# Adsorption of Hexavalent Chromium using Natural Goethite: Isotherm, Thermodynamic and Kinetic Study

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## ABSTRACT

This paper examines the potential of natural goethite as an adsorbent for removing Cr(VI) from the aqueous solution through adsorption isotherms, thermodynamics and kinetics study. The study is based on the batch experiments as a function of initial Cr(VI) concentrations, contact time, pH and temperature at fixed solid/solution ratio. The pH has pronounced effect on process of removal and removal is higher in lower pH range, maximum (99.14 %) being at pH 2. The adsorption of Cr(VI) onto goethite is endothermic in nature and therefore, higher temperature favours the uptake. The adsorbent capacity was determined using Langmuir, Freundlich, Dubinin-Radushkevich and Temkin adsorption isotherm models. The results showed that the adsorption fits best to the Langmuir isotherm model with the adsorption capacity 0.727 mg/g. Pseudo-first-order kinetic, pseudo-second-order kinetic and intraparticle diffusion were used to analyze the adsorption kinetic at different initial Cr(VI) concentrations. The kinetic study indicated that the pseudosecond order model explained the adsorption mechanism and intra-particle diffusion was found to be the rate-controlling step. The negative values of Gibb's free energy explained that the adsorption was feasible and spontaneous.

## **INTRODUCTION**

The presence of Cr(VI) in wastewater is a major concern due to its high toxicity, carcinogenic and mutagenic properties (Buerge and Hug 1999). The Cr(VI) occurs in many industrial effluents like leather tanning, mining, electroplating, ceramic, textile industries and chromate preparation etc. (Hu et al. 2009; Anupam et al. 2011). The Cr(VI) is highly soluble in water, and thus, can move readily through soil and aquifer in different geological environment (Fendorf 1995; Dubey and Gopal 2007). Hence, proper treatment is required to reduce its concentration below the permissible limit before discharge the Cr(VI)containing wastewater. Based on its health effect and impact on the environment, the tolerance limit of Cr(VI) in potable water and discharge into inland surface water was set at 0.05 mg/L and 0.1 mg/L respectively (EPA 1990).

Various physico-chemical and biological techniques have been studied for the removal of Cr(VI) from waste water such as chemical precipitation (Yang and Kravets 2000), anion exchange resins (Shi et al. 2009), membrane processes (Kulkarni et al. 2007), reverse osmosis (Rad et al. 2009), ultrafiltration (Korus and Loska 2009), oxidation or reduction (Turan and Altundogan 2014), biosorption (Panda et al. 2011) and adsorption (Jung et al. 2013; Song and Wu 2014) etc. These methods have significant disadvantages like incomplete removal, high operation and maintenance cost, monitoring system, reagent, energy requirements, production of toxic sludge or other disposal waste product (Nemr et al. 2008). Adsorption has been proved to be one of the easily applicable and an economically feasible method for the remediation of  $\mbox{Cr}(\mbox{VI})$  (Choppala et al. 2013).

Several authors have used various natural and synthetic materials that are available in large quantities and also environmental friendly for removing Cr(VI). Among them, materials like limonite (Baig et al. 2013), akaganeite (Lazaridis et al. 2005), hematite,  $\alpha$ -alumina (Ajouved et al. 2010; Kim et al. 2007), kaolinite (Zachara et al. 1988; Rao et al. 2012), amorphous iron oxyhydroxide (Zachara et al. 1987), boehmite (Granados-Correa and Jiménez-Becerril 2009), calcined bauxite (Baral et al. 2007), mixed magnetite-maghemite nanoparticles (Chowdhury and Yanful 2010), micelle-clay (Qurie et al. 2013) have been extensively used for removal of Cr(VI) from wastewater. It has been found that iron and aluminium oxides have shown very high affinity towards Cr(VI) in an acidic medium (Ajouyed et al. 2010; Wu et al. 2016). An iron-aluminium-complex, rich laterite soil is naturally available material which can be used for removal of Cr(VI) ions was studied by many authors (Xiaohong et al. 2009; Mitra et al. 2016). Since, less work has been done on the removal of Cr(VI) using natural goethite, this paper aims to study the removal of Cr(VI) using natural goethite through the examination of adsorption isotherm, thermodynamics and kinetics study.

## MATERIALS AND METHODS

## Adsorbent

A natural goethite was collected from the Koira iron ore mines, which is located in the northern part of Odisha. The sample was crushed and sieved through 200 mesh size sieve (75  $\mu$ m) and stored for further use. The mineralogy of the sample was studied by X-ray diffraction (Ultima IV; Rigaku CBO technology) using Cu-K $\alpha$  radiation operating at 40kV and 40mA. XRD pattern obtained through the scanning rate of 2°/min and step size of 0.05%.

Mineral identification along with chemical composition and morphology of adsorbent was also carried out using high resolution transmission electron microscope (HRTEM) (FEI Tecnai G2 F30 S-TWIN) operated at 300 kV. The sample was dispersed in ethanol and drop casted on carbon-coated Cu grid which was used further for TEM analysis. The semi-quantitative elemental analysis was done through EDX equipped in HRTEM using Quantax 200 ESPRINT 1.9 version.

## **BATCH ADSORPTION EXPERIMENT**

Batch adsorption experiments was carried out for removal of Cr(VI) ion using goethite by changing initial concentration, pH, contact time and temperature at a fix amount of adsorbent dosage of 10 g/L. A stock solution of Cr(VI) was prepared by dissolving 2.8287 g of  $K_2Cr_2O_7$  (AR grade, Merck reagent) in 1 L of deionized water. The stock solution was diluted to obtain the standard solution of concentration 2, 4, 5, 10, 15, 20 and 25 mg/L. The adsorption studies were carried out by taking 1 g of goethite in 100 ml of Cr(VI) solution

and agitated in an orbital shaker at 150 rpm and 25  $^{\rm o}$ C. The pH of the solution was adjusted in the range of 2-10 by drop wise addition of 0.1 N H<sub>2</sub>SO<sub>4</sub> and NaOH solution wherever required. The contact time was studies in the range from 10 to 180 min to reach equilibrium. At timed interval, the contents were filtered through 0.22 µm sterile membrane filter paper using a vacuum pump to assure a very rapid and efficient separation of solid material. The concentration of remaining Cr(VI) ions in solution was determined by UV-Visible double beam spectrophotometer (2375 double beam spectrophotometer).

The adsorption isotherms were studied by varying the concentration (5-25 mg/L) of Cr(VI) at fixed equilibrium time of 120 minute. To investigate the kinetic during adsorption, the samples were agitated at different time periods (10, 30, 60, 90, 120 minute) with same dosage (10 g/L). The batch experiments were also conducted at different temperatures (298, 303, 308, and 313 K) to study the effect of temperature on adsorption.

The concentration of Cr(VI) ions in the solution after adsorption was determined by using diphenyl carbazide method (APHA 2012). The absorbance of the purple-violet colored solution developed in acidic solution was recorded within 10 min at 540 nm. All the tests were carried out in triplicate and the mean values were taken for calculation. The amount of Cr(VI) adsorbed at equilibrium ( $q_e$ , mg/g) and the percentage removal of Cr(VI) after adsorption by goethite was calculated by the following equation.

$$q_e = \frac{C_0 - C_e}{M} \times V \tag{1}$$

% Removal of Cr(VI) = 
$$\frac{C_0 - C_e}{C_0} \times 100$$
 (2)

where  $C_0$  and  $C_e$  (mg/L) are the initial and final equilibrium concentrations of Cr(VI), respectively. M is the amount of goethite used (g) and V is the volume of the solution (L).

## **RESULTS AND DISCUSSION**

## **Adsorbent Characterization**

The XRD pattern of the adsorbent is shown in Fig. 1. The XRD pattern indicates that the adsorbent consists of pure goethite. The goethite is identified from its characteristics peak at 4.98, 4.18, 2.69, 2.45, 2.25 and 2.19 Å along with other lower order peaks. The sharp



Fig. 1. X-ray diffraction pattern of goethite.

peaks indicate that it is in well crystalline form. The TEM image and EDX spectra of natural goethite is given in Fig. 2 that show the presence of acicular shaped goethite with subordinate quantify of Si, P and Al. The chemical analysis of goethite using EDX analysis shows concentration of Fe, Si, P and Al is 68.04, 0.81, 0.50 and 0.25 wt% respectively. Mohapatra et al (2008) reported the presence of Si, P and Al in minor quantity in goethite from the Banded Iron Formation of Orissa.

#### **Effect of Initial Concentration**

The removal of Cr(VI) ion was studied by varying the initial concentration from (2 to 25 mg/L) at pH 2 and 5 while keeping the rest of the parameters constant. It was observed that there was decrease in removal of Cr(VI) with increase in concentration (Fig. 3). The result showed that at 2 mg/L nearly 100% of Cr(VI) ions was removed at pH 2; but only 25 % was removed at the concentration of 25 mg/L. At pH 5, around 47% and 24% of Cr(VI) was removed at the concentration of 2 and 25 mg/L, respectively. This is due to the fixed number of available surface sites of goethite which become limited or saturated by Cr(VI) at certain concentration (Akar et al. 2009; Mor et al. 2007). Hence, more and more Cr(VI) ions compete for the same sites with the increase in concentration that causes decrease in removal percentage (Jung et al. 2013).

## **Effect of Contact Time**

The adsorption of Cr(VI) ions as a function of time was studied to determine the equilibrium time onto goethite. These experiments were carried out at different Cr(VI) concentration such as 2, 5 and 20 mg/L at pH 2 and keeping other parameters constant (Fig. 4). The uptake of Cr(VI) was studied for 10, 30, 60, 90, 120 and 180 minute at 2, 5 and 20 mg/L concentrations. The results indicate that the adsorption of Cr(VI) increased gradually and after 120 minute there is hardly any change in adsorption as equilibrium is achieved. At the initial time of adsorption there are more vacant sites available in the adsorbent. Hence, faster rate of adsorption occurred with the increased concentration gradient between the adsorbate in solution and adsorbent (Acharya et al. 2009). After filling the vacant sites of adsorbent, the molecules also penetrate through the pores and again adsorbed inside the surface of the adsorbent at the slower rate, which is also known as intraparticle diffusion (Baral et al. 2009).

## Effect of pH

The pH of the aqueous solution is one of the important controlling factors during adsorption process. This is mostly due to pH-dependant speciation of Cr(VI) ion and development of surface charge on the adsorbent (Weng et al., 2008). Hence, the removal of Cr(VI) ions by goethite was studied over a pH range of 2-10 with the initial concentration of 5 and 10 mg/L while keeping other parameters constant. Experimental results indicate that the removal efficiency decreases with increase in pH (Fig. 5). Maximum removal of 66% and 54% was observed at initial Cr(VI) concentration of 5 and 10 mg/ L respectively at pH 2. However, removal was not much after pH 8. These result shows that goethite can adsorb Cr(VI) ions more readily in an acidic pH range. The Cr(VI) exists in the form of several species like  $\operatorname{Cr}_3 \operatorname{O}_{10}^{2^-}$ ,  $\operatorname{H}_2 \operatorname{Cr}_2 \operatorname{O}_7$ ,  $\operatorname{Cr}_2 \operatorname{O}_7^{2^-}$ ,  $\operatorname{CrO}_4^{2^-}$ ,  $\operatorname{HCrO}_4^-$ ,  $\operatorname{H}_2 \operatorname{CrO}_4^-$  etc. depending on the solution pH (Zhao et al. 2013). Based on the Eh-pH diagram, among the Cr(VI) species, the  $HCrO_4^-$  and  $CrO_4^{2-}$  species are most dominant within pH range 1.0-6.5 and at pH > 6.5 respectively (Rai et al. 1989). With the increase in pH,  $HCrO_4^-$  is converted to  $CrO_4^{2-}$  and  $\text{CrO}_{7}^{2-}$  ions through Eqs (3) to (5)

$$H_2 CrO_4 \to H^+ + HCrO_4^- \tag{3}$$

$$H_2 CrO_4^- \to H^+ + HCrO_4^{2-} \tag{4}$$

$$2HCrO_4^- \to Cr_2O_7^{2-} + H_2O \tag{5}$$

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Fig.2. TEM image of goethite (a) and its EDX spectrum (b).

The highest adsorption removal efficiency was obtained at optimum pH 2, where  $HCrO_{4}^{-}$  ion was considered to be the dominant species. Adsorption free energy of various chromium species  $(CrO_{4}^{2-}, HCrO_{4}^{-})$  and  $Cr_{2}O_{7}^{2-}$  is one of the important factors affecting the adsorptive ability in different pH (Zhao et al. 2010). Among all the species, the adsorptions free energy of  $HCrO_{4}^{-}$  and  $CrO_{4}^{2-}$  are in the range of -2.26 to -0.52 kcal/mol and -2.13 to -0.34 kcal/mol, respectively (Weng et al. 1997). Hence, due to the lower value of the adsorption free energy of  $HCrO_{4}^{-}$  it is more favorably adsorbed than  $CrO_{4}^{2-}$  and  $Cr_{2}O_{7}^{2-}$  ions at lower pH (Hyder et al. 2014).



Fig. 3. Effect of concentration on removal of Cr(VI) by goethite at different pH 2 and 5, adsorbent dosage 10 g/L, contact time 2 h, temperature 25  $^{\circ}$ C and rotation speed 150 rpm.



**Fig. 4.** Effect of contact time on removal of Cr(VI) by goethite at different concentration 2, 5 and 20 mg/L, adsorbent dosage 10 g/L, pH 2, temperature 25 °C and rotation speed 150 rpm.

Further, the goethite has the property to develop the variable surface charge based on the prevailing pH condition. At low pH, the surface is surrounded by hydronium ions (H<sup>+</sup>) and thus, the hydroxyl goethite surface is protonated (Fe-OH<sub>2</sub><sup>+</sup>) and become positively charged. Hence, the surface favors more adsorption of  $HCrO_4^-$  ions by the electrostatic force of attraction towards goethite as mentioned in Eq. (6) and leads to high percentage removal of Cr(VI). However, when the pH value increases the adsorption capacity decreases due to electrostatic repulsion between deprotonated surface (Fe-OH) and  $HCrO_4^-/Cr_2O_7^{-2-}$  ions lead to the gradual reduction in the adsorption of Cr(VI) species (Eq. 7) (Weng et al. 2008; Namasivayam and Yamuna, 1995).

$$Fe - OH_2^+ + HCrO_4^- \rightarrow Fe - HCrO_4 + H_2O \text{ at low pH}$$
(6)

$$Fe - OH + HCrO_{4} \rightarrow Fe - HCrO_{4} + OH^{-}$$
 at high pH (7)

$$Fe - OH + CrO_{\Lambda}^{2-} \rightarrow Fe - CrO_{\Lambda}^{-} + OH^{-}$$
 at high pH (8)

From the above equations, it can be seen that at higher pH more OH<sup>-</sup> ions are available which competes with  $HCrO_4^-$  and  $CrO_4^{2-}$  ions at adsorption sites. Hence, the formation of complexes through adsorbing Cr(VI) ions is ultimately decreasing (Namasivayam and Sureshkumar, 2008).

#### **Effect of Temperature**

Influence of temperature on the adsorption of Cr(VI) ions was conducted through series of experiments between 298 and 313 K temperature. The effect of this parameter for the Cr(VI) removal was



Fig. 5. Effect of pH on removal of Cr(VI) by goethite at different concentration 5 and 10 mg/L, adsorbent dosage 10 g/L, contact time 2 h, temperature 25  $^{\circ}$ C and rotation speed 150 rpm.



**Fig. 6.** Effect of temperature on removal of Cr(VI) by goethite at different concentration 2, 4, 5 and 10 mg/L, adsorbent dosage 10 g/L, pH 2, contact time 2 h and rotation speed 150 rpm.

 $\ensuremath{\textbf{Table 1}}\xspace$  . The percentage removal of  $\ensuremath{\mathsf{Cr}}(\ensuremath{\mathsf{VI}}\xspace)$  at different temperatures onto goethite

Temperature		Percentage sorbed (%)				
(K)	2 mg/L	4 mg/L	5 mg/L	10 mg/L		
298	99.14	53.91	48.8	40.1		
303	99.57	61	54.5	46.2		
308	99.71	64.55	57.6	51.8		
313	99.87	68.09	60.4	53.3		

observed at different Cr(VI) concentration of 2, 4, 5, 10 mg/L at pH 2 with a constant adsorbent dose 10 g/L (Fig. 6). It is observed that the removal of Cr(VI) ions increases with increase in temperature which indicates that there is a better adsorption at higher temperature (Table 1). It was found that percentage removal of Cr(VI) increased from 53 to 68%, 48 to 60% and 40 to 53% at the concentration 4, 5, 10 mg/L respectively when the temperature increased from 298 to 313 K. Thus, the adsorption was found to be endothermic in nature (Selen et al. 2014). Moreover, the increase in sorption may be attributed to the increase in the number of the adsorption sites generated because of breaking of some internal bonds near the edge of active surface sites of adsorbent (Acharya et al. 2009).

### **Thermodynamic Studies**

To determine the feasibility and the nature of the adsorption process various thermodynamic parameters such as Gibb's free energy change ( $\Delta G^{\circ}$ ), enthalpy change ( $\Delta H^{\circ}$ ) and entropy change ( $\Delta S^{\circ}$ ) were calculated at different temperatures between 298 and 313 K using the following equations.

$$K_c = \frac{q_e}{C_e} \tag{9}$$

$$\Delta G = -RT \ln K_c \tag{10}$$

$$\log K_c = \frac{\Delta S^\circ}{2.303R} - \frac{\Delta H^\circ}{2.303RT}$$
(11)

The equilibrium constant,  $K_c$  (L/g), of the adsorption process is calculated first (Khezami and Capart, 2005); where  $q_e$  is the amount of Cr(VI) adsorbed per unit mass of goethite (mg/g) and  $C_e$  is the equilibrium concentration in solution (mg/L), R is the ideal gas constant (8.314 J/mol K) and T is the absolute temperature in Kelvin (K). The enthalpy ( $\Delta$ H°) and entropy ( $\Delta$ S°) were calculated from the slope and intercept based on the Van't Hoff plot between log  $K_c$  and 1/T respectively (Fig. 7). It is observed that the value of standard free energy,  $\Delta$ G°, is negative and it decreases with the increasing



Fig. 7. A plot of log  $K_c$  and 1/T of Cr(VI) adsorption by goethite at concentration of 2 mg/L, adsorbent dosage 10 g/L and pH 2.

 Table 2. Thermodynamic parameters of Cr(VI) adsorption at different temperatures by goethite

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	Temperature (K)	∆G° (kJ/mol)	∆H° (kJ/mol)	ΔS° (J/mol /K)	R <sup>2</sup>
	298 303 308 313	-6087.39 -7930.52 -10009.82 -11978.3	60.29	225.19	0.9981

temperature (Table 2). It indicates that the adsorption of Cr(VI) onto goethite is feasible and spontaneous even at high temperature (Selen et al. 2014). The enthalpy change during the adsorption process is 60.29 kJ/mol. The positive value of  $\Delta H^{\circ}$  confirmed the endothermic nature of the adsorption. Additionally, the positive value of  $\Delta S^{\circ}$  reveals the increased randomness at the solid-solution interface during the adsorption process (Malkoc and Nuhoglu, 2007).

#### **Adsorption Isotherm Models**

The adsorption isotherms are used to obtain the adsorption capacity and affinity of adsorbent. The amount of Cr(VI) ion adsorbed per unit of adsorbent and remaining in solution at equilibrium can be obtained through isotherm study. The batch experimental data were analyzed using various isotherm models such as Langmuir, Freundlich, Dubinin-Radushkevich and Temkin with initial concentrations of Cr(VI) varied from 5 to 25 mg/L at pH 2.

The Langmuir isotherm is applied to the monolayer adsorption sites on an energetically homogenous surface with a finite number of identical sites (Nemr et al. 2008). Once a site is occupied by Cr(VI), no further adsorption can take place (Ramos-Ramírez et al. 2009). The linear form of the Langmuir model is described by the Eq. (12).

$$\frac{C_e}{q_e} = \left(\frac{1}{Q_0 b}\right) + \left(\frac{1}{Q_0}\right) C_e \tag{12}$$

where  $C_e$  and  $q_e$  are the equilibrium concentration (mg/L) and the amount of Cr(VI) adsorbed per gram of goethite (mg/g), respectively. The  $Q_0$  and b are the adsorption capacity of the goethite (mg/g) and the Langmuir affinity constant (L/mg) of the binding sites, respectively. The values of Langmuir constants  $Q_0$  and b were determined from the slope and intercept respectively using the plot between  $C_e/q_e$  and  $C_e$  (Fig. 8a). The results reveal that the Langmuir isotherm has a maximum correlation coefficient ( $R^2 = 0.994$ ) which indicated that the uptake occurred on a homogenous surface through monolayer adsorption. The maximum adsorption capacity of goethite was found to be 0.727 mg/g. Table 3 summaries the comparison of the maximum adsorption capacities of various natural adsorbent including goethite.

Adsorbent	pН	$Q_{_o}$ (mg/g)	Reference
Dolomite	2	10.1	Albadarin et al. (2012)
Bentonite	2	0.57	Khan et al. (1995)
Kaolinite	4	0.447	Fritzen et al. (2006)
Montmorrillonite	2	0.167	Fritzen et al. (2006)
Feldspar	2.5	0.091	Singh et al. (1992)
Siderite	2	17	Erdem et al. (2004)
Limonite	3	10.03	Baig et al. (2013)
Wollastonite	2.5	0.686	Sharma (2001)
Goethite	2	0.727	Present study

Table 4. Separation factor  $(R_{_{\rm I}})$  of Cr (VI) adsorption at different concentration onto goethite

C <sub>0</sub> (mg/L)	R <sub>L</sub>	
5	0.251	
10	0.144	
15	0.100	
20	0.077	
25	0.063	

The result shows that goethite has the reasonable better adsorption capacity and affinity compared with other natural adsorbents. The essential features of Langmuir isotherm can be expressed in terms of dimensionless constant known as separation factor or equilibrium parameter ( $R_L$ ) using Eq. (13). It is used to predict whether the adsorption is favorable or unfavorable. When the value of  $R_L$  lies between 0 and 1 indicates favorable adsorption;  $R_L > 1$  indicates unfavorable adsorption,  $R_L = 1$  represents the linear adsorption, and the adsorption operation is irreversible if  $R_L = 0$  (Hyder et al. 2014).

$$R_{L} = \frac{1}{1 + bC_{0}}$$
(13)

where b (L/mg) and  $C_0$  (mg/L) are the Langmuir affinity constant and initial concentration of Cr(VI). Table 4 indicates the positive values of  $R_L$  for different initial Cr(VI) concentrations, and it is within 0 and 1. Thus, it indicates the adsorption is favorable and also feasible onto goethite.

The Freundlich isotherm is an empirical equation employed to describe a heterogeneous system. It can be used to describe the adsorption intensity of the goethite towards Cr(VI) and is expressed as follows (Qiu et al. 2015).

$$\log q_e = \log K_f + (1/n) \log C_e$$
 (14)

where  $K_f$  (mg/g) and n (g/L) are the empirical Freundlich constants which represent the bond strength and the adsorption intensity of the heterogeneous surface. These parameters were determined from the intercept and slope using Eq. (14) and shown in (Fig. 8b). The result from the Table 5 indicates that the adsorption reaction is favourable as the magnitude of n is 3.48, which lies between 1 and 10 (Zhao et al. 2013). In addition to the above finding, the experimental R<sup>2</sup> value of this model is very less. Thus, it can be concluded that the adsorption of Cr(VI) onto goethite is not a multi-molecular adsorption process (Wang et al. 2012).

The Dubinin-Radushkevich isotherm is applied to estimate the nature of adsorption processes, whether physical or chemical, based



**Fig. 8. (a)** Langmuir, **(b)** Freundlich, **(c)** Dubinin-Radushkevich, **(d)** Temkin adsorption isotherms obtained from various concentrations at fixed temperature 25°C by goethite.

on the free energy of adsorption (E). This isotherm does not assume a homogeneous surface or constant sorption potential (Singha et al. 2011; Akçay 2006). The linear form of this model is represented in Eq. (15).

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$$\ln q_e = \ln q_m - K_{DR} \varepsilon^2 \tag{15}$$

$$\varepsilon = RT \ln \left( 1 + \frac{1}{C_e} \right) \tag{16}$$

$$E = \frac{1}{\sqrt{-2K_{DR}}} \tag{17}$$

where  $q_{\rm m}$  (mg/g) is the isotherm constant represents the maximum adsorption capacity of goethite.  $K_{\rm DR}$  (mol²/kJ²) is a constant related to mean adsorption energy. The  $\varepsilon$  is Polanyi potential and the magnitude of E represents the mean free energy of adsorption. The plot of ln  $q_{\rm e}$  versus  $\varepsilon^2$  gives the values of  $K_{\rm DR}$  and qm from the slope and intercept respectively using Eq. (15). The straight line with a correlation coefficient (R² = 0.982) indicates that the D-R model was well fit to the adsorption of Cr(VI) ions. Again the positive value of free energy (E) proves the endothermic nature of adsorption.

The Temkin model assumes that the heat of sorption decreases linearly with the surface coverage due to interaction of adsorbent and adsorbate (Brdar et al. 2012). The linear form of Temkin isotherm is represented as follows:

$$q_e = \frac{RT}{b_T} \ln a_T + \frac{RT}{b_T} \ln C_e$$
(18)

where  $b_{\rm T}$  (kJ/mol) is the Temkin isotherm constant related to the heat of adsorption and  $a_{\rm T}$  (L/g) is the equilibrium binding constant corresponding to the maximum binding energy. R (8.314 x  $10^{-3}$  kJ/mol K) is the Universal gas constant and T is the temperature in Kelvin (K). The constants  $b_{\rm T}$  and  $a_{\rm T}$  were obtained from the slope and intercept respectively from of linear plot between  $q_{\rm e}$  and  $\ln C_{\rm e}$  using Eq. (18) (Fig. 8d).

Table 5. Comparison of isotherm models of Cr(VI) adsorption by goethite at different concentration

	Langmuir			Freundlich			Dubinin-Ra	dushkevich			Temkin	
Q <sub>°</sub> (mg/g)	b (L/mg)	$\mathbb{R}^2$	K <sub>f</sub> (mg/g)	n (L/mg)	$\mathbb{R}^2$	q <sub>m</sub> (mg/g)	K <sub>DR</sub> (mol²/kJ²)	E (kJ/mol)	R <sup>2</sup>	a <sub>r</sub> (L/g)	b <sub>r</sub> (KJ/mol)	$\mathbb{R}^2$
0.727	0.594	0.994	0.313	3.484	0.862	0.653	5 x 10 <sup>-7</sup>	1	0.982	8.449	17.90	0.891



**Fig. 9.** (a) Pseudo first order kinetic model, (b) Pseudo second order kinetic model of Cr(VI) adsorption by goethite at different concentrations 2 and 5 mg/L, adsorbent dosage 10 g/L, contact time 2 h, pH 2 at 25°C.

#### Adsorption kinetic and modeling

To understand the different adsorption mechanism various kinetic models such as pseudo first order, pseudo second order and intraparticle diffusion models were used. The kinetic data were obtained from the plots of various models as given in Table 6 based on the absorption experiment. Where q and q (mg/g) are the amounts of Cr(VI) adsorbed at equilibrium and at time (t) respectively.  $K_1$  and  $K_2$  are the rate constants of the Pseudo first and second order equations (19) and (20),  $K_d$  is the intraparticle diffusion coefficient of Eq. (21) and it was calculated from the slope of the graph;  $C_1$  is the intercept called intraparticle diffusion constant. All the models of the kinetic sorption onto goethite were plotted (Fig. 9) and the graph of intraparticle diffusion was shown in Fig. 10. The q<sub>a</sub> cal was determined from the slope for both Pseudo first and second order models; K1 and K2 were determined from the intercept of the graph. The experimental data of the models were compared with the parameters obtained from the graph of models shown in Table 7. It is observed that pseudo second order kinetic model is more suitable for the Cr(VI) adsorption onto goethite as the theoretical adsorption capacity values (q\_, cal) is more closer to that of experimentally derived parameter (q, exp).

The intraparticle diffusion model parameters were shown in Table 8 to determine whether bulk diffusion, film diffusion or intraparticle diffusion is the rate limiting step (Albadarin et al. 2012). The model suggested that if the sorption mechanism is only controlled by an intraparticle diffusion step, then a plot of  $q_t$  and  $t^{1/2}$  gives a linear relationship and the line passes through the origin (Olu-Owolabi et al. 2014). The adsorption mechanism follows more than one diffusion mechanism when the plot do not passes in origin (Doke et al. 2013). In the present study, the plot shows linearity and not passing through the origin indicating Cr(VI) adsorption is controlled by more than



Fig. 10. Intraparticle diffusion model of Cr(VI) adsorption by goethite at different concentrations 2 and 5 mg/L, adsorbent dosage 10 g/L, contact time 2 h, pH 2 at 25 °C.

 $\ensuremath{\textbf{Table 6.}}$  The kinetic models of Cr(VI) adsorption can be expressed by the following equations

Kinetic models	Equation	Plots	Eq. no.
Pseudo-first order model	$\log(q_e - q_t) = \log q_e - K_1/2.303t$	$\log(q_e - q_t)$ vs t	(19)
Pseudo-second order model	$t/q_t = t/q_e + 1/K_2 q_e^2 t$	t/q <sub>t</sub> vs t	(20)
Intra-particle diffusion	$q_t = K_d t^{1/2} + C_1$	$\boldsymbol{q}_t \; vs \; t^{1/2}$	(21)

 Table 7. Comparison of kinetic parameters of Cr(VI) adsorption at different concentration onto goethite

C <sub>0</sub> (mg/L)	q <sub>e</sub> ,exp (mg/g)	Pse ki	Pseudo first order kinetic model			udo second or kinetic model	der
		q <sub>e</sub> ,cal (mg/g)	K <sub>1</sub> (1/min)	R <sup>2</sup>	q <sub>e</sub> ,cal (mg/g)	K <sub>2</sub> (g/mg/min)	$\mathbb{R}^2$
2	0.199	0.01	0.363	0.997	0.211	0.446	0.998
5	0.329	0.006	0.563	0.962	0.415	109.68	0.965

 Table 8. Intraparticle diffusion model parameters of Cr(VI) adsorption at different concentration by goethite.

C <sub>0</sub> (mg/L)	Intraparticle coefficient $(K_d) (mg/g /min^{1/2})$	Intraparticle constant $(C_1)$ (mg/g)	R <sup>2</sup>
2	0.01	0.091	0.982
5	0.03	0.001	0.967

one mechanism. It indicates that there is some degree of boundary layer diffusion and film diffusion also plays an important role along with the intrarparticle diffusion. In Table 8, it is seen that the rate constant  $K_d$  increases with increase in the Cr(VI) concentration, which may be due to the greater concentration driving force (Albadarin et al. 2012). The intercept  $C_1$  represents the thickness of the boundary layer and it is found to be very small. It implies that the role of surface diffusion is very less as rate-limiting mechanism.

#### CONCLUSION

This study reveals that natural goethite can act as an effective and promising adsorbent to be utilized for the removal of  $\mbox{Cr}(\mbox{VI})$  ions from aqueous solution. The feasibility of adsorption process was studied in batch scale with the different parameters. The Cr(VI) removal rate decreased with increasing pH and lowering with initial Cr(VI) concentration. The increase in temperature promotes more adsorption towards goethite due to endothermic nature. Thermodynamic study obtained that the adsorption of Cr(VI) is spontaneous and feasible. The comparison of the experimental values of different isotherms showed that Langmuir isotherm confirms well from its correlation coefficient value with maximum adsorption capacity 0.727 mg/g. This observation revealed that the adsorption of Cr(VI) onto goethite is a monolayer sorption. The kinetic studies of adsorption suggested that, the sorption followed pseudo-second-order kinetic model, where the Cr(VI) ions slowly diffuse inwards and adsorb to the inner site of adsorbent.

Acknowledgements: First author acknowledges the TEQIP-II for financial support in the form of fellowship and the NIT, Rourkela for providing analytical facilities.

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(Receieved: 23 December 2017; Revised form accepted: 11 May 2018)