

A Method for Estimating Crack-initiation Stress of Rock Materials by Porosity

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Abstract: Crack-initiation stress of a rock under compression is the stress level that marks the initiation of the rock microfracturing process or in other words, the onset of new damage to the rock. This paper proposed a simple methodology with justifications to explore the feasibility of using total and effective porosities as estimators of crack-initiation stress of brittle crystalline rock materials under uniaxial compression. The validity/applicability of the proposed method was examined by an experimental study of granitic materials from Malanjkhand, Madhya Pradesh. It was found that effective porosity depicts better correlation with crack-initiation stress than with uniaxial compressive strength of the granitic materials. On the other hand, total porosity does not show any perceptible correlation with uniaxial compressive strength and crack-initiation stress. Plausible reasons for the nature of the obtained results were also explained in view of rock failure process under compression. It is concluded that following the proposed method, effective porosity can be used as a physical index to obtain a quick estimate of crack-initiation stress of the investigated rocks empirically.

Keywords: Granite, Crack-initiation stress, Uniaxial compressive strength, Rock failure process, Porosity.

INTRODUCTION

An excavation in rocks causes redistribution of *in-situ* stresses and this could lead to brittle fracturing at or near the excavation boundary and permeability increase of the host rock in close proximity of the excavation (Lau and Chandler, 2004; Verma et al., 2011). Ascertaining the initiation and development of stress-induced microcracks in brittle rock is, therefore, potentially important. Crack-initiation stress (ci) of a rock under compression is the stress level that marks the initiation of the rock microfracturing process or in other words, the onset of new damage to the rock.

In-situ, a rock mass is generally under triaxial stress conditions. As compressive strength of a rock material increases with the increase in confining pressure, uniaxial compressive strength (UCS) provides a measure of minimum strength a rock material can have under compression and therefore, UCS is considered as the parameter to gauge strength of rock materials in Rock Mass Rating (RMR) proposed by Bieniawski (1989). Although UCS of a rock material corresponds to maximum uniaxial compressive stress the material can sustain prior to failure, formation and propagation and/or coalescence of microcracks begin long before this stage. In order to understand this, laboratory

tests involving various rock types, loading conditions, specimen shapes, and observation methods have been performed by many researchers (e.g. Brace et al., 1966; Bieniawski, 1967; Wawersik and Brace, 1971; Lajtai and Lajtai, 1974; Hallbauer et al., 1973; Swan, 1975; Henry et al., 1977; Chen et al., 1979; Nolen-Hoeksema and Gordon, 1987; Huang et al., 1993; Martin and Chandler, 1994; Eberhardt et al., 1998; Li et al., 2003; Zhang and Wong, 2013; Nicksiar and Martin, 2012 and 2013; Palchik, 2013). According to these investigations, determination of crack-initiation stress under uniaxial/triaxial compression not only requires quality machined specimens (ASTM D4543, 2001) but also demands sophisticated and expensive laboratory test setup (elaborated in the next section). In spite of such pricey methods adopted by previous researchers, accuracy of the obtained crack-initiation stress value was not guaranteed. Predicting crack-initiation stress empirically from another meaningful/relevant rock index property that is easy to determine and inexpensive is, therefore, useful at site investigation stage for obvious reasons. Porosity is one of the most often used physical indices to predict rock mechanical properties (e.g. Dunn et al., 1973; Dearman et al., 1978; Lumb, 1983; Palchik and Hatzor, 2000; Kahraman et al., 2005; Basu, 2006). It is also well-known that role of

microcracks is of great importance in controlling the mechanical behavior of rocks (e.g. Kranz, 1983; Goodman, 1989; Akesson et al., 2001; Nasser et al., 2005; Basu et al., 2009). However, till date, no attempt has been made to predict crack-initiation stress by porosity or by any other rock index property. This paper proposes a simple methodology to explore the feasibility of using total porosity (ratio of total volume of voids to total rock volume) and effective porosity (a measure of interconnectedness of pores with reference to water permeability) as estimators of crack-initiation stress of rock materials under uniaxial compression. The validity of the proposed method is examined by an experimental study of granitic materials from Malanjkhanda, Madhya Pradesh.

JUSTIFICATION FOR THE PROPOSED METHODOLOGY

When a brittle crystalline rock material is subjected to uniaxial compression (Fig. 1a), the failure process of the material could be divided into a number of stages. Based on

the stress-strain behavioral response of the material, Brace (1964) and Bieniawski (1967) described these stages as (i) crack closure, (ii) linear elastic deformation, (iii) crack initiation and stable crack growth and (iv) crack-damage and unstable crack growth leading to failure. The generalized axial stress (σ_{axial}) vs. axial (ϵ_{axial}) and lateral ($\epsilon_{lateral}$) strain curves expected from a uniaxial test of a brittle crystalline rock material is presented in Fig. 1b. The elements of crack development within the rock specimen under uniaxial compression are explained in Fig. 1c in relation to the different stress thresholds indicated in Fig 1b. Under uniaxial state of stress, pre-existing microflaws/microcracks/Griffith flaws (assumed to be elliptical in shape) with suitable dimensions and orientations with respect to the maximum principal stress get closed as the applied compressive stress reaches a particular level known as crack-closure stress (cc) (Figs. 1b and c). During the process of crack closure, a non-linear stress-strain response is exhibited (Fig. 1b). The rock material which has become virtually flawless/intact starts portraying linear elastic behavior (Fig. 1b). When the tensile stresses induced by compression exceed the local tensile

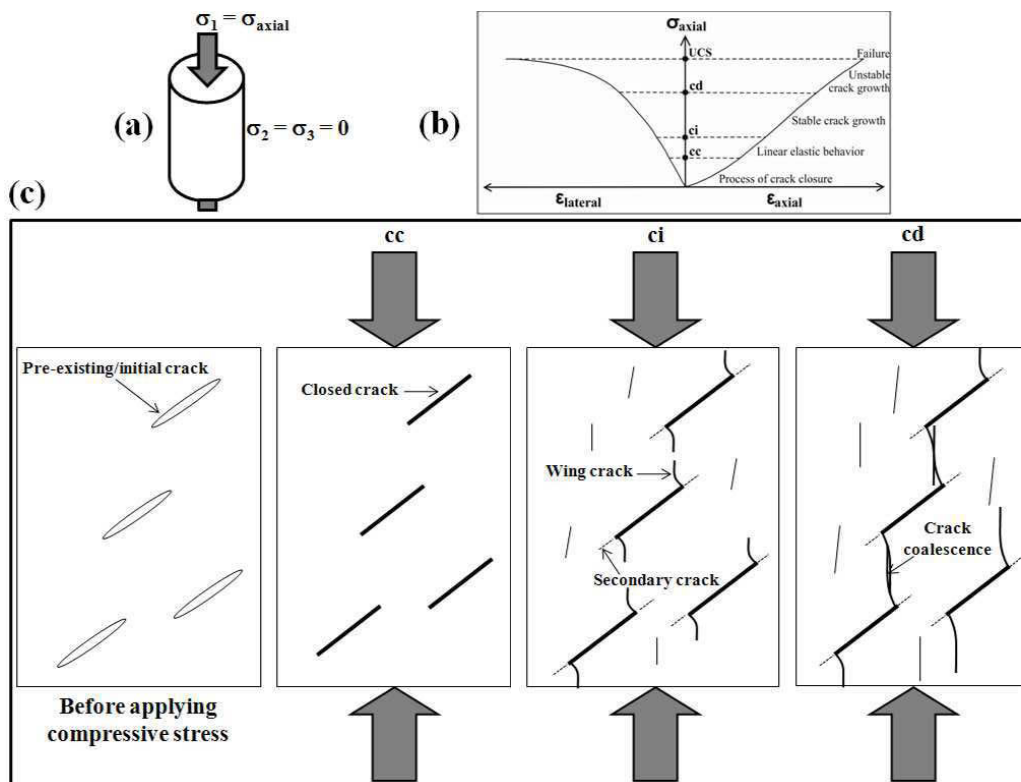


Fig.1. (a) Schematic representation of uniaxial compression of a brittle crystalline cylindrical rock specimen. (b) Generalized axial stress (σ_{axial}) vs. axial (ϵ_{axial}) and lateral ($\epsilon_{lateral}$) strain curves expected from a uniaxial compression test of a brittle crystalline rock material and corresponding stages of rock failure process (abbreviations used: cc = crack-closure stress, ci = crack-initiation stress, cd = crack-damage stress, and UCS = uniaxial compressive strength) [modified after Martin (1993)]. (c) Elements of crack development (initiation, propagation and coalescence) within the rock specimen under uniaxial compression in relation to the different stress thresholds (i.e. cc, ci and cd) (modified after Cai et al. 2004).

strength at the tips of the pre-existing flaws, crack propagates from those tips and propagating cracks, known as wing cracks, make themselves parallel to the maximum principal stress (Einstein and Dershowitz, 1990; Bobet and Einstein, 1998) (Fig. 1c). Secondary cracks also form simultaneously with wing cracks, but in the crack planes of the flaws (Bobet and Einstein, 1996) (Fig. 1c). These new cracks are generated at crack-initiation stress (σ_{ci}) where the stress-strain curves depart from linearity indicating development and growth of stable cracks (Figs. 1b and c). As at this stage, crack growth can be stopped by controlling the applied stress, it is known as stable crack growth. The stress level beyond which crack propagation and coalescence become unstable/time-dependent is known as crack-damage stress (σ_{cd}) (Figs. 1b and c). In other words, from crack-damage stress level (σ_{cd}), with little or no increase in applied stress, crack coalescence can continue and subsequently, unstable crack growth leads to specimen failure. The crack-initiation stress, as determined through laboratory testing, has been defined as the point where the lateral strain curve departs from linearity (Brace et al., 1966; Bieniawski, 1967; Lajtai and Lajtai, 1974). However, examination of the lateral strain curve reveals that the identification of this point can be very subjective as at no time is the lateral stress-strain curve truly linear. Noting this difficulty, Martin (1993) suggested the use of the calculated crack-volumetric strain to identify crack initiation and defined crack initiation stress as the stress level at which dilation (crack-volume increase) begins in the crack-volume plot (readers are referred to Martin and Chandler, 1994). It should be noted that approximation of volumetric strain requires simultaneous measurement and recording of both axial and lateral strains ($\epsilon_{\text{volumetric}} \approx \epsilon_{\text{axial}} + 2\epsilon_{\text{lateral}}$). Nicksiar and Martin (2012) have recently introduced a technique that relies on the lateral strain response. In this method, the change in recorded lateral strain relative to a reference line is used to calculate lateral strain difference value. The crack initiation stress is determined by fitting a best-fitted parabola and selecting the stress associated with maximum strain difference. This technique, however, is also not free from approximation error.

Acoustic emission is another tool to identify initiation and propagation of cracks in rocks under compression (Scholz, 1968; Hardy, 1977; Eberhardt et al., 1998). The elastic strain energy stored within a rock material under compression is suddenly released in the form of elastic waves and the related acoustic emission patterns correlate well with the stress-strain behavior of the material under compression as described in the previous paragraph. In either of these techniques (i.e. techniques of determining crack-initiation stress from crack-volume plot and from acoustic emission

patterns), complex and expensive experimental setups are needed, whereas, finding out error-free value of crack initiation stress is not guaranteed.

In this study, analysis of the axial stress vs. axial strain curve obtained from uniaxial tests of rock materials is proposed to find out crack-initiation stresses. As axial strain is easier to determine and record than lateral strain in practice and as in terms of magnitude it is greater than lateral strain because of the Poisson's effect, axial stress vs. axial strain curve is expected to depict different stages of failure processes more conspicuously than axial stress vs. lateral strain curve. By doing this, both approximation of volumetric strain and measurement of lateral strain could be avoided. The proposed method is also significantly cheaper than acoustic emission technique.

Feasibility of using total and effective porosities (n_t and n_e respectively) in estimating crack-initiation stress of granitic materials determined by adopting the method described above is also proposed to be explored in this study. It is well-known that existing pores (or flaws) in a rock material under compression are significant stress concentrators and therefore, strongly influence the rock strength (Dunn et al., 1973; Logan, 1987; Scott and Nielson, 1991). Relations between UCS of rock materials and porosity have been reported by a number of researchers (e.g. Dunn et al., 1973; Dearman et al., 1978; Lumb, 1983; Vernik, et al., 1993; Schultz and Li, 1995; Al-Harthi et al., 1999; Tugrul and Zarif, 1999; Palchik and Hatzor, 2000; Kahraman et al., 2005; Basu, 2006; Yilmaz and Yuksek, 2009). In Indian context, however, there exist a few studies that have presented relations between compressive strength and porosity. Gupta and Rao (1998) found that negative curvilinear relationships exist between UCS and n_t of fresh to weathered Malanjkhanda granites, Nagpur basalts and Delhi quartzites. Chatterjee and Mukhopadhyay (2002) demonstrated a negative linear relationship between UCS and n_e for rocks like sandstones, siltstones, limestones, shale and augen gneiss from Krishna-Godavari and Cauvery basins. Chatterjee et al. (2005) provided relations of UCS and n_e for Indian black decorative stones from ten active quarries in Andhra Pradesh. An unusual positive linear relationship was found by them. This unacceptable relation seems to have been resulted from the flawed approach of mixing data from different rock types with different geology adopted in this investigation. Mishra and Basu (2013) demonstrated why data from different rock types should not be clubbed together while correlating porosity and UCS. Although determination of σ_{ci} of rocks under uniaxial compression has been a part of several research works, to the best of the authors' knowledge, no attempt has been

made to check the efficiency of n_t and n_e in predicting c_i . As crack-initiation takes place from the tips of the pre-existing flaws, performance of n_t and n_e in estimating c_i is proposed to be evaluated in this study. Granite is a virtually isotropic crystalline igneous rock and the porosity of this rock is mainly attributed to microcracks present in it. Moreover, several earlier studies explored the issue of crack-initiation stress determination following other methods for granitic materials. Therefore, granite is consciously chosen to examine the validity of the proposed method in this study.

SAMPLES

Core samples (diameter \approx 58mm) of granitic rocks were collected from Malanjkhanda Copper Project, Malanjkhanda, Madhya Pradesh for the investigation. Malanjkhanda granitoid is exposed in Balaghat district of Madhya Pradesh, which intrudes the Amgaon and Nandgaon Groups, and is overlain by younger Chilpi metasediments (Kumar et al., 2004). Granites collected for testing are from gray and pink granitoid of Palaeoproterozoic (\sim 2400 Ma) age. These granitoids are essentially mica-bearing, and have been subjected to deuteric alterations (Panigrahi et al., 2004).

Only fresh or slightly discolored intact and uniform cores (devoid of densely spaced fractures, any shear signature or mixed lithology) were selected for the investigation. Preliminary visual inspection of the cleaned core surfaces ascertained comparable mineralogy and texture of the samples. All samples are grayish or pinkish in colour, medium grained and display equigranular phaneritic texture (Fig. 2). Uniaxial compression test specimens (length-diameter ratio \approx 2:1) were prepared according to ASTM D4543 (2001) stipulations. Two/three specimens from the same core sample were also obtained for determining effective porosity (n_e). Powdered equivalents of the samples were prepared for total porosity (n_t) measurement.

LABORATORY INVESTIGATIONS AND DATA ANALYSIS

An Automatic Compression Test Machine (AIM-314-FA[®]) of 1000kN loading capacity was used for uniaxial compression tests (Fig 3a). The compressive strength of rocks usually increases with the increase in loading rate (Vutukuri et al., 1974). Martin (1993) noted that UCS of granite is not a unique material property but is dependent on loading conditions such as the loading rate. Therefore, the standards (e.g. ASTM D2938, 2001) stipulate the loading rate in case of UCS determination. The crack-initiation stress was found to be more characteristic of the material, essentially independent of loading rate (Martin, 1993; Eberhardt, 1998). In this study, a loading rate of 0.5kN/s was employed in compliance with ASTM D2938 (2001). An LVDT attached to a compressometer gripping the core specimen was meant for measuring axial deformation (Fig. 3a). The data acquisition system (Fig. 3a) was operational to record both applied load and axial deformation simultaneously. A total of 39 uniaxial tests were carried out along with continuous and simultaneous recording of load and axial deformation. From the failure load, UCS was calculated (Fig. 3b). It should be noted that according to the stipulations by ASTM D4543 (2001), a uniaxial compression test specimen should be cylindrical in shape and the specimen shall have a length-to-diameter ratio of 2.0 to 2.5 and a diameter of not less than 47 mm. As in this study, the specimen shape and size were in compliance with ASTM D4543 (2001), no size correction to re-calculate the UCS values was needed. From the axial stress vs. axial strain curve obtained by processing load-deformation data in Microsoft Excel[®], crack-initiation stress (c_i) was determined as the stress level where the stress-strain curve departed from linearity (Fig. 3b). For example, in Fig 3b, the point corresponding to crack-initiation stress was determined where the slope of the straight line dropped which is



Fig.2. Examples of collected granite cores and a generalized photomicrograph of the granite.

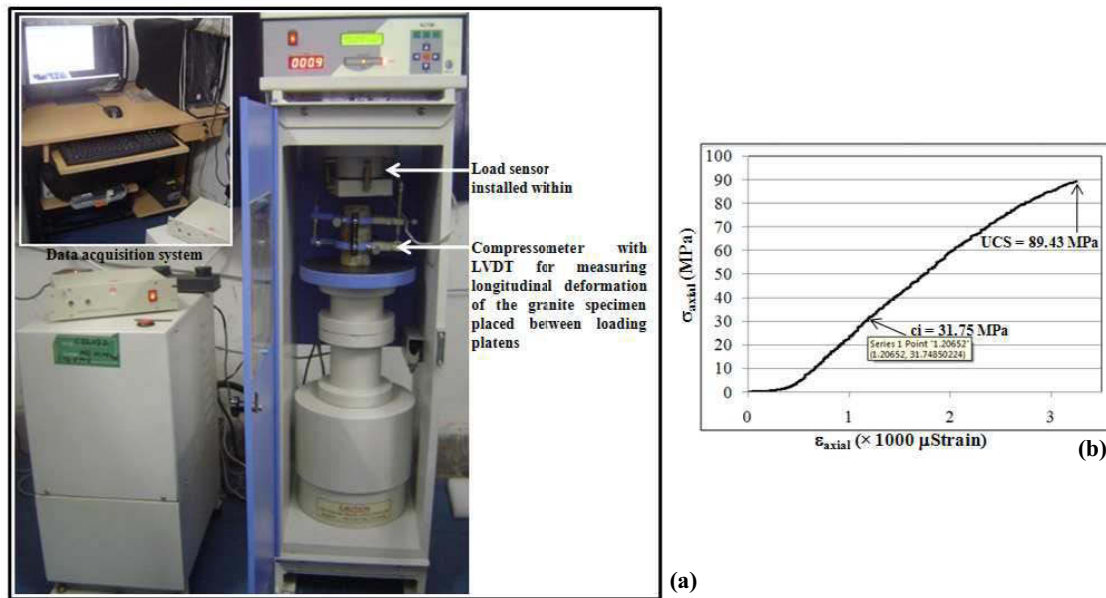


Fig.3. (a) Laboratory setup for uniaxial compression test. **(b)** An example of determining crack-initiation stress (ci) and uniaxial compressive strength (UCS) of a tested granite specimen from the axial stress (σ_{axial}) vs. axial strain (ϵ_{axial}) curve obtained by processing axial load and axial deformation data.

calculated from the Excel data sheet of axial stress and axial strain values.

In this study, both n_t and n_e were measured for all samples under investigation. For determination of n_e , a representative rock piece ($> 50\text{gm}$) was saturated by immersing it into water in a vacuum of around 90kPa for at least 2 hrs. The vacuum pressure applied in this study was more than that (800Pa) specified in ISRM (1979) in order to saturate rocks like fresh granites. Dry mass (M_{dry}) and saturated mass (M_{sat}) of the specimen, and mass of the saturated specimen while suspended inside water (M_{sus}) were measured. n_e was calculated from the following equation:

$$n_e = ((M_{sat} - M_{dry}) / (M_{sat} - M_{sus})) \times 100\% \quad (1)$$

For determining n_t , the rock specimen was powdered (Basu, 2006). Mass (M_p) and volume (V_p) of any portion of the powder were measured and volume (V_{eq}) of the equivalent mass of an intact rock specimen (i.e. before powdering) was calculated by dividing M_p by the dry density of the intact rock specimen [i.e. $\rho_{dry} = (M_{dry} / (M_{sat} - M_{sus}))$, $\rho_{water} = 1\text{gm/cc}$]. n_t was calculated from the following equation:

$$n_t = ((V_{eq} - V_p) / V_{eq}) \times 100\% \quad (2)$$

The values of n_e and n_t representative for a sample were obtained by averaging two to three vigilant test results.

The complete test results including n_e , n_t , ci and UCS for all samples are summarized in Table 1. It should be noted

that no ci value is given against Sample no. 20 in Table 1, as the distance sensor (LVDT) attached to the compressometer did not function properly during the uniaxial test of the corresponding specimen. When UCS and ci were plotted against n_t separately, widely scattered data points showed crude negative distributions (Fig. 4). On the other hand, when UCS and ci were plotted against n_e , conspicuous negative linear relations emerged (Fig. 5). The equations for the trend lines (best-fit lines) and corresponding absolute values of Pearson's correlation coefficients ($|R|$ values) are given in the Fig. 5. For the plots UCS vs. n_e and ci vs. n_e , the degrees of freedom are 37 and 36 respectively (Table 1). Hence, minimum theoretical $|R|$ values of 0.408 and 0.413 are necessary to consider the correlations as statistically significant at 99% confidence level respectively (calculated using the url: <http://secamlocal.ex.ac.uk/people/staff/dbs202/cat/stats/corr.html>). Figure 5 depicts that $|R|$ values for both UCS vs. n_e and ci vs. n_e plots are greater than the calculated $|R|$ values at 99% confidence level. Therefore, it can be concluded that both correlations in Fig. 5 are statistically significant. Based on the $|R|$ value, however, the correlation between ci and n_e appears to be much better than the correlation between UCS and n_e .

Porosity of a rock is a measure of the void space with respect to the bulk volume of the rock. The void space within the rock is attributed to the presence of pores and cracks/fissures which may function as stress concentrators when the rock is subjected to compression. Palchik (1999) showed

Table 1. Laboratory test results

Sample no.	ne (%)	nt (%)	ci (MPa)	UCS (MPa)
1	0.22	0.83	23.26	127.74
2	0.14	0.88	63.88	142.05
3	0.12	0.59	75.99	179.45
4	0.16	0.62	67.33	146.05
5	0.17	0.46	69.34	139.93
6	0.19	0.63	48.39	83.57
7	0.17	0.74	59.26	118.90
8	0.19	1.03	60.00	137.77
9	0.16	0.82	60.00	179.25
10	0.15	0.91	76.35	165.81
11	0.21	1.78	56.92	158.93
12	0.24	1.25	30.20	98.49
13	0.18	1.10	64.99	112.48
14	0.16	0.69	58.78	152.26
15	0.18	0.72	48.28	179.13
16	0.17	1.07	48.22	144.03
17	0.22	1.36	41.44	144.60
18	0.21	2.13	50.92	166.50
19	0.11	1.04	70.69	180.35
20	0.16	0.58	—	184.08
21	0.11	0.71	85.48	154.43
22	0.21	2.47	59.88	130.34
23	0.20	1.31	52.14	159.17
24	0.17	0.87	53.53	153.77
25	0.19	0.68	40.66	154.99
26	0.22	1.14	35.62	80.73
27	0.23	2.02	31.68	86.44
28	0.19	1.74	43.17	182.71
29	0.19	0.80	41.09	171.28
30	0.24	0.98	33.09	93.48
31	0.18	0.77	56.19	162.18
32	0.18	0.91	50.27	170.90
33	0.15	1.11	78.37	154.37
34	0.18	0.96	58.68	153.30
35	0.23	1.45	31.75	89.43
36	0.17	0.60	72.47	152.80
37	0.21	1.37	50.14	152.06
38	0.20	0.88	54.46	138.43
39	0.23	2.22	40.00	98.81

ne = effective porosity, nt = total porosity, ci = crack-initiation stress, UCS = uniaxial compressive strength

Note: ne and nt for each sample were obtained by averaging two/three vigilant test results from individual specimen

that in porous heterogeneous sandstones, porosity has an effect on UCS, whereas the role of grain boundaries is negligible. Although unlike sedimentary rocks, a brittle crystalline rock such as granite is devoid of primary pores, it inevitably contains numerous microscopic/submicroscopic flaws/cracks (e.g. grain boundary, intra- and trans-granular cracks) which are distributed with random orientation throughout the volume of the material. Crack initiation is caused by the stress concentrations at the ends of these cracks. It should be noted that microcracks only with suitable orientations and dimensions give rise to new cracks from their tips. Moreover, the process of crack coalescence is a

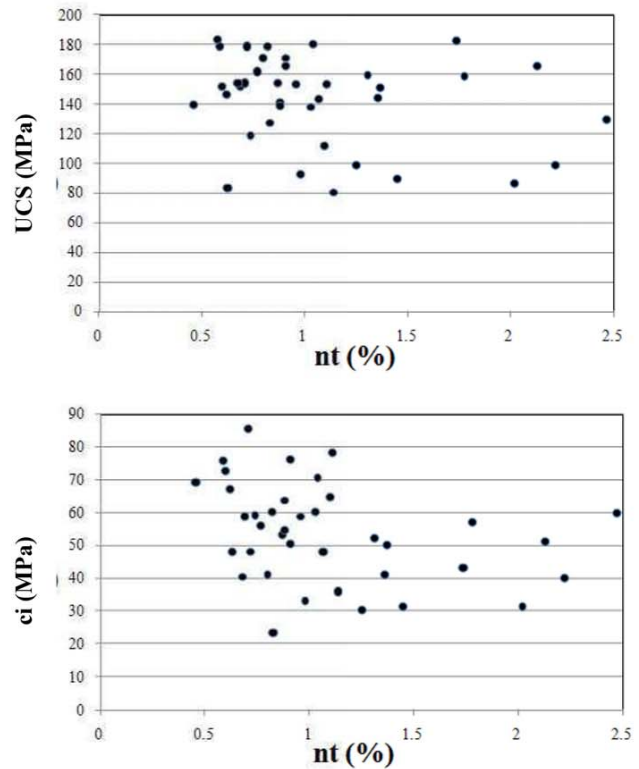


Fig.4. Uniaxial compressive strength (UCS) and crack-initiation stress (ci) plotted separately against total porosity (nt).

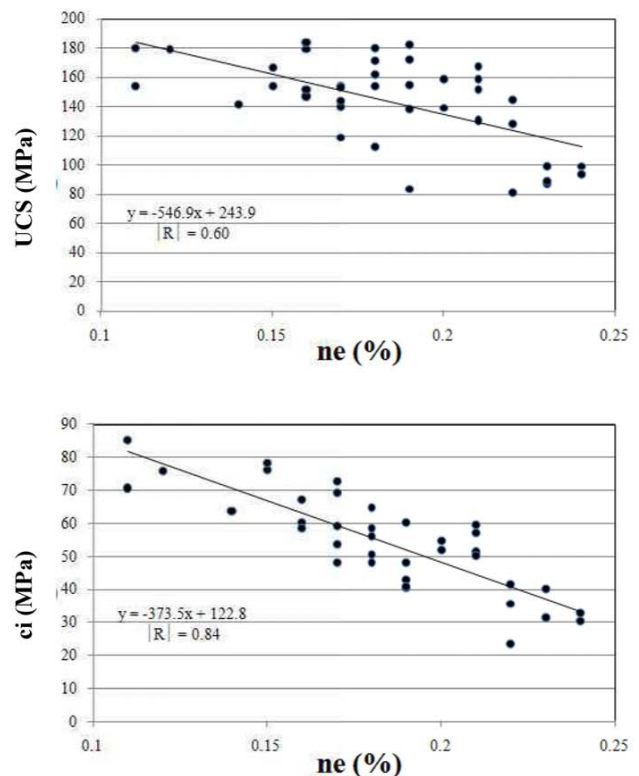


Fig.5. Uniaxial compressive strength (UCS) and crack-initiation stress (ci) plotted separately against effective porosity (ne).

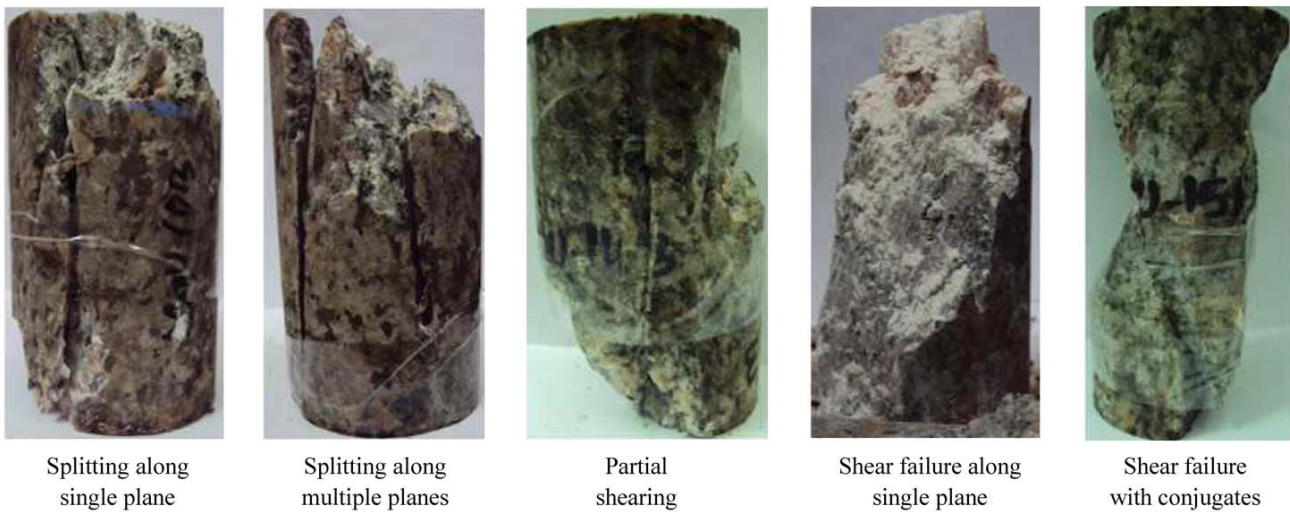


Fig.6. Examples of common failure modes of granite specimens under uniaxial compression.

function of distribution and interconnectedness of the pre-existing microcracks. This is also supported or supplemented by various failure modes of the granite specimens under uniaxial compression (Fig. 6). All these points explain significantly stronger relations of UCS and c_i with n_e than with n_t (Figs. 4 and 5). Basu (2006) also found n_e to be more efficient than n_t in predicting UCS of granitic rock materials of different weathering grades from Hong Kong.

Another point to be noted is that the correlation between c_i and n_e is better than that between UCS and n_e (Fig. 5). After the crack initiation from the tips of the pre-existing cracks of the rock specimen under uniaxial compression, a stage of stable crack growth is attained which is followed by unstable crack growth that initiates at crack-damage stress (c_d) (Fig. 1). This unstable crack growth eventually leads to failure of the rock specimen (Fig. 1). It is, therefore, evident that the pattern, density and distribution of microcracks during the stages of stable and unstable crack growth are significantly different from the nature of the pre-existing cracks (i.e. microcracks before applying compressive stress) (Fig. 1). At crack initiation stress, however, this difference is understandably less (Fig. 1). This explains a better performance of n_e in estimating c_i than in predicting UCS of the granitic materials. Palchik and Hatzor (2002) showed that there exists a negative curvilinear relation between c_d and n_t of limestones and dolomites. However, the data point distribution was too scattered to be presented in the form of any correlation equation which could be attributed to the reasons explained.

CONCLUSIONS

Establishing the initiation and development of stress-

induced microcracks in brittle rock under compression is important. For understanding the onset of rock damage, expensive laboratory tests involving various rock types, loading conditions, specimen shapes, and observation methods were performed by many researchers in the past. Nevertheless, finding out an error-free value of crack initiation stress was not possible. This study proposed a method to estimate crack-initiation stress of rock materials empirically by rock physical indices like total and effective porosities, which is a much simpler and less expensive technique than the methods employed before. The validity of the proposed method was examined by an experimental investigation of granitic materials from Malanjkhand (in the state of Madhya Pradesh, India). The following conclusions are drawn based on the study.

- Effective porosity is significantly more efficient than total porosity in predicting uniaxial compressive strength and crack-initiation stress of the granitic materials.
- Effective porosity is more efficient in estimating crack initiation stress than in predicting uniaxial compressive strength of the granitic materials.
- Plausible reasons for the nature of the obtained results can also be explained in view of rock failure process under compression.

It should, however, be noted that for the first time, a method of estimating crack-initiation stress of rock materials by porosity has been proposed and the validity of this simple and low-cost method has been examined experimentally by investigating granitic materials (from Malanjkhand) in this study. Further research with the said objective needs to be carried out considering other brittle crystalline rocks from

other areas with specific geology in order to be ascertained about the efficiency of effective porosity as a physical index to obtain a quick estimate of crack-initiation stress of such rocks.

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