ORIGINAL ARTICLE



# Divisions based on groundwater chemical characteristics and discrimination of water inrush sources in the Pingdingshan coalfield

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Abstract Within the Pingdingshan coalfield, the spatial distribution characteristics of key groundwater chemical components were studied in four aquifers that influence coal-mining operations. Thirty-six water samples were collected from the four aquifers, which were divided into smaller units. Discriminant models of mine-water inrush sources were developed for the three divisions I, II<sub>I</sub>, and II<sub>II</sub>, and engineering verification was conducted. The results showed that the main indices influencing groundwater chemical characteristics were  $Na^++K^+$ ,  $Ca^{2+}$ , Mg<sup>2+</sup>, Cl<sup>-</sup>, SO<sub>4</sub><sup>2-</sup>, and HCO<sup>3-</sup> in the Pingdingshan coalfield with regional variations according to faults and synclines. The Guodishan fault was the primary groundwater chemical division structure, which divides the Pingdingshan coalfield into two primary groundwater chemically characteristic units, divisions I and II. The Likou syncline was the secondary groundwater chemically characteristic structure, which divides division II into two secondary groundwater chemically characteristic units:

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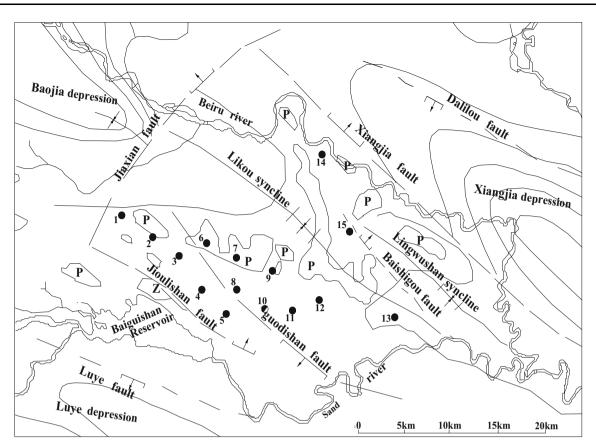
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divisions  $II_I$  and  $II_{II}$ . Discriminant models of water inrush sources in divisions I,  $II_I$ , and  $II_{II}$  (12 discriminant functions) were developed, and engineering verification showed that discrimination accuracy for 16 groundwater samples in four aquifers of three divisions was 93.75 %.

**Keywords** Geological characteristics · Key groundwater chemical components · Distribution law · Detail division · Water inrush source · Discriminant models

## Introduction

Water disasters are a serious threat to mining safety. Finding water inrush sources and approaches is the basis of water disaster control, and discriminating water inrush sources accurately is a prerequisite for finding water inrush approaches. The study of element sources and transport in subterranean waters in different geological environments combines the disciplines of water chemistry and hydrogeology (Wang et al. 2012; Huang et al. 2012; Masaoki et al. 2014; Rajesh et al. 2012; Frondini et al. 2014; Srinivasamoorthy et al. 2014; Kuldip et al. 2011; Chidambaram et al. 2013). Recently, discriminating water inrush sources based on chemical characteristics has been a research focus using both quantitative and semi-quantitative methods (Clemens et al. 2002; Zhuk and Serikova 2005; Li 2008; Huang and Chen 2011a, b; Wang et al. 2011; Zhou et al. 2010). Discriminant models have been widely used for identifying water inrush sources, but the accuracy decreases in complex hydrogeological coalfields (Vittecoq et al. 2014; Lavoie et al. 2014; Lahcen et al. 2004), and thus the pertinence and effectiveness of water inrush prevention and control strategies reduce. Based on coalfield geological characteristics, every aquifer influencing coal-mining



**Fig. 1** Structural outline map of the Pingdingshan coalfield. *Numbers* show mine area, 1 was the Xiangshan mine, 2 the eleventh mine, 3 the ninth mine, 4 the fifth mine, 5 the seventh mine, 6 the sixth mine, 7 the fourth mine, 8 the third mine, 9 the first mine, 10 the second mine,

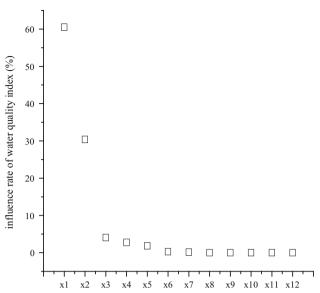
11 the tenth mine or Wuzhai mine, 12 the twelfth mine, 13 the eighth mine, 14 the thirteenth mine, and 15 the Shoushan mine. P was Permian, and Z profile

|    | K <sup>+</sup> +Na <sup>+</sup> | Ca <sup>2+</sup> | Mg <sup>2+</sup> | Cl <sup>-</sup> | $SO_4^{2-}$ | HCO <sub>3</sub> <sup>-</sup> | Total<br>hardness | Permanent<br>hardness | Temporary hardness | Total<br>alkalinity | Salinity | рН   |
|----|---------------------------------|------------------|------------------|-----------------|-------------|-------------------------------|-------------------|-----------------------|--------------------|---------------------|----------|------|
| 1  | 809.60                          | 4.80             | 15.07            | 151.02          | 143.12      | 1796.42                       | 74.00             | 0.00                  | 74.00              | 1472.00             | 2920.03  | 8.30 |
| 2  | 1109.73                         | 15.63            | 8.88             | 94.66           | 24.98       | 2498.77                       | 26.95             | 0.00                  | 26.95              | 830.82              | 3923.80  | 8.40 |
| 3  | 1036.85                         | 10.42            | 1.22             | 64.17           | 4.80        | 2288.25                       | 31.03             | 0.00                  | 31.03              | 2176.87             | 3614.37  | 8.40 |
| 4  | 284.16                          | 13.03            | 7.05             | 31.56           | 4.94        | 768.84                        | 61.58             | 0.00                  | 61.58              | 630.60              | 1109.58  | 7.80 |
| 5  | 321.34                          | 3.80             | 1.38             | 81.52           | 21.13       | 599.42                        | 15.53             | 0.00                  | 15.53              | 575.95              | 1080.37  | 8.10 |
| 6  | 68.31                           | 57.72            | 23.35            | 18.08           | 94.14       | 329.50                        | 239.88            | 0.00                  | 239.88             | 269.86              | 592.50   | 7.50 |
| 7  | 158.24                          | 167.13           | 173.4            | 30.49           | 1335.23     | 52.48                         | 1129.42           | 1085.52               | 43.90              | 43.01               | 1917.53  | 6.30 |
| 8  | 31.27                           | 76.35            | 11.07            | 21.27           | 46.50       | 277.03                        | 237.74            | 10.53                 | 227.21             | 227.21              | 464.09   | 7.80 |
| 9  | 14.02                           | 76.18            | 12.64            | 19.01           | 40.33       | 248.96                        | 242.20            | 38.02                 | 204.18             | 204.18              | 411.14   | 7.40 |
| 10 | 14.25                           | 73.21            | 13.98            | 18.53           | 39.09       | 249.57                        | 240.23            | 35.52                 | 204.72             | 204.72              | 411.63   | 7.50 |

operations were divided into smaller sections according to chemical distribution. Then, a water inrush source discriminant model was developed for every division and was found to have strong pertinence and high discriminant accuracy.

According to hydrogeological conditions in the Pingdingshan coalfield, this study analyzed the

groundwater chemical characteristics of four aquifers influencing mining activities, determined their key groundwater chemical components, divided the four aquifers into key chemical component divisions by analyzing 36 groundwater samples, constructed a three-division discriminant model of water inrush sources, and performed engineering verification using 16 test samples. The results



water quality index

**Fig. 2** Groundwater-quality index weights for the Pingdingshan coalfield. Na<sup>+</sup>+K<sup>+</sup>, Ca<sup>2+</sup>, Mg<sup>2+</sup>, Cl<sup>-</sup>, SO<sub>4</sub><sup>2-</sup>, HCO<sub>3</sub><sup>-</sup>, total hardness, permanent hardness, temporary hardness, total alkalinity, salinity, and pH were, respectively, defined as variables  $x_1$ ,  $x_2$ ,  $x_3$ ,  $x_4$ ,  $x_5$ ,  $x_6$ ,  $x_7$ ,  $x_8$ ,  $x_9$ ,  $x_{10}$ ,  $x_{11}$ , and  $x_{12}$ 

provide a reference for correct discrimination of water inrush sources.

### **General Situation**

The Pingdingshan coalfield is located in the eastern extension of a latitudinal structural zone in the Qinling Mountains and an E-type reflex arc top in the northwest wing of Huanyang Mountain. This area is a complex of latitudinal and E-type structures and forms a series of northwest compound folds in which main northwest tension–torsion and compression–torsion faults and secondary northeast tension–torsion faults control the coalfield structure. At present, the Xiangshan mine and the first through twelfth mines are located in the shallow south to Likou syncline, with the thirteenth mine and the Shoushan mine in the north to Likou syncline. The Guodishan fault forms a natural boundary between the third, fourth, and sixth mines and the seventh, ninth, and eleventh mines (Fig. 1).

The main mining seams in the Pingdingshan coalfield are the Taiyuan formation of the Carboniferous and the Shanxi and Xiashihezi formations of the Permian. The main aquifers influencing mining are composed of uppermiddle thick Cambrian limestone, thin Taiyuan formation carboniferous limestone, Permian sandstone, and Quaternary gravel (Wang and Li 1992). Upper Middle Cambrian and Taiyuan formation carboniferous limestone aquifers are both direct and indirect water-filling sources of the Ji mining seam. Recharge conditions of Permian sandstone aquifers are worse because they are recharged by loose sand-gravel pore water at the bottom of the Quaternary and fissure weathering water through outcrops, and the degree of water penetration appears to show regional discrepancies due to fractures and faults. Sand-gravel Quaternary aquifers are recharged by precipitation and surface water, and their degree of water penetration is more affected by mining and the seasons.

The southwestern portion of the coalfield is a recharge area, whereas the eastern portion is a runoff area, and runoff is slow. The Cambrian and Carboniferous aquifers accept surface water infiltration directly or indirectly from the Quaternary and Permian and form a runoff trend from southwest to northeast. Before large-scale mining in the Pingdingshan coalfield, natural groundwater discharge was the main runoff mechanism. With increases in mining scale, long groundwater discharges form hydrophobic drop funnels around every mine, which compound each other from east to west, forming a long narrow shape from northwest to southeast, and have become the principal means of groundwater discharge from the mine area.

#### **Component selection**

Underwater chemistry is complex due to the occurrence environment, geological structure, and recharge conditions (Jin et al. 2001; Alexander et al. 2009; Pierre et al. 2014; Soren et al. 2008). Accurate selection of key groundwater chemical components is a prerequisite for dividing up the hydrogeological units and constructing discriminant models of water inrush sources.

Recharge water sources directly affect groundwater chemical components and, therefore, sample points for determining key chemical components should be located in groundwater recharge areas. The main aquifer recharge area is located in a bare Neogene limestone zone in the southwestern part of the Guodishan fault and, therefore, Permian samples from this area can serve to represent and analyze key groundwater chemical components in the Pingdingshan coalfield.

Using 10 groundwater samples from the ninth, fifth, and seventh mines, 12 water-quality indices, including  $Na^++K^+$ ,  $Ca^{2+}$ ,  $Mg^{2+}$ ,  $Cl^-$ ,  $SO_4^{2-}$ ,  $HCO_3^-$ , total hardness, permanent hardness, temporary hardness, total alkalinity, salinity, and pH, were monitored (Table 1). The weights of these 12 water-quality indices were analyzed using the SPSS statistical software, and the resulting groundwater-quality index weights are shown in Fig. 2.

Figure 2 shows that the main groundwater-quality indices are the first six chemical components in the water,

Table 2 Analytical data for 25 samples on key groundwater chemical components

| Aquifer       | Mine       | No. | Coordinate |           | $K^++Na^+$ | Ca <sup>2+</sup> | $Mg^{2+}$ | $Cl^{-}$ | $SO_4^{2-}$ | $HCO_3^-$ |
|---------------|------------|-----|------------|-----------|------------|------------------|-----------|----------|-------------|-----------|
|               |            |     | X          | Y         | (mg/L)     | (mg/L)           | (mg/L)    | (mg/L)   | (mg/L)      | (mg/L)    |
| Quaternary    | Ninth      | 3   | 38,425,484 | 3,741,341 | 100.97     | 114.63           | 16.65     | 64.52    | 310.75      | 194.65    |
|               | Seventh    | 5   | 38,430,608 | 3,736,734 | 52.9       | 201.8            | 24.18     | 62.39    | 298.75      | 389.31    |
|               | Sixth      | 6   | 38,429,816 | 3,742,702 | 50.83      | 216.83           | 30.25     | 136.84   | 196.92      | 461.31    |
|               | Tenth      | 11  | 38,439,494 | 3,738,439 | 19.78      | 176.95           | 22.72     | 52.47    | 227.18      | 326.46    |
|               | Thirteenth | 14  | 38,442,571 | 3,750,766 | 11.15      | 122.24           | 27.76     | 48.11    | 46.18       | 391.33    |
|               | Shoushan   | 15  | 38,445,834 | 3,743,743 | 14.49      | 171.94           | 10.57     | 70.55    | 119.59      | 341.71    |
| Permian       | Ninth      | 3   | 38,425,484 | 3,741,341 | 809.6      | 4.8              | 15.07     | 151.02   | 143.12      | 1796.42   |
|               | Fifth      | 4   | 38,428,890 | 3,740,353 | 1073.29    | 13.03            | 5.05      | 79.415   | 14.89       | 2393.51   |
|               | Seventh    | 5   | 38,430,608 | 3,736,734 | 224.60     | 24.85            | 10.59     | 43.72    | 40.07       | 565.92    |
|               | Sixth      | 6   | 38,429,816 | 3,742,702 | 600.28     | 7.28             | 12.15     | 101.82   | 86.92       | 1162.06   |
|               | Forth      | 7   | 38,432,077 | 3,740,188 | 35.19      | 79.62            | 24.69     | 26.83    | 58.18       | 328.18    |
|               | Thirteenth | 14  | 38,442,571 | 3,750,766 | 391.13     | 16.8             | 10.33     | 54.137   | 178.50      | 671.14    |
| Carboniferous | Xiangshan  | 1   | 38,421,062 | 3,744,778 | 29.9       | 106.95           | 42.24     | 47.50    | 123.12      | 379.27    |
|               | Eleventh   | 2   | 38,424,402 | 3,743,841 | 29.58      | 106.54           | 19.71     | 27.83    | 101.27      | 284.96    |
|               | Seventh    | 5   | 38,430,608 | 3,736,734 | 34.11      | 88.99            | 13.27     | 26.16    | 64.41       | 289.41    |
|               | Tenth      | 11  | 38,439,494 | 3,738,439 | 400.22     | 21.77            | 7.99      | 91.68    | 53.01       | 817.40    |
|               | Twelfth    | 12  | 38,442,149 | 3,738,563 | 88.4       | 66.42            | 24.84     | 112.01   | 144.86      | 159.99    |
|               | Thirteenth | 14  | 38,442,571 | 3,750,766 | 270.67     | 18.94            | 8.75      | 58.86    | 59.56       | 584.26    |
|               | Shoushan   | 15  | 38,445,834 | 3,743,743 | 374.22     | 22.48            | 13.74     | 92.47    | 102.95      | 809.11    |
| Cambrian      | Seventh    | 5   | 38,430,608 | 3,736,734 | 36.02      | 64.50            | 29.11     | 25.70    | 62.96       | 260.88    |
|               | Tenth      | 11  | 38,439,494 | 3,738,439 | 240.56     | 44.21            | 30.71     | 63.93    | 248.15      | 432.21    |
|               | Twelfth    | 12  | 38,442,149 | 3,738,563 | 106.90     | 51.60            | 25.54     | 90.37    | 29.07       | 392.31    |
|               | Eighth     | 13  | 38,447,363 | 3,735,660 | 133.39     | 54.98            | 32.54     | 56.60    | 159.14      | 371.41    |
|               | Thirteenth | 14  | 38,442,571 | 3,750,766 | 160.08     | 77.15            | 40.82     | 82.6     | 304.51      | 335.61    |
|               | Shoushan   | 15  | 38,445,834 | 3,743,743 | 183.08     | 17.43            | 18.1      | 62.39    | 227.18      | 197.7     |

with a total contribution of 99.85 %. Therefore,  $Na^++K^+$ ,  $Ca^{2+}$ ,  $Mg^{2+}$ ,  $Cl^-$ ,  $SO_4^{2-}$ , and  $HCO_3^-$  were chosen as the key groundwater chemical components in the Pingdingshan coalfield.

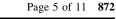
# Sampling and analysis

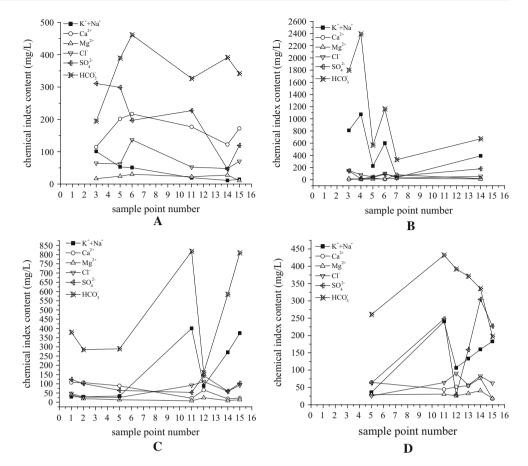
For analysis of groundwater spatial distribution in the Pingdingshan coalfield, the 15 mines were numbered from northwest to southeast (the Xiangshan mine was No. 1, the eleventh mine No. 2, the ninth mine No. 3, the fifth mine No. 4, the seventh mine No. 5, the sixth mine No. 6, the fourth mine No. 7, the third mine No. 8, the first mine No. 9, the second mine No. 10, the tenth mine or Wuzhai mine No. 11, the twelfth mine No. 12, the eighth mine No. 13, the thirteenth mine No. 14, and the Shoushan mine No. 15). Twenty-five samples were collected from the four aquifers in sequence in addition to the original 10 samples, including 6 samples from the Quaternary, 6 samples from the Permian, 7 samples from the Carboniferous, and 6 samples from the Cambrian. Sample analysis results are shown in Table 2.

Comparison of typical characteristics Key-component 1 distribution curves for the four main aquifers (Fig. 3) were drawn according to the results in Table 2. Groundwater chemical characteristics curves for the four aquifers change significantly between the fifth, seventh, and sixth mines and the twelfth, eighth, and thirteenth mines. Key groundwater chemistry components of the Quaternary and Permian decrease gradually from west to east. A discrepancy in Quaternary groundwater chemical characteristics is obvious between the seventh, sixth and thirteen mines because key groundwater chemical components are significantly affected by the Guodishan fault and the Likou syncline.  $K^+ + Na^+$  and  $HCO_3^-$  concentrations in Permian groundwater change obviously at the seventh and sixth mines, where key groundwater chemical components are significantly affected by the Guodishan fault.

Key groundwater chemical component concentrations

Fig. 3 Key-component spatial distribution *curves* of the four aquifers in the Pingdingshan coalfield. **a** was in the Quaternary, **b** in the Permian, **c** in the Carboniferous, **d** in the Cambrian





in the Carboniferous and Cambrian increase gradually from west to east. Groundwater component concentrations in the Carboniferous changed markedly at the seventh and twelfth mines:  $K^++Na^+$  and  $HCO_3^$ concentrations increased sharply at the seventh mine and decreased markedly at the twelfth mine. Moreover, groundwater component concentrations in the Cambrian increased sharply at the seventh mine, but this trend began to change at the twelfth mine. These results indicated that the Guodishan fault is the primary geological structure affecting key groundwater chemical components in the Carboniferous and Cambrian, with the Likou syncline playing a secondary role.

 Spatial distribution characteristics Contour maps of key groundwater chemical components (Fig. 4) were drawn according to the results in Table 2. The key chemical component contours of the Permian aquifer were similar to those for the Quaternary, gradually declining from west to east in the Pingdingshan coalfield and stabilizing at the sixth mine. These results indicate that the Guodishan fault is the main water-resisting geological structure in the area. Key chemical component contours of the Cambrian aquifer were similar to those of the Carboniferous, with stable trend from west to east in the Pingdingshan coalfield. However, key chemical component contours peaked at the eighth and Shoushan mines because of the Guodishan fault and the Likou syncline.

The analysis described above shows that the groundwater chemical characteristics of the Permian aquifer are similar to those of the Quaternary, that the Guodishan fault is the main water-resisting structure in the area, and that on the two sides of the Likou syncline, groundwater chemical component concentrations are different. The groundwater chemical characteristics of the Cambrian aquifer are similar to those of the Carboniferous, which are more influenced by the Guodishan fault and the Likou syncline.

# **Results and validation**

The Guodishan fault is the primary dividing structure of groundwater chemical characteristics, which divides the Pingdingshan coalfield into two primary groundwater chemically characteristic divisions, I and II. The Likou syncline is a secondary dividing structure for groundwater

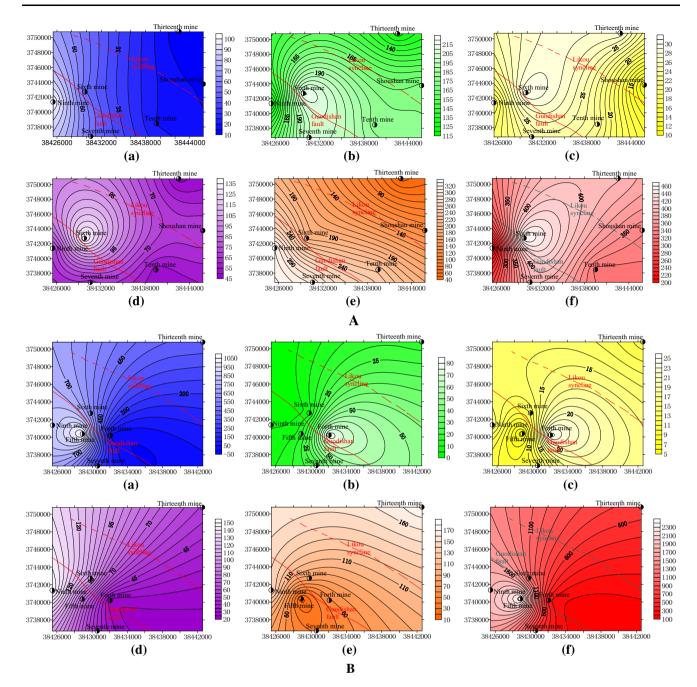


Fig. 4 Contours of key groundwater chemical components in the different aquifers. A was in the Quaternary, **B** in the Permian, **C** in the Carboniferous, and **D** in the Cambrian. **a** Showed  $K^+$ +Na<sup>+</sup> content,

 $b~{\rm Ca}^{2+}$  content,  $c~{\rm Mg}^{2+}$  content,  $d~{\rm Cl}^-$  content,  $e~{\rm SO_4}^{2-}$  content, and  $f~{\rm HCO_3}^-$  content

chemistry characteristics, which divides II into two secondary groundwater chemically characteristic divisions,  $II_I$  and  $II_{II}$  (Fig. 5).

Division I occurs to the west of the Guodishan fault, including the fifth, seventh, ninth, Xiangshan, and eleventh mines; division  $II_I$  occurs between the Guodishan fault and the Likou syncline, including the first, second, third, fourth, sixth, eighth, tenth, twelfth,

and Wuzai mines; and division  $II_{II}$  occurs to the east of the Likou syncline, including the Shoushan and thirteenth mines.

The groundwater chemical characteristics of the four aquifers influencing mining operations appeared to have a regional distribution. Discriminant models of groundwater inrush sources in divisions I,  $II_I$ , and  $II_{II}$  were constructed based on sample data and detailed groundwater chemical

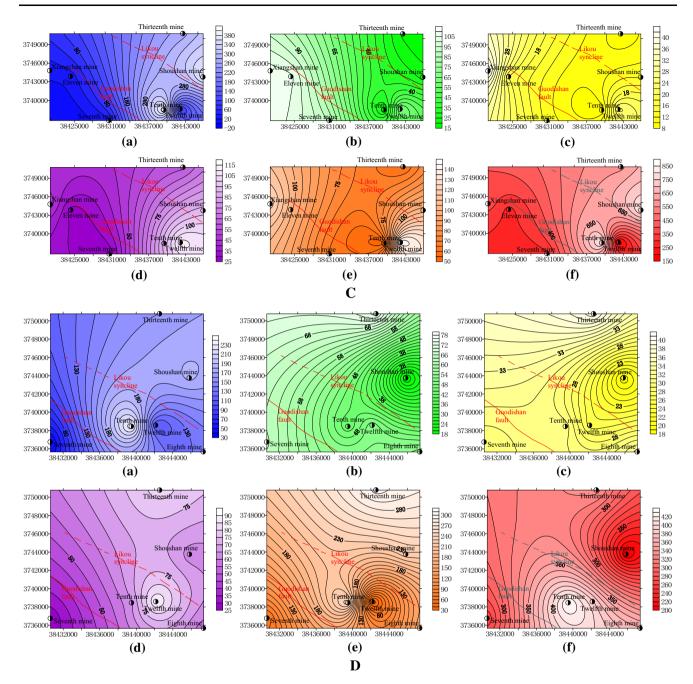


Fig. 4 continued

divisions in the Pingdingshan coalfield, and an engineering verification was conducted.

The discriminant functions were determined according to the Mahalanobis distance (Huang and Chen 2011a, b):

$$y_{g}(x) = C_{0g} + C_{1g}X_{1} + C_{2g}X_{2} + \dots + C_{pg}X_{p}$$
 (1)

Take  $G = \{x_1, x_2, \dots, x_m\}^T$  as an *m*-dimensional population,  $X = \{x_1, x_2, \dots, x_m\}^T$ , and suppose that  $u_i = E(X_i)(i = 1, 2, \dots, m)$ , so that the overall average

vector is  $\mu = (\mu_1, \mu_2, \dots, \mu_m)^T$  and the covariance matrix of population *G* is  $Cov(G) = E[(G - \mu)(G - \mu)^T]$ .

The Mahalanobis distance between sample X and population G is defined as:

$$d^{2}(X,G) = (X-\mu)^{T} \sum_{i=1}^{-1} (X-\mu)$$
(2)

If there are  $K(K \ge 2)$  *m*-dimensional populations and  $X = \{x_1, x_2, \dots, x_m\}^T$  is any given *m*-dimensional sample,

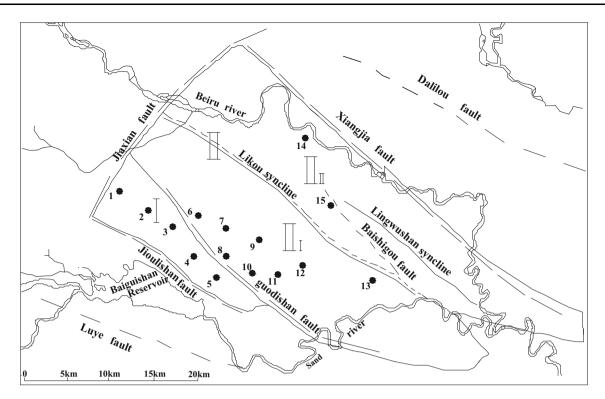


Fig. 5 Groundwater chemical characteristic divisions in the Pingdingshan coalfield. I and II belong to the primary divisions.  $II_I$  and  $II_{II}$  belong to the secondary divisions

the sample Mahalanobis distance to every population can be calculated, and then the sample belongs to the minimum population of Mahalanobis distances.

Take the Mahalanobis distance variance of new  $G_i$  and  $G_j$  samples as:

$$d^{2}(x,G_{1}) = \min\{d^{2}(x,G_{i})\} \quad (i = 1, 2, \cdots, m)$$
(3)

Therefore, sample  $X \in G_i$ .

Based on groundwater chemically characteristic divisions I, II<sub>I</sub>, and II<sub>II</sub> in the Pingdingshan coalfield and 36 sample data points for four aquifers in 15 mines (Table 3), the required models were constructed, and the discriminant functions for the Quaternary, Permian, Carboniferous, and Cambrian for the three divisions were denoted as  $Y_1$ ,  $Y_2$ ,  $Y_3$ , and  $Y_4$ .

Division I:

$$Y_1(X) = -103.195 - 0.686X_1 + 1.168X_2 - 2.184X_3 + 0.967X_4 - 0.387X_5 + 0.287X_6$$

$$Y_2(X) = -41.149 - 0.383X_1 + 0.741X_2 - 0.735X_3 + 0.544X_4 - 0.300X_5 + 0.157X_6$$

$$Y_3(X) = -24.529 + 0.379X_1 + 0.326X_2 + 0.541X_3 + 0.204X_4 - 0.083X_5 - 0.159X_6$$

$$\begin{split} Y_4(X) &= -36.457 - 0.654X_1 + 0.484X_2 - 1.807X_3 \\ &+ 0.529X_4 - 0.172X_5 + 0.267X_6 \end{split}$$

Division II<sub>I</sub>:

$$Y_1(X) = -90.835 + 0.536X_1 + 1.710X_2 - 0.794X_3 - 0.300X_4 - 0.244X_5 - 0.193X_6$$

$$Y_2(X) = -55.600 - 0.471X_1 - 0.938X_2 + 3.828X_3 + 0.110X_4 + 0.126X_5 + 0.285X_6$$

$$Y_3(X) = -27.124 - 0.280X_1 - 0.521X_2 + 2.203X_3 + 0.148X_4 + 0.089X_5 + 0.169X_6$$

$$Y_4(X) = -98.111 - 1.203X_1 - 2.170X_2 + 5.350X_3 + 0.482X_4 + 0.373X_5 + 0.532X_6$$

Division II<sub>II</sub>:

$$Y_1(X) = -104.394 + 1.138X_1 + 2.384X_2 + 1.320X_3 + 0.161X_4 - 0.517X_5 - 0.549X_6$$

$$Y_2(X) = -39.389 - 1.195X_1 - 1.612X_2 - 2.704X_3 + 0.921X_4 + 0.674X_5 + 0.558X_6$$

$$Y_3(X) = -13.808 + 0.143X_1 + 0.323X_2 + 0.052X_3 + 0.154X_4 - 0.036X_5 - 0.059X_6$$

$$Y_4(X) = -27.106 - 0.014X_1 + 0.204X_2 - 0.357X_3 + 0.467X_4 + 0.089X_5 - 0.013X_6$$

Six key groundwater chemical components for 16 samples were, respectively, entered into the discriminant the models for divisions I,  $II_I$ , and  $II_{II}$ . Table 4 shows the

**Table 3** Original sample datafrom the four aquifers

| Division | Aquifer       | No. | K <sup>+</sup> +Na <sup>+</sup><br>(mg/L) | Ca <sup>2+</sup><br>(mg/L) | Mg <sup>2+</sup><br>(mg/L) | Cl <sup>-</sup><br>(mg/L) | $SO_4^{2-}$ (mg/L) | HCO <sub>3</sub> <sup>-</sup><br>(mg/L) |
|----------|---------------|-----|---|----------------------------|----------------------------|---------------------------|--------------------|---|
| I        | Quaternary    | 1   | 52.90                                     | 201.80                     | 24.18                      | 62.39                     | 298.75             | 389.31                                  |
|          |               | 2   | 100.97                                    | 114.63                     | 16.65                      | 64.52                     | 310.75             | 194.65                                  |
|          | Permian       | 3   | 809.60                                    | 4.80                       | 15.07                      | 151.02                    | 143.12             | 1796.42                                 |
|          |               | 4   | 1109.73                                   | 15.63                      | 8.88                       | 94.66                     | 24.98              | 2498.77                                 |
|          |               | 5   | 1036.85                                   | 10.42                      | 1.22                       | 64.17                     | 4.80               | 2288.25                                 |
|          |               | 6   | 321.34                                    | 3.80                       | 1.38                       | 81.52                     | 21.13              | 599.42                                  |
|          | Carboniferous | 7   | 90.67                                     | 65.99                      | 18.55                      | 36.23                     | 15.06              | 393.76                                  |
|          |               | 8   | 54.28                                     | 73.80                      | 7.20                       | 8.80                      | 9.30               | 253.2                                   |
|          |               | 9   | 12.88                                     | 139.28                     | 33.17                      | 38.64                     | 184.92             | 324.41                                  |
|          |               | 10  | 39.79                                     | 89.58                      | 43.74                      | 44.31                     | 77.33              | 423.48                                  |
|          |               | 11  | 41.63                                     | 112.02                     | 39.24                      | 40.41                     | 160.9              | 374.66                                  |
|          | Cambrian      | 12  | 30.10                                     | 47.42                      | 8.57                       | 29.96                     | 55.02              | 273.11                                  |
|          |               | 13  | 39.08                                     | 63.93                      | 3.65                       | 17.02                     | 32.51              | 245.91                                  |
| III      | Quaternary    | 14  | 50.83                                     | 216.83                     | 30.25                      | 136.84                    | 196.92             | 461.31                                  |
|          |               | 15  | 19.78                                     | 176.95                     | 22.72                      | 52.47                     | 227.18             | 326.46                                  |
|          | Permian       | 16  | 32.89                                     | 90.73                      | 24.47                      | 21.86                     | 76.13              | 352.39                                  |
|          |               | 17  | 37.49                                     | 68.50                      | 24.91                      | 31.80                     | 40.23              | 303.97                                  |
|          |               | 18  | 600.28                                    | 7.28                       | 12.15                      | 101.82                    | 86.92              | 1162.06                                 |
|          | Carboniferous | 19  | 88.40                                     | 66.42                      | 24.84                      | 112.01                    | 144.86             | 159.99                                  |
|          |               | 20  | 513.99                                    | 14.56                      | 1.10                       | 101.82                    | 57.94              | 1074.77                                 |
|          |               | 21  | 286.44                                    | 28.97                      | 14.87                      | 81.54                     | 48.07              | 560.02                                  |
|          | Cambrian      | 22  | 101.02                                    | 50.10                      | 30.40                      | 81.46                     | 22.34              | 420.01                                  |
|          |               | 23  | 97.66                                     | 52.10                      | 26.75                      | 96.73                     | 32.97              | 361.68                                  |
|          |               | 24  | 95.33                                     | 60.12                      | 25.54                      | 96.73                     | 13.12              | 408.35                                  |
|          |               | 25  | 236.07                                    | 46.21                      | 31.30                      | 64.38                     | 278.37             | 432.97                                  |
| IIII     | Quaternary    | 26  | 6.44                                      | 199.40                     | 61.97                      | 124.78                    | 107.59             | 583.96                                  |
|          |               | 27  | 14.49                                     | 171.94                     | 10.57                      | 70.55                     | 119.59             | 341.71                                  |
|          | Permian       | 28  | 595.38                                    | 7.15                       | 10.13                      | 49.63                     | 257.2              | 985.86                                  |
|          |               | 29  | 415.92                                    | 4.77                       | 5.79                       | 56.72                     | 262.92             | 583.35                                  |
|          |               | 30  | 162.08                                    | 38.48                      | 15.08                      | 56.03                     | 15.37              | 444.21                                  |
|          | Carboniferous | 31  | 237.82                                    | 29.86                      | 15.07                      | 66.65                     | 113.35             | 538.81                                  |
|          |               | 32  | 467.51                                    | 18.04                      | 8.51                       | 106.91                    | 102.81             | 937.62                                  |
|          |               | 33  | 318.50                                    | 22.20                      | 17.90                      | 88.77                     | 20.15              | 820.30                                  |
|          |               | 34  | 258.75                                    | 37.27                      | 22.6                       | 57.78                     | 202.69             | 556.5                                   |
|          | Cambrian      | 35  | 160.08                                    | 77.15                      | 40.82                      | 82.60                     | 304.51             | 335.61                                  |
|          |               | 36  | 183.08                                    | 17.43                      | 18.10                      | 62.39                     | 227.18             | 197.70                                  |

discrimination results. The discriminant accuracy for the 14 samples was 93.75 %.

# Conclusions

1. The key groundwater chemical components of the four aquifers in the Pingdingshan coalfield were  $Na^++K^+$ ,  $Ca^{2+}$ ,  $Mg^{2+}$ ,  $Cl^-$ ,  $SO_4^{2-}$ , and  $HCO_3^-$ . Key chemical component concentrations decreased gradually from west to east in Quaternary and

Permian aquifers, but increased in Carboniferous and Cambrian aquifers.

- 2. Key groundwater chemical components in the four aquifers were significantly different on the two sides of the Guodishan fault, which is a major water-resisting structure. Certain differences were also found to exist on the two sides of the Likou syncline, which is a water-conducting structure, over long recharge distances and burial conditions.
- 3. The Guodishan fault divides the Pingdingshan coalfield into two primary groundwater chemical divisions,

 Table 4 Engineering verification results in the Pingdingshan coalfield

| Division | No. | $X_1$ (mg/L) | <i>X</i> <sub>2</sub> (mg/L) | <i>X</i> <sub>3</sub> (mg/L) | <i>X</i> <sub>4</sub> (mg/L) | <i>X</i> <sub>5</sub> (mg/L) | <i>X</i> <sub>6</sub> (mg/L) | Aquifer       | Discriminate  | Basis                       |
|----------|-----|--------------|------------------------------|------------------------------|------------------------------|------------------------------|------------------------------|---------------|---------------|-----------------------------|
| I        | 1   | 284.16       | 13.03                        | 7.05                         | 31.56                        | 4.94                         | 768.84                       | Permian       | Permian       | Min adjacent Y <sub>2</sub> |
|          | 2   | 68.31        | 57.72                        | 23.35                        | 18.08                        | 94.14                        | 329.5                        | Permian       | Permian       | Min adjacent Y <sub>2</sub> |
|          | 3   | 27.37        | 143.08                       | 19.68                        | 36.16                        | 179.15                       | 314.25                       | Carboniferous | Carboniferous | Min Y <sub>3</sub>          |
|          | 4   | 2.69         | 98.4                         | 6.6                          | 28.4                         | 18.1                         | 268.49                       | Carboniferous | Carboniferous | Min Y <sub>3</sub>          |
|          | 5   | 37.03        | 91.98                        | 49.82                        | 59.56                        | 107.11                       | 389.92                       | Carboniferous | Carboniferous | Min Y <sub>3</sub>          |
|          | 6   | 83.72        | 169.14                       | 36.21                        | 63.46                        | 303.03                       | 423.48                       | Carboniferous | Carboniferous | Min Y <sub>3</sub>          |
|          | 7   | 38.87        | 82.16                        | 18.1                         | 30.13                        | 101.34                       | 263.61                       | Cambrian      | Cambrian      | Min Y <sub>4</sub>          |
| $II_{I}$ | 8   | 133.57       | 44.09                        | 19.46                        | 86.55                        | 47.86                        | 379.18                       | Cambrian      | Cambrian      | Min Y <sub>4</sub>          |
|          | 9   | 246.07       | 41.21                        | 30.3                         | 63.48                        | 218.37                       | 430.97                       | Cambrian      | Cambrian      | Min adjacent Y <sub>4</sub> |
|          | 10  | 234.01       | 48.22                        | 30.92                        | 64.38                        | 277.47                       | 433.91                       | Cambrian      | Cambrian      | Min adjacent Y <sub>4</sub> |
|          | 11  | 31.51        | 107.01                       | 30.13                        | 67.00                        | 125.36                       | 286.18                       | Cambrian      | Cambrian      | Min Y <sub>4</sub>          |
| IIII     | 12  | 10.28        | 72.95                        | 10.21                        | 10.99                        | 19.21                        | 241.63                       | Quaternary    | Carboniferous | Min Y <sub>3</sub>          |
|          | 13  | 452.1        | 12.4                         | 5.96                         | 116.42                       | 86.16                        | 922                          | Carboniferous | Carboniferous | Min adjacent Y <sub>3</sub> |
|          | 14  | 303.51       | 8.02                         | 2.43                         | 51.06                        | 5.76                         | 629.7                        | Carboniferous | Carboniferous | Min adjacent Y <sub>3</sub> |
|          | 15  | 179.86       | 74.75                        | 30.13                        | 63.81                        | 310.27                       | 352.09                       | Cambrian      | Cambrian      | Min Y <sub>4</sub>          |
|          | 16  | 119.83       | 77.15                        | 36.21                        | 49.98                        | 244.47                       | 338.05                       | Cambrian      | Cambrian      | Min Y <sub>4</sub>          |

division I to the west and division II to the east. The Likou syncline divides division II into two secondary groundwater chemical divisions,  $II_I$  to the west and  $II_{II}$  to the east.

- 4. Discriminant models of the water inrush sources for the four aquifers were developed based on the three groundwater chemical divisions in the Pingdingshan coalfield and achieved a discrimination accuracy of 93.75 %.
- 5. The groundwater chemical divisions can be obtained following analysis of the coalfield hydrogeology and water chemical characteristics. The discrimination model of these groundwater chemical divisions can increase the discrimination accuracy of water inrush resources, which can improve the pertinence to and effectiveness on mining inrush water prevention.

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