

Numerical analysis and simulation of an impulse driven piezoelectric needle-free jet injector†

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Abstract

Transdermal drug delivery using needle free jet injections entails ejection of a liquid drug through a fine nozzle at elevated pressure, thus generating a narrow high-velocity fluid jet readily penetrable into skin and tissue. The idea of a simple and compact piezoelectric powered needle free injector (NFI) is introduced in this article, which offers electric control of injection volume in microliters. An impulse of up to 3500 N-s or more is generated by the multilayer piezoelectric actuator to drive the needle-free injector. The governing equations for the force and mass balance over the syringe plunger were derived to represent the driving mechanism for a compact needlefree injector. Furthermore, simulation was carried out to witness the effect of variation in parameters like impulse force, nozzle diameter and nozzle length on the injection dynamics, and the results prove the dependence of injection characteristics on aforementioned parameters, respectively. Finally, the specifications for fabrication of 10 μl volume delivering piezoelectric-impulse driven needle-free injector were obtained through analysis of multiple simulation results.

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Keywords: Multilayer piezoelectric actuator; Mechanical impulse; SimulationX; Liquid jet injection; Compact injector

1. Introduction

Rapid discovery and development of drugs with the passage of time has ensured the cure of many diseases, but effective drug delivery has been an under-explored area of research. Transdermal drug delivery represents an attractive alternative to the most commonly adopted oral delivery of drugs and is expected to offer an alternative to hypodermic injection, too [1-4]. Drugs with large molecules like most of the vaccines are injected through needles as they cannot be administered orally or absorbed by skin [5]. The need for trained nurses, needle phobia, and inadequate delivery of improper volumes of drugs has catalyzed the research to find drug delivery alternatives which offer simple and painless drug administration [6]. Various kinds of micro-needles are being developed for advancement in drug delivery through the skin, but there are challenges to delivering high molecular weight drugs [7-10]. Chemical penetration catalyzers, skin permeabilization and jet injectors as well are the recently studied areas for transdermal drug delivery [11-16]. The non-parental transdermal delivery of biopharmaceuticals is widely studied field these days, yet there are fierce complications for penetration of drug molecules into stratum corneum [17, 18]. Jet injectors, for parental administration of drug with high velocity into skin, have been studied in the past seven decades [19, 20]. Some drawbacks of jet injectors include splash-back of drug, unreliable drug depth, unpredicted dose delivery, painful bruises and bleeding [21- 24]. The causes of this unreliability include unsuitability of available devices to tackle variation in skin thickness, large drug volumes, and large nozzle sizes, which is also the cause of splash-back and pain caused by jet injectors [21, 23]. These limitations of jet injectors are addressed in the recent research. Jet injectors are now being used for transdermal gene delivery by stratum corneum disruption and intra-cavernosal therapies as well [25, 26].

In this paper, idea of electrically controlled drug delivery using impulse type jet injector is proposed for improved and consistent microliter drug administration by lesser pain. The proposed design of an impulse type needle free injector is powered by the instantaneous expansion of multilayered piezoelectric actuator to displace fluid through a fine sized nozzle. Conventional spring powered, compressed gas powered, and bubble driven injection device do not offer compact and silent operation with accurate control of injection speed [27-29]. In addition, drug pressure, and nozzle size have not been addressed previously. Previous studies have shown that piezo-

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electric actuators can be used to achieve high velocity fluid jets for penetration and delivery of insulin into animal skin [30, 31]. The recent multilayered piezoelectric (PZT) actuators have lower power consumption, fast expansion, no wear and tear, vacuum and clean room compatibility, and exhibit better conversion efficiency of electrical to mechanical energy [32- 37]. They can generate blocking force ranging from 300 N to 14000 N with maximum strokes varying from 13/9 μm to 270/200 μm by application of -30 V \sim 150 V potential difference [38]. If necessary, the scope for applications of piezoelectric actuators is enhanced by using displacement amplification mechanisms to enhance the stroke length of piezostack actuator, which include lever-type, moonie-type, rainbow-type, cymbal-type, ellipse-type, rhombus-type, bridge-type, rhombus with hinges, compound bridge-type, and threedimensional displacement amplification mechanisms [39-45]. The displacement amplification enhances the displacement up to 12 times, but it reduces the blocking force proportional to the displacement amplified [46]. The conventionally available multilayered piezoelectric actuator, without displacement amplification accessories, is considered as a power source for impulse type needle free injector [47, 48].

In this study, governing equations for numerical analysis of a compact, piezoelectric impulse driven needle free jet injector were derived. Instead of solving the equations repeatedly by changing minor parameters in a conventional way, model simulations were carried out to study the effect of force generated by multilayered piezoelectric actuator on pressure drop across the nozzle, which had not been addressed previously. The approach of utilizing simulation tool instead of cumbersome numerical solutions was adopted. Furthermore, the effect of variation of nozzle length and nozzle diameter, by keeping the piezostack force constant, on injection dynamics was analyzed. The piezostack force, which accelerates the plunger, was varied from 1000 N to 3500 N to observe its effect on pressurization of drug volume, which is the core parameter for the high velocity jet propagation out of a fine sized nozzle. The simulation model verifies the feasibility of utilizing the impulse mechanism to power the needle free injector and potential possibility of realization of piezo-stack impulse mechanism in needle free drug delivery device. The simulation results emphasize that the injection characteristics strongly depend on force generated by piezostack actuator, diameter of nozzle and length of nozzle, respectively.

2. Numerical analysis and modeling

2.1 Conceptual design

The proposed prototype of needle free jet injector to be designed is composed of a metal frame, the upside of which provides stiff support to the rigid end of piezoelectric actuator. The position of actuator can be adjusted by upper adjust-nut. The metal frame is connected to the syringe plunger through screw threads, and the drug supply line equipped with unidirectional check valve opens in the plunger cavity, as shown

Fig. 1. Piezoelectric impulse needle free jet injector assembly.

Fig. 2. Impulse NFI: (a) Excited state; (b) neutral state.

in Fig. 1.

2.2 Working mechanism

The injector is powered by DC supply line through the frame. Upon application of a voltage, the piezoelectric actuator excites, which in turn induces an instantaneous impulse to the syringe plunger. The plunger accelerates downwards by increasing the compression in the spring; as a result, the drug volume inside the plunger cavity gets pressurized causing a high pressure jet of drug from the nozzle at the bottom of the injector. When the DC supply is disconnected, the piezostack contracts and the spring force overcomes the accumulative mass of piezostack and syringe plunger by moving the plunger upwards. This phenomenon can be controlled by controlling the DC supply.

Fig. 2 represents the working principle of the piezoelectric impulse needle-free injector.

2.3 Mathematical model

The mechanism of impulse needle-free injector can be represented mathematically by derivation of governing equations considering the aforementioned working principle of needle free injector. The length of piezo-stack actuator in neutral state is *L^o* . When electric voltage is applied, the piezostack expands

Fig. 3. Force balance over syringe plunger.

and its length increases proportional to the applied potential difference. The piezostack length is represented as $L_{PZT} = L_o +$ *f(V)*. If *x* represents the expansion in length of piezostack, then *x* is the function of applied voltage $[x = f(V)]$. Thus, the relationship representing length of PZT stack at any instant is given below. Spring

Spring

Fig. 4. Control volume consi

The piece can expected as the mozzle as sh

its length

$$
L_{pz\overline{z}} = L_o + x. \tag{1}
$$

Similarly, the syringe plunger is considered in mechanical contact with the piezostack actuator. The return spring has free length of L^{\prime}_{o} . x_{o} is the pre-compression in the spring, which is considered to reduce the dead band. *xPL* is further compression in the spring caused by expansion of piezostack actuator. The total compression in the spring is expressed as $x_s = x_o + x_{PL}$. The spring length further decreases by expansion of piezostack actuator. The relationship to represent the instantaneous length of spring is expressed as follows. *Lextralistics* $\lim_{x \to a} E_x - x_n$. (a) proposinte call that is the syring that the syring $\left(\frac{\pi}{4}D_n\right)$ is the function of applied voltage $[x = f(t)]$. Thus, the relation of applied voltage $[x = f(t)]$. Thus, the relation below

$$
L_{SPR} = L_o - x_o - x_{PL} \tag{2}
$$

Eqs. (1) and (2) represent the geometrical consideration for expansion of piezostack with respect to contraction in spring and vice versa.

The force balance over the syringe plunger suggests that the sum of all the forces acting on the syringe plunger is equal to the mass times acceleration of the syringe plunger, which can be expressed as $(\sum F)_{PL} = m_{PL}$, $\ddot{x}_{PL} = 0$. If the needle-free injector assembly is considered to be positioned downwards against the gravity, then the forces acting on syringe plunger include particular methanic methanic methanic state for the present as $x_i = x_a + x_{Bx}$.

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The gravity and piezostack force are considered to be positive; thus the opposing forces are taken as negative. The ex pression for force balance over the syringe plunger is given in Eq. (3).

$$
F_{p_{ZT}} + m_{p_L}g - k(x_{p_L} + x_o) - \left[\frac{\pi}{4}D_p^2 \cdot P\right] - C_f \dot{x}_{p_L} = m_{p_L} \ddot{x}_{p_L} \ . \tag{3}
$$

Fig. 4. Control volume consideration for pressure evaluation in plunger cavity.

Manipulation of force balance Eq. (3) gives pressure build up across the nozzle as shown in Eq. (4).

$$
P = \frac{F_{p_{ZT}} + m_{p_L}g - k(x_{p_L} + x_o) - C_f \dot{x}_{p_L} = m_{p_L} \ddot{x}_{p_L}}{(\pi/A) D_P^2}.
$$
 (4)

The syringe plunger movement causes displacement in volume of fluid below plunger. The expression for volume of the fluid displaced by the plunger is represented by Eq. (5). VO_{out}

volume consideration for pressure evaluation in plunger

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nozzle as shown in Eq. (4).
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$$
\frac{dV_f}{dt} = \left(\frac{\pi}{4}D_{PL}^2\right) \cdot \dot{x} \,. \tag{5}
$$

Similarly, the fluid jet injected out of the nozzle can be ex pressed as Eq. (6).

$$
Q_{OUT} = \left(\frac{\pi}{4}D_{N}^{2}\right) \cdot v_{f} \tag{6}
$$

Manipulation of force balance Eq. (3) gives pressure build-
across the nozzle as shown in Eq. (4).
 $P = \frac{F_{\text{rzT}} + m_{\text{rz}}g - k(x_{\text{rz}} + x_o) - C_x\dot{x}_{\text{rz}} = m_{\text{rz}}\ddot{x}_{\text{rz}}}{(\frac{\pi}{4})D_v^2}$. (4)

The syringe plunger movement oulation of force balance Eq. (3) gives pressure build-
s the nozzle as shown in Eq. (4).
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yringe plunger movement causes displacement in Consideration of liquid chamber of needle-free injector as a control volume results in the expression for drug flow out of nozzle, which is expressed as Eq. (7). Fig. 4 represents the control volume under consideration. *PHOTER FORTER 1* **PHOTER 12 PLACE 12 PHOTER 12 PLACE 12 PHOTER 12** is displaced by the plunger. The expression for volume of the

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sseed as Eq. (6).
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b>ZZE, which is expressed as Eq. (7). Fig. 4 represents the
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$$
\left(\frac{\pi}{4}D_{p_1}^2\right) \cdot \dot{x} = \frac{V}{\beta} \frac{dP}{dt} \left(\frac{\pi}{4}D_{y_1}^2\right) \cdot v_f.
$$
(7)
The expression for velocity of fluid out of nozzle can be de-
ved from Bernoulli's Eq. (8).

$$
P_1 + \frac{1}{2}\rho v_1^2 + \rho g z_1 = P_2 + \frac{1}{2}\rho v_2^2 + \rho g z_2.
$$
(8)
The height difference $(z_2 - z_1)$ in this case is negligible and v_1

The expression for velocity of fluid out of nozzle can be derived from Bernoulli's Eq. (8).

$$
P_1 + \frac{1}{2}\rho v_1^2 + \rho g z_1 = P_2 + \frac{1}{2}\rho v_2^2 + \rho g z_2.
$$
 (8)

The height difference $(z_2 - z_1)$ in this case is negligible and v_1 is zero; thus Eq. (8) reduces to Eq. (9).

$$
P = P_{ATM} + \frac{1}{2}\rho v_2^2.
$$
 (9)

The expression for jet velocity out of nozzle Eq. (10) can be substituted in Eq. (7) to get final expression Eq. (11) for the velocity of plunger, which causes jet injection out of nozzle.

$$
v_f = \sqrt{\frac{2(P - P_{\text{atm}})}{\rho}}\tag{10}
$$

$$
\left(\frac{\pi}{4}D_{p_L}^2\right) \dot{x} = \frac{V}{\beta} \frac{dP}{dt} \left(\frac{\pi}{4}D_{\gamma}^2\right) \sqrt{\frac{2(P - P_{\text{ATM}})}{\rho}} \ . \tag{11}
$$

$$
\dot{x} = \frac{\frac{V}{\beta} \frac{dP}{dt} \left(\frac{\pi}{4} D_{\gamma}^{2}\right) \sqrt{\frac{2(P - P_{\text{atm}})}{\rho}}}{\left(\frac{\pi}{4} D_{\text{PL}}^{2}\right)}.
$$
\n(12) Nozle p

The system of above derived twelve equations can be solved for the forces acting on plunger, velocity and acceleration of syringe plunger, pressure build up in the drug chamber, and velocity of drug ejected out of nozzle. Instead of repeatedly solving the above equations to get results necessary for specification design of impulse jet injector, a simulation model for the impulse needle free injector was developed. Using the theory behind the derived equations, a simulation model for impulse needle free jet injector was used to carry out multiple simulations for derivation of useful results to derive design specification of proposed needle free injector.

2.4 Simulation modeling

The simulation of the impulse type needle free injector is carried out using a simulation tool called Simulation $X^{\textcircled{8}}$ 3.7 software by ESI ITI GmbH [34, 49]. The simulation model is developed by division of needle-free injector assembly into three parts in accordance with the mathematical model. The [29]. The simulation model is shown in Fig. 5. first part represents piezostack force generation mechanism, the second portion represents movement of syringe plunger due to mechanical impulse, and the third part represents drug dynamics due to pressure generated in plunger cavity and nozzle. It using a smultaion food called Smultaion X⁻³ 3. It used to the intuo considered as trag, when the sign significant called Smultaion X-3. It is used of the material model is the IP46 in SimulationX. The fluid propertie tware by ESI ITI GmbH [34, 49]. The simulation model is **IILP46** in SimulationX. The fluid properties like bulk relogional by division of needle-free injector assembly into luss and density are defined and temperature is re by ESI TIT GmbH [34, 49]. The simulation model is

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between the third correla-free injector assembly into lus and density are defined and temperature is second

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The spring mass damper in the second part helps to control the chaotic friction-induced vibration and ensures the stability of impulse propagation [50]. The parameters considered during simulation are in Table 1. The linear multi-step method is introduced to solve the first-order ordinary differential equations and a fifth-order backward differentiation formula $(5th$ BDF) as shown in Eq. (13) is employed in the linear multistep method. by $\frac{1}{2}$ to the simulation of $\frac{1}{2}$ in the simulation model is the two in Sintance intervals in accordance with the mathematical model. The $\frac{1}{2}$ 103 in accordance with the mathematical model is the sim accord is on the
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$$
y_{n+6} - \frac{360}{147} y_{n+5} + \frac{450}{147} y_{n+4} - \frac{400}{147} y_{n+3} + \frac{225}{147} y_{n+2} - \frac{72}{147} y_{n+1} + \frac{10}{147} y_n = \frac{60}{147} h f(t_{n+6}, y_{n+6}).
$$
\n(13)

After linearization, the results are analyzed by a sparse matrix solver. The minimum step size is 0.1 ns and the minimum

Table 1. Parameters considered for simulation of NFI.

Components	Parameter	Unit		
PZT part	PZT force= 3500; 1000	[N]		
	Piezo-stack mass=50	lgl		
Plunger part	Spring stiffness = 100000	[N/m]		
	Plunger mass=20	[g]		
Plunger cavity	Diameter = $10 - 20$	[mm]		
	Plunger stroke = $0.05 - 2.0$	mm		
	Dead volume $= 0.5$	\lceil mm ³ \rceil		
Nozzle part	Drug volume = $5 - 20$	\lceil mm ³ \rceil		
	Nozzle length $= 0.01 -0.5$	mm		
	Nozzle diameter = $0.01 - 0.3$	[mm]		
		Pressure buildup Piezo-stack force generation & injection formation		
	RigidSupport			
VoltageSignal	PlungerCavity ing Damper			
		M. A. Trimzi et al. / Journal of Mechanical Science and Technology 33 (8) (2019) 3851~3858 Table 1. Parameters considered for simulation of NFI.		

Fig. 5. Simulation model for proposed impulse needle free injector.

output size is 0.1 μs. The default value of damping coefficient is used for the fluid considered as drug, which is built-in fluid HLP46 in SimulationX. The fluid properties like bulk modulus and density are defined and temperature is set to be 25 °C

The purpose of simulation is to observe the effect of various parameters like PZT force, nozzle length, and nozzle diameter, on the injection dynamics. The flow rate across the nozzle *Qout* is calculated by Eq. (14). The meter-in pressure drop inside nozzle is also considered, whereas the value of constant *K* depends on the flow rate. **Example 12.** Internal due to impulse
 Example 12. The default value of damping coefficient

alation model for proposed impulse needle free injector.

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The purpose of simulation is to observe the effect

$$
Q_{out} = \frac{2.D_{N}.A_{N}}{C_{f}.L_{N}.v.\rho} \cdot \frac{1}{1+K} . P_{ab} . \qquad (14)
$$

Similarly, mass flow rate (*m dot* in *grams per second*) is resulted by product of density and volume flow as shown in Eq.

$$
mdot = \rho \cdot Q_{\text{out}}.\tag{15}
$$

3. Results and discussion

3.1 Influence of design parameters on injection kinetics

The simulation results are obtained by gradual variation of

Fig. 6. Effect of force variation on pressure drop across nozzle, injection volume, and mass flow rate.

the force from 1000 N to 3500 N, diameter of nozzle from 0.01 mm to 0.3 mm, and length of nozzle from 0.05 mm to 0.5 mm. The obtained results are then analyzed and conclusions are derived from results. The final simulation delivers the optimum parameters for fabrication of impulse type needle free injector to deliver 10 μl injection volume per shot.

3.1.1 Influence of FPZT on injection dynamics

The first case is the consideration of variation in piezostack force applied in the form of impulse to the syringe plunger. The applied voltage controls the expansion of multilayered piezostack precisely; therefore, the input force over the syringe plunger is electrically controlled by applied voltage [32]. Graphs are plotted (Fig. 6) to witness the effect of variation in PZT force on pressure built-up in drug chamber, injection volume per unit time out of nozzle, and mass of drug injected out of nozzle per unit time. The gradual increase in applied impulse force results in increased pressure difference across the nozzle causing increase in injection volume flow and mass flow and vice versa.

The piezostack force is varied from 1000 N to 3500 N with a difference of 500 N without reaching maximum blocking force limit of piezostack actuator. The gradual decrease in instantaneous impulse force results in considerable reduction in pressure across the nozzle, volume flow rate, and mass flow rate out of nozzle (Fig. 6). The force applied by piezostack, accelerates the syringe plunger, which controls the injection dynamics.

3.1.2 Effect of nozzle diameter (DN) on injection dynamics

Effect of variation in nozzle diameter on pressure drop across nozzle, volumetric flow rate, and mass flow rate out of nozzle is plotted (Fig. 7). The nozzle diameter is varied by keeping the nozzle length and other parameters constant. The diameter of nozzle is a fundamental parameter to be considered for successful design of needle free injector. Reduction in diameter of nozzle enhances pressure buildup in plunger cavity, whereas decreases the drug volume injected out of nozzle. The reason for considering 0.01 mm to 0.3 mm diameter of nozzle is to keep the size of nozzle practically fabricate-able

Fig. 7. Influence of nozzle diameter variation on pressure drop across nozzle, injection volume, and mass flow rate.

Fig. 8. Effect of nozzle length variation on pressure drop across nozzle, injection volume, and mass flow rate.

for realization of needle-free injector.

The nozzle diameter is a very significant parameter for needle-free injectors. The minor variation in diameter of nozzle can result is undesired drug volume delivery, which should be avoided. For this reason, nine different nozzle diameters were considered, ranging from 0.01 mm to 0.30 mm, to observe the effect of nozzle diameter on pressure drop across the nozzle (Fig. 7).

The length of nozzle (0.01 mm) and input force (3500 N) were kept constant during simulation. The results indicate that a gradual increase in nozzle diameter increases the drug volume injected out of the nozzle. Therefore, reduction in pressure buildup across a nozzle results in weak jet propagation, which finally results in splash back with zero skin penetration capability.

3.1.3 Effect of nozzle length (LN) on injection dynamics

Influence of nozzle length variation on pressure built-up in drug chamber, volume flow rate out of nozzle, and mass flow rate of drug injected out of nozzle was obtained through simulation. Fig. 8 shows the simulation results for six nozzle lengths from 0.50 mm to 0.05 mm, respectively.

Fig. 8 helps one to observe the effect of nozzle length variation on volume and mass flow rate, out of nozzle. Pressure drop across a nozzle increases with increase in nozzle length

Table 2. Optimum specifications for needle free injector design.

Parameters	Value
Nozzle diameter	$100 \mu m$
Nozzle length	$100 \mu m$
Piezostack blocking force	3500 N
Plunger cavity diameter	15.6 mm
Plunger stroke	$55 \mu m$
Dead volume	5 mm ³

Fig. 9. Simulation results for optimized 10 μl delivery NFI.

as the friction across the walls of nozzle is increased. The opposite phenomenon happens by increasing the nozzle diameter. The nozzle length and nozzle diameter are inversely related to each other. During simulation, nozzle diameter (0.30 mm), applied force (3500 N) and other parameters were kept constant. The trend of inverse dependency of injection volume on nozzle length is very minor because the value of nozzle diameter was kept bigger $(D_N: 0.30 \text{ mm})$ to keep the simulated nozzle geometry practically possible for fabrication.

3.2 Optimum parameters for NFI design

Multiple simulations were carried out by changing various parameters to observe their influence on injection dynamics. In the end, some parameters were selected from literature, whereas others were selected by hit and trial method. Table 2 represents the optimum parameters for design of piezoelectric impulse driven needle-free injector for delivery of 10 μl injection volume per shot. As the piezoelectric actuators generate L_{PZT} very short displacements in terms of tens of micrometers over L_{SPR} application of 150 V, the small volume delivery in terms of F_{PZT} microliters is possible at elevated pressure or 120 bar and D_{PL} more, which ensures the penetration of fine liquid jet into skin.

The simulation result in Fig. 9 represents the volume and \dot{x}_{p} pressure built-up profile with respect to applied piezoelectric m_{PL} force. The piezoelectric actuator's blocking force and stroke \ddot{x}_{PL} length are taken from commercial PIEZOMECHANIK catalogue [38]. The other parameters are obtained through simulation to get 10 μl injection volume. The instantaneous pressure β
build-un of 182.58 bar is generated due to instantaneous mebuild-up of 182.58 bar is generated due to instantaneous mechanical impulse transfer by piezostack actuation. From pres-

sure build-up to pressure drop, 10 μl of fluid volume is jetted across the nozzle. This whole phenomenon takes place in less than 20 milliseconds. The process can be repeated to get multiple shots in very short time, as multilayer piezoelectric actuators offer high frequencies up to 20 kHz.

4. Conclusions

The impulse mechanism for needle-free drug delivery using piezostack actuated jet injector is proposed. A numerical analysis for modeling of needle free injector was carried out. Simulations were performed to observe the effect of applied force and nozzle geometry on the built-up pressure, injection mass and volume flow through nozzle. Following conclusions were obtained:

- The expansion of the piezo-stack is a function of applied voltage. Thus, the injection volume can be electronically controlled by controlling the applied voltage. The voltage applied to the piezo-stack directly affects the phenomenon of jet formation from a nozzle.

- The nozzle length and diameter are inversely related. The fabrication of nozzles with less than 100 μm is practically challenging, whereas nozzles with diameters exceeding 100 μm result in splash back or no penetration of jet into skin due to low pressure jetting. The optimum size for nozzle diameter (100 μm) and nozzle length (100 μm) is obtained through simulation.

- Finally, simulation for 10 μl jet injector design was conducted and the crucial parameters for fabrication of jet injector were evaluated. The plunger cavity diameter was optimized to be 15.6 mm due to limited (55 μm) stroke of piezostack actuators.

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Nomenclature-

- *L* Piezostack expansion
- *LSPR* : Compression in spring
- *Force applied by piezo-stack*
- **PLUA**: Diameter of plunger
- $x = f(V)$: Displacement of Pzt stack
- **PLO** *z* Velocity of plunger
- *mPL* : Mass of plunger
- *PL* &&*x* : Acceleration of plunger
- V_f : Plunger cavity
- *ρ* : Density of HLP46 fluid
- *β* : Bulk modulus of HLP46 fluid
- *DN* : Diameter of nozzle
- v_f : Velocity of fluid passing through nozzle
- *Qout* : Drug volume displaced out of nozzle
- *mdot* : Mass flow out of nozzle
- *dP/dt* : Change in pressure with time
- *Pab* : Pressure drop across nozzle
- *C^f* : Friction coefficient
- *A^N* : Cross-section area of nozzle
- *L^N* : Length of nozzle
- v : Kinematic viscosity

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