ORIGINAL ARTICLE

Fluoride removal efficiencies of Al-EC and Fe-EC reactors: process optimization using Box–Behnken design of the surface response methodology

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Abstract

In this study, surface response methodology was employed to investigate the efect of diferent interacting factors on the removal of fuoride from synthetic water using aluminum electrocoagulation (Al-EC) and iron electrocoagulation (Fe-EC) in diferent reactors. Box–Behnken design of a Design Expert version 11 was used for the optimization and evaluation of the process independent variables: applied electric density, initial pH, initial fuoride concentration and treatment time on the efficiency of fluoride removal as a response. Results showed that the effect of current density and initial fluoride concentration was signifcant model terms for fuoride reduction in Fe-EC and Al-EC reactors, respectively. The Al-EC reactor model presented the R^2 value of 79.2% while Fe-EC presented R^2 value of 75.8%, showing that both models can predict the response well. The reduction by 94% (initial concentration of 16 mgF/L) was established at optimal operating parameters of 18.5 mAcm−2, pH 6.80 in 50 min using Al-EC. On the other hand, 16 mgF/L was reduced by 92% to 1.28 mgF/L in Fe-EC reactor at optimal condition of 6.5 mAcm−2, pH 6.50 in 50 min. Experimental results correlated well to the model predicted results that were 95 and 94% for Al-EC and Fe-EC, respectively. Both reactors manage to reduce fuoride to a level recommended by WHO $(\leq 1.5 \text{ mg/L})$ for drinking purpose.

Keywords Electrocoagulation · Defuoridation · Box–Behnken design · Surface response

Introduction

It is approximated that 90% of population of people living in African Rift valley is afected with dental and skeletal fuorosis due to consumption of groundwater water containing elevated levels of fuoride (Fawell et al. [2006\)](#page-10-0). Despite

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availability of various methods such as adsorption, ion exchange, fltration, coagulation and membrane processes for defuoridation (Mohapatra et al. [2009\)](#page-10-1), in the African Rift Valley zone, people are mainly using bone char and Nalgonda methods (Osterwalder et al. [2014\)](#page-10-2). This is due to their low cost, efectiveness and availability of materials (García-Lara and Montero-Ocampo [2010](#page-10-3)). However, the methods face rejection by some users because of odor and ofensive taste especially when there is poor production of bone char (Fawell et al. [2006\)](#page-10-0). On the other hand, Nalgonda method requires high chemical coagulants for effective fluoride removal, resulting into a high sludge production that becomes a challenge in their disposal. Thus, electrocoagulation has demonstrated to be an alternative treatment method to avoid high production of sludge, odor and smell as on chemical coagulation.

Electrocoagulation (EC) method involves electricity for in situ generation of coagulant that destabilizes chemical pollutants in water (Moussa et al. [2017\)](#page-10-4). The common electrodes include aluminum, titanium, zinc, copper and iron; aluminum and iron being superior than the others,

due to their efficiency and availability (Moussa et al. [2017](#page-10-4)). In EC, the metal ion dissociates from the anode (Eqs. [1](#page-1-0) and [3](#page-1-1)) while water at the surface of the cathode dissociates into H^+ and OH^- ions, the two react to form metal hydroxide (coagulant) as shown in Eqs. ([2](#page-1-2)) and ([4\)](#page-1-3) for aluminum and iron, respectively. The coagulant then provides surface site for charge neutralization, adsorption, coagulation and co-precipitation which remove fuoride by floc formation (Kobya et al. [2006\)](#page-10-5).

$$
Al_{(s)} \to Al^{3+} + 3e^{-1}
$$
 (1)

$$
Al^{3+} + nH_2O \to Al(OH)^{3-1}_n + nH^+ \tag{2}
$$

$$
\text{Fe}_{(s)} \to \text{Fe}^{2+} + 2e^{-1} \tag{3}
$$

$$
4Fe^{2+} + 10H_2O + O_2 \rightarrow 4Fe(OH)_3 + 8H^+ \tag{4}
$$

The efficiency of EC experiments depends on interaction among several independent factors, namely the current applied, initial pH, treatment time, conductivity of the sample and initial pollutant concentration (Moussa et al. [2017\)](#page-10-4). Recently, optimization of EC operation factors has been performed by varying a single factor while keeping other factors fxed at a specifc set of conditions. This process is time consuming and requires high number of runs leading to poor optimization due to ignoring of some interaction (Tir and Moulai-Mostefa [2008\)](#page-10-6). The mentioned shortfalls can be easily solved by a response surface methodology (RSM). The method uses various designs such as factorial design (FD) (Daghrir et al. [2013](#page-10-7)), central composite design (CCD) (Amani-Ghadim et al. [2013\)](#page-10-8), D-optimal design (DOP) (Tir and Moulai-Mostefa [2008\)](#page-10-6), and Box–Behnken design (BBD) (Behbahani et al. [2011](#page-10-9)). The frst three designs face a challenge of higher number of experiments required and thus become costly. On the other hand, the BBD provides the same information as the others but with the advantage of less number of experiments (Box and Behnken [1960](#page-10-10)). Furthermore, the BBD does not contain combinations in which all factors are simultaneously at their highest or lowest levels, which is important in avoiding experiments performed under extreme conditions that may cause unsatisfactory results (Box and Behnken [1960\)](#page-10-10), hence selected for this work.

The aim of this study was to optimize and model fuoride removal from aqueous solutions in two separate electrocoagulation reactors, Al-EC and Fe-EC, establish and compare their efficiencies on fluoride removal and to determine relationship between responses and four quantitative variables (initial pH, initial fuoride concentration, current density and treatment time) using Box–Behnken design (BBD).

Materials and methods

Material preparation

The fuoride solution was prepared using sodium fuoride (NaF), where 2.21 g of sodium fuoride was dissolved in 1000 mL of distilled water to make 1000 ppm of fuoride in the stock solution. Then, serial dilution was used for a specifc concentration preparation. Meanwhile the electrodes, aluminum and iron electrodes plates of 10 cm \times 2 cm, each were pre-cleaned by rubbing with sandpaper, rinsed in NaOH (2 M) and HCl (2 M) to remove any particles attached on the surface before washing with distilled water. The electrodes were then dried at 105 °C before the start of experiments. After each experiment, electrodes were dissolved in 1 M hydrochloric acid for 10 min to remove any remaining particles on the surface that may reduce EC performance.

Design of experiment

In this study, the Box–Behnken design BBD was selected for the optimization of EC process used for the fuoride reduction. The four-factorial and a three-level BBD with fve replicas at the center point leading to twenty-nine (29) experiments was employed for response surface modeling in this study. The variables (independent factors) chosen were: the applied electric current density (*A*), initial pH of the water sample (*B*), treatment time (*C*) and initial concentration of fluoride (*D*). Meanwhile, the percentage fluoride reduction was considered as dependent factor (response).

The electrocoagulation set up and sample analysis

The EC experiments were carried-out in a batch mode reactor (Fig. [1\)](#page-2-0). The reactions were conducted in 800 cm^3 beaker, with a working volume of 600 cm^3 . The two aluminum electrode plates with a total surface area of 80 cm^2 each were connected to other two aluminum as cathode in a monopolar parallel connection MP-P. This makes the efective surface area to volume ratio the reactors (*S*) to be 0.15 cm−1. Similar reactor set up for the iron electrode Fe-EC was employed. The anodes and cathodes were placed alternatively and parallel to each other at a specifc distance of 1.5 cm. Thereafter, the end poles of sacrifcial electrodes were connected to the anode in a direct current (DC) power source, (BK Precision 1796).

The experiments were then performed in series of combination of diferent operation parameters as shown in Table [2.](#page-3-0) On the other hand, the conductivity of water sample was improved by addition of small amount of sodium chloride (200–300 mg) as it has ability to eliminate the passive flms **Fig. 1** Experimental setup for electrocoagulation reactions: **a** Schematic diagram: *1* Anode Fe or Al *2* Cathode, *3* Interelectrode distance 1.5 cm, *4* Reactor (800 cm^3) , 5 Water sample (600 cm^3) , 6 Working volume (600 cm^3) , **b** Photograph of the reactor setup and experimentation

 $\overline{7}$ \mathbf{a} $\dot{3}$

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on aluminum electrodes according to corrosion pitting phenomenon (Mansouri et al. [2011](#page-10-11)). After each set of experiment, samples were taken then fltered (Whatman flter paper 0.6 micron) and analyzed using ion selective electrode (ISE) for fnal fuoride concentration. Percentage of fuoride removal was then calculated (Eq. [5\)](#page-2-1).

$$
Red(\%) = \frac{(F_0 - F_t) \times 100}{F_0} \tag{5}
$$

where F_0 and F_t are initial and final fluoride concentration, respectively.

Results and discussion

The actual values of process variables and their variation limits shown in Table [1](#page-2-2) were selected based on the values obtained from various studies as well as in preliminary experiments. Results of the experiments performed are presented in Table [2](#page-3-0) showing the actual and predicted reduction of fuoride at diferent combinations of operating parameters using aluminum and iron electrodes, respectively.

Evaluation of the data

For the evaluation of experimental data on their validity in optimization of operation parameters, the response variable was ftted by a second-order model in the form of quadratic polynomial equation given by Eq. ([6\)](#page-2-3) as proposed by (Khedmati et al. [2017\)](#page-10-12).

$$
Y = b_0 + \sum b_{ii} X_i + \sum b_{ii} X_i^2 + \sum b_{ij} X_i X_j
$$
 (6)

In this equation *Y* is the response variables (fuoride reduction) and b_0 , b_i , b_{ii} , and b_{ij} are constant coefficients of intercept, linear, quadratic and interactive terms, respectively and X_i and X_j represent the four independent variables (current density, initial pH, treatment time, and initial concentration). Experimental data shown in Tables [2](#page-3-0) were analyzed using Design-Expert version 11 program including ANOVA and regression to obtain the interaction between the process variables to the response. Two-dimensional, contour plots and three-dimensional curves of the response surfaces were developed using the same program to explain the interactions among variables and their effect to the fluoride reduction.

Optimization procedure

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Table [3](#page-4-0) shows the key fndings after analysis of variance and regression of the data set presented in Table [2](#page-3-0) to assess the validity of the model prediction for Al-EC and Fe-EC, respectively. In this study, the coefficients of the model for constant terms, cubic efects, quadratic efects and interaction efects were evaluated. The model low *p*-values of 0.0087 and 0.022, and large *F*-values 3.81 and 3.07 imply that at least one of the terms in each model has a significant efect on the response in Al-EC and Fe-EC setups,

Table 1 Experimental range and levels of independent variables for Al-EC and Fe-EC experiments

Table 2 The Box–Behnken design (BBD) showing actual and predicted fuoride reduction for Al-EC and Fe-EC reactor at diferent operation parameters

respectively (Karimifard and Moghaddam [2018](#page-10-13)). The lack of ft *p* value of 0.1125 for Al-EC and 0.7344 for Fe-EC both being \geq 0.05 made lack of fit not significant to both setups (Karimifard and Moghaddam [2018\)](#page-10-13). As seen from Table [3,](#page-4-0) the initial pH (*B*), and initial fuoride concentration (*D*) are both significant to the model ($p < 0.05$), where initial fluoride concentration being the most significant $p < 0.0001$ to Al-EC. For the Fe-EC, the current density appears to be the only significant factor $p = 0.01$. The interaction between initial pH and initial concentration (BD), and between initial concentrations themselves (D^2) are highly significant factors $(p < 0.05)$ as compared to other interaction terms in both reactors.

The regression coefficient R^2 of 0.79 and 0.75 for Al-EC and Fe-EC, respectively, show that the interaction among the factors in experimental data to both models can fairly predict the response (Karimifard and Moghaddam [2018\)](#page-10-13). The adequate precision which is 7.8 for Al-EC and 6.4 for Fe-EC also signifes that the signal-to-noise ratio is appropriate

and adequate. The adjusted R^2 of 0.58 and 0.50 both being lower than the R^2 values suggest that the new number of factors included in the model in trying to modify it could not improve the model (Karimifard and Moghaddam [2018](#page-10-13)). The $R²$ values observed indicate that the regression models explained electro-defuoridation fairly. Hence, the response surface model developed in this study for predicting fuoride removal efficiency was considered to be satisfactory.

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From the normal probability plot of residuals as shown in Fig. [2](#page-4-1)a and b it can be ascertained with assumption that both models were relatively satisfactory as the points in the plot form fairly straight-line. In the case of actual residual against ft plot, for a model to be reliable, no series of increasing or decreasing points patterns such as increasing residuals with increasing fts and a predominance of positive or negative residuals should be found. Furthermore, the data shown in Table [3](#page-4-0) can also be observed and confrmed in Fig. [3](#page-5-0)a and b showing alignment between the residuals and predicted fuoride reduction. The predicted and actual plots Fig. [4](#page-5-1)a and

Table 3 ANOVA and regression results for the response surface quadratic model for fuoride reduction by Fe-EC and Al-EC reactors

Source	Fe-EC		Al-EC		
	F-Value	p -value	F-Value	p -value	
Model	3.07	0.022	3.81	0.0087	Significant
$A-J$	7.75	0.0146	4.48	0.0528	
B -pH	2.93	0.1088	8.13	0.0128	
C -time	4.12	0.0619	0.3444	0.5666	
D -Conc	0.0395	0.8453	17.56	0.0009	
AB	0.0012	0.973	0.0073	0.9331	
AC	0.1441	0.7099	0.0194	0.8911	
AD	0.8207	0.3803	4.08	0.063	
BC	0.1715	0.6851	0.0995	0.7571	
BD	13.39	0.0026	4.71	0.0477	
CD	1.47	0.2449	3.47	0.0837	
A^2	1.22	0.2887	0.0822	0.7786	
B ²	1.32	0.2702	0.6344	0.439	
C^2	0.6246	0.4425	1.18	0.2966	
D^2	11.77	0.0041	10.07	0.0068	
Residual					
Lack of fit.	0.6525	0.7344	3.64	0.1125	Not significant

Al-EC: $R^2 = 0.79$; Adj $R^2 = 0.58$; Adeq precision=7.8; Fe-EC: $R^2 = 0.75$; Adj $R^2 = 0.50$; Adeq precision = 6.4

b further indicate the close agreement between the actual and predicted results, suggesting that the model could well predict within the range of operation parameter. Therefore, it can be concluded that the quadratic model of the response surface developed in this study correlating fuoride reduction with process variables is best suited to explain the experimental data of electrocoagulation process.

Efect of individual operating parameters

The effect of individual operating parameters, current density, initial pH, treatment time and initial fuoride concentration considered in this study is shown in the plots presented in Figs. [5](#page-6-0) and [6](#page-6-1) for Al-E and Fe-EC, respectively. The parameters were measured as the function of fuoride reduction. These parameters are known to be key factors for operation of electrocoagulation system (Moussa et al. [2017](#page-10-4)).

The efect of current density

From the plots, it can be observed that, from the lower current density there is a linear increase on fuoride reduction to a maximum current of 38.5 and 16 mA/cm² for Al-EC and Fe-EC, respectively. At these points, there is maximum removal of fuoride by 97% for Al-EC and 95% for Fe-EC. According to Faraday's law (Eq. [7](#page-4-2)), as the applied current increases, dissolution of aluminum and iron ions also tend to increase, leading to high formation of coagulant $\text{Al}(\text{OH})_3$ and Fe(OH)₃, bubble and floc size (Mehmet Kobya et al. [2011\)](#page-10-14).

$$
W = \frac{ItM}{NF} \tag{7}
$$

where *W* is the theoretical amount of aluminum or iron produced by current *I* (A) passed for a period of time *t* (s), *M* is molecular mass (Al; 26.98 g/mol: Fe; 55.84 g/mol), *N* is number of electrons transferred (*N*−3 for Al; 2 for Fe), *F* is Faradays constant (96,485 C/mol).

Fig. 2 Normal probability plots **a** Al-EC, **b** Fe-EC reactors

Fig. 3 Residual vs predicted plots for fuoride removal **a** Al-EC reactor, **b** Fe-EC reactor

Fig. 4 Plots for predicted against actual results for fuoride removal **a** Al-EC, **b** Fe-EC

However, removal efficiencies started to decline when the $J \ge 16.1$ mAcm⁻² for Fe-EC and ≥ 50 mA/cm² for Al-EC. Higher current density means high generation of coagulant near the electrode that restrict the free movement of particles causing overpotential to build up in the reactor due to ohmic drop (Nasrullah et al. [2012](#page-10-15)). This prevents further adsorption of the fluoride ion as observed at $J \ge 16.1$ mAcm⁻² and *J*≥ 50 mAcm−2. The ohmic drop was also confrmed

that at the same treatment time both reactors attained the same amount of coagulant dosage of 0.000063 g/L. It can be ascertained that at the coagulant dose \geq 0.000063 g/L no further fuoride reduction can be achieved as the kinetic of particles become restricted. The lower ohmic drop in Fe-EC than Al-EC is attributed to the higher molar mass of iron that achieved the same amount of coagulant as aluminum at lower electric current by a factor of ~ 0.3 .

Fig. 6 Main efect plots of parameters for fuoride removal efficiency on Fe-EC reactor

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Initial fuoride concentration

The infuence of initial fuoride concentration appears to be similar to both Al-EC and Fe-EC systems. For Al-EC, at a lower fuoride concentration starting from 2 to 26 mgF/L, there is increase in fuoride reduction rate from 78 to 95%. At this point, the ratio between adsorbate (*F*−) and adsorbent Al(OH)₃ and Fe(OH)₃ is very low and permits rapid uptake of fuoride. But as the initial fuoride level reaches \sim 27 mgF/L, the removal rate slows down and remains constant as its limited by availability of free surfaces on the coagulant for further uptake (Vasudevan et al. [2009](#page-10-16)). However, above 30 mgF/L, the reduction appears to decrease to 92%. Likewise, for Fe-EC, the removal increases with initial fuoride concentration from 2 mgF/L and reaches maximum at 21 mgF/L. Above this level, there is decrease in removal efficiency to 91 from 95% at highest initial concentration of 40 mgF/L. The decrease in removal is due to competition for complexation sites which limit fuoride removal and subsequent further stirring tends to lead to desorption (Vasudevan et al. [2009](#page-10-16)). This study also found that $Fe(OH)_{3}$ reaches saturation point at a lower fuoride concentration of 21 mgF/L compared to 27 mgF/L of $Al(OH)_{3}$.

Initial pH of the water sample

From the plot, it is interesting to see that the fluoride removal by Al-EC increases 78–96% as the initial pH of the sample increases. The maximum fuoride removal is attained at pH 7.5–8.5. This is because at a lower pH \sim 4, there is a higher hydrogen ion concentration leading to formation of soluble HF. At a pH \geq 4, amorphous hydroxide Al(OH)₃ starts to form due to hydrolysis of water at the cathode, the amount of this amorphous further increases with pH as more hydroxide is added that lead to more uptake of fuoride. The amorphous $AI(OH)$ ₃ has minimum solubility and is finally polymerized into Aln(OH)_{3n} , which results into dense flocs formation with large surface area (Holt et al. [1999\)](#page-10-17) for high fluoride uptake. However, at $pH \geq 9$, the removal remains constant signifying formation of negatively charged aluminum hydroxide $Al(OH)₄$ that repels with the fluoride ion in the solution (Mechelhoff et al. 2013). Meanwhile, Fe-EC behaves diferently, and the highest reduction is attained at pH 4.5–5.5 beyond which there is insignifcantly slow down from 95 to 92% at pH 9. In acidic medium, there is higher dissolution of iron (Cañizares et al. [2007\)](#page-10-19) leading to the formation of high amount coagulant $Fe(OH)_2$. Study by (Sasson et al. 2009) also revealed significant high $Fe²⁺$ dissolution rate at pH values of 5–6 than that at pH 8–9. In this context, it is important to note that the chemical dissolution of the electrode surfaces is promoted at alkaline pHs (for the case of aluminum) and at acidic pHs (for the case of iron).

Treatment time

In this investigation, the reduction efficiencies in both aluminum and iron electrodes appeared to exhibit exponential relation to time. For Al-EC, there is an increase in fuoride reduction from 90% at 10 min to 93% with the maximum removal at 40 min. Above this time, there is significant decrease on removal efficiency to 91.7% in 60 min. For the Fe-EC, more similar trend is observed; however, the removal efficiency remained constant at a longer time of 50–60 min. This indicates that further treatment time beyond 40 min and 50 min for Al-EC and Fe-EC, respectively, has negative infuence on the fuoride removal. For both cases during the frst 10 min, there is appreciable enough in situ generated hydroxides of aluminum and iron to reduce fuoride by 90%. The longer time needed for iron to reach maximum fuoride reduction may be due to small current density applied during this investigation as compared to aluminum electrode. This is attributed to high adsorption capacity of in situ generated aluminum coagulant for fuoride ion (Smedley et al. [2003](#page-10-21)).

Combined efect of operational parameters on fluoride removal efficiency

The current density is considered as the key factor controlling efficiency of any electrocoagulation reaction (Moussa et al. [2017\)](#page-10-4). However, in this study other factors when correlated to current density are observed to limit fuoride removal in both reactors' Figs. [7](#page-8-0) and [8](#page-8-1)a–c. Generally, the maximum fuoride removal observed is \sim 96 and \sim 94% for Al-EC and Fe-EC, respectively. At a lower treatment time \leq 39 and \leq 45 min and initial fluoride concentration \leq 27 and \leq 21 mgF/L for Al-EC and Fe-EC, respectively, the removal increased at all current density applied. However, above these levels there is signifcant reduction in fuoride removal, despite the increase in current density. This indicates that the treatment time and initial fluoride concentration are limiting factors in their higher levels. Despite further dissolution of Al^{3+} and Fe^{2+} as the function of current and time, when the $F⁻/Al(OH)₃$ and $F^{-}/Fe(OH)_{2}$ is ≥ 1 adsorption cannot take place (Vasudevan et al. [2009\)](#page-10-16). Figures [7](#page-8-0) and [8](#page-8-1)d also verify similar fnding that an increase in treatment time at initial concentration≥27 and \geq 21 mgF/L has no significant impact on the fluoride removal. At any suggested operation condition of current density, initial pH and treatment time, the maximum initial fuoride that can be removed effectively (i.e. ≤ 1.5 mgF/L) is 27 and 21 mgF/L for Al-EC and Fe-EC, respectively.

Fig. 7 Surface plots with con tour as a function of **a** treatment time and current density at pH 6.5 and initial concentration 21 mg/L, **b** initial concentration and current density at pH 6.5 and treatment time 35 min, **c** pH and current density at initial concentration of 21 mgF/L and time 35 min, **d** concentration and time at current density 28 mAcm^{-2} and pH 6.5

Fig. 8 Surface plots with con tour as a function of **a** treatment time and current density at pH 6.5 and initial concentration 21 mgF/L, **b** initial concentra tion and current density at pH 6.5 and treatment time 35 min, **c** pH and current density at initial concentration of 21 mgF/L and time 35 min, **d** concentration and time at current density 12.4 mAcm⁻² and pH 6.5

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Time (min)

 $\overline{2}$

Concentration (mg/L)

Table 4 Experimental and predicted results on a few selected solutions suggested for optimization tests for AL-EC and Fe-EC

Model equations

Final equation model in term of coded factors Al‑EC

The fnal regression model in terms of coded factors has been expressed by the following second-order polynomial equation:

For the Fe-EC, the best removal was predicted to be 94% at initial fuoride concentration of 16 mgF/L, current density 6.25 mAcm−2 in 60 min. The observed result at this optimum condition was 92.00% that confrmed to be close to the predicted removal.

$$
Red\%Al, EC = 92.96 + 3A + 4.05B + 0.83C + 5.95D - .0.21AB + 0.34AC - 4.96AD - 0.77B
$$

- 5.33BD + 4.57CD - 0.55A² - 1.54B² - 2.09C² - 6.12D²
Red%Fe, EC = 94.58 + 0.56A - 0.34B + 0.40C - 0.04D - 0.01AB - 0.13AC - 0.31AD
+ 0.14BC + 1.26BD - 0.29A² - 0.31B² - 0.21C² - 0.93D²

Final equation in terms of actual factors

Conclusion

In terms of actual factors, an empirical relationship between $F⁻$ removal efficiency and the variables has been expressed by the following second-order polynomial equation:

In this research work, the effects of four main parameters in the electrocoagulation process including initial pH, initial fuoride concentration, current density and reaction time were evaluated and compared on the reduction of

Red%Al, EC =11.65 + 1.24*j* + 7.85*pH* + 0.11*t* + 2.18Conc − 0.01*j* ∗ *pH* − 0.001*j* ∗ *t* − 0.03*J* ∗ Conc − 0.01*pH* ∗ *t* − 0.11*pH* ∗ Conc + 0.01*t* ∗ Conc − 0.01*J*² − 0.24*pH*² − 0.003*t* ² − 0.01Conc2 Red%Fe, EC = + 91.32 + 0.38 − 0.12 + 0.05*t* − 0.003Conc − 0.001*j* ∗ *pH* − 0.0009*J* ∗ *t* − 0.003*j* ∗ Conc + 0.0023*pH* ∗ *t* + 0.03*pH* ∗ Conc − 0.0009*t* ∗ Conc − 0.008*j* ² − 0.05*pH*² − 0.0003*t* ² − 0.0025Conc²

Fluoride removal by Al‑EC and Fe‑EC optimization

The main objective of optimization was to determine the optimum values of variables for fuoride removal with EC from the model obtained using experimental data. In both reactors Al-EC and Fe-EC, the operating parameters were chosen so as to maximize fuoride reduction at the minimal current density, pH, initial fuoride concentration and treatment time were left at a range. Several sets of experiments were suggested by the model and two of them were performed.

From the experimental results shown in Table [4](#page-9-0), Al-EC achieved the reduction of initial 16–0.92 mgF/L that satisfes WHO minimum fuoride level for drinking water. This 94.25% reduction was achieved at optimal conditions of initial fuoride concentration of 16 mgF/L, current density 18.5 mAcm−2 initial pH 6.8 and treatment time 50 min.

fuoride in Al-EC and Fe-EC reactors. The results showed that the initial fuoride concentration was signifcant factor on Al-EC reactor and current density was the only main factor in Fe-EC reactor. The ANOVA results presented fairly R^2 values of 79.23 and 75.45% for Al-EC and Fe-EC fuoride removal, respectively, indicating the good accuracy of the polynomial models for both models. From the optimization, the Al-EC attained 94% fuoride removal at initial pH of 6.8, initial fuoride concentration of 16 mgF/L, current density of 18.5 mAcm−2 and reaction time of 50 min. The Fe-EC attained 92% removal at pH of 6.5, initial fuoride concentration of 16 mgF/L, current density of 6.25 mAcm−2 and reaction time of 60 min. It can be ascertained that both electrodes Al and Fe attained reduction of fuoride to a permissible WHO standard for drinking water $(\leq 1.5 \text{ mg/L})$ at optimized operational parameters.

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Compliance with ethical standards

Conflict of interest The authors declare that there is no confict of interest.

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