

## Phosphate enrichment mechanism in CaO–SiO<sub>2</sub>–FeO–Fe<sub>2</sub>O<sub>3</sub>–P<sub>2</sub>O<sub>5</sub> steelmaking slags with lower binary basicity

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**Abstract:** The addition of silica to steelmaking slags to decrease the binary basicity can promote phosphate enrichment in quenched slag samples. In this study, we experimentally investigated phosphate enrichment behavior in CaO–SiO<sub>2</sub>–FeO–Fe<sub>2</sub>O<sub>3</sub>–P<sub>2</sub>O<sub>5</sub> slags with a P<sub>2</sub>O<sub>5</sub> content of 5.00% and the binary basicity  $B$  ranging from 1.0 to 2.0, where the (%Fe<sub>2</sub>O<sub>3</sub>)/(%CaO) mass percentage ratio was maintained at 0.955. The experimental results are explained by the defined enrichment degree  $R_{C_2S-C_3P}$  of solid solution 2CaO·SiO<sub>2</sub>–3CaO·P<sub>2</sub>O<sub>5</sub> (C<sub>2</sub>S–C<sub>3</sub>P), where  $R_{C_2S-C_3P}$  is a component of the developed ion and molecule coexistence theory (IMCT)– $N_i$  model for calculating the mass action concentrations  $N_i$  of structural units in the slags on the basis of the IMCT. The asymmetrically inverse V-shaped relation between phosphate enrichment and binary basicity  $B$  was observed to be correlated in the slags under applied two-stage cooling conditions. The maximum content of P<sub>2</sub>O<sub>5</sub> in the C<sub>2</sub>S–C<sub>3</sub>P solid solution reached approximately 30.0% when the binary basicity  $B$  was controlled at 1.3.

**Keywords:** phosphates enrichment; mechanisms; steelmaking; slags; basicity

### 1. Introduction

High dephosphorization ability and a reasonable melting point are the basic and indispensable properties of traditional steelmaking slags. However, the enriched phosphate in steelmaking slags can adversely affect the recyclability in traditional metallurgical processes because of the limited refining ability. To dispose and reutilize accumulated steelmaking slags in an environmentally friendly manner, various techniques such as floatation [1], carbon reduction [2], and silicon reduction [3] for extracting phosphate from traditional steelmaking slags have been developed; however, none of these approaches has achieved the objective of simultaneously recycling the slags and reusing phosphate.

The principle of selective enrichment and phase separation [4–6], which has been applied to dispose slags with minimal boron [4], vanadium [5], and titanium [6] contents, can also be applied to extract phosphate from steelmaking slags. The selective enrichment and phase separation of

phosphate in steelmaking slags [7] involve cooling molten slags with an optimized chemical composition under reasonable cooling conditions to promote the growth of phosphate-enriched grains. These grains can be obtained through phase separation based on differences between the physicochemical properties of the phosphate-enriched grains and the slags, such as differences in their density and magnetic field intensity.

Many researchers have investigated the enrichment behavior of phosphate in various slags [8–13]. In addition, we have previously elucidated the enrichment mechanism of phosphate in CaO–SiO<sub>2</sub>–FeO–Fe<sub>2</sub>O<sub>3</sub>–P<sub>2</sub>O<sub>5</sub> steelmaking slags with the binary basicity  $B$  ranging from 2.0 to 3.5 using X-ray powder diffraction (XRD), scanning electron microscopy (SEM), and energy-dispersive X-ray spectroscopy (EDS) [7]. These methods were used to observe the crystal structures of the components of quenched slag samples in this study. Meanwhile, the defined mass action concentration  $N_i$  based on the ion and molecule coexistence theory

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(IMCT) [7,14–17] was calculated to represent the reaction ability of structural units or ion couples in the slags. Moreover, we used the enrichment possibility  $N_{ci-cj}$  and enrichment degree  $R_{ci-cj}$  of phosphate to explain the experimental results [7] and deduced that the enrichment mechanism of phosphate in the slags involves the P<sub>2</sub>O<sub>5</sub> component, which can easily bond with CaO to form tricalcium phosphate 3CaO·P<sub>2</sub>O<sub>5</sub> (C<sub>3</sub>P). C<sub>3</sub>P subsequently reacts with the produced dicalcium silicate, 2CaO·SiO<sub>2</sub> (C<sub>2</sub>S), to generate solid solution C<sub>2</sub>S–C<sub>3</sub>P [18–19] under fixed cooling conditions. The maximum value of 84.4% for the defined enrichment degree  $R_{C_2S-C_3P}$  of solid solution C<sub>2</sub>S–C<sub>3</sub>P corresponds to a binary basicity  $B$  of 2.5 for the slags and (%Fe<sub>2</sub>O<sub>3</sub>)/(%CaO) mass percentage ratio of 0.955. However, the mass percentage of P<sub>2</sub>O<sub>5</sub> in the phosphate-enriched phase obtained from the slags with a binary basicity  $B$  of 2.5 is approximately 16% [7], which is still lower than that of P<sub>2</sub>O<sub>5</sub> obtained by Wang *et al.* [20–21] from modified steelmaking slags with a binary basicity  $B$  of 1.3. Wang *et al.* [20–21] further reported that decreasing the binary basicity  $B$  of steelmaking slags can effectively deplete the quantity of C<sub>2</sub>S generated in the slags, thereby improving phosphate enrichment.

In the present study, we used methods similar to those reported in our previous study [7] to improve phosphate enrichment in traditional steelmaking slags by investigating the enrichment mechanism of phosphate in CaO–SiO<sub>2</sub>–FeO–Fe<sub>2</sub>O<sub>3</sub>–P<sub>2</sub>O<sub>5</sub> steelmaking slags in which the binary basicity  $B$  has been lowered by the addition of silica as a diluent. The optimized (%Fe<sub>2</sub>O<sub>3</sub>)/(%CaO) mass percentage ratio of 0.955 in the slags determined in our previous study [7] was also used in this study. The effects of binary basicity  $B$  in the range of 1.0–2.0 and P<sub>2</sub>O<sub>5</sub> content in the range of 5.00%–10.00% on phosphate enrichment in the slags under the condition of (%Fe<sub>2</sub>O<sub>3</sub>)/(%CaO) = 0.955 were probed through experiments. Similarly, by combining the experimental and calculation results, we elucidated the phosphate enrichment mechanism in CaO–SiO<sub>2</sub>–FeO–Fe<sub>2</sub>O<sub>3</sub>–P<sub>2</sub>O<sub>5</sub> slags with the binary basicity  $B$  ranging from 1.0 to 2.0.

## 2. Description of IMCT– $N_i$ thermodynamic model for CaO–SiO<sub>2</sub>–FeO–Fe<sub>2</sub>O<sub>3</sub>–P<sub>2</sub>O<sub>5</sub> slags based on IMCT

The defined mass action concentrations  $N_i$  of structural units or ion couples in slags, which are based on the IMCT [7,14–17] for metallurgical slags, can be used to reliably represent the reaction abilities of components, similar to traditionally applied activities  $a_{R,i}$  of components relative to

pure liquid or solid matter as the standard state in classical metallurgical physicochemistry. The reaction abilities of not only the components but also the formed species in the slags can be calculated using the developed IMCT– $N_i$  thermodynamic model. The developed IMCT– $N_i$  thermodynamic model for calculating the  $N_i$  of structural units or ion couples in CaO–SiO<sub>2</sub>–FeO–Fe<sub>2</sub>O<sub>3</sub>–P<sub>2</sub>O<sub>5</sub> slags based on the IMCT [7,14–17] has been reported in detail elsewhere [7]. For the benefit of the reader, the IMCT– $N_i$  model developed for CaO–SiO<sub>2</sub>–FeO–Fe<sub>2</sub>O<sub>3</sub>–P<sub>2</sub>O<sub>5</sub> slags is briefly described here.

### 2.1. Structural units in CaO–SiO<sub>2</sub>–FeO–Fe<sub>2</sub>O<sub>3</sub>–P<sub>2</sub>O<sub>5</sub> slags

On the basis of the IMCT [7,14–17], the applied CaO–SiO<sub>2</sub>–FeO–Fe<sub>2</sub>O<sub>3</sub>–P<sub>2</sub>O<sub>5</sub> slag system is composed of Ca<sup>2+</sup>, Fe<sup>2+</sup>, and O<sup>2-</sup> as three simple ions; SiO<sub>2</sub>, Fe<sub>2</sub>O<sub>3</sub>, and P<sub>2</sub>O<sub>5</sub> as three simple molecules; and 3CaO·SiO<sub>2</sub> (C<sub>3</sub>S), 2CaO·SiO<sub>2</sub> (C<sub>2</sub>S), CaO·SiO<sub>2</sub> (CS), etc. as 11 complex molecules according to the related binary and ternary phase diagrams [19,22] of CaO–SiO<sub>2</sub>, CaO–P<sub>2</sub>O<sub>5</sub>, CaO–FeO–SiO<sub>2</sub>, CaO–FeO–P<sub>2</sub>O<sub>5</sub>, etc. at elevated temperatures, as summarized in Table 1. This table is the same as that reported previously [7]. Notably, (Ca<sup>2+</sup> + O<sup>2-</sup>) and (Fe<sup>2+</sup> + O<sup>2-</sup>) should be treated as ion couples according to the IMCT [7,14–17].

According to the IMCT [7,14–17], the total equilibrium mole number  $\Sigma n_i$  of all 16 structural units in 100 g slags can be expressed as

$$\Sigma n_i = 2n_1 + 2n_2 + n_3 + n_4 + n_5 + n_{c1} + n_{c2} + \dots + n_{c11}, \quad \text{mol} \quad (1)$$

The defined [7,14–17]  $N_i$  of the structural unit  $i$  or ion couple (Me<sup>2+</sup> + O<sup>2-</sup>) can be described by

$$N_i = \frac{n_i}{\Sigma n_i}, \quad N_{MeO} = N_{Me^{2+}, MeO} + N_{O^{2-}, MeO} = \frac{n_{Me^{2+}, MeO} + n_{O^{2-}, MeO}}{\Sigma n_i} = \frac{2n_{MeO}}{\Sigma n_i} \quad (2)$$

All defined [7,14–17] equilibrium mole numbers  $n_i$  and mass action concentrations  $N_i$  of the formed structural units or ion couples in CaO–SiO<sub>2</sub>–FeO–Fe<sub>2</sub>O<sub>3</sub>–P<sub>2</sub>O<sub>5</sub> slags [7] are also listed in Table 1. Certainly, the mass action concentrations  $N_{ci}$  of all 11 complex molecules can be expressed by  $K_{ci}^\ominus$ ,  $N_1$  ( $N_{CaO}$ ),  $N_2$  ( $N_{SiO_2}$ ),  $N_3$  ( $N_{FeO}$ ),  $N_4$  ( $N_{Fe_2O_3}$ ), and  $N_5$  ( $N_{P_2O_5}$ ) on the basis of the mass action law through  $K_{ci}^\ominus = N_{ci} / (N_{Me1O}^x N_{Me2O}^y)$  by taking  $xMe1O \cdot yMe2O$  as an example of complex or associated molecule  $ci$ .

### 2.2. Establishment of IMCT– $N_i$ model for CaO–SiO<sub>2</sub>–FeO–Fe<sub>2</sub>O<sub>3</sub>–P<sub>2</sub>O<sub>5</sub> slags

The mass conservation equations of five components in

**Table 1. Expressions of structural units as ion couples, simple or complex molecules, their mole number  $n_i$ , and mass action concentrations  $N_i$  in 100 g CaO–SiO<sub>2</sub>–FeO–Fe<sub>2</sub>O<sub>3</sub>–P<sub>2</sub>O<sub>5</sub> slags based on the IMCT**

Item	Structural units as ion couples or molecules	No. of structural units or ion couples	Mole number $n_i$ of structural units or ion couples / mol	Mass action concentration $N_i$ of structural units or ion couples
Simple cations and anions (3)	Ca <sup>2+</sup> + O <sup>2-</sup>	1	$n_1 = n_{\text{Ca}^{2+}, \text{CaO}} = n_{\text{O}^{2-}, \text{CaO}} = n_{\text{CaO}}$	$N_1 = \frac{2n_1}{\sum n_i} = N_{\text{CaO}}$
	Fe <sup>2+</sup> + O <sup>2-</sup>	3	$n_3 = n_{\text{Fe}^{2+}, \text{FeO}} = n_{\text{O}^{2-}, \text{FeO}} = n_{\text{FeO}}$	$N_3 = \frac{2n_3}{\sum n_i} = N_{\text{FeO}}$
Simple molecules (3)	SiO <sub>2</sub>	2	$n_2 = n_{\text{SiO}_2}$	$N_2 = \frac{n_2}{\sum n_i} = N_{\text{SiO}_2}$
	Fe <sub>2</sub> O <sub>3</sub>	4	$n_4 = n_{\text{Fe}_2\text{O}_3}$	$N_4 = \frac{n_4}{\sum n_i} = N_{\text{Fe}_2\text{O}_3}$
	P <sub>2</sub> O <sub>5</sub>	5	$n_5 = n_{\text{P}_2\text{O}_5}$	$N_5 = \frac{n_5}{\sum n_i} = N_{\text{P}_2\text{O}_5}$
Complex molecules (11)	3CaO·SiO <sub>2</sub>	c1	$n_{c1} = n_{3\text{CaO}\cdot\text{SiO}_2}$	$N_{c1} = \frac{n_{c1}}{\sum n_i} = N_{3\text{CaO}\cdot\text{SiO}_2}$
	2CaO·SiO <sub>2</sub>	c2	$n_{c2} = n_{2\text{CaO}\cdot\text{SiO}_2}$	$N_{c2} = \frac{n_{c2}}{\sum n_i} = N_{2\text{CaO}\cdot\text{SiO}_2}$
	CaO·SiO <sub>2</sub>	c3	$n_{c3} = n_{\text{CaO}\cdot\text{SiO}_2}$	$N_{c3} = \frac{n_{c3}}{\sum n_i} = N_{\text{CaO}\cdot\text{SiO}_2}$
	2FeO·SiO <sub>2</sub>	c4	$n_{c4} = n_{2\text{FeO}\cdot\text{SiO}_2}$	$N_{c4} = \frac{n_{c4}}{\sum n_i} = N_{2\text{FeO}\cdot\text{SiO}_2}$
	2CaO·P <sub>2</sub> O <sub>5</sub>	c5	$n_{c5} = n_{2\text{CaO}\cdot\text{P}_2\text{O}_5}$	$N_{c5} = \frac{n_{c5}}{\sum n_i} = N_{2\text{CaO}\cdot\text{P}_2\text{O}_5}$
	3CaO·P <sub>2</sub> O <sub>5</sub>	c6	$n_{c6} = n_{3\text{CaO}\cdot\text{P}_2\text{O}_5}$	$N_{c6} = \frac{n_{c6}}{\sum n_i} = N_{3\text{CaO}\cdot\text{P}_2\text{O}_5}$
	4CaO·P <sub>2</sub> O <sub>5</sub>	c7	$n_{c7} = n_{4\text{CaO}\cdot\text{P}_2\text{O}_5}$	$N_{c7} = \frac{n_{c7}}{\sum n_i} = N_{4\text{CaO}\cdot\text{P}_2\text{O}_5}$
	3FeO·P <sub>2</sub> O <sub>5</sub>	c8	$n_{c8} = n_{3\text{FeO}\cdot\text{P}_2\text{O}_5}$	$N_{c8} = \frac{n_{c8}}{\sum n_i} = N_{3\text{FeO}\cdot\text{P}_2\text{O}_5}$
	4FeO·P <sub>2</sub> O <sub>5</sub>	c9	$n_{c9} = n_{4\text{FeO}\cdot\text{P}_2\text{O}_5}$	$N_{c9} = \frac{n_{c9}}{\sum n_i} = N_{4\text{FeO}\cdot\text{P}_2\text{O}_5}$
	2CaO·Fe <sub>2</sub> O <sub>3</sub>	c10	$n_{c10} = n_{2\text{CaO}\cdot\text{Fe}_2\text{O}_3}$	$N_{c10} = \frac{n_{c10}}{\sum n_i} = N_{2\text{CaO}\cdot\text{Fe}_2\text{O}_3}$
	FeO·Fe <sub>2</sub> O <sub>3</sub>	c11	$n_{c11} = n_{\text{FeO}\cdot\text{Fe}_2\text{O}_3}$	$N_{c11} = \frac{n_{c11}}{\sum n_i} = N_{\text{FeO}\cdot\text{Fe}_2\text{O}_3}$

100 g slags can be established from the defined [7,14–17]  $n_i$  and  $N_i$  for all structural units (Table 1) and from  $\sum n_i$  in Eq. (1) as

$$b_1 = \left( \frac{1}{2}N_1 + 3N_{c1} + 2N_{c2} + N_{c3} + 2N_{c5} + 3N_{c6} + 4N_{c7} + 2N_{c10} \right) \sum n_i = \left( \frac{1}{2}N_1 + 3K_{c1}^{\ominus} N_1^3 N_2 + 2K_{c2}^{\ominus} N_1^2 N_2 + K_{c3}^{\ominus} N_1 N_2 + 2K_{c5}^{\ominus} N_1^2 N_5 + 3K_{c6}^{\ominus} N_1^3 N_5 + 4K_{c7}^{\ominus} N_1^4 N_5 + 2K_{c10}^{\ominus} N_1^2 N_4 \right) \sum n_i = n_{\text{CaO}}^0, \quad \text{mol} \quad (3a)$$

$$b_2 = (N_2 + N_{c1} + N_{c2} + N_{c3} + N_{c4}) \sum n_i = (N_2 + K_{c1}^{\ominus} N_1^3 N_2 + K_{c2}^{\ominus} N_1^2 N_2 + K_{c3}^{\ominus} N_1 N_2 + K_{c4}^{\ominus} N_2 N_3^2) \sum n_i = n_{\text{SiO}_2}^0, \quad \text{mol} \quad (3b)$$

$$b_3 = \left( \frac{1}{2}N_3 + 2N_{c4} + 3N_{c8} + 4N_{c9} + N_{c11} \right) \sum n_i = \left( \frac{1}{2}N_3 + 2K_{c4}^{\ominus} N_2 N_3^2 + 3K_{c8}^{\ominus} N_3^3 N_5 + 4K_{c9}^{\ominus} N_3^4 N_5 + K_{c11}^{\ominus} N_3 N_4 \right) \sum n_i = n_{\text{FeO}}^0, \quad \text{mol} \quad (3c)$$

$$b_4 = (N_4 + N_{c10} + N_{c11}) \sum n_i = (N_4 + K_{c10}^{\ominus} N_1^2 N_4 + K_{c11}^{\ominus} N_3 N_4) \sum n_i = n_{\text{Fe}_2\text{O}_3}^0, \quad \text{mol} \quad (3d)$$

$$\begin{aligned}
 b_5 &= (N_5 + N_{c5} + N_{c6} + N_{c7} + N_{c8} + N_{c9}) \sum n_i = \\
 &(N_5 + K_{c5}^{\ominus} N_1^2 N_5 + K_{c6}^{\ominus} N_1^3 N_5 + K_{c7}^{\ominus} N_1^4 N_5 + \\
 &K_{c8}^{\ominus} N_3^3 N_5 + K_{c9}^{\ominus} N_3^4 N_5) \sum n_i = n_{P_2O_5}^0, \quad \text{mol} \quad (3e)
 \end{aligned}$$

According to the principle that the sum of the equilibrium mole fractions of all structural units in a fixed amount of slags under equilibrium conditions is equal to unity, we obtain

$$\begin{aligned}
 N_1 + N_2 + N_3 + N_4 + N_5 + N_{c1} + N_{c2} + N_{c3} + N_{c4} + N_{c5} + \\
 N_{c6} + N_{c7} + N_{c8} + N_{c9} + N_{c10} + N_{c11} = \\
 N_1 + N_2 + N_3 + N_4 + N_5 + K_{c1}^{\ominus} N_1^3 N_2 + K_{c2}^{\ominus} N_1^2 N_2 + \\
 K_{c3}^{\ominus} N_1 N_2 + K_{c4}^{\ominus} N_2 N_3^2 + K_{c5}^{\ominus} N_1^2 N_5 + \\
 K_{c6}^{\ominus} N_1^3 N_5 + K_{c7}^{\ominus} N_1^4 N_5 + K_{c8}^{\ominus} N_3^3 N_5 + K_{c9}^{\ominus} N_3^4 N_5 + \\
 K_{c10}^{\ominus} N_1^2 N_4 + K_{c11}^{\ominus} N_3 N_4 = 1.0 \quad (4)
 \end{aligned}$$

Eqs. (3)–(4) are composed of the governing equations of the developed IMCT– $N_i$  model for calculating the mass action concentrations  $N_i$  of structural units or ion couples in CaO–SiO<sub>2</sub>–FeO–Fe<sub>2</sub>O<sub>3</sub>–P<sub>2</sub>O<sub>5</sub> slags. Obviously, the developed IMCT– $N_i$  model includes six unknown parameters, i.e.,  $N_1$  ( $N_{CaO}$ ),  $N_2$  ( $N_{SiO_2}$ ),  $N_3$  ( $N_{FeO}$ ),  $N_4$  ( $N_{Fe_2O_3}$ ),  $N_5$  ( $N_{P_2O_5}$ ), and  $\sum n_i$ , with six independent equations. The unique solution of  $N_i$ ,  $\sum n_i$ , and  $n_i$  can be obtained by solving the algebraic equation group of Eqs. (3)–(4) by combining these equations with the definition of  $N_i$  in Eq. (2).

The developed IMCT– $N_i$  model was applied to calculate the  $N_i$  of structural units or ion couples in slags with the binary basicity  $B$  ranging from 1.0 to 2.0 at an interval of 0.05 and with the P<sub>2</sub>O<sub>5</sub> mass percentage and (%Fe<sub>2</sub>O<sub>3</sub>)/(%CaO) mass percentage ratio maintained at 5.00% and 0.955, respectively.

### 3. Experimental

#### 3.1. Preparation of synthetic slags

The investigated CaO–SiO<sub>2</sub>–FeO–Fe<sub>2</sub>O<sub>3</sub>–P<sub>2</sub>O<sub>5</sub> slag system was synthesized from the prepared ferrous oxide (FeO) powder samples and reagent-grade CaO, SiO<sub>2</sub>, Fe<sub>2</sub>O<sub>3</sub>, and P<sub>2</sub>O<sub>5</sub> powders. In accordance with the method suggested by Pahlevani *et al.* [23], the FeO powder samples were prepared by mixing pure powders of iron and reagent-grade Fe<sub>2</sub>O<sub>3</sub> in a pure iron crucible and heating the mixture under an argon atmosphere at 1673 K for 60 min. The prepared FeO powder samples and the reagent-grade powders of CaO, SiO<sub>2</sub>, Fe<sub>2</sub>O<sub>3</sub>, and P<sub>2</sub>O<sub>5</sub> were mixed in a platinum crucible with an inner diameter in 30.0 mm and a height in 50.0 mm. The platinum crucible with the mixed slag samples was placed in an Al<sub>2</sub>O<sub>3</sub> crucible to allow easy removal of the

samples from the furnace during experiments.

A vertical-tube-type furnace with MoSi<sub>2</sub> rods as heating elements was used in conjunction with a programmed heating/cooling routine. The temperature precision of the heating furnace was approximately ± 3 K. High-purity argon (99.999vol%) was controlled at a flow rate of 0.4 L/min as a carrier gas to avoid the re-oxidation of the prepared FeO during heating and cooling of the slag samples in test-run experiments.

Eight test-run experiments were performed to investigate the influence of binary basicity  $B$  in the range of 1.0–2.0 on the phosphate enrichment behavior in the quenched slag samples. The chemical compositions of the eight slag samples are summarized in the left columns of Table 2. The binary basicity values  $B$  of the slags in test-run experiment Nos. 1–7 were individually designed as 1.0, 1.2, 1.3, 1.4, 1.5, 1.7, and 2.0 under the conditions of a P<sub>2</sub>O<sub>5</sub> mass percentage of 5.00% and (%Fe<sub>2</sub>O<sub>3</sub>)/(%CaO) mass percentage ratio of 0.955; these conditions were determined in a previous study [7] to promote phosphate enrichment. In addition, to probe the influence of the initial P<sub>2</sub>O<sub>5</sub> content on phosphate enrichment in the slags, we designed test-run experiment No. 8, in which the P<sub>2</sub>O<sub>5</sub> mass percentage was fixed at 10.00% under conditions of a binary basicity  $B$  of 1.3 and (%Fe<sub>2</sub>O<sub>3</sub>)/(%CaO) ratio of 0.955.

#### 3.2. Experimental procedures

The heating program differed from the cooling program. The heating schedule is described as follows: (1) the platinum crucible containing the mixed slag sample was placed into the furnace at ambient temperature; (2) high-purity Ar gas at a flow rate of 0.4 L/min was charged into the reaction tube for at least 30 min before the furnace power was switched on; (3) the sample was heated under an Ar atmosphere from ambient temperature to a fixed temperature of 1773 K at a rate of 2.0–5.0 K/min using a proportional–integral–derivative (PID) controller; and (4) the temperature was maintained 1773 K for 30 min under an Ar atmosphere to completely melt and fully synthesize the slags. By contrast, the cooling schedule consisted of the following steps: (1) the furnace temperature was decreased from 1773 to 1573 K at a rate of 2.0 K/min; (2) the temperature was maintained at 30 min at 1573 K to promote growth of phosphate-enriched grains; (3) the temperature was further decreased from 1573 to 1373 K at 2.0 K/min as a secondary slow-cooling stage to further promote condensation; and (4) the temperature was maintained at 1373 K for another 30 min as a secondary isothermal stage to ensure complete condensation.

**Table 2. Chemical compositions of eight synthesized slag samples with a (%Fe<sub>2</sub>O<sub>3</sub>)/(%CaO) mass percentage ratio of 0.955 and corresponding EDS analysis results**

Test No.	Position	Zones	Chemical composition of slags / wt%					Binary basicity, <i>B</i>	EDS analysis results / wt%				Average of P <sub>2</sub> O <sub>5</sub> / wt%
			CaO	SiO <sub>2</sub>	FeO	Fe <sub>2</sub> O <sub>3</sub>	P <sub>2</sub> O <sub>5</sub>		CaO	SiO <sub>2</sub>	Fe <sub>2</sub> O <sub>3</sub>	P <sub>2</sub> O <sub>5</sub>	
1	1	white	31.56	31.56	14.35	17.53	5.00	1.0	0.20	0.69	98.53	0.58	—
	2	gray							33.16	40.56	19.84	6.44	6.44
2	3	white	33.41	27.84	15.19	18.56	5.00	1.2	0.21	0.02	99.77	tr.	—
	4	white							0.16	0.02	99.82	tr.	—
	5	gray							42.28	26.68	26.21	4.82	—
	6	gray							41.64	27.21	26.31	4.84	—
	7	dark							42.78	26.71	18.40	12.11	12.11
3	8	white	34.18	26.29	15.54	18.99	5.00	1.3	0.22	0.81	98.49	0.48	—
	9	white							0.29	0.65	98.67	0.39	—
	10	gray							36.31	39.55	18.99	5.14	—
	11	gray							36.75	38.68	18.33	6.24	—
	12	dark							52.13	15.79	0.93	31.15	31.09
13	dark	51.08	16.81	1.09	31.02								
4	14	white	34.87	24.91	15.85	19.37	5.00	1.4	0.28	0.02	99.70	0.00	—
	15	white							0.22	0.02	99.76	0.00	—
	16	gray							44.07	30.15	23.50	2.27	—
	17	gray							44.57	30.30	22.72	2.41	—
	18	dark							61.69	17.61	5.78	14.92	16.62
19	dark	62.19	16.45	4.23	17.13								
20	dark	62.35	15.87	3.99	17.79								
5	21	white	35.49	23.66	16.13	19.72	5.00	1.5	0.45	0.83	98.72	0.00	—
	22	white							0.40	1.04	98.17	0.39	—
	23	gray							36.35	39.20	21.12	3.33	—
	24	gray							35.61	39.32	20.92	4.15	—
	25	dark							51.38	29.07	5.06	14.49	13.82
26	dark	51.23	30.19	5.42	13.16								
6	27	white	36.56	21.51	16.62	20.31	5.00	1.7	1.02	0.80	98.18	0.00	—
	28	white							1.29	tr.	98.24	0.47	—
	29	gray							36.55	41.02	19.44	2.99	—
	30	gray							36.62	42.69	18.50	2.18	—
	31	dark							51.56	33.14	6.04	9.27	13.72
32	dark	53.23	25.38	3.21	18.18								
7	33	white	37.85	18.92	17.20	21.03	5.00	2.0	1.05	0.66	98.30	0.00	—
	34	gray							29.59	34.66	34.49	1.26	—
8	35	dark	32.38	24.91	14.72	17.99	10.00	1.3	53.96	26.93	6.11	13.00	13.00
	36	white							0.35	0.09	99.56	tr.	—
	37	gray							36.77	33.33	26.09	3.81	—
	38	dark							55.67	7.00	7.26	30.07	30.04
	39	dark							55.47	7.35	7.17	30.01	

Note: "tr." indicates that the concentration of a component was lower than the minimum detection limit of the EDS analyzer.

Afterwards, the platinum crucible containing the slag sample was immediately removed from the furnace and rapidly quenched in a water pool. The obtained slag samples were dried in an oven at 403 K for at least 4 h. The dried slag samples were used as raw materials for the subsequent detection of mineralogical phases, as described in Section 3.3.

Importantly, the (%FeO)/(%Fe<sub>2</sub>O<sub>3</sub>) mass percentage ratio in the slag samples was kept almost constant during melting and condensation because high-purity Ar gas was flowing into the furnace tube during each test run. To avoid any change of valence of the iron in Fe<sub>2</sub>O amphoteric oxides, the Ar gas with 99.999% purity was rigorously purified by a gas purification train for approximately 1 h before the heating procedure was started. With regard to the gas purification train, the moisture was removed by passing the Ar gas through columns containing silica gel and dry anhydrous magnesium perchlorate Mg(ClO<sub>4</sub>)<sub>2</sub>; the CO<sub>2</sub> content was then lowered by passing the Ar gas through a column of Ascarite, and oxygen impurities in the Ar gas were subsequently oxidized using two furnaces in series containing copper turnings maintained at 973 K and magnesium turnings maintained at 773 K.

### 3.3. Detection of mineralogical phases in slag samples

The methods used to characterize the mineralogical phases in the slag samples in this study were the same as those used in our previous study [7]. The XRD experiments were performed on a powder X-ray diffractometer (Rigaku Dmax-2500) equipped with a Cu-K<sub>α</sub> radiation source to identify the crystal structure of the quenched slag samples. For observation of the micromorphology of the quenched slag samples, the samples were mounted in epoxy resin, ground with SiC sandpapers, polished, and coated with carbon for SEM (JSM–6480) analysis. The EDS was subsequently used to construct elemental mapping images and to further identify the chemical composition of the microstructures formed in the quenched slag samples.

## 4. Results and discussion

### 4.1. Characterization of crystal phases in slags

The EDS results for eight slag samples are summarized in the right-hand side of Table 2. The influence of binary basicity *B*, which ranged from 1.0 to 2.0, on the mass percentage of P<sub>2</sub>O<sub>5</sub> in the phosphate-enriched phase, as determined by EDS analysis of the quenched slags, is shown in Fig. 1. Obviously, the greatest mass percentage of P<sub>2</sub>O<sub>5</sub> in a phosphate-enriched phase was 31.09%, as observed for the test run No. 3.

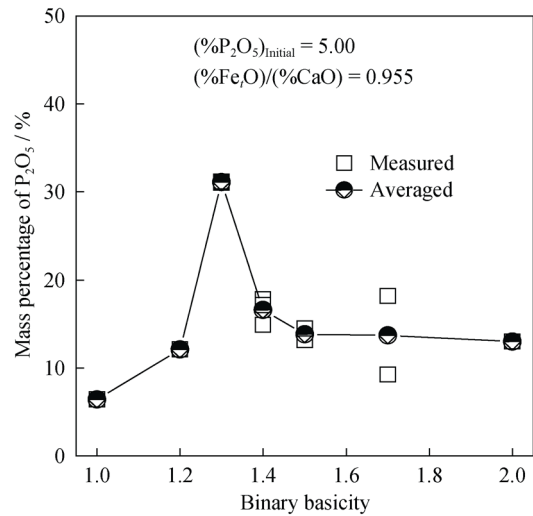


Fig. 1. Relation between binary basicity *B* in a range of 1.0–2.0 and P<sub>2</sub>O<sub>5</sub> mass percentage in the phosphate-enriched phase, as determined by EDS analysis, in quenched slag samples. The (%P<sub>2</sub>O<sub>5</sub>) and (%FeO)/(%CaO) mass percentage ratio in samples were maintained at 5.00 and 0.955, respectively.

The three slag samples labeled as No. 1, No. 3, and No. 7 in Table 2 were selected as representative slag samples for detection of the crystal structure in the slags via XRD analysis. The XRD patterns of the aforementioned three slag samples are displayed in Fig. 2. In the case of slag sample No. 1 (Fig. 2(a)), whose binary basicity *B* was 1.0, the main mineralogical phases are Fe<sub>3</sub>O<sub>4</sub> and compound CS; the phosphate-enriched phase was not detected. In the case of slag sample No. 3 (Fig. 2(b)), whose binary basicity *B* was 1.3, the main mineralogical phases are Fe<sub>3</sub>O<sub>4</sub> and Ca<sub>3</sub>Fe<sub>2</sub>(SiO<sub>4</sub>)<sub>3</sub>, and the phosphate-enriched phase is detected as a C<sub>2</sub>S–C<sub>3</sub>P solid solution. In the case of slag sample No. 7 (Fig. 2(c)), whose binary basicity *B* was 2.0, the main mineralogical phases are Fe<sub>3</sub>O<sub>4</sub>, compound C<sub>2</sub>S, and solid solution C<sub>2</sub>S–C<sub>3</sub>P.

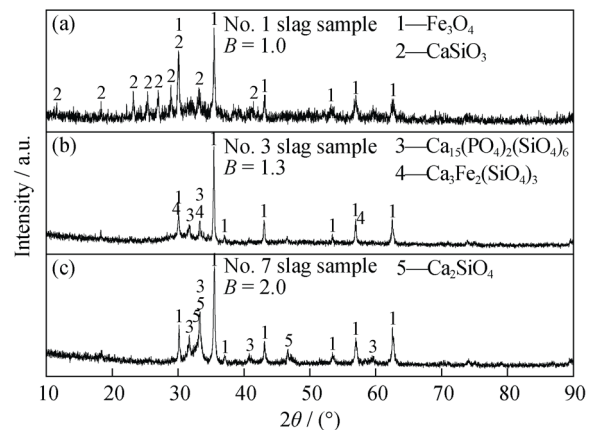


Fig. 2. X-ray diffraction patterns of slag samples obtained from test runs No. 1 (a), No. 3 (b), and No. 7 (c).

SEM and EDS analyses were used to identify the chemical compositions of the microstructures formed in the quenched slag samples. The SEM image of slag sample No. 3 is shown in Fig. 3(a). The corresponding EDS mapping images of elements Ca, Fe, P, Si, and O in slag sample No. 3 are also illustrated in Figs. 3(b)–(f), respectively. Three zones — white, gray, and dark zones — are clearly evident in slag sample No. 3 in Fig. 3(a). On the basis of the results in Fig. 3(c), Fig. 3(f), and Fig. 3(a), the white zone in Fig. 3(a) is composed primarily of Fe and O; i.e., it is an iron-oxide-enriched phase. Similarly, a comparison of re-

sults in Fig. 3(b), Fig. 3(c), and Fig. 3(e) with those in Fig. 3(a) reveals that the gray zone in Fig. 3(a) consists of Ca, Fe, and Si; i.e., this zone is the matrix phase. Moreover, combining the results in Fig. 3(b), Fig. 3(d), and Fig. 3(e) with those in Fig. 3(a) reveals that the dark zone in Fig. 3(a) is composed primarily of Ca, Si, and P; i.e., it is the phosphate-enriched phase.

We deduced that the elements Fe and O detected in the white zone could exist as  $\text{Fe}_3\text{O}_4$ ; while the Ca, Fe, and Si detected in the gray zone as the matrix phase could exist as calcium silicate ( $\text{CS-C}_2\text{S}$ ) and kirschsteinite ( $\text{CaO}\cdot\text{SiO}_2\cdot\text{FeO}$ ),

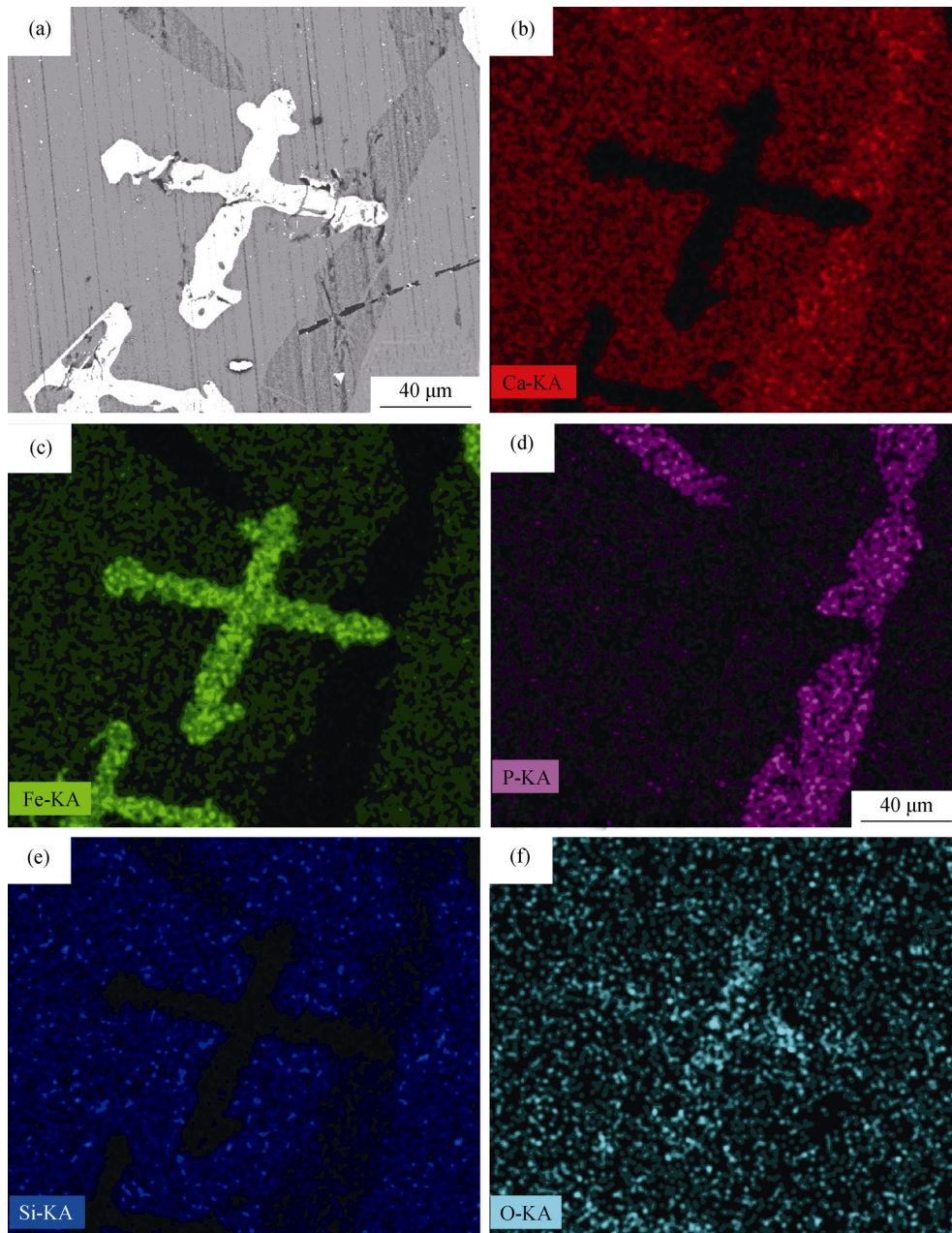


Fig. 3. SEM images of slag sample No. 3 (a) and corresponding EDS mapping images of Ca (b), Fe (c), P (d), Si (e), and O (f) in quenched slag samples with binary basicity  $B$  as 1.3 and  $(\%P_2O_5)$  as 5.00.

and the Ca, Si, and P detected in the dark zone could exist as solid solution C<sub>2</sub>S–C<sub>3</sub>P.

The SEM images of the slag samples from test runs No. 1–No. 8 are displayed in Fig. 4. In the case of slag sample No. 1, whose binary basicity  $B$  was 1.0, we combined the SEM image in Fig. 4(a) with the corresponding EDS results for point 1 and point 2 in Table 2 and deduced that iron oxides dominate the white zone assigned as point 1 in Fig. 4(a); by contrast, we deduced that a phosphate phase is dispersed in the gray zone as the matrix phase assigned as point 2 in Fig. 4(a). No phosphate-enriched phase, i.e., no dark zone, was observed in Fig. 4(a).

In the case of slag sample No. 2, whose binary basicity  $B$  was 1.2, we combined the SEM image in Fig. 4(b) with the corresponding EDS results from point 3 to point 7 in Table 2 and deduced that iron oxides dominate the white zones represented by point 3 and point 4 in Fig. 4(b); we also deduced that a large amount of the matrix phase was generated as the gray zone represented by point 5 and point 6. In addition, a small amount of solid solution C<sub>2</sub>S–C<sub>3</sub>P was also formed as the dark zone indicated by point 7. The presence of this solid solution was deduced by comparing the results in Fig. 4(a) with those in Fig. 4(b); the results of this comparison indicate that increasing the binary basicity  $B$  from 1.0 to 1.2 can promote the formation of this dark phase. However, the amount of dark phase formed is not sufficient to be precipitated as dark stripes. The corresponding EDS results from point 5 to point 7 in Table 2 further indicate that the determined mass percentage of P<sub>2</sub>O<sub>5</sub> at point 5 and point 6 (gray phase) is lower than that at point 7 (dark phase); this result implies that parts of phosphate can be condensed from the gray matrix phase into the dark, stripe-shaped phase.

In the case of slag sample No. 3, whose binary basicity  $B$  was 1.3, we combined the SEM image in Fig. 4(c) with the corresponding EDS results from point 12 to point 13 in Table 2 and deduced that the dark phase can clearly be produced as a columnar shape. According to the mass percentage of P<sub>2</sub>O<sub>5</sub> at point 12 and point 13 (dark phase) determined by the EDS and reported in Table 2, phosphate can be well enriched in the dark phase, where the mass percentage of P<sub>2</sub>O<sub>5</sub> in the phosphate-enriched phase can reach approximately 31.00%. Notably, the results obtained for the points in white and gray phases will not be discussed in the following text.

In the case of slag sample No. 4, whose binary basicity  $B$  was 1.4, the combination of the SEM image in Fig. 4(d) with the corresponding EDS results from point 18 to point 20 in Table 2 reveals that the dark phase, i.e., the phos-

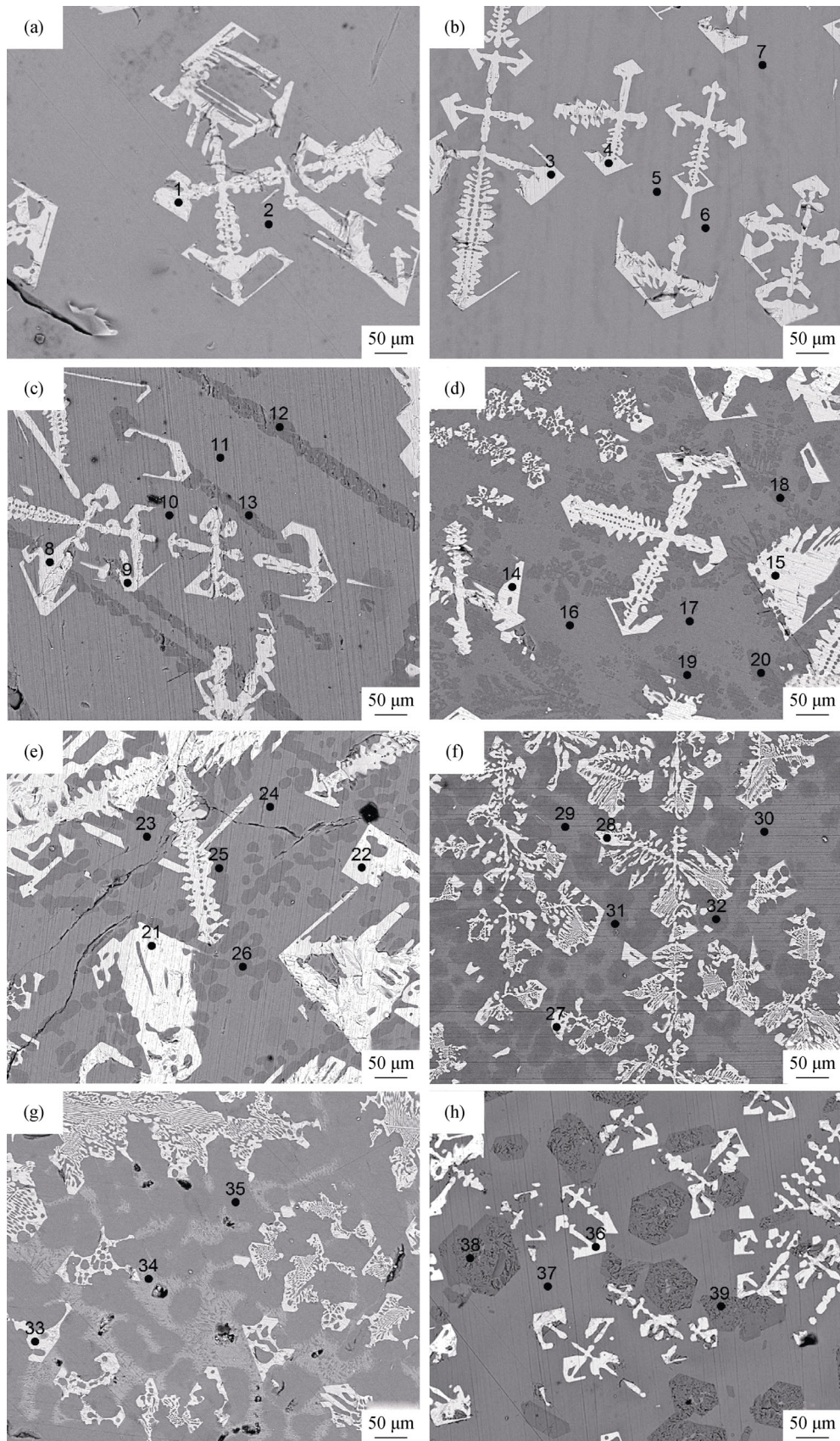
phate-enriched phase, exhibits a granular shape. A comparison of the SEM image of slag sample No. 3 in Fig. 4(c) with that of slag sample No. 4 in Fig. 4(d) reveals that an increase in the binary basicity  $B$  from 1.3 to 1.4 can lead to an obvious variation of the shape of the dark phase from column to granule. Meanwhile, a comparison of the mass percentage of P<sub>2</sub>O<sub>5</sub> determined by EDS for slag sample No. 3 slag with that for slag sample No. 4 in Table 2 reveals that an increase in the binary basicity  $B$  from 1.3 to 1.4 can also result in a significantly decrease in the P<sub>2</sub>O<sub>5</sub> mass percentage from 31.09% to 16.62%; i.e., the extent of phosphate enrichment is substantially diminished. This phenomenon can be interpreted as an increase in the binary basicity leading to an increase in the quantity of C<sub>2</sub>S generated. Thus, we deduced that the number of crystal nuclei formed during instantaneous nucleation in Fig. 4(d) is greater than that in Fig. 4(c). The generated C<sub>3</sub>P phase (dark phase) with unchangeable quantity can widely disperse in smaller-sized shapes, as shown in Fig. 4(d). Thus, an increase in the quantity of C<sub>2</sub>S formed can lead to an increase of the dark-phase area. Consequently, the mass percentage of P<sub>2</sub>O<sub>5</sub> in the dark phase should, compared with that in Fig. 4(c), decrease under the condition of a binary basicity  $B$  of 1.4.

From the viewpoint of promoting phosphate enrichment, the optimal binary basicity  $B$  of the slags is approximately 1.30. Thus, the results from slag sample No. 3 in Fig. 4(c) and in Table 2 were selected as criteria for comparison in this section.

As demonstrated in the case of slag samples No. 5 (Fig. 4(e)) and No. 6 (Fig. 4(f)), whose binary basicity  $B$  values were 1.5 and 1.7, respectively, increasing the binary basicity  $B$  from 1.3 in the case of slag sample No. 3 (Fig. 4(c)) to 1.5 or 1.7 in the cases of these slag samples clearly does not lead to substantial variation in the shapes of white and dark phases. Comparing the mass percentage of P<sub>2</sub>O<sub>5</sub> determined by EDS for slag samples No. 5 and No. 6 slag with that obtained for No. 4 slag sample (Table 2) reveals that an increase in the binary basicity  $B$  to 1.5 and 1.7 can deteriorate the phosphate-enrichment behavior. Interestingly, the boundaries between the gray phase and dark phase for slag sample No. 6 (Fig. 4(f)), whose binary basicity  $B$  was 1.7, were not as clear as those observed in slag sample No. 5 (Fig. 4(e)), whose binary basicity  $B$  was 1.5. Thus, the formed calcium silicate phase in the matrix phase (gray phase) and the generated phosphate-enriched phase (dark phase) exhibit greater affinity for transferring CS to C<sub>2</sub>S at a binary basicity  $B$  of 1.7.

As demonstrated in the case of slag sample No. 7 (Fig. 4(g)), whose binary basicity  $B$  was 2.0, a further increase in





**Fig. 4.** SEM images of quenched slag samples obtained from test runs No. 1 to No. 8 (a–h, respectively). The (%Fe<sub>2</sub>O<sub>3</sub>)/(%CaO) mass percentage ratio was maintained at 0.955.

the binary basicity  $B$  from 1.7 to 2.0 did not lead to substantial changes in the shapes of white and gray phases compared to the shapes observed in slag sample No. 6 (Fig. 4(f)) with a binary basicity  $B$  of 1.7. However, an increase of the binary basicity  $B$  from 1.7 to 2.0 did cause an increase of the dark-phase area in Fig. 4(g). We deduced that increasing the binary basicity  $B$  from 1.7 to 2.0 does not obviously affect the phosphate enrichment results.

Fig. 4(h) shows the SEM image of slag sample No. 8, whose binary basicity  $B$  was 1.3, prepared under the condition of a P<sub>2</sub>O<sub>5</sub> mass percentage of 10.00%. Comparing the SEM results for slag sample No. 3 in Fig. 4(c) with those for slag sample No. 8 in Fig. 4(h) leads to the conclusion that increasing the initial mass percentage of P<sub>2</sub>O<sub>5</sub> in the slag sample from 5.00% to 10.00% obviously affects the SEM results; specifically, the area of the dark phase is obviously enlarged. However, comparing the summarized results of the mass percentage of P<sub>2</sub>O<sub>5</sub> determined by EDS for slag sample No. 3 with those for slag sample No. 8 in Table 2 reveals that increasing the initial mass percentage of P<sub>2</sub>O<sub>5</sub> in the slag sample from 5.00% to 10.00% does not lead to detectable variation of the determined mass percentage of P<sub>2</sub>O<sub>5</sub> in the phosphate-enriched phase. Thus, increasing the initial mass percentage of P<sub>2</sub>O<sub>5</sub> from 5.00% to 10.00% can only facilitate formation of the phosphate-enriched phase, not increase the mass percentage of P<sub>2</sub>O<sub>5</sub> in the enriched phase. This result implies that the maximum value of phosphate enrichment of approximately 30.00% is not affected by varying the initial mass percentage of P<sub>2</sub>O<sub>5</sub> in the slag samples under conditions of a binary basicity  $B$  of 1.3 and a

(%Fe<sub>2</sub>O<sub>3</sub>)/(%CaO) mass percentage ratio of 0.955.

### 4.2. Discussion

#### 4.2.1. Effect of binary basicity on the mass action concentrations $N_i$ of six structural units

According to the developed IMCT– $N_i$  model described in Section 2, three complex molecules of calcium silicates — 3CaO·SiO<sub>2</sub> (C<sub>3</sub>S), 2CaO·SiO<sub>2</sub> (C<sub>2</sub>S), and CaO·SiO<sub>2</sub> (CS) — can be formed in CaO–SiO<sub>2</sub>–FeO–Fe<sub>2</sub>O<sub>3</sub>–P<sub>2</sub>O<sub>5</sub> slags; in addition, three main complex molecules that contain P<sub>2</sub>O<sub>5</sub> — 2CaO·P<sub>2</sub>O<sub>5</sub> (C<sub>2</sub>P), 3CaO·P<sub>2</sub>O<sub>5</sub> (C<sub>3</sub>P), and 4CaO·P<sub>2</sub>O<sub>5</sub> (C<sub>4</sub>P) — can also be generated in the slags. Fig. 5(a) shows the relation between the binary basicity  $B$  in the range of 1.0–2.0 and the calculated  $N_{ci}$  of the aforementioned three calcium silicates as C<sub>3</sub>S, C<sub>2</sub>S, and CS for slags at a temperature of 1773 K and in which the mass percentage of P<sub>2</sub>O<sub>5</sub> and the (%Fe<sub>2</sub>O<sub>3</sub>)/(%CaO) mass percentage ratio are maintained at 5.00% and 0.955, respectively. Similarly, the relation between the binary basicity in the range of 1.0–2.0 and the calculated  $N_{cj}$  of the three main complex molecules containing P<sub>2</sub>O<sub>5</sub> (C<sub>2</sub>P, C<sub>3</sub>P, and C<sub>4</sub>P) in the slags under the same conditions is illustrated in Fig. 5(b). The results in Fig. 5(a) indicate that the calculated value of  $N_{C_3S}$  is much smaller than the calculated values of  $N_{C_2S}$  and  $N_{CS}$ , consistent with the reported CaO–SiO<sub>2</sub> phase diagram [19]. Thus, the contribution of C<sub>3</sub>S to the formed calcium silicates can be disregarded. Increasing the binary basicity  $B$  from 1.0 to 2.0 can result in an increasing trend of the calculated  $N_{C_2S}$  value but a decreasing trend of the  $N_{CS}$  value. Obviously, the calculated  $N_{CS}$  and  $N_{C_2S}$  values exhibit competing

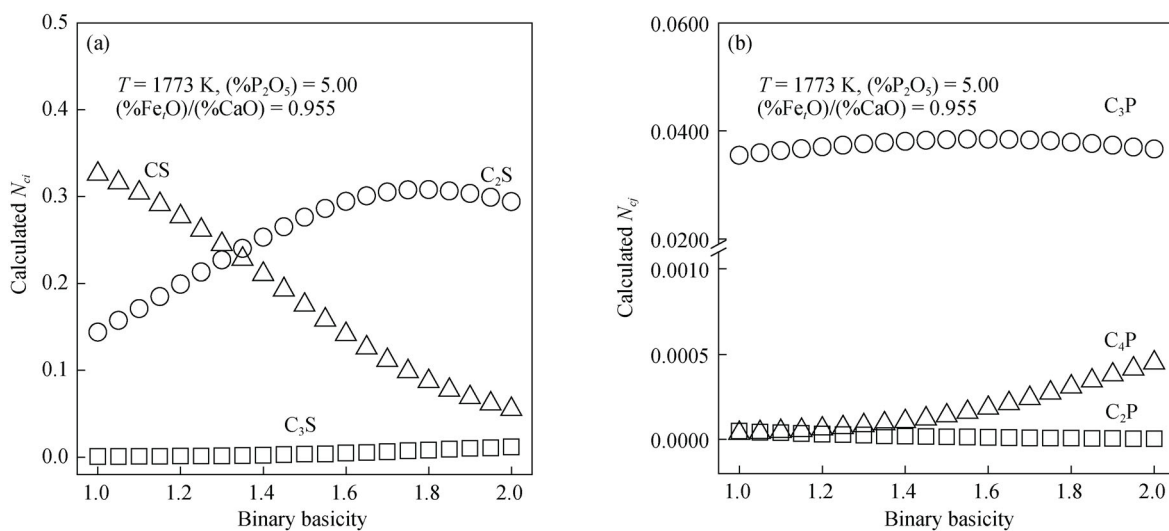


Fig. 5. Relation of binary basicity in a range of 1.0–2.0 at interval of 0.05 and calculated mass action concentrations  $N_{ci}$  of three calcium silicates as C<sub>3</sub>S, C<sub>2</sub>S, or CS (a) or calculated mass action concentrations  $N_{cj}$  of three P<sub>2</sub>O<sub>5</sub>-containing structural units as C<sub>2</sub>P, C<sub>3</sub>P, or C<sub>4</sub>P (b) for CaO–SiO<sub>2</sub>–FeO–Fe<sub>2</sub>O<sub>3</sub>–P<sub>2</sub>O<sub>5</sub> slags at a temperature of 1773 K under the conditions of (%P<sub>2</sub>O<sub>5</sub>) = 5.00 and (%Fe<sub>2</sub>O<sub>3</sub>)/(%CaO) = 0.955.

behaviors for the slags with the binary basicity  $B$  between 1.0 and 2.0.

According to Fig. 5(b), the calculated  $N_{C_3P}$  is substantially greater than the calculated  $N_{C_2P}$  and  $N_{C_4P}$ . The calculated  $N_{C_3P}$  exhibits an asymmetrically parabolic trend as the binary basicity  $B$  is increased from 1.0 to 2.0. The maximum value of the calculated  $N_{C_3P}$  corresponds to a binary basicity  $B$  of 1.7. The influence of binary basicity  $B$  in the range of 1.0–2.0 on the calculated  $N_{C_3P}$  is opposite its influence on  $N_{C_4P}$ . Thus, increasing the binary basicity  $B$  from 1.0 to 2.0 can result in a decreasing tendency of  $N_{C_2P}$  but an increasing tendency of  $N_{C_4P}$ .

4.2.2. Phosphate enrichment phenomenon at binary basicity less than 1.3

To explain the tendency of the phosphate enrichment in the quenched slag samples to decrease when the binary basicity  $B$  is less than 1.3, we apply the enrichment possibility  $N_{ci-cj}$  of phosphate as well as the enrichment degree  $R_{ci-cj}$  of phosphate in slags defined in our previous study [7]. Because the calculated  $N_{C_2P}$  and  $N_{C_4P}$  values are much smaller than the calculated  $N_{C_3P}$ , as shown in Fig. 5(b), the contribution of  $C_3P$  to phosphate enrichment is substantially greater than the contributions of  $C_2P$  and  $C_4P$ . Thus, the contributions of both  $C_2P$  and  $C_4P$  to the enrichment possibility  $N_{ci-cj}$  of phosphate and to the enrichment degree  $R_{ci-cj}$  of phosphate in the slags can be disregarded.

Under this circumstance, the enrichment possibility  $N_{ci-C_3P}$ , which is defined as the product of the calculated  $N_{ci}$  for complex molecule  $ci$  containing calcium silicates and the calculated  $N_{C_3P}$ , can be expressed by

$$N_{C_2S-C_3P} = N_{C_2S}N_{C_3P}, \quad N_{CS-C_3P} = N_{CS}N_{C_3P}, \quad N_{C_3S-C_3P} = N_{C_3S}N_{C_3P} \quad (5)$$

The summation of the enrichment possibility  $N_{ci-C_3P}$  for all three of the aforementioned structural units can be expressed as

$$\sum \left( N_{ci-C_3P} \frac{M_{P_2O_5}}{M_{ci-C_3P}} \right) = N_{C_2S}N_{C_3P} \frac{M_{P_2O_5}}{M_{C_2S-C_3P}} + N_{CS}N_{C_3P} \frac{M_{P_2O_5}}{M_{CS-C_3P}} + N_{C_3S}N_{C_3P} \frac{M_{P_2O_5}}{M_{C_3S-C_3P}} \quad (6)$$

Thus, the ratio of the defined [7] enrichment possibility  $N_{ci-C_3P}$  to the summation of the enrichment possibility for all three of the aforementioned structural units, i.e.,

$$\sum \left( N_{ci-C_3P} \frac{M_{P_2O_5}}{M_{ci-C_3P}} \right), \text{ is defined as enrichment degree}$$

$R_{ci-C_3P}$ . The defined enrichment degree  $R_{C_2S-C_3P}$  of solid solution  $C_2S-C_3P$  can be calculated by

$$R_{C_2S-C_3P} = \frac{N_{C_2S}N_{C_3P} \frac{M_{P_2O_5}}{M_{C_2S-C_3P}}}{N_{C_2S}N_{C_3P} \frac{M_{P_2O_5}}{M_{C_2S-C_3P}} + N_{CS}N_{C_3P} \frac{M_{P_2O_5}}{M_{CS-C_3P}} + N_{C_3S}N_{C_3P} \frac{M_{P_2O_5}}{M_{C_3S-C_3P}}} = \frac{N_{C_2S} \frac{M_{P_2O_5}}{M_{C_2S-C_3P}}}{N_{C_2S} \frac{M_{P_2O_5}}{M_{C_2S-C_3P}} + N_{CS} \frac{M_{P_2O_5}}{M_{CS-C_3P}} + N_{C_3S} \frac{M_{P_2O_5}}{M_{C_3S-C_3P}}} \quad (7)$$

Fig. 6 shows the relation of binary basicity  $B$  in the range of 1.0–1.3 to the enrichment degree  $R_{C_2S-C_3P}$  of solid solution  $C_2S-C_3P$  or to the mass percentage of  $P_2O_5$  in the phosphate-enriched phase determined by EDS analysis of the quenched slags, in which the initial mass percentage of  $P_2O_5$  was 5.00%. Although the enrichment degree  $R_{C_2S-C_3P}$  of solid solution  $C_2S-C_3P$  based on the IMCT [7,14–17] is greater than the determined mass percentage of  $P_2O_5$  in the phosphate-enriched phase in the quenched slag samples with the binary basicity  $B$  less than 1.3, a similar increasing tendency of the enrichment degree  $R_{C_2S-C_3P}$  of solid solution  $C_2S-C_3P$  or the determined mass percentage of  $P_2O_5$  in the phosphate-enriched phase is observed when the binary basicity  $B$  is less than 1.3. Thus, the enrichment degree  $R_{C_2S-C_3P}$  of solid solution  $C_2S-C_3P$  calculated on the basis of the IMCT [7,14–17] can be used to predict the phosphate enrichment phenomenon in the quenched slag samples with the binary basicity  $B$  less than 1.3.

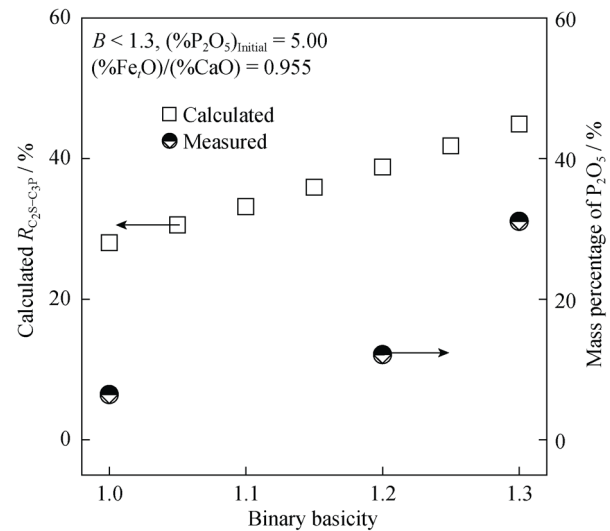


Fig. 6. Relation between binary basicity  $B$  in a range of 1.0–1.3 and calculated enrichment degree  $R_{C_2S-C_3P}$  or determined mass percentage of  $P_2O_5$  in the phosphate-enriched phase in quenched slag samples in which  $(\%P_2O_5)$  is 5.00.

By combining the experimental results obtained from the SEM images in Fig. 4(a) or Fig. 4(b) with the calculation results in Fig. 5(a), we deduced that the produced C<sub>2</sub>S, rather than CS, is the main precursor that bonds C<sub>3</sub>P in the quenched slag samples with the binary basicity *B* less than 1.3. However, greater *N*<sub>CS</sub> in the slags with the binary basicity *B* less than 1.3 does not promote phosphate enrichment in the quenched slag samples. Certainly, the enrichment degree *R*<sub>C<sub>2</sub>S–C<sub>3</sub>P</sub> of solid solution C<sub>2</sub>S–C<sub>3</sub>P cannot explain the decreasing trend of the mass percentage of P<sub>2</sub>O<sub>5</sub> in the phosphate-enriched phase for the quenched slag samples with the binary basicity *B* greater than 1.3.

Notably, the enrichment degree *R*<sub>C<sub>2</sub>S–C<sub>3</sub>P</sub> of solid solution C<sub>2</sub>S–C<sub>3</sub>P and the mass percentage of P<sub>2</sub>O<sub>5</sub> in the phosphate-enriched phase are both distinct parameters and are related to each other provided that the entire slag system is correctly defined.

#### 4.2.3. Phosphate enrichment phenomenon at binary basicity greater than 1.3

According to the definition of *N<sub>i</sub>* in Eq. (2), the equilibrium mole number *n<sub>i</sub>* can be calculated as *n<sub>i</sub>* = *N<sub>i</sub>*Σ*n<sub>i</sub>*. Thus, the mole fraction of C<sub>3</sub>P in solid solution C<sub>2</sub>S–C<sub>3</sub>P can be calculated by

$$x_{C_3P} = n_{C_3P} / (n_{C_2S} + n_{C_3P}) = N_{C_3P} \Sigma n_i / (N_{C_2S} + N_{C_3P}) \Sigma n_i = N_{C_3P} / (N_{C_2S} + N_{C_3P}) \quad (8)$$

The mass percentage of C<sub>3</sub>P in solid solution C<sub>2</sub>S–C<sub>3</sub>P can be determined as

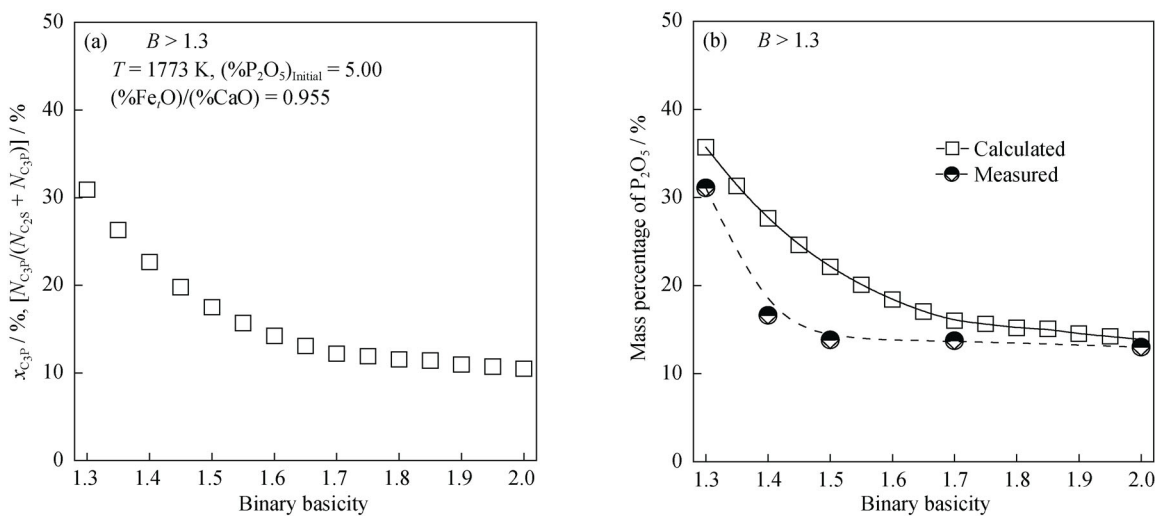
$$(\%C_3P) = 100 \times \frac{n_{C_3P} \times M_{C_3P}}{n_{C_2S} \times M_{C_2S} + n_{C_3P} \times M_{C_3P}} =$$

$$100 \times \frac{N_{C_3P} \times M_{C_3P} \times \Sigma n_i}{(N_{C_2S} \times M_{C_2S} + N_{C_3P} \times M_{C_3P}) \times \Sigma n_i} \quad (9)$$

The mass percentage of P<sub>2</sub>O<sub>5</sub> in solid solution C<sub>2</sub>S–C<sub>3</sub>P can be predicted by

$$(\%P_2O_5) = (\%C_3P) \times \frac{M_{P_2O_5}}{M_{C_3P}} = 100 \times \frac{N_{C_3P} \times M_{P_2O_5}}{N_{C_2S} \times M_{C_2S} + N_{C_3P} \times M_{C_3P}} \quad (10)$$

Fig. 7(a) shows the relation between the binary basicity *B* in the range of 1.3–2.0 and the calculated mole fraction *x*<sub>C<sub>3</sub>P</sub> of C<sub>3</sub>P in solid solution C<sub>2</sub>S–C<sub>3</sub>P or the mass action concentration ratio *N*<sub>C<sub>3</sub>P</sub> / (*N*<sub>C<sub>2</sub>S</sub> + *N*<sub>C<sub>3</sub>P</sub>) for the slags at a temperature of 1773 K and with the mass percentage of P<sub>2</sub>O<sub>5</sub> fixed at 5.00%. Meanwhile, Fig. 7(b) shows the relation of the binary basicity *B* in the range of 1.3–2.0 to the mass percentage of P<sub>2</sub>O<sub>5</sub> in the phosphate-enriched phase determined by EDS analysis or to the mass percentage of P<sub>2</sub>O<sub>5</sub> in solid solution C<sub>2</sub>S–C<sub>3</sub>P calculated on the basis of Eq. (10) for the slags. As shown in Fig. 7(a), an increase of the binary basicity *B* from 1.3 to 2.0 can cause an obvious decreasing trend of the mass action concentration ratio *N*<sub>C<sub>3</sub>P</sub> / (*N*<sub>C<sub>2</sub>S</sub> + *N*<sub>C<sub>3</sub>P</sub>) in the slags. Meanwhile, the mass percentage of P<sub>2</sub>O<sub>5</sub> in solid solution C<sub>2</sub>S–C<sub>3</sub>P, as calculated by Eq. (10), also tends to increase as the binary basicity *B* is increased from 1.3 to 2.0. Moreover, the mass percentage of P<sub>2</sub>O<sub>5</sub> in solid solution C<sub>2</sub>S–C<sub>3</sub>P, as calculated by Eq. (10), is in good agreement with the mass percentage of P<sub>2</sub>O<sub>5</sub> in the phosphate-enriched phase determined by EDS analysis. The greater amount of C<sub>2</sub>S can decrease the phosphate enrichment



**Fig. 7.** Relation between binary basicity *B* in a range of 1.3–2.0 and calculated mole fraction *x*<sub>C<sub>3</sub>P</sub> of C<sub>3</sub>P in solid solution C<sub>2</sub>S–C<sub>3</sub>P or calculated mass action concentration ratio *N*<sub>C<sub>3</sub>P</sub> / (*N*<sub>C<sub>2</sub>S</sub> + *N*<sub>C<sub>3</sub>P</sub>) (a) and mass percentage of P<sub>2</sub>O<sub>5</sub> in the phosphate-enriched phase determined by EDS analysis or calculated mass percentage of P<sub>2</sub>O<sub>5</sub> in solid solution C<sub>2</sub>S–C<sub>3</sub>P (b) in quenched slag samples in which (%P<sub>2</sub>O<sub>5</sub>) is 5.00.

in the quenched slag samples when the binary basicity  $B$  is greater than 1.3.

Combining the results in Fig. 6 with those in Fig. 7 leads to the reasonable deduction: (1) most phosphate will exist as  $C_3P$  in the slags at elevated temperatures; (2) the formed  $C_3P$  can be easily bonded with  $C_2S$  to produce solid solution  $C_2S-C_3P$  in the quenched slag samples; (3) maintaining the binary basicity  $B$  at 1.3 can result in the maximum phosphate enrichment for the slags with a  $P_2O_5$  mass percentage of 5.00% and a  $(\%Fe_2O)/(\%CaO)$  mass percentage ratio of 0.955; (4) the phosphate enrichment in the quenched slag samples with the binary basicity  $B$  less than 1.3 can be predicted on the basis of their  $C_2S$  content; (5) the phosphate enrichment in the quenched slag samples with the binary basicity  $B$  greater than 1.3 can be predicted on the basis of the  $C_3P$  content in the solid solution  $C_2S-C_3P$  and on the basis of a greater amount of  $C_2S$  diminishing the phosphate enrichment in the quenched slag samples.

Thus, a binary basicity  $B$  of 1.3, a  $P_2O_5$  content of 5.00%, and a  $(\%Fe_2O)/(\%CaO)$  the mass percentage ratio of 0.955 are recommended to promote selective phosphate enrichment and phase separation of the investigated steelmaking slags.

## 5. Conclusions

Phosphate enrichment behavior has been experimentally investigated in  $CaO-SiO_2-FeO-Fe_2O_3-P_2O_5$  slags with the binary basicity  $B$  ranging from 1.0 to 2.0 and with the mass percentage ratio  $(\%Fe_2O)/(\%CaO)$  maintained at 0.955. The experimental results have been explained by the defined enrichment degree  $R_{C_2S-C_3P}$  of solid solutions containing  $P_2O_5$ . This defined enrichment degree is a component of the developed IMCT- $N_i$  model for calculating the mass action concentrations  $N_i$  of structural units in the slags. The main findings are summarized as follows.

(1) The asymmetrically inverse V-shaped relation between the binary basicity  $B$  in the range of 1.0–2.0 and the phosphate enrichment in the quenched slag samples can be correlated for slags under the applied two-stage cooling conditions. The maximum content of  $P_2O_5$  in solid solution  $2CaO-SiO_2-3CaO-P_2O_5$  ( $C_2S-C_3P$ ) is approximately 30.0% and is obtained for slags with a binary basicity  $B$  of 1.3 and in which the mass percentage ratio  $(\%Fe_2O)/(\%CaO)$  was maintained at 0.955.

(2) The promotive effect of binary basicity  $B$  in the range of 1.0–1.3 on the phosphate enrichment in the quenched slag samples with a  $P_2O_5$  content of 5.00% can be quantitatively explained by the defined enrichment degree  $R_{C_2S-C_3P}$  of

the solid solution  $C_2S-C_3P$  in the slags. The formed  $C_2S$ , rather than  $CS$ , in the slags with binary basicity  $B$  ranging from 1.0 to 1.3 can be bonded by  $C_3P$  to form the solid solution  $2CaO-SiO_2-3CaO-P_2O_5$  ( $C_2S-C_3P$ ) under fixed cooling conditions.

(3) The deteriorative effect of binary basicity  $B$  in the range of 1.3–2.0 on phosphate enrichment in the quenched slag samples with a  $P_2O_5$  content of 5.00% can be quantitatively explained on the basis of the calculated  $C_3P$  content in the solid solution  $C_2S-C_3P$ . Although increasing the binary basicity  $B$  from 1.3 to 2.0 can improve the absolute amount of  $C_2S$ , the  $C_3P$  content in the solid solution  $C_2S-C_3P$  tends to decrease as the binary basicity  $B$  of the slags is increased within this range.

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