# **ORIGINAL ARTICLE**



# **Improved chaotic bat algorithm and its application in multi**‑**objective operation of cascade reservoirs considering diferent ecological fow requirements**

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## **Abstract**

With growing concerns on renewable energy and environment, the multi-objective operation (MOO), which considering the economic benefts and ecological benefts, becomes an important optimization problem. To handle this problem, a new multi-objective optimization approach named improved chaotic bat algorithm (ICBA) is proposed in this paper. In ICBA, chaos theory is used to generate initial population and update pulse emission rate to improve population diversity. The selfadaptive loudness update mechanism is designed to control the convergence speed according to the iterations process. Furthermore, the Montana Method with seasonal variation is proposed to calculate downstream ecological fow. The feasibility and efectiveness of the proposed ICBA method are demonstrated by the simulations of the Qingjiang cascade reservoirs in diferent hydrological years. Four scenarios are set up to compare the power generation results and the downstream ecological fow satisfaction rate under diferent ecological fow requirements. The results show that average annual operation schemes obtained by the ICBA can meet the minimum and suitable ecological fow requirements. Compared to the scenario 1 (optimization goal only consider the power generation requirement), the scenario 4 (optimization goal consider both power generation and ideal ecological fow requirement) proposed in this paper can improve the satisfaction rate of ideal ecological flow requirement, and has little influence on the average annual power generation. As compared with other several algorithms, the ICBA can obtain better operation results in diferent hydrological years and provide a new efective tool for designing reasonable operation schemes of cascade reservoirs.

**Keywords** Bat algorithm · Chaos · Multi-objective operation · Self-adaptive

# **Introduction**

Reservoirs alter the spatial and temporal distribution of runoff to serve multiple functions, such as flood control, water resources allocation, hydropower generation, navigation and recreation, which play an important role in promoting social and economic development (Chang et al. [2017](#page-14-0)). The conventional practice of reservoir operation mainly focuses on the maximization of social-economic benefts while ignoring

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the downstream ecosystem requirements, and serious damaging the structure and function of river ecosystems (Xia et al. [2008](#page-14-1)). The goal with maximizing satisfaction rate of downstream ecological flow is to minimize the ecological lack water volume in hydropower generation, which requires enough water discharge. At the same time, maximum power generation is the basic requirement of hydropower station (Hu et al. [2019](#page-14-2)), which mainly focuses on more water volume for power generation in flood season and high water level in non-food season (Zhang et al. [2013](#page-14-3)). However, the high water level in the non-food season will lead to a decrease in outfow. Ecological goals and power generation goals are contradictory and difficult to optimize at the same time. Therefore, the multi-objective operation (MOO) is becoming an important optimization problem.

At present, many researchers solve the MOO problem using evolutionary and metaheuristic algorithms, such as genetic algorithm (GA) (Chen et al. [2016](#page-14-4); Dai et al. [2016](#page-14-5); Liu et al. [2019](#page-14-6)), artifcial bee colony (ABC) (Choong et al. [2017](#page-14-7)), shufing frog leaping algorithm (SFLA) (Yang et al. [2018](#page-14-8)), shark machine learning algorithm (SMLA) (Allawi et al. [2018](#page-13-0)) and harmony search (HS) (Bashiri-Atrabi et al. [2015](#page-14-9)). The bat algorithm (BA) is a new metaheuristic algorithm based on the echolocation features of microbats (Yang [2010\)](#page-14-10). The applications of BA demonstrated that it was easy to implement and can deal with highly nonlinear problems efficiently (Yang  $2010$ ; Yang and Gandomi  $2012$ ). Case studies included micro-grid operation management (Bahmani-Firouzi and Azizipanah-Abarghooee [2014](#page-13-1)), interconnected power system (Sathya and Mohamed Thameem Ansari [2015](#page-14-12)) and dam-reservoir operation (Ethteram et al. [2018](#page-14-13)), and others. Original versions of bat algorithm have been frequently modifed or hybridized to improve performance. To improve the convergence rate and precision of bat algorithm, Xie et al. ([2013\)](#page-14-14) put forward an improved bat algorithm based on diferential operator and Levy fights trajectory (DLBA). The results showed that the proposed DLBA is feasible and effective. Mirjalili et al.  $(2013)$  $(2013)$  proposed a binary bat algorithm (BBA), which has artifcial bats navigating and hunting in binary search spaces by changing their positions. They calculated dispersion relation of photonic crystal waveguide, and compared the BA with binary particle swarm optimization (BPSO) and genetic algorithm (GA). They recommended applying the BBA to diferent practical application. The hybrid self-adaptive bat algorithm (HSABA) was proposed by combined bat algorithm with diferent evolution (DE) in literature (Fister et al. [2014\)](#page-14-16). They compared this algorithm with some algorithms, and concluded that the HSABA performs better than other comparison algorithms. However, there are some limitation in BA and proposed algorithms: (1) the initial population randomly generated in BA may be highly repetitive and concentrated in a limited space, which will lead to the decrease of population diversity. (2) The rapid change of loudness *A* may cause BA to trap into local optima. (3) The most popular penalty method for dealing with equality constraints of reservoir operation problem is difficult to satisfy complex multi-objective scheduling of cascade reservoirs.

In this paper, to realize win–win goal of economic benefts and ecological benefts of cascade reservoirs, a multiobjective operation model is established to consider power generation and diferent ecological fow requirements. The new method named the Montana Method with seasonal variation is proposed to calculated diferent ecological fows. Moreover, to solve the multi-objective operation model, an improved chaotic bat algorithm (ICBA) is proposed in this paper. The main improvements of the proposed ICBA method are as follows: (1) Chaos is a common non-linear phenomenon with certainty, ergodicity and the stochastic property (Alatas and Akin [2009](#page-13-2)). Recently, chaotic sequences have been adopted instead of random sequences.

Somewhat good results have been shown in many applications (Aydin et al. [2010;](#page-13-3) Wong et al. [2005\)](#page-14-17). To improve the population diversity, the population initialization based on chaos theory was adopted. (2) The pulse emission rate was generated based on Sinusoidal map and varied to a chaotic number between 0 and 1. (3) The self-adaptive loudness update mechanism was designed to control the convergence speed according to the iterations process. (4) The constraint handling method with constraint transformation was used when solve the MOO problem.

The rest of the paper is organized as follows. The mathematical modeling of the MOO problem is introduced in "[Mathematical modeling of the MOO problem](#page-1-0)". The standard Bat Algorithm is described in "[Overview of standard bat](#page-3-0) [algorithm](#page-3-0)". "[Improved chaotic bat algorithm \(ICBA\)](#page-4-0)" presents the proposed improved chaotic bat algorithm (ICBA) for solving the MOO problem in detail. "[Case study](#page-5-0)" reports the application in Qingjiang River and discusses the application results. Finally, "[Conclusions](#page-13-4)" outlines the conclusions of this work.

# <span id="page-1-0"></span>**Mathematical modeling of the MOO problem**

# **Objective function**

In this paper, multi-objective operation mainly considers economic benefts and ecological benefts, which are refected in the total power generation of cascade power stations and the downstream ecological flow requirement. Therefore, the mathematical modeling of the multi-objective operation need meet two objective functions:

① Maximizing power generation:

$$
\max f_1 = \max \sum_{i=1}^{I} \sum_{k=1}^{K} N_{i,k} \times t_{i,k},
$$
 (1)

$$
N_{i,k} = P_i \times Q_{i,k}^{\text{LEC}} \times \overline{H}_{i,k},\tag{2}
$$

where  $f_1(kWh)$  is the total power generation of cascade reservoirs during the scheduling period; *I* is the number of reservoirs; *K* is the number of periods;  $N_{ik}$  is the power output of *i*th reservoir at the *k*th period (kW);  $t_{i,k}$  is the operational time of the *i*th reservoir at the *k*th period (h);  $P_i$  is the synthetic output coefficient of *i*th reservoir;  $Q_{i,k}^{\text{LEC}}$  is the generation flow of *i*th reservoir at the *k*th period (m<sup>3</sup>/s);  $\overline{H}_{i,k}$  is the average water head of *i*th reservoir at the *k*th period (m).

② Maximizing satisfaction rate of downstream ecological flow:

$$
\max f_2 = \max \sum_{i=1}^{I} \alpha_i \sum_{k=1}^{K} \beta_k \times G_{i,k},
$$
 (3)

$$
G_{i,k} = \begin{cases} \frac{Q_{i,k}^{\text{OUT}}}{Q_{i,k}^{\text{DE}}} \times 100\% & \text{if } Q_{i,k}^{\text{OUT}} < Q_{i,k}^{\text{DE}} \\ 100\% & \text{if } Q_{i,k}^{\text{OUT}} \ge Q_{i,k}^{\text{DE}} \end{cases}
$$
(4)

where  $f_2$  is the total satisfaction rate of downstream ecological flow during the scheduling period; *I* is the number of reservoirs; *K* is the number of periods;  $\alpha_i$  is the weight coefficient assigned to *i*th reservoir,  $\sum_{i=1}^{I} \alpha_i = 1$ ;  $\beta_k$  is the weight coefficient assigned to *k*th period,  $\sum_{k=1}^{K} \beta_k = 1$ ;  $G_{i,k}$  is the satisfaction rate of downstream ecological flow of *i*th reservoir at the *k*th period;  $Q_{i,k}^{\text{OUT}}$ is the outflow of *i*th reservoir at the *k*th period  $(m^3/s)$ ;  $Q_{i,k}^{\text{DE}}$  is downstream ecological flow of *i*th reservoir at the *k*th period  $(m^3/s)$ .

Two optimization objectives are competitive with each other, and it is generally impossible to obtain optimal solution at the same time. The magnitude order of two objective functions is diferent. Therefore, this paper adopts the Technique for Order Preference by Similarity to Ideal Solution (TOPSIS) method (Srdjevic et al. [2004](#page-14-18)) to transform the multi-objective function into a single-objective function, so that the optimization results can be as close as possible to their respective ideal points. The converted objective function is given as follows:

$$
f(f_1, f_2) = \min \sqrt{\left(\frac{f_1^{\max} - f}{f_1^{\max}}\right)^2 + \left(\frac{f_2^{\max} - f}{f_2^{\max}}\right)^2},
$$
 (5)

where  $f(f_1, f_2)$  is holistic objective that contains both power generation objectives and ecological objectives;  $f_1^{\text{max}}$  is the maximum total power generation of cascade reservoirs when the objective function  $\mathbb O$  is considered only;  $f_2^{\max}$  is the maximum total satisfaction rate of downstream ecological flow when the objective function ② is considered only.

#### **Constraints**

Objective functions are subject to following constraints:

Reservoir storage continuity constraint:

$$
SV_{i,k} = SV_{i,k-1} + (Q_{i,k}^{IN} - Q_{i,k}^{OUT}) \times t_{i,k},
$$
 (6)

where SV*i*,*k* and SV*i*,*k*−1 are reservoir storage of *i*th reservoir at the *k*th and  $(k-1)$ th period, respectively  $(m^3)$ ;  $Q_{i,k}^{\text{IN}}$  and  $Q_{i,k}^{\text{OUT}}$  are inflow and outflow of *i*th reservoir at the *k*th period, respectively  $(m^3/s)$ .

② Reservoir water level constraint:

<span id="page-2-0"></span>
$$
Z_{i,k}^{\min} \le Z_{i,k} \le Z_{i,k}^{\max},\tag{7}
$$

where  $Z_{i,k}$  is the reservoir water level of *i*th reservoir at the *k*th period (m);  $Z_{i,k}^{\min}$  and  $Z_{i,k}^{\max}$  are minimum and maximum reservoir water level of *i*th reservoir at the *k*th period, respectively (m).

③ Reservoir release constraint:

$$
Q_{i,k}^{\text{OUT,min}} \le Q_{i,k}^{\text{OUT}} \le Q_{i,k}^{\text{OUT,max}},\tag{8}
$$

where  $Q_{i,k}^{\text{OUT,min}}$  and  $Q_{i,k}^{\text{OUT,max}}$  are minimum and maximum reservoir outfow of *i*th reservoir at the *k*th period, respectively  $(m^3/s)$ .

④ Power generation constraint:

$$
N_{i,k}^{\min} \le N_{i,k} \le N_{i,k}^{\max},\tag{9}
$$

where  $N_{i,k}^{\min}$  and  $N_{i,k}^{\max}$  are minimum and maximum reservoir power output of *i*th reservoir at the *k*th period, respectively (kW).

⑤ Reservoir storage constraint:

$$
SV_{i,k}^{\min} \leq SV_{i,k} \leq SV_{i,k}^{\max},\tag{10}
$$

where  $SV_{i,k}^{\min}$  and  $SV_{i,k}^{\max}$  are minimum and maximum reservoir storage of *i*th reservoir at the *k*th period, respectively  $(m^3)$ .

## **Downstream ecological fow acquisition**

There are more than 200 methodologies for calculating environmental fow. They could be classifed into hydrological, hydraulic rating, habitat simulation and holistic methodologies. Hydrological methods constituted the highest proportion of methodologies recorded (Tharme [2003\)](#page-14-19), with the Montana Method (Tennant [1976](#page-14-20)) being the most popular. Grading standard of the condition of river ecosystem in Montana Method is shown in Table [1.](#page-3-1)

The downstream ecological fow at the *k*th period can be obtained according to the base fow standard recommended by Montana Method:

$$
\begin{cases}\n\Phi_{i,k}^{\min} = Q_i^{\text{avg}} \theta_{i,k}^{\min} \\
\Phi_{i,k}^{\text{sur}} = Q_i^{\text{avg}} \theta_{i,k}^{\text{sui}} \\
\Phi_{i,k}^{\text{ide}} = Q_i^{\text{avg}} \theta_{i,k}^{\text{ide}}\n\end{cases} \tag{11}
$$

where  $\Phi_{i,k}^{\min}, \Phi_{i,k}^{\text{sui}}$  and  $\Phi_{i,k}^{\text{ide}}$  are minimum, suitable and ideal downstream ecological fow of *i*th reservoir at the *k*th period obtained by Montana Method, respectively;  $Q_i^{\text{avg}}$  is the average annual downstream flow of *i*th reservoir;  $\theta_{i,k}^{\min}, \theta_{i,k}^{\text{sui}}$  and  $\theta_{i,k}^{\text{ide}}$  are requirement index of minimum, suitable and ideal downstream ecological fow of *i*th reservoir at the *k*th period,

Description of flows	Recommended base flow regimes (Percent of average annual flow)					
	Oct. ~ Mar $(\%)$	Apr. $\sim$ Sep $(\%)$				
Maximum	200	200				
Optimal range	$60 - 100$	$60 - 100$				
Outstanding	40	60				
Excellent	30	50				
Good	20	40				
Fair or degrading	10	30				
Poor or minimum	10	10				
Severe degradation	< 10	< 10				

<span id="page-3-1"></span>**Table 1** Grading standard of the condition of river ecosystem in Montana Method

respectively. Based on base fow regimes in Table [1,](#page-3-1) assuming that the  $\theta_{i,k}^{\min}$ ,  $\theta_{i,k}^{\sup}$  and  $\theta_{i,k}^{\text{ide}}$  are 10%, 30% and 65% in October to March, and 30%, 50% and 75% in April to September, respectively.

The original Montana Method used the average annual flow as reference. The calculation results are susceptible to extreme flow (extreme wet or extreme dry) events. Montana Method focuses on the fow inter-annual change of fow, weakening the gap between river fow in wet season and dry season. If the original Montana Method is used to calculate the ideal downstream ecological fow in this paper, the ideal downstream ecological flow may be much higher than average flow in some dry months. When the river fow season changes greatly in 1 year, the river fow may not be able meet suitable and ideal ecological fow requirements in many months. It is more necessary to consider seasonal changes of rivers and select more realistic ecological fow at this time. Therefore, the Montana Method with seasonal variation is presented in this paper. The specifc expression is given as follows.

$$
\begin{cases}\nQ_{i,k}^{\text{DE,min}} = \lambda_1^{\min} \Phi_{i,k}^{\min} + \lambda_2^{\min} \xi_{i,k} \Phi_{i,k}^{\min} \\
Q_{i,k}^{\text{DE,sui}} = \lambda_1^{\text{sui}} \Phi_{i,k}^{\text{sui}} + \lambda_2^{\text{sui}} \xi_{i,k} \Phi_{i,k}^{\text{sui}} \\
Q_{i,k}^{\text{DE,ide}} = \lambda_1^{\text{ide}} \Phi_{i,k}^{\text{ide}} + \lambda_2^{\text{ide}} \xi_{i,k} \Phi_{i,k}^{\text{ide}}\n\end{cases} \tag{12}
$$

$$
\xi_{i,k} = \frac{Q_{i,k}^{\text{avg}}}{Q_i^{\text{avg}}},\tag{13}
$$

where  $Q_{i,k}^{\text{DE,min}}$ ,  $Q_{i,k}^{\text{DE,sui}}$  and  $Q_{i,k}^{\text{DE,ide}}$  are minimum, suitable and ideal downstream ecological fow when considering seasonal changes of *i*th reservoir at the *k*th period, respectively;  $\Phi_{i,k}^{\min}$ ,  $\Phi_{i,k}^{\text{sui}}$  and  $\Phi_{i,k}^{\text{ide}}$  are minimum, suitable and ideal downstream ecological fow of *i*th reservoir at the *k*th period obtained by Montana Method, respectively;  $\lambda_1$  and  $\lambda_2$  are weight coefficient,  $\lambda_1 + \lambda_2 = 1$ ;  $\lambda_1^{\min}$  and  $\lambda_2^{\min}$  are assumed as 0.7 and 0.3, respectively;  $\lambda_1^{\text{sui}}$  and  $\lambda_2^{\text{sui}}$  are assumed as 0.5 and 0.5,

respectively;  $\lambda_1^{\text{ide}}$  and  $\lambda_2^{\text{ide}}$  are assumed as 0.3 and 0.7, respectively;  $Q_{i,k}^{\text{avg}}$  is the average downstream flow of *i*th reservoir at the *k*th period;  $Q_i^{\text{avg}}$  is the average annual downstream flow of *i*th reservoir.

# <span id="page-3-0"></span>**Overview of standard bat algorithm**

The bat algorithm is a new heuristic algorithm based on the echolocation behavior of microbats. To simplify and facilitate application, the algorithm adopts following idealized rules:

- ① All bats apply echolocation to sense distance, and they always "know" the diference between prey and obstacles in some magical way.
- ② Bats fy randomly with speed *V* and a fxed frequency  $F_{min}$  to search for prey at position *X*, varying frequency *F* and loudness *A*. They can automatically accommodate the frequency and adjust pulse emission rate *r* according to their proximity to the target.
- ③ Assume the loudness changing from maximum to minimum.

In the BA, position and speed update can be obtained from Eqs.  $(15)$  $(15)$  and  $(16)$  $(16)$ .

<span id="page-3-2"></span>
$$
F_j = F_{\min} + \left(F_{\max} - F_{\min}\right) \times \beta,\tag{14}
$$

$$
V_j^g = V_j^{g-1} + \left(X_j^{g-1} - X_*\right) \times F_j,\tag{15}
$$

<span id="page-3-3"></span>
$$
X_j^g = X_j^{g-1} + V_j^g,\tag{16}
$$

where  $j$  is the number of bats;  $g$  is the iteration number;  $F_j \in \left[ \tilde{F}_{\min}, F_{\max} \right]$  is frequency;  $\beta \in [0, 1]$  is a random vector drawn from a uniform distribution;  $V_j^g$  is the speed of *j*th bat in *g*th generation;  $X_j^g$  is the position of *j*th bat in *g*th generation;  $X_*$  is the current global best location.

If rand  $1 > r_j^g$ , bat walks around the current best solution to complete local search according to Eq. ([17](#page-3-4)). If rand  $2 < A_j^g$   $\&f(X_{j,\text{new}}^g) < f(X_{*})$ , accept new solution  $X_{j,\text{new}}^g$ . Then, reduce  $A_j^{\hat{g}}$  and increase  $r_j^g$  $j$ <sup>s</sup> according to Eqs. ([18\)](#page-3-5) and  $(19)$  $(19)$ :

<span id="page-3-4"></span>
$$
X_{j,\text{new}}^g = X_j^g + \varepsilon \times \overline{A^g},\tag{17}
$$

<span id="page-3-5"></span>
$$
A_j^{g+1} = \alpha \times A_j^g,\tag{18}
$$

<span id="page-3-6"></span>
$$
r_j^{g+1} = r_j^1 \times \left[1 - \exp(-\gamma \times g)\right],\tag{19}
$$

where  $\varepsilon \in [0, 1]$  is a random number;  $X_{j, new}^{g}$  is the new position of *j*th bat in *g*th generation after local search;  $\overline{A^g}$  is the mean loudness of all bats in *g*th generation;  $A_j^g$  is the loudness of *j*th bat in *g*th generation;  $r_i^g$  $j_j^s$  is the pulse emission rate of *j*th bat in *g*th generation;  $\alpha$  and  $\gamma$  are constants. For any  $0 < \alpha < 1$  and  $\gamma > 0$ :

$$
A_j^g \to 0, \quad r_j^g \to r_j^1, \quad \text{as } g \to \infty. \tag{20}
$$

# <span id="page-4-0"></span>**Improved chaotic bat algorithm (ICBA)**

Assuming that the *D*-dimensional real space is the search space of optimization problem, the algorithm is a generation population  $R^g = \{X_1^g, X_2^g, \dots, X_i^g, \dots, X_{NP}^g\}$  composed of NP *D*-dimensional real parameter vectors  $X_j^g = \left\{ x_{j,1}^g, x_{j,2}^g, \ldots, x_{j,d}^g \ldots, x_{j}^g \right\}$ *j*,*D*  $\}$ . Where *j* is the number of individuals in the population,  $j = 1, 2, \dots, NP$ ; *g* is the iteration number,  $g = 1, \ldots, g_{\text{max}}$ . Based on the introduction of standard BA in previous section, we will explain how to combine the bat algorithm with chaotic theory in this section.

#### **The population initialization based on chaos theory**

The diversity and distribution of the initial population can infuence fnal optimal solutions of the algorithm. As other evolutionary algorithms, initial population is usually generated randomly, which may lead to problems such as the repeated solutions occupying memory space and the concentration of initial solution in a certain interval. Generating random sequences with a long period and good uniformity is very important for heuristic optimization. Its quality determines the reduction of storage and computation time to achieve a desired accuracy. Chaos is a deterministic, random-like process found in non-linear, dynamical system, which is non-period, non-con verging and bounded. The nature of chaos is apparently random and unpredictable and it also possesses an element of regularity. In this paper, the initial population is generated based on chaos principle, which could enhance diversity and uniformity of the population distribution (Alatas et al. [2009](#page-13-5)). Here the Logistic Map is selected. Its equation is as follows:

<span id="page-4-1"></span>
$$
x_d^{q+1} = \mu x_d^q \left( 1 - x_d^q \right) d = 1, 2 \dots, D; q = 1, 2 \dots, q_{\text{max}}, \tag{21}
$$

where  $x_d^q$  is a chaotic variable,  $x_d^1 \notin \{0.25, 0.5, 0.75\}$ ; *q* is the iteration number;  $\mu$  is the control parameter. When  $\mu$ =4, Eq. ([21\)](#page-4-1) is chaotic state.

Generate  $D$  different initial values within interval  $(0, 1)$ , and then generate *D* chaotic sequences with different trajectories by iteration using Eq.  $(21)$  $(21)$  $(21)$ . For example, when  $\mu$ =4,  $x_d^1$ =0.7, and  $q_{\text{max}}$ =100, Logistic sequences diagram is shown in Fig. [1a](#page-4-2).

Convert chaotic variables  $x_d^q$  $\frac{q}{d}$  to value interval of the decision variables  $[Z_d^{\min}, Z_d^{\max}]$ , and the individual *j* is expressed as  $Z_j = \{Z_{j,1}, Z_{j,2}, \cdots, Z_{j,d} \cdots, Z_{j,D}\}$ :

$$
Z_{j,d} = Z_d^{\min} + \left(Z_d^{\max} - Z_d^{\min}\right) \cdot x_d^q \qquad j = q,\tag{22}
$$

where  $Z_d^{\text{max}}$  and  $Z_d^{\text{min}}$  are the upper and lower limitations of the *d*th decision variable, respectively;  $Z_{i,d}$  is the value of the *j*th bat in *d*th dimension.

#### **The pulse emission rate based on chaos theory**

In the standard BA, pulse emission rate is monotonically decreased in the iterations progress. However, better results



<span id="page-4-2"></span>**Fig. 1** Chaotic value distributions during 100 iterations

have been reported when the  $r_j$  has been varied chaotically. In literature (Gandomi and Yang [2014](#page-14-21)), thirteen diferent chaotic sequences were tried to tune  $r_i$ . The best results is the CBA-IV with Sinusoidal sequences. Therefore, pulse emission rate *rj* is generated based on Sinusoidal map and varied to a chaotic number between 0 and 1 in this paper. Its equation is as follows:

$$
x_j^{g+1} = \mu \left( x_j^g \right)^2 \sin \left( \pi x_j^g \right) g = 1, 2 \dots, g_{\text{max}}, \tag{23}
$$

where  $x_i^g$  $\frac{g}{j}$  is a chaotic variable; *g* is the iteration number;  $\mu$  is the control parameter. When  $\mu$  = 2.3 and  $x_j^1$  = 0.7, it can be simplified to  $x_j^{g+1} = \sin\left(\pi x_j^g\right)$ *j* ), where  $g = 1, 2, ..., g_{\text{max}}$ .

Generate *NP* different initial values within interval  $(0, 1)$ , and then generate NP chaotic sequences with diferent trajectories by iteration using Eq.  $(23)$  $(23)$ . Finally, assign chaotic variables to pulse emission rate  $r_j^g$ . For example, when  $\mu$ =2.3,  $x_j^1$ =0.7, and  $g_{\text{max}}$ =100, Sinusoidal sequences diagram is shown in Fig. [1b](#page-4-2).

#### **Self**‑**adaptive loudness update mechanism**

In standard bat algorithm, both the local search operation and the condition of accepting optimal solutions are related to loudness. Therefore, the value of loudness directly afects the local search range and optimization results of the algorithm. In standard bat algorithm, the attenuation coefficient of loudness  $\alpha$  is a constant, which can largely determine the convergence speed of the algorithm. If the loudness reduces too fast, the convergence speed of the algorithm can be improved, but the algorithm may fall into the local optimal solution. Therefore, the self-adaptive loudness update mechanism is designed in this paper, which controls the convergence speed according to the iterations process. Now we have:

$$
A_j^{g+1} = \begin{cases} \alpha A_j^g & \text{if } \alpha A_j^g \ge \frac{A_{\text{max}}}{2} \\ \frac{A_{\text{max}}}{2} - \frac{\left(\frac{A_{\text{max}}}{2} - A_{\text{min}}\right) * \left(g - g^A\right)}{g_{\text{max}}} & \text{if } \alpha A_j^g < \frac{A_{\text{max}}}{2} \end{cases},\tag{24}
$$

where *j* is the number of bats; *g* is the iteration number;  $\alpha$  is the attenuation coefficient of loudness;  $A_j^g$  is the loudness of *j*th bat in *g*th generation;  $A_{min}$  and  $A_{max}$  are minimum and maximum loudness, respectively;  $g<sup>A</sup>$  is the maximum number of iterations that satisfies  $\alpha A_j^g \ge \frac{A_{\text{max}}}{2}$ ;  $g_{\text{max}}$  is the maximum iteration.

Set  $A_{\text{max}} = 1$ ,  $A_{\text{min}} = 0$  according to the reference (Yang [2010\)](#page-14-10). It is assumed that better solutions can be found in each generation, and the loudness  $A_j^g$  in each generation

needs to be updated. The comparison of the  $A_j^g$  between ICBA and BA is shown in Fig. [2.](#page-6-0)

Loudness  $A_j^g$  is the search range of local search. As seen in Fig. [2](#page-6-0), the change of loudness  $A_j^g$  in ICBA is slower than that in BA when  $\alpha$  changes. Therefore, compared to the BA, the search range of local search in ICBA is less infuenced by the value of  $\alpha$ . Moreover, the condition for accepting new solutions in BA and ICBA is rand  $2 < A_j^B \&f\left(X_{j,\text{new}}^g\right) < f(x_s)$ , the greater opportunity to accept better solutions can be achieved by using the proposed ICBA over BA, which demonstrates the superiority of the ICBA algorithm.

#### <span id="page-5-1"></span>**Constraint handling method**

This section mainly focus on how to handle the reservoir water level constraint (7), reservoir release constraint (8) and power output constraint (9) when the proposed ICBA algorithm is applied to solve MOO problem. The way of constraint handling determines whether a reasonable optimal solution can be found for reservoir operation. At present, the penalty method is most popular strategy for dealing with equality constraints of reservoir operation problem. However, this strategy is difficult to satisfy complex multiobjective scheduling of cascade reservoirs, so the constraint handling method with constraint transformation (Lu et al. [2011](#page-14-22)) is used in this paper.

The reservoir release constraint (8) and power output constraint (9) are converted to constraint corridor of water level in the constraint handling method with constraint transformation. Flow-water level corridor  $[Z^{\min}_{Q(i,t)}, Z^{\max}_{Q(i,t)}]$  and outputwater level corridor  $[Z_{N(i,t)}^{\min}, Z_{N(i,t)}^{\max}]$  can be obtained respectively. Then, combining the water level corridor with reservoir water level constraint  $[Z_{i,t}^{\min}, Z_{i,t}^{\max}]$  in formula [\(7](#page-2-0)), feasible water level range of the reservoir can be obtained by taking intersection. In addition, the intersection is empty if there is a confict between constraints. At this time, reservoir water level constraint will have priority.

#### **The implementation of ICBA for MOO problem**

The flowchart of the improved chaotic bat algorithm (ICBA) for MOO problem is presented in Fig. [3](#page-7-0).

## <span id="page-5-0"></span>**Case study**

#### **Study area and scenarios setting**

The Qingjiang River is one of the main tributary of Yangtze River. The 423 km long Qingjiang River has a catchment area of  $1.7 \times 10^3$  km<sup>2</sup>. Along the Qingjiang River,



<span id="page-6-0"></span>**Fig. 2** Comparison of the loudness between ICBA and BA

a three-step cascade reservoir (Shuibuya, Geheyan, and Gaobazhou) has been constructed from upstream to downstream (Guo et al. [2018](#page-14-23)). The characteristic of these three reservoirs and main parameters of power stations are given in Table [2.](#page-7-1) Figure [4](#page-8-0) shows the location of cascade reservoirs in the Qingjiang River. The downstream ecological fow results are listed in Table [3](#page-9-0).

According to the requirements of power generation and downstream ecological flow, four different scheduling scenarios are carried out in this paper.

Scenario 1: Power generation operation for cascade reservoirs is conducted. The downstream ecological fow requirement is not considered as the optimization goal. However, the satisfaction rates of minimum, suitable and ideal downstream ecological flow are calculated based on the outfow results of power generation operation.

Scenario 2: Cascade reservoirs are focused on the power generation and minimum downstream ecological flow requirement.

Scenario 3: Cascade reservoirs are focused on the power generation and suitable downstream ecological flow requirement.

Scenario 4: Cascade reservoirs are focused on the power generation and ideal downstream ecological flow requirement.

#### **Basic data and parameter setting**

According to the runoff data of the Qingjiang River basin from 1971 to 2005 year, the typical representatives of 1996 year, 2005 year, 1986 year and 2001 year are selected as the wet, normal, dry and extreme dry years, respectively. Using algorithms to solve scheduling model, water level of each reservoir is encoded, and the *j*th individual in the population can be expressed as  $Z_j = \{z^l_{j,l},..., z^l_{j,K}; z^2_{j,l},..., z^2_{j,K};$  $z^3_{j,l},..., z^3_{j,K}$ . Where  $z^l_{j,k}(k=1,2,...,K)$  is water level of the Shuibuya Reservoir;  $z_{j,k}^2(k=1,2,...,K)$  is water level of the



<span id="page-7-0"></span>**Fig. 3** The fowchart of ICBA for MOO problem

Geheyan Reservoir;  $z^3_{j,k}(k=1,2,...,K)$  is water level of the Gaobazhou Reservoir.

To verify the efectiveness of ICBA in the application of multi-objective scheduling, ICBA is compared with other algorithms, including chaotic genetic algorithm (CGA), chaotic particle swarm optimization (CPSO), chaotic differential evolution (CDE) and standard bat algorithm (BA). CGA mimics the process of natural evolution and generates new generations by selection, crossover, and mutation. CDE also produces new generations by selection, crossover, and mutation. However, the mutation of CDE is carried out on the basis of two paternal individuals, while the mutation in CGA is generated randomly. CPSO is based on the migration and clustering behavior of birds. In the optimization process, particles calculate their next fight direction and speed according to the optimal position of the whole particle swarm, its own optimal position in previous generations and the current position. BA is a heuristic algorithm based on the echolocation behavior of microbats. Bats search for global optimal solution by varying frequency and adjust pulse emission rate. In ICBA, the updating of pulse emission rate is based on chaos theory. The self-adaptive loudness update mechanism is designed to control the convergence speed according to the iterations process.

The initial population is generated based on chaos principle (Eq. [21](#page-4-1)) in the ICBA, CGA, CPSO and CDE. The population size  $NP = 200$  and the maximum iteration of algorithm  $g_{\text{max}} = 100$  are set for each algorithm. For ICBA, the maximum iteration of chaos operator  $q_{\text{max}} = 200$  in the population initialization; the frequency *F* is varied from 0 to 1; the loudness *A* is decreased from 1 to 0; the  $\alpha = \gamma = 0.9$ (Yang [2010](#page-14-10)). For CGA, the maximum iteration of chaos operator  $q_{\text{max}} = 200$  in the population initialization; the crossover and mutation operators are 1 and 0.01, respectively (Wang and Guo [2013\)](#page-14-24). For CPSO, the maximum iteration of chaos operator  $q_{\text{max}} = 200$  in the population initialization; the inertial constant is 0.3; the cognitive constant is 1; the social constant is 1 (Wang and Guo [2013\)](#page-14-24). For CDE, the maximum iteration of chaos operator  $q_{\text{max}} = 200$  in the population initialization; the crossover and mutation operators are 0.5 and 0.5, respectively (Wang and Guo [2013](#page-14-24)). For BA, the frequency *F* is varied from 0 to 1; the loudness *A i*s decreased from 1 to 0; the  $\alpha = \gamma = 0.9$  (Yang [2010](#page-14-10)). We defned the scheduling period is one year, and the period length is one month. During flood season from June to July every year, the reservoir water level should be controlled below the food control level.

#### **Average annual operation results**

Runoff datum from 1971 to 2005 year is selected to calculate average annual operation results. Table [4](#page-9-1) shows average annual power generation results of cascade reservoirs in Qingjiang River under diferent scenarios calculated by the proposed ICBA algorithm. The downstream ecological flow satisfaction rate results of Shuibuya Reservoir, Geheyan Reservoir and Gaobazhou Reservoir are presented in Table [5.](#page-9-2) To verify the efectiveness of ICBA in the application of MOO

<span id="page-7-1"></span>**Table 2** Characteristic water level of cascade reservoirs and main parameters of power stations





<span id="page-8-0"></span>**Fig. 4** Location of cascade reservoirs in the Qingjiang River

problem, ICBA is compared with several other algorithms, including CGA, CPSO, CDE and BA. Average annual power generation and the satisfaction rate of downstream ecological fow under scenarios 2, 3 and 4 are analyzed. The specifc results are shown in Table [6.](#page-10-0)

From Table [5](#page-9-2), when considering requirements of minimum and suitable downstream ecological flow, the downstream ecological fow satisfaction rate of scenario 1, 2 and 3 are 100%, which can completely meet the minimum and suitable downstream ecological fow requirements. In Table [4](#page-9-1), average annual power generation under these three scheduling scenarios is the same, among which Shuibuya reservoir has the largest average annual power generation  $(37.356 \times 10^8 \text{ kWh}).$ 

As can be seen from Tables [4](#page-9-1) and [5,](#page-9-2) when considering ideal downstream ecological flow requirement, the scenario 4 can increase the overall satisfaction rate of ecological fow by 1.772% compared to the scenario 1, while decreasing the average annual power generation by about  $0.1 \times 10^8$  kWh. The ecological flow satisfaction rate of Geheyan increases the largest, from 97.496 to 99.743%. Compared to the scenario 1, the scenario 4 proposed in this paper can improve the satisfaction rate of ideal downstream ecological flow requirement, and has little infuence on the average annual power generation.

As showed in Table [6](#page-10-0), when using the average annual flow as the reservoir inflow, the overall satisfaction rate of downstream ecological fow are higher than 96%. Moreover,

<span id="page-9-0"></span>**Table 3** Downstream ecological flow of cascade reservoirs  $m^3/s$ 

Period	Month	Shuibuya			Geheyan			Gaobazhou		
		Minimum	Suitable	Ideal	Minimum	Suitable	Ideal	Minimum	Suitable	Ideal
Spawning season $(Apr. ~ Sept.)$	4	78.86	133.53	203.44	90.84	166.80	273.32	93.42	173.97	288.37
	5	89.73	163.73	266.86	109.72	219.27	383.49	112.79	227.78	401.38
	6	97.22	184.54	310.57	117.25	240.18	427.41	120.51	249.23	446.42
	7	107.46	212.99	370.31	134.07	286.90	525.51	137.76	297.15	547.05
	8	81.68	141.38	219.93	99.70	191.43	325.02	102.51	199.23	341.41
	9	78.48	132.48	201.24	93.40	173.93	288.28	96.05	181.28	303.72
Ordinary times $(Oct. \sim Mar.)$	10	25.21	74.71	159.92	28.43	90.86	208.89	29.25	94.92	221.22
	11	22.53	61.36	119.42	24.87	73.03	154.82	25.59	76.64	165.76
	12	20.04	48.91	81.65	21.22	54.76	99.41	21.84	57.90	108.92
		19.57	46.53	74.42	20.39	50.63	86.86	20.99	53.66	96.05
	2	20.27	50.05	85.12	21.48	56.07	103.37	22.11	59.24	112.99
	3	22.07	59.05	112.40	24.66	71.99	151.67	25.38	75.57	162.53

<span id="page-9-1"></span>**Table 4** Average annual power generation under diferent scenar- $\cos \times 10^8$  kWh



in Table [6,](#page-10-0) CPSO, CDE, BA and ICBA can fully meet the minimum (scenario 1) and suitable (scenario 2) downstream ecological fow requirement of three reservoirs. The total average annual power generation generated by BA is greater than that of CGA, CPSO and CDE. When considering the minimum and suitable downstream ecological flow requirements, the total average annual power generation of ICBA is  $0.623 \times 10^8$  kWh and  $0.644 \times 10^8$  kWh higher than that of BA, respectively. When considering the ideal ecological flow requirement, the overall ecological flow satisfaction rate obtained by ICBA is the highest (98.860%) and slightly higher than that of BA (98.851%).

Therefore, the above results fully prove that the MOO problem can be solved by the ICBA. Compared to other algorithms, the ICBA method proposed in this paper can get better results.

#### **Typical hydrological year operation results**

It can be seen from foregoing analysis that average annual operation schemes of cascade reservoirs in Qingjiang River can meet the minimum and suitable downstream ecological flow requirements. Therefore, reservoir scheduling schemes in diferent typical hydrological years are designed in terms of meeting the ideal downstream ecological fow requirement (scenario 4). Meanwhile the ecological conditions of dry year and extreme dry year are analyzed in this section.

# <span id="page-9-3"></span>**Analysis of power generation and ecological satisfaction rate in typical hydrological year**

The operation results of scenario 1 and scenario 4 are compared and analyzed in Table [7](#page-10-1). Due to limited space, taking Shuibuya Reservoir and Geheyan Reservoir as examples, reservoir operation processes are shown in Fig. [5](#page-11-0).

In Table [7,](#page-10-1) when considering the ideal downstream ecological flow requirement, the overall satisfaction rate of downstream ecological fow of scenario 4 in wet year are 100%, which can completely meet the requirement of ideal downstream ecological flow. The overall satisfaction rates of downstream ecological flow in two scenarios can reach more than 93% and 83% in normal year and dry year, respectively. Moreover, as can be seen from Table [7,](#page-10-1) the annual power

<span id="page-9-2"></span>



<span id="page-10-0"></span>

Scenarios	Algorithm	Power generation $(10^8 \text{kwh})$				Satisfaction rate of downstream ecological flow			
		Shuibuya	Geheyan	Gaobazhou	Total	Shuibuya $(\%)$	Geheyan $(\%)$	Gaobazhou $(\%)$	Overall $(\%)$
Scenario 2	<b>CGA</b>	36.848	29.092	9.233	75.173	99.997	100	100	99.999
	<b>CPSO</b>	36.957	28.735	9.099	74.791	100	100	100	100
	<b>CDE</b>	37.127	29.181	9.237	75.545	100	100	100	100
	BA	37.056	29.335	9.578	75.969	100	100	100	100
	<b>ICBA</b>	37.356	29.636	9.600	76.592	100	100	100	100
Scenario 3	CGA	36.764	29.079	9.167	75.010	99.994	99.993	100	99.996
	<b>CPSO</b>	36.919	28.694	8.949	74.562	100	100	100	100
	<b>CDE</b>	37.027	29.203	9.271	75.501	100	100	100	100
	BA	37.032	29.330	9.586	75.948	100	100	100	100
	<b>ICBA</b>	37.356	29.636	9.600	76.592	100	100	100	100
Scenario 4	<b>CGA</b>	36.683	29.046	8.888	74.617	95.236	96.794	98.483	96.838
	<b>CPSO</b>	36.325	28.898	8.993	74.216	96.264	97.885	97.835	97.328
	<b>CDE</b>	36.815	29.094	9.247	75.156	96.418	98.179	98.549	97.715
	BA	37.004	29.281	9.502	75.787	96.845	99.718	99.991	98.851
	<b>ICBA</b>	37.306	29.582	9.603	76.492	96.837	99.743	100	98.860

<span id="page-10-1"></span>**Table 7** Operation results under scenario 1 and scenario 4 in diferent hydrological years



generation in extreme dry year is the least. Compared to the scenario 1, the scenario 4 can increase the overall satisfaction rate of downstream ecological flow by about 2.903% while decreasing the annual power generation by about  $0.515 \times 10^8$  kWh in extreme dry year.

With detailed operation results of two reservoirs displayed in Fig. [5,](#page-11-0) the feasibility of the proposed ICBA is verifed by testing the constraint violation conditions of the two schemes selected. It can be seen that infows of Shuibuya Reservoir are the same, while infows of Geheyan Reservoir are diferent under two schemes in Fig. [5](#page-11-0). That is because Shuibuya Reservoir is the frst reservoir of Qingjiang cascade reservoirs, which is located in the upper reaches of Geheyan Reservoir. The release of Shuibuya Reservoir will afect infow of Geheyan Reservoir. Moreover, the infow of reservoirs during the food season (from June to July) is the largest in the whole year in Fig. [5](#page-11-0). Therefore, the water

level of reservoirs needs to be controlled below the food control level.

## **Analysis of ecological status in downstream control sections in dry year and extreme dry year**

Based on results of reservoir discharge simulated in "[Analy](#page-9-3)[sis of power generation and ecological satisfaction rate in](#page-9-3) [typical hydrological year](#page-9-3)" under dry and extreme dry years, we analyzed downstream ecological status according to the grading standard of river ecosystem condition obtained by Montana Method in Table [1.](#page-3-1) The specifc analysis results are shown in Tables [8](#page-12-0), [9](#page-12-1) and [10.](#page-13-6)

It can be seen that the ecological status in dry year are generally better than those in extreme dry year in Tables [8,](#page-12-0) [9](#page-12-1) and [10](#page-13-6). Meanwhile, the satisfaction rate of downstream ecological flow can basically reach more than 20% of



<span id="page-11-0"></span>**Fig. 5** Reservoirs operation processes under scenario 1 and scenario 4 in diferent hydrological year

average annual fow in dry year, which is a good ecological condition.

The less infow of Shuibuya Reservoir in January leads to fair or degrading ecological condition in extreme dry year. When entering food control period in June and July, the reservoir water level should be controlled below the food control level. Moreover, the infow is relatively large at this time, and the satisfaction rate of downstream ecological flow can reach more than 70% of average annual flow, which are in the optimal range. From August to October is the storage period of reservoirs, and discharge decreases lead to gradual deterioration of downstream ecological condition. November

<span id="page-12-0"></span>**Table 8** Downstream ecological status of Shuibuya Reservoir in dry year and extreme dry year

Month	Dry year				Extreme dry year				
	Inflow of reservoir	Outflow of reservoir	Percent of average annual flow $(\%)$	Description of flows	Inflow of reservoir	Outflow of reservoir	Percent of average annual flow $(\%)$	Description of flows	
January	48.200	87.423	34.074	Excellent	24.000	30.921	12.052	Fair or degrad- ing	
February	52.400	96.237	37.510	Excellent	55,000	65.498	25.529	Good	
March	108.200	179.723	70.050	Optimal range	93.000	108.382	42.243	Outstanding	
April	164.000	187.072	72.914	Optimal range	314.000	369.200	143.902	Maximum	
May	227.500	227.500	88.672	Optimal range	198.000	257.138	100.224	Maximum	
June	368.400	368.400	143.590	Maximum	312.000	330.979	129.004	Maximum	
July	620.400	481.968	187.855	Maximum	227.000	227.000	88.477	Optimal range	
August	149.300	149.300	58.192	Excellent	114.000	114.000	44.433	Good	
September	263.100	253.871	98.950	Optimal range	33.000	33.000	12.862	Poor or mini- mum	
October	71.200	41.207	16.061	Fair or degrad- ing	242.000	188.173	73.343	Optimal range	
November	80.200	80.200	31.259	Excellent	118.000	58.612	22.845	Good	
December	59.800	59.800	23.308	Good	75.000	22.096	8.612	Severe degra- dation	

<span id="page-12-1"></span>**Table 9** Downstream ecological status of Geheyan Reservoir in dry year and extreme dry year



<span id="page-13-6"></span>



and December are low water period of reservoirs, and the ecological condition is worse. In extreme dry year, infow of reservoirs is the lowest in December. The satisfaction rate of downstream ecological fow of three reservoirs is less than 10% of average annual flow, resulting in serious ecological degradation.

# <span id="page-13-4"></span>**Conclusions**

In this paper, an improved chaotic bat algorithm (ICBA) has been established to handle the MOO problem. The ICBA is applied to the MOO problem of the Qingjiang cascade reservoirs in southern China. The results show that the minimum (scenario 2) and suitable (scenario 3) downstream ecological fow requirements can be satisfed, when the average annual flow is used as the reservoir inflow. When considering the ideal downstream ecological flow requirement, the overall satisfaction rate of downstream ecological flow can reach more than 90% in wet year and normal year. Compared to the scenario 1, the scenario 4 proposed in this paper can improve the satisfaction rate of ideal downstream ecological fow requirement, and has little infuence on the annual power generation. In December of extreme dry year, the satisfaction rate of downstream ecological flow of cascade reservoirs is lower than 10% of average annual flow, resulting in serious ecological degradation.

The case study is implemented to verify the validity and feasibility of the ICBA method. The results indicate that compared to other several algorithms, the ICBA method proposed in this paper can signifcantly improve both power generation and satisfaction rate of downstream ecological flow, which provides a new approach for solving the MOO problem. However, the MOO of cascade reservoirs is very complex. The more ecological issues, such as sediment deposition and water quality of cascade reservoirs, need to be considered in detailed in the further.

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## **Declarations**

**Conflict of interest** The authors declare that they have no confict of interest.

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