



Time series prediction of seasonal precipitation in Iran, using data-driven models: a comparison under different climatic conditions

Pouya Aghelpour¹ · Vijay P. Singh² · Vahid Varshavian¹

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Abstract

Seasonal total precipitation is one of the important meteorological variables and its prediction is useful for the supply of water to different sectors. This study aims to compare Seasonal Autoregressive Integrated Moving Average (SARIMA), Multilayer Perceptron (MLP), Adaptive Neuro-Fuzzy Inference System-Subtractive Clustering (ANFIS-SC), and ANFIS-Fuzzy Cluster Means (ANFIS-FCM) for the prediction of seasonal precipitation. The precipitation data were obtained for the 1951–2018 period from 8 stations located in different climatic zones of Iran. The stations and their climates are Anzali (per-humid moderate climate), Babolsar (humid moderate climate), Kermanshah (semi-arid cold climate), Shiraz (semi-arid moderate climate), Bushehr (arid warm climate), Shahroud (arid cold climate), Isfahan (extra-arid cold climate), and Zahedan (extra-arid moderate climate). The time-lagged precipitation as input for all models was chosen using the autocorrelation function (ACF), and the data were divided into two periods: 1951–2001 for training (75%) and 2002–2018 for testing (25%). Based on the evaluation criteria (root mean squared error [RMSE], normalized root mean squared error [NRMSE], Wilmott Index [WI], Akaike Information Criterion [AIC], and Bayesian Information Criterion [BIC]), results showed that the SARIMA stochastic model was more accurate than the artificial intelligence methods and had the least over- and under-estimations. MLs exhibited good prediction accuracy, but ANFIS-FCM had a little higher accuracy. Consequently, due to the high accuracy and simplicity, the stochastic model is reported as the best predictor for seasonal precipitation in all climates. In terms of the R^2 values, the models showed better fitting in wet and normal years than in drought years. Further, the model predictions were more accurate in per-humid and humid areas than in arid and extra-arid climates. Also, the NRMSE values were in the range of 0.1 and 0.2, which indicated that SARIMA's performance was medium and well. A significant result of this study was that results for different climates based on RMSE were completely opposite to those based on NRMSE, WI, and R^2 . This contrast was caused by the neglect of data range in the RMSE equation, so it is not a good choice to compare the results under different climates and it is better to use its normalized form "NRMSE."

Keywords Seasonal precipitation · ANFIS-FCM · Normalized RMSE · Time series prediction · SARIMA · Stochastic models

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✉ Vahid Varshavian
v.varshavian@basu.ac.ir

Pouya Aghelpour
aghelpour_p68@yahoo.com

Vijay P. Singh
vsingh@tamu.edu

¹ Department of Water Science and Engineering, Faculty of Agriculture, Bu-Ali Sina University, Hamedan, Iran

² Department of Biological and Agricultural Engineering & Zachry Department of Civil & Environmental Engineering, Texas A&M University, 321 Scoates Hall, 2117 TAMU, College Station, TX 77843-2117, USA

Introduction

Precipitation experiences monthly and seasonal variation. Along with temperature, it is one of the major factors essential for climate classification and for assessing climate change and its consequences. It is the source of surface water, subsurface water, groundwater, lakes and reservoirs, and Cryospheric water. Precipitation directly or indirectly affects all aspects of human life, and therefore, its prediction is of fundamental significance.

Time series models have long been used for prediction, in hydrological and meteorological sciences (Aghelpour and Varshavian 2020; Aghelpour et al. 2019; Pandey et al. 2019; Dabral and Murry 2017; Yan

and Ma 2016; Valipour et al. 2013). Tran Anh et al. (2019) used ARIMA to predict monthly precipitation in Vietnam. Wang et al. (2013) employed SARIMA for predicting monthly precipitation in Shouguang, China. Bari et al. (2015) and Mahmud et al. (2016) evaluated SARIMA for predicting monthly precipitation in Bangladesh. Several studies have reported on the accuracy of precipitation prediction by time series models at different scales: annual scale (Nyatuame and Agodzo 2018), monthly scale (Abdul-Aziz et al. 2013; Eni and Adeyeye 2015; Dwivedi et al. 2019; Wang et al. 2014), and daily scale (Nanda et al. 2013), but not at the seasonal scale.

In recent years, machine Learning (ML) models have also been used for meteorological and hydrological predictions (Mohammadi et al. 2020; Moazenzadeh and Mohammadi 2019; Aghelpour et al. 2019; Abbasi et al. 2019; Moazenzadeh et al. 2018). For example, MLP and ANFIS have been used to predict wind speed (Maroufpoor et al. 2019; Deo et al. 2018); river flow (Aghelpour and Varshavian 2020; Poul et al. 2019; Parsaie et al. 2019); meteorological, hydrological, and agricultural drought indices (Aghelpour et al. 2020a; Aghelpour et al. 2020c; Malik et al. 2019; Kisi et al. 2019; Maca and Pech 2016); solar radiation (Jahani and Mohammadi 2018; Halabi et al. 2018; Khosravi et al. 2018); snow cover area (Aghelpour et al. 2020b); and monthly precipitation (Ghamariadyan et al. 2019; Tran Anh et al. 2019; Dwivedi et al. 2019; Nanda et al. 2013). Total seasonal precipitation has been predicted using ANFIS and MLP in Australia (Hossain et al. 2020; Mekanik et al. 2016; Mekanik et al. 2013), and total monthly precipitation in South Korea (Lee et al. 2018). In these predictions, time lags of teleconnection climatic signals, such as El Niño Southern Oscillation (ENSO), Indian Ocean Dipole (IOD), or East Atlantic Pattern (EA), were used as model input but the accuracy of MLs was not compared with time series models. Studies show that if climatic signals are not available, both ML and time series-based models can do precipitation prediction. Therefore, the current research aims to use and compare some of these numerical models in predicting seasonal precipitation, without teleconnection climatic signals. Also, literature survey shows that the time series prediction of total seasonal precipitation does not seem to have been done for any type of Iranian climate. Therefore, this study addresses this issue in different climate regions of Iran (from per-humid to extra-arid areas), using time series, stochastic models, and artificial intelligence models and compare these model types under similar input conditions. Also, the impact of climate type on the prediction accuracy of seasonal precipitation by different models is investigated.

Materials and methods

Study area

Iran has considerable climatic diversity, ranging from per-humid climates of Caspian Sea's south side and semi-arid regions of the Zagros mountains to arid and extra-arid regions in central, south, and southeast parts. Based on the Extended De-Martonne classification method (Rahimi et al. 2013), Iran has all 28 climatic classes from which 8 stations were selected. These stations were selected because they have the longest records, are spread out countrywide, and have the maximum differences between their climate classes in terms of temperature and humidity. Stations' locations are shown in Fig. 1.

Data

Total monthly precipitation data for the period of 1951–2018 was obtained from Iran Meteorological Organization (IRIMO). Seasonal (3 months) precipitation was calculated by summing monthly precipitation corresponding to each season, thus yielding 4-season data sets. The characteristics of the stations and their precipitation data are shown in Table 1.

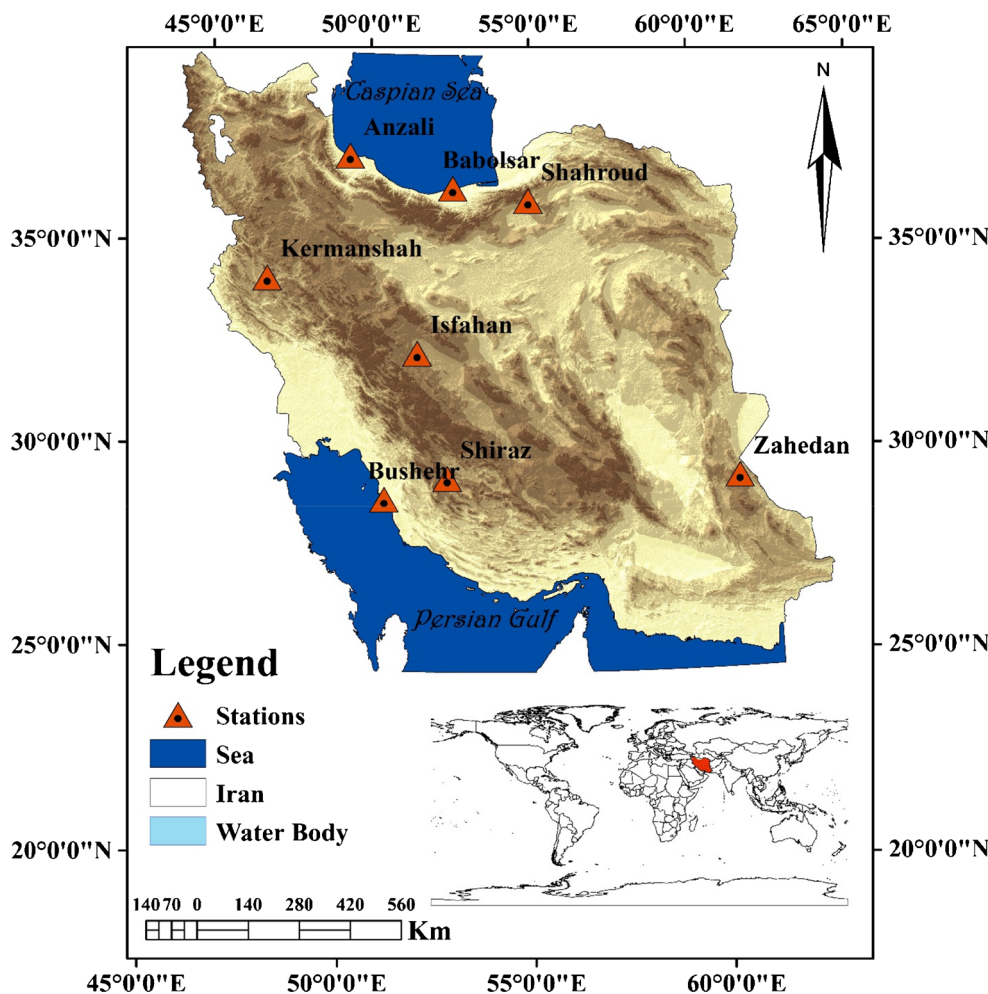
The input for predictive models constituted time-lagged seasonal precipitation, which was selected using the autocorrelation function (ACF). Then, the data were divided into two parts: 75% (including first 51 years) for the training of models and 25% (last 17 years) for testing.

Time series models

The time series model refers to a model commonly used to measure time-based data. An observed time series is considered to be one realization of a stochastic process. The simplest model proposed for simulating the time series consists of a process in which the events have been taking place at different times and at constant intervals; each event is independent of other values (Salas et al. 1988). Time series models are based on calibrated regression coefficients, multiplied by the time lags of the original series. In these models, inputs are the time lags of the original series and the coefficients are optimized by the least squares (LS) algorithm.

The basic types of these models are Autoregressive (AR) and Moving Average (MA) and the rest of the models originate from these two models, such as Autoregressive Moving Average (ARMA) and Autoregressive Integrated Moving Average (ARIMA). If there is a seasonal trend in the data, seasonal variants of time series models, such as PARMA (Periodic ARMA) and SARIMA (Seasonal ARIMA), can be used (Salas et al. 1988). This study used the seasonal SARIMA model. This model, which is mainly used to simulate the stochastic behavior in seasonal time series, is a linear parametric stochastic model which is denoted by

Fig. 1 Stations' position in Iran



SARIMA(p,d,q)×(P,D,Q)_ω, where ω denotes the periodicity of the series; p, d, q, show the non-seasonal degrees of AR, Integrated & MA and P, D, and Q show the seasonal degrees of AR, Integrated & MA. A general relationship can be expressed as below:

$$\Phi_P(B^\omega) = (1 - \phi_1 B^{\omega \times 1} - \dots - \phi_P B^{\omega \times P}) \tag{1}$$

$$\phi_p(B) = (1 - \phi_1 B^1 - \dots - \phi_p B^p) \tag{2}$$

$$\nabla_\omega^D = (1 - B^\omega)^D \tag{3}$$

$$\nabla^d = (1 - B)^d \tag{4}$$

$$\Theta_Q(B^\omega) = (1 - \theta_1 B^{\omega \times 1} - \dots - \theta_Q B^{\omega \times Q}) \tag{5}$$

$$\theta_q(B) = (1 - \theta_1 B^1 - \dots - \theta_q B^q) \tag{6}$$

$$\Phi_P(B^\omega) \phi_p(B) \nabla_\omega^D \nabla^d X_t = \theta_q(B) \Theta_Q(B^\omega) \varepsilon_t \tag{7}$$

Here, X_t stands for the stochastic variable and ε_t is a normal random variable with mean μ and variance σ_ε^2 . Moreover, parameters B , Φ , ϕ , ∇_ω^D and ∇^d , Θ , θ represent the backward operators of seasonal autoregressive, non-seasonal autoregressive, seasonal differencing and non-seasonal

differencing, seasonal moving average, and non-seasonal moving average, respectively (Salas et al. 1988).

Multilayer Perceptron

The concept of perceptron was first introduced by McCulloch and Pitts in (1943) as an artificial neuron. A Multilayer Perceptron (MLP) network provides a nonlinear relationship between input and output vectors which is accomplished by connecting neurons from one layer to another (previous or next layer). The output of each neuron is multiplied by weight coefficients and given as input to a nonlinear excitation function. In the training phase, the training data are given to perceptron, then the grid weights are adjusted to minimize the error between the target and the output of the model, or to reach the number of training times to the default value. Then, different inputs (which were not present in the training phase) are used for model validation. The training of these neural networks can be stated as an optimization problem with a large number of variables (Rumellhart 1986). For further information details, one can refer to Rumellhart 1986;

Table 1 Stations' climate and coordinates with the statistics of seasonal precipitation data

Station	Climate	Latitude (°)	Longitude (°)	Altitude (m)	Period	Mean (mm)	Std. ^(a) (mm)	Min. (mm)	Max. (mm)	Skew. ^(b)
Anzali	Per humid-Moderate	37.47	49.47	− 26.2	Train	467.40	329.60	32.8	1790.3	1.30
					Test	439.50	292.90	54.6	1168.3	0.78
Babolsar	Humid-Moderate	36.72	52.65	− 21.0	Train	220.10	144.30	7.5	674.5	0.90
					Test	227.90	178.50	7.4	1017.5	1.74
Kermanshah	Semi arid-Cold	34.35	47.15	1318.6	Train	111.82	96.76	0.0	494.8	0.81
					Test	101.05	82.90	0.0	269.4	0.29
Shiraz	Semi arid-Moderate	29.53	52.60	1484.0	Train	85.40	100.45	0.0	473.1	1.37
					Test	72.00	82.50	0.0	333.8	1.32
Bushehr	Arid-Warm	28.98	50.83	19.6	Train	68.76	96.28	0.0	686	2.39
					Test	56.71	77.21	0.0	319.5	1.51
Shahroud	Arid-Cold	36.42	54.95	1345.3	Train	38.44	32.93	0.0	155.3	1.01
					Test	35.26	23.80	0.0	92.9	0.43
Isfahan	Extra arid-Cold	32.62	51.67	1550.4	Train	29.97	31.18	0.0	218.2	1.82
					Test	34.77	31.84	0.0	121.4	0.86
Zahedan	Extra arid-Moderate	29.47	60.88	1370.0	Train	22.93	29.23	0.0	156.7	1.76
					Test	16.92	22.46	0.0	86.3	1.51

^a Std standard deviation

^b Skew skewness

Haykin 1999; Jahani and Mohammadi 2018; and Aghelpour and Varshavian 2020.

Adaptive Neuro-Fuzzy Inference System

Adaptive Neuro-Fuzzy Inference System (ANFIS) is a model that uses a neural network learning algorithm and fuzzy logic for designing nonlinear maps between input and output spaces. The model is capable of learning through the neural network and defining and using the relationships between input and output variables by fuzzy rules and subsequently creating the input structure of the system. ANFIS uses a variety of methods for fuzzy clustering, the strongest of which is known as Subtractive Clustering (SC) and Fuzzy Cluster Means (FCM). In this study, these two methods are used for ANFIS clustering to provide ANFIS-SC and ANFIS-FCM. These clustering methods are described below.

Subtractive Clustering

The subtractive clustering method assumes that each data point is a potential cluster center and calculates a measure of the likelihood that each data point would define the cluster center on the basis of the density of surrounding data points. Considering a set of n data points $\{x_1, x_2, \dots, x_i\}$ in m -dimensional space, it is assumed that all data points within a cubic space have been normalized. In subtractive clustering,

each of the data points is considered as a potential cluster center (Kisi et al. 2018). As a result, the density index D_i corresponding to the data x_i can be expressed as:

$$D_i = \sum_{j=1}^n \exp\left(-\frac{\|x_i - x_j\|}{\left(\frac{r_a}{2}\right)^2}\right) \quad (8)$$

Here, r_a is a positive quantity called cluster radius. If many data points are adjacent to a data point, then that data point has the maximum density. After measuring the density of each data point, data point with the highest density is selected as the first data center clustering (Kisi et al. 2018; Hiremath et al. 2012). If the effect of a limited area of the center of the first cluster center is removed, the following formula can be used to measure the density of other points.

$$D_i = D_i - D_{c1} \sum_{j=1}^n \exp\left(-\frac{\|x_i - x_{c1}\|^2}{\left(\frac{r_b}{2}\right)^2}\right) \quad (9)$$

Here, x_{c1} and D_{c1} are the selected points and density potential, respectively, and r_b is a positive constant. To avoid approaching the cluster centers, the r_b constant value is normally larger than r_a (r_b is considered $1.5r_a$). After measuring the density for each data point, the next cluster center x_{c2} is selected and the measured density for all data points will be recalculated. This process continues until a sufficient number of cluster centers produce (Kisi et al. 2018; Kisi et al. 2014; Aqil et al. 2007).

Fuzzy Cluster Means

In fuzzy clustering, each pattern might belong to several clusters or segments. One of the most functional clustering algorithms is the K-mean algorithm. This unsupervised algorithm in large datasets, exposed with some limitations in the process, may not work properly. To deal with this disadvantage, different clustering algorithms have been proposed. Among them, a fuzzy cluster means, as a proper alternative method, is used (Kisi et al. 2018; Kisi and Zounemat-Kermani 2016). Fuzzy cluster means was developed by Dunn (1973), and Bezdek (2013) improved it.

The Fuzzy Cluster Means (FCM) method blocks a set of N vector $x_i, i = 1, \dots, N$, into c fuzzy clusters, where each pattern corresponds to a cluster with a degree specified by a membership grade u_{ij} between 0 and 1. The final object by the FCM algorithm is to find c cluster centers so that the cost function of the dissimilarity measure can be minimized. The aim is minimizing the objective function that is defined as below:

$$Min J_{FCM} = \sum_{c=1}^C \sum_{i=1}^N w_{ic}^p \|w_i - v_c\|^2 \quad s.t. \sum_{c=1}^C w_{ic} = 1, i = 1, 2, \dots, N \tag{10}$$

which p ($1 < p$) is known as fuzzifier portion; N , is the number of data points; C , the number of clusters; w_{ic} , the number of belongings of the i^{th} data point to the c^{th} cluster; v_c is the cluster's center; and x is the number of the input for calculating the amount of w_{ic} the following formula is used (Kisi et al. 2018; Bezdek et al. 1984):

$$w_{ic} = \frac{1}{\sum_{L=1}^C \left(\frac{d_{ic}^2}{d_{ij}^2}\right)^{\frac{1}{p-1}}} \quad \text{for } i = 1, 2, \dots, N \text{ and } c = 1, 2, \dots, C \tag{11}$$

For the beginning of the center vectors, centers are calculated by:

$$v_c = \frac{\sum_{j=1}^N w_{jc}^p x_j}{\sum_{j=1}^N w_{jc}^p} \tag{12}$$

FCM procession continues until a convergence condition is achieved.

Measuring prediction accuracy

In the current study, seven criteria were used for evaluating the prediction accuracy: root mean squared error (RMSE), normalized root mean squared error (NRMSE), mean absolute

error (MAE), Wilmott Index (WI), coefficient of determination (R^2), Akaike Information Criterion (AIC), and Schwarz Bayesian Information Criterion (BIC) were as follows:

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (y_i - f_i)^2} \tag{13}$$

$$NRMSE = \frac{RMSE}{\text{Maximum}_{y_i} - \text{Minimum}_{y_i}} \tag{14}$$

$$MAE = \frac{1}{n} \sum_{i=1}^n |y_i - f_i| \tag{15}$$

$$WI = 1 - \frac{\sum_{i=1}^n (y_i - f_i)^2}{\sum_{i=1}^n (|f_i - \bar{y}| + |y_i - \bar{y}|)^2} \tag{16}$$

$$R^2 = \left[\frac{\sum_{i=1}^n (y_i - \bar{y})(f_i - \bar{f})}{\sqrt{\sum_{i=1}^n (y_i - \bar{y})^2} * \sqrt{\sum_{i=1}^n (f_i - \bar{f})^2}} \right]^2 \tag{17}$$

$$AIC = n \ln \left(\frac{\sum_{i=1}^n (y_i - f_i)^2}{n} \right) + 2p \tag{18}$$

$$BIC = n \ln \left(\frac{\sum_{i=1}^n (y_i - f_i)^2}{n} \right) + p \ln(n) \tag{19}$$

Here, y_i is the observed precipitation; \bar{y} is the average value of observed precipitation; f_i is the predicted precipitation; \bar{f} is the average value of predicted precipitation; n is the count of data; and p is the number of model parameters. Prediction results will be better if the values of RMSE, NRMSE, and MAE were close to 0, and the values of WI and R^2 were close to 1. Also, the smaller AIC and BIC values show the better performance of the model.

The Minitab software was used to implement the time series model, and MATLAB software was used to implement the MLP and ANFIS models. Graphs were made by software Excel and Minitab.

Results

Results of time series model

To find the appropriate input matrix, the Autocorrelation Function (ACF) was used. Four examples of ACF plots are shown.

Because of the regular crossing of signification lines (at lags of 2, 6, 10, 14, 18... in the negative direction; and at lags

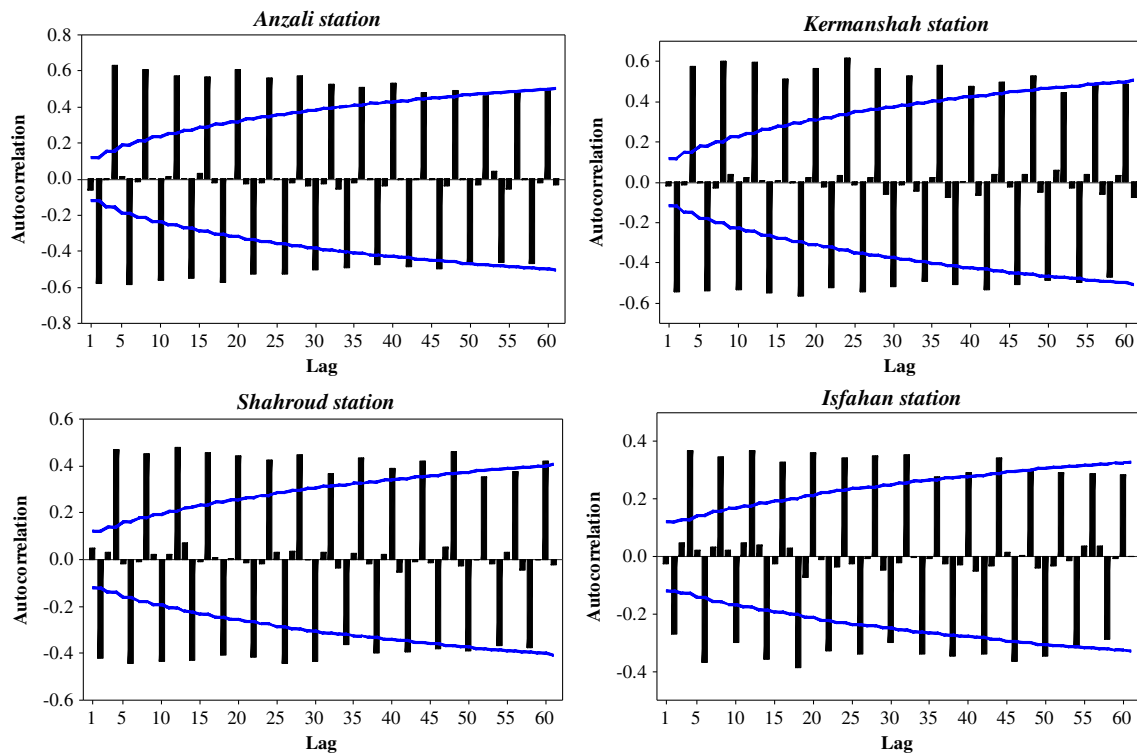


Fig. 2 Samples of ACF plot, for seasonal precipitation data

of 4, 8, 12, 16, 20... in the positive direction) as shown in Fig. 2, it is clear that for all stations, there was a return period of 4 lags (4 seasons). It means there was a seasonal periodic trend among the precipitation data, suggesting that the applicable

model of time series models is the Seasonal Autoregressive Integrated Moving Average (SARIMA) model. The model pattern of $SARIMA(p,d,q)(P,D,Q)_\omega$, was changed to $SARIMA(p,d,q)(P,D,Q)_4$. The seasonal differencing degree

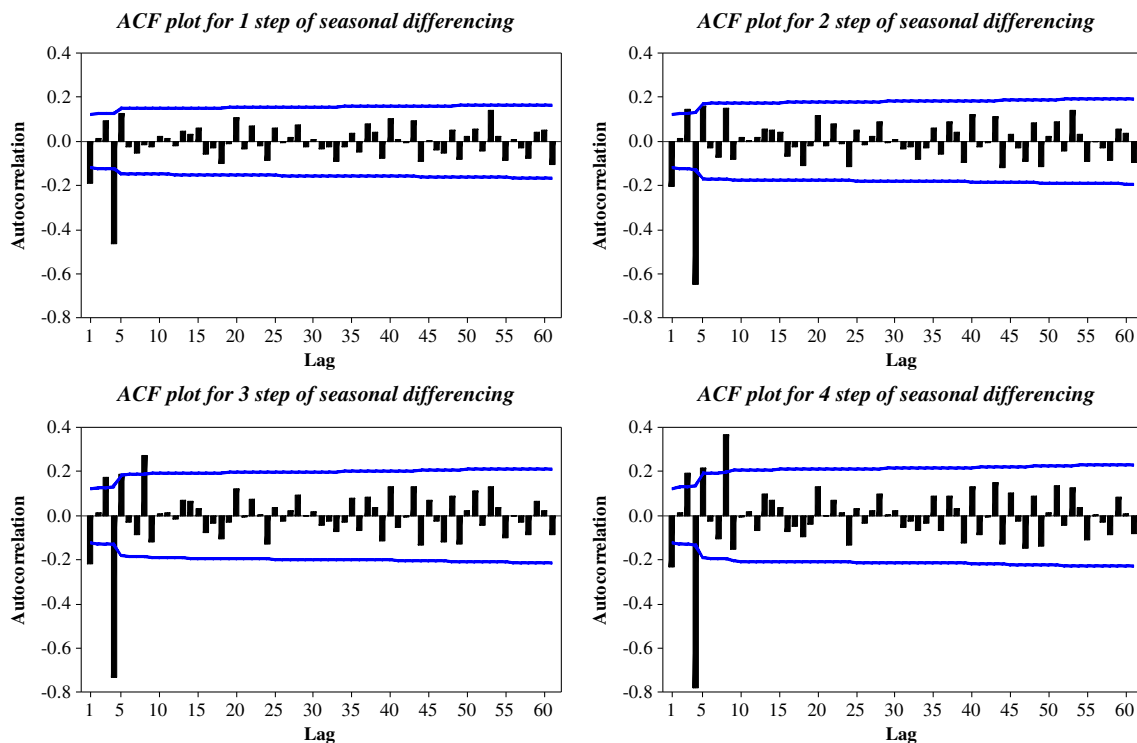


Fig. 3 Changes of ACF by four steps of seasonal differencing (Anzali station)

of this pattern (D) was determined by differencing the data with lag equal to the return period (lag = 4). As an example, for Anzali station, it was done four times, as shown in Fig. 3.

The figure shows that the crossing of signification lines increased with an increasing seasonal differencing degree. For example, in $D = 1$ (ACF plot for 1 step of seasonal differencing), there were two lags out of the significance level, in $D = 2$, $D = 3$, and $D = 4$, the number of crossed lags were 3, 4, and 5, respectively. Thus, the least crossing belonged to the differencing degree of 1 and the model pattern changed to SARIMA(p,d,q)(P,1,Q)₄. To determine the other degrees of seasonal and non-seasonal Autoregressive and Moving average (p, q, P and Q), a trial and error approach was used. The degrees were examined among 0 to 5 for each station, and the best one(s) were evaluated by the evaluation criteria (Table 2).

For some of the stations (including Anzali, Kermanshah, Shiraz, and Bushehr), the best SARIMA model was clear, so the single best model is shown in Table 2 for these stations. For other stations (including Babolsar, Shahroud, and Isfahan), more than one SARIMA model was fitted. In the test period for Babolsar, models SARIMA(1,0,5)(0,1,2)₄ and SARIMA(2,0,5)(1,1,1)₄ were the best models and there was just a little difference between their 2nd and 3rd decimal places, but according to the principle of parsimony (Salas et al. 1988), the model SARIMA(1,0,5)(0,1,2)₄ should be chosen, because of its fewer parameters. By this principle, the chosen models for Shahroud, Isfahan, and Zahedan were SARIMA(0,0,5)(0,1,0)₄, SARIMA(0,0,4)(0,1,2)₄, and SARIMA(0,0,4)(0,1,4)₄, respectively. The lowest prediction error of SARIMA belonged to Zahedan Station, which is located in an extra-arid moderate region; with RMSE = 17.726 mm per season, NRMSE = 0.205, WI = 0.743, AIC

= 399.007, and BIC = 407.885. The highest prediction error belonged to Anzali station in the per-humid moderate area, with RMSE = 156.394 mm per season, NRMSE = 0.140, WI = 0.911, AIC = 695.705, and BIC = 704.597.

Results of ML models

For the selection of input for the ML models (MLP, ANFIS-SC, and ANFIS-FCM), ACF was used. To make a logical comparison between the time series and ML models, inputs should be similar. From the ACF plots (Fig. 2), the even time lags of seasonal precipitation had significant autocorrelations, so the time lags 2, 4, 6, 8, 10, 12, 14, 16, 18, and 20 were used as input for the ML models. The models were implemented and the evaluation results are shown in Table 3.

For the ML prediction, the models were calibrated for their parameters. For the MLP model, the parameters were the number of hidden layers, the number of neurons in each hidden layer, and the type of transfer function; for ANFIS-SC, the only parameter was the cluster’s radius; for ANFIS-FCM, the only parameter was the number of clusters, which were optimized by trial and error. Results showed that the ML model had a close accuracy in predicting seasonal precipitation. The least error was due to the ANFIS-FCM model with clusters = 2 for Zahedan station with RMSE = 20.045 mm per season, NRMSE = 0.232, WI = 0.676, AIC = 415.722, and BIC = 424.600. The highest prediction error of ML models was for ANFIS-SC with a cluster radius = 0.55, which was for Anzali station with RMSE = 172.456 mm per season, NRMSE = 0.155, WI = 0.899, AIC = 708.419, and BIC = 717.297.

Table 2 Assessment of SARIMA model (The bold rows show the best prediction performance of each station)

Station	Model	Train					Test				
		NRMSE	RMSE	WI	AIC	BIC	NRMSE	RMSE	WI	AIC	BIC
Anzali	SARIMA(1,0,4)(1,1,2)₄	0.117	205.915	0.866	2138.890	2152.362	0.140	156.394	0.911	695.705	704.597
Babolsar	SARIMA(1,0,5)(0,1,2)₄	0.122	81.451	0.896	1768.511	1781.695	0.107	108.395	0.867	645.086	654.560
	SARIMA(2,0,5)(1,1,1) ₄	0.122	81.413	0.895	1768.683	1781.855	0.107	108.438	0.866	645.508	654.917
Kermanshah	SARIMA(0,0,4)(3,1,2)₄	0.124	61.237	0.857	1653.900	1667.093	0.179	48.134	0.896	534.861	543.739
Shiraz	SARIMA(0,0,5)(0,1,2)₄	0.141	66.725	0.831	1688.233	1701.426	0.173	57.660	0.844	559.420	568.298
Bushehr	SARIMA(5,0,0)(0,1,4)₄	0.100	68.847	0.796	1700.753	1713.946	0.166	53.054	0.835	548.098	556.976
Shahroud	SARIMA(0,0,5)(0,1,0)₄	0.157	24.399	0.769	1285.811	1299.005	0.196	18.220	0.818	402.743	411.621
	SARIMA(1,0,3)(0,1,3) ₄	0.156	24.186	0.791	1282.310	1295.503	0.202	18.757	0.818	406.694	415.572
Isfahan	SARIMA(0,0,4)(0,1,2)₄	0.115	24.998	0.690	1295.521	1308.714	0.202	24.572	0.744	443.418	452.296
	SARIMA(0,0,5)(0,1,2) ₄	0.114	24.962	0.690	1294.947	1308.141	0.202	24.500	0.740	443.018	451.896
Zahedan	SARIMA(0,0,4)(0,1,4)₄	0.127	19.920	0.840	1200.696	1217.889	0.205	17.726	0.743	399.007	407.885
	SARIMA(0,0,4)(1,1,4) ₄	0.126	19.708	0.843	1200.417	1213.611	0.208	17.924	0.740	400.512	409.390
	SARIMA(0,0,5)(0,1,0) ₄	0.129	20.290	0.824	1212.056	1225.249	0.208	17.986	0.740	410.983	419.861

Table 3 Assessment of machine learning models (The bold rows show the best prediction performance of each station)

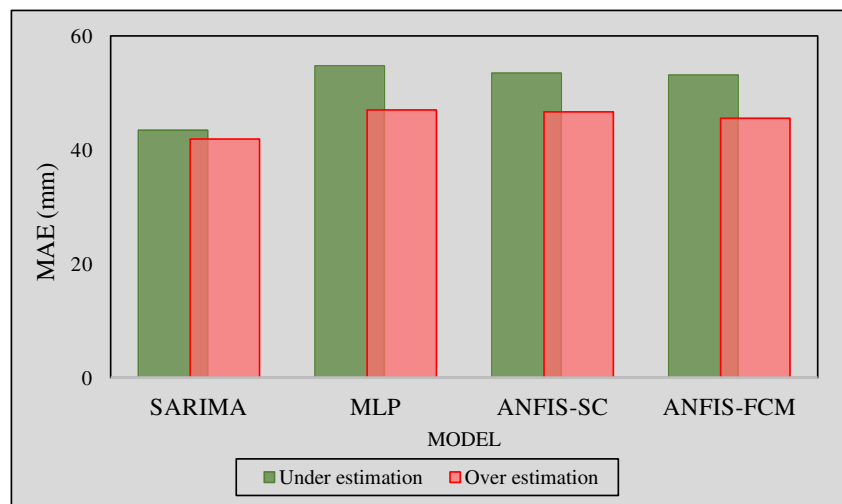
Station	Model	Parameter(s)	Train					Test				
			NRMSE	RMSE	WI	AIC	BIC	NRMSE	RMSE	WI	AIC	BIC
Anzali	<i>MLP</i>	10-1, satlin ^(a)	0.113	198.515	0.880	1955.039	1967.898	0.153	170.683	0.895	707.013	715.891
	<i>ANFIS-SC</i>	0.55 ^(b)	0.115	201.348	0.878	1960.253	1973.113	0.155	172.456	0.899	708.419	717.297
	<i>ANFIS-FCM</i>	2 ^(c)	0.123	215.621	0.853	1985.456	1998.316	0.149	166.280	0.903	703.459	712.338
Babolsar	<i>MLP</i>	6-4-1, tansig	0.123	81.987	0.899	1629.613	1642.472	0.119	119.727	0.822	658.788	667.666
	<i>ANFIS-SC</i>	0.65	0.117	78.005	0.912	1611.294	1624.154	0.119	120.138	0.828	659.254	668.132
	<i>ANFIS-FCM</i>	2	0.127	84.441	0.893	1640.467	1653.327	0.116	117.483	0.840	656.215	665.093
Kermanshah	<i>MLP</i>	8-1, tansig	0.123	60.826	0.873	1519.750	1532.610	0.258	69.387	0.786	584.598	593.476
	<i>ANFIS-SC</i>	0.68	0.120	59.314	0.881	1510.484	1523.343	0.259	69.907	0.808	585.614	594.492
	<i>ANFIS-FCM</i>	2	0.120	59.153	0.882	1509.488	1522.348	0.248	66.789	0.805	579.409	588.287
Shiraz	<i>MLP</i>	6-1, satlin	0.127	60.009	0.875	1514.775	1527.634	0.202	67.582	0.790	581.014	589.892
	<i>ANFIS-SC</i>	0.71	0.123	58.010	0.886	1502.308	1515.168	0.192	64.254	0.827	574.146	583.024
	<i>ANFIS-FCM</i>	3	0.129	60.952	0.870	1520.514	1533.374	0.191	63.719	0.821	573.009	581.887
Bushehr	<i>MLP</i>	10-6-1, satlin	0.073	50.419	0.912	1450.693	1463.552	0.180	57.531	0.816	559.114	567.992
	<i>ANFIS-SC</i>	0.57	0.084	57.590	0.881	1499.634	1512.494	0.186	59.277	0.794	563.181	572.059
	<i>ANFIS-FCM</i>	2	0.085	58.308	0.877	1504.193	1517.053	0.178	56.894	0.813	557.602	566.480
Shahroud	<i>MLP</i>	5-1, tansig	0.139	21.537	0.859	1137.682	1150.542	0.264	24.499	0.677	443.012	451.890
	<i>ANFIS-SC</i>	0.84	0.142	22.026	0.851	1145.937	1158.797	0.255	23.687	0.708	438.428	447.306
	<i>ANFIS-FCM</i>	3	0.150	23.369	0.824	1167.712	1180.572	0.245	22.777	0.737	433.104	441.982
Isfahan	<i>MLP</i>	12-1, satlin	0.153	19.117	0.830	1093.807	1106.667	0.216	26.164	0.703	451.956	460.834
	<i>ANFIS-SC</i>	0.78	0.156	19.518	0.821	1101.453	1114.313	0.221	26.787	0.730	455.155	464.033
	<i>ANFIS-FCM</i>	2	0.167	20.848	0.780	1125.714	1138.573	0.210	25.519	0.750	448.562	457.440
Zahedan	<i>MLP</i>	6-3-1, satlin	0.130	20.394	0.786	1117.611	1130.471	0.247	21.278	0.614	423.841	432.719
	<i>ANFIS-SC</i>	0.66	0.122	19.124	0.823	1093.952	1106.812	0.259	22.372	0.587	430.664	439.542
	<i>ANFIS-FCM</i>	2	0.124	19.452	0.814	1100.204	1113.064	0.232	20.045	0.676	415.722	424.600

^a In the Parameter(s) column, MLP’s parameters are the number of the hidden layers, number of the neurons in hidden layers, and the type of the transfer function. For example 10-1, satlin means there is one hidden layer in makeup of MLP model, with 10 neurons in the hidden layer and the transfer function is “satlin.” In 10-1, satlin, “1” shows the number of neurons in output layer, which must be equal 1 with “purelin” transfer function

^b ANFIS-SC’s parameter is cluster’s radius

^c ANFIS-FCM’s parameter is number of the clusters

Fig. 4 Investigating under and over estimation of the models, using MAE



Comparison between models

Models were compared by their mean absolute error (MAE) and they were also compared between their under and overestimations (Fig. 4). To draw the graph of Fig. 2, observed precipitation data for all of the stations in the prediction period (test period) were compared with their related predictions made by the models. They were separated for each model and then their MAE was calculated for underestimation and overestimation separately.

Comparison between drought classes

At the first glance, the error of model under-estimation was larger than that of over-estimation. This may be due to the nature of precipitation data, which have irregularity and sudden jumps in their time series and the models cannot usually determine them and usual precipitation occurrences. Among these four models, SARIMA had the lowest MAE in both under-estimation (MAE = 43.45 mm) and over-estimation (MAE = 41.89 mm) and also the difference between under-estimation and over-estimation was the least, so it can be regarded as the best model among other models. It seems that there was not a significant difference between MLs, but according to their MAE, ANFIS-FCM can be selected as the best of MLs (MAE of under-estimation = 53.13 mm, MAE of over-estimation = 45.51 mm), ANFIS-SC the second one (MAE of under estimation = 53.46 mm, MAE of over-estimation = 46.67 mm), and MLP the third one (MAE of underestimation = 54.74 mm, MAE of over-estimation = 47.01 mm), with minor differences.

After determining the best predictor model (known as SARIMA), its accuracy was evaluated in different years from the perspective of meteorological drought classes. For this, the Standardized Precipitation Index (SPI) was used to determine drought classes at the annual scale, and then the years were separated into 3 classes of drought, normal, and wet years. The observed and predicted data of the test period for each station were investigated using the scatter plot (Fig. 5), and the R^2 values were calculated for different drought years separately.

At the first glance, the best correlations for all classes were for Anzali station and the weakest correlations for Isfahan station (because of their fitted regression line's closeness and distance to the 1:1 line and also the R^2 value). For all of the stations, the fitted regression line of the classes "wet" (blue dots) and "normal" (green dots) was located below the 1:1 line, which showed the model under-predicted in these two classes. At stations Anzali, Babolsar, Shiraz, and Bushehr, the fitted regression plots of drought years (shown by the red dots) were completely at the top of 1:1 line and at stations Kermanhah, Shahroud, Isfahan, and Zahedan, half of the drought's regression lines were over and the others were under

the 1:1 line. So, it can be generally regarded that the model over-predicted precipitation in drought years. From the R^2 values, the model's predictions were more correlated with observations in wet and normal years than in drought years.

Comparison under different climatic classes

To compare under different climates, the bar charts (Fig. 6) were constructed to show the prediction errors for all stations.

In Fig. 6, the stations were sorted by their dryness from left (the most humid) to right (the driest), and then the values of 3 criteria of RMSE, NRMSE, and WI were calculated for the test period. In the RMSE bar chart, the prediction error was the highest for Anzali station (about $155 \frac{\text{mm}}{\text{season}}$), which is located in a per humid-moderate climate region (refer to Table 1). With decreasing humidity of the climate, the model error also decreased which showed that the least error occurred in the extra arid-moderate climate region of Zahedan station with about $18 \frac{\text{mm}}{\text{season}}$. But in the NRMSE bar chart, the trend was complete to the contrary. It showed that the least normalized error occurred for humid climate stations and the highest ones for extra arid climate stations. For example, the NRMSE of Anzali and Babolsar were about 14 and 11, respectively; but in continuation, it got its highest values for Isfahan and Zahedan stations (about 20). In conclusion, referring to the third criterion was necessary, WI. The bar chart of WI showed similar results for RMSE. The best prediction belonged to the per humid-moderate climate region of Anzali station with $WI \approx 0.91$. The value of WI reduced for the dry climate area of stations Isfahan and Zahedan with the amount of 0.74 approximately. It can be said that RMSE was not a good criterion to compare different modeling results, because in different climates, it showed opposite results. This issue can also be confirmed by referring to the R^2 values in different climates, as shown in Fig. 5. Also, two samples are shown in Fig. 7 as a time series plot for seeing the model predictions against their observation values for stations Anzali and Isfahan.

Discussion

SARIMA model has not been used to predict seasonal cumulative precipitation so far, so the current study can be compared with monthly predictions. Dabral and Murry (2017) implemented SARIMA for monthly precipitation of Doimukh station in India. They compared SARIMA's prediction and observed data by showing the average data of each month (both observed and predicted) in tabular form (Tables 2 and 3 of this paper). In terms of cumulative annual precipitation, only Anzali station was the closest and most similar to Doimukh station, so Anzali station is discussed.

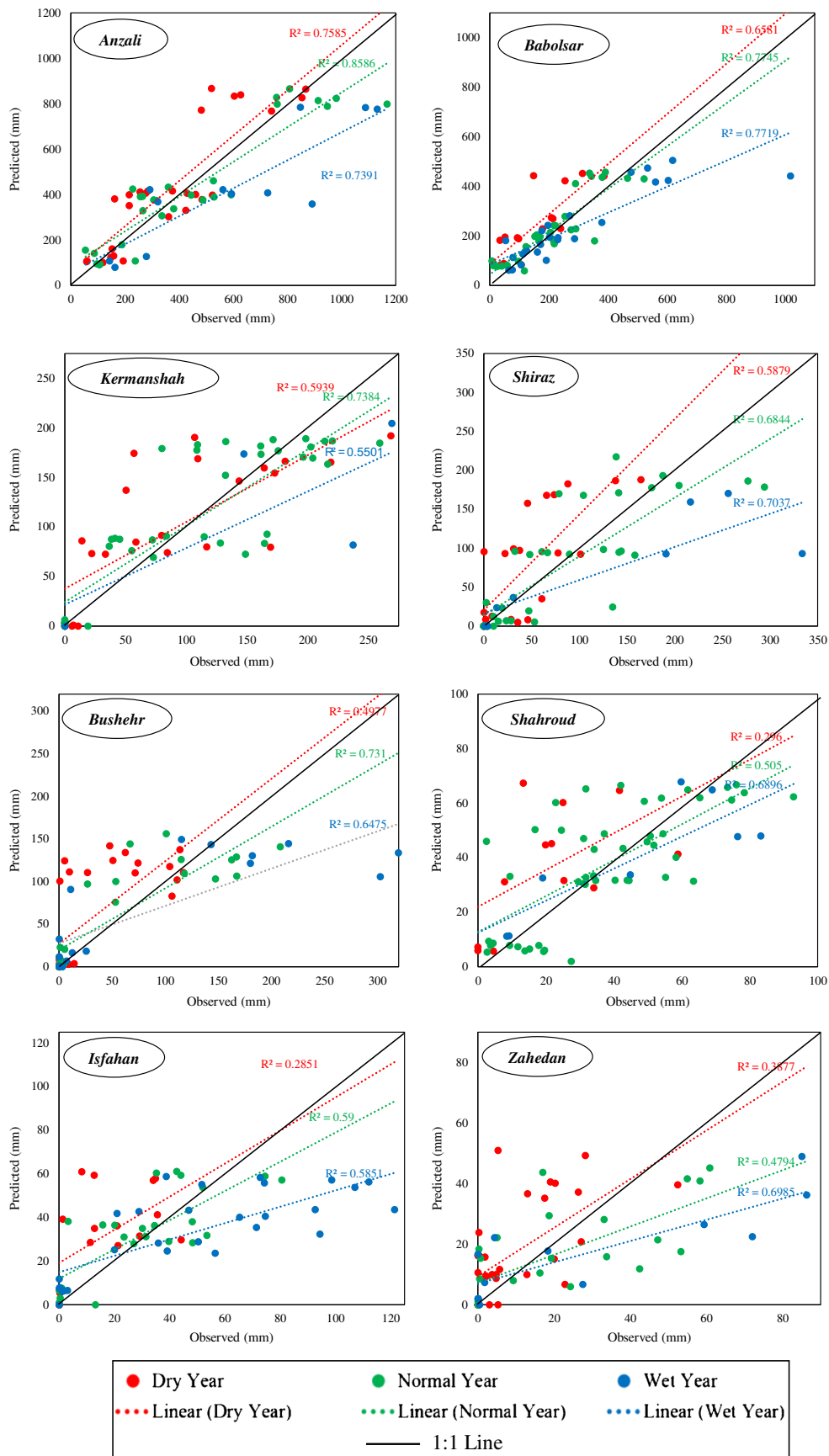


Fig. 5 Regression plots of SARIMA outputs vs observed precipitation data in all stations, for different drought classes

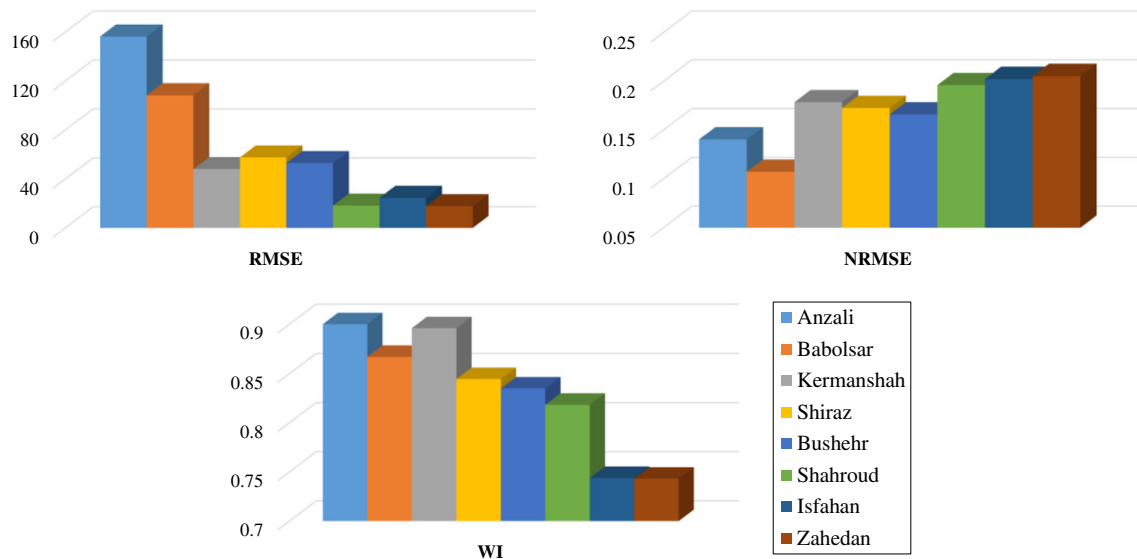


Fig. 6 Comparing the models' accuracy in different climates

The monthly amounts of Tables 2 and 3 from the study of Dabral and Murry (2017) were extracted. Then, their monthly average amounts were changed to seasonal average amounts and were compared with Anzali's seasonal average. The two criteria NRMSE and WI were calculated for these two stations' seasonal average precipitation for comparing with SARIMA's prediction for both training and test periods (shown in Fig. 8). Results showed that SARIMA for Anzali had better results than did Doimukh in both test and training periods. This difference can be due to the climate difference and also the annual precipitation regime. In Iran's climates (especially the cities on the margin of the Caspian Sea, such as Anzali and Babolsar), the most part of annual precipitation occurred in autumn and winter and the least precipitation amounts belonged to summer; while in Indian climates, the peak of precipitation is in monsoon season which occurs in summer. Also, it can result from the return period of SARIMA, 12 for Dabral and Murry's study and 4 for the current study. This shows the current method for SARIMA can yield a better seasonal precipitation prediction, while the NRMSE value of Anzali station (0.032) was about 37% better than Doimokh's (0.044) in the test period. Also, the NRMSE value for Anzali in the training period was 0.023, which was less than half of Doimukh's NRMSE = 0.054, but it can be related to the difference between their statistical periods (in the current research; the data belongs to 68 years but in the mentioned research, it belongs to 26 years). SARIMA has also been reported as a good predictor for the prediction of monthly precipitation in some other studies in Bangladesh (Mahmud et al. 2016), India (Bari et al. 2015), and Nigeria (Eni and Adeyeye 2015) which is in line with the current study. Predicting seasonal precipitation in

Australia using machine learning methods had similar results (Mekanik et al. 2013) and even weaker results (Hossain et al. 2018), in comparison to the current study (according to the available values of R & R^2), with this advantage that they used climatic indexes as predictor inputs. But, an ML model with these inputs cannot be logically compared with the time series model because it just uses lags of the same precipitation data as input.

The difference in error between similar climates can also relate to physical and synoptic reasons. For example, both Anzali and Babolsar stations are located in humid climatic class, but have different prediction results (referring to Fig. 6 and NRMSE criterion). The impact of Siberian high pressure on the eastern part of the Caspian Sea's southern coasts (Babolsar) is more atmospheric stability in the region, while the western coasts of the Caspian Sea (Anzali) are relatively more affected by western systems, such as the Black Sea and the Mediterranean Sea than eastern coasts. Atmospheric instability can cause irregularities in time series, reducing autocorrelation of the series and consequently reducing prediction accuracy in an area such as Anzali compared to Babolsar which despite having a similar climate differs in the prediction accuracy. For semi-arid climatic stations (Kermanshah and Shiraz), differences in prediction accuracy are also observed. Effective systems in the Kermanshah region include low-pressure of Saudi Arabia, low-pressure of Sudan, and Mediterranean fronts that have severe impacts on the atmospheric instability and consequently precipitation of Kermanshah, while southwestern Iran (Shiraz station) can be only affected by weaker-just the two low-pressures of Saudi Arabia and Sudan. In addition, Shiraz's adaptation to the subtropical high-pressure belt may also be another reason for greater atmospheric stability in this area (29.53°

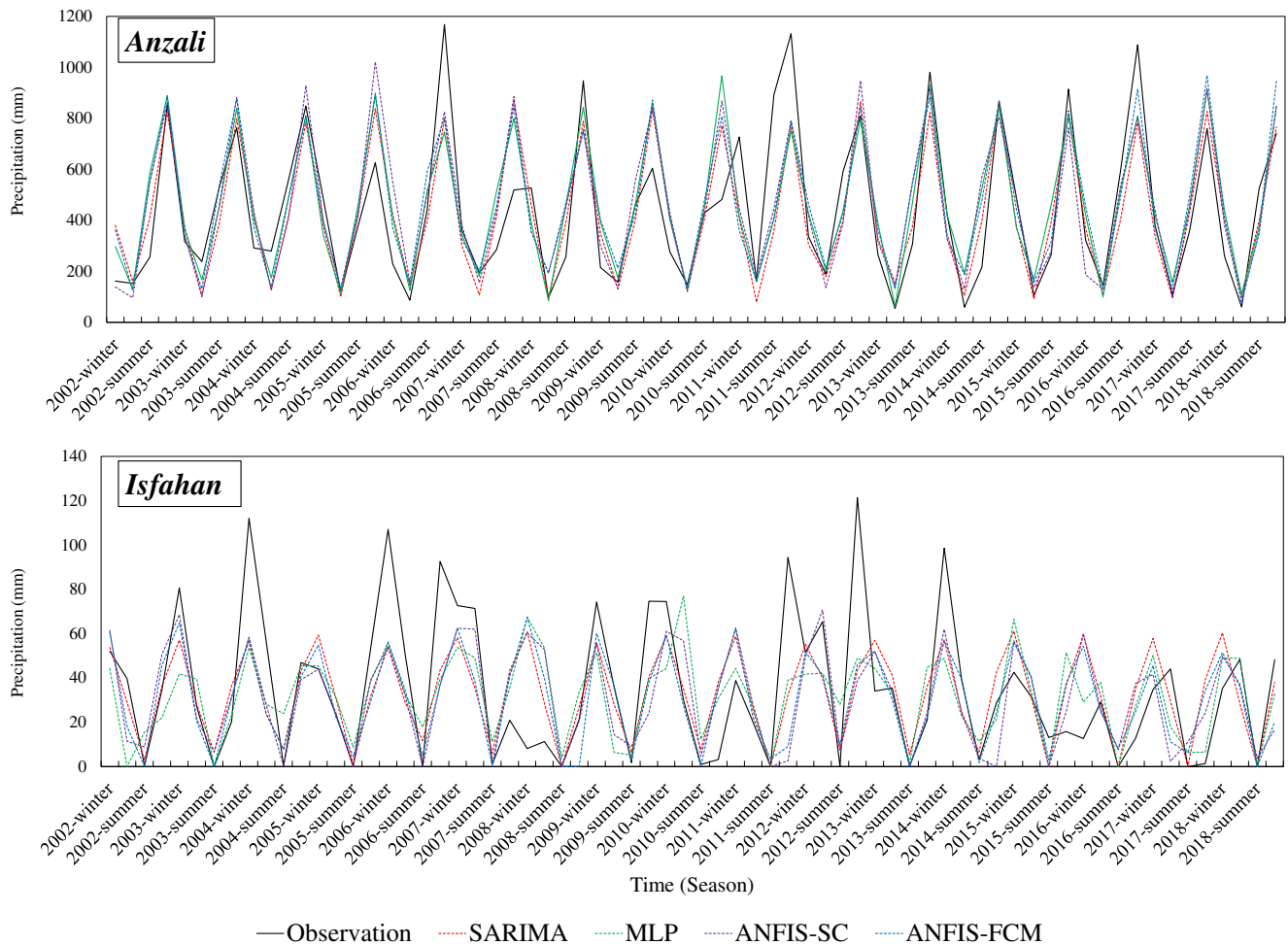


Fig. 7 Time series plot of observation vs output for two samples of the stations

latitude) than in Kermanshah (at 34.35° latitude). This is also true for the difference in prediction accuracy between the two arid climate stations of Bushehr (latitude 29°) and Shahroud (latitude 36.42°), which have provided more accurate predictions in the Bushehr region (Fig. 6 and NRMSE criterion). The difference between the two

stations in the extra-arid climate is much smaller than in the other regions. Trade winds and monsoon systems sometimes affect the Sistan and Baluchestan area (Zahedan station) and cause atmospheric instability in the area, which may be a reason for the poorer prediction accuracy of Zahedan compared to Isfahan.

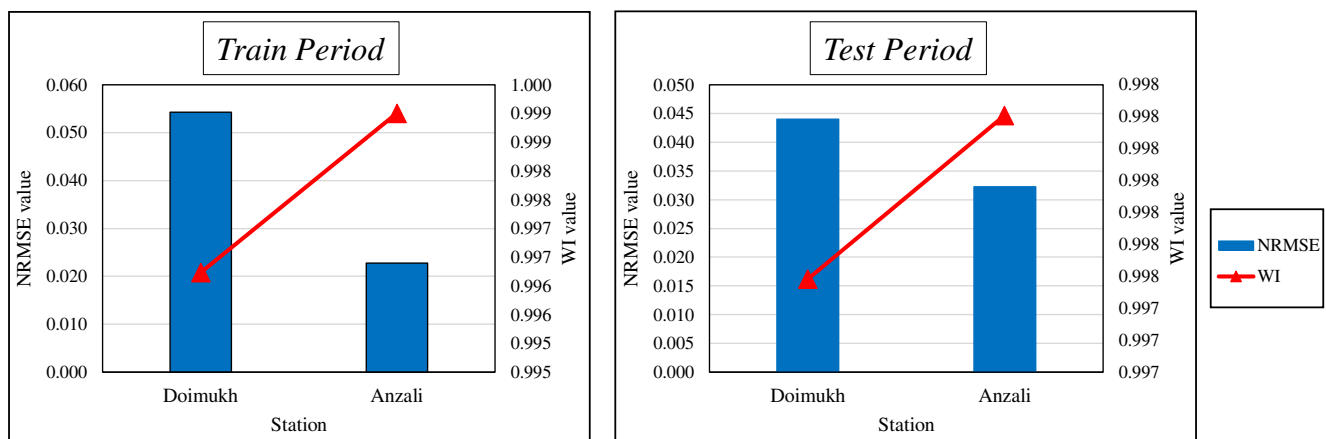


Fig. 8 Comparing the accuracy of SARIMA between Anzali station in this study, and Doimukh station in the study of Dabral and Murry (2017)

Conclusion

It was found that the SARIMA linear model better predicted seasonal precipitation in Iranian climates than did ML models. The linear relation of seasonal precipitation's time lags was stronger than nonlinear relations in such areas. So, SARIMA is recommended for Iran. Among MLs, ANFIS was the best model (especially with the FCM clustering method), which has the least parameter for optimization, while MLP has more parameters for its network's makeup. All of the models predict well in wet and normal years than in drought years. According to the NRMSE value which is in the range of 0.1 to 0.2, SARIMA's performance was not excellent, but it was in good and medium classes, so it has potential for prediction of seasonal precipitation in other areas. Among the regions studied, the per-humid and humid climate regions, such as for Anzali and Babolsar, can have more accurate predictions than the arid and extra-arid climate regions, like for Bushehr, Shahroud, Isfahan, and Zahedan. The significant result is that the evaluation criterion "RMSE" is a good criterion to compare some models for one station, but it cannot be a good criterion for different climate regions. Because RMSE does not consider the variation range of data and in different climates, the variation range of data (especially precipitation data) is highly changeable; it is better to use RMSE's normalized form as "NRMSE." It is suggested to use climatic indexes as predictor inputs for the ML models, and optimize the MLs for precipitation prediction in Iran using complex optimization algorithms to check their efficiency.

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Declarations

Conflict of interest The authors declare that they have no competing interests.

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