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Influences of petrographic and textural properties on the strength of very strong granitic rocks

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Abstract In this study, the petrographic characteristics affecting the strength of granitic rocks were investigated and a new mineralogical-based model was suggested for the prediction of uniaxial compressive strength (UCS) in line with the obtained data. Increase in quartz and alkali feldspar contents with decrease in plagioclase content partially increase the strength of granitic rocks. However, the results of modal analyses show that the rate of physically competent minerals do not directly affect strength of the granitic rock because the mineral size has a greater effect on strength than that of mineral type. The higher strength values were determined for the rocks containing monotype mineral in terms of size and quantity. In the scope of the study, significant relationships with a 0.89 correlation coefficient between UCS values and the Quality Index values (QI) were determined using mineral percentages, content and size. Because the modal analysis technique is a time-consuming process, ultrasonic velocity ratio (UVR) was defined in order to evaluate rock strength in the study and significant relationships were found with the correlation coefficient of 0.77 between UVR and QI. To estimate UCS using only ultrasonic wave velocity, it was determined whether there is a statistical relationship between UVR and UCS. The test result shows significant relation was found characterized with correlation

& Hakan Ersoy blavetirraa@hotmail.com Serhat Acar serhat_acar@windowslive.com coefficient of 0.84 value. UCS values obtained from the proposed equation and experimental studies were compared to test the suggested model; the results of the study showed that UCS values can be predicted without needing modal analysis with the new method proposed.

Keywords Granite · Petrographic · Texture · UCS · Ultrasonic velocity ratio

Introduction

Uniaxial compressive strength (UCS) of rock material is perhaps the main strength parameter used in almost all engineering projects related to rock environment (Cargill and Shakoor [1990](#page-13-0); Ersoy and Kanık [2012](#page-13-0)). The strength of rock material is obtained generally from compressive strength tests, especially uniaxial applied stress, which is standardized by ASTM [\(1999](#page-12-0)) on cube samples and ISRM [\(2007](#page-13-0)) on core samples in the laboratory. However, highquality and well-prepared core/cube samples with regular geometry are necessary, and gathering sufficient number of samples is the most important difficulties for this test. For this reason, the prediction models for estimating UCS from simple, non-destructive and easily applied laboratory tests have been suggested to overcome such difficulties (Kahraman [2001;](#page-13-0) Katz et al. [2000](#page-13-0); Koncagul and Santi [1999](#page-13-0); Wong et al. [1996](#page-14-0)). However, some researchers have found that sound velocity is closely related to rock prop-erties (Gaviglio [1989;](#page-13-0) Chang et al. [2006](#page-13-0); Yalçınalp et al. [2008](#page-14-0); Babacan et al. [2009;](#page-12-0) Moradian and Behnia [2009](#page-13-0); Karakul and Ulusay [2013\)](#page-13-0) while others have correlated UCS with index properties such as porosity, density and also P-wave velocity (Ramana and Venkatanarayana [1973](#page-13-0); Yasar and Erdogan [2004\)](#page-14-0).

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New statistical techniques such as analytic hierarchy process, artificial neural networks and fuzzy inference systems have also been used to estimate strength parameters (Grima and Babuska [1999](#page-13-0); Gokceoglu and Zorlu [2004](#page-13-0); Karakus and Tütmez [2006;](#page-13-0) Dehghan et al. [2010;](#page-13-0) Yagiz et al. [2011](#page-14-0); Ersoy and Kanik [2012;](#page-13-0) Mishra and Basu [2013](#page-13-0)). The development of the estimation models on the uniaxial compressive strength using petrographical characteristic of rock sample has become an attractive investigation area in rock engineering projects during recent years. Therefore, many researchers have carried out some studies in determining the strength properties of rock material by using petrographic characteristics (Tuğrul and Zarif [1999](#page-13-0); Ulusay et al. [1994](#page-13-0); Gokceoglu and Zorlu [2004;](#page-13-0) Ceryan et al. 2008 ; Zorlu et al. 2008 ; Özçelik et al. 2012).

Although some specific empirical models have been suggested and these recent trends have become attractive for engineering geologists, a general and functional model for the prediction of the UCS of rock material using index and properties for different types of rocks has not been developed in the literature (Gokceoglu [2002;](#page-13-0) Coggan et al. [2013;](#page-13-0) Heidari et al. [2013](#page-13-0); Öztürk and Nasuf 2013). Besides, very different UCS values were determined on the core and/or cube samples obtained from the same rock block by many researchers. Mineral composition and size, texture as well as porosity, the arrangement of voids (fabric) and weathering state are the most important reasons for this situation. For this aim, the granitic rocks which exposed over large areas in the eastern Black Sea Region (NE Turkey) were selected within the scope of the study (Fig. [1\)](#page-2-0) and the effects of the mineralogical parameters on uniaxial compressive strength are discussed in this paper. By using ISRM [\(2007](#page-13-0)) methods suggested on 250 rock samples obtained from nine different granite masses in Giresun, Trabzon and Rize, the index and strength tests were conducted, petrographic analyses were carried out, and the statistical relations were analyzed between obtained data. Based on the results of the statistical analysis, some general prediction models and a new approach related to mineralogical and physic-mechanical properties were suggested for very strong granitic rocks.

Regional geology and sampling location

The eastern Pontides, as an example of paleo-island arc setting, are a major metallogenetic province in the eastern Black Sea coastal region and form a 500 km long and 100 km wide mountain chain along the Black Sea coast. The eastern Pontides were subdivided into northern, eastern and axis zones on the basis of structural and lithological differences (Özsayar et al. 1981 ; Bektas et al. [1995;](#page-13-0) Okay and Sahinturk [1997](#page-13-0)). The northern zone is dominated by Late Cretaceous, Middle Eocene volcanic and volcaniclastic rocks, whereas pre-Late Cretaceous sedimentary rocks are widely exposed in the southern zone (Arslan et al. [1997](#page-12-0), [2013;](#page-12-0) Eyuboglu et al. [2011\)](#page-13-0).

In this region, there are five different lithostratigraphic units: Paleozoic Gümüşhane Granite and Pulur Metamorphites forming the basement, Early to Middle Jurassic riftrelated sediments and volcanoclastics, Late Jurassic to mid-Cretaceous platform carbonates, Middle to Late Cretaceous rift-related sediments, Eocene-Neogene volcano-sedimentary rocks (Yılmaz and Kandemir [2006](#page-14-0)). Also, in this region, plutonic rocks have a range of ages and compositions and were probably emplaced into a variety of geodynamic environments between Jurassic and Paleocene time (Okay and Sahinturk [1997;](#page-13-0) Arslan and Aslan [2006\)](#page-12-0).

Granitic intrusions in the northern zone extend NW–SE whereas those in the southern zone are nearly E–W oriented. The contacts of the intrusions with the volcanic rocks are sharp, epidotized and include volcanic xenoliths. The margins of the southern zone intrusions often contain abundant angular mafic microgranular enclaves of diorite to quartz diorite composition. Petrographically, intrusions show variations in both color and mineralogy with fine to medium granular, monzonitic, poikilitic, rapakivi, anti-rapakivi and graphic textures (Arslan and Aslan [2006\)](#page-12-0). Based on modal mineralogy, the northern rocks are monzonite, quartz monzonite, monzodiorite and quartz monzodiorite whereas the southern samples are monzogranite and granodiorite.

Within the scope of the study, granitic rocks which widely outcropped and confront in the various engineering projects in the northern zone of the eastern Pontides (NE Turkey) were analyzed. For this aim, nine different granite masses in Giresun, Trabzon and Rize in the northern zone of the eastern Black Sea Region were selected to investigate (Fig. [1\)](#page-2-0).

Petrographic observations

In the study, 165 thin sections in total from the studied granitic rocks were examined under an optical microscope (Nikon-LV 100 Pol) to determine the petrographic properties and weathering stages of each sample. The modal mineralogy of selected samples was determined by point counting with a Swift automatic counter fitted with a polarizing microscope. In each thin-section, a total of 200–250 points (0.4 mm between two points) were counted and normalized to 100%. Thus, the granitoid was classified according to the QAPF (quartz, alkali feldspar, plagioclase, feldspathoid) diagram for coarse-grained plutonic rocks and was named according to the percentage of quartz, alkali feldspar and plagioclase on the QAP half of the

Fig. 1 Granitic rocks exposed in the eastern Black Sea Region (NE Turkey) and the sampling locations

diagram (Fig. [2\)](#page-3-0). The main rock types, mineralogical compositions and textural features of the studied granitic rocks are summarized in Table [1](#page-4-0).

The studied rocks include a wide variety of rock types such as syenogranite, monzogranite, granodiorite, tonalite, monzonite, quartz monzonite, quartz monzodiorite. Petrographically, granitic rocks show variations in terms of color, texture and mineralogy. The modal mineralogy is mainly 19–46% plagioclase, 6–40% orthoclase, 25–37% quartz, 4–18% mafic minerals such as hornblende, augite, biotite and 1% opaques. Chlorite, sericite, epidote and calcite are secondary. Generally, they have monzonitic, graphic and rarely myrmekitic textures and range from fine to medium-coarse-grained rocks (Fig. [3\)](#page-5-0). The samples may contain abundant medium-fine grained plagioclase, biotite, hornblende and opaques. Plagioclase occurs as euhedral to subhedral crystals, and a myrmekitic texture is observed at the contact between orthoclase and plagioclase. Some large plagioclase crystals are alterated to sericite. Orthoclase mainly occurs as subhedral large crystals, and quartz is subhedral to anhedral with irregular internal cracks. Hornblende and biotite are the main mafic phase in the studied samples. The modal mineralogy and mineral size of selected samples from the granitic rocks are given in Table [2](#page-6-0).

Granitic rocks with granular and phaneritic in texture are a common type of intrusive, felsic, igneous rocks. These rocks consisting of predominantly of alkali feldspar, plagioclase and quartz are a variety of coarse-grained plutonic rock. Alkali feldspar and quartz are physically competent minerals, but having the competent minerals does not mean that the rock is so hard. In accordance with the findings obtained from mineralogical-based analysis, it is not feasible to clearly speak of an effect of rock forming minerals on rock strength. However, it is likely to mention that the increase in the rate of alkali feldspar and the decrease in the

Fig. 2 Classification of the studied granitic rocks based on QAP modal mineralogy

rate of plagioclase may partially increase rock strength. Figure [4](#page-6-0) shows the uniaxial compressive strength increase with the increase in quartz and alkali feldspar and decreasing plagioclase. Thus, there is a positive correlation between UCS and A/P. This gives an indication that the percentage of only quartz may not play an important role to determine the UCS of the studied granitic rocks.

Sample preparation and laboratory tests

An experimental program was conducted on rock cores for determination of both physical and strength properties of granitic rock materials. For that purpose, a total of twenty oriented block samples were collected from the nine different granitic bodies for laboratory testing and 250 NX-size core specimens having a 2.5:1 length to diameter ratio were prepared from the block samples. Rock samples were carefully inspected before testing, and the freshest and most representative samples from granitic rocks (163 samples) were selected to perform index and strength properties based on petrographical studies. Unit weight, water absorption by weight, apparent porosity and uniaxial compressive strength (UCS) were measured according to the ISRM [\(2007](#page-13-0)). A Pundit Plus ultra-sonic pulse instrument giving more precise rock sample measurements and two 54 kHz transducers having piezoelectric properties were used in this study to calculate ultrasonic longitudinal wave velocity.

Table 1 General mineralogical and petrographical characteristics of the studied granitic rock groups

Sample	Location	Texture	Mineralogy	Rock name		
	<i>Ikizdere</i> (Rize)	Porphyric monzonitic	Plagioclase, quartz, orthoclase, hornblende and biotite	Monzogranite, granodiorite		
2	<i>Ikizdere</i> (Rize)	Microlitic Porphyric	Plagioclase, quartz, orthoclase, hornblende, chloride, sphene	Monzogranite, syenogranite		
3	Ilicaköy (Rize)	Porphyric	Plagioclase, quartz, orthoclase, hornblende, biotite chloride, sericite	Monzogranite, granodiorite, quartz monzonite		
4	<i>Ikizdere</i> (Rize)	Microlitic Porphyric	Plagioclase, quartz, orthoclase, Hornblende, biotite	Monzogranite, granodiorite		
5	Caykara (Trabzon)	Porphyric monzonitic	Plagioclase, quartz, orthoclase, hornblende, biotite, chloride	Monzogranite, granodiorite		
6	Caykara (Trabzon)	Porphyric	Plagioclase, quartz, orthoclase, hornblende, biotite, chloride, epidote	Monzogranite, granodiorite		
7	Dereli (Giresun)	Microlitic, Porphyric	Plagioclase, quartz, orthoclase, hornblende, biotite, chloride,	Syenogranite, monzogranite		
8	Hemsin (Rize)	Porphyric	Plagioclase, quartz, orthoclase, hornblende, biotite, chloride, epidote, sericite	Granodiorite, tonalite		
9	Ilicaköy (Rize)	Microlitic, Porphyric	Plagioclase, quartz, orthoclase, hornblende, biotite, chloride,	Granodiorite, monzogranite		

Table [3](#page-7-0) provides a summary of the physical properties of the granitic rock samples. The value of water absorption by weight varied from 0.14 to 0.56% and apparent porosity ranged between 0.38 and 1.47% for all samples. The unit weight of the granitic rocks fluctuated between 22.80 and 26.66 kN/m³ for a dry condition, and these values ranged between 22.88 and 26.72 kN/m³ for saturated condition. Depending more on the mineral shapes and occurrence of the microcracks and less on weathering features, the UCS values varied in a wide range as found in the study. While the minimum and maximum UCS values of the rock materials are 64 and 261 MPa, respectively, the average UCS values for all rock groups are between 134 and 211 MPa (Table [4\)](#page-7-0).

In the study, the ultrasonic tests were also conducted for saturated and dry conditions. The minimum and maximum values of P-wave velocity for dry samples are 3163 and 5742 m/s; these values are 3759 and 5888 m/s for saturated condition, respectively, for all samples. The average value of P-wave velocity of the rock groups for dry condition ranged from 3888 and 4584, and 4407 and 5324 m/s for saturated condition (Table [4](#page-7-0)).

Rock materials are generally classified based on their strength values, especially from uniaxial compressive strength (Singh and Goel [2011\)](#page-13-0). However, the mineralogical properties and also P-wave velocity can be often used for both predicting the rock material properties and evaluating of weathering degree (Bell [2007\)](#page-13-0). Some definitions based upon the ultrasonic velocities and UCS of the rock material for the recognition of weathering grades for granitic rock were proposed (Iliev [1967](#page-13-0); Brown [1981](#page-13-0); Bieniawski [1974](#page-13-0)). Considering to these research, more than 90% of all rock samples are classified as fresh/slightly weathered and strong/very strong.

Statistical relations between UCS and index properties

The uniaxial compressive strength of rock materials greatly depends on their index properties such as porosity, water absorption and mineral composition. One of the most important measurements to assess the strength properties of the granitic rock is P-wave velocity (Sachpazis [1990](#page-13-0); Tuğrul and Zarif [1999;](#page-13-0) Palchik [1999](#page-13-0); Ceryan et al. [2008](#page-13-0); Karakul and Ulusay [2013\)](#page-13-0). Thus, there has been an upward trend on the prediction of UCS; therefore, many researchers have carried out studies in determining the strength characteristics of rock material more easily and in shorter time by simple index properties. Regression analysis is usually preferred for establishing the statistical relationships between these variables. Relationship intensity of between variables is defined by regression values and correlation coefficients. As regression analysis provides a means of summarizing the relationship between variables, simple regression analysis-based methodology was used to establish some numerical relationships among ultrasonic wave velocity, apparent porosity and UCS of

Fig. 3 Microphotographs of the studied granitic rocks (P: Plagioclase, Q: quartz, AF: orthoclase, H: hornblende, B: biotite, E: epidote)

rock materials. In the methodology, while the UCS and V_p are depending variable, index properties were considered to be explanatory variables. According to the regression analysis results, V_{p} and UCS decrease with increased apparent porosity and water absorption by weight. The relationships with some negative correlations were

Table 2 Modal mineralogy/mineral composition and mineral size of the studied granitic rock groups

Fig. 4 Relationship between mineral content and UCS of the studied rocks

characterized by 0.85, 0.87 and 0.82 correlation coeffi-cients (Fig. [5a](#page-8-0)–c). Thus, UCS and V_p were considered as a depending and explanatory variables, respectively, for the determination of the relationship between UCS and V_p . Figure [5](#page-8-0)d shows some positive correlations between UCS and V_p , and the relationships were characterized by 0.80 correlation coefficients.

Construction of the mineralogical-based methodology

The ultrasonic wave velocity of rock materials is directly affected by mineralogical properties and micro-fissure ratio. Thus, petrographical and longitudinal wave velocity based methodology was suggested by Fourmaintraux

Table 3 Some index properties of the studied granitic rocks

Sample groups	Water absorption by weight $(\%)$				Apparent porosity $(\%)$			Unit weight $(dry, %)$			Unit weight (saturated, $\%$)					
	Max.	Min.	SD.	Ave.	Max.	Min.	SD.	Ave.	Max.	Min.	SD.	Ave.	Max.	Min.	SD.	Ave.
1(n: 18)	0.32	0.26	0.03	0.28	0.82	0.66	0.08	0.73	26.36	24.66	0.8	25.5	26.43	24.73	0.9	25.5
2(n: 19)	0.38	0.32	0.03	0.35	1.01	0.84	0.09	0.91	25.92	24.83	0.6	25.3	26.02	24.92	0.6°	25.3
3(n: 17)	0.42	0.27	0.08	0.32	1.11	0.72	0.20	0.84	26.03	24.48	0.8	25.6	26.12	24.56	0.8	25.6
4(n: 20)	0.41	0.32	0.05	0.36	1.08	0.81	0.14	0.93	25.89	22.80	1.4	25.3	25.99	22.88	1.5	25.4
5(n: 15)	0.56	0.42	0.07	0.45	1.47	1.11	0.19	1.18	25.90	25.09	0.4	25.7	26.05	25.20	0.3	25.8
6(n: 17)	0.48	0.27	0.10	0.37	1.24	0.70	0.24	0.96	26.52	25.14	0.6°	25.6	26.62	25.23	0.7	25.7
7(n: 21)	0.34	0.21	0.07	0.26	0.88	0.54	0.16	0.68	26.35	25.33	0.5	25.8	26.43	25.39	0.4	25.9
8(n:18)	0.29	0.14	0.07	0.22	0.78	0.38	0.19	0.58	26.66	25.71	0.5	26.1	26.72	25.74	0.5	26.2
9(n: 18)	0.55	0.35	0.10	0.49	1.47	0.91	0.23	1.30	26.46	25.35	0.6°	25.9	26.59	25.48	0.6	26.0

Table 4 P-wave velocity (dry and saturated conditions) and UCS values of the granitic rocks

[\(1976](#page-13-0)) to determine the degree of the micro-fissure and the related ''Quality Index (QI)'' of rocks. QI is related to the ratio of the micro-fissure (directly weathering degree) especially for granitic rocks contrary to their mineral content. Using petrographic techniques, a weathering classification from fresh to residual soils was also established by Ceryan et al. ([2008\)](#page-13-0) based on the percentage of secondary minerals, microcracks and voids. Quality Index is the ratio of the measured longitudinal velocity of the samples to velocity calculated on a basis of the mineralogical composition and is calculated with the following equation.

$$
QI(\%) = \frac{V_1}{V_1^*} \times 100
$$
 (1)

where QI: Quality Index, V_1 : measured P-wave velocity of rock sample, V_1^* : calculated P-wave velocity of fresh and unfissured rock. If the mineralogical content of the rock material is known, V_1^* can be calculated with the following equation.

$$
\frac{1}{V_1^*} = \sum_{i} \frac{C_i}{V_{1,i}} \tag{2}
$$

where $V_{1,i}$: P-wave velocity of "mineral i" (Quartz = 6050 m/s, alkali feldispar = 5800 m/s; plagioclase $= 6250$, mafic minerals $= 6500$ according to Four-maintraux [1976\)](#page-13-0) and C_i : volumetric rate of "mineral i" in the rock (modal analysis).

In this study, QI values were calculated and fissuring degree of granitic rocks was determined for all samples using the results obtained (Fig. [6a](#page-9-0)). Thus, weathering classification of the rocks based on secondary mineral and percentage microcracks and voids was carried out (Fig. [6b](#page-9-0)). These analyses indicated that more than 95% of all samples of the rocks are fresh and more than 50% of the granitic rocks are unfissured and slightly fissured.

In this study, certain numerical relations between UCS and Quality Index values of the fresh granitic rocks were established to achieve more rapid and practical solutions for the prediction of UCS values. According to the regression analysis results, a positive linear relation was observed (Fig. [6](#page-9-0)c). The relationship is characterized by a correlation coefficient of 0.89 and is represented by the following formulas.

$$
UCS = 2.6QI - 19\tag{3}
$$

Fig. 5 Statistical relationships among some physico-mechanical properties of the studied granitic rocks

where UCS: uniaxial compressive strength (MPa) and QI: Quality Index (%).

A rock's strength can be dependent on many different factors such as micro-fissure ratio, the state of weathering, mineral composition, structure and texture. The previous studies on rock material indicate that the rocks containing large amounts of physically competent minerals are obvi-ously strong (Tuğrul and Zarif [1999](#page-13-0); Gokceoglu and Zorlu 2004 ; Özçelik et al. 2012 ; Gokceoglu 2002 ; Heidari et al. 2013 ; Öztürk and Nasuf 2013). The results of these said aforementioned studies show that weathering changes hard minerals into softer ones and loosens up the structure of a rock. Thus, the cohesive strength can be lost with the high micro-fissure ratio.

The statistical relationship among UCS, mineral content and average mineral size was investigated to determine the effect of mineral content and size on the uniaxial compressive strength of the studied granitic rocks (Fig. [7](#page-10-0)a, b). The modal mineralogy shows that the average quartz, plagioclase and orthoclase contents ranged between 25–34, 16–46 and 6–40%, respectively. The content of mafic minerals such as hornblende, augite, biotite is less than 15%. In taking note of the petrographic observations on 165 thin sections, it is realized that mafic minerals were subjected to chemical weathering (moderately) which was separate of the other minerals. The mineralogy-based analysis results on granitic rocks show that strength decreases with mafic mineral content and increases with the alkali feldspar ratio (except group 8). Grain size analysis result shows that the size of quartz and plagioclase ranged between 1 and 2 mm and the size of alkali feldspar is between 1 and 4 mm. Although increasing the quartz amount is considered to lead to a strength increase, contrary to this, the most important parameters effecting on UCS values are alkali feldspar amount and size for the granitic rocks that were studied.

Also, because the mineral composition and UCS do not directly show a significant statistical relation (Figs. [4b](#page-6-0), [7a](#page-10-0)), multiple regression analysis could not be carried out between them. For this reason, for estimation of UCS values of granitic rocks, micro-fissure and weathering properties-based methodology was chosen for the study.

Fig. 6 Distribution of the rock types investigated on the classification scheme for fissuring developed by Fourmaintraux [\(1976](#page-13-0)) (a) and proposed by Ceryan et al. ([2008\)](#page-13-0) (b). Positive linear relation between UCS and QI (c)

The relationships between the UCS and V_p have been generally established only for dry condition, and the effect of saturation on test results was generally ignored (Kahraman [2001;](#page-13-0) Yasar and Erdogan [2004](#page-14-0); Karakus¸ and Tütmez [2006](#page-13-0); Cobanoglu and Celik [2008;](#page-13-0) Sarkar et al. [2012;](#page-13-0) Karakul and Ulusay [2013](#page-13-0)). Only in a few studies, two conditions (dry and saturated) were regarded and the results of the studies indicated that the effect of saturation of these properties is considerably different (Török and Vasarhelyi [2010](#page-13-0)). The differences are considered as a result of the mineralogical properties and the porosity of the rock materials. Thus, the study focuses on the correlation between UCS and V_p of various granitic rocks under saturated and dry condition because the experimental results indicated that strength properties of the rocks changed with different saturation conditions. A new model based on ultrasonic wave velocity that is related to the mineralogical properties of the granitic rock materials was proposed. For this purpose, the saturated and dry ultrasonic wave velocities were used in the determination of Quality

Index of granitic rocks (Fig. [7c](#page-10-0)) and ultrasonic velocity ratio (UVR) was defined as below:

$$
UVR = \frac{[V_{p}(s) - V_{p}(d)]}{V_{p}(d)}
$$
\n(4)

where UVR: ultrasonic velocity ratio, $V_p(s)$ and $V_p(d)$ are p-wave velocities for saturated and dry conditions.

According to the regression analysis results, a negative logarithmic relation was observed between UVR and QI. The relationship is characterized by a correlation coefficient of 0.77. In this case, if saturated and dry sonic velocity values of the rock are known, the Quality Index values of fresh granitic rocks can be defined with the equation below.

In addition to this, the determination of the mineral content of granitic rocks through modal analysis is timeconsuming and also requires expertise. Therefore, in this study the graphic below was suggested for estimation of Quality Index values and thereby UCS values of rocks (Fig. [8\)](#page-11-0). As it is seen in the graphic, if ultrasonic velocity

Fig. 7 Effect of the mineral content and size on UCS of the very strong granitic rocks (a, b) and relationship between Quality Index value and proposed ultrasonic velocity ratio of the studied rocks (c)

ratio of the very strong granitic rock is known, the uniaxial compression values can be calculated with the formula below:

$$
UCS = 116 - 33.8 \text{UVR}(r = 0.84) \tag{5}
$$

where UCS (MPa), UVR: ultrasonic velocity ratio (Eq. [4](#page-9-0)). It should be noted that this proposed formula can be used for only stronger to very stronger samples $[V_p(-)]$ s) > 4000 m/sn and/or $V_p(d)$ > 5000 m/sn] (Ersoy et al. [2014\)](#page-13-0).

The significance of the r values was evaluated by the t test at a confidence level of 95%. As shown in Table [5](#page-11-0), it is concluded that there is a significant relationship between UCS and UVR.

Model testing

There are statistically significant relationships with a correlation coefficient of 79% between the UCS and Quality Index of the fresh granitic rocks. However, there are the relationships with a correlation coefficient of 77% between Quality Index and ultrasonic velocity ratio. Nevertheless, there is a need for testing the usability of the strength parameters that have been determined statistically. A goodness of fit test establishes whether an observed frequency distribution differs from a theoretical distribution; however, a model's suitability is tested using the difference between observed and expected values. The normal distribution is a continuous probability distribution which is often used as a first approach for describing real-valued random variables tending to cluster around a single mean value. A normal distribution would thus be expected in the histograms showing the difference between observed and expected values.

For this purpose, the experimental program was conducted again on rock cores for determination of the meaningful relation between the UCS values obtained from compressive strength tests and the calculated UCS values using proposed graphs/equations. A total of thirteen oriented samples were collected from the three different granitic bodies for laboratory testing. Uniaxial compressive strength (UCS) and ultrasonic wave velocity for saturated Fig. 8 Suggested graph to predict UCS values from the petrographic based methodology

Table 5 Significance of the r value

^a Correlation is significant at the 0.01 level (2-tailed)

and dry conditions were measured according to the ISRM [\(2007](#page-13-0)). After the tests, the UCS values of same samples were calculated using the proposed graph. Table [6](#page-12-0) provides a summary of the test results of the granitic rock samples. Line-scatter plot diagrams of the calculated with model and experimentally measured values were prepared. The UCS values calculated with the two different methods were compared, and it was observed that there was a statistically significant relation between the different methods. The correlation values were found to be 0.84 for these statistical relations (Fig. [9\)](#page-12-0). The results showed that the proposed model was suitable for the fresh granitic rocks.

Conclusion and discussion

This study is related to discussion of the petrographic properties affecting on the strength of the very strong granitic rocks, determination of the statistical relations between the petrographical characteristics and UCS of these rocks, and a new approach on mineralogical/textural based predictive model for the indirect estimation of UCS for these rocks was proposed in the study.

The texture of granitic rocks is commonly granular and phaneritic, and main minerals of these rocks are alkali

Table 6 Summary of the test results for model testing

N ₀	Location	$V_{\rm p}$ (m/s)		UVR	UCS (MPa)			
		Saturated	Dried		Calculated	Measured		
1	Caykara	4835	4173	0.16	178	170		
2	Caykara	4778	3969	0.20	170	145		
3	Caykara	4795	4104	0.17	176	162		
4	Caykara	5174	4311	0.20	170	169		
5	Dereli	5203	4372	0.19	172	146		
6	Ikizdere	4891	4291	0.14	182	153		
7	Caykara	4878	4031	0.21	169	171		
8	Ikizdere	6015	5630	0.07	207	220		
9	<i>İkizdere</i>	6028	5689	0.06	211	200		
10	Ikizdere	5875	5300	0.11	191	185		
11	Dereli	4839	3987	0.21	168	137		
12	Dereli	4909	4279	0.15	181	181		
13	Ikizdere	5201	4701	0.11	192	207		

Fig. 9 Line-scatter plot diagrams for measured UCS (using experimental values) compared to calculated UCS (using proposed formula)

feldspar, plagioclase and quartz. Quartz and alkali feldspar content is not the only determining parameters on UCS values of these rocks. Although these minerals are physically competent minerals, increase in the quartz and alkali feldspar may partially increase rock strength.

The point to take into consideration is that contrary to general belief, the increase in the rate of quartz mineral will not equally increase rock strength. As is known, granitic rocks consist of minerals with different resistances and quartz is a rigid mineral with a high level of elasticity module. Quartz mineral, with a higher hardness, does not keep the rock structure together, but instead, it causes a rock fraction along the minerals by pressuring on the ones with lower resistances. This condition is clearly observed in the study.

Smaller granular sizes within basalt and gabbro rocks, which consist of only one type of mineral, are known to increase rock strength (Goodman [1989](#page-13-0); Johnson and Degraff [1988](#page-13-0)). However, in granitic rocks which are the subject of this study, equal sizes of rock forming minerals decrease rock strength. The reason for this condition is that in rocks with equal size minerals with different hardness rates, the rock strength is controlled by minerals with lower strength. Particularly, when it is considered that the increase in the sizes of alkali feldspar minerals increases rock strength, under the conditions where the rock behavior is controlled by only one type of mineral, the rock strength is determined to be higher.

In this study, the uniaxial compressive strength (UCS) was predicted using the Quality Index (QI) values obtained from the mineral percent and P-wave velocity, and a correlation coefficient was determined as 0.84. However, the significant relationship between QI and UVR was investigated with the correlation coefficient of 0.77. Although both models have high correlation coefficient values, these models are very time-consuming because modal analysis is necessary to determine QI values. For this purpose, a new predictive model ''ultrasonic velocity ratio'' (UVR) was defined in the study for determination of the Quality Index of granitic rocks using the saturated and dry ultrasonic wave velocities, Furthermore, a new graphic was proposed in this study for the estimation of Quality Index values and thereby UCS values of rocks. The obtained correlation coefficient with 0.784 between UVR and UCS was tested using t test, and the significant relationship was obtained between QI and UVR.

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