity, drag force	Study investigated the hemodynamics factors affecting the drag force on a stent-graft TA model (no arch branches)
180	I	PI	R	FV-PW	O	U	L	WSS, LDL, velocity, strain rate, molecular viscosity	First detailed mass transport study. The influence of pulsatile flow on LDL transport and WSS was analyzed
159	P-M	N	R	MV	O	U	L	WSS, velocity	Blood flow of nine healthy patients was simulated. Patient-specific viscosities were measured. Comparison with MRI data measured at ascending aorta
160	P-M	N	R	MV + FV-PW	O	U	L	WSS, velocity	Two velocity inlet boundary conditions were simulated to compare the WSS distribution
81	P-M	N	CMM	0D	0D	U	L	Pressure, velocity, WSS, OSI	Detailed multiscale study investigated blood flow dynamics in a healthy TA model under rest and exercise conditions, and in a TA coarctation model under pre and post-intervention
106	P-M	N	R	FV	O	S	L	Velocity, LDL, WSS	Four TA geometric model variations were simulated to assess the influence of helical blood flow on LDL transport
188	P-M	N	R	MV	Z + O	U	L + SST	Velocity, TAWSS, OSI, turbulence level	Detailed study investigated laminar and transitional blood flow on a TA aneurysm model. Zero pressure at descending aorta, outflow at branches. Comparison with MRI data measured at descending aorta
213	I	N	R	MV	MP	U	L	Velocity, pressure, WSS, OSI	Study investigated the relationship between aortic dissection and blood flow dynamics. <i>In-vitro</i> flow rate and pressure data was used as boundary conditions. Comparison with MRI data measured at different locations
104	P-M	N	R	FV	O	S	L	Helicity density, Sherwood number, hemoglobin, WSS	Three TA geometric model variations were simulated to assess the influence of helical blood flow on oxygen transport
209	I	N	ALE	FV-PW	PP	U	L	Von Mises stress, velocity, wall deformation	Three TA geometric model variations (no arch branches) were simulated to assess the influence of curvature and flexibility on the wall Von Mises stress
210	I	N	ALE	FV-PW	PP	U	L	Velocity, strain rate, WSS, wall deformation	An aneurysm TA model (no arch branches) was used to investigate the combined effects of FSI and different viscosities on blood flow dynamics

TABLE 1. Continued.

[]	Geometry	Blood	A. Wall	B. Conditions			Flow	Simulation results	Major insights and contributions
				Inlet	Outlet	Time			
105	P-M	N + Ca	R	FV-PW	-	B	L	Helicity density, OSI, Sherwood number, WSS	Detailed study investigated the effect of both non-Newtonian and pulsatile blood flow on LDL and oxygen transport
30	P-M	N	R + ALE	1D	1D	U	L	WSS, velocity, pressure, wall deformation	Study investigated the effect of different sets of boundary conditions. Pressure and flow rate data obtained from 1D simulations was imposed as boundary conditions. An arterial wall boundary condition was considered
179	I	PI	R	FV-PW	O	U	L	LDL	Study examined the LDL accumulation in the aortic wall with shear dependent endothelium properties
9	I	N	R	FV-PW	-	B	SST	Velocity, WSS, wall stress distribution, turbulence level	Study investigated blood flow dynamics for physiologic and extracorporeal circulation, the latter being the main focus. A model based on the prescription of loss coefficients was used as outlet boundary conditions
99	P-M	N	R + CMM	MV	0D + O	U	SST	Velocity, pressure-volume relation, TAWSS, OSI, WSS	Detailed comparison between FSI and a rigid-wall TA models. Lumped parameter model coupled to the descending aorta, outflow at branches. A physiological range of different wall stiffnesses was simulated. Comparison with MRI data measured at descending aorta
196	P-C	N	R	FV-PW	PP + O	U	L	Velocity, pressure, TAWSS	Study investigated blood flow dynamics on pre-aneurysmal and post-aneurysmal dissecting TA models. Pressure at descending aorta, outflow at branches
43	P-C	N	R	MV	Z + MV	U	L	Velocity, TAWSS, OSI	Study investigated blood flow dynamics on pre-aneurysmal and post-aneurysmal TA models. Zero pressure at descending aorta, measured velocities at branches
77	Curved tube	N	R	FV-PW	Z	B	L + SST	Velocity, WSS, pressure, OSI	Study investigated the effect of different severities of TA coarctation and stenosis on blood flow dynamics
138	P-M	N	R	FV	O	S	SST	WSS, velocity	Study investigated blood flow dynamics on a coarctation and three post-coarctation TA models
93	P-M	N	CMM	MV	0D	U	L	Velocity, TAWSS, OSI, wall deformation	Study investigated blood flow dynamics on a healthy and four coarctation TA models under rest and exercise conditions. An arterial wall boundary condition was considered
92	P-M	N	R	MV	0D	U	L	TAWSS, OSI, velocity	Study investigated blood flow dynamics on healthy and post-surgical coarctation TA models

TABLE 1. Continued.

ID	B. Conditions						Major insights and contributions		
	Geometry	Blood	A. Wall	Inlet	Outlet	Time		Flow	Simulation results
52	P-M	N	R	MV	MV	U	L	Velocity, OSI, TAWSS, RRT	Detailed study investigated the effect of different sets of outlet boundary conditions obtained from <i>in vivo</i> measured flow rates. Measured velocity at descending aorta, six treatment schemes at branches
98	P-M	N	R	MV	OD + MV	U	LES	WSS, LDL, velocity	First mass transport study that used a patient-specific TA model. It was investigated how the LDL surface concentration change during a cardiac cycle. Lumped parameter model coupled to the descending aorta, measured velocities at branches
97	P-M	N	R	MV	OD + MV	U	LES	WSS, velocity, TAWSS, OSI	A decomposition similar to Reynolds decomposition was introduced to understand how WSS affects the TA wall
17	P-M	N	R + FSI	FV-PW	OD	U	L	Pressure, mass flow rate, WSS, helical flow index	Study investigated blood flow dynamics on FSI, compressible fluid and rigid wall TA models
202	I	N	R	PP	PP	U	L	Velocity, pressure, WSS	Two TA geometric model variations were simulated to assess the influence of hypotension and hypertension pressure conditions on blood flow dynamics
115	P-C	N	ALE + CMM	MV	OD	U	L	2D contour comparison, wall deformation	Two geometric model variations were simulated, using a distinct FSI technique for each. An arterial wall boundary condition was considered
162	P-M	N	R + ALE	1D	1D	U	L	WSS, TAWSS, velocity, pressure, wall deformation	Detailed comparison between FSI and a rigid-wall TA model. Pressure and flow rate data obtained from 1D simulations was imposed as boundary conditions. An arterial wall boundary condition was considered
29	P-C	N	CMM	OD	OD	U	L	Pressure, velocity, cardiac workload	Study investigated blood flow dynamics on various aortic arch obstructions models. The hemodynamic significance of aortic coarctation and various types of aortic hypoplasia to calculate the cardiac workload was determined
28	P-C	N	CMM	OD	OD	U	L	Pressure, velocity, cyclic wall strain	Detailed study investigated local and systemic effects on blood flow dynamics within the TA and coronary, carotid, and cerebral arteries due to aortic coarctation and spatial variations in wall adaptation
214	P-M	N	R	MV + FV-PW	OD	U	SST	Velocity, TAWSS, OSI, turbulent kinetic energy	Healthy (tricuspid aortic valve) and post-surgical coarctation TA models were simulated to account for the disturbances from the aortic valve

TABLE 1. Continued.

[]	B. Conditions					Major insights and contributions			
	Geometry	Blood	A. Wall	Inlet	Outlet				
117	P-M	N	R	FV + PV + MV	MV	U	L	Velocity, WSS, TAWSS, OSI, RRT, helicity density	Influence of different velocity inlet boundary conditions was analyzed in more detail compared to Renner <i>et al.</i> ¹⁶⁰

Note 1: Idealized; P: Patient-specific; M: MRI-based; C: CT-based; N: Newtonian; Pl: Power law; Ca: Carreau; R: Rigid; FV: Flat velocity profile; PV: Parabolic velocity profile; PW: Pulsatile waveform; SW: Sinusoidal waveform; PP: Pulsatile pressure waveform; MV: Measured velocity; MP: Measured pressure; OD: Lumped parameter model; 1D: Distributed parameter model; O: Outflow; Z: Zero pressure; B: Both; S: Steady; U: Unsteady; L: Laminar.

CONCLUSIONS AND FUTURE CHALLENGES

Over the past decades, computational simulations of blood flow have gained great relevance in understanding the human cardiovascular system, in particular the origin and development of different CVDs. The sophistication of the models and the quality of the results has increased dramatically as the developments in the resolution of medical-imaging data and the performance of computers has improved significantly. However, as noted previously, this level of sophistication requires more information than the mere definition of the domain of interest: there is a pressing need to characterize the mechanical behavior of the vasculatures and the external tissues around it with patient-specific boundary conditions. It is clear that given the large patient-to-patient variability of the cardiovascular system, the interactions between the fluid and a solid that is constrained by external tissues must be defined on a patient-specific basis.

In addition, we must move from computational “snapshots” focusing on a mechanical state and on the role of WSS in vascular pathophysiology, to studies focusing on dynamic mechanobiological processes that encompass the time course of arterial growth and remodelling (G&R). By growth, we mean a change in mass; by remodelling, we mean a change in structure. Arteries exhibit a remarkable ability to adapt throughout life: we observe arterial adaptation in development and aging, adaptations to injury, adaptations in disease, and adaptations to changes in the overall hemodynamic state of the patient. Arterial diseases are diseases of the arterial wall; hence internal tissue-level stresses affect the normal biologic phenomena in many cases as much or more than WSS. The main remodelling agents in the arterial wall are the ECs, vascular smooth muscle cells, and fibroblasts. Many studies have attempted to elucidate the role of each of these elements in arterial G&R. From a computational standpoint, two main approaches have been proposed: the kinematic-growth approach^{157,187} and the constrained-mixture approach.^{71,89,212} Although new computational approaches have been recently suggested,^{108,175,216} there is a pressing need to determine whether G&R relations that have hold for modest adaptations would hold in pathological conditions.

Interventional and surgical therapies used in the treatment of CVDs attempt to restore blood flow to compromised organs and tissues at no risk to the patient. Ideally, these therapies should result in sufficient blood flow at appropriate physiologic pressures while avoiding adverse flow conditions that may lead to procedural failure or poor outcomes. Unfortunately, most of the advances in surgical techniques and interventions have come about as a result of a trial-and-error design process. Currently, alternate and new techniques are

evaluated by performing the new procedure on a series of patients, and then evaluating clinical outcomes. Physicians do not have all the tools needed to evaluate the multiple options and to design the optimal corrective procedures, since diagnostic imaging, physical measurements, and empirical data are insufficient to predict the outcome of a given treatment for an individual patient owing anatomic and physiologic variations and system complexity.

In the new paradigm of predictive medicine, the surgical community would achieve more effective healthcare from computational tools to construct and evaluate patient-specific anatomic/physiologic models that could optimize treatment, predict outcomes of surgical interventions and optimize application of cardiovascular devices. In order to achieve clinical translation, these models ultimately should exploit patient-specific clinical visualisation modalities and experimentally obtained material properties in combination with fluid dynamics and solid mechanics models. Detailed knowledge about physiological (control) mechanisms and pathophysiological processes is necessary to arrive at clinically relevant decision making tools. Ultimately, these models should account for processes operating at different time scales, ranging from transient behaviour of pressure and flow during a cardiac cycle, to effects of altered physiological demands or therapeutic interventions, through much longer time-scale processes involving G&R due to disease progression and aging. However, much of our current understanding of CFD hemodynamics is still explanatory rather than predictive, and this new frontier in computational modelling has an almost limitless number of open problems to challenge investigators for many years to come. We hope that this review will stimulate computational research that will contribute to the continued improvement of cardiovascular health through a strong interaction and cooperation between engineers and clinicians.

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