#### **ORIGINAL ARTICLE**



# Distribution, mode of occurrence, and significance of rare-earth elements in coal from Samaleswari open cast coal blocks, Odisha, India with their provenance and paleodepositional environment

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#### Abstract

This study aims to thoroughly examine the distribution, concentration, and occurrence of a broad selection of REEs and major elements in coal samples from Samaleswari coal block, IB valley, Odisha, India using advanced geochemical tools. A total of 85 coal samples from four boreholes were characterized using proximate analysis and calorific value measurements. The corresponding ash samples were examined using X-ray Diffraction (XRD), X-ray Fluorescence (XRF), Electron Probe Microanalyzer (EPMA), and Inductively Coupled Plasma Mass Spectrometry (ICP-MS). The coal ash samples were delineated to be rich in SiO<sub>2</sub> (42–65%) along with a lower proportion of Al<sub>2</sub>O<sub>3</sub> (24–41%), Fe<sub>2</sub>O<sub>3</sub> (5–6%), and TiO<sub>2</sub> (1–2%). The average concentration of REEs in the four boreholes was found to be 510 ppm, with the distribution pattern being Ce>La > Nd > Y > Pr > Sc > Sm > Gd > Dy > Er > Yb > Eu > Ho > Tb > Tm > Lu. The concentration of critical REEs varied in the range of 100-300 ppm, and outlook coefficient (Cout) ranged from 0.7 to 1.0, demonstrating our coal seams' suitability as a promising source of REEs. A higher concentration of REEs in BH1 was correlated with a relatively higher proportion of apatite. The increment in REE concentration with depth was speculated to be due to their close association with hematite, especially in BH1 and BH2. A strong positive correlation of all the REEs with clay minerals and specifically TiO<sub>2</sub> reinstates their abundance in fine-grained clastic sedimentary rocks which are not significantly affected by weathering. Point analysis using EPMA and Scanning Electron Microscope-Energy Dispersive Analysis X-ray (SEM-EDAX) confirmed the coexistence of La, Ce, Pr, and Nd in the Fe-containing aluminosilicate matrix. In addition, the major oxide ratio and their plot entail terrestrial depositional environment in the basin during coal formation and deposited in semi-arid climatic conditions.

**Keywords** Samaleswari coal  $\cdot$  Rare-earth element distribution  $\cdot$  Pearson correlation  $\cdot$  Geochemistry  $\cdot$  Mineralogy  $\cdot$  Paleodepositional conditions

## Introduction

Coal is a combination of several organic and inorganic components. The inorganic constituents of the coal can often result from the deposition of sediments by fluids existing in the basin, sediment infilling during diagenesis, or input from syn-sedimentary volcanic activities (Ward 2016). The

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inorganic part of the coal is as important as the organic components, as it conveys crucial information about the depositional settings, the geological history of the strata, and regional tectonic movement (Wang et al. 2017). For many decades, coal has been utilized only as a fossil fuel to generate heat energy. However, recent research has proved that coal ash produced from industries and coal deposits can act as a storehouse of many economic minerals and important trace and rare-earth elements (Seredin et al. 2013; Hower et al. 2016; Ward 2016; Dai et al. 2018; Qin et al. 2018). Productive utilization of coal ash has been a persistent area of research and development (Bhattacharjee and Kandapal 2002). Coal combustion by-products are considered as alternative resources for REEs, owing to their enrichment in critical REEs and low-to-no-cost availability as waste

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products (Mayfield and Lewis 2013; Seredin et al. 2013; US department of energy 2017; Dai and Finkelman 2018; Sorokin et al. 2019). On an average, if coal typically contains 60 ppm of REE, a power plant ash produced from coal will have approximately 470 ppm of REEs (Seredin and Dai 2012). Consequently, utilization of coal ash waste for REE extraction, instead of augmenting mining exploration, is undoubtedly an environmentally sustainable approach. (Franus et al. 2015; Kolker et al. 2017).

Rare-earth elements are considered a critical raw material because of the large difference between global demand and their fewer resources (Franus et al. 2015). Identification of REE distribution and assessment of their possible association with other mineral oxides are crucial to improve the efficiency of their extraction. Most of the preliminary investigations on the mapping and distribution of REEs were performed in China (Zheng et al. 2007; Wang et al. 2008; Dai et al. 2016a). Subsequently, it gained a broader perspective owing to elevated demand, and research groups around the world started uncovering their own REE resources in coal deposits through distribution studies. In addition to economic importance, the distribution of rare-earth elements along with trace elements and mineralogical characterization has been provided important information about the provenance, mode of occurrence, and paleodepositional setting of the concern basin (Dai et al. 2016a, 2018; Wang et al. 2022).

Many researchers have studied rare-earth element distribution along with geochemistry and mineralogy of coal and coal-bearing strata throughout the globe (Birk and White 1991; Kortenski and Bakardjiev 1993; Seredin et al. 1996; Seredin 1998; Eskenazy 2009; Seredin et al. 2013; Dai et al. 2016a; Hower et al. 2016; Kolker et al. 2017; Dai et al. 2018; Qin et al. 2018; Sorokin et al. 2019; Tatar and Alipor-Asll 2020; Firman and Haya 2021; Wang et al. 2022). As concern to Indian coal-bearing strata, such kinds of investigations are very limited and based on sporadic samples (Saha et al. 2016, 2018; Saikia et al. 2021). Despite this, India has about 6% of the total global reserve of REEs but produces only 1% of the global supply, which is far below its actual capacity (Indian Bureau of Mines 2019). Exploration of potential geographical sources of valuable elements from coal necessitates both: (1) recognizing coals with high concentrations of REEs and then (2) formulating efficient strategies to extract the valuables. At present, even though research is targeted toward both goals; the emphasis is primarily on development of efficient extraction strategies of these elements. Therefore, the present investigation focuses on the distribution of REEs, major elements in major coalfield located at Samaleswari Open Cast Coal Block using advanced geochemical techniques. Samaleswari Coal Block belongs to IB valley Coalfield, Odisha. The total coal reserve in IB river was estimated to be 29,619.67 million tons, according to the recent statistics published by the Geological Survey of India (Geological Survey of India 2019). The knowledge of mineralogical composition (both REE and trace elements) of this particular area is crucial in terms of its further utilization for indigenous resources.

# **Geological setting**

In the present investigation, the coal samples have been collected from the Samaleswari area, located in IB Valley Coalfield, Odisha. The IB river basin is a part of the Mahanadi Gondwana basin that lies in a major NW–SE-trending lineament extending over 150 km from Korba, Chhattisgarh, to Sambalpur, Odisha. The IB Valley Coalfield is named after a tributary of Mahanadi (Mishra et al. 2016). It consists of two sub-basins, i.e., Hingir in the north and Rampur in the south (Fig. 1), marked by a major fault (Singh et al. 2013).

The IB basin is exposed in a westerly plunging synclinal flexure in the form of a half elliptical basin closed toward the northwest. The basement is marked by Precambrian gneissic rocks exposed by the periphery of the basin (Manjrekar et al. 2006; Singh et al. 2013; Senapati and Behera 2015). The S–W boundary fault juxtaposes these Archean rocks with the younger Permian rocks. The sedimentary rocks started with the Talchir Formation, which unconformably overlies the basement, followed by the Karharbari and Barakar Formations of the Lower Permian age (Table 1). The upper Permian to lower Triassic sedimentary Formations are represented by Lower Kamathi and Upper Kamathi Formation, which are correlated with Barren Measures and Ranighanj Formation for the generalized Gondwana succession.

Samaleswari coal block is located in the Jharsuguda district with latitude 21°46'–21°49'N and longitude 83°52'–83°56'E, as depicted in Fig. 1. Four boreholes were selected from this area for the present study, each containing 3–4 seams with varying depths. The total number of coal samples collected, along with the respective depth of each borehole, is tabulated in Table 2.

#### **Materials and methods**

A total of 85 coal samples from four boreholes (BH1, BH2, BH3, and BH4) of Samaleswari Coal Block were collected for the present investigation. The collected coal samples were pulverized in a ball mill with 100% passing of -212  $\mu$ m (-72 mesh) sieve prior to analysis. Proximate analysis, viz., moisture, ash, and volatile matter content, of the coal was performed using proximate analyzer as per IS 1350 (Part 1): RA 2019. The Gross Calorific Value (GCV) of coal samples was determined using Parr 6200 bomb calorimeter (Parr, USA) as per ASTM D 5865:2019. The coal ash sample was prepared by heating the coal sample



Fig. 1 Location of Samaleswari Open Cast Mines, IB valley, Odisha, India (after Senapaty and Behera 2015)

|  | Table 1 | Geological | succession of | the IB v | valley coal | field (adap | oted from | Senapaty | / and Behera 20 | )15) |
|--|---------|------------|---------------|----------|-------------|-------------|-----------|----------|-----------------|------|
|--|---------|------------|---------------|----------|-------------|-------------|-----------|----------|-----------------|------|

| Age                           | Formation   | Lithology  |
|-------------------------------|---|--|
| Recent                        |   | Alluvium; sand, silt and clay of older alluvium, younger flood plain deposits  |
| Sub-recent                    |   | Laterites/recent gravel and conglomerate beds  |
| Up. Permian to lower Triassic | Kamthi (upper) = Raniganj<br>Kamthi (lower) = Barren meas-<br>ures<br>Barakar | Conglomerates, pebbly and ferruginous sandstones<br>Gray and carbonaceous shales, sandstone, clay and iron stone nodules<br>Gray sandstone, carbonaceous shale, silt stone with thick coal seams |
| Lower Permian                 | Karharbari  | Black carbonaceous sandstone, pebble bed, coal seams   |
|                               | Talcher   | Diamictite, greenish sand stone, olive and chocolate shales  |
| Unconformity                  |   |  |
| Precambrian                   |   | Granite gneisses, amphibolites, etc.   |

in presence of air at 850 °C for 1 h in a muffle furnace as per IS:1350 (Part 1): RA 2019. Lithium metaborate and lithium tetraborate were purchased from Loba Chemie. Nitric acid (reagent grade, 65%) was procured from Rankem, India. Deionized (DI) water was produced in the lab using a Milli Q water purification system (Millipore).

The elemental composition of the selected coal ash sample was determined using X-ray fluorescence (XRF)

Table 2 Details of boreholes selected for sample collection

| Borehole name | Depth (meter)                             |
|---------------|---|
| BH1           | 19.78–450.98                              |
| BH2           | 8.40-404.19                               |
| BH3           | 12.58-416.00                              |
| BH4           | 13.80-375.84                              |
|               | Borehole name<br>BH1<br>BH2<br>BH3<br>BH4 |

spectrophotometer (S8 Tiger, Bruker) using the press pellet method. Quantitative measurement of rare-earth elements in all the coal ash samples was determined using an inductively coupled plasma-mass spectrometer (ICP-MS) (Perkin Elmer, Model ELAN DRC-e with Axial Field Technology). The XRD pattern was recorded over a 2 $\theta$  range of 5°- 90°, with a step size of 0.03° using Ni-filtered Cu K $\alpha$  radiation. The qualitative mineralogical analysis of all acquired XRD patterns was performed using High Score plus software on the basis of JCPDS database. Point analysis of representative coal ash samples from each borehole was performed using both electron probe micro-analyzer (EPMA) (JXA 8230, JEOL) and Scanning Electron Microscopy (SEM) (FEI NOVA NANOSEM 430) using acceleration voltage of 15 kV.

#### **Determination of total REE concentration**

The total REE concentration was determined according to the protocol published previously (Banerjee et al. 2021). For each set of experiment, coal ash sample (0.1 g) was mixed with fusion mixture of lithium metaborate (0.2 g, LiBO<sub>2</sub>) and lithium tetraborate (0.15 g, Li<sub>2</sub>B<sub>4</sub>O<sub>7</sub>). The fusion mixture was thoroughly shaken to avoid lump formation during the course of reaction. The coal ash–borate mixture was then fused at 950 °C in a muffle furnace for 1 h, followed by stepwise cooling at 300 °C and then room temperature. Nitric acid solution (10%) was added to the fused sample and the resultant mixture was stirred to ensure complete dissolution. The extracted solution obtained was then transferred into a 250 ml volumetric flask and taken forward for ICP-MS analysis.

#### Statistical analysis methods

Box-and-whisker plot diagrams were constructed to analyze the distribution of REEs in chosen boreholes. Agglomerative hierarchical clustering (AHC) was performed between elemental oxides and REEs to establish their degree of correlation. The Pearson's concentration coefficient was used to show the interrelationship and coherence pattern among REEs of the coal ash samples which were examined.

### **Results and discussion**

#### **Chemical composition of coal**

The results obtained for proximate analysis of the four selected boreholes (BH1, BH2, BH3, BH4) of Samaleswari Block are presented in Tables 3 and 4 and Table S-1a, b. It is evident from the tabulated results that there is a significant variation in the quality of coal samples from one borehole to another. The gross calorific values demonstrated a notable increase as we increased the depth from where the samples were collected, owing to reduction in the content of mineral matter. On the basis of the proximate analysis, the average ash content in the four boreholes ranged from 49 to 51%, fixed carbon concentration ranged from 23 to 25% and the moisture content varied from 3.8 to 5% (Table 5). The coal collected from the deepest band of each borehole demonstrated highest quality. For example, for borehole BH1, the sample collected at a depth of 450 m showed highest GCV value (5036 kcal/ kg), lowest mineral matter content (31%), and lowest moisture content (3.44%). Similar observations were made for all the boreholes. The average values of all the parameters obtained in individual boreholes are tabulated in Table 5.

#### **Major-element concentrations in coals**

The chemistry of feed coal and the process parameters during its combustion largely dictates the chemical composition of the resultant coal ash. As evident from the XRF analysis, coal ash corresponding to coals of Samaleswari Block is typically comprised of the following oxides: SiO<sub>2</sub>, Al<sub>2</sub>O<sub>3</sub>, Fe<sub>2</sub>O<sub>3</sub>, and TiO<sub>2</sub> in higher proportions and CaO, MgO, K<sub>2</sub>O, P<sub>2</sub>O<sub>5</sub>, Na<sub>2</sub>O, and SO<sub>3</sub> in minor concentration (shown in Tables 6 and 7 and Table S-2a, b). SiO<sub>2</sub> and Al<sub>2</sub>O<sub>3</sub> were the two major oxides whose concentration varied in the range of 42-65% and 24-41%, respectively, across the four boreholes. Interestingly, Fe<sub>2</sub>O<sub>3</sub> demonstrated the highest variation in concentration among the entire samples which were examined. For instance, in sample A24 (BH1), the concentration of  $Fe_2O_3$  was only 1.08% (Table 6), whereas in sample B13 (BH2), it was present in 22.5% (Table 7). The concentration of hematite (Fe<sub>2</sub>O<sub>3</sub>) increased with depth, more prominently for BH1 and BH2. The increase in REE concentration could be well correlated with hematite abundance in these two boreholes (Table 6 and 7). Hematite bearing REE phases is a common occurrence in coal samples of varied geological origin (Oreskes et al. 1990; Abaka-Wood 2022). Overall, the oxides of the major elements (Si, Al, Fe, and Ti) measured up to approximately 94% of the total ash compositions, the remaining 6% being that of the minor oxides. The Table 3Proximate analysis ofBH1 (VM volatile matter, GCVgross calorific value)

| Depth (m)     | Samples | Moisture (%) | Ash (%) | VM (%) | Fixed carbon (%) | GCV (kcal/kg) |
|---------------|---------|--------------|---------|--------|------------------|---------------|
| 19.78–30.44   | A1      | 4.88         | 53.18   | 22.84  | 19.10            | 2725.31       |
| 51.97-53.20   | A2      | 6.94         | 38.02   | 29.59  | 25.45            | 3835.75       |
| 92.93–95.68   | A3      | 3.84         | 55.68   | 21.37  | 19.11            | 2660.18       |
| 108.34-112.28 | A4      | 3.71         | 57.61   | 20.22  | 18.46            | 2500.61       |
| 116.16–118.39 | A5      | 3.57         | 61.11   | 18.40  | 16.93            | 2176.18       |
| 120.10-121.32 | A6      | 4.66         | 49.49   | 22.83  | 23.02            | 3149.48       |
| 139.43-140.00 | A7      | 4.11         | 55.94   | 19.69  | 20.26            | 2585.80       |
| 142.26-143.63 | A8      | 4.11         | 49.30   | 22.24  | 24.35            | 3246.94       |
| 152.20-153.94 | A9      | 3.66         | 57.04   | 19.61  | 19.69            | 2552.62       |
| 162.67–164.30 | A10     | 4.60         | 48.30   | 23.35  | 23.75            | 3226.73       |
| 206.84-207.97 | A11     | 4.64         | 43.17   | 25.63  | 26.55            | 3718.72       |
| 216.55-219.33 | A12     | 4.27         | 46.42   | 24.38  | 24.93            | 3461.08       |
| 275.27-303.86 | A13     | 3.89         | 41.60   | 26.96  | 27.56            | 3994.22       |
| 311.98–315.77 | A14     | 3.74         | 52.48   | 23.98  | 19.80            | 2978.77       |
| 316.75-323.50 | A15     | 3.47         | 43.27   | 26.37  | 26.90            | 3909.44       |
| 311.98-323.50 | A16     | 3.24         | 51.62   | 24.13  | 21.00            | 3131.66       |
| 372.73-377.10 | A17     | 2.98         | 54.96   | 20.32  | 21.74            | 2864.83       |
| 380.15-381.41 | A18     | 2.88         | 54.58   | 20.42  | 22.12            | 2924.13       |
| 382.48-383.28 | A19     | 2.84         | 63.09   | 19.95  | 14.12            | 2115.35       |
| 390.95-394.13 | A20     | 2.94         | 48.26   | 25.03  | 23.77            | 3501.01       |
| 396.12-398.54 | A21     | 3.74         | 37.85   | 27.18  | 31.22            | 4351.56       |
| 399.66-428.26 | A22     | 2.77         | 51.66   | 21.27  | 24.30            | 3203.60       |
| 390.95-428.26 | A23     | 2.66         | 53.58   | 20.58  | 23.18            | 3045.16       |
| 448.76–450.98 | A24     | 3.44         | 30.99   | 28.49  | 37.08            | 5036.16       |
| Average       |         | 3.82         | 49.97   | 23.12  | 23.10            | 3203.97       |

| Table 4  | Proximate analysis of  |
|----------|------------------------|
| BH2 (V.  | M volatile matter, GCV |
| gross ca | lorific value)         |

| Depth (m)     | Samples | Moisture (%) | Ash (%) | VM (%) | Fixed carbon (%) | GCV (kcal/kg) |
|---------------|---------|--------------|---------|--------|------------------|---------------|
| 8.40-9.22     | B1      | 7.02         | 38.02   | 26.12  | 28.85            | 3890.65       |
| 59.28-63.40   | B2      | 4.37         | 54.50   | 20.07  | 21.06            | 2704.77       |
| 77.98-80.44   | B3      | 4.80         | 60.21   | 17.51  | 17.48            | 2133.37       |
| 82.32-83.39   | B4      | 5.98         | 49.57   | 21.14  | 23.31            | 2911.53       |
| 88.05-89.12   | B5      | 4.87         | 54.90   | 20.03  | 20.21            | 2579.48       |
| 101.09-103.13 | B6      | 3.98         | 64.14   | 17.28  | 14.60            | 1852.42       |
| 104.61-106.81 | B7      | 4.98         | 55.28   | 21.41  | 18.33            | 2527.12       |
| 128.64-130.58 | B8      | 4.83         | 50.44   | 22.02  | 22.72            | 3018.70       |
| 176.79–177.69 | B9      | 5.77         | 38.25   | 25.94  | 30.04            | 3997.35       |
| 188.32-189.33 | B10     | 4.54         | 47.77   | 24.61  | 23.09            | 3304.92       |
| 199.66-202.18 | B11     | 3.74         | 58.26   | 20.65  | 17.35            | 2432.03       |
| 238.00-267.64 | B12     | 4.94         | 41.41   | 26.51  | 27.13            | 3830.30       |
| 279.05-281.20 | B13     | 3.86         | 49.89   | 28.65  | 17.60            | 3198.34       |
| 285.24-291.33 | B14     | 4.64         | 44.33   | 24.97  | 26.07            | 3622.12       |
| 332.77-333.84 | B15     | 3.77         | 50.01   | 21.81  | 24.41            | 3202.36       |
| 342.05-381.29 | B16     | 2.99         | 53.35   | 20.89  | 22.77            | 3048.03       |
| 402.17-404.19 | B17     | 3.98         | 37.95   | 23.24  | 34.84            | 4301.03       |
| Average       |         | 4.65         | 48.28   | 22.83  | 24.24            | 3243.64       |

 Table 5
 Summary of average values obtained for proximate analysis of four boreholes (VM volatile matter, GCV gross calorific value)

| Borehole name | Depth (m)    | Samples | Moisture (%) | Ash (%) | VM (%) | Fixed carbon (%) | GCV (kcal/Kg) |
|---------------|--------------|---------|--------------|---------|--------|------------------|---------------|
| BH1           | 19.78-450.98 | 24      | 3.82         | 49.97   | 23.12  | 23.10            | 3204          |
| BH2           | 8.40-404.19  | 17      | 4.65         | 48.28   | 22.83  | 24.24            | 3244          |
| BH3           | 12.58-416.00 | 20      | 4.65         | 48.28   | 22.83  | 24.24            | 3244          |
| BH4           | 13.80-375.84 | 24      | 5.53         | 50.86   | 20.46  | 23.15            | 2880          |

Table 6Major oxide (%) distribution in coal ash of BH1

| Samples | SiO <sub>2</sub> | Al <sub>2</sub> O <sub>3</sub> | Fe <sub>2</sub> O <sub>3</sub> | K <sub>2</sub> O | TiO <sub>2</sub> | CaO  | MgO  | Na <sub>2</sub> O | $P_2O_5$ | SO <sub>3</sub> |
|---------|------------------|--------------------------------|--------------------------------|------------------|------------------|------|------|-------------------|----------|-----------------|
| A1      | 60.6             | 28.9                           | 3.45                           | 1.89             | 1.49             | 1.22 | 0.91 | 0.11              | 0.89     | 0.19            |
| A2      | 60               | 25.3                           | 6.59                           | 2.98             | 1.2              | 0.74 | 1.34 | 0.15              | 0.53     | 0.69            |
| A3      | 63.7             | 27.3                           | 2.32                           | 2.52             | 1.26             | 0.52 | 1.19 | 0.15              | 0.46     | 0.3             |
| A4      | 64.9             | 25.5                           | 2.64                           | 3.14             | 1.17             | 0.46 | 1.35 | 0.12              | 0.25     | 0.18            |
| A5      | 65.3             | 24.4                           | 3.26                           | 3.30             | 1.08             | 0.38 | 1.44 | 0.14              | 0.15     | 0.24            |
| A6      | 63.2             | 26.7                           | 3.09                           | 3.12             | 1.24             | 0.43 | 1.42 | 0.14              | 0.13     | 0.24            |
| A7      | 62.8             | 25.6                           | 5.07                           | 2.44             | 1.2              | 0.72 | 1.23 | 0.11              | 0.31     | 0.29            |
| A8      | 60.8             | 28.9                           | 3.79                           | 2.39             | 1.33             | 0.53 | 1.1  | 0.08              | 0.33     | 0.44            |
| A9      | 63.5             | 27.7                           | 2.6                            | 2.48             | 1.36             | 0.49 | 1.15 | 0.11              | 0.2      | 0.22            |
| A10     | 60.3             | 29.7                           | 3.48                           | 2.32             | 1.53             | 0.53 | 1.26 | 0.09              | 0.18     | 0.29            |
| A11     | 59.3             | 31.4                           | 3.07                           | 1.93             | 1.6              | 0.57 | 0.97 | 0.08              | 0.4      | 0.25            |
| A12     | 59               | 32                             | 3.97                           | 1.5              | 1.66             | 0.4  | 0.74 | 0.07              | 0.23     | 0.2             |
| A13     | 55.5             | 34.6                           | 4.7                            | 0.89             | 2.01             | 0.79 | 0.57 | 0.06              | 0.54     | 0.1             |
| A14     | 47.3             | 37.4                           | 11.15                          | 0.75             | 1.87             | 0.27 | 0.62 | -                 | 0.1      | 0.16            |
| A15     | 49.8             | 38.9                           | 6.8                            | 0.86             | 2.13             | 0.39 | 0.52 | 0.07              | 0.14     | 0.06            |
| A16     | 51.1             | 37.4                           | 7.33                           | 0.83             | 1.95             | 0.28 | 0.53 | 0.07              | 0.1      | 0.07            |
| A17     | 61.4             | 30.6                           | 3.8                            | 0.98             | 1.88             | 0.28 | 0.46 | 0.06              | 0.11     | 0.07            |
| A18     | 56.1             | 34.5                           | 4.92                           | 0.93             | 1.96             | 0.32 | 0.54 | 0.06              | 0.21     | 0.09            |
| A19     | 55               | 28.3                           | 12.48                          | 0.87             | 1.58             | 0.34 | 0.65 | _                 | 0.24     | 0.13            |
| A20     | 49.5             | 35.3                           | 10.17                          | 0.81             | 1.75             | 0.82 | 0.62 | -                 | 0.52     | 0.24            |
| A21     | 50               | 31.2                           | 13.05                          | 0.89             | 1.79             | 0.92 | 0.75 | 0.06              | 0.66     | 0.16            |
| A22     | 57.8             | 32.8                           | 5.01                           | 0.86             | 1.86             | 0.49 | 0.48 | 0.06              | 0.28     | 0.08            |
| A23     | 54.9             | 35.5                           | 5.19                           | 0.83             | 1.84             | 0.48 | 0.49 | 0.09              | 0.31     | 0.1             |
| A24     | 55               | 39.7                           | 1.08                           | 0.84             | 2.17             | 0.27 | 0.31 | 0.09              | 0.08     | 0.08            |
| Average | 57.78            | 31.2                           | 5.38                           | 1.68             | 1.62             | 0.53 | 0.86 | 0.09              | 0.31     | 0.203           |

average content of both major and minor elements (Tables 6 and 7) and (Table S-2a, b) was in the decreasing order of  $SiO_2 > Al_2O_3 > Fe_2O_3 > TiO_2 > K_2O > MgO > CaO > P_2O_5 > SO_3 > Na_2O$ .

#### **Rare-earth elements**

The results obtained for rare-earth concentrations of all the 85 coal ash samples are tabulated in Table 8a-d. The concentration of individual REEs (both LREE and HREE), total REEs, average value of REEs, ratio of LREE/HREE, and outlook coefficient data of all samples are included in the same. Noticeable variation in total REE concentration was found within all the analyzed samples from four boreholes (348.86 to 971.06 ppm) with an average value of 510 ppm. Typically, the concentration of REE increased in coal ash samples as we increased the depth of borehole. This could be collectively suggestive of felsic composition in the source region as weathering of felsic rocks can cause enrichments of LREEs in the residue. The four REEs which were predominantly present were Ce (112–353 ppm), La (69–225 ppm), Nd (44–136 ppm), and Y (34–110 ppm) (Table 8a-d). Lu and Tm, which belong to the HREEs, were present in the lowest concentrations (0.5–1.8 ppm) showing their minimal association with the inorganic matter. The distribution pattern of REEs followed the order Ce > La > Nd > Y > Pr > Sc > Sm > Gd > Dy > Er > Yb > Eu > Ho > Tb > Tm > Lu where the most abundant lanthanide was Ce and the least abundant was Lu. The ratio of  $\Sigma LREE/\Sigma$ HREE among different boreholes varied from 2.56 to 5.35 with an Table 7Major oxide (%)distribution in coal ash of BH2

| Samples | SiO <sub>2</sub> | Al <sub>2</sub> O <sub>3</sub> | Fe <sub>2</sub> O <sub>3</sub> | K <sub>2</sub> 0 | TiO <sub>2</sub> | CaO  | MgO  | Na <sub>2</sub> O | $P_2O_5$ | SO3  |
|---------|------------------|--------------------------------|--------------------------------|------------------|------------------|------|------|-------------------|----------|------|
| B1      | 61.9             | 27.4                           | 3.68                           | 2.58             | 1.22             | 0.84 | 1.18 | 0.13              | 0.09     | 0.53 |
| B2      | 62.8             | 27.9                           | 2.87                           | 2.41             | 1.26             | 0.61 | 1.09 | 0.11              | 0.46     | 0.19 |
| B3      | 64.1             | 26.1                           | 3.03                           | 3.1              | 1.14             | 0.39 | 1.36 | 0.14              | 0.09     | 0.23 |
| B4      | 58.57            | 26.3                           | 4.00                           | 2.92             | 1.24             | 0.52 | 1.34 | 0.11              | 0.1      | 0.34 |
| B5      | 64               | 28                             | 2.17                           | 2.23             | 1.44             | 0.51 | 0.96 | 0.12              | 0.1      | 0.15 |
| B6      | 65.1             | 27                             | 2.13                           | 2.48             | 1.32             | 0.37 | 0.97 | 0.12              | 0.09     | 0.11 |
| B7      | 58.6             | 27.6                           | 7.63                           | 2.29             | 1.26             | 0.62 | 1.16 | 0.14              | 0.11     | 0.24 |
| B8      | 61.2             | 29.2                           | 3.14                           | 2.37             | 1.54             | 0.51 | 1.24 | 0.14              | 0.1      | 0.23 |
| B9      | 56.7             | 33.7                           | 3.47                           | 1.76             | 1.67             | 0.67 | 0.95 | 0.08              | 0.29     | 0.26 |
| B10     | 59.6             | 29.7                           | 5.27                           | 1.67             | 1.78             | 0.42 | 0.79 | 0.1               | 0.12     | 0.25 |
| B11     | 53.2             | 36.8                           | 5.49                           | 1.4              | 1.48             | 0.27 | 0.72 | 0.09              | 0.1      | 0.15 |
| B12     | 51.8             | 38.2                           | 4.73                           | 0.86             | 1.98             | 0.79 | 0.53 | 0.07              | 0.49     | 0.14 |
| B13     | 41.6             | 31.2                           | 22.49                          | 0.77             | 1.65             | 0.47 | 1.01 | -                 | 0.15     | 0.22 |
| B14     | 52.7             | 34.6                           | 7.93                           | 0.92             | 2.05             | 0.38 | 0.6  | -                 | 0.17     | 0.24 |
| B15     | 58               | 30.2                           | 7.14                           | 0.69             | 1.91             | 0.48 | 0.6  | -                 | 0.26     | 0.14 |
| B16     | 54.9             | 35.7                           | 4.83                           | 0.82             | 1.87             | 0.5  | 0.48 | 0.06              | 0.31     | 0.08 |
| B17     | 56               | 37.9                           | 1.55                           | 0.86             | 2.42             | 0.3  | 0.33 | 0.06              | 0.07     | 0.05 |
| Average | 57.7             | 31.0                           | 5.39                           | 1.77             | 1.60             | 0.51 | 0.90 | 0.11              | 0.18     | 0.21 |

average value of 3.85, which validated the higher affinity of LREE (around 80%) for the inorganic matter in Samaleswari coal block. The fraction of HREE remained considerably low (20%) for all of them.

#### **REE distribution and their significance**

The method of resource assessment originally proposed by Seredin and Dai typically assisted in evaluating the suitability of coal or its by-product as a source for the extraction of REE. The ratio of critical to excessive REEs in the source (Seredin and Dai 2012) gives us the Outlook Coefficient ( $C_{outl}$ ), which is instrumental toward suitability assessment of a particular area. In compliance with previous literature, the coal ash samples which were examined proved to be a promising source of REEs based on the calculated  $C_{outl}$ (Eq. 1) which varied from 0.7 to 1.0 (Lin et al; 2017; Franus et al; 2015)

$$Coutl = \frac{(Nd + Eu + Tb + Dy + Er + Y) / \sum REE}{(Ce + Ho + Tm + Yb + Lu) / \sum REE}.$$
 (1)

The PAAS (Post-Archean Australian Shale) normalized plots (Taylor and McLennan 1985) of all the samples from four boreholes are represented in Fig. 2a-d and Table 8. It showed that all the boreholes demonstrated a similar pattern, indicating similarity in depositional conditions that prevailed throughout the period as REE fractionation is independent of diagenesis. Overall, flat REE pattern indicated a mixed source of sedimentation. The (La/Yb)<sub>N</sub> ratio was calculated to quantify the fractionation between LREE and HREE

(Table 8). The result showed that the ratio varied between 1.52 and 0.74 for BH1, 1.30 and 0.92 for BH-2, 1.25 and 1.44 for BH-3, and 0.94 and 1.17 for BH-4 and most of the  $(La/Yb)_N$  is greater than  $\geq 1$ , which indicated that samples were primarily LREE intensified and possibly associated phosphate and carbonate rocks (Wang and Liang., 2015). Most Eu anomalies were found to be lower than 1, varying from 0.8 to 1, except for BH-2, where it varied from 0.49 to 0.52. BH-2, thus, showed significantly negative Eu anomalies as compared to the other three boreholes. To sum it up, slightly negative Eu anomaly (Eu/Eu\*) and high LREE/HREE ratio indicates felsic influence in sedimentation (Tobia et al. 2019).

As presented in Tables 9 and 10 and Table S-3a, b for all the coal ashes which were analyzed in this study, the concentration of critical rare-earth elements varied in the range of 100-300 ppm and C<sub>outl</sub> ranged from 0.7 to 1.0. Coal seams from the Samaleswari coal block could therefore be considered a promising source of REE elements (Seredin and Dai 2012). To ensure that the conclusion drawn from the study is representative of the whole coal ash stockpile, we chose to analyze 17-24 coal samples from each borehole. The REE content of all the samples was grossly similar to data represented previously by Franus et al. (2015). The total REE content of individual boreholes (Tables 9 and 10) varied within the range of 413-663 ppm (BH1), 349-704 ppm (BH2), 385–615 ppm (BH3), and 363–971 ppm (BH4). Roughly, all the coal ash samples demonstrated their respective REE content to be either similar or significantly higher than the world's average (445 ppm) (Kertis and Yudowich 2009). In accordance with literature precedence Dai et al (2016a),

Sample

A1

A2

A3

A4

A5

A6

A7

A8

A9

A10

A11

A12

A13 A14

A15

A16

A17

A18

A19

A20

A21

A22

A23

A24

B1

B2

B3

B4

В5

B6

B7

B8

B9

B10

B11 B12

B13

B14

B15

B16

B17

Borehole

BH-1

Table 8  $La/Yb_N$  fractionation and Ce and Eu anomalies' distribution in the four boreholes of Samaleswari coal

La/Yb

1.52

1.26

1.42

1.23

1.24

1.31

1.27

1.30

1.47

1.42

1.35

1.37

1.43

1.27

1.35

1.34

1.44

1.54

1.69

1.37

1.48

1.54

1.48

0.74

0.92

1.20

1.18

1.20

1.10

1.16

1.22

1.14

1.43

0.99

1.29

1.29

1.20

1.19

1.99

1.42

1.30

| e and Eu anon | nalies' distribution | Table 8 (c | ontinued) |       |              |              |
|---------------|----------------------|------------|-----------|-------|--------------|--------------|
| coal block    |                      | Borehole   | Sample    | La/Yb | Ce anomalies | Eu anomalies |
| Ce anomalies  | Eu anomalies         | BH-3       | C1        | 1.25  | 0.91         | 0.92         |
| 0.54          | 1.00                 |            | C2        | 1.51  | 0.90         | 0.92         |
| 0.56          | 0.96                 |            | C3        | 1.42  | 0.02         | 0.03         |
| 0.51          | 1.07                 |            | 05        | 1.42  | 0.92         | 0.95         |
| 0.58          | 0.91                 |            | C4        | 1.35  | 0.92         | 0.92         |
| 0.49          | 1.00                 |            | C5        | 1.30  | 0.90         | 0.91         |
| 0.51          | 0.97                 |            | C6        | 1.37  | 0.90         | 0.93         |
| 0.51          | 0.99                 |            | C7        | 1.34  | 0.93         | 0.94         |
| 0.50          | 0.99                 |            | C7        | 1.54  | 0.95         | 0.94         |
| 0.39          | 0.88                 |            | C8        | 1.42  | 0.91         | 0.91         |
| 0.70          | 1.05                 |            | C9        | 1.30  | 0.90         | 0.89         |
| 0.40          | 1.04                 |            | C10       | 1.47  | 0.94         | 0.91         |
| 0.54          | 0.88                 |            | C11       | 1 34  | 0.95         | 0.90         |
| ).59          | 1.01                 |            | 011       | 1.34  | 0.25         | 0.90         |
| 1.8/          | 0.91                 |            | C12       | 1.24  | 0.95         | 0.91         |
| J.89          | 0.90                 |            | C13       | 1.64  | 0.93         | 0.92         |
| ).90<br>) 95  | 0.91                 |            | C14       | 1.26  | 0.93         | 0.94         |
| ) 83          | 0.92                 |            | C15       | 1.20  | 0.93         | 0.93         |
| ) 85          | 0.89                 |            | 015       | 1.20  | 0.95         | 0.95         |
| 1.85          | 0.89                 |            | C16       | 1.20  | 0.95         | 0.95         |
| 0.83          | 0.90                 |            | C17       | 1.45  | 0.92         | 0.97         |
| .89           | 0.89                 |            | C18       | 1.42  | 0.90         | 0.96         |
| .86           | 0.91                 |            | C19       | 1.21  | 0.92         | 0.96         |
| .87           | 0.90                 |            | 019       | 1.21  | 0.92         | 0.90         |
| ).85          | 0.49                 |            | C20       | 2.15  | 0.93         | 0.86         |
| ).86          | 0.51                 |            | C21       | 1.46  | 0.92         | 0.84         |
| 0.85          | 0.54                 |            | C22       | 1.39  | 0.92         | 0.86         |
| ).84          | 0.52                 |            | C23       | 1 27  | 1.02         | 0.87         |
| ).86          | 0.55                 |            | 625       | 1.27  | 0.02         | 0.07         |
| ).87          | 0.54                 |            | C24       | 1.44  | 0.93         | 0.84         |
| ).86          | 0.51                 | BH-4       | DI        | 0.94  | 0.92         | 0.85         |
| 0.87          | 0.55                 |            | D2        | 1.34  | 0.90         | 0.85         |
| ).83          | 0.53                 |            | D3        | 1.37  | 0.89         | 0.80         |
| 0.82          | 0.50                 |            | D5        | 1.20  | 0.09         | 0.75         |
| 0.86          | 0.48                 |            | D6        | 1.14  | 0.92         | 0.83         |
| 0.85          | 0.52                 |            | D7        | 1.25  | 0.93         | 0.82         |
| 0.84          | 0.52                 |            | D8        | 1.27  | 0.92         | 0.83         |
| 0.88          | 0.56                 |            | D9        | 1.46  | 0.90         | 0.82         |
| 0.81          | 0.55                 |            | D10       | 1.26  | 0.92         | 0.80         |
| 1.65          | 0.57                 |            | D11       | 1.43  | 0.95         | 0.82         |
| .0.           | 0.32                 |            | D12       | 1.48  | 0.94         | 0.82         |
|               |                      |            | D13       | 1.31  | 0.93         | 0.86         |
|               |                      |            | D14       | 1.19  | 0.95         | 0.86         |
|               |                      |            | D15       | 1.85  | 0.95         | 0.87         |
|               |                      |            | D16       | 1.63  | 0.91         | 0.87         |
|               |                      |            | D17       | 1.52  | 0.93         | 0.85         |
|               |                      |            | D18       | 1.60  | 0.91         | 0.86         |
|               |                      |            | D19       | 1.16  | 0.89         | 0.85         |
|               |                      |            | D20       | 1.17  | 0.95         | 0.89         |

 $\begin{array}{l} Description: Eu_N/Eu_N^*: Eu \ anomalies \ ((Eu_n)/(Sm_n^*Gd_n)^{0.5}) \ Ce_N/Ce_N^*: \\ Ce \ anomalies \ ((Ce_n)/(La_n^*Pr_n)^{0.5}); \ La/Yb_N: \ fractionation \ of \ normalise \ (Ce_n)/(La_n^*Pr_n)^{0.5}); \ La/Yb_N: \ fractionation \ of \ normalise \ (Ce_n)/(La_n^*Pr_n)^{0.5}); \ La/Yb_N: \ fractionation \ of \ normalise \ (Ce_n)/(La_n^*Pr_n)^{0.5}); \ La/Yb_N: \ fractionation \ of \ normalise \ (Ce_n)/(La_n^*Pr_n)^{0.5}); \ La/Yb_N: \ fractionation \ of \ normalise \ (Ce_n)/(La_n^*Pr_n)^{0.5}); \ La/Yb_N: \ fractionation \ of \ normalise \ (Ce_n)/(La_n^*Pr_n)^{0.5}); \ La/Yb_N: \ fractionation \ of \ normalise \ (Ce_n)/(La_n^*Pr_n)^{0.5}); \ La/Yb_N: \ fractionation \ of \ normalise \ (Ce_n)/(La_n^*Pr_n)^{0.5}); \ La/Yb_N: \ fractionation \ of \ normalise \ (Ce_n)/(La_n^*Pr_n)^{0.5}); \ La/Yb_N: \ fractionation \ of \ normalise \ (Ce_n)/(La_n^*Pr_n)^{0.5}); \ La/Yb_N: \ fractionation \ of \ normalise \ (Ce_n)/(La_n^*Pr_n)^{0.5}); \ La/Yb_N: \ fractionation \ of \ normalise \ (Ce_n)/(La_n^*Pr_n)^{0.5}); \ La/Yb_N: \ fractionation \ of \ normalise \ (Ce_n)/(La_n^*Pr_n)^{0.5}); \ La/Yb_N: \ fractionation \ of \ normalise \ (Ce_n)/(La_n^*Pr_n)^{0.5}); \ La/Yb_N: \ fractionation \ of \ normalise \ (Ce_n)/(La_n^*Pr_n)^{0.5}); \ La/Yb_N: \ fractionation \ of \ normalise \ (Ce_n)/(La_n^*Pr_n)^{0.5}); \ La/Yb_N: \ fractionation \ of \ normalise \ (Ce_n)/(La_n^*Pr_n)^{0.5}); \ La/Yb_N: \ fractionation \ (Ce_n)/(La_n^*Pr_n)^{0.5}); \ La/Yb_N: \ (Ce_n)/(La_n^*Pr_n)^{0.5}); \ La/Yb_N: \ fractionationation \ (Ce_n)/(La_n^*Pr_n)^{0.5}); \ La/Yb_N: \ (Ce_n)/(La_n^*Pr_n)^{0.5}); \ La/Yb_N: \ fractionationationation \ (Ce_n)/(La_n^*Pr_n)^{0.5}); \ La/Yb_N: \ (Ce_n)/(La_n^*Pr_n)^{0.5$ ized Lanthanum and Ytterbium value, PAAS (Post-Archean Australian Shale) REEs' value was used as a reference for normalization



Fig. 2 UCC normalized plots of all the samples from four boreholes

we observed that the concentrations of all REEs except lanthanum (La) and cerium (Ce) are almost similar to world hard coal ash data (Fig. 3). Concentration coefficients (CC) obtained by calculating the ratio of average concentration of REEs in coal ash samples from Samaleswari coal block *vs* average of the corresponding element in world hard coal ash is shown in Fig. 4. It substantiated the fair enrichment of La and Ce (1 < CC < 2) along with weak enrichment of Sm (0.5 < CC < 1). An overall estimation suggested that the coal samples from the Samaleswari block were profoundly enriched in LREE, but depleted in HREE.

A box and whisker plot is another effective way to graphically display and understand the variation in any set of data obtained from multiple resources. The REE distribution obtained in the coal samples from four boreholes of the Samaleswari block is summarized in Fig. 5. As evident from the plots, BH1 showed a maximum concentration of all REE concentrations except Ce, Nd, Sc, and Y. On the other hand, BH4 exhibited higher values of Ce, Pr, Nd, and Y. BH4 had shown wide range variation between minimum, maximum, and quartiles (Q1, Q2, and Q3) values of Ce (128.74-353.44 ppm). BH2 and BH3 showed the least variation in concentration of REEs among the four boreholes. The concentration of all the HREE and some of LREE (Sm, Eu, La, and Gd) was significantly higher in BH1. Thus, out of the four boreholes, BH1 would be an ideal choice for further investigation on REE extraction.

# Agglomerative hierarchical clustering and Pearson correlation

The correlation of REEs with major elemental oxides in the coal ash matrix has been reported previously (Franus et al. 2015; Hood et al. 2017; Wang et al. 2019; Kolker 2017). The occurrence of REE in aluminosilicate glass matrix showing strong positive correlation between Al and Si with REE was consistently found by multiple articles with respect to US coals (Kolker 2017; Stuckman et al. 2018). To delineate the correlation of REEs with the mineralogical framework in coal samples in the present study, multidimensional statistical methods, such as correlation matrix (CM) and agglomerative hierarchical clustering (AHC) analysis, were applied. The agglomerative hierarchical clustering (AHC) analysis has been performed for all the four boreholes under investigation. The dendrograms obtained by the centroid clustering method using SPSS software are presented in Fig. 6a-d. Additionally, the Pearson concentration coefficient of all the samples acquired from four boreholes was analyzed using the chemical data set of rare-earth elements (ppm) and major oxides (%). The data obtained are tabulated in Tables 9 and 10 and Table S-3a, b. A detailed analysis of the primary correlations is as follows.

#### BH1

The correlation between REE and major oxides of BH1 is presented in Fig. 6a and Table 11. All REEs except Ce, Nd,

| Table 9 Com           | prehens | ive data | of REE | (mqq) | analysi | s of the | coal san | nples ac | quired 1    | rom BF  | H1 borel      | hole of | Samales | swari co             | al bloc | 4      |        |        |        |         |         |         |         |             |
|-----------------------|---------|----------|--------|-------|---------|----------|----------|----------|-------------|---------|---------------|---------|---------|----------------------|---------|--------|--------|--------|--------|---------|---------|---------|---------|-------------|
| Sample                | A1      | A2       | A3     | A4    | A5      | A6       | A7 ,     | 48 /     | 49 <i>i</i> | A10 /   | <b>V</b> 11 / | A12 /   | A13 /   | <b>\</b> 14 <i>⊧</i> | A15 /   | A16 /  | ×17 ⊭  | v18 A  | 19 A   | 20 A    | 21 A    | 22 A    | 23 A    | 24          |
| La                    | 124.8   | 134.8    | 129.6  | 114.7 | 127.0   | 162.8    | 133.0    | 148.0    | 221.0       | 72.0 2  | 25.3 1        | 11.5    | 75.6    | 90.2 1               | 08.0    | 94.2 1 | 19.3 1 | 24.9 1 | 01.0   | 89.9 13 | 31.4 1  | 17.0 10 | 05.7 1  | 13.6        |
| Ce                    | 132.0   | 150.7    | 131.8  | 119.8 | 112.5   | 140.4    | 119.8    | 128.9    | 119.1 2     | 07.0    | 56.7          | 156.9 1 | 79.4 1  | 53.0 1               | 88.7    | 65.1 1 | 98.7 1 | 89.1 1 | 62.6 1 | 44.0 22 | 21.8 19 | 94.7 1' | 75.1 1  | 94.4        |
| Pr                    | 24.9    | 28.3     | 27.3   | 19.4  | 22.1    | 24.4     | 21.8     | 24.1     | 22.0        | 26.9    | 35.2          | 25.8    | 27.5    | 18.3                 | 22.1    | 18.9   | 24.4   | 22.0   | 19.0   | 18.1    | 28.7    | 21.8    | 20.7    | 23.4        |
| Nd                    | 51.8    | 58.5     | 51.8   | 46.5  | 44.0    | 54.7     | 47.1     | 49.6     | 46.9        | 82.5    | 59.4          | 59.4    | 68.7    | 57.3                 | 69.3    | 59.7   | 75.9   | 69.0   | 58.7   | 56.9    | 92.9    | 73.7    | 55.2    | 75.5        |
| Sm                    | 18.6    | 22.9     | 16.6   | 13.5  | 16.0    | 20.0     | 17.4     | 19.5     | 18.9        | 20.4    | 29.3          | 21.7    | 21.8    | 12.9                 | 15.0    | 13.0   | 16.9   | 15.0   | 12.3   | 12.6    | 20.1    | [4.9    | 4.0     | 16.6        |
| Eu                    | 4.1     | 4.7      | 4.3    | 2.9   | 3.6     | 4.0      | 3.5      | 3.8      | 3.2         | 4.3     | 6.0           | 3.8     | 4.4     | 2.4                  | 2.7     | 2.4    | 3.2    | 2.7    | 2.3    | 2.3     | 3.7     | 2.7     | 2.6     | 3.1         |
| Gd                    | 19.8    | 22.4     | 21.1   | 15.9  | 17.5    | 18.3     | 15.2     | 16.5     | 15.5        | 17.7    | 24.8          | 18.7    | 19.0    | 11.4                 | 13.3    | 11.5   | 15.5   | 13.7   | 11.2   | 11.3    | 1.7     | 13.3    | 12.3    | 16.1        |
| Tb                    | 2.5     | 3.4      | 3.3    | 2.4   | 2.2     | 2.8      | 2.5      | 2.9      | 2.6         | 2.9     | 4.5           | 3.2     | 3.2     | 1.8                  | 2.0     | 1.7    | 2.3    | 2.0    | 1.6    | 1.7     | 2.5     | 2.0     | 1.9     | 2.6         |
| Dy                    | 13.2    | 14.9     | 13.8   | 12.0  | 12.9    | 16.9     | 14.3     | 15.1     | 19.9        | 16.9    | 24.6          | 17.3    | 17.7    | 10.9                 | 12.1    | 10.7   | 13.9   | 12.5   | 10.1   | 10.4    | 15.0    | 12.1    | 1.3     | 18.2        |
| Но                    | 2.5     | 2.9      | 2.7    | 2.3   | 2.5     | 3.1      | 2.6      | 2.8      | 3.8         | 3.1     | 4.5           | 3.3     | 3.3     | 2.0                  | 2.2     | 1.9    | 2.5    | 2.3    | 1.8    | 1.9     | 2.6     | 2.2     | 2.1     | 3.7         |
| Er                    | 8.2     | 9.3      | 8.2    | 5.0   | 8.1     | 9.5      | 8.9      | 9.6      | 9.0         | 10.1    | 15.1          | 10.7    | 10.1    | 5.6                  | 6.2     | 5.4    | 6.8    | 6.6    | 5.0    | 5.2     | 7.4     | 6.0     | 5.7     | 11.3        |
| Tm                    | 1.0     | 1.2      | 1.1    | 1.1   | 1.2     | 1.3      | 1.2      | 1.2      | 1.7         | 1.3     | 1.8           | 1.4     | 1.4     | 0.8                  | 0.9     | 0.8    | 1.0    | 0.9    | 0.9    | 0.8     | 1.0     | 0.9     | 0.8     | 1.7         |
| Yb                    | 6.0     | 7.9      | 6.7    | 6.8   | 7.5     | 9.1      | 7.7      | 8.4      | 11.1        | 8.9     | 12.3          | 9.2     | 9.1     | 5.3                  | 5.9     | 5.2    | 6.1    | 6.0    | 4.4    | 4.8     | 6.5     | 5.6     | 5.3     | 11.4        |
| Lu                    | 1.1     | 1.5      | 1.2    | 0.9   | 1.0     | 1.2      | 1.0      | 1.1      | 1.0         | 1.2     | 1.7           | 1.3     | 1.2     | 0.8                  | 0.9     | 0.8    | 0.9    | 0.9    | 0.6    | 0.7     | 1.0     | 0.9     | 0.8     | 1.8         |
| Sc                    | 21.0    | 17.7     | 18.7   | 14.1  | 15.1    | 16.4     | 13.1     | 16.0     | 16.9        | 19.3    | 16.5          | 13.5    | 13.2    | 19.5                 | 16.1    | 18.1   | 17.1   | 20.1   | 17.5   | 12.7    | [ 6.8]  | 2.2     | 14.6    | 23.3        |
| Y                     | 39.3    | 49.2     | 39.8   | 36.5  | 33.6    | 43.2     | 39.4     | 38.8     | 36.4        | 68.9    | 44.9          | 50.4    | 44.8    | 45.9                 | 51.5    | 45.3   | 57.4   | 58.5   | 42.0   | 43.3 (  | 50.5 5  | 53.2    | 17.6    | 98.6        |
| $\Sigma^{\text{REE}}$ | 470.8   | 530.4    | 478.0  | 413.8 | 426.7   | 528.2    | 448.6 4  | 186.3 5  | 549.1 (     | 63.4 6  | 62.4 5        | 568.1 6 | 600.3 4 | 38.0 5               | 17.0 4  | 54.6 5 | 62.1 5 | 46.3 4 | 51.1 4 | 16.4 6  | 31.9 53 | 33.1 48 | 35.6 6  | 15.3        |
| LREES                 | 376.1   | 422.3    | 382.5  | 332.6 | 342.7   | 424.7    | 357.8    | 390.5 4  | 146.7 5     | 30.8 5  | 36.6 4        | 157.8 4 | 196.3 3 | 45.4 4               | 19.2    | 64.7 4 | 54.0 4 | 36.3 3 | 67.2 3 | 35.0 5  | 16.4 43 | 38.1 39 | 95.7 4  | 42.6        |
| HREES                 | 94.7    | 108.0    | 95.5   | 81.1  | 84.0    | 103.5    | 90.7     | 95.7     | 102.3       | 32.5 1  | 25.8 1        | 10.3 1  | 03.9    | 92.5                 | 97.7    | 89.8   | 08.0 1 | 6.60   | 83.9   | 81.3 1  | 15.4    | 95.0 8  | 39.9 1  | 72.7        |
| Critical              | 119.0   | 140.0    | 121.2  | 105.3 | 104.3   | 131.1    | 115.7    | 119.8    | 118.1       | 85.6 1  | 54.4 1        | 44.8 1  | 48.8 1  | 23.8 1               | 43.9    | 25.2   | 59.6 1 | 51.4 1 | 19.8 1 | 19.7 18 | 81.9 12 | 49.8 13 | 34.3 20 | <b>09.4</b> |
| Excessive             | 142.6   | 164.3    | 143.5  | 131.0 | 124.7   | 155.2    | 132.4    | 142.3    | 136.7 2     | 21.6 1  | 77.0          | 172.2   | 94.3 1  | 61.9 1               | 98.6    | 73.8 2 | 09.2 1 | 99.2 1 | 70.3 1 | 52.1 23 | 33.0 2( | )4.2 18 | 34.0 2  | 13.1        |
| Uncritical            | 209.1   | 226.1    | 213.3  | 177.5 | 197.7   | 241.9    | 200.5    | 224.2    | 294.3       | 256.2 3 | 31.0 2        | 251.1 2 | 27.1 1  | 52.3 1               | 74.5    | 55.6 1 | 93.4 1 | 95.7 1 | 61.0 1 | 44.6 2  | 17.0 17 | 79.2 10 | 57.3 1  | 92.9        |
| Coutl                 | 0.8     | 0.0      | 0.8    | 0.8   | 0.8     | 0.8      | 0.9      | 0.8      | 0.9         | 0.8     | 0.9           | 0.8     | 0.8     | 0.8                  | 0.7     | 0.7    | 0.8    | 0.8    | 0.7    | 0.8     | 0.8     | 0.7     | 0.7     | 1.0         |
| LREE/<br>HREE         | 4.0     | 3.9      | 4.0    | 4.1   | 4.1     | 4.1      | 3.9      | 4.1      | 4.4         | 4.0     | 4.3           | 4.2     | 4.8     | 3.7                  | 4.3     | 4.1    | 4.2    | 4.0    | 4.4    | 4.1     | 4.5     | 4.6     | 4.4     | 2.6         |

| Table 10 Compi | chensive d | ata of REI | 3 (ppm) an | alysis of the | e coal sam | ples acquin | ed from BH | 12 borehole | e of Samale | eswari coal | block |       |       |       |       |       |      |
|----------------|------------|------------|------------|---------------|------------|-------------|------------|-------------|-------------|-------------|-------|-------|-------|-------|-------|-------|------|
| Sample         | B1         | B2         | B3         | B4            | B5         | B6          | B7         | B8          | B9          | B10         | B11   | B12   | B13   | B14   | B15   | B16   | B17  |
| La             | 86.42      | 80.53      | 69.63      | 78.52         | 87.52      | 78.67       | 76.42      | 91.51       | 138.4       | 105.6       | 66.68 | 107.2 | 84.72 | 105.9 | 159.9 | 114.9 | 150  |
| Ce             | 150.4      | 139.2      | 121        | 133.3         | 147.2      | 135.7       | 131.4      | 164.9       | 221.9       | 181.9       | 157.3 | 181.3 | 139.6 | 182.5 | 222.1 | 187.2 | 249  |
| Pr             | 19.01      | 17.08      | 15.21      | 16.94         | 17.58      | 16.52       | 16.24      | 20.94       | 27.52       | 24.54       | 19.83 | 22.63 | 17.43 | 21.32 | 24.98 | 22.11 | 30.5 |
| Nd             | 59.52      | 53.88      | 47.09      | 53.08         | 56.4       | 52.32       | 50.22      | 62.74       | 81.6        | 69.23       | 58.75 | 67.16 | 51.5  | 65.94 | 72.05 | 69.73 | 90.8 |
| Sm             | 12.9       | 11.41      | 10.24      | 11.62         | 11.85      | 11.24       | 10.98      | 13.91       | 17.47       | 16.47       | 13.48 | 14.93 | 11.51 | 14.13 | 15.28 | 14.53 | 19.8 |
| Eu             | 1.32       | 1.2        | 1.12       | 1.24          | 1.36       | 1.22        | 1.15       | 1.57        | 1.89        | 1.7         | 1.32  | 1.59  | 1.25  | 1.65  | 1.75  | 1.69  | 2.15 |
| Gd             | 12.16      | 10.47      | 9.19       | 10.63         | 11.17      | 10.11       | 9.85       | 13.01       | 15.96       | 15.48       | 12.18 | 13.57 | 10.73 | 13.31 | 14.48 | 13.26 | 18.5 |
| Tb             | 1.47       | 1.17       | 1.09       | 1.36          | 1.46       | 1.3         | 1.25       | 1.6         | 1.89        | 1.75        | 1.37  | 1.61  | 1.25  | 1.77  | 1.65  | 1.54  | 2.1  |
| Dy             | 11.53      | 9.38       | 8.22       | 9.61          | 10.52      | 9.17        | 8.84       | 11.79       | 14.25       | 14.48       | 11.02 | 12.41 | 10.39 | 12.76 | 13.02 | 12.17 | 17   |
| Но             | 1.6        | 1.17       | 1.02       | 1.26          | 1.51       | 1.25        | 1.2        | 1.47        | 1.74        | 1.73        | 1.22  | 1.44  | 1.27  | 1.72  | 1.63  | 1.39  | 1.97 |
| Er             | 4.86       | 3.46       | 3.03       | 3.55          | 4.24       | 3.5         | 3.36       | 4.12        | 5.09        | 5.25        | 3.58  | 3.99  | 3.85  | 4.87  | 4.75  | 3.83  | 5.64 |
| Tm             | 0.87       | 0.6        | 0.52       | 0.55          | 0.69       | 0.57        | 0.55       | 0.67        | 0.87        | 0.95        | 0.6   | 0.67  | 0.62  | 0.8   | 0.78  | 0.65  | 0.95 |
| Yb             | 6.92       | 4.95       | 4.35       | 4.83          | 5.84       | 5           | 4.63       | 5.92        | 7.14        | 7.83        | 5.15  | 6.12  | 5.21  | 6.54  | 5.92  | 5.96  | 8.49 |
| Lu             | 0.8        | 0.57       | 0.5        | 0.5           | 0.64       | 0.55        | 0.5        | 0.65        | 0.82        | 0.93        | 0.55  | 0.62  | 0.57  | 0.7   | 0.65  | 0.57  | 0.9  |
| Sc             | 22.46      | 17.33      | 18.44      | 17.07         | 20.96      | 19.73       | 18.69      | 26.87       | 24.04       | 23.09       | 22.04 | 23.62 | 22.09 | 27.34 | 29.77 | 24.81 | 34.4 |
| Y              | 62.24      | 43.97      | 38.18      | 44.62         | 54.22      | 42.78       | 39.49      | 49.68       | 61.97       | 56.28       | 42.25 | 48.76 | 43.31 | 55.96 | 58.3  | 56.04 | 72.6 |
| RE             | 454.4      | 396.4      | 348.9      | 388.7         | 433.1      | 389.6       | 374.7      | 471.3       | 622.5       | 527.1       | 440.6 | 507.5 | 405.3 | 517.2 | 627   | 530.3 | 704  |
| LREEs          | 341.7      | 313.8      | 273.5      | 305.3         | 333        | 305.8       | 296.2      | 368.6       | 504.7       | 414.8       | 352.8 | 408.3 | 316.7 | 404.8 | 510.5 | 423.4 | 560  |
| HREEs          | 112.7      | 82.6       | 75.4       | 83.3          | 100.1      | 83.8        | 78.5       | 102.8       | 117.8       | 112.3       | 87.8  | 99.2  | 88.6  | 112.5 | 116.5 | 106.9 | 144  |
| Critical       | 140.9      | 113.1      | 98.7       | 113.5         | 128.2      | 110.3       | 104.3      | 131.5       | 166.7       | 148.7       | 118.3 | 135.5 | 111.5 | 142.9 | 151.5 | 145   | 190  |
| Excessive      | 160.5      | 146.5      | 127.4      | 140.4         | 155.8      | 143         | 138.3      | 173.6       | 232.4       | 193.3       | 164.8 | 190.1 | 147.3 | 192.3 | 231.1 | 195.7 | 261  |
| Uncritical     | 152.9      | 136.8      | 122.7      | 134.8         | 149.1      | 136.3       | 132.2      | 166.2       | 223.4       | 185.1       | 157.5 | 181.9 | 146.5 | 182   | 244.4 | 189.6 | 253  |
| Cour           | 0.88       | 0.77       | 0.78       | 0.81          | 0.82       | 0.77        | 0.75       | 0.76        | 0.72        | 0.77        | 0.72  | 0.71  | 0.76  | 0.74  | 0.66  | 0.74  | 0.73 |
| LREE/HREE      | 3.03       | 3.8        | 3.63       | 3.66          | 3.33       | 3.65        | 3.77       | 3.59        | 4.28        | 3.69        | 4.02  | 4.11  | 3.58  | 3.6   | 4.38  | 3.96  | 3.88 |



Fig. 3 Comparison of REE content between World Coal Ash and Coal Ash of Samaleswari Coal Block

Y, and Sc showed positive correlation and affinity with the major oxides, such as SiO<sub>2</sub>, K<sub>2</sub>O, MgO, Na<sub>2</sub>O, and SO<sub>3</sub>, but negative correlation with Al<sub>2</sub>O<sub>3</sub> and TiO<sub>2</sub>. Nevertheless, Ce, Sc, Nd, and Y (Sc being the strongest) demonstrated a strong affinity and positive concentration coefficient with Al<sub>2</sub>O<sub>3</sub> and TiO<sub>2</sub> (r=0.5-0.76) and a weak association with other oxides. The correlation between all the major oxides  $(SiO_2,$  $K_2O$ ,  $Na_2O$ , and MgO) was noticeably high (0.7 < r < 0.97). Calcium and phosphorus showed positive correlation with each other (r=0.94), supporting the abundance of apatite in the coal samples of BH1. The positive correlation of La, Ce, and Nd with TiO<sub>2</sub> (r=0.76) is suggestive of melting of monazite [(Ce, La, Nd, Th)PO<sub>4</sub>] or REE-bearing titanium mineral (titanate) resulting in dispersion of REEs in glass phase. Mafic-felsic igneous and metamorphic rocks commonly possess titanate mineral which can preserve multivalent trace elements via substitution.

#### BH2

In BH2, all REEs demonstrated positive correlation with only two oxides— $TiO_2$  and  $Al_2O_3$  with concentration coefficients ranging between (0.6 < r < 0.9) and (0.3 < r < 0.7), respectively (Fig. 6 and Table 12). The co-occurrence of REEs with clay minerals (kaolinite and illite) and titanate is well documented (Rautenbach 2021). Fe-containing aluminosilicate mineral phase showed a positive correlation with all the REEs, although weaker for some. Ca, Fe-enriched aluminosilicate glasses are well known to be enriched with REEs compared to pure aluminosilicates (Kolker et al. 2017). Of note, Al-substituted apatite ( $Ca_5(PO_4)_3$ ) showed good correlation with all the REEs.

#### BH3 and BH4

Hierarchical clustering and coefficient correlation enumerating the results obtained for borehole BH3 (Table S-4a and Fig. 6c) and BH4 (Table S-4b and Fig. 6c) demonstrated a



**Fig. 4** Concentration Coefficient (CC, average concentration of element in coal ash samples investigated vs. average of corresponding element in world hard coal ash). World hard coal ash data were taken from Wang et al. (2019)

similar pattern with respect to the association of REE and major oxides. The result clearly showed that both LREEs and HREEs were only associated with  $\text{TiO}_2$  (0.6 < r < 0.8), indicating a strong correlation with titanate mineral. Smaller correlation coefficients of HREEs in particular with terrigenous elements ( $\text{SiO}_2$ ,  $\text{Al}_2\text{O}_3$ ,  $\text{Fe}_2\text{O}_3$ ) confirm their comparatively stronger association with the organic matter in coal.

#### Mineralogical characterization

The mineralogical composition of coal ash is dependent on the geochemistry and properties of feed coal and also on ash temperature. Coal ash is highly enriched with REEs; however, on contrary, REE-bearing minerals are less common in coal ash than coal. Such contradictions not only make the analysis of REEs with coal ash matrix highly complicated, but it also leads to a range of possible alternatives to trace phase retention. Thus, comparison and crossvalidation of the results obtained from various analytical methodologies, such as XRD, XRF, and EPMA (shown in subsequent section), were desirable to provide an overall scenario of REE association in the selected coal block. Profiling of the major oxides present in all the coal ash samples is presented in Tables 6 and 7 and Table S-2a, b. Typically, Indian coal ashes are characterized by relatively higher concentrations of SiO2 and Al2O3 followed by contents of  $Fe_2O_3$ , which tallies well with our results. These elements are mainly brought in by quartz, clay minerals, and pyrites (Zhao et al. 2013).

Owing to its geological origin, Indian coal seams are sandwiched in between sandstone and shale deposited in the form of rhythmic layers (Singh et al. 2013), resulting in higher percentage of quartz in Indian coals (Bandopadhyay and Chatterjee 2006; Mukherjee and Srivastava 2006). Silica (SiO<sub>2</sub>), which is present in ~60% concentration in our **Fig. 5** Box-and-whisker plots of rare-earth element (ppm) in coal ash samples of BH1, BH2, BH4, and BH3. The box expressed Q1 (lower side of the box)—25% quartile, Q3 (upper side of the box)—75% quartile



#### Fig. 5 (continued)



coal ash samples (Tables 6 and 7a-d), is primarily present as quartz rather than clay mineral. XRD studies revealed the presence of higher proportions of quartz, and smaller proportions of anatase (TiO<sub>2</sub>), apatite ((Ca<sub>5</sub>(PO<sub>4</sub>)<sub>3</sub>), and hematite (Fe<sub>2</sub>O<sub>3</sub>) (Fig. 7a-d) in these samples. XRF analysis demonstrated that 23–41% of the coal ash composition comprises Al<sub>2</sub>O<sub>3</sub> (Tables 6 and 7); nonetheless, their corresponding peaks were absent in X-ray diffractograms. It was concluded to be due to conversion of kaolinite ((Al<sub>2</sub>Si<sub>2</sub>O<sub>5</sub>(OH)<sub>4</sub>)) and illite (K<sub>1.5</sub>Al<sub>4</sub>(Si<sub>6.5</sub>Al<sub>1.5</sub>) O<sub>20</sub>(OH)<sub>4</sub>) to metakaolinite and mullite at elevated temperatures (Varga 2007; Rautenbach 2021).

#### EPMA study

Minerals and poorly crystalline mineroloids are highly probable sites for rare-earth enrichment. Although delineation of exact association of REEs with coal ash minerals is an arduous task, some possible associations with major oxides can be detected to portray the variations in affinity. According to literature precedence, the majority of REEs were either dispersed throughout the glass phase (AlSiK matrix) or as trace phases partitioning into the glass phase or as independent particles outside the glass matrix (Hower et al. 2013; Hood et al. 2017; Kolker et al. 2017). The EPMA point analysis results of some of the selected coal ash samples (Table 13, Figs. 8, 9, 10 and 11), supported by their correlation pattern (Fig. 7a-d), demonstrated the possible presence of REEbearing titanium mineral (e.g., titanite [CaTiSiO<sub>5</sub>] (King et al. 2012)) in these boreholes. It was thus speculated that the REEs were dispersed in the glass phase as Ti co-existed with Si and to a large extent with Ca in all the coal ash samples. Interestingly, in BH4, prominent correlation was observed between Ti and Ce which has literature precedence (King et al. 2012). The co-localization of Ce, La, and Nd, but not Sm, in the aluminosilicate matrix was considered as direct evidence of dispersion of LREE enriched monazite into the glass phase of our chosen coal block, supporting previous hypothesis (Mohanty et al. 2003; Stuckman 2018; Hood et al. 2017; Kolker et al. 2017). Incorporation of Fe into the glass phase resulting in fine intergrowths of Feoxides during coal combustion has literature precedence (Yang et al. 2014). The proportions of Fe-oxides were highly variable throughout the four boreholes; however, they were found to be closely associated with REE-bearing glass phase



Fig. 6 Hierarchical cluster of analytical data of rare-earth elements and major elements of coal ash samples

particularly in BH1 and BH2, supported by both EPMA (Table 13) and XRF results (Tables 6 and 7).

Further, a qualitative analysis of REE enrichment for two boreholes, BH1 and BH4, is shown in Figs. 12 and 13, respectively. The results obtained by SEM-EDAX analysis were in fair agreement with the conclusions drawn from EPMA and XRD analysis. It reinstated that REEs in the chosen boreholes were present in an encapsulated manner in the Fe–Al–Si matrix of coal ash samples.

#### Provenance and paleodepositional settings

The oxides' form of inorganic constituents provides useful information about the inorganic matter source (provenance), paleoclimate, paleotectonic, and paleodepositional setting of the region (Ward 2002; Dai et al. 2016b; Zhao et al. 2017). The high concentrations of SiO<sub>2</sub> and Al<sub>2</sub>O<sub>3</sub> suggest the existence of a substantial amount of aluminosilicate minerals in Samaleswari coals (Tables 6 and 7 and Tables S4a,b). For

| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | $ \begin{array}{ ccccccccccccccccccccccccccccccccccc$  | $ \begin{array}{ ccccccccccccccccccccccccccccccccccc$   | La<br>1<br>- 0.14<br>0.69<br>- 0.08<br>0.83<br>0.79<br>0.79<br>0.79<br>0.79<br>0.87<br>0.87<br>0.87<br>0.83 | Ce<br>1<br>0.20<br>0.98<br>0.03<br>0.03<br>- 0.11<br>- 0.11<br>0.01<br>- 0.01<br>- 0.03<br>- 0.04<br>- 0.10 | Pr<br>1<br>0.27<br>0.93<br>0.90<br>0.90<br>0.90<br>0.90<br>0.74<br>0.78<br>0.74<br>0.78<br>0.74<br>0.63 | Nd<br>1<br>0.10<br>- 0.03<br>- 0.07<br>0.07<br>0.03<br>0.01<br>- 0.05<br>- 0.05 | Sm<br>1<br>0.93<br>0.87<br>0.93<br>0.88<br>0.88<br>0.88<br>0.84<br>0.90<br>0.76 | Eu<br>1<br>0.96<br>0.95<br>0.76<br>0.76<br>0.76<br>0.69<br>0.69 | Gd<br>1<br>0.93<br>0.73<br>0.66<br>0.65 | Tb<br>1<br>0.86<br>0.85<br>0.89<br>0.79 | Dy<br>1<br>0.99<br>0.93<br>0.94                                       | Ho<br>1<br>0.93<br>0.97 | Er 1<br>0.91<br>0.91 | Tm<br>1<br>0.99                                     | - XP                                      | Ē                             | S                |
|--|--|---|---|---|---|---|---|---|---|---|---|-------------------------|----------------------|---|---|-------------------------------|------------------|
| $ \begin{array}{                                     $   |  |   | •   | - 0.02<br>0.27  | 0.72<br>0.15  | 0.03<br>0.28  | 0.74<br>0.02  | 0.76<br>0.08  | 0.79<br>0.13                            | 0.83<br>0.03                            | 0.78<br>0.10  | 0.84<br>0.16            | $0.88 \\ 0.14$       | 0.84<br>0.12  | 0.83<br>0.11                              | $\frac{1}{0.32}$              | -                |
| 3 $0.58$ $-0.22$ $0.49$ $-0.27$ $-0.41$ $-0.46$ $-0.32$ $-0.14$ $-0.15$ $-0.19$ $-0.16$ $-0.10$ $0.20$ 7 $0.28$ $-0.29$ $0.27$ $-0.34$ $-0.44$ $-0.48$ $-0.57$ $-0.58$ $-0.61$ $-0.57$ $-0.02$ 9 $0.24$ $-0.60$ $0.34$ $0.50$ $0.56$ $0.45$ $0.29$ $0.23$ $0.38$ $0.40$ $0.34$ $-0.61$ 9 $0.76$ $-0.12$ $0.67$ $-0.22$ $-0.38$ $-0.43$ $-0.43$ $-0.12$ $-0.16$ $0.34$ $0.24$ $-0.12$ $0.67$ $-0.22$ $0.39$ $0.40$ $0.24$ $0.10$ $0.07$ $-0.18$ $-0.19$ $-0.12$ $-0.12$ $0.57$ $-0.25$ $0.35$ $0.39$ $0.40$ $0.24$ $0.10$ $0.07$ $0.16$ $0.19$ $-0.19$ $-0.14$ $0.36$ $0.25$ $0.47$ $0.25$ $0.25$ $0.26$ $0.29$ $0.24$ $0.10$ $-0.19$ $-0.14$ $0.36$ $0.50$ $0.50$ $0.62$ $0.47$ $0.22$ $0.26$ $0.29$ $0.29$ $0.20$ $-0.14$ $0.36$ $0.25$ $0.36$ $0.52$ $0.47$ $0.22$ $0.29$ $0.31$ $0.11$ $-0.12$ $-0.14$ $0.36$ $0.26$ $0.23$ $0.40$ $0.24$ $0.26$ $0.29$ $0.29$ $0.29$ $0.29$ $-0.14$ $0.36$ $0.26$ $0.25$ $0.47$ $0.22$ $0.26$ $0.29$ $0.26$ $0.29$   | 3 $0.58$ $-0.22$ $0.49$ $-0.27$ $-0.41$ $-0.46$ $-0.32$ $-0.14$ $-0.13$ $-0.15$ $-0.19$ $-0.16$ $-0.10$ $0.20$ 7 $0.28$ $0.24$ $-0.34$ $0.54$ $0.56$ $0.56$ $0.48$ $-0.32$ $0.33$ $0.38$ $0.40$ $0.34$ $-0.01$ 9 $0.76$ $-0.12$ $0.67$ $-0.22$ $-0.38$ $0.47$ $0.20$ $0.56$ $0.45$ $0.24$ $0.11$ $-0.16$ $-0.18$ $-0.19$ $-0.13$ $-0.10$ 9 $0.76$ $-0.12$ $0.67$ $-0.22$ $-0.38$ $0.40$ $0.24$ $0.24$ $0.24$ $-0.10$ 9 $0.76$ $-0.12$ $0.67$ $0.35$ $0.36$ $0.52$ $0.47$ $0.27$ $0.29$ $0.31$ $0.40$ $0.24$ $-0.13$ 9 $0.76$ $-0.12$ $0.35$ $0.36$ $0.52$ $0.47$ $0.27$ $0.26$ $0.29$ $0.31$ $0.29$ $0.20$ $-0.041$ $0.36$ $0.36$ $0.52$ $0.47$ $0.27$ $0.26$ $0.24$ $0.11$ $-0.16$ $-0.13$ $0.24$ $-0.12$ $-0.041$ $0.36$ $0.36$ $0.52$ $0.62$ $0.47$ $0.27$ $0.26$ $0.24$ $0.26$ $0.24$ $0.26$ $-0.041$ $0.36$ $0.26$ $0.52$ $0.52$ $0.24$ $0.26$ $0.24$ $0.26$ $0.26$ $0.24$ $0.26$ $-0.041$ $0.36$ $0.26$ $0.26$ $0.24$ $0.24$ $0.26$ $0.24$ $0.$  | 3 $0.58$ $-0.22$ $0.41$ $-0.45$ $-0.41$ $-0.13$ $-0.15$ $-0.16$ $-0.10$ $0.27$ 7 $0.28$ $-0.23$ $0.24$ $-0.43$ $-0.48$ $-0.57$ $-0.57$ $-0.60$ $0.34$ $-0.61$ $-0.57$ $-0.67$ $-0.67$ $-0.61$ $0.57$ $-0.61$ $0.57$ $-0.67$ <t< td=""><td>-</td><td>0.74 - 0.54</td><td>0.15<br/>0.27</td><td>0.74<br/>- 0.49</td><td>0.04<br/>0.33</td><td>-0.05</td><td>-0.04</td><td>0.02<br/>0.45</td><td>0.20<br/>0.35</td><td>0.25<br/>0.38</td><td>0.23<br/>0.36</td><td>0.26<br/>0.44</td><td>0.24<br/>0.43</td><td><math>0.41 \\ 0.35</math></td><td>0.53 - 0.15</td></t<> | -   | 0.74 - 0.54   | 0.15<br>0.27  | 0.74<br>- 0.49  | 0.04<br>0.33  | -0.05   | -0.04                                   | 0.02<br>0.45                            | 0.20<br>0.35  | 0.25<br>0.38            | 0.23<br>0.36         | 0.26<br>0.44  | 0.24<br>0.43                              | $0.41 \\ 0.35$                | 0.53 - 0.15      |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | $ \begin{array}{cccccccccccccccccccccccccccccccccccc$   | 33  | 0.58  | - 0.22  | 0.49  | - 0.27  | - 0.41  | - 0.46                                  | - 0.32                                  | -0.14   | - 0.13                  | - 0.15               | - 0.19  | - 0.16                                    | - 0.10                        | 0.20             |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  |  | $ \begin{array}{cccccccccccccccccccccccccccccccccccc$   | 47  | 0.28<br>- 0.68  | -0.29   | 0.27<br>- 0.60  | - 0.34<br>0.34  | - 0.43<br>0.50  | - 0.48<br>0.56                          | - 0.48<br>0.45                          | -0.50   | - 0.57<br>0.32          | -0.53                | - 0.58<br>0.38                                      | - 0.61<br>0.40                            | -0.57                         | - 0.02<br>- 0.10 |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$   |  |   | 29  | 0.76  | - 0.12  | 0.67  | - 0.22  | - 0.38  | - 0.43                                  | - 0.31                                  | - 0.11  | - 0.12                  | - 0.16               | - 0.18  | - 0.19                                    | - 0.13                        | 0.20             |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$   |  | $ \begin{array}{cccccccccccccccccccccccccccccccccccc$   |   | - 0.12  | 0.35  | -0.01   | 0.35  | 0.39  | 0.40                                    | 0.24                                    | 0.10  | 0.07                    | 0.15                 | 0.00  | -0.01                                     | 0.10                          | - 0.08           |
| $ \begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$  | $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$   | $ \begin{array}{cccccccccccccccccccccccccccccccccccc$   |   | - 0.65  | 0.25  | - 0.55  | 0.35  | 0.50  | 0.52                                    | 0.42                                    | 0.25  | 0.26                    | 0.29                 | 0.31  | 0.33                                      | 0.24                          | - 0.12           |
| $ \begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$  | $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | $ \begin{array}{cccccccccccccccccccccccccccccccccccc$   |   | - 0.41  | 0.36  | - 0.35  | 0.36  | 0.52  | 0.62                                    | 0.47                                    | 0.32  | 0.38                    | 0.37                 | 0.40  | 0.42                                      | 0.50                          | 0.06             |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | $ \begin{array}{cccccccccccccccccccccccccccccccccccc$   |   | - 0.09<br>- 0.44  | 0.40<br>0.36  | 0.01<br>- 0 36  | 0.33  | 0.40  | 0.44<br>0.53                            | 0.27                                    | 0.05  | 0.03<br>0.24            | 0.11                 | - 0.06<br>0 24                                      | - 0.09<br>0.26                            | 0.12<br>0 39                  | - 0.01<br>- 0.03 |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | $ \begin{array}{cccccccccccccccccccccccccccccccccccc$   | 42  | 0.57  | - 0.43  | 0.45  | - 0.49  | - 0.64  | - 0.70                                  | - 0.54                                  | - 0.32  | - 0.34<br>- 0.34        | - 0.39               | - 0.35  | - 0.37                                    | - 0.41                        | 0.04             |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$   |  |   | 33  | 0.58  | - 0.19  | 0.50  | - 0.25  | - 0.38  | - 0.43                                  | -0.30                                   | - 0.13  | - 0.13                  | -0.14                | - 0.19  | -0.17                                     | -0.10                         | 0.20             |
| -0.25  0.20  -0.27  0.25  0.33  0.36  0.40  0.45  0.52  0.46  0.54  0.57  0.51  0.01 | $  -0.25  0.20  -0.27  0.25  0.33  0.36  0.40  0.45  0.52  0.46  0.54  0.57  0.51  0.01 \\  \mathrm{sio}_2  \mathrm{Al}_2\mathrm{O}_3  \mathrm{Fe}_2\mathrm{O}_3  \mathrm{K}_2\mathrm{O}  \mathrm{TiO}_2  \mathrm{CaO}  \mathrm{MgO}  \mathrm{Na}_2\mathrm{O}  \mathrm{P}_2\mathrm{O}_5  \mathrm{SiO}_3 + \mathrm{Al}_2\mathrm{O}_3 + \mathrm{Fe}_2\mathrm{O}_3  \mathrm{Al}_2\mathrm{O}_3 + \mathrm{P}_2\mathrm{O}_5 + \mathrm{CaO}  \mathrm{MgO} + \mathrm{Al}_2\mathrm{O}_3 + \mathrm{SiO}_2 + \mathrm{Al}_2\mathrm{O}_3 + \mathrm{Fe}_2\mathrm{O}_5  \mathrm{Al}_2\mathrm{O}_3 + \mathrm{P}_2\mathrm{O}_5 + \mathrm{CaO}  \mathrm{MgO} + \mathrm{Al}_2\mathrm{O}_3 + \mathrm{SiO}_2 + \mathrm{Al}_2\mathrm{O}_3 + \mathrm{Fe}_2\mathrm{O}_3 + \mathrm{Al}_2\mathrm{O}_3 + \mathrm{P}_2\mathrm{O}_5 + \mathrm{CaO}  \mathrm{MgO} + \mathrm{Al}_2\mathrm{O}_3 + \mathrm{SiO}_2 + \mathrm{Al}_2\mathrm{O}_3 + Al$ |   |   | -0.14   | 0.17  | -0.17   | 0.21  | 0.26  | 0.29                                    | 0.35                                    | 0.44  | 0.50                    | 0.44                 | 0.52  | 0.54                                      | 0.48                          | 0.03             |
|  |  |   | SiO <sub>2</sub>  | -0.25<br>Al <sub>2</sub> O <sub>3</sub> Fe  | 0.20<br>203 K20   | - 0.27<br>TiO <sub>2</sub> CaO  | 0.25<br>MgO   | 0.33<br>Na <sub>2</sub> O P <sub>2</sub> O <sub>5</sub>         | 0.36<br>SO <sub>3</sub> Si              | 0.40<br>$O_2 + AI_2O_3 + ]$             | 0.45<br>Fe <sub>2</sub> O <sub>3</sub> Al <sub>2</sub> O <sub>3</sub> | 0.52<br>$(+P_2O_5+Cat)$ | 0.46<br>MgO+,        | $\frac{0.54}{\text{Al}_2\text{O}_3 + \text{SiO}_2}$ | $\frac{0.57}{\text{SiO}_2 + \text{Al}_2}$ | 0.51<br>0.51<br>$3_3 + K_2 O$ | 0.01             |
|  |  |   |   |   |   |   |   |   |   |   |   |                         |                      |   |   |                               |                  |
|  |  |   |   |   |   |   |   |   |   |   |   |                         |                      |   |   |                               |                  |
|  |  |   |   |   |   |   |   |   |   |   |   |                         |                      |   |   |                               |                  |

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| (continued) |  |
|-------------|--|
| Table 11    |  |

|   | $SiO_2 + Al_2O_3 + K_2O_3$  |    |    |    |    |    |    |    |    |    |   |                  |           |           |        |                  |        |        |         |          |        |                             |                          |                         | 1                          |
|---|-----------------------------|----|----|----|----|----|----|----|----|----|---|------------------|-----------|-----------|--------|------------------|--------|--------|---------|----------|--------|-----------------------------|--------------------------|-------------------------|----------------------------|
|   | $MgO + Al_2O_3 + SiO_2$     |    |    |    |    |    |    |    |    |    |   |                  |           |           |        |                  |        |        |         |          |        |                             |                          | 1                       | 66.0                       |
|   | $Al_2O_3 + P_2O_5 + CaO$    |    |    |    |    |    |    |    |    |    |   |                  |           |           |        |                  |        |        |         |          |        |                             | 1                        | - 0.07                  | - 0.20                     |
|   | $SiO_2 + Al_2O_3 + Fe_2O_3$ |    |    |    |    |    |    |    |    |    |   |                  |           |           |        |                  |        |        |         |          |        | 1                           | 0.78                     | - 0.09                  | - 0.23                     |
|   | $SO_3$                      |    |    |    |    |    |    |    |    |    |   |                  |           |           |        |                  |        |        |         |          | 1      | - 0.78                      | - 0.58                   | -0.13                   | - 0.01                     |
|   | $P_2O_5$                    |    |    |    |    |    |    |    |    |    |   |                  |           |           |        |                  |        |        |         | 1        | 0.31   | - 0.42                      | - 0.13                   | - 0.33                  | - 0.30                     |
|   | $Na_2O$                     |    |    |    |    |    |    |    |    |    |   |                  |           |           |        |                  |        |        | 1       | 0.09     | 0.47   | - 0.76                      | - 0.59                   | 0.52                    | 0.62                       |
|   | MgO                         |    |    |    |    |    |    |    |    |    |   |                  |           |           |        |                  |        | 1      | 0.70    | 0.11     | 0.70   | - 0.92                      | - 0.86                   | 0.10                    | 0.25                       |
|   | CaO                         |    |    |    |    |    |    |    |    |    |   |                  |           |           |        |                  | 1      | 0.21   | 0.14    | 0.94     | 0.32   | -0.50                       | - 0.17                   | -0.30                   | - 0.26                     |
| i | $TiO_2$                     |    |    |    |    |    |    |    |    |    |   |                  |           |           |        | -                | - 0.23 | - 0.94 | - 0.64  | - 0.17   | - 0.69 | 0.86                        | 0.94                     | - 0.05                  | - 0.20                     |
|   | $K_2O$                      |    |    |    |    |    |    |    |    |    |   |                  |           |           | -      | - 0.92           | 0.13   | 0.97   | 0.81    | 0.04     | 0.67   | - 0.91                      | - 0.85                   | 0.29                    | 0.44                       |
|   | $Fe_2O_3$                   |    |    |    |    |    |    |    |    |    |   |                  |           | 1         | - 0.51 | 0.27             | 0.12   | - 0.33 | - 0.69  | 0.17     | - 0.09 | 0.36                        | 0.26                     | - 0.96                  | - 0.99                     |
|   | $Al_2O_3$                   |    |    |    |    |    |    |    |    |    |   |                  | 1         | 0.24      | - 0.85 | 0.94             | - 0.26 | - 0.86 | - 0.59  | - 0.22   | - 0.60 | 0.81                        | 1.00                     | - 0.03                  | - 0.17                     |
|   | $SiO_2$                     |    |    |    |    |    |    |    |    |    |   | 1                | - 0.82    | - 0.74    | 0.83   | - 0.77           | 0.04   | 0.73   | 0.76    | - 0.01   | 0.39   | - 0.68                      | - 0.83                   | 0.60                    | 0.70                       |
|   | Y                           |    |    |    |    |    |    |    |    |    | 1 | - 0.31           | 0.53      | - 0.09    | - 0.42 | 0.60             | - 0.23 | - 0.48 | - 0.15  | - 0.24   | - 0.26 | 0.39                        | 0.52                     | 0.19                    | 0.11                       |
|   |                             | Gd | Tb | Dy | Ho | Er | Tm | Yb | Lu | Sc | Y | SiO <sub>2</sub> | $Al_2O_3$ | $Fe_2O_3$ | $K_2O$ | TiO <sub>2</sub> | CaO    | MgO    | $Na_2O$ | $P_2O_5$ | $SO_3$ | $SiO_2 + Al_2O_3 + Fe_2O_3$ | $AI_2O_3 + P_2O_5 + CaO$ | $MgO + Al_2O_3 + SiO_2$ | $SiO_2 + Al_2O_3 + K_2O_3$ |

|                             | coemciei | It between rai                                  | e-earth elei                     | ments and 1 | major oxiuc | S (BH2) |        |         |          |        |                |                 |                    |                     |        |
|-----------------------------|----------|---|----------------------------------|-------------|-------------|---------|--------|---------|----------|--------|----------------|-----------------|--------------------|---------------------|--------|
|                             | La       | Ce  | Pr                               | Nd          | Sm          | Eu      | Gd     | Tb      | Dy       | Но     | Er             | Tm              | Yb                 | Lu                  | Sc     |
| La                          | 1        |   |                                  |             |             |         |        |         |          |        |                |                 |                    |                     |        |
| Ce                          | 0.97     | 1   |                                  |             |             |         |        |         |          |        |                |                 |                    |                     |        |
| Pr                          | 0.92     | 0.98  | 1                                |             |             |         |        |         |          |        |                |                 |                    |                     |        |
| Nd                          | 0.91     | 0.98  | 0.99                             | 1           |             |         |        |         |          |        |                |                 |                    |                     |        |
| Sm                          | 0.87     | 0.95  | 0.99                             | 0.98        | 1           |         |        |         |          |        |                |                 |                    |                     |        |
| Eu                          | 0.91     | 0.97  | 0.98                             | 0.98        | 0.97        | 1       |        |         |          |        |                |                 |                    |                     |        |
| Gd                          | 0.87     | 0.95  | 0.99                             | 0.98        | 1.00        | 0.97    | 1      |         |          |        |                |                 |                    |                     |        |
| Tb                          | 0.82     | 0.92  | 0.94                             | 0.95        | 0.95        | 0.96    | 0.96   | 1       |          |        |                |                 |                    |                     |        |
| Dy                          | 0.85     | 0.93  | 0.97                             | 0.96        | 0.98        | 0.96    | 0.99   | 0.96    | 1        |        |                |                 |                    |                     |        |
| Но                          | 0.77     | 0.85  | 0.86                             | 0.87        | 0.87        | 0.89    | 06.0   | 0.95    | 0.93     | 1      |                |                 |                    |                     |        |
| Er                          | 0.74     | 0.81  | 0.84                             | 0.84        | 0.85        | 0.84    | 0.88   | 0.91    | 0.91     | 0.98   | 1              |                 |                    |                     |        |
| Tm                          | 0.68     | 0.76  | 0.81                             | 0.80        | 0.83        | 0.79    | 0.86   | 0.85    | 0.89     | 0.94   | 0.98           | 1               |                    |                     |        |
| Yb                          | 0.68     | 0.80  | 0.86                             | 0.86        | 0.89        | 0.86    | 0.91   | 0.91    | 0.94     | 0.95   | 96.0           | 0.97            | 1                  |                     |        |
| Lu                          | 0.59     | 0.70  | 0.78                             | 0.76        | 0.81        | 0.75    | 0.84   | 0.82    | 0.86     | 0.90   | 0.95           | 0.98            | 0.97               | 1                   |        |
| Sc                          | 0.84     | 0.88  | 0.84                             | 0.84        | 0.82        | 0.88    | 0.84   | 0.84    | 0.85     | 0.81   | 0.76           | 0.69            | 0.73               | 0.62                | 1      |
| Υ                           | 0.78     | 0.84  | 0.84                             | 0.88        | 0.84        | 0.86    | 0.87   | 0.88    | 0.88     | 0.94   | 0.93           | 06.0            | 0.92               | 0.85                | 0.78   |
| $SiO_2$                     | - 0.23   | - 0.24  | - 0.23                           | - 0.19      | - 0.22      | - 0.21  | - 0.22 | - 0.18  | - 0.27   | - 0.12 | - 0.12         | - 0.06          | - 0.11             | 0.00                | - 0.28 |
| $Al_2O_3$                   | 0.58     | 0.67  | 0.67                             | 0.68        | 0.69        | 0.66    | 0.66   | 0.61    | 0.66     | 0.45   | 0.39           | 0.36            | 0.49               | 0.31                | 0.63   |
| ${\rm Fe_2O_3}$             | - 0.08   | - 0.15  | -0.17                            | - 0.24      | -0.20       | - 0.19  | -0.18  | - 0.22  | -0.12    | - 0.15 | -0.10          | - 0.13          | - 0.19             | -0.18               | - 0.02 |
| $K_2O$                      | - 0.69   | - 0.68  | - 0.62                           | - 0.60      | - 0.59      | - 0.63  | -0.60  | - 0.55  | - 0.63   | - 0.49 | - 0.46         | -0.40           | - 0.44             | -0.30               | - 0.69 |
| $TiO_2$                     | 0.80     | 0.86  | 0.83                             | 0.83        | 0.83        | 0.88    | 0.84   | 0.83    | 0.86     | 0.75   | 0.69           | 0.62            | 0.71               | 0.56                | 0.87   |
| CaO                         | - 0.07   | - 0.09  | - 0.08                           | - 0.06      | - 0.09      | - 0.12  | - 0.09 | - 0.07  | -0.10    | 0.00   | 0.02           | 0.07            | 0.02               | 0.05                | - 0.25 |
| MgO                         | - 0.73   | - 0.76  | -0.71                            | - 0.72      | -0.71       | - 0.73  | -0.70  | - 0.66  | - 0.72   | - 0.59 | - 0.52         | - 0.48          | -0.57              | -0.41               | - 0.72 |
| $Na_2O$                     | -0.60    | - 0.53  | - 0.44                           | -0.41       | - 0.38      | - 0.46  | -0.41  | - 0.39  | - 0.45   | - 0.39 | - 0.39         | - 0.30          | -0.27              | -0.17               | - 0.55 |
| $P_2O_5$                    | 0.25     | 0.21  | 0.17                             | 0.18        | 0.13        | 0.15    | 0.11   | 0.03    | 0.07     | - 0.05 | - 0.08         | - 0.05          | - 0.03             | - 0.08              | - 0.03 |
| $SO_3$                      | - 0.36   | - 0.36  | - 0.29                           | -0.30       | -0.27       | - 0.34  | - 0.24 | - 0.18  | - 0.21   | - 0.03 | 0.07           | 0.13            | 0.00               | 0.12                | - 0.35 |
| $SiO_2 + Al_2O_3 + Fe_2O_3$ | 0.45     | 0.46  | 0.41                             | 0.39        | 0.39        | 0.42    | 0.39   | 0.32    | 0.42     | 0.31   | 0.31           | 0.32            | 0.33               | 0.27                | 0.56   |
| $Al_2O_3 + P_2O_5 + CaO$    | 0.58     | 0.67  | 0.67                             | 0.68        | 0.68        | 0.66    | 0.65   | 0.61    | 0.65     | 0.45   | 0.39           | 0.35            | 0.49               | 0.31                | 0.61   |
|                             | Y        | SiO <sub>2</sub> Al <sub>2</sub> O <sub>3</sub> | ; Fe <sub>2</sub> O <sub>3</sub> | $K_2O$      | $TiO_2$     | CaO     | MgO    | $Na_2O$ | $P_2O_5$ | $SO_3$ | $SiO_2 + Al_2$ | $O_3 + Fe_2O_3$ | $Al_2O_3 + P_2O_3$ | 0 <sub>5</sub> +CaO |        |
| La                          |          |   |                                  |             |             |         |        |         |          |        |                |                 |                    |                     |        |
| Ce                          |          |   |                                  |             |             |         |        |         |          |        |                |                 |                    |                     |        |
| Pr                          |          |   |                                  |             |             |         |        |         |          |        |                |                 |                    |                     |        |
| Nd                          |          |   |                                  |             |             |         |        |         |          |        |                |                 |                    |                     |        |
| Sm                          |          |   |                                  |             |             |         |        |         |          |        |                |                 |                    |                     |        |
| Eu                          |          |   |                                  |             |             |         |        |         |          |        |                |                 |                    |                     |        |

| (continued) |
|-------------|
| Table 12    |

| $_{2}O_{3} + Fe_{2}O_{3} Al_{2}O_{3} + P_{2}O_{5} + CaO$ |    |    |    |    |    |    |    |    |    |   |         |           |           |             |                  |             |             |             |           |             |                                     | 1                      |  |
|--|----|----|----|----|----|----|----|----|----|---|---------|-----------|-----------|-------------|------------------|-------------|-------------|-------------|-----------|-------------|-------------------------------------|------------------------|--|
| $SiO_2 + AI$   | -  |    |    |    |    |    |    |    |    |   |         |           |           |             |                  |             |             |             |           |             | 1                                   | 09.0                   |  |
| $SO_3$   |    |    |    |    |    |    |    |    |    |   |         |           |           |             |                  |             |             |             |           | 1           | - 0.58                              | - 0.47                 |  |
| $P_2O_5$   |    |    |    |    |    |    |    |    |    |   |         |           |           |             |                  |             |             |             | 1         | - 0.24      | 0.17                                | 0.40                   |  |
| $Na_2O$  |    |    |    |    |    |    |    |    |    |   |         |           |           |             |                  |             |             | 1           | - 0.28    | 0.30        | - 0.52                              | - 0.54                 |  |
| MgO  |    |    |    |    |    |    |    |    |    |   |         |           |           |             |                  |             | 1           | 0.65        | -0.31     | 0.63        | - 0.73                              | - 0.84                 |  |
| CaO  |    |    |    |    |    |    |    |    |    |   |         |           |           |             |                  | 1           | 0.26        | 0.22        | 0.49      | 0.54        | -0.30                               | - 0.09                 |  |
| $TiO_2$  |    |    |    |    |    |    |    |    |    |   |         |           |           |             | 1                | - 0.24      | - 0.89      | -0.70       | 0.21      | - 0.51      | 0.60                                | 0.79                   |  |
| $K_2O$   |    |    |    |    |    |    |    |    |    |   |         |           |           | 1           | - 0.86           | 0.17        | 0.88        | 0.86        | - 0.34    | 0.50        | - 0.75                              | -0.81                  |  |
| $\mathrm{Fe}_2\mathrm{O}_3$                              |    |    |    |    |    |    |    |    |    |   |         |           | 1         | - 0.44      | 0.10             | -0.05       | 0.00        | - 0.59      | -0.01     | 0.07        | 0.26                                | 0.07                   |  |
| SiO <sub>2</sub> Al <sub>2</sub> O <sub>3</sub>          |    |    |    |    |    |    |    |    |    |   | 1       | -0.621    | -0.800.07 | 0.74 - 0.81 | -0.500.80        | 0.07 - 0.15 | 0.42 - 0.85 | 0.74 - 0.55 | -0.200.35 | 0.14 - 0.49 | -0.380.61                           | -0.621.00              |  |
| Υ  |    |    |    |    |    |    |    |    |    | 1 | - 0.03  | 0.43      | -0.25     | - 0.43      | 0.68             | 0.08        | -0.57       | -0.33       | 0.00      | -0.01       | Fe <sub>2</sub> O <sub>3</sub> 0.27 | CaO 0.43               |  |
|  | Gd | Tb | Dy | Но | Er | Tm | Yb | Lu | Sc | Y | $SiO_2$ | $Al_2O_3$ | $Fe_2O_3$ | $K_2O$      | TiO <sub>2</sub> | CaO         | MgO         | $Na_2O$     | $P_2O_5$  | $SO_3$      | $SiO_2 + Al_2O_3 + l$               | $Al_2O_3 + P_2O_5 + i$ |  |

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**Fig.7** XRD analysis of representative coal ash samples from each borehole of Samaleswari coal block: **a** BH1 (sample A21), **b** BH2 (sample B9), **c** BH3 (sample C12), and **d** BH4 (sample D20) (Q—Quartz, H—Haemetite, A—Apatite, and An—Anatase)

most clastic sedimentary rocks, including coal deposits, the ratio of Al<sub>2</sub>O<sub>3</sub> and TiO<sub>2</sub> has been used efficiently as a provenance indicator in different basins (Hayashi et al. 1997; Dai et al. 2015a, b, 2017). In clastic sedimentary rock derived from mafic, intermediate, and felsic dominant sedimentary source regions, the Al<sub>2</sub>O<sub>3</sub>/TiO<sub>2</sub> ratios were found to be in the range of 3-8, 8-21, and 21-70, respectively (Hayashi et al. 1997). All the four borehole coal samples of the Samaleswari coal block have Al<sub>2</sub>O<sub>3</sub>/TiO<sub>2</sub> ratio greater than 21, indicating that the sediment source in the basin was felsic (Fig. 14). The low contents of  $TiO_2$  and MgO in the coals of Samaleswari block also indicate the depletion of Ti and Mg and less mafic minerals, inferring a felsic provenance (Zhang et al. 2020). Moreover, slightly low and negative Eu anomalies (see section 5.1) further support that felsic rock formations have influenced the sediments of the region. The positive correlation of TiO<sub>2</sub> and Al<sub>2</sub>O<sub>3</sub> with  $\sum$ REE indicates that most of Samaleswari coal's REEs mainly occurred in clay minerals. While a negative correlation of  $\sum$ REE with Fe<sub>2</sub>O<sub>3</sub> entails REEs in Samaleswari coal may also occur in phosphate and pyrites.

Apart from organic indices, the inorganic constituents have also been used to know the coal-forming environment (Qin et al. 2018). The major oxide ratio  $[M=(Fe_2O_3+CaO+MgO)/(SiO_2+Al_2O_3)]$  in coals is one of the significant parameters for studying peat-forming conditions. This ratio discriminates between marine and terrestrial environments during peat deposition. The major oxide ratio (M) value of more than 0.23 entails marine depositional conditions, while less than 0.23 indicates a terrestrial depositional environment (Qin et al. 2018). The M values (less than 0.23) in Samaleswari coal indicate that these coals formed in a terrestrial environment (Table 14). The major oxide concentrations in all four boreholes are more or less similar; therefore, the average values of  $SiO_2$ and  $(Al_2O_3+K_2O+Na_2O)$  were plotted on the diagram proposed by Suttner and Dutta (1986), further suggesting that the coal of these boreholes formed under a semi-arid condition (Fig. 15). Moreover, Ce anomalies can give the information about the paleodepositional condition and used as redox indicator. Ce anomaly < 0.78 indicates oxidation condition, and > 0.78 reflects anoxic condition. In the boreholes of Samaleswari coal blocks, the Ce anomaly

Table 13 EPMA point analysis data of the selected coal ash samples acquired from all the four boreholes of Samaleswari coal block

| Boreholes name | Point no. | Fe    | K     | Na   | Mg   | Al    | Si    | Ca   | Ti   | Р    | La   | Ce   | Pr   | Nd   | Sm   |
|----------------|-----------|-------|-------|------|------|-------|-------|------|------|------|------|------|------|------|------|
| CMISW-021      | 1         | 5.12  | 4.32  | 0.19 | 0.95 | 29.68 | 58.3  | 0.27 | 0.65 | nd   | 0.35 | nd   | 0.18 | nd   | nd   |
|                | 2         | 1.95  | 1.32  | 0.09 | 0.72 | 12.38 | 79.96 | 0.4  | 0.41 | nd   | nd   | nd   | 0.73 | 0.23 | 1.82 |
|                | 3         | 5.78  | 4.93  | 0.21 | 1.95 | 31.15 | 47.41 | 2.37 | 3.47 | nd   | 0.10 | 1.07 | 1.17 | 0.14 | 0.26 |
|                | 4         | 6.52  | 4.16  | 0.78 | 1.45 | 32.13 | 50.34 | 1.71 | 2.13 | nd   | 0.73 | 0.04 | nd   | nd   | nd   |
| CMISW-025      | 1         | 7.58  | 6.9   | 0.6  | 0.9  | 32.96 | 48.78 | 0.31 | 0.73 | nd   | nd   | 0.14 | 0.93 | 0.19 | nd   |
|                | 2         | 38.72 | 3.28  | 1.02 | 1.12 | 23.02 | 31.09 | nd   | 0.83 | nd   | 0.68 | 0.23 | nd   | nd   | nd   |
|                | 3         | 7.32  | 10.22 | 0.37 | 0.69 | 32.58 | 45.75 | 0.72 | 0.68 | nd   | 0.20 | 0.29 | 0.28 | nd   | 0.90 |
|                | 4         | 7.12  | 10.78 | 0.49 | 1.23 | 30.75 | 46.13 | nd   | 1.51 | nd   | 1.00 | 0.44 | nd   | 0.56 | nd   |
|                | 5         | 4.41  | 2.91  | 0.24 | 0.74 | 33.65 | 55.05 | 0.26 | 2.03 | nd   | nd   | nd   | 0.34 | 0.37 | nd   |
|                | 6         | 1.43  | 0.8   | 0.32 | 0.55 | 12.74 | 80.04 | 0.45 | 1.74 | nd   | nd   | nd   | nd   | 0.36 | 1.57 |
|                | 7         | 3.23  | 2.33  | 0.22 | 0.62 | 20.31 | 65.12 | 1.16 | 2.24 | nd   | 1.31 | 1.48 | nd   | 1.04 | 0.95 |
| CMISW-27       | 1         | 2.44  | 15.32 | 0.14 | 0.61 | 30.99 | 45.52 | 0.06 | 2.71 | nd   | nd   | 0.57 | 0.61 | nd   | 1.01 |
|                | 2         | 2.68  | 9.86  | 0.90 | 0.85 | 33.21 | 48.45 | 0.41 | 2.54 | nd   | nd   | 0.74 | 0.36 | nd   | nd   |
|                | 3         | 2.37  | 1.53  | nd   | 0.65 | 35.92 | 50.92 | 0.62 | 6.31 | nd   | nd   | 1.11 | 0.57 | nd   | nd   |
|                | 4         | 3.44  | 1.11  | nd   | 0.43 | 23.67 | 64.68 | 0.66 | 3.54 | nd   | nd   | nd   | 1.05 | 0.63 | 0.77 |
| CMISW-08       | 1         | 4.49  | 0.74  | 0.39 | 0.34 | 23.81 | 67.33 | 0.39 | 1.11 | nd   | nd   | 0.75 | 0.66 | nd   | nd   |
|                | 2         | 3.3   | 0.58  | 0.2  | 0.38 | 36.21 | 53.36 | 0.28 | 1.31 | 0.3  | 0.6  | 0.14 | 0.58 | 1.46 | 1.29 |
|                | 3         | 4.77  | 1.00  | 0.6  | 0.6  | 33.89 | 50.48 | 0.39 | 6.77 | 0.21 | nd   | 0.10 | 0.76 | 0.43 | nd   |
|                | 4         | 11.25 | 0.49  | 0.74 | 0.71 | 30.48 | 47.08 | 0.45 | 6.68 | 0.07 | 0.09 | 1.09 | 0.87 | nd   | nd   |

is  $^{>}$  0.78, except few samples on BH 1in upper sections, indicating that these coal blocks were deposited in anoxic condition.

# Implications of exploration of REEs in Samaleswari coal block

Research on exploration and recovery of REE from coal ash is one of the most sought after area, although its augmentation to commercial scale still needs to be determined. Particularly, in Indian scenario, the need to uncover potential REE sources is even more critical knowing the geographical abundance of REEs in Southern Asia. In the present study, two boreholes were found to be potentially rich source of appreciable concentration of La, Ce, Nd, and Y. In particular, the higher concentrations of REEs in BH1 were found to be associated to apatite ore. This means that the isolation of these valuables would be essentially a three-step process: (a) leaching using sulphuric acid, (b) solvent extraction, and (c) precipitation (Battsengel et al. 2018). In BH2, the association of REEs was concluded to be with either monazite or bastnaesite ore. The presence of Yttrium in both boreholes (on an average 48.7 ppm in BH1 and 39.5 ppm in BH2, Tables 9 and 10) indicates the presence of xenotime in coal ash which could be conjoined with the positive correlation with phosphorus in the chosen boreholes (Tables 6 and 7). The lower enrichment of HREE is reflective of the overlap between monazite/bastnaesite

and its aluminosilicate host, thus making it economically un-exploitable. With an understanding of the variations in chemical associations, in future, the main focus would be to design efficient and economic strategies to extract REEs from the two enriched boreholes of Samaleswari coal block.

### **Future work**

The present work demonstrated that the two boreholes BH1 and BH2 of Samaleswari coal block are enriched with REEs. The optimization of extraction of these valuables is thus the next crucial step. Therefore, we are planning to optimize the conditions for leaching out these valuables from the coal ash samples and characterize them. Subsequently, optimization of sequential leaching will be performed to delineate the association of HREE and LREE with the inorganic and organic matter the coal samples of this area.

# Conclusion

The knowledge of distribution and association of REE in coal samples is necessary to develop efficient strategies for their extraction and utilization. Based on the geochemical and mineralogical studies of the coals from the



# **EPMA results**

Fig. 8 EMPA point analysis results of BH1

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Samaleswari coal block, IB valley, Odisha, India, the following conclusions may be drawn:

• The chemical composition of these coals was concluded to be sub-bituminous in rank with a high average ash yield of 49.58% and a low average fixed carbon concentration of 23.46%.

• Eu anomalies are slightly low and negative with high LREE/HREE ratio indicating felsic influence in sedimentation. The ratio of Al<sub>2</sub>O<sub>3</sub>/TiO<sub>2</sub>>21 further sup-



Fig. 9 EMPA point analysis results of BH2



Fig. 10 EMPA point analysis results of BH3

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Fig. 11 EMPA point analysis results of BH4

ports that the sediment source in the basin was felsic in nature.

- The (La/Yb)<sub>N</sub> ratio greater than 1 showed that samples are primarily LREE which are inorganically bound in particular belonged to phosphate and carbonate rocks.
- The concentration of critical rare-earth elements (100– 300 ppm) and the C<sub>outl</sub> (0.7–1.0) indicates that the coal seam from the Samaleswari coal block can be used as a promising source of REE elements.



# **SEM Micrographs**



Fig. 12 SEM micrograph of representative sample of BH1



| Element | Wt %  | At %  |
|---------|-------|-------|
| O K     | 39.33 | 58.36 |
| FK      | 01.49 | 01.86 |
| NiL     | 00.00 | 00.00 |
| MgK     | 02.49 | 02.43 |
| AlK     | 12.89 | 11.34 |
| SiK     | 19.59 | 16.56 |
| YL      | 01.79 | 00.48 |
| P K     | 00.88 | 00.67 |
| S K     | 02.04 | 01.51 |
| KK      | 00.80 | 00.48 |
| ScK     | 00.63 | 00.33 |
| TiK     | 04.56 | 02.26 |
| LaL     | 02.80 | 00.48 |
| CeL     | 03.03 | 00.51 |
| NdL     | 02.12 | 00.35 |
| FeK     | 05.55 | 02.36 |



Fig. 12 (continued)

- The concentrations of all HREEs and some LREEs (Sm, Eu, La, and Gd) were found to be significantly higher in BH1, which possessed higher concentration of apatite.
- The presence of titanate mineral bearing REEs was conclusively proven for all four boreholes.
- EPMA point analysis and SEM-EDAX analysis further corroborated the co-existence of REEs in the alumino-silicate glass phase with significant Fe inclusions.
- The major oxide ratio (M<sup>4</sup>0.23) value more than entails the terrestrial depositional environment in the basin dur-

**Fig. 13** SEM micrograph of representative sample of BH2



#### KV:15.00 TILT: 0.00 TAKE-OFF:42.26 AMPT:12.80 DETECTOR TYPE : SDD APOLLO 40 RESOLUTION :131.42



| Element | Wt %  | At %  |
|---------|-------|-------|
| O K     | 36.29 | 54.63 |
| FK      | 04.03 | 05.11 |
| MgK     | 00.77 | 00.76 |
| AlK     | 14.42 | 12.87 |
| SiK     | 16.59 | 14.23 |
| Y L     | 00.00 | 00.00 |
| P K     | 01.08 | 00.84 |
| S K     | 00.00 | 00.00 |
| KK      | 00.00 | 00.00 |
| ScK     | 00.00 | 00.00 |
| TiK     | 13.83 | 06.95 |
| LaL     | 01.78 | 00.31 |
| CeL     | 02.04 | 00.35 |
| NdL     | 00.00 | 00.00 |
| FeK     | 09.17 | 03.96 |



| Element | Wt %  | At %  |
|---------|-------|-------|
| O K     | 37.07 | 54.97 |
| FK      | 03.51 | 04.38 |
| MgK     | 00.35 | 00.34 |
| AIK     | 17.29 | 15.20 |
| SiK     | 18.63 | 15.73 |
| YL      | 00.00 | 00.00 |
| P K     | 01.88 | 01.44 |
| S K     | 01.31 | 00.97 |
| KK      | 00.64 | 00.39 |
| ScK     | 00.19 | 00.10 |
| TiK     | 04.51 | 02.24 |
| LaL     | 02.98 | 00.51 |
| CeL     | 03.15 | 00.53 |
| NdL     | 01.60 | 00.26 |
| FeK     | 06.88 | 02.92 |

At %

55.43

02.95

00.61

14.66 17.77

00.17

02.06

00.82

00.24

00.31

Wt %

37.67

02.38

00.63

16.80

21.20

00.65

02.71

01.12

00.39

00.60

Element

0 K

FK

MgK

AlK

SiK YL

P K S K

KK



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| ScK     | 00.60 | 00.31 |
|---------|-------|-------|
| TiK     | 02.59 | 01.27 |
| LaL     | 02.71 | 00.46 |
| CeL     | 01.14 | 00.19 |
| NdL     | 03.51 | 00.57 |
| FeK     | 05.90 | 02.49 |
| Flamont | W/+ % | At %  |
| O K     | 27.95 | 48.14 |
| FK      | 02.76 | 04.01 |
| MgK     | 01.46 | 01.66 |
| AIK     | 13.11 | 13.38 |
| SiK     | 14.56 | 14.29 |
| Y L     | 00.57 | 00.18 |
| P K     | 03.52 | 03.13 |
| S K     | 01.28 | 01.10 |
| KK      | 00.47 | 00.33 |
| ScK     | 01.03 | 00.63 |
| TiK     | 03.82 | 02.20 |
| LaL     | 05.83 | 01.16 |
| CeL     | 04.22 | 00.83 |
| NdL     | 02.04 | 00.39 |
| FeK     | 17.38 | 08.57 |



Fig. 14 Plot of TiO<sub>2</sub> versus Al<sub>2</sub>O<sub>3</sub> form average concentration of four bore holes of Samaleswari coals (Imchen et al 2014)



Fig. 15 Plot of SiO<sub>2</sub> versus  $(Al_2O_3 + K_2O + Na_2O)$  showing paleoclimate condition during sedimentation (Suttner and Dutta 1986)

 Table 14 The major oxide ratio for studying peat-forming conditions

| Table 14         The major oxide ratio for studying peat-forming conditions |        |  | Table 14 (continued) |                      |                                       |
|---|--------|--|----------------------|----------------------|---------------------------------------|
| Borehole  | Sample | $\frac{\text{Fe}_2\text{O}_3 + \text{CaO} + \text{MgO}}{\text{SiO}_2 + \text{Al}_2\text{O}_3}$ | Borehole             | Sample               | $Fe_2O_3 + CaO + MgO/SiO_2 + Al_2O_3$ |
| BH-1  | A1     | 0.06   |                      | C7                   | 0.06                                  |
|   | A2     | 0.10   |                      | C8                   | 0.05                                  |
|   | A3     | 0.04   |                      | C0                   | 0.05                                  |
|   | A4     | 0.05   |                      | C9                   | 0.05                                  |
|   | A5     | 0.06   |                      | C10                  | 0.06                                  |
|   | A6     | 0.05   |                      | C11                  | 0.04                                  |
|   | A7     | 0.08   |                      | C12                  | 0.04                                  |
|   | A8     | 0.06   |                      | C13                  | 0.07                                  |
|   | A9     | 0.05   |                      | 616                  | 0.07                                  |
|   | A10    | 0.06   |                      | C14                  | 0.06                                  |
|   | A11    | 0.05   |                      | C15                  | 0.04                                  |
|   | A12    | 0.06   |                      | C16                  | 0.04                                  |
|   | A13    | 0.07   |                      | C17                  | 0.08                                  |
|   | A14    | 0.14   |                      | C19                  | 0.00                                  |
|   | A15    | 0.09   |                      | C18                  | 0.08                                  |
|   | A16    | 0.09   |                      | C19                  | 0.06                                  |
|   | A17    | 0.05   |                      | C20                  | 0.10                                  |
|   | A18    | 0.06   |                      | C21                  | 0.09                                  |
|   | A19    | 0.10   |                      | COO                  | 0.06                                  |
|   | A20    | 0.14   |                      | C22                  | 0.00                                  |
|   | A21    | 0.18   |                      | C23                  | 0.04                                  |
|   | A22    | 0.07   |                      | C24                  | 0.07                                  |
|   | A24    | 0.07   | BH-4                 | D1                   | 0.07                                  |
| BH-2  | B1     | 0.02   |                      | D2                   | 0.05                                  |
|   | B2     | 0.05   |                      | D3                   | 0.06                                  |
|   | B3     | 0.05   |                      | D4                   | 0.05                                  |
|   | B4     | 0.07   |                      | D5                   | 0.04                                  |
|   | B5     | 0.04   |                      | D6                   | 0.11                                  |
|   | B6     | 0.04   |                      | D7                   | 0.05                                  |
|   | B7     | 0.11   |                      | D8                   | 0.07                                  |
|   | B8     | 0.05   |                      | D9                   | 0.06                                  |
|   | В9     | 0.06   |                      | D10                  | 0.06                                  |
|   | B10    | 0.07   |                      | D11                  | 0.06                                  |
|   | B11    | 0.07   |                      | D12                  | 0.07                                  |
|   | B12    | 0.07   |                      | DI3                  | 0.09                                  |
|   | B13    | 0.33   |                      | D14                  | 0.11                                  |
|   | B14    | 0.10   |                      | DIS                  | 0.12                                  |
|   | B15    | 0.09   |                      | D16                  | 0.06                                  |
|   | B16    | 0.06   |                      | D17                  | 0.07                                  |
|   | B17    | 0.02   |                      | D10                  | 0.07                                  |
| BH-3  | C1     | 0.05   |                      | D19<br>D20           | 0.03                                  |
|   | C2     | 0.06   |                      |                      |                                       |
|   | C3     | 0.09   |                      |                      |                                       |
|   | C4     | 0.10   |                      |                      |                                       |
|   | C5     | 0.09   | ing coal for         | rmation and the majo | or oxide plot suggests that           |

0.04

ing coal formation and the major oxide plot suggests that the coal of these boreholes formed under a semi-arid condition.

C6

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**Data availability statement** The data could be made available upon request to the authors.

#### Declarations

Competing interests The authors declare no competing interests.

**Conflict of interest** All authors declare that they have no conflict of interest.

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