

# **Hollow Twist Extrusion: Introduction, Strain Distribution, and Process Parameters Investigation**

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#### **Abstract**

Twist Extrusion is kind of severe plastic deformation process which enhances the strength of materials by applying a shear plastic strain and consequently grain refnement. The strain distribution is minimum at the center of the die and is maximum at outer surfaces. In this article, the plastic strain distribution will be studied within a hollow section. The billet is solid in previous experimental and numerical studies in the literature, but by adding a new die (mandrel) for extruding the hollow billet, it is possible to twist extrude hollow sections. A fnite element model is developed in the ABAQUS fnite element software and the effects of process parameters (slope line angle, thickness and friction coefficient) on equivalent plastic strain distribution are investigated. The numerical results show that the equivalent plastic strain will be increased by increasing the slope line angle and decreasing the thickness and more homogeneity in the strain feld will be obtained. In addition, increasing the friction coefficient higher than 0.2 can lead to an increase in induced plastic strain. The required force for twist extrusion will be increased by increasing the friction coefficient.

#### **Graphical Abstract**



**Keywords** Hollow twist extrusion · HTE · Strain distribution · Slope line angle · Hollow section

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# **1 Introduction**

In recent years, diferent new severe plastic deformation (SPD) techniques are introduced to produce bulk ultrafne grain (UFG) materials. Some of the methods are in the category of top-down, which refnes the grains of bulk material and produce nanosize grains. The introduced methods have corresponding stress and strain distribution, but nonuniform plastic strain distribution can be observed in many of them. The hardening of the sample depends on grain

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refnement and work hardening at low temperature, So, the SPD processes are done as cold processes. The obtained microstructures are in the range of sub-micron, and in some cases, nanoscales ( $\sim$  100 to 300 nm) [[1,](#page-8-0) [2](#page-8-1)]. Main advantages of the SPD process are the higher strength and relatively appropriate formability which makes the UFG materials superior to others  $[3-5]$  $[3-5]$  $[3-5]$ . The size of the workpiece is almost remaining unchanged after performing the process and the process can be repeated in diferent passes to accumulate the induced plastic strain distribution and obtain more homogeneous strain distribution in the sample [[6,](#page-8-4) [7](#page-8-5)]. In most SPD processes, the maximum increase in the yield strength and ultimate tensile strength happens at the frst pass of the process [[8\]](#page-8-6). Diferent SPD processes are developed by the researchers, the most famous SPD processes are equal channel angular pressing (ECAP) and equal channel angular rolling (ECAR) [[9–](#page-8-7)[11\]](#page-8-8), high-pressure torsion (HPT) [\[12](#page-9-0), [13\]](#page-9-1), and twist extrusion (TE)  $[14–18]$  $[14–18]$  $[14–18]$ . In the beginning, the TE process introduced and developed by Beygelzimer et al. [\[19](#page-9-4)–[21\]](#page-9-5).

The die of TE consists of upper and lower straight channels and a twisting channel in the middle. The cross-section of the inlet and outlet are equal but the twist section forces the sample to twist and a shear strain will be created in the plane strain section, consequently, the grain refnement and material deformation will happen in the middle zone of the die (material deformation zone) [[19\]](#page-9-4). Figure [1](#page-1-0) shows a schematic illustration of a twist extrusion process. The material deformation zone or twisting zone can be represented by a slope line angle and rotation angle. The main diference of TE with other SPD process is the existence of two shear planes in the die (at the entrance and exit of the twisting channel), So, higher strain values can be obtained at outer surfaces of the sample compared to other SPD processes, such as ECAP [[17\]](#page-9-6). However, the strain distribution is not homogenous and varies from the center of the sample to the outer surfaces of the sample.

Most of the developed SPD processes are in the laboratory scale and the industries did not use them conventionally.



<span id="page-1-0"></span>

The costing tool is the main concern. Nevertheless, several efforts have been done to investigate different aspects of SPD processes and their efects on diferent materials [[22–](#page-9-7)[24](#page-9-8)]. Several pieces of research are published to emphasize the efect of process parameters [[22](#page-9-7)–[31\]](#page-9-9). Twist extruding of elliptical cross-section  $[25]$  $[25]$ , effect of the material  $[23, 26]$  $[23, 26]$  $[23, 26]$  $[23, 26]$  $[23, 26]$ , spiral equal channel angular extrusion [[27](#page-9-13)], planar twist extrusion  $[28]$  $[28]$ , off-axis twist extrusion  $[29]$  $[29]$  $[29]$ , tubular channel angular pressing [\[31\]](#page-9-9) and multi-channel spiral twist extrusion (MCSTE) [[32\]](#page-9-16) are examples of researches developed based on twist extrusion. In addition, modifcation and combination of two diferent SPD processes for example ECAP and TE are also interesting [\[22,](#page-9-7) [25,](#page-9-10) [33\]](#page-9-17). Professor Yan Beygelzimer is one of the outstanding researchers who published several pieces of research in the TE. Recently a review article was published by Beygelzimer et al. [[34](#page-9-18)] and an extensive survey of the literature on the mechanics of TE was published. The effect of twist extrusion on the microstructural evolution, mechanical properties, behavior of different materials during TE and the material flow during TE was discussed.

As it was mentioned in the literature until now, all of the researches have been focused on the twist extrusion process of solid specimens. To the authors' knowledge, there is not any research on the hollow twist extrusion process. Though, in this article, the hollow twist extrusion process will be introduced and will be investigated using the fnite element analysis by ABAQUS software. For this purpose, the efects of process parameters such as slope line angle, thickness and friction coefficient on the equivalent plastic strain distribution will be probed.

## **2 Finite Element Modeling**

The twist extrusion consists of extruding a billet through a die. Therefore, a fnite element model has been developed in the ABAQUS software. It is supposed that the billet was made from AA-1050 aluminum alloy. The material properties of billet were extracted from [[33\]](#page-9-17). The elastic modulus and Poisson's ratio are defned as 70 GPa and 0.33 respectively. The billet is a hollow square with 30 mm×30 mm external dimensions. The internal square hole is different. The cross sections of the initial billet are adjusted as 15 mm $\times$ 15 mm while studying the effect of slope line angle and friction coefficient. However, for investigation of thickness, the cross section is additionally changed to  $18.75$  mm  $\times$  18.75 mm, 22.5 mm  $\times$  22.5 mm and  $26.25$  mm $\times$  26.25 mm. The length of the initial billet is also 100 mm. Fig. [2](#page-2-0) shows the billet and dies in the isometric view. Three faces of the outer die are set as hidden to better view the inner die. The cross sections of TE die **Fig. 1** Schematic illustration of twist extrusion (TE) process are considered appropriate with the initial billet dimensions.



<span id="page-2-0"></span>**Fig. 2** Schematic illustration of the hollow twist extrusion dies and the initial billet

<span id="page-2-1"></span>**Table 1** Length of twist section for different slope line angle



A concentric mandrel similar to outer die is placed at the center. The die was modeled as a rigid part. The rotation angle is 90° clockwise and the length of the twisting section defned as Table [1](#page-2-1).

The fnite element analysis was done by the explicit solver of the software with enabled nonlinear geometry. The surface-to-surface contact was selected to defne the contact between the billet and the die surfaces. The billet was forced to move 100 mm downward to quit the billet from the die. This billet is meshed by a 3D, 8-node brick continuum element with reduced integration calculation (C3D8R). The die was meshed by a 4-node 3D bilinear rigid quadrilateral element (R3D4). A mesh sensitivity analysis was carried out and 1 mm mesh size was selected for simulation. Table [2](#page-2-2) shows the selected process parameters includes slope line angle, thickness and friction coefficient for numerical investigations. It should be noted that the main analysis was done with slope line angle 45°, 7.5 mm thickness and 0.1 friction coefficient. The other variations are implemented according to the One Factor At Time (OFAT) procedure in the design of experiments method. The literature review shows that higher slope line angles led to more deformation and

#### **3 Results and Discussion**

### **3.1 Verifcation of the FE Model**

As described in the Introduction section, the twist extrusion process is done only for the full solid section and this article is introducing a hollow twist extrusion concept. In this way, for verifcation of the fnite element model, the fnite element model was modifed to extrude a section similar to Kim et al. [[33\]](#page-9-17). The article extrudes a 10 mm  $\times$  10 mm square section by 45° slope line angle of the die from AA1050 aluminum alloy. The material property and frictional condition were defned similarly to Kim et al. [[33](#page-9-17)]. After completing the analysis, the results of the FE model are compared to the reported results of [[33](#page-9-17)] (Fig. [3\)](#page-3-0). The path of plotting the results is defned from the left edge to the right edge of the section (at the middle of width). Comparison of the results show good agreement between the FE model and reported results of Kim et al. [\[33](#page-9-17)]. The mesh size is not specifed at Ref. [\[33](#page-9-17)] and part of the diference may be associated with the element size in the FE model.

<span id="page-2-2"></span>**Table 2** The process parameters variation in the fnite element simulations





<span id="page-3-0"></span>**Fig. 3** Comparison of the equivalent plastic strain distribution for verifcation

#### **3.2 Efect of Slope Line Angle**

Figure [4](#page-3-1) shows the Von Mises stress and equivalent plastic strain (PEEQ) distribution obtained by the fnite element analysis of the twist extrusion process. A path is defned across the center of the hollow square section. Figure [5](#page-4-0) shows the equivalent plastic strain (PEEQ) distribution along the defned path for diferent slope line angle. The horizontal dotted line corresponds to the hollow zone and it is not existing physically. The results show that a higher magnitude of plastic strain will be obtained by increasing the slope line angle. In addition, the inner surfaces of the section experience higher strains depending on the slope line angle.



<span id="page-3-1"></span>**Fig. 4** The Von Mises stress and equivalent plastic strain distribution for slope line angle **a**, **b** 30°; **c**, **d** 45°; **e**, **f** 60°



<span id="page-4-0"></span>**Fig. 5** Comparison of equivalent plastic strain distribution across the centerline of the section for diferent slope line angle



<span id="page-4-1"></span>**Fig. 6** Comparison of the required force for twist extruding of billet with diferent slope line angle

Figure [6](#page-4-1) shows the required force for extruding diferent samples obtained from fnite element analysis.

According to the results of Figs. [4,](#page-3-1) [5](#page-4-0) and [6](#page-4-1), increasing the slope line angle leads to higher residual stress distribution in the fnal billet. The magnitude of stress is higher at the corners of the billet, which experiences more plastic deformation. In addition, the maximum of plastic strain increases by increasing the slope line angle and it can be observed at the corners of billet. By increasing the slope line angle, the area of the region that has higher plastic strains will be decreased and in the slope line angle  $60^{\circ}$  become minimum. More homogeneity in plastic strain distribution can be observed for a higher slope line angle. This is due to the decrease in the length of the material deformation zone (MDZ) in the die and increasing the rate of deformation behavior in twist extruding. Consequently, the required force for extruding the billet through the die will be increased by increasing the slope line angle. The maximum force required for twist extruding are 73, 118 and 243 kN for 30°, 45° and 60° slope line angle. The required force increased by 61.6% and 232.8% compared to the 30° slope line angle.

#### **3.3 Efect of Thickness**

Figure [7](#page-6-0) shows the distribution of Von Mises stress and equivalent plastic strain in hollow twist extrusion. The cross

section is 30 mm $\times$ 30 mm. The results show that when the section is fully solid and no hole exists, a large area of the sample will experience very low plastic strains. Decreasing the thickness leads to more stress concentration at four corners of the extruded section, hence the maximum of stress (residual stress) will be increased. In addition, by decreasing the thickness more homogeneity in the stress will be seen and warping of corners increases at lower thickness. The corners have the highest plastic strain and consequently higher strength (flow stress). By decreasing the thickness, the maximum of residual plastic strain will be increased. The diference between the maximum and minimum plastic strains reduces by decreasing the thickness and more homogeneity in the strain distribution can be observed.

Figure [8](#page-6-1) shows the equivalent plastic strain distribution along the width of the sample passing from the centerline of the section. The x-axis distance starts from the left edge and ends at the right edge of the section. The slope line angle is 45° and the graphs show that the maximum value of plastic strain increases by decreasing the thickness. Comparing the equivalent plastic distribution in Fig. [8](#page-6-1) shows that the slope of the graphs for hollow sections is similar to the full solid section and in the zones which no material exists, the strain distribution does not exist. This is due to applying more pressure at the workpiece and increasing the role of shear stress induced by twisting. The horizontal dotted lines show the inner zone of the hollow section which no material exists in this zone. Comparing the results of plastic strain distribution in Fig. [7](#page-6-0) and the plots of Fig. [8](#page-6-1) demonstrate that higher values of plastic strain can be seen in the contours which are not presented in the plots. Figure [7](#page-6-0) shows that maximum plastic strain value exists at the corners and minimum plastic strain value exists at the center of the lateral edges. The induced strains correspond to the distance from the center of the die. So, the diference between the maximum values of plastic strain in Figs. [7](#page-6-0) and [8](#page-6-1) relates to the location of graph plots in Fig. [8.](#page-6-1) The graphs of Fig. [8](#page-6-1) are plotted at the middle of width crossing from the center. Figure [9](#page-6-2) shows the variation of the required force for twist extrusion for diferent thicknesses. The required force of TE is almost equal for 5.625 mm, 3.75 mm and 7.5 mm (which is not shown in the fgure for more clarity) in comparison by the required force for the full solid section. However, when thickness decreases to 1.875 mm, the required force will be increased considerably. This is due to increasing the contact between the workpiece and die and the resist of material against induced shear stress due to the twisting in the material deformation zone. By decreasing the thickness, the area of the inside square hole will be increased, consequently, the friction force of the internal surface will be increased. The maximum of TE force is 108, 117 and 115 kN for the solid section, 5.625 mm, 3.75 mm thickness respectively. This force is 369 kN for 1.875 mm thickness which shows about



<span id="page-6-0"></span>**Fig. 7** The Von Mises stress and equivalent plastic strain distribution ◂ for diferent thickness **a**, **b** solid section; **c**, **d** 7.5 mm; **e**, **f** 5.625 mm; **g**, **h** 3.75 mm; **i**, **j** 1.875 mm

a 220% increase in force. Therefore, the required force for extruding will be increased by decreasing the thickness to a very small value.

Figure [8](#page-6-1) shows that the diference between the plastic strain distributions is small enough to neglect the changes (about 2% diference can be seen). The previous researches [\[5](#page-8-3), [12](#page-9-0)] show that the minimum and maximum of the plastic strain can be described by Eqs. [1](#page-6-3) and [2.](#page-6-4)

$$
\varepsilon_{\min} \approx a + b \tan \beta \tag{1}
$$

$$
\varepsilon_{\text{max}} \approx \frac{2}{\sqrt{3}} \tan \beta \tag{2}
$$

*a* and *b* are constant and  $\beta$  is the slope line angle. According to Fig. [8](#page-6-1) and Eqs. [1](#page-6-3) and [2,](#page-6-4) the equivalent plastic strain in the twist-extruded workpiece can be expressed by Eq. [3](#page-6-5).

$$
\varepsilon^{p} = \begin{cases}\n0.04 + \frac{r}{\frac{\sqrt{2}}{2}a} \tan \beta & -\frac{a}{2} \le r \le -\frac{a_{i}}{2} \\
\text{No physical material} & -\frac{a_{i}}{2} < r < \frac{a_{i}}{2} \\
0.04 + \frac{r}{\frac{\sqrt{2}}{2}a} \tan \beta & \frac{a_{i}}{2} \le r \le \frac{a}{2}\n\end{cases} \tag{3}
$$

 $a_i$  and  $a$  are the internal out external width of the hollow square section and *r* is the radial distance from the center of the square. The constant number (0.04) stands for the crossflow of material at the center of the die.

It should be noted that the material fow during twist extrusion consists of two parts: a helical flow and deviations from the helical fow. The helical fow is created due



<span id="page-6-1"></span>**Fig. 8** Comparison of equivalent plastic strain distribution across the centerline of the section for diferent thickness



<span id="page-6-3"></span><span id="page-6-2"></span>**Fig. 9** Comparison of the required force for twist extruding of billet with diferent thickness

<span id="page-6-5"></span><span id="page-6-4"></span>to the ideal twisting of the billet in the die. The helical fow varies according to the relative location from the center of twisting. The cross-fow is determined as deviations from the helical fow, resulting in planar fow within a virtual transverse section of the billet. In contrast to the ideal helical flow, the cross-flow leads to displacement of the material points from their initial locations in cross-section. Equation [3](#page-6-5) shows the two mentioned material fow. Researches show that the cross flow increases by increasing the slope line angle and increasing the friction coefficient between the die and the billet [\[35\]](#page-9-19). When the cross-fow is weak, the cross-section of a solid billet rotates as a rigid body when the billet moves through the twisting channel. In this case, a velocity feld for the twist extrusion of a hollow billet on a rigid mandrel practically coincides with a velocity feld for the twist extrusion of a solid billet. The good agreement between the results of plastic strain distribution in the hollow section and solid section can be explained based on the material flow in the twist extrusion process.

#### **3.4 Effect of Friction Coefficient**

Figure [10](#page-7-0) shows the effect of the friction coefficient on Von Mises stress and equivalent plastic strain. Distribution of stress shows that the residual stress distribution is more uniform by increasing the friction coefficient. Moreover, the maximum stress at corners will be increased slightly. The elements distortion will be increased considerably by increasing the friction coefficient, which can be seen in Fig. [10g](#page-7-0). Figure [11](#page-8-9) shows the distribution of the equivalent plastic strain along the centerline of billet. Comparing the equivalent plastic strain in Figs. [11](#page-8-9) and [10](#page-7-0) it can be concluded that the strain distribution is almost constant at friction coefficient  $0.1$  and  $0.2$  and no friction. The magnitude of plastic strain at the contact surface will be increased slightly, but in the inner zone, the distribution is the same. However, the results for friction coefficient  $0.3$  is different and the strain distribution increased considerably. Furthermore, the



<span id="page-7-0"></span>Fig. 10 The Von Mises stress and equivalent plastic strain distribution for different friction coefficient **a**, **b** no friction; **c**, **d** friction coefficient 0.1, **e**, **f** friction coefficient 0.2; **g**, **h** friction coefficient 0.3

small increase in the maximum value of plastic strain can be observed at the corners of the extruded billet. Figure [12](#page-8-10) shows the required force for implementing the twist extrusion process with different friction coefficient. The required force will be increased by increasing the frictional force. The maximum force is considerably high for friction coefficient 0.3. So, increasing the friction coefficient more than  $0.2$ leads to consequently higher extruding force, more element distortion and higher plastic strain distribution.



<span id="page-8-9"></span>**Fig. 11** Comparison of equivalent plastic strain distribution across the centerline of the section for different friction coefficient



<span id="page-8-10"></span>**Fig. 12** Comparison of the required force for twist extruding of billet with different friction coefficient

## **4 Conclusions**

In this article, a new setup for twist extruding of hollow sections were introduced and the efect of process parameters was investigated. The main outcome of this study can be emphasized as follows:

- The equivalent plastic strain distribution will be increased by increasing the slope line angle. The plastic strain at inner surfaces increases similar to outer surfaces.
- The required force for carrying out the twist extrusion will be increased by increasing the slope line angle.
- By decreasing the thickness, part of the section which has a low value of plastic strain will be eliminated and more uniformity in the plastic strain distribution will be obtained.
- The equivalent plastic strain distribution for different thicknesses are similar to plastic strain distribution of full solid section at a constant slope line angle.
- The required force of the twist extrusion will be increased for very small thicknesses.

• Low friction coefficient has a negligible effect on the plastic strain distribution, but the friction coefficient higher than  $0.2$  can lead to an increase in induced plastic strain due to twist extruding. The required force for twist extrusion will be increased by the friction coefficient.

In this article, the authors introduced a new confguration for hollow twist extrusion. The investigation has been done numerically. The next step in the development of the introduced process is the experimental tests and comparison of fnite element results by the presented numerical results.

# **Compliance with Ethical Standards**

**Conflict of interest** The authors declare that they have no confict of interest.

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