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# **Evolving learners' behavior in data mining**

**Nitin Pise1 · Parag Kulkarni1**

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**Abstract** An evaluation and choice of learning algorithms is a current research area in data mining, artifcial intelligence and pattern recognition, etc. Supervised learning is one of the tasks most frequently used in data mining. There are several learning algorithms available in machine learning feld and new algorithms are being added in machine learning literature. There is a need for selecting the best suitable learning algorithm for a given data. With the information explosion of different learning algorithms and the changing data scenarios, there is a need of smart learning system. The paper shows one approach where past experiences learned are used to suggest the best suitable learner using 3 meta-features namely simple, statistical and information theoretic features. The system tests 38 UCI benchmark datasets from various domains using nine classifers from various categories. It is observed that for 29 datasets, i.e., 76 % of datasets, both the predicted and actual accuracies directly match. The proposed approach is found to be correct for algorithm selection of these datasets. New proposed equation of fnding classifer accuracy based on meta-features is determined and validated. The study compares various supervised learning algorithms by performing tenfold cross-validation paired *t* test. The work helps in a critical step in data mining for selecting the suitable data mining algorithm.

**Keyword** Machine learning · Data mining techniques · Classifcation · Data characteristics · Learning algorithms · Intelligent data analysis

 $\boxtimes$  Nitin Pise nnpise@yahoo.com

## **1 Introduction**

There is an immense amount of data available; a lot can be learned from this data. Learning manually is very time consuming. Many researchers have proposed methods to make machines learn from available data automatically. The purpose of learning in machine learning is to empower decision makers so that they can make better decisions. Similarly, machines should be empowered to make better decisions and improve their ability with value addition. In many real-life situations, the problem is not static. It can change with time and depend on the environment in which the problem is to be solved. The solution also can depend upon the decision context. The overall information is required to build the context.

Memorization and rudimentary learning are some of the examples of learning. The goal of learning is to help in better decision making. Learning gives intelligence and is centered on a goal.

There are three types of learning. Learning from a set of examples or historical data is supervised learning. It works on labelled data. This is a very common and the most frequently used forms of learning. It is mostly used for classifcation task in data mining. When labelled data is not available, it is diffcult to use supervised learning. In these situations, learning without a teacher, i.e., unsupervised learning is used. Unsupervised learning is used for clustering applications. In practical situations, we need to learn from not only labelled data but also unlabeled data. This type of learning is called as semi-supervised learning.

Learning is a continuous process. Learning is not only knowledge acquision, but it involves different processes to gather knowledge, manage and augment knowledge. Learning needs prior knowledge. Learners can use the past



<sup>1</sup> College of Engineering, Shivajinagar, Pune 411 005, India



<span id="page-1-1"></span>**Fig. 1** Taxonomy of machine learning algorithms

knowledge to construct new understandings and make decisions on new data.

Different scenarios can be used to learn in supervised learning and expected outcomes can be further used as a learning sample. So if we are in a similar situation in the future, we can suggest the best possible decision available. This can be done if a new scenario is modelled to any of the previous scenarios.

Learning takes different forms, e.g., imitation, memorization, induction, deduction, inference, learning from examples and observation based learning, etc. There is another type of learning in which learning takes place based on the feedback. The feedback is in the form or reward or penalty. This is called reinforcement learning (Sutton and Barto [1998\)](#page-16-0). In this type of learning, learners or software agents learn by interacting with the environment.

Learning can be based on data, different events and patterns. It can be system-based also. Adaptive machine learning algorithm (Kulkarni [2012\)](#page-15-0) can be considered as a model where individuals need to respond and act in changing environments.

Imbalanced learning (Cai et al. [2014](#page-15-1)) is now a popular research topic for number of applications in data mining. Classifcation involving imbalanced class distributions poses a major problem in the performance of classifcation systems (Sun [2007\)](#page-16-1). Many applications such as, network intrusion detection, fraud detection, medical diagnosis, etc., have to suffer due to the problem of imbalanced data. The paper assumes relatively balanced class distributions. So it doesn't depict different methods used to remove the effect of imbalance in data and special methods like SMOTE (Chawla et al. [2002](#page-15-2)).

The paper is prepared into six sections. After the introduction, Sect. [2](#page-1-0) covers the background and related work on this topic. We discuss proposed work in detail in Sect. [3](#page-4-0). Section [4](#page-6-0) describes experimental set up, datasets used and empirical results found out. Section [5](#page-13-0) depicts conclusions from the paper and how the work can be extended further. We conclude the paper listing contributions in the discussion section.

### <span id="page-1-0"></span>**2 Background and related work**

Kulkarni ([2012\)](#page-15-0) refers adaptive machine learning as learning with adapting to the environment, a learning task or a decision scenario. The learning can be based on past knowledge, experience from previous examples and expert advice. A particular method which is successful in one situation or for a specifc task may not prove successful for all the learning types (Wolpert and Macready [1997](#page-16-2)). The learning process is closely associated with the learning problem. It also depends on what we are trying to learn and what are our learning goals. So, while selecting learning algorithms or methods, the problem is required to be understood. The learning problem needs to be analyzed and select the most suitable approach dynamically in adaptive learning. It is not just using more than one methods or moving from one method to other method. But it is selecting data intelligently and choosing the suitable learner.

Sewell [\(2009](#page-16-3)) explains a taxonomy of machine learning in which machine learning algorithms are categorized in six ways. Figure [1](#page-1-1) shows taxonomy of machine learning algorithms. Model type decides whether the machine learing algorithm is probabilistic or non-probabilistic. The probabilistic model involves building a full or partial probability model. A discriminant or regression function is used in non-probabilistic model. Based on reasoning they can be classifed as induction or transduction algorithms. Induction reasoning is learning from past training cases to general rules, that are further operated on the test cases.

Reasoning from observed, training examples to test examples is transduction reasoning.

Machine learning algorithms can be further categorized into batch or online depending upon how the learner receives training data. In batch learning, the learner is provided with all the data at the time of beginning. But this is not done in online learning. One example at a time is provided to the learner, which approximates the output, before receipt of the exact value in online learning. Each new example helps the learner for updating its current hypothesis and the total number of mistakes done during learning decides the quality of learning (Sewell [2009\)](#page-16-3).

Depending upon the task which is to be carried out, machine learning algorithms are divided into classifcation or regression algorithms. Classifcation (Tan et al. [2013\)](#page-16-4) is the assignment of objects to one of a number of existing classes. Classifcation is fnding a function f mapping attribute set x to one of the existing classes y. It is a pervasive problem which encompasses diverse applications such as spam mail detection, analyzing MRI scans to categorize cells as malignant or benign, classifying millions of home loan applications into credit worthy and non credit worthy, and categorizing galaxies with their shapes, etc.

Regression (Tan et al. [2013](#page-16-4)) is a predictive modelling technique where the estimated target variable is continuous. Regression is learning a function f mapping attribute set x into a output y that is continuous-valued. Thus, regression fnds a target function ftting the input data with minimum error. Examples of applications of regression include stock market prediction, projection of the total sales of a company by considering he amount spent for advertising, and so on.

Based on the classifcation model type, machine learning algorithms can be grouped into generative, discriminative or imitative algorithms (Kulkarni [2012](#page-15-0)). The class conditional density  $p(x | y)$  is modelled by some unsupervised learning procedure in generative algorithms (Chapelle et al. [2006](#page-15-3)). Bayes theorem (Mitchell [1997](#page-15-4)) is used to infer predictive density. Discriminative algorithms estimate  $p(y \mid$ x). Support vector machine (SVM) (Joachims [1999\)](#page-15-5) is an example of discriminative algorithm.

There are different kinds of learning in machine learning. Four kinds of learning, namely supervised, unsupervised, semi-supervised learning and reinforcement learning are very important in machine learning. Supervised learning algorithms are classifed by Hormozi et al. [\(2012](#page-15-6)). Supervised learning algorithms are compared empirically in (Caruana and Niculescu-Mizil [2006\)](#page-15-7). Supervised learning algorithms are divided into the following methods:

- Decision trees
- Artifcial Neural Networks
- Support Vector Machine (SVM) (Joachims [1999\)](#page-15-5)
- Instance-based learners
- Bayesian networks
- Probably approximately Correct (PAC) learning (Valiant [1984\)](#page-16-5)
- Inductive Logic Programming (ILP)
- Ensemble methods (Polikar [2006](#page-16-6); Tan et al. [2013\)](#page-16-4)

The back-propagation (BP) learning algorithm is a supervised neural network algorithm. It is used for multilayered feed-forward neural architectures. (Curran et al.

[2011](#page-15-8)) demonstrate that visual spectrum study and a back propagation neural network classifer can be used to discriminate the breadth patten in certain places of the body. Liu and Cao [\(2010](#page-15-9)) proposes application of recurrent neural network (RNN). They propose RNN to solve extended general variational inequalities based on the projection operator and a novel k-winners-take-all network (k-WTA) based on a one-neuron RNN. The advatntages of k-WTA are that it has a simple structure and fnite time convergence. One more application of RNN that is based on the gradient method is proposed by Liu et al. ([2010b\)](#page-15-10) for solving linear programming problems. The proposed network globally converges to exact optimal solutions in fnite time.

SVM (Joachims [1999\)](#page-15-5) is a classifcation technique which is used by a number of researchers and is based on statistical learning theory. SVM is suitable for classifying high-dimensional data (Tan et al. [2013\)](#page-16-4). Selecting the kernel function is probably the trickiest part in SVM. The kernel function is signifcant as it creates the kernel matrix, which plays the important role in summarizing all the data. Linear, polynomial and RBF kernels can be used in SVM.

Approaches to unsupervised learning are as follows:

- Clustering (Tan et al. [2013](#page-16-4))
- Hidden Markov Models (HMMs)
- Principal Component Analysis (PCA)
- Independent Component Analysis
- Adaptive Resonance Theory (ART) (Yegnanarayana [2005](#page-15-3))
- Singular Value Decomposition (SVD)
- Self Organizing Map (SOM) (Kohonen [2001\)](#page-15-11)

Clustering techniques (Witten et al. [2005](#page-16-7)) are used when the instances are to be divided into natural groups. Clustering algorithms are classifed as partitioning, hierarchical, density based and so on.

A detailed survey of semi-supervised learning algorithms is presented by Pise and Kulkarni ([2008\)](#page-16-8). Several semi-supervised classifcation algorithms are very popular which include Co-training, Expectation Maximization (EM) algorithm, transductive support vector machines (TSVMs). Self-training, graph based methods and multi-view learning are other important semi-supervised learning methods. Temporal Difference (TD) learning and Q-learning are important methods in Reinforcement learning which are explained in Kulkarni ([2012\)](#page-15-0).

There are number of algorithms in each of the category. Every algorithm cannot give better accuracy or does not perform well for all the datasets. When we want to work on a particular dataset, we have to evaluate a lot of algorithms for checking whether the particular algorithm is suitable for a given problem. This takes a lot of time by checking results of each of these algorithms on that particular

<span id="page-3-0"></span>

dataset. Instead of wasting the time required for evaluation of each of the algorithm on the particular dataset, we are using a classifer selection methodology based on dataset characteristics. Here three different data characteristics, namely simple, statistical and information theoretic measures are used. The focus of the paper is on supervised machine learning algorithms.

The added taxonomy is depicted in Fig. [2](#page-3-0) (Kulkarni [2012](#page-15-0)). Based on the learning needs, machine learning algorithms are classifed in adaptive, incremental or multi-perspective learning.

Adaptive machine learning (Kulkarni [2012](#page-15-0)) refers to learning that adapts with the environment or a learning problem. The learning uses the gathered information, experience, past knowledge, and expert advice. The learning process is closely associated with the learning problem or what are trying to learn. Hence the choice of learning methods demands an understanding of the learning problem. Adaptive learning involves the intelligent choice of the most appropriate method.

Incremental learning (IL) is proposed in Kulkarni [\(2012](#page-15-0)). The learning is done in stages, and during every stage the learning algorithm receives some new data for learning. So there is a need for incremental learning. IL effectively uses already created knowledge base during the next phase of learning and does not affect accuracy of decision making.

Multi-perspective learning (Kulkarni [2012](#page-15-0)) refers to learning that uses the knowledge and information acquired and is built from different perspectives. Multiperspective decision making uses multi-perspective learning that includes methods for capturing perspectives and the captured data and knowledge perceived from different perspectives.

Further, they can be categorized perceptual, episodic or procedural based on human-like learning mechanism.

Ensemble learning (Polikar [2006\)](#page-16-6) consists of more than one learner for the same problem. Kotsiantis et al. ([2006\)](#page-15-12) depicts a variety of classifcation algorithms and ensembles of classifers that improve classifer accuracy. If we want to improve classifcation accuracy, it is hard to fnd a single classifer or a good committee of experts. There are advantages of ensemble methods, but they have three weakness. Ensembles require more storage because all classifers need to be stored after training. The second weakness is increased computation; as all component classifers must be processed. The third weakness is they are less comprehensible. As multiple learners or classifers are involved in decision making, difficulty is faced by nonexperts in perceiving the underlying reasoning process leading to decision.

An evaluation and selection of classifcation algorithm is a current research topic in data mining, artifcial intelligence and pattern recognition (Kou and Wu [2014\)](#page-15-13). Vilalta and Drissi ([2002\)](#page-16-9) reviews the different aspects of metalearning. Meta-learning is learning about learners. It is learning at a meta-level. It works on the experience gathered from past data, i.e., it works on the past performance of different learners.

Smith-Miles ([2008\)](#page-16-10) presents the algorithm recomendation problem using meta-learning and explains its uses in classifcation, regression, prediction of time series, optimization and constraint satisfaction.

Several systems for algorithm selection are proposed in the literature. Sleenman and Rissakis [\(1995](#page-16-11)) presents an expert system called "Consultant" which fnds out the characters of the application and the data. It questions users several times. This system does not test the data but considers the users' subjective experiences. Michie et al. [\(1994](#page-15-14)) describes STATLOG project in which various metafeatures are extracted from registered datasets, and these meta-features are combined with the performance of the algorithms. Once a new dataset arrives, the system makes comparison of the meta-features of the new dataset and old datasets. This takes a lot of time. Alexandros and Melanie ([2001\)](#page-15-15) describes a system called Data Mining Advisor (DMA) having a set of algorithms and training datasets. K-NN algorithm (Cover and Hart [1967\)](#page-15-16) is used to fnd a similar subset in the training dataset based on the performance of algoritms. It ranks the candidate algorithms and recommends based on the above subset.

The method which combines accuracy and execution time for comparing two algorithms' performance on the similar data set is called Adjusted Ratio of Ratios (ARR) is described in Brazdil and Soares [\(2000\)](#page-15-17). Romero et al. [\(2013\)](#page-16-12) applies meta-learning to recommend the best subset of classifcation algorithms for 32 Moodle datasets. Complexity, domain specifc features and traditional statistical features are used in this paper. But the study is limited as educational datasets are used. Pinto et al. ([2014](#page-16-13)) proposes a framework for decomposing and developing meta-features for metalearning problems. Meta-features namely simple, statistical and information-theoretic metafeatures are decomposed using the framework.



<span id="page-4-1"></span>

Fan and Lei ([2006\)](#page-15-18) explores a meta-learning approach that helps user to choose the most suitable algorithms. Selecting the suitable algorithm is crucial during data mining model building process.

Evolutionary computing (EC) is useful in fne-tuning hyper-parameters for the different learning algorithms. Genetic algorithms (GA), evolutionary programming (EP), etc. are important methodologies in EC. Oduguwa et al. [\(2005](#page-16-14)) bridges the gap between theory of EC and practice by taking case of manufacturing industry. Preitl et al. [\(2006](#page-16-15)) deal with not only theoretical but also application aspects concerning iterative feedback tuning (IFT) algorithms in the design of fuzzy control systems. Closed-loop data computes the likely gradient of the cost functions. IFT or other gradient-based search methods are useful for optimizing hyper-parameters of the learning algorithms. This helps to improve the learner's performance.

So we develop a method which uses supervised learning algorithms and ensembles. Based on the problem to be solved, the different learning algorithms are recommended by this system.

## <span id="page-4-0"></span>**3 Proposed work**

Our work is based on meta-learning (Brazdil et al. [2008](#page-15-19)). Meta-learning is learning about learners. Knowledge learned in previous experiences or experiments is used to manage new problems in a better way and is stored as metadata (F), particularly meta-features (B) and meta-target as shown in Fig. [3.](#page-4-1) The meta-features extracted from A to B depict the relation between the learners and the data used. The Meta-target is required to be extracted through C-D-E for further storing in F. The algorithm that works the best for a given dataset is represented by the meta-target.

Figure [4](#page-5-0) shows the system flow for recommending suitable classifer. Data Characterization Tool (DCT) is implemented in Java for calculating dataset characteristics which are also referred as meta-features. New dataset characteristics are provided to k-NN algorithm and results are stored in the knowledge base that determines learning algorithm performance based on dataset characteristics. Similarity between historical datasets and a new dataset is used to recommend suitable algorithm.

How to defne meta-features or data characteristics is the main issue in meta-learning. The state of the art shows that there are mainly three types of meta-features: (1) simple, statistical and information theoretic (Brazdil et al. [2003](#page-15-20)), (2) model-based (Peng et al. [2002\)](#page-16-16), (3) landmarking (Pfahringer, Bensusan, and Giraud-Carrier [2000](#page-16-17)). In the frst group we fnd out the number of instances, the number of attributes, kurtosis, skewness, correlation between numeric attributes or class entropy to name a few. Application of these meta-features provides knowledge about the problems. A model is generated by applying a learner to a problem or a dataset, i.e., the number of leaf nodes of a decision tree. Some characteristics of this model are captured by model-based meta-features. Land-marking meta-features are created by making a quick performance approximation of a learner in a particular dataset.

We have explored the frst group of meta-features as shown in Table [1](#page-5-1). Table [1](#page-5-1) shows the various meta-features used and how they are denoted in the experimental work. Meta features numbered from 3–13 are simple



<span id="page-5-0"></span>Fig. 4 System flow for recommending suitable classifier

meta-features; kurtosis and skewness are statistical metafeatures and entropy is information theoretic meta-feature.

Kurtosis is a measure of the fatness of the top of a symmetric distribution.

Distribution's degree of kurtosis,

$$
\eta = \beta_2 - 3
$$
  
where 
$$
\beta_2 = \frac{\sum (Y - \mu)^4}{n\sigma^4}
$$
 (1)

*n*σ<sup>4</sup>  $\beta$ <sup>2</sup> is often called "Pearson's kurtosis".

The third moment is used to defne mean Skewness.

$$
\gamma_1 = \frac{\sum (Y - \mu)^3}{n\sigma^3} \tag{2}
$$

 Skewness is negative if shape of distribution is skewed to the right.

Entropy is used for giving the amount of information in bits by a particular signal state.

$$
Entropy (S) = -p + logp+ - p - logp-
$$
 (3)

Where  $p^+$  and  $p^-$  are positive and negative probabilities. The proposed approach uses Euclidean distance which is computed as follows:

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<span id="page-5-1"></span>**Table 1** Meta- features used for experimentation, how they are referred as in database and corresponding database attribute

Ref. as	Meta-features	Database attribute
3	Number of attributes	Norm_attr
4	Number of instances	Norm_inst
5	Number of classes	Norm_class
6	Number of symbolic attributes	Norm_sym
7	Number of numeric attributes	Norm_num
8	Number of missing values	Norm_missing
9	Number of distinct values	Norm_dist
10	% Missing values	<i><b>%missing</b></i>
11	Dimension	Norm_dimension
12	Ratio of symbolic attributes	Norm_sym $%$
13	Ratio of numeric attributes	Norm_num $%$
14	Kurtosis	Kurtosis
15	<b>Skewness</b>	<b>Skewness</b>
16	Maximum probability	Maxprob
17	Entropy	Entropy

using similarity between a new dataset and historical datasets.

#### **3.1 Methodology**

The methodology used in this work consists of the following nine steps:

- 1. Datasets are collected from UCI machine learning repository.
- 2. Meta feature extraction is done using Data Characteristics Tool (DCT) for training.
- 3. A learning algorithm with performance measure is considered. Classifcation accuracy is used as a performance criterion.
- <span id="page-5-2"></span>4. Knowledge base is created by considering performance of learning algorithms and data characteristics or metafeatures of datasets.
- 5. Extraction of meta-features is carried out for new unseen dataset using DCT.

$$
d(p,q) = d(q,p) = \sqrt{(q_1 - p_1)^2 + (q_2 - p_2)^2 + \dots + (q_n - p_n)^2} = \sqrt{\sum_{i=1}^n (q_i - p_i)^2}.
$$
\n(4)

Initially the results were tested using other distance measures such as Manhattan distance, but the results were not satisfactory. Hence Euclidean distance measure is used in the system. An algorithm is recommended

- 6. Use k-NN for fnding out k-similar datasets from the knowledge base.
- 7. Obtaining the algorithms for K-similar datasets.
- 8. Ranking of algorithms.

9. Algorithm recommendation which will help in decision making.

## **3.2 Learning algorithms or classifers used**

Learners or Classifcation algorithms (Nakamura et al. [2014](#page-16-18); Han and Kamber [2011](#page-15-21)) are divided into several types such as function-based classifers (e.g., Support Vector Machine (Joachims [1999](#page-15-5)) and neural network), tree-based classifers (e.g., J48 (Quinlan [1993\)](#page-16-19) and random forest (Leo [2001](#page-15-22)), distance-based classifers (e.g., k-nearest neighbour (Cover and Hart [1967\)](#page-15-16), and Bayesian classifers. All available classifers have advantages and disadvantages. For example, Support Vector Machine (SVM) (Joachims [1999\)](#page-15-5) is a great classifer that gives the best performance for binary class problem. But it frequently performs poorly when applied to imbalanced datasets.

Mitchell [\(1997](#page-15-4)) describes cons of learning methods. Overftting, caused by random noise in the training data is a significant practical difficulty in decision tree learning.

Ensembles are considered in our work due to their better accuracy over single classifers (Polikar [2006](#page-16-6)). Experts consisting of a group of different classifers offer corresponding information regarding the patterns which improves the effcacy of the overall classifcation method (Tiago et al. [2014\)](#page-15-23). The tests are conducted on ten benchmark datasets from UCI machine leaning repository (Frank and Asuncion [2010\)](#page-15-24) using ensemble techniques such as Bagging (Breiman [1996](#page-15-25)), Stacking (Dzeroski and Zenko [2004\)](#page-15-26), AdaBoost (Polikar [2006](#page-16-6)), and LogitBoost (Friedman et al. [1998\)](#page-15-27) which are available in WEKA (Mark et al. [2009\)](#page-15-28). AdaBoost and LogitBoost represent two variations of boosting algorithm. LogitBoost is motivated by statistical view (Friedman et al. [1998\)](#page-15-27). Figure [5](#page-6-1) shows percentage classifcation accuracy of the above ensemble techniques. Stacking performs poorly in comparison with the rest of ensemble techniques used. So AdaBoost, Bagging and LogitBoost are considered further for selecting the suitable algorithm.

Table [2](#page-6-2) shows the different classifers, their categories and abbreviations used in the experimental study.

## **3.3 Algorithm**

The following algorithm shows steps in our approarch. Inputs:

K: the number of neighbours

d: data characteristics of new dataset

DC: data characteristics of historical datasets

Output:

Neighbours: the neighbour dataset for new dataset

Alg []: Set of algorithms

Algorithm:



<span id="page-6-1"></span>**Fig. 5** Percentage classifcation accuracies of various ensembles used

<span id="page-6-2"></span>**Table 2** Classifers from diffent types used in experimentation

Sr.	Classifier	Type	Abbrev.
1	Naïve Bayes	<b>Bayes</b>	NB
2	IBK	Lazy	IΒ
3	J48	Tree	J4
4	Adaboost	Meta	AD
5	Logitboost	Meta	LO
6	PART	Rules	<b>PA</b>
7	<b>Random Forest</b>	Tree	RF
8	<b>Bagging</b>	Meta	BA
9	<b>SMO</b>	<b>Functions</b>	<b>SM</b>

- 1.  $i = 1$ ;<br>2 For ea
- 2. For each  $D \in DC$  do<br>3. Distance Table [i] =
- Distance Table $[i]$  = the distance between d and D i.e. |d-D|
- 4.  $i = i+1$ ;<br>5. Ordering
- 5. Ordering Distance Table in ascending order
- 6. Neighbours  $=$  top K datasets of distance Table
- 7.  $j = 0$ ;
- 8. For each  $i < K$  do
- 9. Alg[j] =  $D_j$ 's Best Algorithm.

## <span id="page-6-0"></span>**4 Experimental study and results**

#### **4.1 Classifcation measures**

Confusion Matrix (Han and Kamber [2011\)](#page-15-21) is used for analyzing performance of classifer. i.e., it indicates how accurate classifcation is performed. Table [3](#page-7-0) shows confusion matrix that contains information about actual and predicted classifcations for a classifer system.

*Accuracy* Accuracy indicates how a measured value is close to its actual or true value.

<span id="page-7-0"></span>**Table 3** Confusion matrix

Predicted class					
Actual class	Yes	No	Total		
Yes	TP	FN	P		
No	FP	TN	N		
Total	$\mathbf{p}$	N'	$P+N$		

*TP* true positive, *FN* false negative, *FP* false positive, *TN* true negative

*Precision* Precision indicates how close the measured values are to each other.

*Recall* Recall is used to measure fraction of relevant instances that are retrieved.

Evaluation measures are calculated as shown in Table [4](#page-7-1) by using confusion matrix from Table [3](#page-7-0). Accuracy, error rate, precison and recall are the commonly used evaluation measures in classifcation. Out of the above classifcation measures, the focus of this paper is on accuracy.

Learner or classifer algorithm selection is a multidecision optimization problem. It is part of multi-objective model type selection problem (Rosales-Perez et al. [2014](#page-16-20)). Model selection involves both the selection of learning algorithms and choice of hyper-parameters for a given algorithm. Fine tuning of hyper-parameters can affect the generalization capability of learning algorithms. More than one classifer measures can play an important role in learner recommendation as the problem changes. EI-Hefnawy [\(2014](#page-15-29)) suggests a modifed particle swarm optimizer (MPSO) to solve fuzzy bi-level single and multi-objective problems. In this approach the bi-level programming problem (BLPP) handles as fuzzy multi-objective problem. The present work has restriction that only classifcation accuracy is used. But this limitation will be removed in the extension of work, where the authors are working with other classifcation measures such as classifer testing time, complexity and comprehensibility of learning algorithm.

## **4.2 Datasets**

Saitta and Neri ([1998\)](#page-16-21) have shown that supervised learning algorithms are used in various application domains. For

<span id="page-7-1"></span>**Table 4** Evaluation measures

Measure	Formula
Accuracy, recognition rate	$(TP + TN)/(P + N)$
Error rate, misclassification rate	$(FP + FN)/(P + N)$
Sensitivity, true positive rate	TP/P
Specificity, true negative rate	TN/N
Precision	$TP/(TP + FP)$

the purpose of the present study, we have used 38 benchmark data sets from the University of California at Irvine Machine Learning Repository (Frank and Asuncion [2010](#page-15-24)). These datasets are from: medical diagnosis (breast-cancer, hypothyroid, etc.), pattern recognition (anneal, iris, etc.), image recognition (ionosphere, segment, etc.), commodity trading (credit-a, labor, etc.) and various control applications (balance).

Table [5](#page-8-0) shows the datasets with the important data characteristics or meta-features. The datasets used in the experimental work are having instances of 10 to 3772. The number of classes for them varies from 2 to 24. The number of symbolic attributes varies from 0 to 69. The number of numeric attributes varies from 0 to 60. That means the total number of features or dimensionality of the datasets is from 4 to 69. Entropy in Table [5](#page-8-0) is calculated using Eq. [3.](#page-5-2) Entropy is an information theoretic meta-feature.

## **4.3 Experimental set‑up**

The system is developed in Java language. All 38 datasets are having attribute relation fle format (ARFF). Metafeatures in Table [1](#page-5-1) are calculated. We have used nine classifers provided by Weka (Witten et al. [2005\)](#page-16-7) as shown in Table [2.](#page-6-2) Weka is a set of machine learning algorithms used for data mining. In this work, the parameters of all the classifers are kept as default.

#### **4.4 Accuracy evaluation and paired** *t* **test**

Table [6](#page-10-0) describes the results evolved by the learner recommendation system. Actual accuracy is calculated using Weka (Witten et al. [2005](#page-16-7)). Pred1 accur. is the first predicted accuracy by the system. Similarly the second and the third recommendations are denoted as Pred2 accur. and Pred3 accur. Finally the best recommended accuracy is decided and its respective classifer is recommended. Difference is the term used to denote the difference between actual and recommended best classifer. It is used for further analysis.

Cross-validation (Hall et al. [2004\)](#page-15-30) is "a model validation technique for evaluating how the results of a statistical analysis will generalize to an independent dataset". It is used in prediction and to assess how a predictive model works in practice.

Cross-validation involves partitioning of original dataset into training and testing datasets. A model developed in training phase is validated using testing dataset. There are different types of cross-validation, such as exhaustive cross-validation, leave-p-out cross-validation, k-fold cross validation, etc. K-fold cross-validation is used in the experimental work. Here k is 10. So it is called tenfold crossvalidation (Hall et al. [2004](#page-15-30)). It works as follows:

• Data is divided into 10 sets of size n/10.

<span id="page-8-0"></span>



- 9 datasets are used for training and testing is done on 1.
- The above process is repeated 10 times and a mean accuracy is taken.

Cross-validation is used to compare the performances of the different predictive modelling performances. Using cross-validation, the two different learners or classifers are compared objectively. The performance measure used in the empirical work for the comparison is the classifcation accuracy.

A general method used for comparing supervised learning algorithms involves carrying out statistical comparisons of the accuracies of trained classifers on specifc datasets (Bouck aert [2003\)](#page-15-31). Dietterich ([1998](#page-15-32)) and Nadeau and Bengio ([2003\)](#page-16-22) explain several versions of the *t* test to solve this problem. So we use tenfold cross-validation paired *t* test for comparing the classifers. Microsoft Excel is used to calculate paired *t* test.

Table [7](#page-11-0) shows classifier accuracies of Bagging classifer, SMO classifer and their differences for 38 bench mark datasets from UCI machine learning repository. This table is used to calculate results as shown in Tables [8](#page-11-1) and [9](#page-12-0) for paired *t* test for statistical comparison of the classifers.

A paired *t* test was performed to determine if the classi fers' accuracy was signifcantly different.

The mean of difference of classifers' accuracy  $(M = -4.45, SD = 13.38, N = 38)$  was significantly less than zero,  $t(37) = -1.82$ , two-tail  $p = 0.047$ , providing evidence that the two classifers are differing in accuracy. A 95 % C. I. about mean accuracy is  $(-6.88, 0.37)$ . The above sample results are shown for comparing two classi fers namely Bagging & Sequential Minimal Optimization (SMO) classifer. SMO is the classifer available in WEKA (Mark et al. [2009\)](#page-15-28) for support vector machine.

Figure [6](#page-12-1) shows difference between actual and best of predicted 3 classifers. Figure [7](#page-12-2) describes the difference between actual and predicted best. As shown in Figs. [6](#page-12-1) and [7](#page-12-2), datasets 23 and 25 show more difference between actual and predicted accuracy and all others have almost best prediction.

The dataset 23 is Iris which is from the pattern recognition domain. The dataset 25 is Lympotherapy which is from medical diagnosis domain. They are having 150 and 148 number of instances, respectively. Also, they have 3 and 4 classes, respectively. These may be the reasons of more difference in predicted accuracies and actual accuracies for datasets 23 and 25. As shown in Fig. [7,](#page-12-2) there are very few datasets where difference is signifcant.

As shown in Fig. [8](#page-12-3), the number of objects on the line and below line indicate predicted accuracy is equal or greater than actual accuracy. Many of the objects are on or close to line so our approach recommends algorithm almost accurately.

<span id="page-10-0"></span>**Table 6** Evaluation database consisting of actual and predicted accuracies



# **4.5 Results of KNN approach**

We have done many tests using different combinations of data characteristics which are listed as below:

- 1. KNN where  $K = 1$  with different groupings
- 2. KNN where  $K = 3$  with different groupings of metafeatures
- 3. KNN where  $K = 3$  with different groupings of metafeatures and normalized values

In Fig. [9](#page-13-1), first 8 entries are using  $K = 1$  without normalization. First best 3 classifers of the same dataset that are found similar for a new dataset are used for evaluation. 9 to 13 entries in the Fig. [9](#page-13-1) are for  $K = 3$  without normalization and 14 onwards entries are for  $K = 3$  with normalization.

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<span id="page-11-0"></span>**Table 7** Classifer accuracies of Bagging classifer, SMO classifer and their differences

BA	<b>SMO</b>	Difference
98.83	97.46	1.37
76.43	80.77	$-4.34$
83.40	87.57	$-4.17$
69.59	67.52	2.07
95.79	96.75	$-0.96$
41.95	66.69	$-24.74$
41.95	66.94	–24.99
91.98	93.62	$-1.64$
84.88	82.66	2.22
85.28	84.88	0.40
73.97	75.09	$-1.12$
60.80	81.41	$-20.61$
76.08	76.8	$-0.72$
83.58	83.48	0.10
35.58	59.36	$-23.78$
72.22	57.36	14.86
80.52	83.86	$-3.34$
79.86	82.74	$-2.88$
81.04	83.89	$-2.85$
80.98	85.77	$-4.79$
99.54	93.58	5.96
91.37	88.07	3.30
94.33	96.27	$-1.94$
82.66	92.97	$-10.31$
96.82	86.48	10.34
96.61	92.92	3.69
98.73	93.87	4.86
76.27	76.6	$-0.33$
87.00	93.1	$-6.1$
92.50	95.63	$-3.13$
91.33	98.33	$-7.00$
60.00	66.00	$-6.00$
36.00	70.00	$-34$
72.66	74.08	$-1.42$
95.74	95.77	$-0.03$
86.96	70.61	16.35
64.00	54.00	10.00
42.49	96.08	$-53.59$

Figure [10](#page-14-0) shows different combinations of meta-features with normalization and predicted  $1<sup>st</sup>$  best classifiers difference over 38 datasets. It is observed that combination of normalized meta-features NV-3-4-5-16-17 gives better recommendation; so we use this combination for recommendation of classifer.

<span id="page-11-1"></span>**Table 8** *T* test paired two samples for means



Prefx NV is used before different combinations of metafeatures in the Figs. [9](#page-13-1) and [10.](#page-14-0) It shows that normalized values of the meta-features are used. Min–max normalization is used for reducing impact of large values of some metafeatures on accuracy of recommendation. E.g. There are two datasets namely Hypothyroid and Sick in UCI machine learning repository (Frank and Asuncion [2010\)](#page-15-24) having 3772 instances each. If we use the number of instances as a meta-feature then it will dominate the other meta-features. Hence normalization of such meta-feature value is required that helps to increase accuracy in recommendation. We have normalized values in the range of 0-1.

Thus the meta-features namely, the number of attributes, the number of instances, the number of classes, the maximum probability of class and the class entropy play a signifcant role in classifer accuracy and algorithm selection for 38 datasets and 9 classifers used in our research work.

Locally weighted regression (Alpaydin [2010\)](#page-15-33) is used to fnd the effect of the above meta-features on classifer accuracy. Locally weighted regression (Cleveland and Devlin [1988](#page-15-34)) is "a way of estimating a regression surface through a multivariate smoothing procedure, ftting a function of the independent variables locally and in a moving fashion analogous to how a moving average is computed for a time series". Figure [11](#page-14-1) shows actual accuracy, predicted accuracy and the accuracy calculated using linear weighted regression as per the approximation function in Eq. [5](#page-11-2) for 38 datasets.

Accuracy =  $90.84153 + 0.00436 \times$  number of instances

 $+ 0.4331 \times$  number of classes

 $+ 0.024926 \times$  number of attributes

 $-3.68516 \times$  entropy

− 6.14672 × maximum probability of class

<span id="page-11-2"></span>(5)

<span id="page-12-0"></span>





<span id="page-12-3"></span>**Fig. 8** Actual Vs best predicted classifer accuracy



Dataset\_ID

<span id="page-12-2"></span>

<span id="page-12-1"></span>**Fig. 6** Dataset Vs actual and the frst three predicted classi-

fiers accuracy



If we fnd out difference of accuracy using regression and actual accuracy for each dataset and take the average of 38 datasets it comes as −0.0016. This shows that our method correctly predicts the best accuracy on a new dataset.

# <span id="page-13-0"></span>**5 Conclusion and future work**

The paper proposes algorithm selection for classifcation problems in data mining. We fnd out meta-features of datasets and the performance of classifers. K-similar datasets are returned based on the similiarity between a new dataset and historical datasets. We recommend the best classifcation algorithm for the given problem. Hence the user saves time for testing different learning algorithms, fne tuning the parameters for different algorithms.

k plays a signifcant role in the performance of the k-NN algorithm. In our system, k used is dynamic, so a nonexpert can choose k.

Our algorithm selection method selects the best classifer based on accuracy as a performance measure with aim for helping non-experts in selecting algorithm. The experiment shows that predicted and actual accuracies match closely for 76 % of 38 benchmark datasets.

Three different categories of meta-features or data characteristics such as simple, statistical, and information theoretic are used and comparatively evaluated. Experiments on meta-features suggest the essential features such as the number of attributes,the number of instances, the number of classes, maximum probability of class, class entropy for classifer selection. These meta-features play a signifcant role in classifer accuracy and recommendation of the best algorithm for 38 benchmark datasets and 9 different classifers used in our empirical work.

The empirical work uses 38 datasets from UCI machine learning repository. But still there is a need to extend the work to include more number of datasets as well as more number of algorithms. The framework which can suggest more number of meta-features is also required. The authors are extending the work to include another type of meta-features called as landmarking features to improve predictive accuracy. Rough sets is helpful for removing redundant meta-features and reducing time required for computation of meta-features. Also there is a demand for research in optimization of the parameters used for the different classifers. There is necessity of more research for fne tuning of hyper-parameters of the different learners. Genetic algorithms and grid search techniques can play a major role in the above optimization.

Classifcation algorithms or learners may perform differently according to the context. Changing classifcation algorithm with dynamic interpretation of sensor data will be need of hour. The algorithm's quality in terms of accuracy and elapsed time can be enhanced by using the context-aware selection of classifer (Kwon and Sim [2013](#page-15-35)). Context-aware selection of classifcation algorithms is an important topic for pursuing further research. This method also provides core logics to expert systems which consider the characteristics of original dataset and current context for selecting optimal classifcation algorithms.



Attribute\_wise\_Results

<span id="page-13-1"></span>**Fig. 9** Combination of meta-features Vs average difference

<span id="page-14-0"></span>



Iris Lymph Sick soybean tic-tac-toe Trains Vote weather

hypothyroid

heart-statlog

<span id="page-14-1"></span>

This study does not consider data streams. So there is a scope for research in making decisions for extracting metafeatures for dynamically changing data. Also intelligent data analysis of Big data in a business intelligence era and formulation of a meta-learning framework in the context of Big data are very hot research topics and require more research efforts.

 $\overline{0}$ 

Anneal balance-scale breast-w

balance-scale

bridges\_version2

bridges\_version2

Colic credit-g diabetes Flags heart-c heart-statlog hypothyroid

 $20$ 

40

60

80

100

120

# **6 Discussion**

Our proposed work shows one approach for algorithm selection in data mining using meta-learning.

The major contributions of the work can be listed as below:

• The Data Characterization Tool for extracting simple, statistical and information-theoretic features is developed.

ic-tac-toe

- Experiments are performed on 38 benchmark datasets, nine classifes are used from different types and three data characterization methods or meta-features are used for experimentation. The experimental work shows that for 76 % datasets, the predicted and actual accuracies closely match. Hence the algorithm selection or recommendation is correct for these datasets. One approach for adaptive learning is proposed and implemented.
- Min–max normalization is used for reducing impact of large values on accuracy of recommendation. Two datasets from UCI machine learning repository (Frank and Asuncion 2010) namely, hypothyroid and sick with

actual accur Pred Acc **Regression acc**  3772 instances each are used to explain the need of normalization. Meta-learning approach has not used normalization that improves accuracy of recommendation. But our approach uses normalization.

• Our work shows that the number of attributes, the number of instances, number of classes, maximum probabilityof class and class entropy are the major data characteristics or meta-features impacting classifer accuracy and algorithm selection. The average error of 38 datasets which is calculated using difference between accuracy from regression and actual accuracy is −0.0016. So it shows that our prediction about the above five meta-features affecting classifcation accuracy as a performance measure of learner is correct. We have contributed in formulating Eq. [5](#page-11-2) which gives approximation function for modelling the classifer accuracy.

Thus new proposed equation of fnding classifer accuracy based on meta-features is formulated and validated.

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