



Resonant Terahertz radiation by p-polarised chirped laser in hot plasma with slanting density modulation

Hitesh Kumar Midha¹ · Vivek Sharma¹ · Niti Kant² · Vishal Thakur¹

Received: 13 September 2023 / Accepted: 26 November 2023
© The Author(s), under exclusive licence to The Optical Society of India 2023

Abstract The production of terahertz (THz) radiation via the interaction between lasers and plasmas is an intriguing and swiftly progressing domain of study within the realms of optics and plasma physics. The aforementioned procedure entails the utilisation of high-intensity laser pulses to engage with a plasma, hence leading to the generation of coherent THz radiation. THz radiation, which falls within the frequency range between microwave and infrared, finds utility in various domains such as imaging, spectroscopy, and materials characterisation. This study examines the interaction of two p-polarised, positively chirped laser beams, with a hot collisional plasma characterised by a slanting up density profile. This study investigates the impact of normalised THz frequency, normalised collisional frequency, chirp parameter, and incidence angle of a laser beam on the normalised THz amplitude. The amplitude of the THz signal diminishes fast in off-resonant conditions and tends towards zero as the normalised THz frequency exceeds 1.2. The normalised amplitude of the THz wave falls as the chirp parameter increases from 0.0011 to 0.0099, considering both the normalised THz frequency and the normalised slanting up density modulation parameter. The amplitude of the THz signal, after being normalised, is also influenced by the incident angle and the collisional frequency. In the off-resonant state, the normalised amplitude of the THz wave tends to approach zero when the collisional frequency exceeds 0.8. The objective of this study is to enhance the current knowledge regarding the estimation of the best incident oblique

angle, chirp parameter, and collisional frequency to attain an energy-efficient THz source.

Keywords Terahertz frequency · p-Polarised laser beam · Slanting up density modulation · Chirp parameter · Energy efficiency

Introduction

The terahertz (THz) frequency range is situated between the infrared and microwave regions, namely between the frequency range of 10^{11} – 10^{13} Hz. The THz gap exhibits significant promise in various domains such as THz spectroscopy, topography, communication, food production and quality control, hence offering substantial chances for scholars and scientists [1–4]. Over the past three decades, there has been a significant increase in the development of systems for generating THz radiation [5–15].

Forlov et al. [16] conducted a theoretical investigation on the effects of p-polarised radiation on semi-bounded plasma. Strong THz amplification is observed when an ultra-short laser pulse is incident at or near the critical angle. The study conducted by Xie et al. [17] focuses on investigating the creation of THz waves by the utilisation of laser-induced air plasma. The findings demonstrate that efficient THz radiation production occurs when the incident laser possesses the same polarisation state. The chirped laser pulse with a hot inhomogeneous ripple density plasma was investigated by Hashemzadeh [18]. The individual conducts research on the impact of frequency chirp, laser intensity, electron temperature, and electron density inhomogeneity on THz wave production. The investigation conducted by Li et al. [19] examines the interaction between laser and solid materials using chirped

✉ Vishal Thakur
vishal20india@yahoo.co.in

¹ Department of Physics, Lovely Professional University, Phagwara, Punjab 144411, India

² Department of Physics, University of Allahabad, Prayag Raj, Uttar Pradesh, India

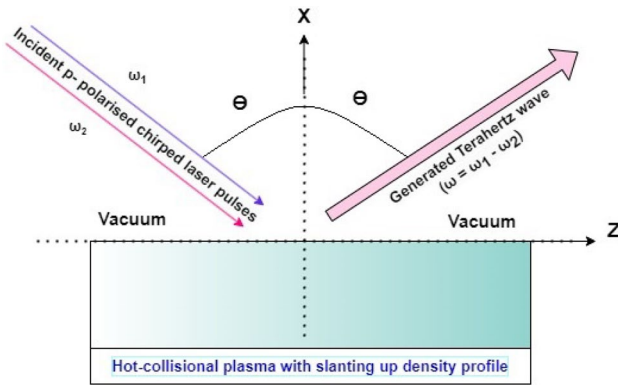
laser pulses at relativistic intensity. This study investigates the generation of transit current through the nonlinear interaction between laser and plasma, specifically focusing on the copper foil material. The study conducted by Huang et al. [20] investigated the concurrent emission of THz and X-rays resulting from the interaction between an intense, brief laser pulse and a thin, unconfined water flow in air. They demonstrate the progression of material alteration. In their study, Liao et al. [21] provide a comprehensive analysis of the diverse techniques employed for the generation of THz radiation. These approaches encompass the utilisation of plasma waves, electron transport, and emission as means of THz generation. The study conducted by Zheng et al. [22] examined the utilisation of particle-in-simulations to investigate the creation of THz waves by laser interactions at the interface between a vacuum and plasma. The energy of induced THz waves is typically on the order of a few megawatts. The study conducted by Amouamouha et al. [23] focuses on the creation of THz radiation through the interaction of a super Gaussian laser beam with a plasma characterised by ripple density. The researchers employed the paraxial approximation approach in their investigation. The researchers tuned various laser plasma settings in order to achieve a THz efficiency of 6.5%. Hamsters [24] have the capability to generate sub-picosecond THz radiation by the use of laser-produced plasma. The author demonstrates that the creation of THz radiation is more pronounced when solid targets are employed as opposed to gas targets. In their study, Thakur et al. [25] investigate the phenomenon of second harmonic production induced by a chirped laser pulse in a plasma density ramp accompanied by a transverse magnetic field. In their research, Hashemzadeh [26] investigated the creation of THz radiation using Hermite-cosh-Gaussian and hollow Gaussian laser beams in a magnetised plasma with spatial variations. The researcher investigates the impact of a decentred parameter and an external magnetic field on the efficiency of THz generation. The study conducted by Jahangiri et al. [27] focuses on the development of powerful THz radiation within the range of 10–70 millijoules (mJ) from plasma formed by argon clusters. In this research, Sharma et al. [28] investigate the characteristics of the cosh-Gaussian laser beam within a wiggler magnetised plasma environment, with a specific focus on its potential for generating second harmonics. The results of argon gas are compared with those of argon clusters. The study conducted by Bakhtiari et al. [29] focuses on the creation of THz radiation by the utilisation of two Gaussian laser array beams. The researchers investigate the laser and array structure factors in order to optimise the creation of THz radiation for enhanced efficiency. In their study, Gurjar et al. [30] investigate the creation of THz waves in a spatially slanted density plasma profile through the

beating of a chirped laser pulse. The maximum amplitude of THz waves occurs when the phase matching resonance condition is satisfied, namely at a specific slanting angle of plasma density. Thakur et al. [31] conducted a study on the phenomenon of self-focusing shown by Hermite-cosh-Gaussian laser pulses in a collisionless cold plasma characterised by an exponential density profile.

The work conducted by Mou et al. [32] investigates the impact of laser chirp on the polarisation of THz radiation. The findings demonstrate that positive and negative chirp has contrasting impacts on the polarisation state and phase difference of THz waves. The numerical investigation conducted by Nguyen et al. [33] examines the impact of chirp and time delay on the efficacy of THz generation. The researchers employ three-dimensional simulation techniques to achieve a conversion efficiency of 10^{-4} for THz radiation. Zhang et al. [34] employ the photocurrent model to theoretically investigate the creation of THz radiation through the interaction of a monochromatic chirped laser pulse with a gas plasma. The chirped and chirp-free laser pulses are compared in terms of their THz yield. In their research, Xing et al. [35] investigate the THz emission resulting from laser chirping in an air plasma. They employ the linear dipole array approach to analyse this phenomenon. In their study, Ghayemmoniri et al. [36] investigate the creation of THz pulses through the interaction of two chirped laser pulses with a carbon nanotube array in the presence of an external tapered magnetic field. The findings demonstrate that a tapered magnetic field has the ability to modulate the THz field.

Scientists and academics employ various laser and plasma characteristics to investigate distinct mechanisms, including self-focusing, Wakefield acceleration, harmonic creation, and THz generation [25, 31, 37–42].

In the present investigation, a pair of p-polarised chirped laser beams are directed towards a hot collisional plasma characterised by a slanting up density profile. The phenomenon of laser plasma interaction leads to the production of high-intensity THz waves. The optimisation of laser and plasma characteristics enables the attainment of an efficient source of THz radiation. Section "[Analytical study of THz generation](#)" of this work involves the analytical derivation of the ponderomotive force, equation of motion, nonlinear plasma current density, and the subsequent generation of THz fields. In this study, section "[Result and discussion](#)" investigates the correlation between the normalised THz electric field and various parameters, such as the normalised THz frequency, normalised slanting up density modulation, incidence angle, normalised collisional frequency, and chirp parameter. In the section "[Conclusion](#)", the Conclusions are presented. The document is concluded by incorporating references.



Analytical study of THz generation

Two p-polarised laser beams are propagating in x - z plane and interact with hot slanting up density plasma modulation having density profile $n = n_0 e^{k_z z}$ (where n_0 is plasma density at $z = 0$ and k_z is wave number of plasma density). Electric and magnetic fields of laser pulses are given by these equations. Electric field of two p-polarised laser beams is

$$\vec{E}_J = (\hat{z} \cos - \hat{x} \sin) E_{0J} e^{-i(\omega_J t - k_J(z \sin + x \cos))}, \quad \text{where } J = 1, 2 \quad (1)$$

In this context, E_{0J} represents the amplitude of the laser beam, θ denotes the angle of incidence, ω_J signifies the angular frequency and k_J represents the propagation constant of incidental laser beam.

Corresponding magnetic field of laser beam is

$$\vec{B}_J(r, z) = \frac{(\vec{k}_J \times \vec{E}_J(r, z))}{\omega_J}, \quad \text{where } J = 1, 2 \quad (2)$$

Incident laser beam is positively chirped, and chirp is represented as

$$\omega_1 = \omega_0 + b\omega_0^2 \left(t - \frac{(z \sin + x \cos)}{c} \right),$$

where ω_0 is the frequency of incident laser beam in the absence of chirp, b is chirp parameter, c is velocity of light in vacuum. We choose ω_2 such as $\omega_1 - \omega_2 = \omega$ lies in THz range.

So,

$$\omega_2 = \omega_1 - \omega = \left\{ \omega_0 + b\omega_0^2 \left(t - \frac{(z \sin + x \cos)}{c} \right) \right\} - \omega \quad (3)$$

During the initial stage, it can be assumed that electrons are in a state of rest, resulting in the absence of any magnetic force acting upon them. The oscillatory velocity of a plasma electron can be determined by using the equation of motion

$$m \left(\frac{d\vec{V}_J}{dt} \right) = -e\vec{E}_J - m\vec{V}_J\nu_{en}$$

where ν_{en} is collision frequency of collisional plasma.

By solving this equation, we get.

$$\vec{V}_1 = \frac{e\vec{E}_1}{im\omega_0 \left\{ 1 + b\omega_0 \left(2t - \frac{(z \sin + x \cos)}{c} \right) \right\} - m\nu_{en}} \quad (4)$$

$$\vec{V}_2 = \frac{e\vec{E}_2}{im\omega_0 \left\{ 1 + b\omega_0 \left(2t - \frac{(z \sin + x \cos)}{c} \right) - \frac{\omega}{\omega_0} \right\} - m\nu_{en}} \quad (5)$$

Here e, m, ν is charge, rest mass and collisional frequency of the plasma electron, respectively.

This oscillatory velocity of plasma electron gives rise to nonlinear ponderomotive force.

Nonlinear ponderomotive force is

$$\vec{F}_P^{NL} = -\frac{e}{2c} (\vec{V}_1 \times \vec{B}_2^* + \vec{V}_2^* \times \vec{B}_1) - \frac{m}{2} \vec{\nabla} (\vec{V}_1 \vec{V}_2^*) \quad (6)$$

Here, * represents the complex conjugate.

Solving this equation by putting values of $\vec{V}_1, \vec{V}_2^*, \vec{B}_1,$ and \vec{B}_2^* and neglecting the higher order derivatives of second term, we get

$$\vec{F}_P^{NL} = (\hat{x} \cos + \hat{z} \sin) \frac{e^2 E_1 E_2^*}{2im\omega_0 c} \left\{ \frac{2 \frac{\nu}{i\omega_0} - \frac{\omega}{\omega_0}}{\left\{ 1 + b\omega_0 \left(2t - \frac{(z \sin + x \cos)}{c} \right) - \frac{\nu_{en}}{i\omega_0} \right\} \left\{ 1 + b\omega_0 \left(2t - \frac{(z \sin + x \cos)}{c} \right) - \frac{\omega}{\omega_0} + \frac{\nu_{en}}{i\omega_0} \right\}} \right\} \quad (7)$$

By solving the equation of motion $\partial \vec{V}_\omega^{NL} / \partial t = \vec{F}_P^{NL} / m - \nu_{en} \vec{V}_\omega^{NL}$ and equation of continuity $\partial n_\omega^{NL} / \partial t + \vec{\nabla} \cdot n \vec{V}_\omega^{NL} = 0$, For slanting up density profile $n = n_0 e^{k_z z}$, we get nonlinear oscillatory velocity and nonlinear density perturbation of plasma electron as per given equation.

$$\vec{V}_\omega^{NL} = \frac{i\omega \vec{F}_P^{NL}}{m(\omega^2 + i\omega\nu_{en})} \quad (8)$$

$$n_{\omega}^{NL} = \frac{n_0 \vec{\nabla} \cdot (e^{k_z z} \vec{F}_P^{NL})}{m(\omega^2 + i\omega v_{en})} \tag{9}$$

In this derivation, we consider n is constant with time, and is a function of z only so $\partial(n)/\partial t = 0$.

This nonlinear density perturbation n_{ω}^{NL} gives rise to self-consistent space charge potential ϕ and field, because of separation of electrons from ions. This gives rise to linear density perturbation as $n_{\omega}^L = -\chi_P \vec{\nabla} \cdot (\vec{\nabla} \phi) / 4\pi e$ where $\chi_P = -\omega_p^2 / (\omega^2 + i\omega v_{en} - k^2 V_{th}^2)$ is electric susceptibility of collisional plasma.

Using Poisson's equation $\nabla^2 \phi = 4\pi(n_{\omega}^L + n_{\omega}^{NL})e$, we get linear force \vec{F}_P^L due to space charge field on electrons such as.

Linear force

$$\vec{F}_P^L = e\vec{\nabla} \phi = \frac{\omega_p^2 e^{k_z z} \vec{F}_P^{NL}}{(1 + \chi_P)(\omega^2 + i\omega v_{en})} \tag{10}$$

as $\omega_p = \sqrt{4\pi n_0 e^2 / m}$ is plasma frequency.

By solving the equation of motion $\partial \vec{V}^{NL} / \partial t = (\vec{F}_P^{NL} + \vec{F}_P^L) / m - v_{en} \vec{V}^{NL}$, one may determine the nonlinear oscillatory velocity of electrons because of the linear and nonlinear ponderomotive forces as

$$\vec{V}_{\omega}^{NL} = \frac{1}{m} \left\{ \frac{\omega^2 + i\omega v_{en} - \omega_p^2 + \omega_p^2 (e^{k_z z})}{(-i\omega + v_{en})(\omega^2 + i\omega v_{en} - \omega_p^2)} \right\} \vec{F}_P^{NL} \tag{11}$$

Here, we consider $\omega_1, \omega_2 \gg \omega_p$.

$\vec{J}^{NL} = -\frac{1}{2} n e \vec{V}^{NL}$, where $n = n_0 e^{k_z z}$ is density perturbation which is much greater than the n_0 .

$$\Rightarrow \vec{J}^{NL} = -\frac{n_0 e}{2m} \left\{ \frac{\omega^2 + i\omega v_{en} - \omega_p^2 + \omega_p^2 (e^{k_z z})}{(-i\omega + v_{en})(\omega^2 + i\omega v_{en} - \omega_p^2)} \right\} \vec{F}_P^{NL} e^{i(kz - \omega t)} \tag{12}$$

where $(k_1 - k_2) = k$ and $(\omega_1 - \omega_2) = \omega$.

This nonlinear current density is responsible for THz generation. By using III and IV Maxwell's equation, $\vec{\nabla} \times \vec{E} = -\frac{1}{c} (\partial \vec{B} / \partial t)$ and $\vec{\nabla} \times \vec{B} = (\epsilon/c) (\partial \vec{E} / \partial t) + (4\pi/c) \vec{J}^{NL}$, we can calculate the THz wave generation equation.

Equation for THz generation is

$$\vec{\nabla} \cdot (\vec{\nabla} E_{THz}) - \nabla^2 E_{THz} = \frac{\omega^2}{c^2} \epsilon E_{THz} + \frac{4\pi i \omega}{c^2} \vec{J}^{NL} \tag{13}$$

In order to neglect higher-order derivatives due to fast variation of THz field. So normalised THz amplitude is

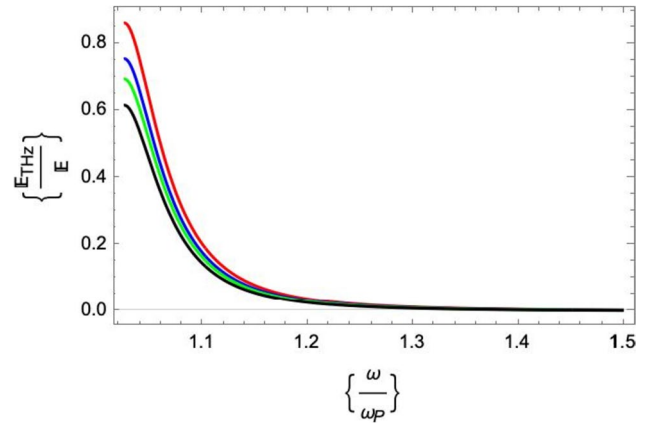


Fig. 1 Variation of normalised THz amplitude with normalised THz frequency for chirp parameter $b = 0.0011$ (red), 0.0044 (blue), 0.0066 (green), 0.0099 (black). For $k_z = 0.9$ k. Other parameters are same as mentioned above (colour figure online)

$$\frac{E_{THz}}{E} = \left[\frac{\omega_p^2 e E}{\epsilon \omega m \omega_0 c} \left\{ \frac{\omega^2 + i\omega v_{en} - \omega_p^2 + \omega_p^2 (e^{k_z z})}{(-i\omega + v_{en})(\omega^2 + i\omega v_{en} - \omega_p^2)} \right\} e^{i(kz - \omega t)} (\hat{x} \cos + \hat{z} \sin) \left(\frac{\frac{\omega}{\omega_0} - 2 \frac{v_{en}}{i\omega_0}}{\left\{ 1 + b\omega_0 \left(2t - \frac{(z \sin + x \cos)}{c} \right) - \frac{v_{en}}{i\omega_0} \right\} \left\{ 1 + b\omega_0 \left(2t - \frac{(z \sin + x \cos)}{c} \right) - \frac{\omega}{\omega_0} + \frac{v_{en}}{i\omega_0} \right\}} \right) \right] \tag{14}$$

Here, we consider incidental beam has same electric field amplitude $E_{01} = E_{02} = E$ is the amplitude of incident laser beam.

Result and discussion

In this investigation of THz generation, two p-polarised laser beams are positively chirped and propagating in hot collisional underdense plasma. For this study we choose suitable laser parameter such as femtosecond Ti-Sapphire laser with wave length of 800 nm having angular frequency 2.35×10^{15} rad/sec, chirp parameter of 0.0011, propagation distance (z)=propagation distance (x)=20 μ m, time $t = 50$ fs, incidence angle is $\pi/6$ radian and electric field amplitude of 1×10^{12} V/m. Plasma parameters are optimised as plasma density is $5 \times 10^{23} \text{m}^{-3}$. Here in the present study, we choose $\omega = 1.025\omega_p$ where $\omega_1, \omega_2 > \omega_p$ and $v_{en} = 0.1\omega_p$.

Effect of normalised THz frequency (ω/ω_p)

In this study variation of normalised THz amplitude is analysed with normalised THz frequency at $k_z = 0.9$ k for chirp parameter $b = 0.0011$ (red), 0.0044 (blue), 0.0066 (green), 0.0099 (black).

For off-resonant condition, normalised THz amplitude decreases rapidly and approaches to zero for normalised THz frequency (ω/ω_p) greater than 1.2. Normalised THz amplitude approaches more than 0.8, as we decrease the chirp parameter from 0.0099 to 0.0011. The maximum normalised THz amplitude decreases from approximately 0.8–0.6. So, increase in chirp parameter decreases the THz conversion efficiency significantly (Fig. 1).

Effect of normalised slanting up density modulation parameter (k_z/k)

This study aims to conduct a theoretical analysis of the relationship between the normalised amplitude of THz radiation and the wave propagation distance of THz waves. The analysis focuses on various values of the chirp parameter $b = 0.0011$ (red), 0.0044 (blue), 0.0066 (green), 0.0099 (black).

This study shows that normalised THz amplitude increases with normalised slanting up density modulation parameter (k_z/k). With the increase in the chirp parameter from 0.0011 to 0.0099, the maximum value of normalised THz amplitude decreases from 0.8 to 0.2 approximately (Fig. 2).

Effect of incidence angle (θ)

This study focus on examining the relationship between the normalised THz amplitude and the incident angle for chirp parameter $b = 0.0011$. In Fig. 3, normalised THz amplitude is shown along vertical axis while, oblique angle (normalised by $\pi/12$) is represented along horizontal axis. This examination shows that normalised THz amplitude changes

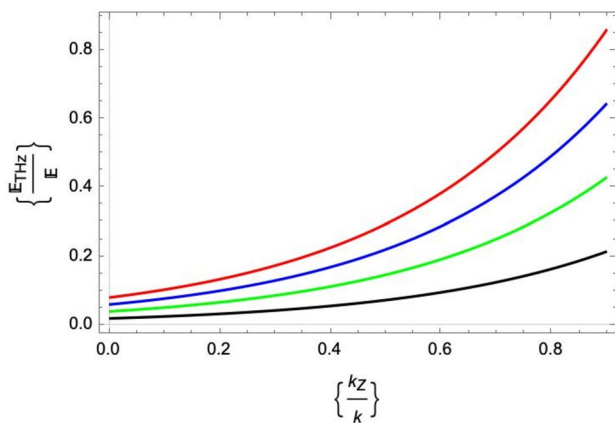


Fig. 2 Variation of normalised THz amplitude with normalised slanting up density parameter for chirp parameter $b = 0.0011$ (red), 0.0044 (blue), 0.0066 (green), 0.0099 (black). Other parameters are same as mentioned above (colour figure online)

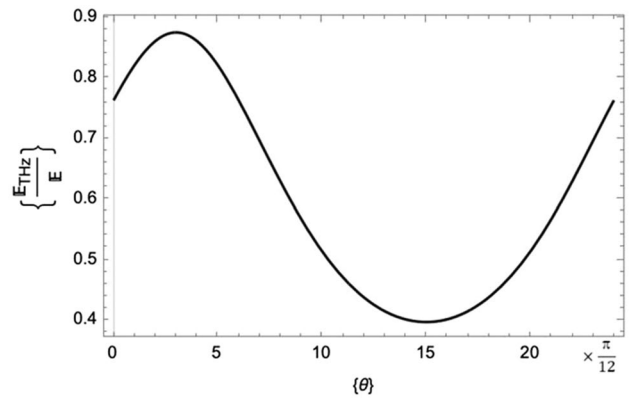


Fig. 3 Variation of normalised THz amplitude with normalised THz frequency for chirp parameter $b = 0.0011$ and $k_z = 0.9 k$. Other parameters are same as mentioned above

in oscillatory manner with incidence oblique angle and the peak of the curve (maximum THz amplitude) is obtained at normalised oblique value 3. Corresponding oblique angle is $3 * \pi/12$ or 45° with selected parameters. It concludes that for effective THz generation, oblique angle also plays a crucial role, and this angle should be optimised to obtain energy-efficient THz generation.

Normalised THz amplitude has maximum value is 0.86 for incidence angle 45° and minimum value is 0.4 for incidence angle 225° .

Effect of normalised collisional frequency (ν_{en}/ω_p)

This study focuses on examining the relationship between the normalised THz amplitude and the normalised collisional frequency for $b = 0.0011$ and $\theta = \pi/6$.

According to the findings of the investigation, the normalised THz amplitude experiences a precipitous drop as the normalised collisional frequency rises. Approximately 0.7 is the maximum value for the normalised THz amplitude. When the normalised collisional frequency is bigger than 0.8 value, the normalised THz amplitude gets closer and closer to zero. This indicates an increase in collisional properties of plasma, and there is corresponding decrease in generated THz amplitude (Fig. 4).

This investigation’s results are consistent with the findings documented by Hashemzadeh [18]. The conclusion drawn by the researchers is that the utilisation of a p-polarised chirped laser beam proves to be an efficacious approach in the generation of THz radiation. During the course of our investigation, we utilised a chirped p-polarised beam within a hot collisional slanting up plasma profile as a method for producing THz waves.

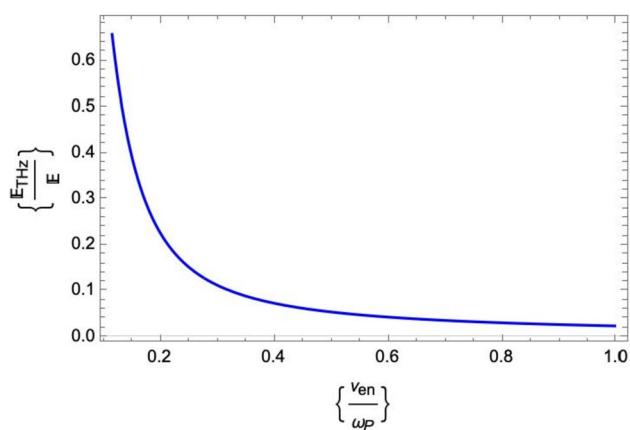


Fig. 4 Variation of normalised THz amplitude with normalised collisional frequency for chirp parameter $b=0.0011$ and $k_z=0.9$ k, $\lambda=800$ nm, $z=x=20$ μ m, $t=50$ fs. Other parameters are same as mentioned above

Conclusion

This study examines the propagation of two p-polarised chirped laser beams in a hot collisional underdense plasma medium. An analytical solution is derived to determine the efficiency of THz generation, considering various characteristics such as the normalised THz frequency, incidence angle, collisional frequency, normalised transverse distance, and frequency chirp. The resulting solution is then analysed to optimise these parameters, aiming to achieve a tuneable and energy-efficient THz source. The normalised THz amplitude exhibits significant values up to 0.8 for normalised THz frequency corresponding to chirp parameter $b=0.0011$. The findings indicate that as the value of the chirp parameter increases from 0.0011 to 0.0099, there is a decrease in the normalised amplitude of the THz signal. The normalised THz amplitude changes in oscillating manner with change in incidence angle from zero to 2π and shows a maximum for incident oblique angle 45° and minima at 225° . This study aims to contribute to the existing body of information about the determination of optimal incident oblique angle, chirp parameter, and collisional frequency for the purpose of achieving an energy-efficient THz source.

Author contribution Hitesh Kumar Midha contributed to derivation, methodology, analytical modelling, and graph plotting; Vivek Sharma contributed to numerical analysis; Niti Kant contributed to numerical analysis and result discussion; and Vishal Thakur contributed to supervision, reviewing, and editing.

Funding Not applicable.

Data availability The data that support the findings of this study are available from the corresponding authors upon reasonable request.

Declarations

Conflict of interest The authors declare no competing interest.

Ethical approval Not applicable.

Consent to participate Not applicable.

Consent for publication Not applicable.

References

1. J. Hebling, K.-L. Yeh, M.C. Hoffmann, K.A. Nelson, High-power THz generation, THz nonlinear optics, and THz nonlinear spectroscopy. *IEEE J. Sel. Top. Quantum Electron.* **14**(2), 345–353 (2008)
2. S. Watanabe, Terahertz polarization imaging and its applications. *Photonics* **5**(4), 58 (2018)
3. K. Rikkinen, P. Kyosti, M.E. Leinonen, M. Berg, A. Parssinen, THz radio communication: link budget analysis toward 6G. *IEEE Commun. Mag.* **58**(11), 22–27 (2020)
4. A.A. Gowen, C. O’Sullivan, C.P. O’Donnell, Terahertz time domain spectroscopy and imaging: emerging techniques for food process monitoring and quality control. *Trends Food Sci. Technol.* **25**(1), 40–46 (2012)
5. N. Gupta, S. Kumar, S.B. Bhardwaj, Stimulated Raman scattering of self focused elliptical q-Gaussian laser beam in plasma with axial temperature ramp: effect of ponderomotive force. *J. Electromagn. Waves Appl.* **36**(6), 767–786 (2022)
6. S. Kumar, S. Vij, N. Kant, A. Mehta, V. Thakur, Resonant terahertz generation from laser filaments in the presence of static electric field in a magnetized collisional plasma. *Eur. Phys. J. Plus* **136**(2), 148 (2021)
7. N. Gupta, Effect of orbital angular momentum of light on self-analytical effects of Laguerre Gaussian laser beams in collisionless plasmas. *J. Opt.* **50**(3), 466–477 (2021)
8. S. Kumar, S. Vij, N. Kant, V. Thakur, Resonant terahertz generation by the interaction of laser beams with magnetized anharmonic carbon nanotube array. *Plasmonics* **17**(1), 381–388 (2022)
9. S. Kumar, N. Kant, V. Thakur, THz generation by self-focused Gaussian laser beam in the array of anharmonic VA-CNTs. *Opt Quantum Electron* **55**(3), 281 (2023)
10. N. Gupta, S.B. Bhardwaj, Nonlinear interaction of Bessel-Gauss laser beams with plasmas with axial temperature ramp. *J. Opt.* **51**(4), 950–959 (2022)
11. V. Thakur, S. Vij, N. Kant, S. Kumar, THz generation by propagating lasers through magnetized SWCNTs. *Indian J. Phys.* **97**(7), 2191–2196 (2023)
12. S. Kumar, S. Vij, N. Kant, V. Thakur, Combined effect of transverse electric and magnetic fields on THz generation by beating of two amplitude-modulated laser beams in the collisional plasma. *J. Astrophys. Astron.* **43**(1), 30 (2022)
13. S. Kumar, S. Vij, N. Kant, V. Thakur, Interaction of obliquely incident lasers with anharmonic CNTs acting as dipole antenna to generate resonant THz radiation., *Waves Rand. Complex Media* 1–13 (2022). <https://doi.org/10.1080/17455030.2022.2155330>
14. N. Gupta, R. Johari, S. Kumar, S.B. Bhardwaj, S. Choudhry, Optical guiding of q-Gaussian laser beams in radial density plasma channel created by two prepulses: ignitor and heater. *J. Opt.* **51**(3), 749–760 (2022)
15. N. Gupta, S. Kumar, S.B. Bhardwaj, S. Kumar, S. Choudhry, Non-linear interaction of quadruple Gaussian laser beams with narrow band gap semiconductors. *J. Opt.* **51**, 269–282 (2021)

16. A.A. Frolov, Terahertz emission at a p-polarized laser radiation action on plasma. *Phys. Plasmas* **28**(1), 013104 (2021)
17. X. Xie, J. Dai, X.-C. Zhang, Coherent control of THz wave generation in ambient air. *Phys. Rev. Lett.* **96**(7), 075005 (2006)
18. M. Hashemzadeh, Terahertz radiation generation through nonlinear interaction of frequency chirped laser pulses with hot inhomogeneous plasmas. *Waves Rand. Complex Media* **32**(5), 2279–2296 (2022)
19. Y.T. Li, et al., Strong terahertz radiation from relativistic laser interaction with solid density plasmas. *Appl Phys Lett* **100**, 25 (2012)
20. H. Huang, T. Nagashima, W. Hsu, S. Juodkakis, K. Hatanaka, Dual THz wave and X-ray generation from a water film under femtosecond laser excitation. *Nanomaterials* **8**(7), 523 (2018)
21. G.-Q. Liao, Y.-T. Li, Review of intense terahertz radiation from relativistic laser-produced plasmas. *IEEE Trans. Plasma Sci.* **47**(6), 3002–3008 (2019)
22. Z.-M. Sheng, H.-C. Wu, K. Li, J. Zhang, Terahertz radiation from the vacuum-plasma interface driven by ultrashort intense laser pulses. *Phys. Rev. E* **69**(2), 025401 (2004)
23. M. Amouamouha, F. Bakhtiari, B. Ghafary, Self-focused amplitude modulated super Gaussian laser beam in plasma and THz radiation with high efficiency. *Results Phys.* **17**, 103086 (2020)
24. H. Hamster, A. Sullivan, S. Gordon, W. White, R. W. Falcone, Subpicosecond, electromagnetic pulses from intense laser-plasma interaction, **71** (1993)
25. V. Thakur, N. Kant, Resonant second harmonic generation in plasma under exponential density ramp profile. *Optik (Stuttg)* **168**, 159–164 (2018)
26. M. Hashemzadeh, Terahertz radiation generation by Hermite-cosh Gaussian and hollow Gaussian laser beams in magnetized inhomogeneous plasmas. *Braz. J. Phys.* **53**(2), 46 (2023)
27. F. Jahangiri, M. Hashida, T. Nagashima, S. Tokita, M. Hangyo, S. Sakabe, Intense terahertz emission from atomic cluster plasma produced by intense femtosecond laser pulses. *Appl. Phys. Lett.* **99**, 26 (2011)
28. V. Sharma, V. Thakur, N. Kant, Second harmonic generation of cosh-Gaussian laser beam in magnetized plasma. *Opt Quantum Electron* **52**(10), 444 (2020)
29. F. Bakhtiari, M. Esmaeilzadeh, B. Ghafary, Terahertz radiation with high power and high efficiency in a magnetized plasma. *Phys. Plasmas* **24**, 7 (2017)
30. M.C. Gurjar, K. Gopal, D.N. Gupta, V.V. Kulagin, H. Suk, High-field coherent terahertz radiation generation from chirped laser pulse interaction with plasmas. *IEEE Trans. Plasma Sci.* **48**(10), 3727–3734 (2020)
31. V. Thakur, N. Kant, Combined effect of chirp and exponential density ramp on relativistic self-focusing of Hermite-Cosine-Gaussian laser in collisionless cold quantum plasma. *Braz. J. Phys.* **49**(1), 113–118 (2019)
32. S. Mou et al., Impact of laser chirp on the polarization of terahertz from two-color plasma. *Photonics Res* **11**(6), 978 (2023)
33. A. Nguyen, P.G.A. de Martínez, I. Thiele, S. Skupin, L. Bergé, THz field engineering in two-color femtosecond filaments using chirped and delayed laser pulses. *New J. Phys.* **20**(3), 033026 (2018)
34. L. Zhang, L.Z. Ji, P.Y. Sun, Z.H. Jiao, S.F. Zhao, G.L. Wang, Enhanced terahertz generation by controlling electron trajectory with chirp laser field. *Indian J. Phys.*, 1–8 (2023). <https://doi.org/10.1007/s12648-023-02834-5>
35. X. Xu et al., Laser-chirp controlled terahertz wave generation from air plasma. *Chin. Phys. Lett.* **40**(4), 045201 (2023)
36. Z. Ghayemmoniri, R.N. Siahmazgi, S. Jafari, Terahertz radiation generation driven by beating of chirped laser pulses in single-walled carbon nanotubes by applying tapered magnetic field. *Eur. Phys. J. D* **77**(3), 48 (2023)
37. H. Hora, Self-focusing of laser beams in a plasma by ponderomotive forces. *Z. Phys. Hadrons Nucl.* **226**(2), 156–159 (1969)
38. P. Sprangle, G. Joyce, E. Esarey, A. Ting, Laser wakefield acceleration and relativistic optical guiding, in *AIP Conference Proceedings* (AIP, 1988), pp. 231–239
39. V. Thakur, N. Kant, Optimization of wiggler wave number for density transition based second harmonic generation in laser plasma interaction. *Optik (Stuttg)* **142**, 455–462 (2017)
40. R.A. Ganeev, High-order harmonic generation in a laser plasma: a review of recent achievements. *J. Phys. B At. Mol. Opt. Phys.* **40**(22), R213–R253 (2007)
41. V. Thakur, N. Kant, Effect of pulse slippage on density transition-based resonant third-harmonic generation of short-pulse laser in plasma. *Front. Phys. (Beijing)* **11**(4), 115202 (2016)
42. U. Teubner, P. Gibbon, High-order harmonics from laser-irradiated plasma surfaces. *Rev. Mod. Phys.* **81**(2), 445–479 (2009)

Publisher's Note Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.

Springer Nature or its licensor (e.g. a society or other partner) holds exclusive rights to this article under a publishing agreement with the author(s) or other rightsholder(s); author self-archiving of the accepted manuscript version of this article is solely governed by the terms of such publishing agreement and applicable law.