#### **ORIGINAL PAPER**



# Riverbank retreat analysis of the U-Tapao River, southern Thailand

Surat Semmad<sup>1</sup> · Tanit Chalermyanont<sup>1,2</sup>

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#### Abstract

Riverbank retreat is a result of complex combinations of several processes, including subaerial processes, fluvial erosion, and bank failure. The objective of this study was to analyze riverbank retreat of six representative riverbanks along the U-Tapao River in southern Thailand using a process-based riverbank retreat model. Field and laboratory tests were conducted to determine index and engineering properties of the riverbank soil required in the modeling. In particular, the erodibility parameters of the riverbank soil were estimated using empirical formulae, measured in situ by performing a submerged jet test, and estimated from long-term bank retreat simulations using the Bank Stability and Toe Erosion Model (BSTEM) incorporated with a lumped adjustment factor. The observed bank retreat over the period from 2002 to 2016 obtained from analysis of aerial imagery was used to verify the validity of the riverbank retreat results. Good agreement with the observations was obtained from BSTEMs using adjusted erodibility parameters.

Keywords Critical shear stress · Erodibility coefficient · Riverbank retreat · BSTEM · Submerged jet test · The U-Tapao River

# Introduction

Riverbank retreat is globally an important issue that affects infrastructure and stream-side properties, in-stream habitats, and water quality (Daly et al. 2015). Excessive sediment from riverbank erosion is among the most common surface water pollutants that degrade water quality and destroy aquatic habitats (ASCE 1998; Wynn and Mostaghimi 2006; Midgley et al. 2012). Moreover, many studies have demonstrated that riverbank erosion contributes a large portion of the sediment yield in a drainage system, which reduces the drainage capacity of the river and thereby causes flooding (e.g., Simon 1989; Grissinger et al. 1991). Thus, riverbank retreat involves the overall ecosystem of the river and causes huge economic losses with damage to natural resources (ASCE 1998).

Riverbank retreat is the integrated product of three main processes: subaerial processes, fluvial erosion, and bank failure (Hooke 1979; Lawler 1992; Lawler et al. 1997; Couper

Tanit Chalermyanont tanit.c@psu.ac.th

and Maddock 2001; Rinaldi and Nardi 2013). Subaerial processes are climate-related phenomena that reduce soil strength, inducing direct erosion and making the bank more susceptible to fluvial erosion by, for example, desiccation cracking (Thorne 1982). Fluvial erosion is the removal of bank material by the action of the river's hydraulic forces (Rinaldi and Nardi 2013), while the collapse of riverbanks due to slope instability is referred to as bank failure (Lawler 1995). Riverbank retreat is a cyclic process, initiated by the fluvial erosion of the river bed and/or toe, which creates a geotechnically unstable riverbank. This instability results in riverbank failure and deposition of failed materials at the bank toe. Subsequent floods remove that failed materials and the bank retreat cycle is repeated until the channel widens enough to reduce the boundary shear stresses to non-erosive levels (Thorne 1982).

The erosion rate of cohesive riverbank is commonly predicted using the excess shear stress equation (Partheniades 1965; Hanson 1990a, 1990b):

$$\varepsilon = k_d (\tau_o - \tau_c)^a \tag{1}$$

where  $\varepsilon$  is the rate of erosion (m/s),  $k_d$  is the erodibility coefficient (m<sup>3</sup>/N.s),  $\tau_o$  is the developed boundary shear stress (Pa),  $\tau_c$  is the critical shear stress (Pa), and *a* is an empirical exponent, often in practice assumed to be unity (Hanson

<sup>&</sup>lt;sup>1</sup> Department of Civil Engineering, Prince of Songkla University, Hat Yai, Songkhla 90112, Thailand

<sup>&</sup>lt;sup>2</sup> Southern Natural Disaster Research Center, Prince of Songkla University, Hat Yai, Songkhla 90112, Thailand

1990a, 1990b; Hanson and Cook 2004). The riverbank erosion is initiated by non-negative excess shear stress ( $\tau_o - \tau_c$ ). Once the erosion is initiated,  $k_d$  defines the rate at which particles are detached from the riverbank (Daly et al. 2013).

In the excess shear stress equation, while  $\tau_{0}$  is simply related to the flow rate of water ( $\tau_o = \gamma_w RS$ , where  $\gamma_w$  is the unit weight of water, R is the local hydraulic radius calculated from the water depth, and S is the channel slope (Daly et al. 2015)), the soil erodibility parameters ( $\tau_c$  and  $k_d$ ) are difficult to quantify (Grissinger 1982). There are many approaches for determining the erodibility parameters. Several studies have derived  $\tau_c$  and  $k_d$  for cohesive soils using various techniques such as flume tests (Hanson and Cook 1997), a laboratory hole erosion test (Briaud et al. 2001; Wan and Fell 2004), and a submerged jet test (Hanson and Cook 1997; Clark and Wynn 2007). Based on such experimental results, many studies have proposed simpler approaches to estimate  $\tau_c$  from other soil properties: from clay content and liquid limit (Smerdon and Beasley 1961), silt-clay content (Julian and Torres 2006), and from unconfined compressive strength (Kamphius and Hell 1983). Once  $\tau_c$  is determined,  $k_d$  can be estimated from empirical formulae (e.g., Hanson and Simon 2001; Wynn 2004; Simon et al. 2011).

Alternatively, in situ measurement of the erodibility parameters can be done using the submerged jet device developed by Hanson (1990b). The jet test is preferred over the flume tests because it can be conducted directly on the intact riverbank material without sampling and sample preparation that would disturb the soil structure, as they do in the flume tests. Determination of  $\tau_c$  and  $k_d$  using the jet test results (i.e., jet pressure and scour depth created) has been proposed by many researchers, such as Hanson and Cook (1997, 2004) and Daly et al. (2013). A detailed description of the jet device and the testing methodology is presented elsewhere (Hanson and Cook 1997; Hanson and Simon 2001; Al-Madhhachi et al. 2013).

Recently, Daly et al. (2015) evaluated the erodibility parameters of the Barren Fork Creek in eastern Oklahoma, USA, by calibration of a process-based riverbank retreat model. Streambank geography, bank soil properties, stream hydrograph, and initial erodibility parameters obtained from the jet test were used as inputs to the process-based riverbank erosion model (i.e., the Bank Stability and Toe Erosion Model, BSTEM), developed by the National Sedimentation Laboratory in Oxford, MS. The computed streambank was compared with the actual streambank retreat obtained from aerial imagery. The initial erodibility parameters were then adjusted until the computed streambank retreat was similar to the observed streambank retreat. The erodibility parameters obtained in this manner accounted for fluvial erosion and bank failure, along with several other field factors such as curvature-driven and turbulence-driven secondary flows and spatial and temporal changes of bank materials due to cyclical wetting and drying.

As a part of the U-Tapao River erosion study and protection project, the objective of this study was to analyze riverbank retreat of six representative composite riverbanks along the U-Tapao River in southern Thailand. The field survey was conducted to determine geometry of the riverbanks. In situ and laboratory measurements were performed to assess the riverbank soil geotechnical and erodibility parameters. Aerial imagery analysis was conducted to determine the actual bank retreats. The Bank Stability and Toe Erosion Model (BSTEM) was used to compute the riverbank retreats. The computed results were verified and validated using measured riverbank retreats from aerial imagery analysis.

### Description of the study area

The study area is located in the U-Tapao River watershed, in the southern part of Thailand (Fig. 1). The U-Tapao River watershed covers 2392 km<sup>2</sup> from the southern Thai-Malaysian border to the Songkhla Lake. This is the most important watershed of southern Thailand and is home to over 700,000 residents. Hat Yai city, the main city in the watershed, is a local center of economy, industry, and tourism in this region. The U-Tapao River, the main river in the watershed, is about 112 km long. It originates in the southern mountainous areas, flows northward through the center of the watershed, and drains into the Songkhla Lake. The average annual rainfall of the watershed is about 1524 mm due to the tropical monsoon climate in this region. Heavy rains in the months from October to December often cause great erosion and frequent failures of the riverbanks.

U-Tapao riverbanks along the midstream area of the watershed are reportedly experiencing high bank retreat problems and were selected as the study area. In this area, the U-Tapao River is about 20 to 40 m wide and 5 to 10 m deep. A picture of the U-Tapao River composite bank in the study area (Fig. 2) shows a typically steep bank face. The typical composite riverbanks in the study area consist mainly of two layers. The top layer (hereafter called "upper bank") is low plasticity cohesive soil with thickness ranging from about 1.0 to 1.5 m. The underlying layer (hereafter called "lower bank") is either cohesive or granular soil, which normally ranges in thickness from about 3.0 to 6.0 m. Field observation indicates toe erosion at the lower banks continuously leads to bank failure and retreat. In this study, six sites were selected at locations along the midstream area of the U-Tapao River and are designated as UT1 to UT6, as shown in Fig. 1 and Table 1. The distance from UT1 to UT6 is about 14 km. Pictures of the



Fig. 1 U-Tapao River watershed and the study site locations

U-Tapao River bank sites are shown in Fig. 3. Around these sites, the typical land use is as para rubber plantations that have bank retreat problems according to local



Fig. 2 An U-Tapao River composite bank showing the typical layers. Upper bank with low plasticity cohesive soil (a) and lower bank with cohesive or granular soil (b)

authorities and land owners. At each site, a representative cross section and a detailed bank stratigraphy were prepared using field survey data.

# Background

# Empirical relationships for determining erodibility parameters

There are several approaches to determine soil erodibility parameters. The parameters can be simply estimated from empirical relationships using soil index properties, as proposed by several researchers. Estimates of  $\tau_c$  can be obtained from empirical equations using plasticity index, dispersion ratio, mean particle size, and percent clay (Smerdon and Beasley 1961), silt-clay content (Julian and Torres 2006), unconfined compressive and vane shear strength (Kamphius and Hell 1983), and dispersion ratio, activity, and soil pH (Thoman and Niezgoda 2008). Based

#### Table 1 Soil properties at the six study sites

Site	Latitude, longitude (m)	Bank layer	Depth from bank top (m)	D <sub>50</sub> (mm)	$P_c(\%)$	PI (%)	SC (%)	$\gamma$ (kN/m <sup>3</sup> )	USCS	Shear strength parameters	
										φ <sup>'</sup> (°)	c <sup>'</sup> (kPa)
UT1	767,023, 659,154	Upper	0.00-1.30	0.047	17.13	6.90	57.91	16.90	CL	30.17	8.24
		Lower	1.31-4.60	0.070	13.01	5.38	47.96	18.23	CL	27.55	9.75
UT2	770,216, 661,222	Upper	0.00-1.50	0.007	35.00	14.70	86.00	18.67	CL	27.38	12.48
		Lower	1.51-4.34	0.250	1.39	NP	10.77	20.11	SM	33.74	1.26
UT3	770,317, 661,286	Upper	0.00-1.40	0.010	25.90	11.54	72.00	18.02	ML	27.17	9.56
		Lower	1.41-4.49	0.103	6.25	NP	41.63	17.98	ML	28.38	5.07
UT4	770,986, 661,074	Upper	0.00-1.50	0.035	17.62	9.33	63.39	17.86	CL	22.61	17.05
		Lower	1.51-7.78	0.236	3.24	NP	13.63	17.63	SM	28.94	2.01
UT5	771,082, 661,237	Upper	0.00-1.00	0.065	11.28	7.54	48.90	18.16	CL	24.31	3.12
		Lower	1.01-5.57	0.001	57.88	17.23	88.00	19.87	CL	23.97	18.27
UT6	775,103, 660,303	Upper	0.00-1.50	0.065	6.93	7.30	49.21	17.23	CL	31.30	3.19
		Lower	1.51-5.16	0.001	61.40	35.12	94.00	18.31	СН	25.52	17.78

 $D_{50}$ , median particle size of soil;  $P_c$ , percentage of clay content; PI, plasticity index; SC, percentage of silt-clay content;  $\gamma$ , bulk unit weight; USCS, Unified Soil Classification System;  $\varphi'$ , effective internal friction angle; c', effective cohesion

on flume testing results, Smerdon and Beasley (1961) developed empirical relationships of  $\tau_c$  to various soil index properties, as shown in Eqs. 2–4.

 $\tau_c = 3.54 \times 10^{-28.1D_{50}} \tag{2}$ 

 $\tau_c = 0.493 \times 10^{0.0182P_c} \tag{3}$ 

$$\tau_c = 0.16(PI)^{0.84} \tag{4}$$

where  $\tau_c$  is the critical shear stress (Pa),  $D_{50}$  is the median particle size of soil (mm),  $P_c$  is the percentage of clay content (i.e., content of soil particles less than 0.002 mm in size), and *PI* is the soil plasticity index.

Julian and Torres (2006) established an empirical equation to estimate  $\tau_c$  from the percentage of silt-clay (*SC*):

$$\tau_c = 0.1 + 0.1779(SC) + 0.0028(SC)^2 - 2.34 \times 10^{-5} \times (SC)^3$$
(5)

Unlike  $\tau_c$ , empirical estimates of  $k_d$  from the soil properties are not available (Hanson and Temple 2002). However,  $k_d$  can be given empirical estimates from known  $\tau_c$ . Such empirical relations between  $k_d$  and  $\tau_c$  have been developed based on submerged jet test results and are often power laws (Hanson and Simon 2001; Wynn 2004; Thoman and Niezgoda 2008). Using the Blaisdell solution (Blaisdell et al. 1981), Simon et al. (2010) concluded from jet test results that  $k_d$  is related to  $\tau_c$ as shown in Eq. 6. Daly et al. (2013) developed a scour depth solution method to fit the jet test results and proposed the relationship in Eq. 7.

$$k_d = 1.62\tau_c^{-0.838} \tag{6}$$

$$k_d = 157\tau_c^{-1.620} \tag{7}$$

where  $k_d$  is the erodibility coefficient (cm<sup>3</sup>/N.s) and  $\tau_c$  is the critical shear stress (Pa). The discrepancy between the various empirical models indicates that, while the type of model might have wide applicability, each model fit is restricted to a specific context of soil samples.

#### Submerged jet test

For cohesive soils, the soil erodibility parameters can be experimentally determined using an in situ submerged jet device. Designed by Hanson (1990b), the device distributes a circular jet through the nozzle at a uniform velocity, to produce shear stresses in the bank material. Consequently, the scours or the eroded depths generated are measured, and their time profiles are used to determine the erodibility parameters. Hanson and Cook (1997) developed an analytical procedure to estimate  $\tau_c$  by fitting a hyperbolic logarithm equation proposed by Blaisdell et al. (1981) to the scour depth vs time data, while  $k_d$  was estimated by fitting the scour data to the excess shear stress equation (Eq. 1). Daly et al. (2013) stated that the conventional Blaisdell solution method is too conservative, so they developed an alternative approach, the so-called scour depth solution method.



Fig. 3 Pictures of U-Tapao River banks showing composite and cohesive riverbanks with steep bank faces

The jet test device has been used numerous times to determine the erodibility of cohesive soils (Hanson et al. 1999; Langendoen et al. 2000; Hanson and Simon 2001; Semmens and Osterkamp 2001; Simon and Thomas 2002; Thoman and Niezgoda 2008; Karmaker and Dutta 2011). Results from most of these studies indicate large variations in  $\tau_c$  and  $k_d$ . After conducting 83 jet tests on stream beds of highly erodible loess in the Midwest of USA, Hanson and Simon (2001) found that  $\tau_c$  ranges from 0.0 to 400 Pa and  $k_d$  ranges from 0.001 to 3.75 cm<sup>3</sup>/N.s. Thoman and Niezgoda (2008) investigated the channel stability of the Power River Basin in Wyoming. They determined erodibility parameters of the cohesive banks using jet tests and found the range for 0.11 to 15.35 Pa for  $\tau_c$  and from 0.27 to 2.38 cm<sup>3</sup>/N.s for  $k_d$ . Karmaker and Dutta (2011) studied the erodibility parameters of many sites along the Brahmaputra in India and reported the ranges from 0.1 to 100 Pa for  $\tau_c$  and from 0.519 to 11.28 cm<sup>3</sup>/(N.s) for  $k_d$ .

#### Process-based riverbank retreat model

A process-based riverbank retreat model has been used to compute the bank retreat and to study factors affecting bank stability and erosion (Wilson et al. 2007; Cancienne et al. 2008; Midgley et al. 2012; Daly et al. 2015). It consists of two main processes which are the bank erosion and the bank failure. The bank erosion includes both bank and bank toe erosions by hydrological processes (e.g., rainfall, river hydrograph, groundwater oscillations) that lead to bank profile changes over time (Rinaldi and Nardi 2013). The bank failure process involves reduction of the resisting forces in the bank soil mass by several factors, such as toe erosion and shear strength decrease due to wetting of soil, until the resisting forces are exceeded by the bank self-weight. The most common process-based riverbank retreat model is the Bank Stability and Toe Erosion Model (BSTEM) developed by the National Sedimentation Laboratory in Oxford, MS, USA (Simon et al. 2000). The current version of BSTEM (Dynamic Version 5.4) has bank stability and toe erosion modules, and the capacity to model a continuous hydrograph by sequentially applying the various model components for a stream depth defined by the hydrograph, redrawing the bank profile, and then moving to the next step of hydrograph (Daly et al. 2015).

Daly et al. (2015) used BSTEM to determine erodibility parameters of composite streambanks by calibrating the parameters to fit two temporal streambank retreat data sets from aerial imagery. They stated that spatial and temporal changes occur in the fluvial resistance of bank materials due to wetting/ drying cycles. In addition, the deeper and faster flows at the outsides of river bends exert elevated shear stresses on the streambank. Therefore,  $\tau_c$  and  $k_d$  can change considerably over time due to the wetting/drying cycles and the subaerial processes. They suggested that a "lumped" adjustment factor  $(\alpha, \text{dimensionless})$  should be used to modify Eq. 1, to account for the simplified hydraulics in BSTEM as well as for potential changes in erodibility, as shown in Eq. 8. This adjustment factor has been utilized in long-term analyses of repeating bank retreats in several prior studies (Langeodoen and Simon 2008; Lai et al. 2012; Nardi et al. 2013; Daly et al. 2015).

$$\varepsilon = k_d (\alpha \tau_o - \tau_c) = \alpha k_d \left( \tau_o - \frac{\tau_c}{\alpha} \right) \tag{8}$$

where  $\varepsilon$  is the rate of erosion (m/s),  $k_d$  is the erodibility coefficient (m<sup>3</sup>/N.s),  $\tau_o$  is the developed boundary shear stress (Pa),  $\tau_c$  is the critical shear stress (Pa), and  $\alpha$  is a "lumped" adjustment factor.

### Methodology

# In situ measurements with a submerged jet test device

In situ measurements of soil erodibility parameters were performed using a submerged jet test device during January to February 2015. The jet test device and the testing procedures complied with ASTM D5852. A total of 24 jet test runs were conducted at the six selected sites described previously. Duplicate jet test runs were conducted on both upper and lower banks at each site (four tests per site). Each test was conducted for 50 min, with scour depth and pressure differential readings taken at 5-min intervals. The  $\tau_c$  and  $k_d$  were estimated from the scour and shear stress data obtained, using the scour depth solution method developed by Daly et al. (2013).

#### Soil testing

At each site, both disturbed and undisturbed soil samples were collected. The disturbed samples were air-dried prior to conducting index property tests. The median particle diameter  $(D_{50})$  and the mass fraction passing sieve no. 200 (i.e., sieve size of 0.75 µm) were determined according to the soil particle size distribution test (ASTM D6913). Plastic limit, liquid limit, and plasticity index of each soil sample were determined following ASTM D4318. Hydrometer analysis (ASTM D422) was conducted to determine the silt-clay content (*SC*). For the undisturbed samples, the multi-stage direct shear (MSDS) test was performed according to ASTM D3080 to determine the shear strength parameters, namely the effective cohesion (c') and the effective internal friction angle ( $\phi'$ ).

#### Aerial imagery analysis

Aerial imagery analysis was conducted to determine the actual bank retreat over time. Aerial images with 0.5-m resolution representing the years 2002, 2010, and 2016 (Fig. 4) were obtained from the Royal Thai Survey Department for the analysis. All the aerial images were geo-referenced with the World Geodetic System 1984 (WGS-84) using ArcGIS10. For each site, the bank edges were digitized along the field-determined reach length. Retreat was determined to have occurred when the digitized bank in the next image appeared to be farther away from the river centerline of year 2002. For example, the 2002 river centerline shown as a light line in Fig. 4 acted



Fig. 4 Aerial photograph of U-Tapao River for bank retreat determination by analysis of aerial imagery

as a reference line, and three digitized bank locations were then overlaid onto the 2016 image. A series of transects were created from the centerline to the bank locations, and the corresponding transect lengths were measured. The bank retreat at each transect was computed by subtracting the current transect length from the previous one. A single bank retreat number for each site was computed by averaging the bank retreats across all transects along the reach length. In this study, the bank retreat for 2010, designated by  $R_{2010}$  (m) was defined as the bank retreat from comparing years 2002 and 2010. Correspondingly,  $R_{2016}$  (m) denotes the bank retreat from comparing 2010 and 2016. The total bank retreat ( $R_{\rm T}$ ) denotes the sum of  $R_{2010}$  and  $R_{2016}$ .

#### **Riverbank retreat analysis**

In this study, a bank retreat analysis for the U-Tapao River was conducted using BSTEM (Dynamic Version 5.4) according to the procedure developed by Daly et al. (2015). The BSTEM input data include river cross section, shear strength parameters, erodibility parameters, and river hydrograph. A representative cross section obtained from field survey was used as the bank geometry. The shear strength parameters (c' and  $\phi'$ ) were obtained from the multi-stage direct shear test described previously. The  $\tau_c$  and  $k_d$  were obtained from the jet tests and were used as initial erodibility parameters. River hydrographs and rating curves for the period from 2002 to 2016, by two nearby available stations (X44 and X90 stations in Fig. 1) of the Royal irrigation department, provided the hydraulic loading at the bank faces. A specific hydrograph for each site was

**Fig. 5** A hydrograph of the site UT6 used in BSTEM analysis

generated via back water curve analysis using boundary conditions such as upstream water discharge, downstream water level, and downstream bed level from both control stations. All generated hydrographs had the same pattern. A representative hydrograph from site UT6 is shown in Fig. 5.

Bank retreat results from the BSTEM runs (BSTEM  $R_{2010}$ ) were compared with the aerial  $R_{2010}$  obtained from aerial imagery analysis. When BSTEM  $R_{2010}$  did not equal the aerial  $R_{2010}$ , this indicated that the initially used erodibility parameters did not represent the field conditions hydrologically and geotechnically. The initial  $\tau_c$  and  $k_d$  were then adjusted using the lumped calibration factor ( $\alpha$ ) described in Eq. 8, and BSTEM  $R_{2010}$  was recomputed. This was iterated until the difference between BSTEM and aerial  $R_{2010}$  was less than 0.5 m (which is the resolution of the aerial images) and the lumped  $\tau_c$  and  $k_d$  were obtained. To verify that these lumped  $\tau_c$ and  $k_d$  values were good for modeling the bank retreat, another set of BSTEM runs was conducted using the 2010 to 2016 hydrographs, and the corresponding BSTEM  $R_{2016}$  values were computed. The BSTEM  $R_{2016}$  model predictions were then compared to observed  $R_{2016}$  from aerial imagery analysis, to validate the models using lumped  $\tau_c$  and  $k_d$  values.

## **Results and discussion**

#### Soil testing results

The laboratory test results are shown in Table 1. Thickness of the upper bank ranged from 1.0 to 1.5 m. The upper bank soil



was classified as either low plasticity silt (ML) or as low plasticity clay (CL), with  $D_{50}$  values from 0.007 to 0.065 mm, SC values from 48.9 to 86.0%,  $P_c$  values from 6.93 to 35.0%, and PI values from 6.90 to 14.7%. Despite being classified as silty or clayey soils, these fine-grained soils with low plasticity exhibit properties between cohesive and non-cohesive soils, and the properties are not exclusively dependent on particle mass and interparticle electrochemical interactions (Grissiniger et al. 1981). Regarding the lower banks, as shown in Table 1, their thickness varied from 2.8 to 6.2 m. Both fine- and coarse-grained soil types were found. They fell into a wide range of soil types, including silty sand (SM), low plasticity silt (ML), low plasticity clay (CL), and high plasticity clay (CH). Fine-grained soil (i.e., ML, CL, and CH) was found in the sites UT1, UT3, UT5, and UT6, while coarse-grained soil (i.e., SM) was found in the sites UT2 and UT4. Shear strength parameters of the upper and lower bank soil (Table 1) were obtained using multi-stage direct shear tests. Effective cohesion (c) ranged from 3.12 to 17.05 (from 1.26 to 18.27) kPa and the effective internal friction angle ( $\phi$ ) ranged from 22.61 to 31.30 (from 23.97 to 33.74) ° for the upper (lower) bank soils.

# Erodibility parameters from jet tests and empirical formulae

The jet test results are presented in Table 2. It was found that  $\tau_c$  of the riverbanks at the selected sites varied in a comparatively narrow range, by about an order of magnitude. The data in

Table 2 indicate that the upper bank soil was slightly more erosion resistant than the lower bank soil. The  $\tau_c$  ranged from 7.12 to 20.93 Pa with a median of 10.99 Pa in the upper bank, while it ranged from 1.43 to 16.88 Pa with a median of 8.525 Pa in the lower bank. The  $k_d$  value ranged from 1.74 to 14.29 cm<sup>3</sup>/N.s with a median of 3.76 cm<sup>3</sup>/N.s. in the upper and from 3.67 to 19.55 cm<sup>3</sup>/N.s with a median of 9.67 cm<sup>3</sup>/N.s in the lower bank.

The  $\tau_c$  and  $k_d$  data in Table 2 were plotted to assess the relationship of  $\tau_c$  and  $k_d$  (Fig. 6). Additionally, erodibility categories as proposed by Hanson and Simon (2001) are also shown in Fig. 6. It was found that the riverbank soil mostly fell in the category "very erodible." Only the CL soil from sites UT4 and UT6 had sufficient erosion resistance to be considered "erodible." As demonstrated by Simon et al. (2010) in Eq. 6 and Daly et al. (2013) in Eq. 7,  $\tau_c$  and  $k_d$  are inversely related and tend to be related by a power law. In this current study, the relationship of  $\tau_c$  and  $k_d$  was fit by the solid line in Fig. 6:

$$k_d = 19.54\tau_c^{-0.547} \tag{9}$$

where  $k_d$  is the erodibility coefficient (cm<sup>3</sup>/N.s) and  $\tau_c$  is the critical shear stress (Pa). It is also seen in Fig. 6 that the relationship between  $\tau_c$  and  $k_d$  obtained in this study has similar trend as that in Daly et al. (2013), whereas the fit in Simon et al. (2010) tends to underestimate the  $k_d$  in our data. This may be due to the fact that Simon et al. (2010) used the Blaisdell solution method to estimate  $\tau_c$  and  $k_d$ , while Daly et al. (2013)

 Table 2
 Jet test results and estimates of erodibility parameters using empirical formulae

Site	Bank layer	Computed $\tau_c$ (Pa)				JET test		Computed $k_d^*$ (cm <sup>3</sup> /N.s)			
		<i>D</i> <sub>50</sub> (Eq. 2)	<i>P<sub>c</sub></i> (Eq. 3)	<i>PI</i> (Eq. 4)	<i>SC</i> (Eq. 5)	$ au_c$ (Pa)	$k_d ({ m m}^3/{ m N.s})$	Simon et al. (2010, Eq. 6)	Daly et al. (2013, Eq. 7)	This study (Eq. 9)	
UT1	Upper	0.17	1.01	0.81	15.25	13.18	4.13	0.17	1.90	4.40	
	Lower	0.04	0.85	0.66	12.49	14.37	3.67	0.20	2.63	4.91	
UT2	Upper	2.25	2.14	1.53	21.22	20.93	1.74	0.13	1.11	3.67	
	Lower	-	0.52	_	2.31	1.43	19.55	0.80	40.41	12.36	
UT3	Upper	1.85	1.46	1.25	18.69	7.12	6.48	0.14	1.37	3.94	
	Lower	-	0.64	_	10.67	2.41	11.36	0.22	3.39	5.35	
UT4	Upper	0.37	1.03	1.04	16.67	16.47	2.23	0.15	1.65	4.19	
	Lower	-	0.56	_	2.99	2.68	7.98	0.65	26.69	10.74	
UT5	Upper	0.05	0.79	0.87	12.76	8.80	3.39	0.19	2.54	4.85	
	Lower	3.23	5.57	1.75	21.49	16.88	6.55	0.12	1.09	3.65	
UT6	Upper	0.05	0.66	0.85	12.85	8.41	14.29	0.19	2.51	4.84	
	Lower	3.30	6.46	3.18	22.13	16.56	15.07	0.12	1.04	3.59	
Mediar	1	0.37	0.93	1.04	14.05	10.99	6.51	0.18	2.21	4.62	
Max		3.30	6.46	3.18	22.13	20.93	19.55	0.80	40.41	12.36	
Min		0.04	0.52	0.66	2.31	1.43	1.74	0.12	1.04	3.59	

\* $k_d$  computed using  $\tau_c$  obtained from Eq. 5

Fig. 6 Relationship of the critical shear stress and the erodibility coefficient, as obtained from the jet tests



and the present study use the scour depth solution method. In the Blaisdell solution, the measured scour time data may give unreliable estimates of both  $\tau_c$  and  $k_d$  (Simon et al. 2010).

The estimated erodibility parameters are tabulated in Table 2. The  $\tau_c$  was measured in situ with the jet test and estimated using the median particle size  $(D_{50})$  and Eq. 2, using percentage of clay content ( $P_c$ ) and Eq. 3, and using plasticity index (PI) and Eq. 4. The median values were 10.99, 0.37, 0.93, and 1.04 Pa, in the same order. The  $\tau_c$  values estimated using  $D_{50}$ ,  $P_c$ , and PI were as much as two orders of magnitude below the experimental  $\tau_c$  from the jet test. This indicates that estimates of  $\tau_c$  from the formula by Smerdon and Beasley (1961) can be very poor. Estimates using the silt-clay content (SC, Eq. 5) following Julian and Torres (2006) were better. Comparing the estimates for an individual site and for its upper and lower banks, the measured jet test  $\tau_c$  values were relatively similar to those estimated from SC. For example, for UT4 (Table 2), the  $\tau_c$  from jet test for the upper (lower) bank was 16.47 (2.68) Pa, while the corresponding estimate was 16.67 (2.99) Pa. Also, Karmaker and Dutta (2011) reported that their best estimates of  $\tau_c$  were based on SC. They stated that the submerged jet test method provides a better estimate of the  $\tau_c$  under field conditions, while the SC-based estimate may be used as an alternative method of estimation.

The  $k_d$  from jet tests and corresponding estimates are given in Table 2. Estimates of  $k_d$  were based on Eq. 6 (Simon et al. 2010), Eq. 7 (Daly et al. 2013), and Eq. 9 (this study), using only the estimates of  $\tau_c$  based on *SC* content (Eq. 5). The median  $k_d$  values were 6.51, 0.18, 2.21, and 4.62 cm<sup>3</sup>/N.s, from the jet test and from Eqs. 6, 7, and 9, in this order. The data in Table 2 indicate that Eq. 9 provided the best estimates of  $k_d$ , while Eq. 7 was better than Eq. 6. As previously mentioned, use of the scour depth solution method in Eqs. 7 and 9 resulted in better estimates of  $k_d$  than the Blaisdell solution method with Eq. 6.

#### Aerial imagery analysis results

The results from analysis of aerial images representing 2002, 2010, and 2016 (Table 3) indicate that bank retreat took place at every site. The  $R_{2010}$  (bank retreat from 2002 to 2010) ranged from 3.04 m (site UT6) to 11.76 m (site UT5) with an average retreat of 8.33 m, while the  $R_{2016}$  (bank retreat from 2010 to 2016) ranged from 1.87 m (site UT1) to 20.06 m (site UT5) with an average of 8.88 m. The  $R_{T}$  (bank retreat from 2002 to 2016) ranged from 7.52 m (site UT6) to 31.83 m (site UT5) with an average of 17.21 m. The retreats observed for the sites UT2 to UT4 were closely similar (Table 3). This is reasonable as these sites are located close to each other (about 1.4 km apart), so their soil properties and hydraulic loadings are expected to not differ by much.

The least 7.52-m  $R_T$  was found at the site UT6, which might be caused by several factors. The lower bank soil of this site was high plasticity clay (CH) with high effective cohesion, resulting in low bank failure potential and correspondingly low bank retreat. In addition, the site UT6 is located in the downstream area close to the Songkhla Lake, so a less steep channel slope is expected. This reduced slope would result in reduced boundary shear stress and, in turn, would reduce the fluvial erosion potential. At the other extreme, the Table 3 Aerial imagery analysis results

Site	Distance from	Land use	Reach length	Bank retreat (m)			
	011(11)		(111)	R <sub>2010</sub>	<i>R</i> <sub>2016</sub>	R <sub>T</sub>	
UT1	_	Rubber plantation	78.04	10.08	1.87	11.96	
UT2	4973	Rubber plantation	69.69	9.39	11.14	20.52	
UT3	5203	Rubber plantation	128.78	9.08	8.31	17.39	
UT4	6333	Rubber plantation	74.83	6.59	7.44	14.04	
UT5	7690	Rubber plantation	55.09	11.76	20.06	31.83	
UT6	13,990	Village	78.37	3.04	4.48	7.52	
			Average	8.33	8.88	17.21	

highest bank retreat was found at the site UT5 with  $R_{2010}$ ,  $R_{2016}$ , and  $R_{\rm T}$  being 11.76, 20.06, and 31.83 m, respectively. The  $R_{2010}$  does not differ much from that of the other sites, but  $R_{2016}$  does. Aerial images of this site clearly show that during 2002 to 2010, retreat occurred but the bank remained straight. However, river bank concave in shape is observed in the 2016 aerial image. Concave banks generally cause both curvaturedriven and turbulence-driven secondary flows that alter the flow fields and the morphology of the banks (Camporeale et al. 2007; Papanicolaou et al. 2007). These secondary flows are here considered to be the major cause of high  $R_{2016}$  of this site. The reason for the emergence of the concave shape at this site is not known. However, it is believed that soil heterogeneity in the river banks combined with the complexity of subaerial and hydrogeological processes to cause this.

At the site UT1,  $R_{2010}$ ,  $R_{2016}$ , and  $R_{T}$  were 10.08, 1.87, and 11.96 m, respectively.  $R_{2016}$  was much less than  $R_{2010}$  or retreats at the other sites (Table 3). Course change of the U- Tapao River was the cause of the low  $R_{2016}$  observed at this site. It is believed that a big flood in 2010 changed the course of the river, as observed in the aerial images, so that the site UT1 became located on the inside of a bend. Bank accretion and formation of point bars are usually found at the insides of bends (Motta et al. 2012).

#### **Riverbank retreat analysis results**

The bank retreats ( $R_{2010}$ ) from BSTEM runs using the  $\tau_c$  and  $k_d$  values from the jet tests were 0.0 m (no retreat) at the sites UT1, UT5, and UT6. In contrast, the  $R_{2010}$  values at sites UT2 to UT4 were very large exceeding 100 m. These simulation results differed dramatically from the observed  $R_{2010}$  values, measured from aerial images (Table 3). The incorrect  $R_{2010}$ estimates from BSTEM runs were caused by several factors. Among these were the spatial and temporal changes of fluvial resistance of the bank materials, due to wetting/drying cycles.

Table 4 Bank retreat analysis results compared to BSTEM simulation runs with adjusted erodibility parameters

Site	Bank layer	JET test		α	Adjusted values		$R_{2010}$ (m)		<i>R</i> <sub>2016</sub> (m)		$R_{\rm T}$ (m)	
		$ au_c$ (Pa)	<i>k<sub>d</sub></i> (cm <sup>3</sup> /N.s)		$ au_c$ (Pa)	$k_d (\mathrm{cm}^3/\mathrm{N.s})$	AIA	BSTEM	AIA	BSTEM	AIA	BSTEM
UT1	Upper Lower	13.18 14.37	4.13 3.67	2.986 2.986	4.41 4.81	12.33 10.95	10.08	9.48	1.87	11.81	11.96	21.29
UT2	Upper Lower	20.93 1.43	1.74 19.55	1.000 0.290	20.93 4.77	1.74 5.86	9.39	9.74	11.14	8.74	20.52	18.48
UT3	Upper Lower	7.12 2.41	6.48 11.36	0.492 0.492	14.47 4.89	3.19 5.59	9.08	9.05	8.31	10.59	17.39	19.64
UT4	Upper Lower	16.47 2.68	2.23 7.98	1.000 0.474	16.47 5.65	2.23 3.78	6.59	6.11	7.44	6.55	14.03	12.66
UT5	Upper Lower	8.80 16.88	3.39 6.55	1.000 3.162	8.80 5.34	3.39 20.70	11.76	13.19	20.06	19.25	31.83	32.45
UT6	Upper Lower	8.41 16.56	14.29 15.07	0.800 2.653	10.52 6.24	11.43 39.99	3.04	3.39	4.48	3.41	7.52	6.80
					RMS (m	ı)	0.69		4.32		4.06	

BSTEM, Bank Stability and Toe Erosion Model; AIA, aerial imagery analysis;  $\tau_c$ , critical shear stress,  $k_d$ , erodibility coefficient;  $R_{2010}$ , bank retreat from 2002 to 2010,  $R_{2016}$ , bank retreat from 2010 to 2016,  $R_T$ ;  $R_{2010} + R_{2016}$ ; RMS, root mean square error between BSTEM and AIA retreats

Fluvial resistance is typically measured at a specific time, but due to the wetting/drying cycles and the subaerial processes, the observed  $\tau_c$  and  $k_d$  can change considerably over time (Daly et al. 2015). Furthermore, the bank retreat can progress inland over a long time period so that it encounters spatial changes of the bank materials, and this affects the  $\tau_c$  and  $k_d$ as well.

To improve the computed bank retreat results, the  $\tau_c$  and  $k_d$ values were adjusted iteratively using trial lumped adjustment factors ( $\alpha$ ) in a series of BSTEM runs, until the computed  $R_{2010}$  were optimally close to the values measured from aerial imagery. The  $\alpha$ , adjusted  $\tau_c$  and  $k_d$ , and computed  $R_{2010}$  values are tabulated in Table 4. It was found that  $\alpha$  values approximately from 0.3 to 3.0 were sufficient to adjust the  $\tau_c$  and  $k_d$  so that the computed  $R_{2010}$  were in good agreement with the measured ones. For sites UT1 and UT3, use of equal  $\alpha$  values for upper and lower banks provided good  $R_{2010}$  results. However, for sites UT2 and UT4 to UT6, it was found that the  $R_{2010}$  were caused only by erosion of the lower banks. Thus, for these sites, the calibration of  $\alpha$  was conducted solely on the lower banks while the  $\alpha$  values of the upper banks were kept as unity. The computed  $R_{2010}$  obtained from BSTEM runs for all sites considered were fairly similar to the observed values, as shown in Fig. 7: the points in the scatter plot fall close to the diagonal line with identical values. The computed and measured  $R_{2010}$  differed in terms of the root mean square (RMS) error by as low as 0.69 m (Table 4), showing that BSTEM with adjusted erodibility parameters can be used to accurately fit our data, modeling the appropriate failure mechanisms of fluvial toe erosion leading to bank undercutting and sloughing of upper cohesive layers, as commonly observed in composite riverbank studies (Rinaldi et al. 2008).



Fig. 7 Comparison of bank retreat measured from aerial imagery to bank retreat computed with BSTEM

Bank retreats ( $R_{2016}$ ) calculated using BSTEM with the adjusted  $\tau_c$  and  $k_d$  values, and another set of hydrographs from 2010 to 2016 are tabulated in Table 4. The  $R_{2016}$  values calculated using BSTEM compared well with the corresponding  $R_{2016}$  values measured from aerial imagery, for all sites except the site UT1. For the sites UT2 to UT6, the absolute difference between measured and computed  $R_{2016}$  ranged from 0.81 to 2.40 m with an average of 1.49 m. This indicates that the erodibility parameters obtained using the lumped adjustment factor could be effectively used to predict the bank retreat. The  $\tau_c$  and  $k_d$  obtained using this technique are better than those obtained from empirical formulae or the jet tests, because these parameters already account for the "lumped" subaerial process, fluvial erosion, and slope failure.

For the site UT1, however, the computed  $R_{2016}$  overestimated the  $R_{2016}$  considerably, by + 9.94 m (Table 4). As mentioned previously, the river course change observed at site UT1 was the probable reason to this overestimate. The  $R_{2016}$  computed using the adjusted erodibility parameters to model  $R_{2010}$  (the course change of the river had not yet occurred) should show about similar rate of retreat as  $R_{2010}$ , given that the hydrograph between these two periods was not much different. However, due to the river course change, turning this site to the inner bend bank, the actual retreat reduced or even reversed to bank accretion. The measured  $R_{2016}$  at this site that was much less than predicted using BSTEM is entirely reasonable on this basis.

#### Conclusions

Steep riverbanks of the U-Tapao River in southern Thailand consisted of two layers. The thickness of upper and lower banks varied from 1.0 to 1.5 m and 3.0 to 6.2 m, respectively. Toe erosion at the lower banks was observed to continuously lead to bank failure. Laboratory test results showed that the riverbank soils along the U-Tapao River consisted of silty sand, low plasticity silt, low plasticity clay, and high plasticity clay. The erodibility parameters from the jet tests indicated that the soils can be classified as erodible to very erodible which were very susceptible to erosion. In addition, the lower bank soils were found to be more erodible than the upper ones. Aerial imagery analysis results revealed that the observed bank retreat from 2002 to 2016 ranged from 7.52 to 31.83 m with an average of 17.21 m. Process-based riverbank retreat analysis which incorporates the erosion of the riverbank soil through excess shear stress equation and the riverbank failure through slope stability equation was conducted using the Bank Stability and Toe Erosion Model (BSTEM) to compute long-term riverbank retreat. The computed retreats were verified with the observed ones. Initial BSTEM runs using the erodibility parameters obtained either from the jet test or the empirical formula over the period from 2002 to 2010 did not provide good predictions of bank retreat. However, good agreement of the retreats was achieved by adjusting the erodibility parameters iteratively, using the lumped adjustment factor. The adjusted critical shear stress and erodibility coefficient of the erodible riverbank soils ranged from 4.41 to 20.93 Pa and 2.23 to 39.99 cm<sup>3</sup>/N.s. These adjusted erodibility parameters are believed to account for local subaerial processes, fluvial erosion, and slope failures that cause the bank retreat. Another set of BSTEM runs using adjusted erodibility parameters was further validated against later observations, over the period from 2010 to 2016, and appeared to provide reasonably good predictions of river bank retreat.

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