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Analysis and Optimization of an Internal Feedback Hydrostatic Turntable Oil Pad Power Consumption Based on Finite Diference Method

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Abstract

The hydrostatic turntable is a critical component of numerous CNC machine tools, as it performs a supporting function and enables precise rotary motion. To ensure that high-precision CNC machines can operate under heavy loads, it is imperative to minimize power consumption. The power consumption of a hydrostatic turntable is afected by various factors, such as oil viscosity, initial oil flm thickness, and oil pad structure. This study focuses on investigating a hydrostatic turntable with internal feedback. The Reynolds equation of the sector oil pad is solved using the fnite diference method to establish the pressure distribution model. Subsequently, the study examines the power consumed by the axial oil pad at diferent initial oil flm thickness, lubricating oil viscosity, and sealing edge width. To minimize power consumption caused by the axial oil pad, this paper employs the genetic algorithm to identify optimal design parameters within specifed constraints. Additionally, the load-bearing performance of the optimized axial oil pad is checked to ensure that the load-bearing capacity and stifness meet the requirements. Finally, the use of simulation software for oil pads in fnite element simulation can preliminarily demonstrate the reliability of the proposed method.

Keywords Hydrostatic turntable · Internal feedback · Finite diference method · Genetic algorithm · energy-saving

Abbreviations

- *A*_s Area of the oil sealing edge and throttle (m^{-2})
- Area of the oil pocket (m^{-2})
- $\frac{A_r}{b}$ Width of gap throttle edge (m)
- *B* Width of oil pad sealing edge (m)
- *f*r Friction in the radial direction (N)
- f_{θ} Friction in the circumferential direction (N)
- F_f Total friction (N)
- *h* Film thickness (m)

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- h_0 Initial oil film thickness (m)
 h_1 Oil film thickness of upper c Oil film thickness of upper oil pad (m) h_2 Oil film thickness of lower oil pad (m)
H Depth of the oil pocket (m) Depth of the oil pocket (m) *i* Numerical counters of the elements of *r j* Numerical counters of the elements of *θ k* Numerical counters of the elements of *z K* Mean stiffness (N m⁻¹) *l* Length of gap throttle edge (m) *L* Width of oil pad sealing edge (m) N_f Total friction power (W) *N*_P Support power (W) $\frac{N_t}{N_{\text{fr}}}$ Total power (W) Dimensionless friction power in radial direction *p* Pressure (MPa) p_0 Oil pocket pressure (MPa) *p*_s Inlet pressure (MPa) p_1 Upper oil pocket pressure (MPa) *p*₂ Lower oil pocket pressure (MPa)
Q Oil supply flow rate (m³ s⁻¹) *Q* Oil supply flow rate $(m^3 \text{ s}^{-1})$ \overline{q}_r Dimensionless fow rate in radial direction *r* Radial coordinate R_0 Outside diametesr of fan oil pad (m)
- R_1 Inside diameter of fan oil pad (m)
- R_{c1} Oil inlet resistance in upper oil pocket (N s m⁻⁵)
 R_{h1} Oil outlet resistance in upper oil pocket (N s m⁻⁵)
- Oil outlet resistance in upper oil pocket (N s m⁻⁵)
- R_{c2} Oil inlet resistance in lower oil pocket (N s m⁻⁵)
- R_{h2} Oil outlet resistance in lower oil pocket (N s m⁻⁵)
U Radial velocity (m s⁻¹)
- *U* Radial velocity $(m s^{-1})$
- \overline{U}_z Dimensionless damping
- *V* Circumferential velocity (rad s^{-1})
- *W* External load on a pair of oil pads (N)
- W_0 Oil pad thrust at no load (N)
- W_1 Upper oil pad thrust (N)
 W_2 Lower oil pad thrust (N)
- Lower oil pad thrust (N)
- *z* Film thickness coordinate
- β_0 Initial throttling ratio
- Δ*h* Oil flm thickness variation (m)
- *θ* Circumferential coordinate
- ρ Density (kg m⁻³)
- ω Rotational angular velocity (rad s⁻¹)
- ω_{SOR} SOR weight in successive Over Relaxation method

1 introduction

The hydrostatic turntable plays a crucial role in the performance of many CNC machine tools by providing support and precise rotary motion $[1-3]$ $[1-3]$ $[1-3]$. Therefore, studying the performance of the hydrostatic turntable is essential for enhancing the efficiency of CNC machines. In response to the requirements of high-precision machine tools, internal feedback hydrostatic turntables have been developed. By automatically adjusting the liquid resistance to meet the bearing capacity demands, the internal feedback oil pad can enhance the stifness of the oil flm. The entire turntable possesses a compact structure and stable performance without requiring manual adjustment. Although limited studies have been conducted on internal feedback hydrostatic turntables, some research is available. Some scholars have examined internal feedback hydrostatic bearings and internal feedback hydrostatic guides and have derived a set of corresponding empirical formulas. A torque motor direct-drive internal feedback closed hydrostatic turntable has been designed and implemented, which exhibits greater oil flm stifness and stability compared to a standard hydrostatic turntable. With varying loads, the oil flm thickness varies minimally, leading to improved precision.

Typically, hydrostatic support is evaluated by solving the Reynolds equation [\[4](#page-15-2)]. The fnite diference method is a relatively mature method for solving the Reynolds equation. Ochoa et al. [[5\]](#page-15-3) proposed a general form of the Reynolds equation for lubrication applications. Wang et al. [\[6](#page-15-4)] modified the Reynolds equation to solve the difficulties of analytically solving second order partial diferential equations involving parameters such as pressure, oil flm thickness, oil viscosity, density, and loading surface velocity. Kumar and Liu [\[7](#page-16-0), [8\]](#page-16-1) derived the Reynolds equation for diferent oil pocket types using the fuid Navier–Stokes equations (N–S equation). Garratt et al. [\[9](#page-16-2)[–11](#page-16-3)] also analyzed the Reynolds equation considering the centrifugal force and analyzed the thermal characteristics. These studies proposed many diferent forms of the Reynolds equation and diferent numerical solutions of Reynolds equation. They provide the necessary basis for the analysis of hydrostatic support performance.

The optimization of hydrostatic systems has been studied by many scholars recently. Niranjan et al. [[12\]](#page-16-4) analyzed the comprehensive efects of recess shape and liquid flm thickness on the performance characteristics of hydrostatic guideways, and proposed a recess shape that exhibited superior performance. Zuo et al. [\[13](#page-16-5)] researched the impact of various parameters on a self-compensating hydrostatic rotary bearing and obtained the optimal parameters. Christoph [\[14](#page-16-6)] improved the bearing performance of a hydrostatic spindle by optimizing the oil film form. Boedo et al. [[15\]](#page-16-7) used the genetic algorithm to optimize the shape of radial sliding bearings. Wang et al. [[16](#page-16-8)] used the particle swarm optimization algorithm to optimize the structure of the oil pad, thus reducing the support power. Cai et al. [\[17\]](#page-16-9) optimized the structure of the oil pad to improve the stifness of the hydrostatic guide rail. Hang et al. [\[18](#page-16-10)] applied the particle swarm optimization method to study the optimization problem of the rectangular oil pad of the air foat. Chan et al. [\[19\]](#page-16-11) applied the multi-objective particle swarm optimization (PSO) method to optimize the load-bearing capacity in the hydrostatic spindle load-bearing model. Cai et al. [\[20\]](#page-16-12) discussed the optimization scheme for the resistance to overturning of gantry guide rail. Cheng et al. [[21](#page-16-13)] carried out a sensitivity analysis on the structural size parameters of the hydrostatic turntable and combined the particle swarm optimization method to improve the static and dynamic load performance of the turntable. Yu et al. [[22](#page-16-14), [23](#page-16-15)] analyzed the infuence of the groove structure of a hydrostatic thrust bearing on the comprehensive tribological performance. These studies address a variety of hydrostatic systems, such as hydrostatic bearings, hydrostatic turntables, hydrostatic guideways, hydrostatic rams. From these studies, it is possible to fnd out the performance changes of these hydrostatic systems, such as bearing capacity, stifness, fow rate, etc. In addition, many optimization methods were proposed by them, which provided guidance for the subsequent research.

Previous studies aimed at improving the load-carrying performance of hydrostatic turntables [\[24](#page-16-16), [25\]](#page-16-17). Only a few of the published studies focused on power consumption [[26](#page-16-18)]. Research focused on reducing energy consumption is also a prominent avenue within the realm of future machine tool studies [[27](#page-16-19)[–29](#page-16-20)]. The power consumption of the hydrostatic turntable is considerably lower than that of the conventional mechanical turntable since there is no direct contact between the hydrostatic turntable and the oil pad. However, even when the load requirements are met, the power consumption of the hydrostatic turntable can still be optimized. In this paper, we employed a torque motor direct-drive internal feedback closed hydrostatic turntable. We simplifed the Reynolds equation and established the pressure distribution model using the fnite diference method. We analyzed the efects of initial oil flm thickness, lubricating oil viscosity, and sealing edge width on the oil supporting power and friction power of the oil pad. Our analysis revealed that viscosity and initial oil flm thickness have opposing efects on oil supporting power and friction power. Subsequently, we selected optimal design parameters using the genetic algorithm to minimize the total power of the oil pad. Subsequently, the load-bearing performance of the optimized oil pad was assessed to ensure that the load-bearing capacity meets the required standards. Finally, we performed fnite element simulation of the oil pad using simulation software to verify the method's reliability [\[30,](#page-16-21) [31\]](#page-16-22).

2 Principle and Calculation

2.1 Model and Principle of Internal Feedback Hydrostatic Turntable

The structure of a torque motor direct-drive internal feedback closed hydrostatic turntable is shown in Fig. [1.](#page-2-0) It is mainly supported by the hydrostatic bearing of the middle layer. One type of hydrostatic bearing is the internal feedback hydrostatic bearing. According to the oil supply mode, it belongs to constant pressure oil supply, and the throttling form is internal gap throttling. The working principle is shown in Fig. [2.](#page-2-1) Internal feedback flow chart is shown in Fig. [3.](#page-3-0) The constant pressure hydraulic oil enters the oil circuit of the axial bearing. Afterwards it is divided into two paths. One way to the upper oil pad, the other way to the lower oil pad. A Δ*h* gap change occurs when the turntable table is subjected to a downward force

Fig. 1 Internal feedback hydrostatic turntable model

Fig. 2 Working principle of axial oil pad schematic diagram

W. At this moment, on one hand, the decrease in clearance h_1 in the upper oil pocket leads to an increase in oil pocket pressure due to increased oil sealing and increased fluid resistance R_{h1} at the sealing edge. At the same time, the gap throttle located in the lower oil pocket, which controls the upper oil pocket, experiences a decrease in fluid resistance R_{c1} at the throttle edge due to the increase in clearance h_2 , resulting in decreased pressure drop during throttling. As a result, the pressure entering the upper oil pocket increases, creating a feedback effect. Similarly, on the other hand, the increase in clearance h_2 in the lower oil pocket leads to a decrease in oil pocket pressure due to decreased oil sealing and decreased fluid resistance R_{h2} at the sealing edge. The gap throttle located in the upper oil pocket, which controls the lower oil pocket, experiences an increase in fluid resistance R_{c2} at the throttle edge due to the decrease in clearance h_1 , resulting in increased pressure drop during throttling. This leads to a decreased pressure entering the lower oil pocket, also creating a feedback effect. This is how the internal feedback bearing works. Through the combined effect of the upper and lower oil pockets (i.e., a closed-loop hydrostatic bearing structure) and the feedback effect of the gap throttles, the internally self-feedback closed-loop hydrostatic bearing exhibits higher oil film stiffness and stability compared to traditional hydrostatic bearings, with smaller variations in oil film thickness under different loads and better precision retention.

The relationship between oil pressure and fuid resistance is shown in Fig. [4.](#page-3-1) From the graph, the pressure in the oil pocket can be determined. The pressure in the upper oil pocket can be expressed using the following formula:

$$
p_1 = \frac{p_s}{1 + \frac{R_{c1}}{R_{h1}}} = \frac{p_s}{1 + (\beta_0 - 1)(\frac{h_1}{h_2})^3}
$$
(1)

The pressure in the lower oil pocket can be expressed using the following formula:

oil pressure and hydraulic

resistance

$$
p_2 = \frac{p_s}{1 + \frac{R_{c2}}{R_{h2}}} = \frac{p_s}{1 + (\beta_0 - 1)(\frac{h_2}{h_1})^3}
$$
(2)

The support for the internal feedback hydrostatic turntable is a closed support [[32](#page-16-23), [33](#page-16-24)]. The table is subjected to a pair of forces of equal magnitude and opposite direction in the no-load condition. Therefore, the load-bearing force of a pair of oil pads is zero when under no load. The table sinks Δh to reach the equilibrium position when the load *W* is applied. The upper oil pad clearance decreases to $h_1 = h_0 - \Delta h$ while the thrust W_1 increases. The lower oil pad clearance increases to $h_2 = h_0 + \Delta h$, while the thrust W_2 decreases. The diference between the two thrusts is equal to the external load, expressed by the following equation:

$$
W = W_1 - W_2 \tag{3}
$$

When the displacement of the table is Δ*h* under the action of *W*. The average stifness of the opposed oil pad is:

$$
K = \frac{W - 0}{\Delta h - 0} \tag{4}
$$

2.2 The Reynolds Equation and FDM Solution

The Reynolds equation is a commonly used tool in the analysis of hydrostatic systems, and it describes the pressure racy and cannot efectively describe the pressure distribution of the oil pad. As such, the Reynolds equation is used to solve for the pressure distribution. The Reynolds equation is derived from the simplifcation of the fuid Navier–Stokes equation in the form of a thin oil flm. Since the dimensions in the thickness direction of the thin oil flm are much smaller than those in the other two directions, the gradient of the pressure in the thickness direction can be neglected. This simplifcation results in a binary second-order partial diferential equation that is used to describe the pressure distribution inside the oil pad. The sectorial diferential Reynolds equation is expressed as follows:

distribution of the viscous oil flm in oil pads. While traditional empirical formulas are easy to calculate, they often lack accu-

$$
\frac{\partial}{\partial r}(r\frac{h^3}{\mu}\frac{\partial p}{\partial r}) + \frac{\partial}{\partial \theta}(\frac{h^3}{\mu}\frac{\partial p}{r\partial \theta}) = 6\frac{\partial}{\partial r}(rUh) + 6\frac{\partial}{\partial \theta}(Vh) + 12r\frac{\partial h}{\partial t} + \frac{\partial}{\partial r}(\frac{h^3\omega^2r^2}{\mu}\rho)
$$
\n(5)

Dimensionless analysis is a common method used in physical research. It can simplify models with various parameters to improve computational effectiveness. The following dimensionless parameters should be defned as follows:

$$
\bar{p} = \frac{p}{p_0}\bar{r} = \frac{r}{R_0}, \bar{z} = \frac{z}{h_0}, \bar{h} = \frac{h}{h_0}, \bar{\mu} = \frac{\mu}{\mu_0}
$$

$$
\bar{U} = \frac{U}{\frac{h_0^2 p_0}{R_0 \mu_0}}, \bar{V} = \frac{V}{\frac{h_0^2 p_0}{R_0 \mu_0}}, \bar{U}_z = \frac{h_0^3 p_0}{\mu_0 R_0^2}, \bar{\rho} = \frac{\rho}{\frac{\mu_0^2 R_0^2}{h_0^4 p_0}}
$$
(6)

Dimensionless scaling of the Reynolds equation is as follows:

$$
\frac{\partial}{\partial \bar{r}} (\bar{r} \frac{\bar{h}^3}{\bar{\mu}} \frac{\partial \bar{p}}{\partial \bar{r}}) + \frac{\partial}{\partial \theta} (\frac{\bar{h}^3}{\bar{\mu}} \frac{\partial \bar{p}}{\bar{r} \partial \theta}) = 6 \frac{\partial}{\partial \bar{r}} (\bar{r} \bar{U} \bar{h}) + 6 \frac{\partial}{\partial \theta} (\bar{V} \bar{h}) \n+ 12 \bar{r} \bar{U}_{z} + \frac{\partial}{\partial \bar{r}} (\frac{\bar{h}^3 \bar{V}^2}{\bar{\mu}} \bar{\rho})
$$
\n(7)

The discretization solution is then performed, as shown in Fig. [5.](#page-4-0) According to Taylor's formula, the partial derivative can be expressed as the diference quotient on the neighboring nodes. During the solution process, the pressure is usually discretized into thousands to tens of thousands of microelements, resulting in a very large discretized matrix. The discretization process is as follows:

$$
\left(\frac{\partial \bar{p}}{\partial \bar{r}}\right)_{i,j} \approx \frac{\bar{p}_{i,j} - \bar{p}_{i-1,j}}{\Delta \bar{r}}, \left(\frac{\partial \bar{p}}{\partial \theta}\right)_{i,j} \approx \frac{\bar{p}_{i,j} - \bar{p}_{i,j-1}}{\Delta \theta}
$$
\n
$$
\left(\frac{\partial^2 \bar{p}}{\partial \bar{r}^2}\right)_{i,j} \approx \frac{\bar{p}_{i+1,j} - 2\bar{p}_{i,j} + \bar{p}_{i-1,j}}{(\Delta \bar{r})^2}, \left(\frac{\partial^2 \bar{p}}{\partial \theta^2}\right)_{i,j} \approx \frac{\bar{p}_{i,j+1} - 2\bar{p}_{i,j} + \bar{p}_{i,j-1}}{(\Delta \theta)^2}
$$
\n(8)

where $p_{i,j}$ denotes the pressure value on node(*i*, *j*).

The Gauss–Seidel iteration is a numerical method for solving systems of linear equations. The discretized Reynolds equation is characterized by the fact that the pressure values at all nodes are applied to the same equation. That is, the Gauss–Seidel iteration solves the Reynolds equation with only one iterative equation for all node values. Therefore, the Gauss–Seidel method is often used in conjunction with the fnite diference method for the solution of the Reynolds equation. The formula is expressed as follows:

Fig. 5 Discrete nodes of pressure distribution

$$
\bar{p}_{ij} = \frac{A(\Delta\theta)^2 + B(\Delta\bar{r})^2 - C\Delta\bar{r}\Delta\theta}{D(\Delta\theta)^2 + E(\Delta\bar{r})^2}
$$
(9)

where
$$
A = \frac{\bar{r}_i \bar{h}_{i,j}^3 \bar{p}_{i+1,j}}{\bar{\mu}_{i,j}} + \frac{\bar{r}_{i-1} \bar{h}_{i-1,j}^3 \bar{p}_{i-1,j}}{\bar{\mu}_{i-1,j}}, B = \frac{\bar{h}_{i,j}^3 \bar{p}_{i,j+1}}{\bar{\mu}_{i,j} \bar{r}_i} + \frac{\bar{h}_{i,j-1}^3 \bar{p}_{i,j-1}}{\bar{\mu}_{i,j-1} \bar{r}_i}
$$

\n
$$
6\Delta\theta(\bar{r}_i \bar{h}_{i,j} \bar{U}_{i,j} - \bar{r}_{i-1} \bar{h}_{i-1,j} \bar{U}_{i-1,j}) + 6\Delta\bar{r}(\bar{h}_{i,j} \bar{U}_{i,j} - \bar{h}_{i,j-1} \bar{U}_{i-1,j-1})
$$

\n
$$
C = \frac{\bar{h}_{i,j}^3 \bar{V}_{i,j} \bar{p}_{i,j}}{+12\bar{r}_i \bar{U}_z \Delta\bar{r} \Delta\theta + \Delta\theta(\frac{\bar{h}_{i,j}^3 \bar{V}_{i,j} \bar{p}_{i,j}}{\bar{\mu}} - \frac{\bar{h}_{i-1,j}^3 \bar{V}_{i-1,j} \bar{p}_{i-1,j}}{\bar{\mu}_{i-1}})
$$

$$
D = \frac{\bar{r}_i \bar{h}_{i,j}^3}{\bar{\mu}_{i,j}} + \frac{\bar{r}_{i-1} \bar{h}_{i-1,j}^3}{\bar{\mu}_{i-1,j}}, E = \frac{\bar{h}_{i,j}^3}{\bar{\mu}_{i,j} \bar{r}_i} + \frac{\bar{h}_{i,j-1}^3}{\bar{\mu}_{i,j-1} \bar{r}_i}
$$

The boundary conditions of the iterative equation are that the dimensionless pressure inside the oil pocket is all 1, and the dimensionless pressure at the outermost part of the sealing edge is all 0. The boundary conditions can be used to calculate the dimensionless pressure values elsewhere by using Eq. [\(9](#page-4-1)). The Successive Over Relaxation method (SOR) is then introduced to accelerate its convergence.

The Successive Over Relaxation method (SOR) is a computational acceleration technique built upon the Gauss–Seidel iteration. It can help the calculation converge faster to meet the required accuracy. Assuming that the iterated calculation value is increased by an increment Δ based on the value of the previous iteration, the formula is expressed as follows:

$$
p^{(n+1)} = p^{(n)} + \Delta
$$
 (10)

Multiplying the weight ω_{SOR} before the increment Δ can achieve faster convergence of the iterated calculation value towards the fnal solution.

$$
p_{\text{SOR}}^{(n+1)} = p^{(n)} + \omega_{\text{SOR}} \cdot \Delta
$$

\n
$$
p_{\text{SOR}}^{(n+1)} = p^{(n)} + \omega_{\text{SOR}} \cdot [p^{(n+1)} - p^{(n)}]
$$
\n(11)

After rearranging, we obtain the formula for SOR weight adjustment

$$
p_{\text{SOR}}^{(n+1)} = \omega_{\text{SOR}} p^{(n+1)} + (1 - \omega_{\text{SOR}}) p^{(n)} \tag{12}
$$

where ω_{SOR} is the Over Relaxation Weight, which is generally taken to be between 1 and 2.

The numerical solution process of the Reynolds equation has good convergence, which can be further accelerated by using the Successive Over Relaxation method for iterative computation.

The numerical integral of the pressure across the oil pad area is used to compute the dimensionless bearing capacity of the single sector oil pad:

$$
\bar{w} = \sum \frac{1}{4} (\bar{p}_{i,j} + \bar{p}_{i+1,j} + \bar{p}_{i,j+1} + \bar{p}_{i+1,j+1}) \cdot \Delta \bar{r} \cdot \Delta \theta \cdot 0.5 \cdot (\bar{r}_{i+1} + \bar{r}_i)
$$
\n(13)

Fig. 6 Sector oil pad pressure distribution model

After further dimensionalization, the bearing capacity of the single sector oil pad is:

$$
W = \bar{w} \cdot p_0 \cdot R_0^2 \tag{14}
$$

The sector oil pad pressure distribution model can be obtained, as shown in Fig. [6](#page-5-0).

2.3 Power Consumption Calculation

Under specifc operating conditions, the power consumed by the hydrostatic support comprises two distinct components. The first component involves driving the oil at a certain pressure through the throttle, support gap, pipeline, and other associated devices, and is represented by the output power of the pump or support power. The second component encompasses the power consumption resulting from the friction generated by the relative motion that shears the oil flm between the table and the bearing.

(1) Oil supporting power of the oil pump (Support power) The flow rate should be calculated first, before the support power. The dimensionless flow rate is calculated as the numerical integration of the fow speed over the fow area of the oil flm:

where
$$
\overline{\mathbf{r}}_i = \mathbf{R}_1 / \mathbf{R}_0
$$
 or $\overline{\mathbf{r}}_i = 1$

$$
\begin{cases} \bar{v}_{i,j,k} = \frac{\bar{z}_k^2 - \bar{z}_k}{2\overline{\mu}} \frac{\bar{p}_{i+1,j} - \bar{p}_{i,j}}{\Delta \theta \cdot \bar{r}_i} + \overline{V}_{i,j} \bar{z}_k \\ \bar{q}_{\theta} = \sum \left[\frac{1}{4} (\bar{v}_{i,j,k} + \bar{v}_{i+1,j,k} + \bar{v}_{i,j,k+1} + \bar{v}_{i+1,j,k+1}) \cdot \Delta \overline{r} \cdot \frac{1}{2} (\overline{h}_{i,j} + \overline{h}_{i,j+1}) \cdot \Delta \overline{z} \right] \end{cases} \tag{16}
$$

where $\theta = 0$ or $\theta = \theta_0$ (θ_0 is the maximum angle of the sector oil pad in radian system).

The total oil discharge flow rate is

$$
\bar{q} = \bar{q}_{\rm r} + \bar{q}_{\theta} \tag{17}
$$

 The oil supporting power of the oil pump at the output flow rate *Q* and the supply pressure p_s is:

$$
p_0 = \frac{p_s}{\beta}, \ Q = \bar{q} \frac{h_0^3 p_0}{\mu_0}, \ N_p = p_s \cdot Q \tag{18}
$$

(2) Friction power

 An oil pad must overcome viscous resistance caused by shearing oil flm while the turntable rotates. According to the law of Newton inner friction, the friction is expressed as:

$$
F_{\rm f} = \mu A_{\rm s} \frac{v}{h} + \mu A_{\rm r} \frac{v}{(h+H)} \tag{19}
$$

 According to engineering experience, the second term in the above equation is usually not counted when *H* is greater than the oil pad clearance *h* more than ten times. However, a quarter of the oil pocket area is included in A_s to roughly estimate the churning loss in the oil pocket, when the viscosity μ is large.

 The power consumed to overcome viscous resistance at a certain speed of motion is the friction power. The expression is:

$$
N_{\rm f} = \sum F_{\rm f} v = \sum \mu A_{\rm f} \frac{v^2}{h} \tag{20}
$$

where $A_f = A_s + \frac{1}{4}A_r$. The equation shows that decreasing the frictional area, using low viscosity oil, and increasing the clearance can all help to reduce the friction force.

 Using FDM to solve for friction as the integral of shear stress over the bearing surface:

$$
\begin{cases} \bar{u}_{i,j,k} = \frac{\bar{z}_{k}^{2} - \bar{z}_{k}}{2\bar{\mu}} \frac{\bar{p}_{i+1,j} - \bar{p}_{i,j}}{\Delta \bar{r}} + \bar{U}_{i,j}\bar{z}_{k} \\ \bar{q}_{r} = \sum \left[\frac{1}{4} (\bar{u}_{i,j,k} + \bar{u}_{i,j+1,k} + \bar{u}_{i,j,k+1} + \bar{u}_{i,j+1,k+1}) \cdot \Delta \theta \cdot \bar{r}_{i} \cdot \frac{1}{2} (\bar{h}_{i,j} + \bar{h}_{i,j+1}) \cdot \Delta \bar{z} \right] \end{cases} \tag{15}
$$

 $\sqrt{ }$

 I

 $\begin{array}{c|c} & \text{if } &$

 The expression for the friction power using FDM is as follows

$$
\begin{cases} \n\bar{N}_{fr} = \sum \frac{1}{4} \left(\frac{\bar{u}_{i,j,k-1} + \bar{u}_{i+1,j,k-1} + \bar{u}_{i,j+1,k-1} + \bar{u}_{i+1,j+1,k-1}}{-\bar{u}_{i,j,k} - \bar{u}_{i+1,j,k} - \bar{u}_{i+1,j+1,k}} \right) \frac{\bar{U}_{i,j} \bar{u} \cdot \Delta \bar{r} \cdot \Delta \theta \cdot \bar{r}_i}{\Delta \bar{z}} \\ \n\bar{N}_{f\theta} = \sum \frac{1}{4} \left(\frac{\bar{v}_{i,j,k-1} + \bar{v}_{i+1,j,k-1} + \bar{v}_{i,j+1,k-1} + \bar{v}_{i+1,j+1,k-1}}{-\bar{v}_{i,j,k} - \bar{v}_{i+1,j,k} - \bar{v}_{i+1,j+1,k}} \right) \frac{\bar{v}_{i,j} \bar{u} \cdot \Delta \bar{r} \cdot \Delta \theta \cdot \bar{r}_i}{\Delta \bar{z}} \\ \nN_f = \frac{(\bar{N}_{fr} + \bar{N}_{f\theta}) \bar{h}_0^2 \bar{r}_0^2}{\mu_0} \n\end{cases}
$$
\n(22)

2.4 Genetic Algorithm (GA) Combined with FDM Optimization Process

The genetic algorithm (GA) is a method that simulates the process of biological evolution under natural selection, originally proposed by Darwin [[34](#page-16-25)[–36](#page-16-26)]. By applying this theory, the GA models the problem to be solved as a process of biological evolution. The GA generates the next generation of solutions by using replication, crossover, and mutation operations, sgradually eliminating solutions with low ftness function values and adding solutions with high ftness function values. Due to its good global search capability,

scalability, and the ease of combination with other algorithms, the genetic algorithm has become widely used in optimization problems. In this paper, the GA is utilized to optimize the hydrostatic turntable parameters. The optimization process includes several steps: initialization, ftness evaluation, selection operation, crossover operation, variation operation, and termination condition judgment. The minimum power N_t is output as the optimal solution. The detailed process of optimization using the GA is shown in Fig. [7.](#page-6-0)

3 Calculation Results and Discussion

3.1 Analysis of the Efect of Viscosity on Power Consumption

Viscosity is a crucial parameter of liquids that directly infuences the performance of hydrostatic support and plays a signifcant role in lubricant selection. The impact of viscosity on the friction force and friction power of the oil pad under diferent structures is illustrated in Fig. [8](#page-7-0), where *B* represents the width of the oil seal edge. As demonstrated in Fig. [8](#page-7-0)a, the friction force on the upper surface of the oil pad rises with the viscosity under the same structure. Similarly, Fig. [8](#page-7-0)b shows that the friction power consumption of the oil pad increases with increasing viscosity under the same structure. This indicates that the friction power consumption generated by the oil pad is mainly caused by the friction force on the upper surface. This phenomenon occurs because higher viscosity means that greater viscous resistance of the oil must be overcome when the table rotates, leading to higher power consumption.

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Fig. 8 Efect of viscosity on friction and friction power

Fig. 9 Effect of viscosity on flow rate and support power

Figure [9](#page-7-1) illustrates the impact of viscosity on the oil supply flow and support power of the oil pad under various structures, where *B* represents the width of the oil seal edge. As demonstrated in Fig. [9a](#page-7-1), the oil supply flow rate of the oil pad decreases with an increase in viscosity under the same structure. Similarly, Fig. [9](#page-7-1)b shows that the support power consumption of the oil pad decreases with an increase in viscosity under the same structure. These results suggest that the power consumption of the support generated by the oil supply to the oil pad is closely related to the flow rate. This phenomenon can be attributed to the fact that an increase in viscosity leads to an increase in the viscous resistance of the

oil, which in turn causes a decrease in the fow rate of the oil. Consequently, for the same load-carrying performance, less oil needs to be supplied as the viscosity increases. As a result, the oil supply fow rate decreases, leading to a decrease in support power consumption.

3.2 Analysis of the Efect of Initial Thickness on Power Consumption

The initial oil film thickness is a critical parameter that significantly affects the performance of a liquid hydrostatic turntable. This parameter affects both the loadcarrying capacity and the power of the oil pad. As shown in Figs. [10](#page-8-0) and [11](#page-8-1), the friction power and support power of the oil pad exhibit varying trends with the initial oil film thickness, where *B* represents the width of the oil sealing edge. The initial oil film thickness exhibits an opposite effect on the friction power and support power under the same structure. Specifically, the friction force and friction power decrease as the initial oil film thickness increases. This phenomenon is due to the increase in the gap between the oil pad and the turntable, resulting in an increase in the thickness of the oil film. Based on the law of Newton inner friction, the friction force between the two plates decreases as the gap increases. Conversely, the oil supply flow and support power increase as the initial oil film thickness increases. This result is due to the fact that the increase in oil film thickness decreases the oil discharge resistance, resulting in an increase in flow rate at a constant oil supply pressure.

Fig. 10 Efect of initial oil flm thickness on friction power

Fig. 11 Efect of initial oil flm thickness on support power

Fig. 12 Diagram of axial oil pad

These four figures, Figs. $8, 9, 10, 11$ $8, 9, 10, 11$ $8, 9, 10, 11$ $8, 9, 10, 11$ $8, 9, 10, 11$ $8, 9, 10, 11$, also show that the width of its oil sealing edge has a minor infuence on the power of the oil pad. The widening of the oil sealing edge has opposite efects on friction power and support power. Friction power increases as the oil sealing edge widens due to the increased contact area between the oil pad and the turntable through the oil flm. Conversely, support power decreases with the widening of the oil sealing edge. This is because the widening of the oil sealing edge increases the oil outlet resistance of the oil pad, leading to a decrease in the flow rate and support power, under constant oil supply pressure (Fig. [12\)](#page-8-2).

3.3 Genetic Algorithm Based Optimization Solution

Table[.1](#page-9-0) shows the parameters of a torque motor direct-drive internal feedback closed hydrostatic turntable oil pad, and

the following is based on this model and optimized according to the process shown in Fig. [7.](#page-6-0)

(1) Solving for optimal viscosity.

Machine tool hydraulic oil is a commonly utilized lubricant, with diferent grades established based on technical standards. For instance, 20 and 30 oil are suitable for hydraulic oil in general machine tools, while 10, 20, or 30 oil are appropriate for sliding bearings. Heavy machine tool guides require 40 and 50 oil, while stamping, casting, and other heavy equipment, as well as mining machinery, necessitate 70 and 90 oil. In addition, 20, 30, and 40 oils may be utilized as dual-purpose hydraulic-rail oil on high-precision grinding machines, serving as lubrication for hydraulic and guideway systems in universal grinding machines, bearing grinding machines, thread grinding machines, and gear grinding machines, as well as for the gear and guideway subsets of machine tools. In summary, the optimal machine tool hydraulic fuid power viscosity typically ranges between 0.01 to 0.09 pa s, and the optimization variables are governed within this range, as depicted in Fig. [13](#page-9-1).

The initialized population number is $X = 50$ before the optimization begins with viscosity as the variable. The chromosome binary code length is $L_{\text{G}} = 10$ because the viscosity is accurate to 0.0001 ($2^9 < \frac{0.09 - 0.01}{0.0001} < 2^{10}$). The maximum evolutionary generation $G = 100$, the crossover probability P_c = 0.8, and the variation probability P_m = 0.1.

The population individual evolution curve at the end of optimization is shown in Fig. [14](#page-10-0). Figure [14](#page-10-0) illustrates the optimization process of the genetic algorithm during iteration. The blue line represents the optimal individual, while the red line denotes the average value of all individuals in the population. After 50 iterations, the average value of the population can oscillate around the optimal value. Therefore, the individual with the minimum power consumption can be determined. The optimization result is that the power is minimized when μ = 0.0328 pa s with the value N_t = 67.53W.

Fig. 13 Variation of total power consumption with viscosity

Fig. 14 Iterative process of GA solving for optimal viscosity

40

50

60

 70

80

90

 \mathbf{R}^2

80

 $\overline{78}$

 \overline{L}

 $\overline{\tau}$

 68

່ເ

 10

 $\overline{20}$

 30

 N_t/W

The oil flm gap of the upper oil pad decreases and the oil flm gap of the lower oil pad increases when a closed type support is loaded. The resulting axial displacement is $\Delta h = 0.9\mu$ m and the rate of change of film thickness is $\varepsilon = \frac{\Delta h}{h_0} = \frac{0.9}{30} = 0.03 < 0.2$ when a pair of oil pads are subjected to *W*=5000 N load. Therefore, the load-bearing performance at this viscosity is fully satisfactory.

The diference between the upper and lower oil pad flm thicknesses and the initial flm thickness is only 3% due to the turntable's very small rate of change in flm thickness under a 3t load. There are a total of twelve oil pads in the axial bearing of the hydrostatic turntable. The power consumption of each oil pad does not difer signifcantly. Therefore, the total power consumption of the axial hydrostatic bearing of the hydrostatic turntable can be approximated as $N_t = 67.52Wx12 = 810.24W$. In summary, the total power consumption of the axial hydrostatic bearing of the hydrostatic turntable was reduced by 11.55% compared to that before optimization.

(2) Optimal initial oil flm thickness solution.

The hydrostatic bearing relies heavily on the presence of a dependable oil flm, which is an essential prerequisite for its efficient operation. The failure of the oil film poses a serious safety hazard, which can signifcantly impair the normal functioning of machine tools. As such, the flm's thickness must be carefully regulated to avoid risking oil film failure due to a lack of sufficient thickness. It is worth noting that the oil flm thickness in the hydrostatic

support system's design must be less than the oil boundary layer thickness since the viscous fow of the sealing edge is a necessary condition for maintaining pressure in the oil pocket [[37](#page-17-0)[–39\]](#page-17-1). This ensures the reliability of the Reynolds equation viscous shear stress calculation. In light of the aforementioned variables and potential errors, the initial oil flm thickness is established between 10μm to 50μ m, as depicted in Fig. [15.](#page-11-0) In addition, the initialized population size is $X = 50$, which is similar to the optimal viscosity solution. The chromosome binary code length is $L_G = 9$. The maximum number of evolutionary generations is $G = 100$. The crossover probability is $P_c = 0.8$ and the variation probability is $P_m = 0.1$.

The population individual evolution curve at the end of optimization is shown in Fig. [15](#page-11-0). The optimization result is that the power is minimized when $h_0 = 17.8 \mu m$ with the value of $N_t = 46.26 W \times 12 = 555.12 W$. The power is down 39.4% from before optimization. The resulting axial displacement is $\Delta h = 0.5 \mu m$ under the load of $W = \frac{30000}{6} = 5000$ N. The rate of change of film thickness is $\varepsilon = \frac{\Delta h}{h_0} = \frac{0.5}{17.8} = 0.028 < 0.2$, so the load-bearing perfor-

(3) Optimal oil sealing edge width solution.

Figure [17](#page-12-0) presents the impact of the oil sealing edge width on the thrust and power of a single oil pad under no-load conditions. As observed from the fgure, increasing the size of the oil sealing edge reduces the power consumption, but it also results in a reduction in the thrust of

(a) Power of individuals per generation (b) Position of individuals per generation

 100

Minimum powe

Average power

Fig. 17 The relationship between load-bearing performance and oil sealing edge

the oil pad. For closed supports, the thrust of a single oil pad is signifcantly diminished, resulting in more axial displacement when a load is applied. As a result, the load capacity and stifness of the entire turntable are reduced. Therefore, it can be inferred that an optimal sealing edge width that minimizes power at a certain pressure does not exist. According to engineering experience and relevant literature [\[2](#page-15-5)], for stationary or low-speed rectangular (sector) and circular closed hydrostatic supports, it is generally

recommended that the ratio of oil sealing edge width to outer diameter should be approximately $\frac{2B}{R_0 - R_1} = 0.3$. The width of the sealing oil edge was calculated to be 10mm, resulting in minimized power, and there is no scope for further optimization.

4 Simulation Verifcation

4.1 Calculation Settings

(1) Modeling and meshing

Initially, a three-dimensional oil film model of the bearing was created using Solidworks and then imported into Workbench Mesh for mesh generation. The quality of the mesh directly affects the accuracy of the computation results. In the grid configuration section, the overall size of the grid is set to 0.5 mm. With regards to the oil film region, given its thickness is approximately 0.03 mm and considered as a thin body, the sweeping technique is utilized to construct the grid. Specifically, ten layers of mesh are drawn along the thickness direction, and the mesh is refined in the vicinity of the thin oil film region. The automatic mesh generation method is applied in other areas.

a) Skewness grid quality evaluation

b) Orthogonal Quality grid quality evaluation

Upon the accomplishment of grid partitioning, Ansys' Mesh Metric can be employed to assess the quality of the partitioned grid. Skewness, which is one of the primary methods for evaluating mesh quality, can be calculated using two algorithms: Equilateral-Volume-Based Skewness and Normalized Equiangular Skewness. Its numerical value ranges between 0 and 1, with 0 being the most desirable and 1 being the least desirable. Figure [18](#page-12-1)a illustrates the evaluation of mesh quality using Skewness, which shows that the skewness values of all meshes are below 0.9, with an average value of 0.12. This assures the convergence of the Fluent calculation. Orthogonal Quality is another approach to check the quality of a mesh, with values ranging from 0 to 1, where 0 represents the lowest quality and 1 represents the highest. As shown in Fig. [18b](#page-12-1), the minimum orthogonal quality of the mesh is 0.15, and the average orthogonal quality is 0.9. Based on the two aforementioned evaluation criteria, the mesh quality is very high, which provides a solid guarantee for the accuracy of the analysis. After completing the meshing process, it is important to assign names to the inlet, outlet, wall, and interface boundaries for setting up the boundary conditions.

(2) Setting of boundary conditions

(1) Inlet boundary The pressure inlet boundary condition is selected at the entrance of the oil pad oil flm. According to Eq. ([1](#page-2-2)), with $h_1 = h_2$ in the initial state, the total pressure is set to $p_s/\beta_0 = 2$ MPa.

(2) Outlet boundary The outlet is located around the gap of the oil flm seal. The outlet boundary is set to the standard atmospheric pressure Pa=0.

(3) Wall boundary The upper surface of the oil flm is set as "wall up" and designated as a rotating wall with a rotation speed of 60 rpm, a rotation center at $(0, 0, 0)$, and a rotation axis along (0, 0, 1).

(4) Defning model The fow of oil in the oil pad can be approximated as steady-state fow. Therefore, the simulation type is set as "Steady State" and the turbulence model selected under "Fluid Models" is the laminar model.

(5) Solution control setting The solution method is set to SIMPLE Scheme, and the other options are set to the default values in Fluent. The initialization method is set as "Hybrid Initialization".

Fig. 19 Pressure cloud map

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(a) Shear stress cloud map

(b) Shear stress vector image

Fig. 20 Shear stress distribution

4.2 Calculation results

The calculated pressure distribution Fig. [19](#page-13-0) shows that the pressure in the oil pocket is about 2.14 MPa. The pressure at the raised part of the throttle is equal to the oil pocket pressure. At the oil sealing edge, the pressure is gradually decreasing to 0. This result is consistent with the result calculated by the fnite diference method.

Figure [20a](#page-14-0) and b depict the cloud map of shear stress distribution and the vector diagram of shear stress. The diagram indicates that the friction is relatively high at the raised part of the oil seal edge and the throttle due to the relatively small oil flm thickness. In contrast, the oil pocket part exhibits relatively low friction as the depth of the oil pocket is much greater than the oil flm thickness. Moreover, the magnitude of the friction force decreases gradually along the direction of rotation of the rotary table. This phenomenon can be attributed to the viscous force that propels the fuid to move with the turntable, thereby causing the oil flm to thicken along the rotation direction and reducing the friction force. The direction of the frictional force can be obtained from the arrow direction in Fig. [20](#page-14-0)b, and the magnitude of the frictional force is refected by the density of the arrows. Figure [20](#page-14-0) a and b together depict the situation of the frictional force acting on the oil pad surface.

4.3 Comparison of results

The main diferences between the simulated and theoretical values are: the simulated value is calculated with the fnite volume method, while the previous theoretical analysis is calculated with the fnite diference method; the controlling equation of the oil flm in the simulation is the three-dimensional N-S equation, while the fnite diference method is the two-dimensional Reynolds lubrication equation; the previous theoretical analysis simplifes the calculation of the oil pad, while the simulation software

Fig. 21 Comparison of viscosity effects

performs the complete solution. Figures [21,](#page-14-1) and [22](#page-15-6) compare the total power solved by simulation and the fnite diference method. Overall, the simulated and theoretical values are in good agreement. The left side of the fgure displays the total power consumption, while the vertical axis on the right side indicates the error.

Through a comparison of the theoretical model with the simulation value, it has been observed that there is some degree of error. However, it has also been found that the error range is kept under 10%. This comparison validates the accuracy and reliability of the theoretical model, numerical method, and oil pad optimization results. Therefore, the results obtained from this study can be considered as a reliable reference for the design and optimization of hydrostatic rotary tables.

Fig. 22 Comparison of flm thickness efects

5 Conclusion

This paper examines the oil pad of an internal feedback hydrostatic turntable, and establishes an oil pad pressure distribution model using the fnite diference method. The fow rate, friction force, support power, and friction power were computed, and the effects of viscosity and initial oil flm thickness on these quantities were analyzed for different structures. Subsequently, the minimum power consumption was determined through genetic algorithm optimization. Finally, the ANSYS Workbench software was employed to validate the theoretical analysis, demonstrating the method's reliability. Overall, this paper proposes an optimization method for minimizing the power consumption of the oil pad of an internal feedback hydrostatic turntable, leading to the following conclusions:

- 1. The friction power and support power of the oil pad are inversely correlated with viscosity under the same structural conditions. Specifcally, higher viscosity results in lower support power and higher friction power. Thus, selecting an appropriate viscosity can reduce the total power consumption of the pad. The optimization process applied to the model in this study resulted in a total power consumption reduction of 11.6%.
- 2. The initial flm thickness exhibits an opposite efect on the friction and support power of the oil pad under the same structural conditions, which is contrary to the efect of viscosity. Choosing a suitable initial flm thick-

ness can similarly reduce the total power consumption of the pad. The optimization process applied to the model in this study led to a total power consumption reduction of 39.4%.

- 3. The total power consumption of the oil pad decreases as the sealing edge size increases; however, this increase is accompanied by a decline in load-bearing performance. Therefore, there is no optimal width of oil sealing edge that minimizes the total power consumption, and the selection of the appropriate width should be based on the specifc circumstances.
- 4. The results of the ANSYS workbench simulation difer slightly from those of the fnite diference method; however, the error is kept under 10%. This provides evidence of the reliability of the fnite diference method.

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Declarations

Competing interest The authors declare no competing fnancial interests.

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