CASE STUDIES



Comparative analysis of traditional and fuzzy FMECA approach for criticality analysis of conventional lathe machine

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Abstract Criticality analysis is a technique for the assessment of criticality rating for every constitutive part. Failure mode effect and criticality analysis (FMECA) are broadly utilized for characterizing, distinguishing and dispensing with potential failures from system, design, or process for the criticality analysis. The determination of the critical ranking of failure modes for criticality analysis is a vital issue of FMECA. The traditional method of FMECA determines the critical ranking of failure modes using the risk priority numbers, which is the product of evaluation criteria like the occurrence, severity and detection of each failure mode but it may not be realistic in some applications. The practical applications reveal that the criticality analysis using traditional FMECA has been considerably criticized for several reasons. In this paper, first, a detailed FMEA to find out the various failure modes of each component of a conventional lathe machine is performed and thereafter, the Fuzzy FMECA approach is used to perform the criticality analysis. A comparative analysis of fuzzy FMECA with traditional FMECA is also done to find out the most superior approach for the criticality analysis. It was concluded that the fuzzy FMECA approach is the most superior approach for the criticality analysis of a system.

Keywords FMEA \cdot FMECA \cdot RPN \cdot Criticality analysis \cdot RCM

1 Introduction

Criticality analysis is a technique for the assessment of criticality rating for every constitutive part. Catic et al. (2011) defined the criticality as a relative proportion of components failure modes effects on which reliable and safe operation of the system implied. Failure Modes and Effects Analysis (FMEA) has been broadly utilized for characterizing, distinguishing and dispensing with potential failures from system, design, or process for the criticality analysis (Stamatis et al. 1995). In 1960, FMEA originated the first time in the aerospace and automotive industry (Bowles and Peldez 1995). Juran (1989) defined FMEA as a methodology, to analyze a proposed design for possible ways in which failure can happen. Sharma et al. (2005) defined it as a bottom-up and structured approach to investigating the effect of potential failure modes. According to Popovic et al. (2010), it can be defined as a procedure to evaluate the system reliability that can be applied to its lifetime. Furthermore, FMEA is an approach to assess the risks and therefore the standards of FMEA are to recognize potential hazards together with the focused system and prioritize the remedial actions (Catic et al. 2011). When the criticality analysis combines with FMEA, Then FMEA becomes FMECA.

FMECA helps to direct the maintenance of the desired failure modes and prevent failure causes. It follows with the selection of optimal maintenance actions using decision logic in the final stage of Reliability Centered Maintenance (RCM). It is a comprehensive tool to assist in structuring maintenance management procedures, by systematically

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considering each failure mode of a system. According to Bertolini (2006) failure modes analysis provides information about (1) the functional importance of the subsystem, (2) description of all potential failure modes of the system, and (3) criticality analysis which ranks all failure modes in a logical order.

To determine the criticality ranking of failure modes for the selection of maintenance actions is a vital issue in FMECA. The Risk Priority Numbers (RPNs) are used to determine the criticality ranking of failure modes in traditional FMECA. The RPN can be determined by multiplying the evaluation criteria, i.e. Occurrence (O), Severity (S) and Detection (D) of each failure mode but it may not be realistic in each application. It is proved to be one of the most imperative early preventive actions for systems that can prevent sudden failure. However practical applications reveal that the criticality analysis using traditional FMECA have been considerably criticized for a number of reasons (Ben-daya and Raouf 1996; Gilchrist 1996; Chang et al. 2001; Braglia et al. 2003a, b; Bowles 2003; Pillay and Wang 2003; Sankar and Prabhu 2001; Teng and Ho 1996; Xu et al. 2002; Gargama and Chaturvedi 2011). Specifically:

- The RPN is strongly dependent only on the small variation of three parameters, i.e. S, O and D. The same RPN could result in starting from different values of S, O, and D.
- The consideration of the relative importance of S, O, and D is not taken into account.
- Interdependencies between different failure modes and their effects of a system are not taken into account.
- The precise estimation of these three factors is difficult. The linguistic scale can be used to provide more information in FMEA.
- To determine RPN, the mathematical formula "RPN = S × O × D" has been debated, as it lacks a completely scientific basis.

Significant efforts have been made in FMEA literature to overcome these drawbacks of the conventional FMECA. As a result, Fuzzy logic is widely used in FMECA literature. Bowles and Peldez (1995) presented two fuzzy-based approaches, first is based on numerical ranking and another is based on linguistic ranking for RPN calculation. They state that fuzzy resolves several problems in conventional method evaluation and has various advantages compared to numerical methods. Chang et al. (1999) used fuzzy linguistic terms to assess O, S, and D, and grey relational analysis to determine the risk priorities of potential causes. Xu et al. (2002) proposed a fuzzy FMEA assessment for a gas turbocharger of a diesel engine. Pillay and Wang (2003) developed a fuzzy rule-based approach to avoid the utilization of a conventional method for calculating RPN. Braglia et al. proposed a fuzzy "Technique for Order of Preference by Similarity to Ideal Solution" (TOPSIS) FMECA, which is a fuzzy version of the technique for order preference by TOPSIS method and states that fuzzy allows to combine severity, detectability, and probability of a failure in a more flexible structure. Braglia et al. 2003a, b proposed a risk function using a fuzzy if-then rule. Wang et al. (2009) proposed a fuzzy weighted geometric mean approach to evaluate the risk in FMECA. Bertolini (2006) presented a fuzzy VIKOR criticality analysis for the FMECA technique and tested utilizing an industrial case study, dealing with an Italian oil refinery. It was concluded that fuzzy logic appears to be a powerful tool for performing a complete criticality analysis because (1) it is possible to consider a potentially larger number of failure criteria, (2) it is possible to give degree of importance to the criteria themselves, (3) it makes the analysis simpler, because of use of precise data in the form of fuzzy numbers, and (4) it is possible to manage the evaluation of tangible (quantitative) and intangible (qualitative) criteria.

Hence, in this paper, to find out the various failure modes of each component of a conventional lathe machine, a detailed FMEA is prepared and thereafter, traditional and fuzzy FMECA are used to perform the criticality analysis. A comparative analysis is also done to find out a better approach of FMECA for the criticality analysis.

2 Traditional FMECA

The traditional FMECA is a tool for evaluating potential failure modes and their causes. It helps in prioritizing the failure modes and recommends remedial measures for the prevention of catastrophic failures and the improvement of the quality of the product. There are two phases in FMECA. In the first phase, it deals with the identification of the potential failure modes and their effects, and in the second phase, it deals with performing criticality analysis to identify the criticality level of each failure mode by ranking the RPN (Sharma et al. 2006). The traditional FMECA is described in the following eight steps.

- Identify the system and divide it into subsystems to focus the search for components.
- Identify all potential failure modes, their causes and the effects of failure modes of the entire system.
- Assess each failure mode in terms of S, O, and D.
- Determine the RPN using "RPN = $S \times O \times D$ ".
- Determine the critical ranking of each failure mode.
- Determine whether remedial action is required or not.
- Develop recommendations to improve system performance.
- Prepare a FMECA report by summarizing the analysis in tabular form.

3 FMEA of conventional lathe machine

In this section, to perform the FMECA, a lathe machine is considered with three major subsystems i.e. (1) feed mechanism (including the feed motor, feed rod, lead screw



Fig. 1 FSI of lathe machine

Table 1 FMEA of lathe	machine	components
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etc.), (2) carriage (including the tool post, cross slide, saddle etc.), and (3) headstock assembly (including the gearbox, bearings, belt drive, motor, chuck etc.). Based on the working structure of conventional lathe machine, the six highly critical components in terms of Functionally Significant Items (FSI) i.e. (1) electrical motor, (2) oil seals, (3) gearbox, (4) bearing, (5) lead screw, and (6) belt drive are identified. FSI can be defined as a component that has a significant impact on its function on the system. The six functionally significant items and FMEA chart of lathe machine components are presented in Fig. 1 and Table 1 respectively.

4 Criticality analysis of conventional lathe machine using traditional FMECA

Each failure mode is sequentially numbered as a failure mode pointer for the evaluation of the risk priority of each component. The influence of three parameters: S, O, and D are considered to evaluate the criticality or risk priority of a component. The severity reflects the gravity of the failure consequences. Occurrence defined as an index of the frequency of component failure. Detection has defined an index to detect a failure assuming that it has occurred. These parameters are measured on a scale of 1 to 10, as the number 1 presents the weak importance of failure while

Component	Component function	Failure mode	Failure effect
1. Oil seals	Provide a leak-proof seal between parts	1.1 Face wear	Leakage in parts
		1. 2. Embrittlement	Seal components get damaged
2. Motor	Converts electrical energy to mechanical energy	2.1. Overheating failure	Cause separation of greases and breakdown of oils causing bearing failure
		2.2. Power supply anomalies	Voltage unbalances leads to overheating and decreased efficiency
3. Gear box	Provides speed and torque conversions from a	3.1. Wear	1. Gear teeth eroded by wear
	rotating power source		2. Bearings seize
		3.2. Surface fatigue failure	1. Gear tooth may break
			2. Formation of craters on gear teeth (Pitting)
		3.3. Breakage	Cracking of vital components in gears
4. Bearing	Supporting and aligning other parts of the lathe machine	4.1. Wear	Premature failure of contact surfaces
		4.2. Indentation	1. Denting on ball bearing
			2. The Bearing will not run properly
		4.3. Collapse	Bearing breakage due to deep-seated rust and uneven distribution of load
5. Lead screw	Converts rotary motion into linear motion	5.1. Failure	Wear and abrasion of the lead screw causes its failure
6. Belt drive	Power transmission between shafts	6.1. Pulley misalignment	Belt failure
		6.2. Belt slip	Wear and heat generated with reduced belt life
		6.3. Belt fatigue	Broken belt

Table 2 Evaluation criteria of failure modes for conventional FI	MECA
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Sev	erity	Occurrence		
1	Insignificant effect. Minimal or no correction required	1	Without failure registry in the last 2 years	
2	The very insignificant effect corrected immediately by the operation team	2	1 or 2 Failures in the past 2 years	
3	The insignificant effect corrected immediately by the maintenance	3	3 or 4 Failures in the past 2 years	
4	The minor effect, the component suffers to a gradual degradation case if not repaired	4	5 or 6 Failures in the past 2 years	
5	The moderate effect, the component does not execute its function, but the maintenance of failure does not demand the stop of the machine	5	7 or 8 Failures in the past 2 years	
6	The moderate effect, maintenance demands stop of the machine during 1 day or less	6	9 or 10 Failures in the past 2 years	
7	The critical effect, maintenance demands stop of the machine for more than 1 day	7	10 or 11 Failures in the past 2 years	
8	The very critical effect, the machine has to be stopped and takes longer repair time	8	12 or 13 Failures in the past 2 years	
9	The very critical effect, failure brusquely interrupts the system functions	9	14 or 15 Failures in the past 2 years	
10	The catastrophic effect that can cause damages to properties or people	10	More than 15 failures in the past 2 years	
Det	ection			

100% automatic inspection of the defect. Maintenance of the defect or mechanical equipment is very obvious 1

- 2 Almost 100% inspection of all parts of the lathe machine is done automatically
- 3 Failure identified automatically most of the times and sometimes by the manual inspection
- 4 Failure in the lathe machine is indicated directly by the operator
- Failure identified by the maintenance team during daily inspections 5
- 6 The lathe machine undergoes 100% manual inspection and observations
- 7 Failure identified by abnormal noises
- 8 Failure is identified by performing some tests and not just by direct inspection
- 9 Failure identified by random or indirect tests only
- Occult failure, impossible to be identified by the operator or maintenance team 10

Failure RPN Severity Occurrence Detection Criticality Failure Severity Occurrence Detection mode mode ranking 3 5 15 4.1 3 2 1 6 1 3 3 2 18 5 4.2 3 2 3 5 2 2 20 4 4.3 2 3 3 5 2 7 3 3 4 1 10 5.1

6.1

6.2

6.3

4

7

7

2

2

2

3

8

6

10

8

9

Table 3 RPN and criticality ranking of failure modes for conventional FMECA

number 10 presents the strong importance of failure. The classification criteria for each one of these parameters for failure mode evaluation are presented in Table 2. From these parameters, RPN is determined by multiplying S, O, and D. After that, the criticality ranking has been decided based on the value of RPN of various failure modes of each

1

2

1

component. The highest value of RPN assigned the criticality ranking 1. The RPN's of failure modes of each component are shown in Table 3. It has been observed that failure mode numbers 6.3 and 3.1 are the highest and lowest criticality ranking respectively. Also, criticality ranking for failure mode numbers (1.2, 4.2, and 4.3), (3.2,

1

2

3

RPN

6

18

18

36

8

28

42

Criticality

ranking

9

5

5

2

8

3

1

1.1

1.2

2.1

2.2

3.1

3.2

3.3

3

4

6

1

1

1

Table 4 Evaluation criteria of failure modes for fuzzy FMECA

Severity			Occurrence		
R	The insignificant effect corrected immediately by the maintenance	R	The probability of failure is zero		
L	The minor effect, the component suffers to a gradual degradation case if not repaired	L	Failure is likely occurred once		
М	The moderate effect, the component does not execute its function, but the maintenance of failure demands the stop of the machine	М	The probability of failure is moderate (3 to 5 failures) in the past 2 years		
Н	The critical effect, maintenance demands stop of the machine	Н	The probability of failure is high (6 to 8 failures) in the past 2 years		
VH	The very critical effect, failure brusquely interrupts the system functions	VH	The probability of failure is extremely high (9 or more failures) in the past 2 years		
Dete	ction				
R	Failure indicated directly by the operator				

L Failure identified by the maintenance team during daily inspections

- M Failure identified by abnormal noises
- H Failure identified by thorough inspection and it is not feasible to be done
- VH Occult failure, impossible to be identified by the operator or maintenance team

and 6.1), and (3.3, and 4.1) is the same because of RPN value is equal as 18, 8 and 6 respectively.

5 Criticality analysis of conventional lathe machine using fuzzy FMECA

A fuzzy approach of FMECA is used to evaluate the effect of functional failure and criticality analysis for each component of the lathe machine. The detailed explanation of this approach is presented in the following sections.

5.1 Fuzzy membership function of S, O, and D

Each failure mode is sequentially numbered as a failure mode pointer for the evaluation of the risk priority of each component. The influence of the parameters S, O and D are considered to evaluate the criticality or risk priority of a component. These parameters are measured on a five-point linguistic scale $V = \{R = remote, L = low, M = moderate, L = low,$ H = high, VH = very high and the evaluation criteria of each one of these parameters is presented in Table 4. To measure the average of linguistic scale values (V), the trapezoidal fuzzy number is adopted from (Yang et al. 2010) to define the membership of these factors and presented in Fig. 2. A team of four experts from maintenance areas was constituted to decide the rating of S, O, and D for each failure mode. The following equations are used to determine the deduced values of the given rating of S_i, O_i, D_i for each failure mode.

Moderate High Very High Remote Low 1.0 Membership value 3 5 0 1 2 4 6 7 8 9 10

Fig. 2 Membership function plot of S, O, and D (Yang et al. 2010)

$$S_{i} = (S_{iL}, S_{iM1}, S_{iM2}, S_{iR}) \\ = \left\{ \sum_{j=1}^{m} (S_{ijL}, S_{ijM1}, S_{ijM2}, S_{ijR}) \right\} / m$$
(1)

$$O_{i} = (O_{iL}, O_{iM1}, O_{iM2}, O_{iR}) \\ = \left\{ \sum_{j=1}^{m} (O_{ijL}, O_{ijM1}, O_{ijM2}, O_{ijR}) \right\} / m$$
(2)

$$D_{i} = (D_{iL}, D_{iM1}, D_{iM2}, D_{iR}) \\ = \left\{ \sum_{j=1}^{m} (D_{ijL}, D_{ijM1}, D_{ijM2}, D_{ijR}) \right\} / m$$
(3)

where $i = 1, ..., n; j = 1, ..., m; S_{ij} = Fuzzy$ scores of the ith failure mode; j = jth expert; m = Total number of expert.

The rating is given by experts for each failure mode and the deduced values determined by Eq. (1) to (3) of the membership function of these factors.

5.2 Determination of fuzzy RPN values

The risk space diagram is adopted according to risk assessment on aviation safety management given by (Yang et al. 2010) for calculating the α -cut fuzzy value of S_i, O_i, and D_i and presented in Fig. 3. The right-hand and left-hand values of S_i, O_i, and D_i are calculated by α - level using Zadehl's extension principle and are expressed by the following equations.

$$S_{iL}^{\alpha} = S_{iL} + \alpha (S_{iM} - S_{iL}) \tag{4}$$

$$S_{iR}^{\alpha} = S_{iR} - \alpha (S_{iR} - S_{iM}) \tag{5}$$

$$O_{iL}^{\alpha} = O_{iL} + \alpha (O_{iM} - O_{iL}) \tag{6}$$

$$O_{iR}^{\alpha} = O_{iR} - \alpha (O_{iR} - O_{iM}) \tag{7}$$

$$D_{iL}^{\alpha} = D_{iL} + \alpha (D_{iM} - D_{iL}) \tag{8}$$

$$D_{iR}^{\alpha} = D_{iR} - \alpha (D_{iR} - D_{iM}) \tag{9}$$



Fig. 3 Risk space diagram of the ith failure mode (Yang et al. 2010)

where $\begin{bmatrix} S_{iL}^{\alpha} & \text{and } S_{iR}^{\alpha} \end{bmatrix}$ represents the left-hand and righthand value of S interval of ith failure mode by α -level. $\begin{bmatrix} O_{iL}^{\alpha}, & O_{iR}^{\alpha} \end{bmatrix}$ and $\begin{bmatrix} D_{iL}^{\alpha}, & D_{iR}^{\alpha} \end{bmatrix}$ represents O and D interval respectively. Subsequently left-hand and right-hand values of fuzzy RPN for each failure mode are calculated using weighted Euclidean distance formula using Eqs. 10 and 11.

$$RPN_{iL}^{\alpha} = \sqrt{\sum_{x} w_x^2 (x_{iL}^{\alpha} - x_{i\min}^{\alpha})^2} / \sqrt{\sum_{x} w_x^2}$$
(10)

$$RPN_{iR}^{\alpha} = \sqrt{\sum_{x} w_{x}^{2} \left(x_{iR}^{\alpha} - x_{i\min}^{\alpha}\right)^{2}} / \sqrt{\sum_{x} w_{x}^{2}}$$
(11)

where W_x represents the weights of the risk factor (x = S, O, D) which is adopted as [0.5396, 0.2970, 0.1634] respectively from (Carmignani 2009). In the above equation x_{imin} represents the minimum value of x_i equals to zero according to Fig. 2. After that, the centroid method is used to calculate the defuzzified RPN value. Then the criticality ranking of each failure mode is decided based on the defuzzified RPN value. The values of defuzzified RPN and criticality ranking of each failure mode using Eqs. (4) to (11) are presented in Table 5. It has been observed that the defuzzified RPN is different for each failure mode and none of the failure modes have the same criticality ranking.

6 Comparative analysis of traditional and fuzzy FMECA

In this section, the criticality ranking for each failure mode is compared using traditional FMECA and fuzzy FMECA approach. The comparative analysis of the criticality

Table 5 Defuzzified RPN and criticality ranking of failure modes for fuzzy FMECA

S. no.	Failure mode	$\alpha = 0$		$\alpha = 0.5$		$\alpha = 1.0$		Defuzzified RPN	Criticality ranking	
			RPNiL	RPNiR	RPNiL	RPNiR	RPNiL	RPNiR		
1	1.1	3.72	6.58	4.14	6.18	4.58	5.79	5.17	12	
2	1.2	3.48	6.88	3.95	6.42	4.42	5.96	5.19	11	
3	2.1	4.11	7.69	4.61	7.19	5.1	6.7	5.9	7	
4	2.2	1.13	3.96	1.51	3.47	1.89	3	2.5	14	
5	3.1	5.06	8.11	5.54	7.72	6.03	7.32	6.63	4	
6	3.2	5.06	8.11	5.54	7.72	6.03	7.32	6.60	5	
7	3.3	6.12	8.69	6.59	8.4	7.06	8.11	7.5	1	
8	4.1	4.06	7.66	4.56	7.16	5.05	6.66	5.86	8	
9	4.2	3.83	7.47	4.32	6.97	4.82	6.48	5.65	9	
10	4.3	4.56	8.04	5.06	7.54	5.56	7.04	6.3	6	
11	5.1	6.08	8.62	6.56	8.44	7.04	8.15	7.49	2	
12	6.1	3.84	7.08	4.3	6.62	4.76	6.17	5.47	10	
13	6.2	1.28	4.33	1.74	3.84	2.22	3.35	2.8	13	
14	6.3	4.98	8.31	5.48	7.81	5.97	7.31	6.65	3	

 Table 6
 Comparison of criticality ranking of failure modes

Component Failure mode		Fuzzy FMECA	Traditional FMECA	
1. Oil seals	1.1. Face wear	12	6	
	1.2. Embrittlement	11	5	
2. Motor	2.1. Overheating	7	4	
	2.2. Power supply anomalies	14	7	
3. Gear box	3.1. Wear	4	10	
	3.2. Surface fatigue failure	5	8	
	3.3. Breakage	1	9	
4. Bearing	4.1. Wear	8	9	
	4.2. Indentation	9	5	
	4.3. Corrosion	6	5	
5. Lead screw	5.1. Wear	2	2	
6. Belt drive	6.1. Pulley misalignment	10	8	
	6.2. Belt slip	13	3	
	6.3. Belt fatigue	3	1	

ranking of each failure mode is presented in Table 6. It has been observed that none of the failure modes have the same criticality ranking using fuzzy FMECA. Fuzzy FMECA considers the linguistic value and different weights of S, O, and D, which can be logically accepted and fuzzy RPN values are also different for each failure mode. Hence, Fuzzy FMECA can be considered as a better approach for criticality analysis of a system for the implementation of RCM.

7 Conclusion

FMEA is conducted to find out the failure modes of each component of a conventional lathe machine and the criticality analysis of failure modes using traditional FMECA and fuzzy FMECA approach. A comparative analysis of all the above approaches was done to find out a better approach of FMECA for criticality analysis of different failure modes of a system.

Criticality analysis using traditional FMECA reveals that failure mode numbers (3.2 and 6.1), (3.3 and 4.1), and (1.2, 4.2 and 4.3) are having the same criticality ranking 8, 9 and 5 respectively. All these failure modes having the same RPN 8, 6 and 18, even the S, O and D values are different for these failure modes. All these failure modes will not have the same impact on the failure of the lathe machine; therefore, defining the same criticality ranking for different failure modes is not logical. Also, as per the results, fatigue in the belt is the most critical and wear in the gearbox is the less critical failure mode.

Criticality analysis using fuzzy presents that each failure mode is having different criticality ranking based on defuzzified RPN values determined by fuzzy mathematics. Also, S, O, and D gave different weights for calculating the defuzzified RPN values using the centroid method for various α -cut fuzzy values. According to the results, breakage in the gearbox is the most critical and anomalies in power supply for the electric motor are less critical, which are the most appropriate results compared to the other two approaches.

Hence, it has been observed that fuzzy FMECA can be used to overcome the issues of conventional FMECA. Fuzzy FMECA considers the linguistic value and different weights of S, O, and D, which can be logically accepted. This approach provides more realistic results and flexible reflection in a real situation as FMEA is described in terms of the fuzzy variable. Also, the interdependencies among the various failure modes can be explored easily using fuzzy. Finally, it is concluded that the fuzzy approach can be considered as a better approach of FMECA for criticality analysis of different failure modes of a system.

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