



# Development of earthquake early warning system for Kachchh, Gujarat, in India using $\tau_c$ and $P_d$

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## Abstract

Development of earthquake early warning system (EWS) is in advanced stage in different parts of the world including India. The success of EWS for mitigating seismic risk and saving human lives has been well documented in Mexico, Japan, and Taiwan, where the alert is issued to the public. Taking advantage of the recorded ground motion data from the network of Institute of Seismological Research (ISR), India, with magnitude range 3.0–5.2, we investigated correlations between various ground motion parameters like peak ground acceleration (PGA), peak ground velocity (PGV), peak ground displacement (PGD),  $P_a$ ,  $P_v$ ,  $P_d$ , and  $\tau_c$ . Three- to 5-s time windows are considered to measure  $P_a$ ,  $P_v$ ,  $P_d$ , and  $\tau_c$  from the vertical component of the waveforms. Linear regression analysis is performed at various time steps (3- to 5-s time interval). The results show that considering 4- and 5-s windows exhibits good relationships compared with the 3-s window, which shows more scattering. These empirical relationships using  $\tau_c$  and  $M$  as well as  $P_d$  and  $M$  are very helpful in determining the earthquake magnitude and subsequently taking steps toward risk assessment.

**Keywords** Earthquake early warning (EEW) · Institute of Seismological Research (ISR) ·  $P_d$  ·  $\tau_c$  · PGA · PGV · PGD · Seismic risk

## Introduction

The success of earthquake early warning (EEW) for mitigating seismic risk and saving human lives has been well documented in Mexico, Japan, Taiwan, and other parts of the World. EEW is a process in which warning is issued before the arrival of strong ground shaking. Mexico and Japan are providing EEW alerts to the public (Allen et al. 2009; Kamigaichi et al. 2009; Wu et al. 2007). The EEW system of Mexico utilizes peak ground motion (PGM), to issue 60 s or more warning to the public in Mexico City (around 300 km away) from earthquake occurring near the

Guerrero gap subduction zone (Anderson et al. 1995; Espinosa-Aranda et al. 1995). Japan uses more than 4500 instruments for real-time recording of earthquakes as well as for providing a warning (Hoshiba et al. 2008). Depending upon the location of occurrence of the earthquake, the warning time in Japan may range from a few seconds to 40 s. Taiwan provides warning alert to authorities and in recent time to public (Chen et al. 2015; Wu et al. 2016). In Taiwan, the Central Weather Bureau (CWB) is the official agency to issue the warning to authorities as well as the public. CWB uses about 400 instruments for real-time recording as well as issuing warning to the public. On the other hand, the National Taiwan University (NTU) uses a network of about 612 low-cost P-alert sensors for research purpose (Wu et al. 2013; Wu et al. 2019). There are two types of EWS, namely onsite and regional (Kanamori 2005). Onsite warning may be provided using a single station or a small network of stations for one location. In this system, as soon as P-wave is recorded by the sensor, an alarm is generated at site and systems in close proximity may go for auto shutdown like nuclear power plants. A regional warning requires a dense seismic network near the epicentral zone and high-speed communication system, which can transmit the seismic signal within few seconds to Central Recording System (CRS). As seismic waves travel slower than

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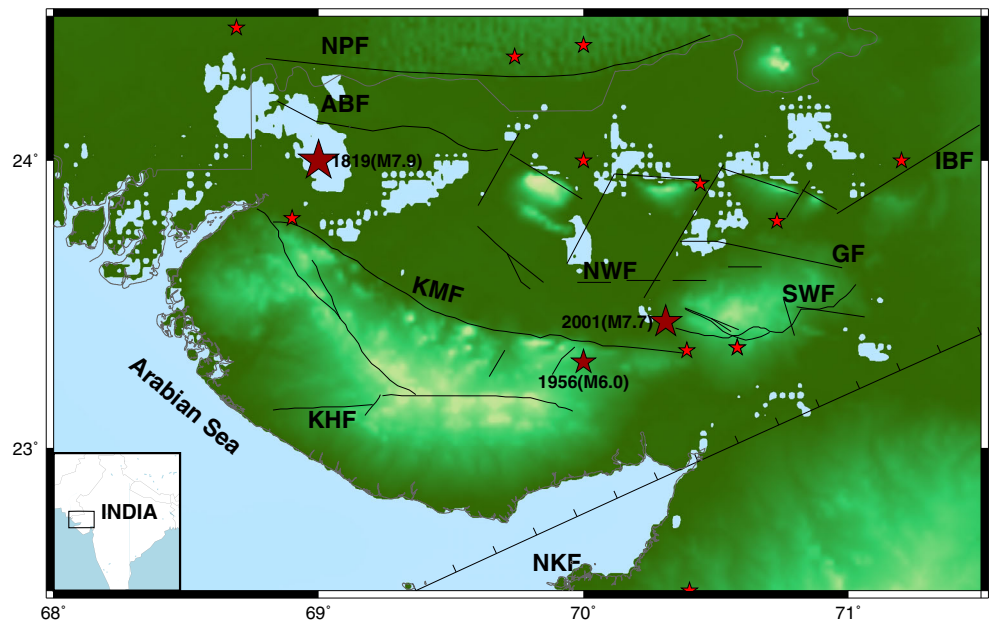
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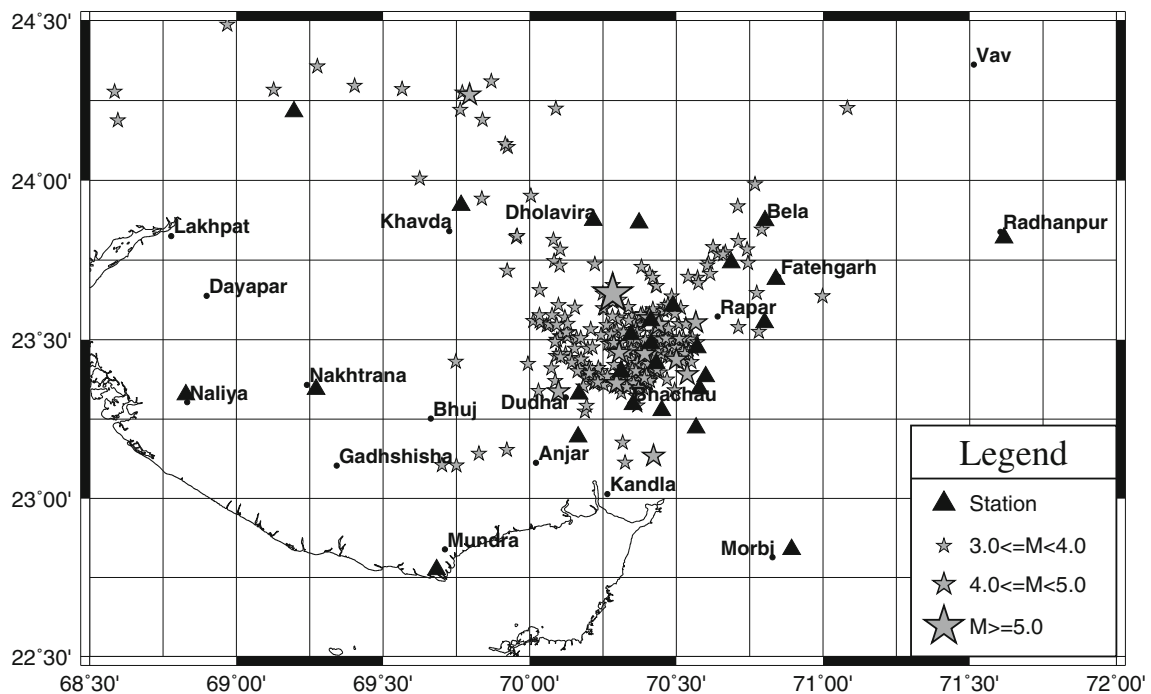
**Fig. 1** Fault map of Kachchh, Gujarat. Major faults Katrol Hill Fault (KHF), Kachchh Mainland Fault (KMF), South Wagad Fault (SWF), Island Belt Fault (IBF), and Nagar Parkar Fault (NPF) are shown. The location of major earthquakes: 1819 Mw 7.8 Allah Bund earthquake and the 2001 Mw 7.7 Bhuj earthquake as well as some of other earthquakes having magnitude  $\geq 6$  are also shown



electromagnetic waves (for communication), using the data of the first few seconds (3–5 s), it is possible to provide the regional warning within 15 s. In general, in an onsite EEW application, a single station can provide warning in regions without a seismic network and maximize warning time at sites close to the epicenter (Lockman and Allen 2005).

In regional EEW, determining earthquake magnitude is one of the crucial aspects, as this can be the sole parameter on the basis of which warning will be issued. However, determining magnitude from the initial few

seconds of the waveform is not straight forward, as fault may be still rupturing. In this context, Wu et al. (1998) used a technique exploiting initial 10 s of signal to relate it with the local magnitude  $M_L$ . In another study, 22 s of signal data are used by Taiwan CWB to determine the earthquake parameters. Since shear waves travel at a speed of 3 km/s, this approach provides early warning for areas beyond 70 km only. Both these two approaches are purely empirical, whereas recent approaches based on peak displacement amplitude ( $P_d$ ) and the characteristic



**Fig. 2** Map showing the location of various earthquakes used in present study and stations recording these earthquakes

period ( $\tau_c$ ) look more appealing. These two parameters estimated from the initial few seconds (3–5 s) after P-wave arrival are used widely for determining whether an earthquake will be damaging or not. A  $P_d$  value larger than 0.5 cm and  $\tau_c$  larger than 1 s are indicators of damaging earthquakes (Wu and Kanamori 2005a, 2008a). In addition,  $P_d$  is supposed to be a better indicator for the intensity of an earthquake than  $\tau_c$  as the latter is more sensitive to the signal to noise ratio (SNR).  $P_d$  is a physical parameter and magnitude estimation using it seems more reasonable. As per Olson and Allen (2005), earthquake magnitude is controlled by the initial stages of the rupture, which justifies the effectiveness of  $P_d$  amplitude theory in EEW.

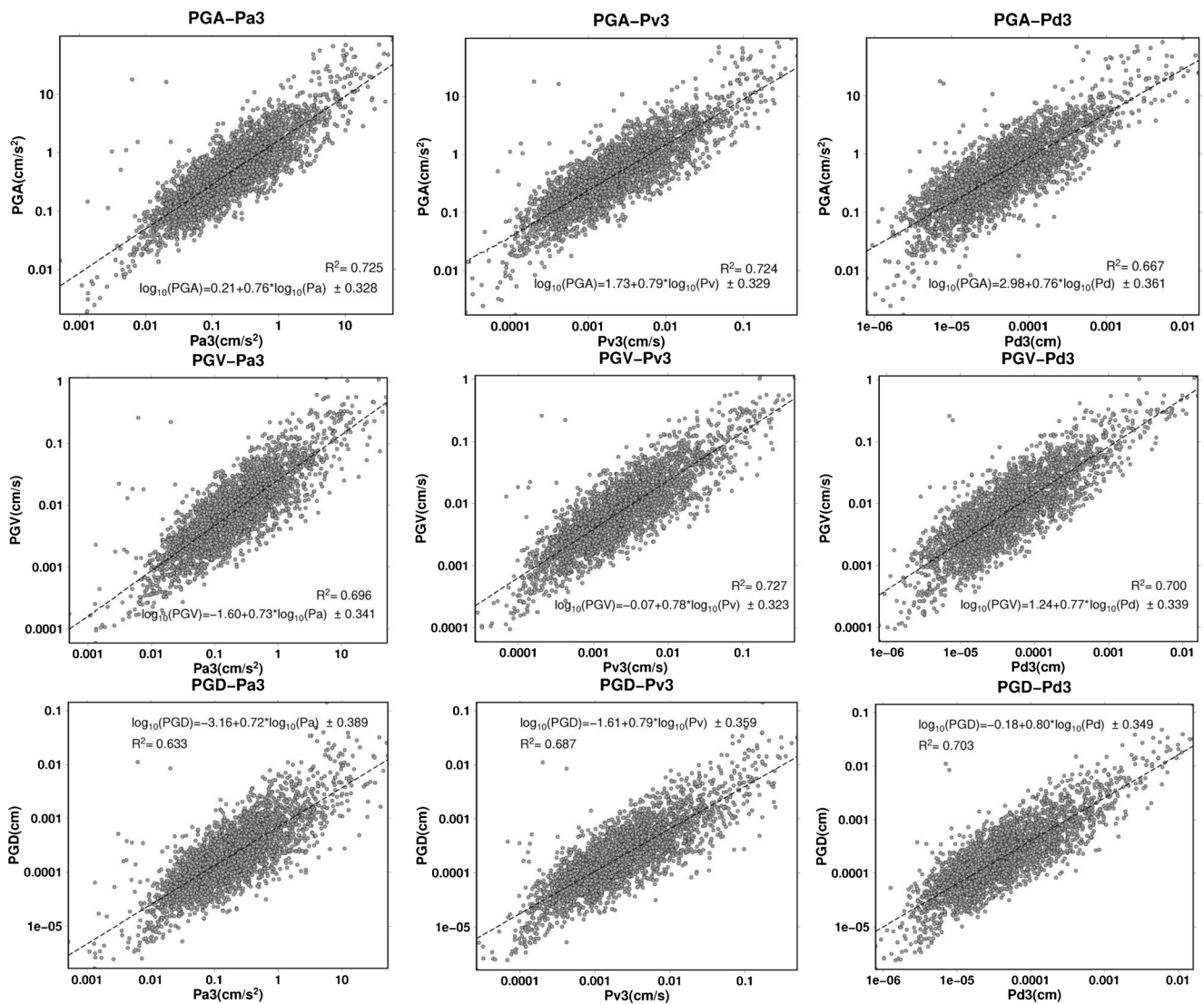
India is at risk of prevalence of high magnitude earthquake from the Himalayas in the north (Mittal et al. 2016a, 2016b) and northeast, Gujarat in west, and Andaman and Nicobar in the southern part of India. Following the probability of occurrence of the devastating earthquake in northern Himalayas, the Indian Institute of Technology, Roorkee (IITR), installed a network of 100 seismic stations for developing EEW system (Kumar et al. 2014). This network was installed based on the performance of strong motion instrumentation network in the Himalayas (Mittal et al. 2006; Kumar et al. 2012). This network is in operation and working perfectly. Despite its operation for the last 4 years, no big earthquake is recorded by this network to test the effectiveness of the network. Mittal et al. (2019a, 2019b) tested the performance of these 100 instruments' network using the recorded earthquakes from Taiwan and synthesized records. They found that in the event of an earthquake in the Himalayas, Delhi (the national capital of India) may have a lead time of 60 s. On the premise of performance of these 100 instruments, IITR is installing 100 additional instruments to have a wide coverage area.

The state of Gujarat is located in the westernmost part of the intraplate region of India. Gujarat being an industrial state is a hub of many petrochemical industries, oil industries, and ports. Gujarat is vulnerable to natural disasters like earthquakes and is of importance owing to increasing population. The Kachchh region of Gujarat has already witnessed two massive damaging earthquakes—1819  $M_w$  7.8 Allah Bund earthquake and the 2001  $M_w$  7.7 Bhuj earthquake within the span of 182 years (Johnston and Kanter 1990; Rastogi 2001). Additionally, the region has also experienced seven other  $M \geq 6.0$  earthquakes (Quittmeyer and Jacob 1979; Rastogi 2001, 2004). The 2001 Bhuj earthquake in Kachchh region caused widespread damage in terms of fatalities and economic loss. The earthquake was so massive that damage was even witnessed in Ahmedabad, 240 km away

**Table 1** Various attenuation relationships between various ground motion parameters for varying time windows (3–5 s)

Regression parameters	Time window	Regression coefficients		
		A	B	C
PGA and $P_a$	3 s	0.21	0.76	0.328
PGA and $P_v$		1.73	0.79	0.329
PGA and $P_d$		2.98	0.76	0.361
PGV and $P_a$		-1.60	0.73	0.341
PGV and $P_v$		-0.07	0.78	0.323
PGV and $P_d$		1.24	0.77	0.339
PGD and $P_a$		-3.16	0.72	0.389
PGD and $P_v$		-1.61	0.79	0.359
PGD and $P_d$		-0.18	0.80	0.349
$\tau_c$ and M		1.42	0.16	0.116
$P_d$ and M	-7.62	1.03	0.404	
PGA and $P_a$	4 s	0.17	0.76	0.305
PGA and $P_v$		1.68	0.78	0.304
PGA and $P_d$		2.93	0.76	0.336
PGV and $P_a$		-1.63	0.73	0.321
PGV and $P_v$		-0.13	0.77	0.301
PGV and $P_d$		1.17	0.77	0.315
PGD and $P_a$		-3.20	0.72	0.374
PGD and $P_v$		-1.68	0.78	0.342
PGD and $P_d$		-0.28	0.79	0.330
$\tau_c$ and M		1.39	0.15	0.116
$P_d$ and M	-7.71	1.08	0.449	
PGA and $P_a$	5 s	0.12	0.75	0.292
PGA and $P_v$		1.62	0.78	0.288
PGA and $P_d$		2.86	0.76	0.318
PGV and $P_a$		-1.68	0.73	0.310
PGV and $P_v$		-0.19	0.77	0.285
PGV and $P_d$		1.10	0.76	0.294
PGD and $P_a$		-3.24	0.72	0.367
PGD and $P_v$		-1.74	0.77	0.331
PGD and $P_d$		-0.36	0.79	0.312
$\tau_c$ and M		1.39	0.15	0.113
$P_d$ and M	-7.70	1.10	0.453	

from the epicenter, causing human lives as well as building collapse. Valuable human lives can be saved if timely earthquake alert is provided and individuals are very much prepared. To monitor the seismic activity and reporting in Gujarat state of India, the Institute of Seismological Research (ISR) in 2006 installed the Gujarat Seismic Network (GSNet) consisting 22 online broadband seismograph (BBS) stations and 40 offline strong motion accelerograph (SMA) (Chopra et al. 2008). Presently, data from 45 seismic stations is coming online via VSAT and 50 more SMAs are proposed to be



**Fig. 3** Empirical relationships between ground motion parameters (PGA, PGV, PGD,  $P_a$ ,  $P_v$ ,  $P_d$ ) for 3-s window after P-wave arrival. Pearson correlation coefficient (regression coefficient) is calculated between

$\log_{10}(\text{PGM})$  and  $\log_{10}(\text{Pm3})$ , where  $M = A$  (acceleration),  $V$  (velocity),  $D$  (displacement) and  $m = a, v, d$ . Finally, a straight line is fitted between  $\log_{10}(\text{PGM})$  and  $\log_{10}(\text{Pm3})$  with standard error

installed in the seismically active region of Kachchh, Gujarat.

Encouraged by the performance and working of EEW in the Himalayas, ISR as a pilot project has begun building the EEW system for urban areas like Ahmedabad from earthquakes originating in Kachchh region. ISR is planning to install a network of EEW instruments in eastern Kachchh region of Gujarat, India. A lot of work has been done to see the applicability of the EEW system for this region. Peak ground acceleration (PGA), peak ground velocity (PGV), and peak ground displacement (PGD) are routinely used parameters to define the strength of shaking. In the present work, several relationships between various parameters like PGA, PGV, PGD,  $P_a$ ,  $P_v$ , and  $P_d$  have been estimated using GSNNet data. The main focus is

kept on estimating  $P_d$  and  $\tau_c$  values, which are crucial in deciding the magnitude of an earthquake and ultimately the severity of an earthquake. These parameters play a key role in issuing the EEW warning.

### Seismotectonics of Kachchh region

Broadly, Gujarat is divided into three divisions, namely Saurashtra, Kachchh, and Mainland Gujarat. Gujarat geology is the outcome of various climatic and igneous activities. Gujarat structure is divided into two parts, namely Precambrian structural trends and Mesozoic structural trends. Precambrian basement is overlain by younger rocks of Jurassic, Cretaceous, Tertiary, and Quaternary



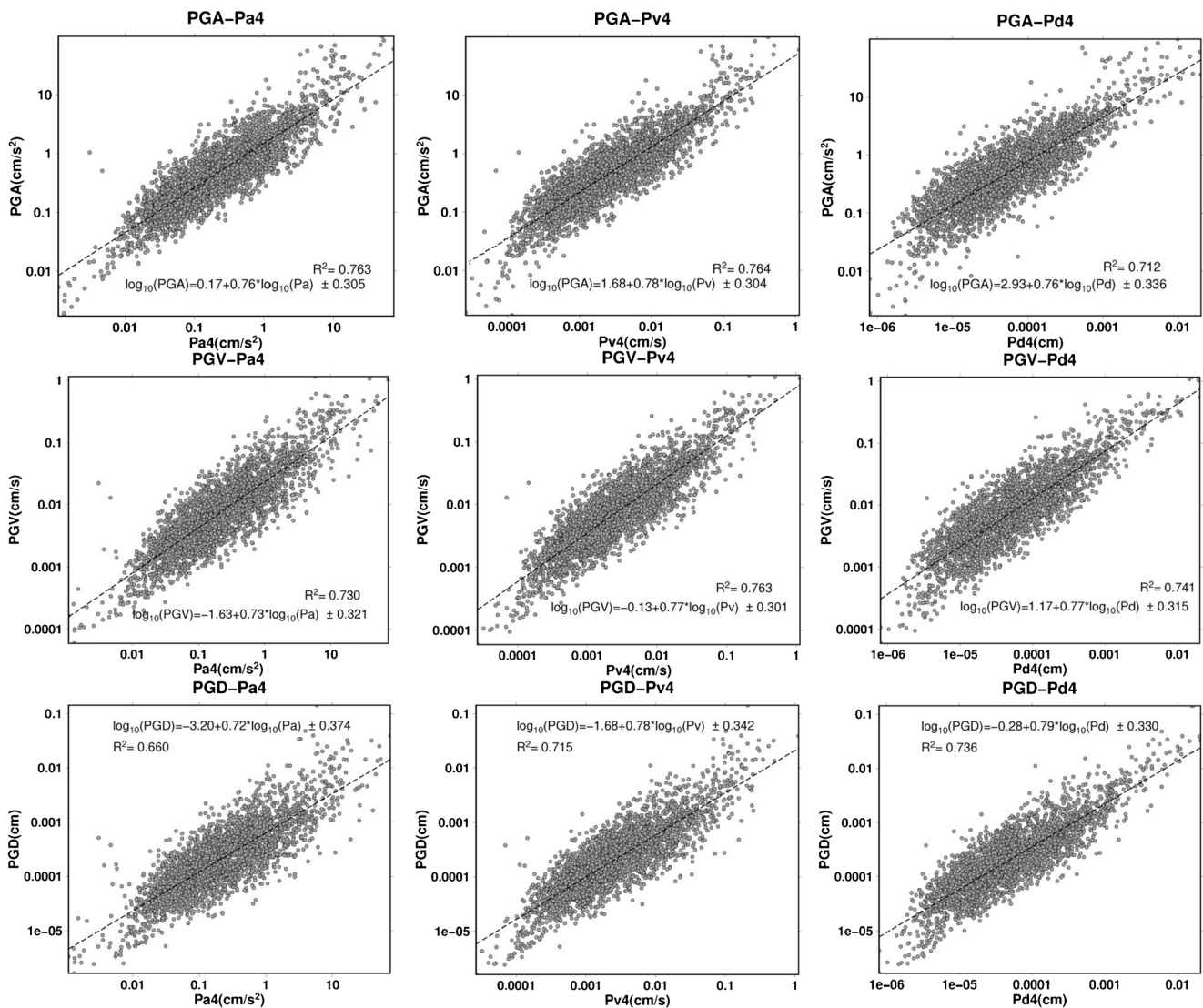


Fig. 4 Empirical relationships between ground motion parameters (PGA, PGV, PGD,  $P_a$ ,  $P_v$ ,  $P_d$ ) for 4-s window after P-wave arrival

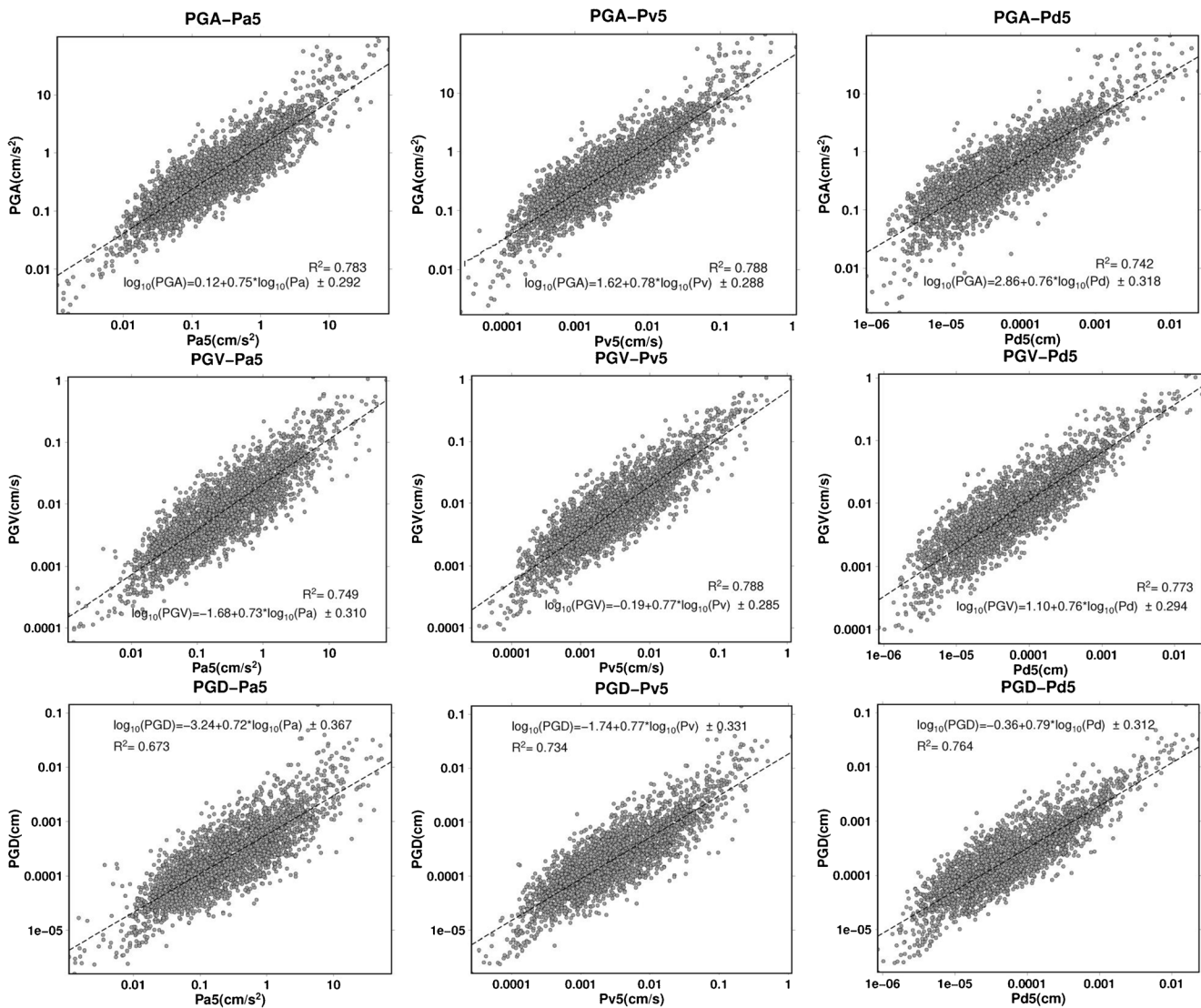
periods (Biswas 1987, 2005; Merh 1995). Deccan basalt covers the major parts of Saurashtra, South Gujarat, and some portions of Kachchh with intervening Cretaceous and Tertiary rocks at many places.

Narmada, Kachchh, and Cambay are the three marginal rifts which form an integral part of Gujarat with the presence of many active faults (Biswas 1987, 2005; Talwani and Gangopadhyay 2001). The faults in these rifts follow important tectonic trends, viz. Kachchh basin in Delhi trend, the Narmada in Satpura trend, and Cambay basin in Dharwar trend. The Kachchh region is occupied with pre-Quaternary rocks (Gupta et al. 2001) and is characterized by uplifted highlands and islands surrounded by plains of the Great Rann, Banni, and Little Rann. The mainland Kachchh is a rocky terrain with northern hill range and Katrol hill range bounded in their north by a fault. The tilted block uplifts in the region are caused by sub-parallel faults. From north to south, uplifts are bounded by

different faults, namely Nagar Parkar Fault (NPF), Allah Bund Fault (ABF), Island Belt Fault (IBF), Kutch Mainland Fault (KMF), and South Wagad Fault (SWF). The northern hill range is bounded by major faults, namely the Kachchh Mainland Fault (KMF) and Katrol Hill Fault (KHF). The most strained region is where KMF overhangs the South Wagad Fault (SWF) (Biswas 2005). The Bhuj earthquake in 2001 of  $M_w$  7.7 that claimed around 14,000 lives was located in this Kachchh region close to KMF (Fig. 1).

### Data and methodology

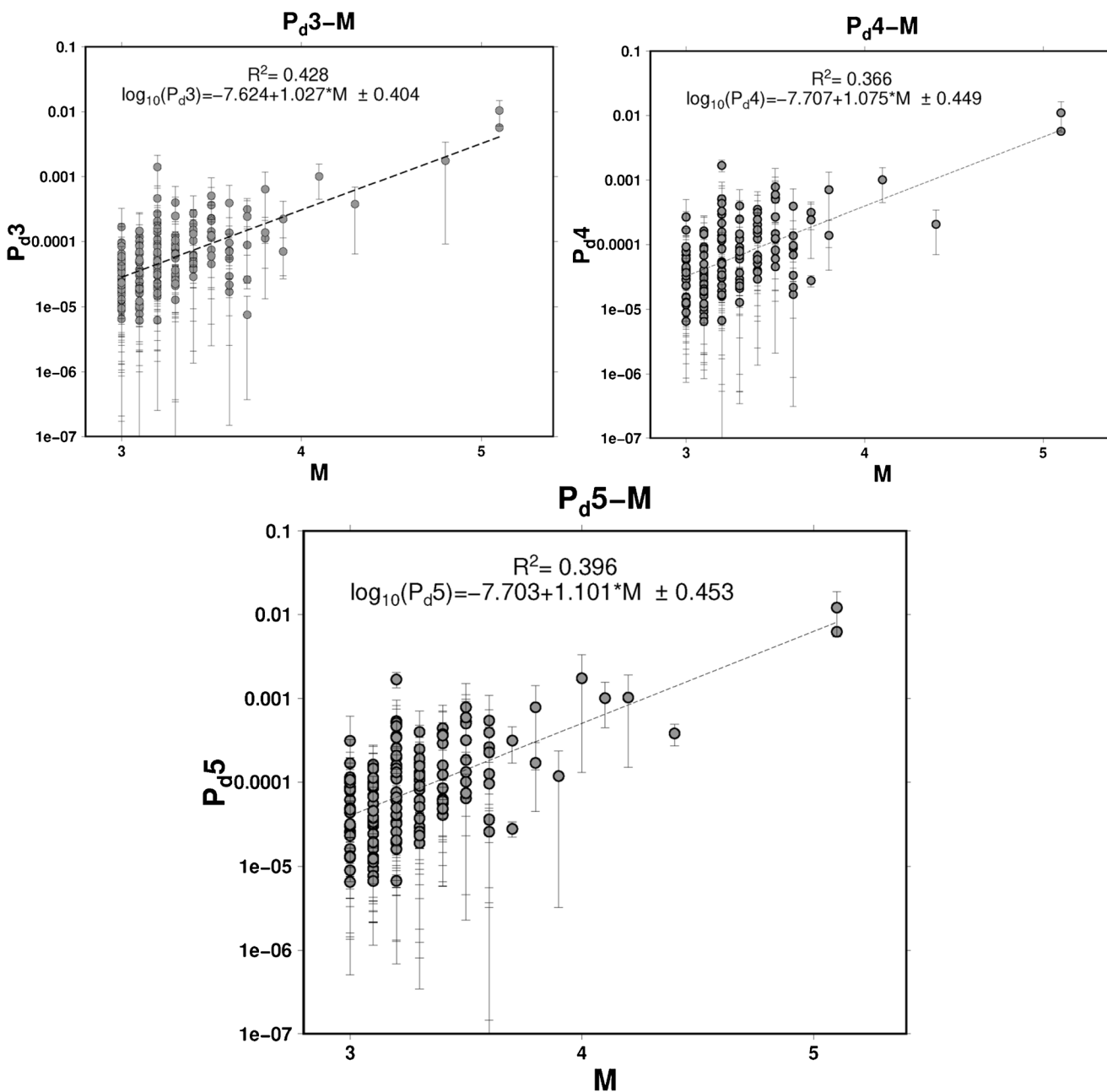
A total of 310 earthquakes originating from Kachchh area during 2010 to 2015 having  $M$  3.0–5.2 have been utilized in the present analysis. These earthquakes were recorded by 27 broadband seismograph stations of GSNet (Fig. 2).



**Fig. 5** Empirical relationships between ground motion parameters (PGA, PGV, PGD,  $P_a$ ,  $P_v$ ,  $P_d$ ) for 5-s window after P-wave arrival

All the seismographs are equipped with 120-s CMG-3T broadband sensor with 24-bit recorder. The stations record ground motion velocity continuously at 100 samples per second. A total of 2986 records with an epicentral distance less than 100 km have been used in this study. Each seismogram is first corrected for instrument response and then differentiated to get acceleration and integrated for displacement. A 0.075 Hz high-pass recursive Butterworth filter is applied to remove low frequency drift caused by the integration process. Since we are dealing with the initial portion of the waveform, using high-pass filter will not cause any effect on estimating parameters. From the first 3 s, 4 s, and 5 s of the P-phase of vertical acceleration, velocity, and displacement time series, we estimated the maximum acceleration ( $P_a$ ), velocity ( $P_v$ ), and displacement ( $P_d$ ) respectively. Peak ground acceleration (PGA), velocity (PGV), and displacement (PGD) are

picked from the larger ground motion of the two horizontal components. We used the P-wave to estimate the overall size of an earthquake. Both P- and S-waves are generated due to the seismic fault motion, but the amplitude of P-wave is, on average, much smaller than the amplitude of S-wave. For a point double-couple source, the ratio of the maximum P-wave amplitude to that of the S-wave is approximately 0.2. Thus, the S-wave is primarily responsible for damage owing to the earthquake. However, the waveform of the P-wave reflects how the slip on the fault plane is occurring. As P-wave carries information and S-wave carries energy, so by observing the P-wave over some time, we can have source information during this time. It is obvious that a longer average time period ( $\tau_0$ ) would provide more accurate information of the source. However, if  $\tau_0$  is too long, the early warning merit of the method is compromised. The following method is used to



**Fig. 6** Empirical relationships between  $P_d$  and  $M$  for different time windows (3–5 s) after P-wave arrival. Following Kanamori (2005) and Wu and Kanamori 2005a, 2005b), average  $P_d$  and its standard deviation are calculated for each event. Then, Pearson correlation coefficient

(regression coefficient) is calculated between  $\log_{10}(P_d)$  and magnitude ( $M$ ). Finally, a straight line is fitted between  $\log_{10}(P_d)$  and  $M$  with standard error

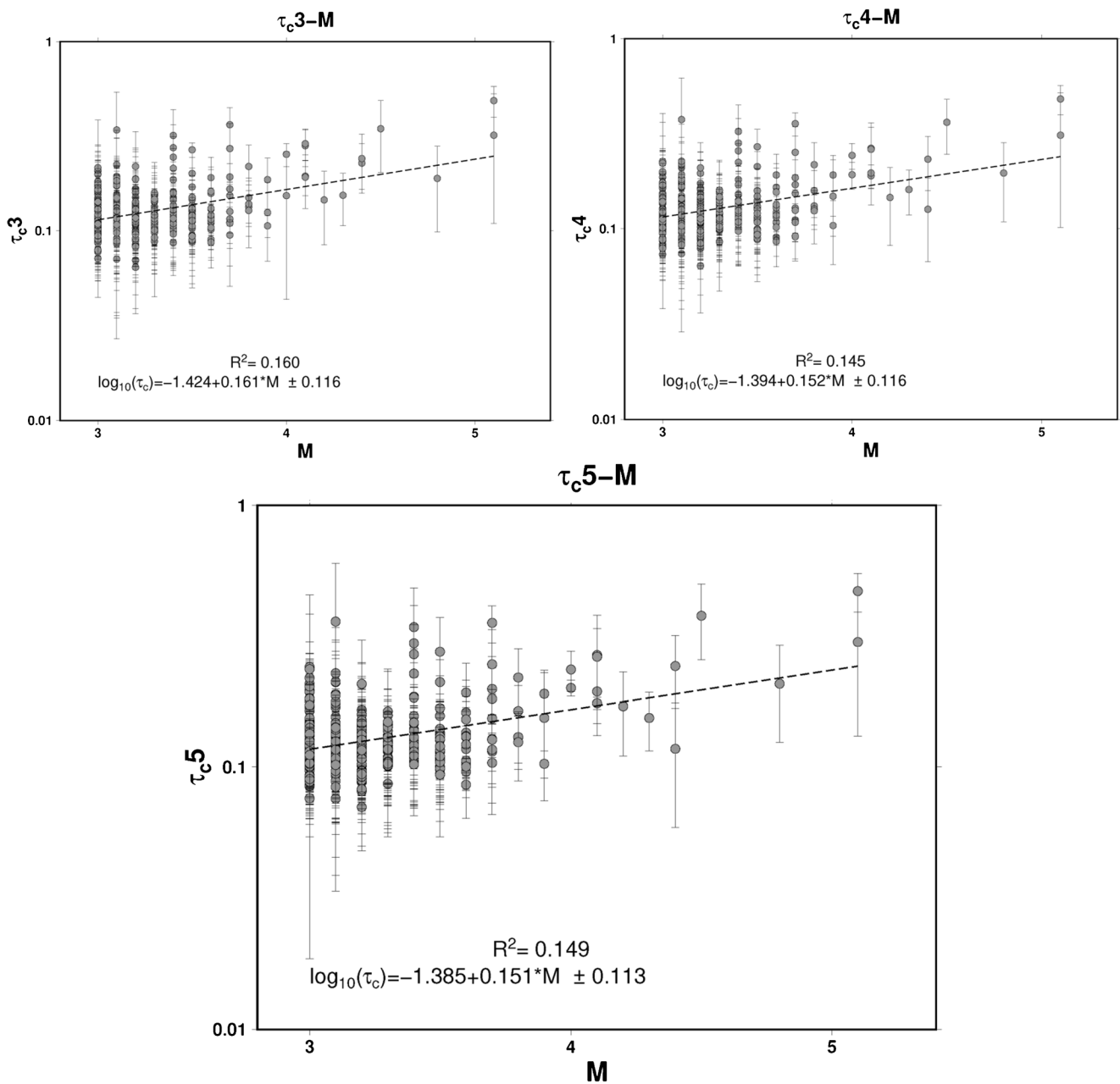
estimate various parameters modified after Nakamura (1988) and proposed by Wu and Kanamori (2005a).

$$r = \frac{\int_0^{\tau_0} u^2(t) dt}{\int_0^{\tau_0} u^2(t) dt} \tag{1}$$

where  $u(t)$  is displacement and is obtained by integrating over some time, typically 3 s after P-wave arrival. Using Parseval’s theorem,

$$r = \frac{4\pi^2 \int_0^{\infty} f^2 |\hat{u}(f)|^2 df}{\int_0^{\infty} |\hat{u}(f)|^2 df} = 4\pi^2 \langle f^2 \rangle \tag{2}$$

where  $f$  is the frequency,  $\hat{u}(f)$  is the frequency spectrum of  $u(t)$  and  $\langle f^2 \rangle$  is the average of  $f^2$  weighted by  $|\hat{u}(f)|^2$ . Then,  $\tau_c$  is given as below:



**Fig. 7** Empirical relationships between  $\tau_c$  and  $M$  for different time windows (3–5 s) after P-wave arrival. Following Kanamori (2005) and Wu and Kanamori (2005a, 2005b)), average  $\tau_c$  and its standard deviation are calculated for each event. Then, Pearson correlation coefficient

(regression coefficient) is calculated between  $\log_{10}(\tau_c)$  and magnitude ( $M$ ). Finally, a straight line is fitted between  $\log_{10}(\tau_c)$  and  $M$  with standard error

$$\tau_c = \frac{1}{\sqrt{(f^2)}} = \frac{2\pi}{\sqrt{r}} \tag{3}$$

This parameter is used to represent the period of the waveform.  $\tau_c$  estimated from initial few seconds typically 3 s is used to estimate magnitude for events  $\leq 6$ . However, for the events  $\geq 6.5$ , the magnitude can be estimated using  $\tau_c$  from

greater time windows. This procedure takes longer time and may not be practical for nearby cities (Wu and Kanamori 2005b).  $\tau_c$  estimation uses the frequency content of P-wave while another parameter  $P_d$  adopts the amplitude content of the initial part of waveforms. Displacement is estimated from velocity using the integration process with a cutoff frequency of 0.075 Hz. In the same way, acceleration is estimated from velocity using differentiation. Finally,  $P_d$ ,  $P_v$ , and  $P_a$  are estimated from initial 3 s, 4 s, and 5 s after the P-wave arrival.



**Table 2** Comparison of regression relations obtained in the present study with regression relations established by other researchers using different datasets

Place	EEW parameters	Regression equations	References
Southern California	$\tau_p^{max}-M$	$M_w = 7 \log(\tau_p^{max}) + 5.9$	Allen and Kanamori (2003)
Taiwan	$\tau_c-M$	$M_w = 4.525 \log(\tau_c) + 5.036$	Wu and Kanamori (2005a)
Taiwan	$\tau_c-M; P_d-M$	$M_w = 3.088 \log(\tau_c) + 5.30$ $\log(p_d) = -3.80 + 0.72M - 1.44 \log R \pm 0.29$	Wu et al. (2006)
Southern California	$P_d-M$	$\log(p_d) = -3.46 + 0.72M - 1.37 \log(R) \pm 0.305$	Wu and Zhao (2006)
Northern California	$\tau_p^{max}-M; P_d-M$	$M_w = 5.22 \log(\tau_p^{max}) + 6.66; \log(p_d) = 0.73 M_w - 3.77$	Wurman et al. (2007)
Taiwan, Southern California, and Japan	$\tau_c-M$	$M_w = 3.37 \log(\tau_c) + 5.78$	Wu and Kanamori (2008a)
Japan	$\tau_p^{max}-M; P_d-M$	$\log(\tau_p^{max}) = 0.21 M_L - 1.22; \log(p_d) = 0.66 M_L - 4.02$	Brown et al. (2009)
Japan, Taiwan and, Central Italy	$\tau_c-M$	$\log(\tau_c) = 0.21(\pm 0.01) M_w - 1.2$	Zollo et al. (2010)
Istanbul	$\tau_c-M$	$\log(\tau_c) = 0.142 M_w - 0.475 \pm 0.1433$	Alcik et al. (2011)
Taiwan	$P_d-M$	10 s $\log_{10}(P_d) = -1.741 + 0.55 * M - 1.285 \log(R) \pm 0.252$	Chen et al. (2017)
Gujarat, India	$P_d-M$	3 s $\log_{10}(P_d) = -7.624 + 1.027 * (M) \pm 0.404$	Present work
	$\tau_c-M$	$\log_{10}(\tau_c) = -1.424 + 0.161 * (M) \pm 0.116$	
Gujarat, India	$P_d-M$	4 s $\log_{10}(P_d) = -7.707 + 1.075 * (M) \pm 0.449$	Present work
	$\tau_c-M$	$\log_{10}(\tau_c) = -1.394 + 0.152 * (M) \pm 0.155$	
Gujarat, India	$P_d-M$	5 s $\log_{10}(P_d) = -7.703 + 1.101 * (M) \pm 0.453$	Present work
	$\tau_c-M$	$\log_{10}(\tau_c) = -1.385 + 0.151 * (M) \pm 0.113$	

## Results and discussion

Following the data analysis by Wu and Kanamori (2005a), the vertical velocity time history is integrated to obtain displacement and a high-pass 0.075 Hz Butterworth filter is applied to avoid noise. In a similar way, velocity time history is differentiated to obtain acceleration time history. Instead of fixing a single time window, we choose to work for three-time windows, i.e., 3 s, 4 s, and 5 s.  $\tau_c$  and  $P_d$  are estimated from the earthquakes recorded in Kachchh region having magnitude range 3–5.2. Linear regression analysis is performed at various time steps (3- to 5-s time interval) to find the various empirical relationships.

The various ground motion parameters (PGA, PGV, and PGD) are plotted against estimated parameters ( $P_a$ ,  $P_v$ , and  $P_d$ ) for three different time windows (3–5 s). The results show 1:1 correlation between PGA:  $P_a$ , PGV:  $P_v$ , and PGD:  $P_d$ . PGA and estimated  $P_v$  values are found in a proportion of 1:100, while PGA and  $P_d$  values show 1:1000 proportion. Similarly, PGV and  $P_d$  show 1:100 proportion. We observe that  $P_a$ ,  $P_v$ , and  $P_d$  correlate well with peak amplitude parameters, and the highest correlation is observed for 5-s time window. Particularly,  $P_v$  and  $P_d$  are more correlated with PGA than  $P_a$ . Also,  $P_v$  and  $P_d$  have more long-period energy than  $P_a$  and correlate better with PGV. For 3- and 4-s window, some difference in values is observed. From here, it can be concluded that 5 s after the occurrence of earthquake, maximum peak values ( $P_a$ ,  $P_v$ , and  $P_d$ ) have been observed. Having 1:1 correlation between  $P_a$  and PGV,  $P_v$  and PGV, and  $P_d$  and PGD strengthens our viewpoint to use initial few seconds of waveform for magnitude estimation.

The proposed linear relationship between various parameters is of the following type:

$$\log_{10}(PGA/PGV/PGD) = A + B * \log_{10}(P_a/P_v/P_d) \pm C$$

where  $A$  and  $B$  are constants to be determined through regression analysis and  $C$  is a standard error in the estimate.

Using the above guidelines, the various estimated relationships for different time windows (3–5 s) between different parameters are given in Table 1. Also, the relations plotted for 3-s, 4-s, and 5-s window are given in Figs. 3, 4, and 5 respectively.

The values of  $\tau_c$  and  $P_d$  shift contrastingly for different time windows (3–5 s). In general, the value of  $P_d$  varies between 8e–07 to 0.04 cm. The values estimated from the present dataset are lower compared with the expected one. The value of  $P_d$  shows more scatter for 3-s window compared with 4- and 5-s window. Secondly,  $P_d$  values estimated from 3-s window are less in comparison with other higher time windows. For events with magnitude  $\geq 6$ , the value of  $P_d$  using Taiwan and global data is 0.35 cm (Wu and Kanamori 2005a).  $P_d$  of vertical displacement in the first several seconds after the arrival of the P-wave have been studied in different parts of the world (Wu et al. 2007; Wu and Kanamori 2008a, 2008b, 2005b; Zollo et al. 2006; Chen et al. 2017; Mittal et al. 2019b) and reflects the attenuation relationship with distance as a function of magnitude and is also well correlated with the peak ground velocity (PGV).

The proposed regression analysis between magnitude ( $M$ ) and  $P_d$  is:

$$\log_{10}(P_d) = A + B * (M) \pm C$$

The plot between  $M$  and  $P_d$  for 3–5 s is given in Fig. 6.

The values of  $\tau_c$  for different time windows vary from .04 to 0.6. In the same way as  $P_d$ , the values of  $\tau_c$  for 3-s window are more scattered compared with higher time windows. For most events with  $M > 5$  in Taiwan,  $\tau_c$  is  $\geq 1$  s, while the same value of  $\tau_c$  is obtained for the events with  $M > 6$  in Southern California. In our case, even some of the earthquakes have magnitude  $\geq 5$ , but the values of  $\tau_c$  are not even close to 1. This may be due to the difference in signal to noise (S/N) ratio, especially for smaller earthquakes. This difference in  $\tau_c$  values is expected to decrease as the event size increases (Wu et al. 2007). But in most of the cases, it may not be a reliable EEW parameter owing to S/N sensitivity.

In a similar way, the proposed regression analysis between magnitude ( $M$ ) and  $\tau_c$  is:

$$\log_{10}(\tau_c) = A + B * (M) \pm C$$

Using above guidelines, the estimated relationships for different time windows (3–5 s) between  $\tau_c$  and  $M$  are plotted in Fig. 7 and summarized in Table 1.

A better correlation is observed between  $P_d$  and  $M$  in comparison with  $\tau_c$  and  $M$ . The correlation is better if a 5-s time window is considered. So in our viewpoint, the  $\tau_c$  cannot be considered as one of the reliable EEW parameter for Kachchh region using data from GSNNet. For practical early warning purposes, we are concerned with the events with  $M > 6$ . For estimating the magnitude of bigger earthquakes in a reliable way, different time windows need to be used after P-wave arrival. In recent time, Chen et al. (2017) used 10 different time windows (1–10 s) to estimate the magnitude of bigger earthquakes. They concluded that larger time windows are needed for estimating the magnitude efficiently using  $P_d$  methodology, but at the cost of reducing EEW warning time. Mittal et al. (2019b) used  $P_d$  methodology in India to find the magnitude of earthquakes. They used recorded earthquakes from Taiwan having magnitude close to 6. In addition, they used synthesized data for two historical earthquakes. Their estimated  $P_d$  values are in agreement with others (e.g., Chen et al. 2017; Wu et al. 2016), which confirms the applicability of  $P_d$  methodology in India. A comparison of present findings with others in the world is shown in Table 2. However, using data in the present work, this comparison may not be valid due to non-availability of higher magnitude earthquakes. ISR will be using the global data of  $M > 6.0$  for fine tuning the estimated relationships and comparison in future.

## Conclusion

We investigated correlations between various ground motion parameters like PGA, PGV, PGD,  $P_a$ ,  $P_v$ ,  $P_d$ , and  $\tau_c$  using broadband data of GSNNet having a magnitude range 3–5.2, operated by the Institute of Seismological Research (ISR), and showed 1:1 correlation. This correlation strengthens the basis that the initial few seconds of the waveform can be used to infer the important information about earthquakes. Three- to 5-s time windows are considered to measure  $P_a$ ,  $P_v$ ,  $P_d$ , and  $\tau_c$  from the vertical component of the waveforms. In Gujarat, the stations of Gujarat State Seismic Network are not densely distributed all over the Kachchh region. Earthquake early warning system for far away cities of Gujarat is possible with earthquake occurring in the eastern part of Gujarat with the dense network. ISR is going to install about 50 SMA in Kachchh region of Gujarat to have a denser network. So if detection of the P arrival and  $\tau_c$  and  $P_d$  estimations are done within 15 s, then early warning may be provided to the cities around 70 km or more from epicenter. Also by that time, S-waves carrying destructive waves have travelled 60 km from the epicenter, so warning is possible for regions beyond 60 km. A better correlation is observed between  $P_d$  and  $M$  in comparison with  $\tau_c$  and  $M$ . The correlation is better if a 5-s time window is considered. So in our viewpoint, the  $\tau_c$  cannot be considered as one of the reliable EEW parameters for Kachchh region using data from GSNNet owing sensitivity of  $\tau_c$  to signal to noise ratio. Due to earthquakes of  $M > 6.0$ , VSAT systems may be disturbed, so use of fiber cable for transmitting the data is preferable. However,  $\tau_c$  and  $P_d$  methods may overcome this difficulty because  $\tau_c$  and  $P_d$  are measured from the beginning of P arrival, before telemetry interruption occurs.

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