### **ORIGINAL ARTICLE**



# **Predictive models to estimate sediment volumes deposited by debris fows (Vargas state, Venezuela): an adjustment of multivariate statistical techniques**

WilliamsMéndez<sup>1,2</sup> • José Córdova<sup>3</sup> [·](http://orcid.org/0000-0003-0742-663X) Lelys Bravo de Guenni<sup>4</sup> • Henry Pacheco<sup>5</sup> · Kervin Chunga<sup>1</sup> · **Theoflos Toulkeridis[6](http://orcid.org/0000-0003-1903-7914)**

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### **Abstract**

Debris fows are a moving mass composed from water and solids mixture, mainly in form of sediments, with a high destructive power. The debris volume that is transported and deposited outside the drainage system of a watershed has a great importance in the defnition of its hydrological response. The objective of this work was to propose predictive models generated through the adjustment of multivariate statistical techniques, to estimate the sediment volumes deposited by debris fows. Measurements and calculations of the morphometric parameters of the watersheds and drainage networks have been performed with the support of GIS software and spreadsheets. The relationships between morphometric parameters and sediment volumes have been analyzed by applying multivariate statistical techniques such as linear correlation analysis. The principal component analysis and multiple linear regression analysis have been performed with principal components, which allowed the generation of predictive models. From the predictive models generated for the sediment volumes deposited by the debris flow event of December 1999, raised results closer to reality with better Pearson's correlation coefficients from those related to the gradient and shape of the watershed relief and extension of the drainage network morphometric variables. For the estimation of deposited sediment volumes due pre- and post-1999 event conditions, only the predictive models generated with the gradient and shape of the watershed relief variable have had good results.

**Keywords** Morphometry · Sediment volume · Debris fow · Hydrological response · Predictive model · Multivariate statistical

# **Introduction**

In watersheds developed in mountainous environments such as natural hydrological systems, fows are represented by volumes of water and solids that generally constitute debris as a result of rains captured in their areas of origin. These activate hydro-geomorphological processes such as erosion

 $\boxtimes$  Williams Méndez williamsmendez@gmail.com

- <sup>1</sup> Departamento de Construcciones Civiles, Facultad de Ciencias Matemáticas, Físicas y Químicas, Universidad Técnica de Manabí, 130105 Portoviejo, provincia de Manabí, Ecuador
- <sup>2</sup> Centro de Investigación Estudios del Medio Físico Venezolano, Instituto Pedagógico de Caracas, Universidad Pedagógica Experimental Libertador, El Paraíso, Caracas 1020, Distrito Capital, Venezuela

and runoff-related transport, which are often able to generate extreme foods and debris fows (Van Steijn [1996](#page-19-0); Coussot and Meunier [1996;](#page-17-0) Vallance and Scott [1997;](#page-18-0) Jakob et al. [2005](#page-17-1); Tichavský and Šilhán [2015\)](#page-18-1).

These observable and measurable effects on watersheds outflows are what are known as their hydrological responses (Santi et al. [2011](#page-18-2); Ballesteros-Cánovas et al. [2015;](#page-16-0) Palau

- <sup>3</sup> Departamento de Procesos y Sistemas, Universidad Simón Bolívar, Sartenejas, Baruta 1080, estado Miranda, Venezuela
- Departamento de Cómputo Científico y Estadística, Universidad Simón Bolívar, Sartenejas, Baruta 1080, estado Miranda, Venezuela
- <sup>5</sup> Departamento de Ingeniería Agrícola, Facultad de Ingeniería Agrícola, Universidad Técnica de Manabí, 13132 Lodana, provincia de Manabí, Ecuador
- <sup>6</sup> Universidad de las Fuerzas Armadas ESPE, Sangolquí, Quito, Ecuador



<span id="page-1-0"></span>**Fig. 1** Overview of deposits and efects of December 1999 debris fow event in Venezuela's Vargas state: **a** deposits (white color) of the event on the alluvial fans (from left to right) Macuto, Punta El Cojo, Camurí Chiquito, Punta El Caribe and Punta Cerro Grande, **b** impact of debris fows on the population (Los Corales sector) and **c** debris

fow deposits in the main channel of the Camurí Chiquito creek (stretch over alluvial fans), dissected after the event. Satellite image IKONOS from Centro de Procesamiento Digital de Imágenes [CPDI] ([1999\)](#page-16-5)

et al. [2017](#page-18-3)). One of the quantifable and important parameters in its defnition, particularly in the case of debris fows, is the volume of debris that has been transported and deposited outside the watershed. In this regard, sediment volume refers to the amount of sediment, debris or solid charge present in a stream (Costa [1984](#page-16-1), [1988;](#page-17-2) Iverson [1997\)](#page-17-3). The sediment load of a debris flow is deposited due to a sudden decrease of the channel slope. This occurs when the debris fow leaves the mountainous sector and enters in a topographically fatter area. In many cases, these fat areas are alluvial fans, whose genesis is linked to the occurrence of these same hydro-geomorphological processes (debris flows).

The activation of debris flows depends on several factors such as precipitation (distribution, duration, and intensity), relief, topographic slopes, drainage network, alteration and depth of the ground cover, lithology, vegetation cover, and anthropogenic interventions. Among these factors, vegetation (types of plant formations in terms of their density and coverage) and lithology play a fundamental role in the genesis of debris fows, which has been widely demonstrated in the literature and in various localities worldwide. However, the purpose of this study is not to demonstrate that this is the case, but rather to focus on other elements of the system (morphometry of the watersheds and their drainage systems) for which little documentation has been provided on their relationship with the volumes and/or magnitudes of the deposits by debris fows.

On the other hand, the surface and vertical distribution of the diferent vegetal formations present in the study area, from the coastline to the summit of the studied mountain front, presents a fairly similar pattern in all watersheds. Likewise, lithological types, in which most superficially exposed rocks are foliated metamorphic, with some slight changes.

The type, structure and nature of the rocky outcrops, are determinants for the sediment granulometry generated by the action of meteorological and erosive processes, but there are also other variables that operate spatially at greater scales, such as for example, the morphometry of watersheds and their drainage systems, which ultimately determines the volumes of sediments that a watershed as a whole can contribute to a debris fow event.

The results obtained from the multivariate statistical analyzes and the models generated in this research, document interesting fndings. It is demonstrated which are the specifc morphometric parameter groups that have a signifcant relationship with the volumes of sediments of the debris fows.

The study area was chosen to be the watersheds of the north slope of the El Ávila massif, in the Vargas state, Venezuela, for the development and application of predictive models of sediment volumes. This site has been located on a relatively rugged mountainous slope, which is suitable for a torrential character with sudden and aggressive hydrological reactions, as evidenced by the sudden foods and debris flows that occurred in December 1999 (Larsen et al. [2001a,](#page-17-4) [b](#page-17-5); Pérez [2001](#page-18-4); García-Martínez and López [2005](#page-17-6); Nadim et al. [2006](#page-18-5)) (Fig. [1\)](#page-1-0).

A series of studies have been conducted to estimate the volumes of sediments produced in watersheds, transported and deposited by rivers of the northern slope of the El Ávila massif, using a variety of other methodologies (Córdova and González [2003;](#page-16-2) Artigas et al. [2004](#page-16-3), [2006](#page-16-4); Hernández



Local map and study area

<span id="page-2-0"></span>**Fig. 2** Location of the watersheds of the study area: (*A*) Piedra Azul Creek, (*B*) Osorio Creek, (*C*) Cariaco Creek, (*D*) San José de Galipán River, (*E*) El Cojo Creek, (*F*) Camurí Chiquito Creek, (*G*) San Julián Creek, (*H*) Seca Creek, (*I*) Cerro Grande River, (*J*) Uria River, (*K*)

Naiguatá River and (*L*) Camurí Grande River. Cartographic base from Instituto Geográfco de Venezuela Simón Bolívar [IGVSB] ([2003\)](#page-17-19); satellite image LANDSAT 7 ETM from CPDI (2002)

[2006](#page-17-7); López et al. [2006;](#page-17-8) Artigas and Córdova [2010](#page-16-6); Martínez [2010\)](#page-17-9) and more recent methods for estimating sediment volumes from debris flows and other types of mass disposal processes (Bremer and Sass [2012](#page-16-7); Tiranti et al. [2016](#page-18-6); Legorreta Paulín et al. [2017;](#page-17-10) Martha et al. [2017;](#page-17-11) Martin et al. [2017](#page-17-12)).

Other recent efforts in the study of the debris flows, have focused on analyzing and understanding the genesis of these flows linked to the occurrence of rainfall events, proposing models taking into account aspects such as thresholds, extreme events, rainfall intensity-duration and probabilities (Chen et al. [2016;](#page-16-8) Giannecchini et al. [2016](#page-17-13); Marra et al. [2016](#page-17-14); Bel et al. [2017;](#page-16-9) Destro et al. [2017](#page-17-15); Dietrich and Krautblatter [2017;](#page-17-16) Fan et al. [2017;](#page-17-17) Ma et al. [2017;](#page-17-18) Wei et al. [2017\)](#page-19-1).

The main objective of this study has been to explain the relationships between volumes of sediment deposited by water courses (debris fows) of mountainous environments and the morphometric parameters of watersheds and drainage systems that generate them, using multivariate statistical techniques. In addition, we seek to reduce the dimensionality of independent variables (morphometric parameters), to produce efective predictive models applicable to the studied watersheds as well as others located in similar physiographic contexts .

# **Study area**

The watersheds selected for this study, due to their hydrogeomorphological interest resulting from the catastrophic event of December 1999, are located in the central-northern Region of Venezuela, more precisely in the central part of the Vargas state, and extend on the northern slope of the El Ávila massif, at its western end, occupies an area of about 198.89 km<sup>2</sup> (Fig. [2](#page-2-0)). This area is part of the Coastal Mountain Range, part of the Caribbean Mountainous System, in its central section. It is located in the eastern sector of the northern slope of the Serranía del Litoral. Specifcally, on the El Ávila massif (Fig. [3](#page-3-0)).

The area borders the Caribbean Sea to the north, where the main water courses flow into the corresponding watersheds. To the south, it borders the watersheds of the southern slope of the El Ávila massif and the city of Caracas. To the east appear the Care and Anare river watersheds, La Cortada row and the Naranjal and La Cruz topographic summits, and to the west the Las Pailas and the Tacagua watersheds as well as the Tacagua pass.

Watersheds considered to be exorheic hydro-geomorphological systems in which three relief unit's characteristic of these systems have been distinguished: a catchment area, a main drainage channel and an alluvial fan, each with its own morphological characteristics and processes. Topographically, they are depressed morphology units more or less similar to funnels, a basic confguration that determines the torrential behavior of these systems. Hence, the topographic features (steep slopes between 15% and more than 45%; average slopes between 24.32 and 34.13%; heights between 25 and 2770 m.a.s.l.) indicate strong irregular terrain conditions, morphodynamic instability and sudden hydrological responses. Creeks and rivers in the studied area have very short watercourses (between 3.55 and 13.55 km) from their nascent to the mouth in the mountain front, along which they fowed, presenting steep slope variations, typical of



<span id="page-3-0"></span>**Fig. 3** 3D reconstructed surface with shading overlay, on which one can appreciate the alluvial fans and watersheds of the northern slope of the El Ávila massif in the study area

torrential systems in mountainous environments with very pronounced reliefs.

# **Geology**

The geology is represented by outcrops of lithodemic units belonging to the strips of the Ávila Metamorphic Association (Peña de Mora Augengneis, San Julián Complex, Caruao Metatonalite and Naiguatá Metagranite) and the La Costa Metamorphic Association (Serpentinite bodies, Nirgua Amphibolite, Tacagua Schist and Antímano Marble) (Urbani [1999,](#page-18-7) [2000,](#page-18-8) [2002a](#page-18-9), [b](#page-18-10), [c](#page-18-11), [d,](#page-18-12) Urbani et al. [2006\)](#page-18-13). These include:

- (a) *Peña de Mora Augengneis* (Paleozoic–Precambrian), with augengneises, quartzite layers, aplite dykes, marble lenses and quartz-muscovite schists.
- (b) *San Julián Complex* (Paleozoic–Precambrian), with schists and quartz-plagioclase-micaceous gneisses.
- (c) *Caruao Metatonalite* (Pre-Mesozoic), with metaigneous rocks corresponding to tonalites, amphibolites, diorites, trondhjemites, granites, granodiorites, gneisses and amphibole schists.
- (d) *Naiguatá Metagranite* (Pre-Mesozoic), with mediumgrained leuco-syenite-granite with slight banding.
- (e) *Serpentinite bodies*, including various types of serpentinites, amphibolites and rodingites.
- (f) *Nirgua Amphibolite* (Mesozoic), with various types of amphibolites, schists, marbles, quartzites, gneisses, epidocites and serpentinites.
- g) *Tacagua Schist* (Jurassic–Cretaceous), with dark gray and light green schists.
- (h) *Antímano Marble* (Cretaceous), with massive marbles of clear gray color with layers of quartz-micaceous schists, associated with concordant bodies of amphibolic rocks.
- (i) *Alluvium* (Holocene) with overlying discordance on the rocks of the La Costa Metamorphic Association in the lower parts of the watersheds. They are shaped by alluvial fans and valley bottom deposits.

# **Vegetation**

The vegetation formations are well described in Steyermark and Huber's studies ([1978\)](#page-18-14), Huber and Alarcón [\(1988](#page-17-20)), Amend ([1991\)](#page-16-10) and Vareschi ([1992\)](#page-19-2), and for which some of their main characteristics are described below:

- (a) *Littoral vegetation,* situated between sea level and 50 m.a.s.l., it is composed of very low species, mainly herbaceous, subfrutic and halophytic crawlers.
- (b) *Cardonal and spine,* located between 50 and 300 m.a.s.l., is a community of low to medium size (0.5–5 m), adapted to the drought, of variable density between open to very closed, strongly armed and columnar cactus.
- (c) *Deciduous forest,* low to medium height (10–20 m), with 1–2 arboreal strata and a dense understory, which is generally located between 300 and 600 m.a.s.l., has

a high percentage of deciduous tree species, and others that can reach heights between 15 and 20 m.

- (d) *Semi*-*deciduous forest,* located between 600 and 800 m.a.s.l., of medium height and comprising 2–3 dense arboreal strata. They are composed of deciduous and evergreen trees.
- (e) *Transitional forest,* located between 800 and 1500 m.a.s.l., medium to high heights (25–30 m) with 2 or 3 arboreal strata, abundant epiphytes and a relatively dense understory.
- (f) *Cloudy forest,* located between 1200 and 2200 m.a.s.l., the trees are very highs and evergreen, with a great variety of epiphytic species on their trunks.
- (g) *Sub*-*páramo,* heights higher than 2200 m.a.s.l.
- (h) *Gallery forest,* they accompany the courses of rivers and creeks, the shrub and herbaceous strata are well developed.
- (i) *Secondary vegetation,* atypical species of the region, the result of human intervention or reforestations.

# **Materials and methods**

With basic cartographic information (Dirección de Cartografía Nacional [DCN], [1958](#page-17-21), [1979;](#page-17-22) Gobernación del Distrito Federal [GDF], [1984;](#page-17-23) Servicio Autónomo de Geografía y Cartografía Nacional [SAGECAN], [1995](#page-18-15)) at scales of 1:5000 (39 topographic plans) and 1:25,000, (6 topographic charts), the base maps have been assembled with which the polygons corresponding to the study area (watersheds) have been delineated. Both map covered the entire study area. This information has been rasterized and digitized using the ArcGIS 9.2 software with its ArcHydro and Spatial Analysis modules. With this last module and using the of 1:25,000 base map, the Digital Elevation Model (DEM) of the study area was generated afterwards. Then from this, we were able to establish the longitudinal and transverse topographic profles of the relief, as well as those of the river and creek channels.

The measurements and calculations of the morphometric parameters of the watersheds and their drainage networks were made on a digitized map at scale of 1:5000 and the DEM, obtaining basic linear, longitudinal, surface, elevation and clinometric parameters. This scale of work (1:5000) provided more accurate and approximate values for most of the basic morphometric parameters. Then, with the information obtained and the corresponding mathematical equations that defne the rest of the parameters, we proceeded to their respective estimates (Table [1\)](#page-5-0).

The hydrological information has been represented by the corresponding sediment volumes, namely the debris fows event of December 1999, before to the debris fows event of 1999 ( $Tr = 100$  years) and after the debris flows event of

1999 ( $tr = 100$  years), as previously suggested by Córdova and González ([2003\)](#page-16-2) and Artigas and Córdova ([2010\)](#page-16-6). Córdova and González ([2003](#page-16-2)) had previously estimated these hydrological parameters (sediment volumes) for the same watersheds of the study area, by calibrating and applying the method developed by the U.S. Army Corps of Engineers (USACE), which takes into account the volumes of debris observed after a debris fow event, as well as a set of physical and natural variables. The volumes of debris observed were estimated by topographic–cartographic methods.

To interpret the degree of relationship between the morphometric parameters and the sediment volumes, a linear correlation analysis (LCA) has been performed. It is based on the estimation of the Pearson's correlation coefficient by the product of moments method, using the Xlstat complement of Microsoft Excel.

A principal component analysis (PCA) has been developed (Pearson [1901](#page-18-16); Hotelling [1933\)](#page-17-24) with the morphometric parameters, to reduce its dimensionality and to identify those that each has signifcant weight in their relationships with sediment volumes. Hereby, the type of PCA that has been performed is based on the correlations method. The PCA has been run using the SPSS Statistics Version 17.0 statistical package, for each set of parameters grouped in the same morphometric variable. The standardized scores for each watershed have been used as the values of the new variables representative of the morphometric parameters. We performed with them multiple linear regression analysis (MLRA).

The MLRA have been performed using the SPSS Statistics version 17.0 statistical package.

MLRA has been performed for each of the groups of principal components (PC), each of which represents groups of morphometric parameters as independent variables or predictors. Once the results of the MLR have been obtained, the PC's of the morphometric parameter groups that gave adequate results in their relationships with the sediment volumes have been identifed, and those PC that did not satisfy the generated models have been then rejected. Predictive statistical-mathematical models have been constructed with the non-standardized coefficients  $(\beta)$  of the constants and the PC's generated by the MLRA. The magnitudes of the sediment volumes deposited by the main watercourses (debris flows) have been estimated according to these new models.

### **Results and discussion**

# **Morphometry of watersheds and their drainage networks**

Based on the morphometric parameters of the watersheds and their drainage networks (Table [2\)](#page-8-0), and more particularly

<span id="page-5-0"></span>



**Table 1** (continued)



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Table 1 (continued)

Statistic	$A$ (km <sup>2</sup> )		$\text{As}_{\text{larger}}\,(\text{km}^2)$	$\text{As}_{\text{smaller}}\left(\text{km}^2\right)$		$P$ (km)	$L$ (km)		$W_{\rm m}$ (km)	$W_{\text{max}}$ (km)		$D$ (km)		Aer $(km2)$	Pc(km)
Maximum value	31.38	25.55		8.83		25.10	8.70		3.74	6.18		6.32	51.79		19.86
Minimum value	2.89	1.63		1.26		6.80	2.88		1.00	1.40		1.92	4.03		6.03
Mean	13.89	9.23		4.65		16.15	6.08		2.06	3.26		3.97	22.05		12.46
Statistic	$h$ (masl)	$H$ (masl)		$H_{\rm m}$ (masl)	$H_r$ (masl)		$h_0$ (masl)		$R_{\text{max}}$ (m)	R(m/km)		$S_{\rm m}$ (m/m)	C <sub>ms</sub>		$Sms_m(m/m)$
Maximum value	125	2770		1316.76	2550		125	2745		442.50	0.34		0.71	0.41	
Minimum value	25	1280		547.71	1200		25	1230		270.83	0.24		0.00	0.20	
Mean	48.85	2122.08		939.70	2040.38		48.85		2073.23	353.45	0.30		0.39	0.27	
Statistic	$Rms_{max}(m)$		<b>Tfms</b>	$\mathrm{Sts}_{\mathrm{m}}\left(\mathrm{m}/\mathrm{m}\right)$		H <sub>I</sub>	$Cm$ (masl/km <sup>2</sup> )		Co		$Rr$ (m/km)		MRn	E	Prc
Maximum value	2525		1367.37	0.82		0.55	195.57			154,518.28	180.88		0.91	0.68	25.94
Minimum value	1150		666.30	0.50		0.35	34.74			36,620.01	92.20		0.42	0.48	16.00
Mean	1991.54		1020.23	0.65		0.43	98.66			84,764.85	136.94		0.63	0.57	21.38
Statistic	Kc		$\mathbf{I}$	Ih		Is	Ff		C <sub>1</sub>	Re		Rc		If	$I1-a$
Maximum value	1.43		3.01	0.77		4.38	0.46		2.08	0.76		0.79		2.03	1.13
Minimum value	1.12		1.36	0.51		1.01	0.23		1.48	0.54		0.48		1.60	1.13
Mean	1.29		2.03	0.64		1.89	0.33		1.77	0.64		0.60		1.84	1.13
Statistic	Cf	Cr		$Lms$ (km)	$Lv_m(km)$		$Lts$ (km)	$\boldsymbol{S}$		St	Sh		$Gc$ (km)		$Dd$ (km/km <sup>2</sup> )
Maximum value	0.46	3.40	13.55		11.00		255.55		1.66	1.34	13.55	11.00		255.55	
Minimum value	0.23	1.72	3.55		3.00		34.03		1.09	1.02	3.55		3.00	34.03	
Mean	0.33	2.50		7.86	6.75		123.33		1.33	1.13	7.86		6.75	123.33	
Statistic	$Dt (km^{-1})$		Cmc (km <sup>2</sup> /km)		$E_m(km)$		Lsf(km)	Tt		Di (km)	$R_{m}$	$N_{\rm t}$		$\boldsymbol{\mathcal{U}}$	$\rm Rb_m$
Maximum value	1136.46		0.18		0.04		0.10	1.52		5.21	2.80		1120	6	4.99
Minimum value	87.08		0.07		0.02		0.03	1.06		2.75	1.83	169		4	3.58
Mean	430.41		0.11		0.03		0.05	1.30		4.09	2.27		497.54	5.15	4.10
Statistic		$Rl_m$		$\rm{Rs}_m$			$Fsm (Nt/km2)$			$Ct (N_1/km^2)$			Cs		$M(N_1)$
Maximum value		2.84		1.66		76.92				60.85			0.58		886
Minimum value		1.92		1.16	15.48					11.72			0.50		127
Mean	2.26			1.41	40.83				31.51				0.55		384.54

<span id="page-8-0"></span>**Table 2** Morphometric parameters of the watersheds and drainage networks

those referred to the watershed scale variable, these hydrogeomorphological systems fall into the category of microwatersheds due to their small dimensions. Regarding the parameters of the gradient and shape of the watershed relief variable, they are defned as topographically very rugged areas with steep slopes and large altitudinal roughness. The watershed shape parameters indicate that they are semi-circular to semi-elongated planimetric morphologies, while in the case of the extension of the drainage network parameters, they indicate branched drainage systems, and considerable densities at short lengths and small sinuosity channels being rectilinear. In the case of the order and magnitude of the drainage network variable, its parameters indicate networks of high magnitudes and orders, as well as high levels of torrentially.

The geometry of the systems (watershed scale parameters) are the ones that determine in greater proportion the specifc conditions that favor the occurrence of fash floods, with hydrographs of sharp peaks and short duration. They also occur as shorter concentration times in the presence of signifcant storms in intensity, duration and dimensions, as they determine are the areas where rainwater is collected. In addition to the morphometric parameters grouped in the scale watershed variable, others corresponding to variables defning diferent attributes of these hydro-geomorphological systems, contribute in the same way to a signifcant weight in controlling the amplitudes and characteristics of the hydrological and morphodynamic responses of the watersheds.

These morphometric parameters are represented in specifc by the slopes of the longitudinal profles of the main creeks and rivers, the prominent mountainous relief (massiveness coefficient, orographic coefficient and Melton roughness number), the short lengths of the main

<span id="page-9-0"></span>Table 3 Correlation coefficients between the sediment volumes and the morphometric parameters of the watersheds and drainage networks

Hydrological response parameter Morphometric parameter	Sediment volume (event of December 1999) (Vs- Dec1999)	Sediment volume prior to the debris flows (Tr = 100 years) ( $V_{\text{prior-df}}$ ) (m <sup>3</sup> )	Sediment volume after the debris flows (Tr = 100 years) ( $Vs_{after-df}$ ) (m <sup>3</sup> )			
	(m <sup>3</sup> )					
Area $(km^2)$	$0.71*$	0.73	0.73			
Larger slope area $(km^2)$	0.66	0.73	0.73			
Smaller slope area $(km^2)$	0.70	0.57	0.55			
Perimeter (km)	0.69	0.72	0.70			
Length (km)	0.66	0.66	0.63			
Mean width (km)	0.75	0.78	0.77			
Maximum width (km)	0.67	0.68	0.68			
Diameter (km)	0.74	0.75	0.74			
Equivalent rectangle area to the watershed $(km2)$	0.67	0.67	0.66			
Circle perimeter equal to the water- shed area (km)	0.74	0.75	0.74			
Minimum height (masl)	0.40	0.24	0.25			
Maximum height (masl)	0.42	0.33	0.31			
Mean height (masl)	0.48	0.42	0.40			
Main stream rising height (masl)	0.34	0.30	0.29			
Main stream outlet height (masl)	0.40	0.24	0.25			
Maximum relief (m)	0.38	0.30	0.29			
Relief ratio (m/km)	$-0.73$	$-0.80$	$-0.78$			
Mean relief slope (m/m)	$-0.08$	$-0.15$	$-0.16$			
Concavity of the main stream longi- tudinal profile	0.13	0.14	0.16			
Mean slope of the main stream longi- $-0.73$ tudinal profile (m/m)		$-0.77$	$-0.75$			
Main stream maximum relief (m)	0.30	0.28	0.26			
Main stream topographic factor	$-0.17$	$-0.23$	$-0.23$			
Mean slope of the drainage network total streams $(m/m)$	$-0.19$	$-0.21$	$-0.21$			
Hypsometric integral	0.25	0.35	0.31			
Massiveness coefficient (masl/km <sup>2</sup> )	$-0.76$	$-0.75$	$-0.74$			
Orographic coefficient	$-0.73$	$-0.71$	$-0.73$			
Relative relief (m/km)	$-0.73$	$-0.81$	$-0.80$			
Melton roughness number	$-0.80$	$-0.83$	$-0.83$			
Elongation	0.68	0.69	0.71			
Relative crenulation perimeter	$-0.50$	$-0.37$	$-0.41$			
Compactness coefficient	$-0.49$	$-0.35$	$-0.40$			
Lengthening index	$-0.50$	$-0.48$	$-0.51$			
Homogeneity index	0.21	0.24	0.24			
Symmetry index	0.43	0.63	0.63			
Form factor	0.67	0.69	0.72			
Caquot lengthening	$-0.68$	$-0.67$	$-0.70$			
Elongation ratio	0.68	0.69	0.71			
Circularity ratio	0.45	0.29	0.35			
Form index	$-0.49$	$-0.35$	$-0.40$			
Form coefficient	0.67	0.69	0.72			
Roundness coefficient	$-0.68$	$-0.66$	$-0.69$			
Main stream length (km)	0.51	0.57	0.56			
Main stream valley mean length (km)	0.63	0.67	0.65			

#### **Table 3** (continued)



\*Signifcant correlation coefcients (*p* value≤0.05)

watercourses, the high orders of the watersheds considering that they are small systems, the total number of drainage system streams and their magnitudes.

### **Hydrological response: sediment volumes**

The hydrological response parameters to which this study refers are fundamentally related to sediment volumes, as expressions of hydrologic dynamics that distinguish the hydro-geomorphological systems of mountainous environments and their torrential behaviors. The sediment volumes transported during the debris fows event of December 1999 ranged from 839,182 to 2,636,280  $m<sup>3</sup>$ , with an average of  $1,685,968.42 \text{ m}^3$ . For volumes of sediment produced under pre- and post-debris fows conditions of December 1999 and for a 100 years return period, these values ranged between 484,302 and  $1,313,876.60 \text{ m}^3$  in the first case, and between 559,328.60 and  $1,450,556.80 \text{ m}^3$  for the second, with average values of 867,840.55  $\text{m}^3$  and 1,023,799.75  $\text{m}^3$  respectively .

These magnitudes refer to the solid discharges in the watersheds hydrological responses, representing signifcant amounts that demonstrate the aggression, the hydrologic and morphodynamic power of the debris fows events that have occurred and could occur in the future in the studied sector, under the combination of triggering efects such as extraordinary rainfall and conditions of high susceptibility of the physical environment such as lithology, slope, landforms, vegetation, drainage, and soils.

### **Linear correlation analysis**

The LCA provided a frst approximation of the degree of relationship between the dependent variables (morphometric parameters) and independent variables (volumes of sediments) involved in the study and allowed us to identify the specifc morphometric parameters frst, that have greater signifcance in terms of their impact or control on the hydrological response (debris flows) of the watersheds.



Bold values represent the principal component number of each variable, in which the cumulative variance (%) reaches more than 80% representativeness

The best correlation coefficients  $(> 0.70; p \text{ value } \leq 0.05)$ between the sediment volumes and the morphometric parameters of the watersheds and drainage networks have been observed, in order of importance for the gradient and shape of the watershed relief and watershed scale variables  $(Table 3)$  $(Table 3)$ . The correlation coefficients obtained with the parameters of the watershed scale variable are signifcant, since they have values between 0.66 and 0.78, similarly indicating a considerable weight of the watershed dimen sions in the sediment yield and transport during extreme events. Morphometric parameters with the best correlations  $(>0.70)$  with sediment volumes are the area, mean width, diameter and circle perimeter equal to the watershed area

(Table [3](#page-9-0)). The morphometric parameters of the gradient and shape of the watershed relief variable with good correlation coef cients  $(>0.70; \leq 0.05)$  with the sediment volumes have been those linked to inequalities (relief ratio), slopes (mean slope of the main stream longitudinal profle) and the prominent mountainous relief (massiveness coefficient, orographic coefficient, relative relief and Melton roughness number). These coefficients have been negative because the lower slopes of the main streams and a relatively less mountainous terrain correspond to watersheds of greater areas. However, the greater slopes and the more pronounced mountainous terrain present the watersheds of less extensive areas. This is the result of denudation rates (vertical and regressive ero sion) of the most pronounced relief in the watersheds of larger areas.

# **Principal components analysis of morphometric parameters**

<span id="page-11-0"></span>According to the analysis of the total explained variance (ATEV) in the PCA (Table [4](#page-11-0)), all the morphometric param eters grouped in the watershed scale variable are explained in the same component (PC 1), in because of their high correlations between all these parameters. Thus, PC 1 correlates with 94.38% of the grouped parameters. In the case of the gradient and shape of the watershed relief variable, four PC have been obtained which correlate together for approximately 91.42% of the parameters representing the mentioned variable (Fig. [4](#page-12-0)). With the watershed shape variable, ATEV achieved its best percentage of representation in two PCs that total up 90.58% of the parameters that represent it. For the extension of the drainage network variable, three PCs have been generated, in the third of which 93.82% of the cumulative total variance has been correlated. Within the order and magnitude of the drainage network variable, three PCs have been obtained in the same form, in which an accumulated PC 3 explained and reached a total variance of 84.65%.



<span id="page-12-0"></span>**Fig. 4** PC diagrams of the morphometric parameters corresponding to the variables **a** watershed scale, **b** gradient and shape of the watershed relief, **c** watershed shape, **d** extension of the drainage network and **e** order and magnitude of the drainage network

The coefficients obtained from the scores (weights) for each parameter of each morphometric variable, which have been regrouped according to the PC (new variables), we observed that in the watershed scale variable, all its parameters have similar scores. For the other morphometric variables, signifcant diferences have been observed regarding their score coefficients for each morphometric parameter, and according to each PC in which they have been grouped, allowed to rank them in order of importance (Fig. [5\)](#page-13-0).

### **Multiple linear regression analysis**

The models generated by the MLRA between the PC of the watershed scale variable and sediment volumes produced good correlation coefficients (between 0.730 and 0.742)



<span id="page-13-0"></span>**Fig. 5** PC diagrams in rotated space of the morphometric parameters corresponding to the variables **a** gradient and shape of the watershed relief, **b** watershed shape, **c** extension of the drainage network and **d** order and magnitude of the drainage network

and low determination indices (between 0.533 and 0.551). The signifcance demonstrated low values (between 0.006 and 0.007) and the Durbin–Watson test gave values greater than 1.4, indicating that there were no serious or important autocorrelations, so the variables considered in the model appear to be independent. Better results have been obtained with the gradient and shape of the watershed relief variable, indicating that these morphometric parameters are good predictors of debris volumes. For the shape of the watershed shape variable, the statistical evaluators of the efficiency of the models presented less optimal values, indicating a less reliable variable as a predictor of sediment volumes.

Very good results have been obtained with the extension of the drainage network variable, although slightly less adapted than the gradient and shape of the watershed relief variable, with which these models are considered as quite acceptable predictors. The resulting models with the order and magnitude of the drainage network variable showed very low correlation coefficients and determination indices. With very high signifcance and Durbin–Watson test values greater than 1.4, the data reveal that the morphometric parameters of this variable cannot be considered as predictors of sediment volumes.

In the results of MLRA-generated  $\beta$ -coefficients between the PC of each one of the morphometric parameters groups and the sediment volume parameters, we observed that for the watershed scale variable, all the predictive models have been presented as acceptable alternatives for estimating the magnitudes of sediment volumes, since the 95% confdence intervals for β occupy ranges or amplitudes greater than zero. As a result, all these predictive models are satisfed with the single PC generated for such variable.

The predictive models, which correspond to the gradient and shape of the watershed relief variable, satisfy only

Hydrological response parameter	Morphometric variable	Predictive statistical-mathematical model of sediment volumes				
Sediment volume (event of December 1999) (Vs- Dec1999 $(m3)$	Watershed scale	$Y = \beta_0 + \beta_1 X_1$ $Vs\text{-}Dec1999 = 1,664,659.595 + 387,055.437 (PC1)$				
	Gradient and shape of the watershed relief	$Y = \beta_0 + \beta_2 X_2 + \beta_3 X_3$ $Vs-Dec1999 = 1,774,218.744 + (-456,631.453(PC2)) + (-361,128.173(PC3))$				
	Watershed shape	$Y = \beta_0 + \beta_1 X_1$ $Vs\text{-}Dec1999 = 1,689,853.701 + 300,943.038 (PC1)$				
	Extension of the drainage network	$Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \beta_3 X_3$ $Vs-Dec1999 = 1,710,616.073 + (-249,259.773(PC1)) + 224,241.079(PC2)$ $+(-328.038.396(PC3))$				
Sediment volume prior to the debris flows $(Tr = 100 \text{ years})$	Watershed scale	$Y = \beta_0 + \beta_1 X_1$ $V_{\text{S}_{\text{prior-df}}} = 856,136.743 + 212,589.038(PC1)$				
$(Vs_{prior\text{-df}})(m^3)$	Gradient and shape of the watershed relief	$Y = \beta_0 + \beta_2 X_2 + \beta_3 X_3$ $V_{\text{S}_{\text{prior-df}}} = 914,395.354 + (-258,457.229(PC2)) + (-160,091.436(PC3))$				
	Watershed shape	$Y = \beta_0 + \beta_1 X_1$ $V_{\text{5}} = 869,802.192 + 178,301.838(PC1)$				
	Extension of the drainage network	$Y = \beta_0 + \beta_2 X_2$ $V_{\text{S}_{\text{prior-df}}} = 872,484 + 152,077.774(\text{PC2})$				
Sediment volume after the debris flows $(Tr = 100 \text{ years})$	Watershed scale	$Y = \beta_0 + \beta_1 X_1$ $V_{S_{\text{short}}=1} = 1,011,982.558 + 214,648.581 (PC1)$				
$(Vs_{after\text{-df}})(m^3)$	Gradient and shape of the watershed relief	$Y = \beta_0 + \beta_2 X_2 + \beta_3 X_3$ $V_{S_{\text{after,df}}}=1,073,998.700+(-266,846.725(PC2))+(-169,819.436(PC3))$				
	Watershed shape	$Y = \beta_0 + \beta_1 X_1$ $V_{\text{S}_{\text{after.}}\text{df}} = 1,025,933.695 + 188,337.200(PC1)$				
	Extension of the drainage network	$Y = \beta_0 + \beta_2 X_2$ $V_{\text{Safter,df}} = 1,028,949.535 + 155,519.996(PC2)$				

<span id="page-14-0"></span>**Table 5** Predictive statistical-mathematical models (equations) of sediment volumes

PCs 2 and 3, reaching 95% confdence intervals for β, but biased towards negative values, whereas PC 1 and 4 have been excluded from the models, since zero is included within their 95% confdence intervals for β. The watershed shape variable, of the two PCs representative of their morphometric parameters, only the frst satisfes the predictive models, with 95% confidence intervals for β, which is towards the positive values.

In the predictive models of the extension of the drainage network variable, it is perceived that for the sediment volumes parameter of the December 1999 debris flows event, the three representative PCs of the morphometric parameters satisfy these models, with the intervals of 95% confidence for  $β$  of PC 1 and 3 less than zero and that of PC 2 greater than this value. In the case of the sediment volumes before and after the December 1999 debris event, only the PC 2 satisfes the models. Therefore, PCs 1 and 3 have been discarded for the construction of such. For the order and magnitude of the drainage network variable, none of the three PCs representative of their morphometric parameters satisfes their respective predictive models, since the 95% confidence intervals for  $\beta$  in these cases include the zero value in their ranges.

### **Predictive models of debris volumes**

Predictive models with linear equations have been constructed with the PC of each morphometric variable and for each sediment volume parameter (Table [5](#page-14-0)). The magnitudes of the latter have been estimated, by comparing them later with the magnitudes taken as input data in the analysis statistics, by adjusting the Pearson's correlation coefficients  $(Table 6)$  $(Table 6)$ .

These models only worked with the watershed scale, gradient and shape of the watershed relief, watershed shape and extension of the drainage network variables. The sediment volumes from December 1999 debris flow event, its best predictive models have been represented by the gradient and shape of the watershed relief and extension of the drainage network variables, while with the watershed scale, watershed shape and order and magnitude of the drainage network variables, their correlation coefficients indicate that these models have not been very efficient as predictors. With the sediment volumes before and after the debris flows event of December 1999, only those generated with morphometric parameters of the gradient and shape of the watershed relief variable functioned as good predictive

### <span id="page-15-0"></span>**Table 6** Sediment volume magnitudes estimated with the predictive models



Bold values represent the best correlation coefficients obtained between the initial sediment volumes estimated by Córdova and González [\(2003](#page-16-2)) and those estimated by the predictive models obtained in this research

models. The rest of the morphometric variables obtained very poor quality adjustments, as evidenced by the low correlation coefficients.

# **Conclusions**

The sediment volumes, which have been previously estimated and taken as input in this study, reveal important magnitudes in the yield, transport and deposition of sediments, related to the occurrence of extreme rainfall events, clearly demonstrating the hazard. It is obvious that fash floods represent these hydro-geomorphological systems.

The LCA revealed good correlations between the sediment volumes and most of the morphometric parameters corresponding to the watershed scale variable, as well as some parameters of the gradient and shape of the watershed relief variable.

The PCA has reduced the dimensionality of the morphometric parameters groups, defning as new variables the components or factorials created for each group or initial morphometric variable.

The MLRA with PC of the morphometric variables gave very good correlation and determination indices between the sediment volumes and the PC's of the gradient and shape of the watershed relief variable, as well as good indices with the PC's of the extension of the drainage network and watershed scale variables.

For each sediment volumes parameter considered in this study, predictive models of such hydrological responses have been obtained from the MLRA. Each model responds to the PC's with a set of morphometric parameters grouped in morphometric variables. In this way, the estimations of magnitudes of the sediment volumes with the predictive models generated in this research, and compared with the magnitudes taken as input data, revealed that the most suitable models are those corresponding to the gradient and shape of the watershed relief variable.

Among some interesting aspects to develop in future research studies, related to factors and/or elements of the physical environment as predictors of the occurrence of debris fow events, we expect to: (a) analyze the particular relations morphometric parameters of the drainage networks with each of the lithological outcrops and each vegetation formation. This will support the understanding of the weight of each type of rock and vegetation in sediments production and, in its diferential contribution to the generation of debris flows; (b) to study in detail and in a comparative way the depth of the alteration profles, the volumes of regolith and its mineralogy, developed on each type of rock, to identify lithologies that contribute most in the activation of debris fows; and (c) analyze the density and depth of the root system of each vegetation formation in the soils, in

terms of the relative stability they offer to the materials of the slopes, considering the topographic slope as a conditioning element.

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